

Zermelo 1908 (Zermelo set theory)

Sets

Extensionality (sets), Elementary sets, Union, Power set, Infinity, Separation, Choice

Fraenkel 1922,

Skolem 1922

Stated: *Replacement*

Elementary sets
Separation, Choice

Function existence axioms
Limitation of size

Limitation of size
Replacement
Neumann choice

Function existence axioms
Pairing, Class existence axioms
Separation, Regularity

Separation
Neumann choice
global choice

Legend:

Approach
Primitives
Axioms



Von Neumann 1925, 1928

Functions, Arguments

Extensionality (functions), Function existence axioms, Union, Power set, Infinity, Limitation of size

Stated but not adopted: *Regularity*

Von Neumann 1929

Functions, Arguments

Extensionality (functions), Function existence axioms, Union, Power set, Infinity, Replacement, Neumann choice

Proved relatively consistent: *Regularity*

Bernays 1931 [letter to Gödel],

1937, 1941 [axioms published]

Classes, Sets (two sorts)

Extensionality (classes), Pairing, Class existence axioms, Union, Power set, Infinity, Separation, Replacement, Neumann choice, Regularity

Gödel 1940 (NBG)

Classes, Sets (one sort)

Extensionality (classes), Pairing, Class existence axioms, Union, Power set, Infinity, Replacement, Global choice, Regularity