

# Estimating the optimal threshold for a diagnostic biomarker in case of complex biomarker distributions

Fabien Subtil – Muriel Rabilloud

## Additional file 2

Part 1 - Complementary simulations or results relative to section “Heterogeneity in the variance of biomarker measurements”

**Relative bias of the optimal threshold assuming a Gaussian or a Student-*t* distribution with the coverage probability and the mean width of the 95% credible interval (unequal number of subjects in diseased and non-diseased groups, Design 1)**

$N_0$	$N_1$	$\sigma_0$	$\sigma_1$	Relative bias *				Coverage probability †				CI mean width †			
				Mode		Median		Mean		Quantile		HPD		Quantile	
				Gauss	<i>t</i>	Gauss	<i>t</i>	Gauss	<i>t</i>	Gauss	<i>t</i>	Gauss	<i>t</i>	Gauss	<i>t</i>
100	50	0.07	0.07	-0.00115	-0.00343	-0.00115	-0.00378	-0.00115	-0.00363	0.948	0.948	0.947	0.948	0.017	0.019
100	50	0.05	0.05	-0.00091	-0.00333	-0.00094	-0.00366	-0.00092	-0.00352	0.947	0.948	0.942	0.945	0.017	0.019
100	50	0.03	0.03	-0.00046	-0.00196	-0.00031	-0.00194	-0.00035	-0.00196	0.947	0.949	0.942	0.946	0.013	0.014
100	75	0.07	0.07	-0.00058	-0.00120	-0.00071	-0.00134	-0.00068	-0.00131	0.953	0.954	0.952	0.953	0.024	0.023
100	75	0.05	0.05	-0.00059	-0.00132	-0.00050	-0.00145	-0.00051	-0.00140	0.949	0.954	0.945	0.952	0.015	0.016
100	75	0.03	0.03	-0.00010	-0.00070	-0.00007	-0.00068	-0.00008	-0.00068	0.954	0.960	0.950	0.955	0.011	0.012

True marker distribution in the  $N_0$  non-diseased subjects: Gaussian distribution (mean = -0.3, standard deviation =  $\sigma_0$ )

True marker distribution in the  $N_1$  diseased subjects: Gaussian distribution (mean = -0.25, standard deviation =  $\sigma_1$ )

\* Relative bias of the mode, the median, and the mean estimates of the optimal threshold.

† Coverage probability and credible interval (CI) mean width found with the quantile and the Highest Posterior Density (HPD) region method.

Gauss: Gaussian distribution – *t*: Student-*t* distribution.

**Relative bias of the optimal threshold using the empirical, boxcox, and kernel methods, with the coverage probability and the mean width of the 95% credible interval (Design 1)**

$N_0$	$N_1$	Relative bias *				Coverage probability †			CI mean width †			
		$\sigma_0$	$\sigma_1$	Empirical	Boxcox	Kernel	Empirical	Boxcox	Kernel ‡	Empirical	Boxcox	Kernel ‡
100	50	0.07	0.07	-0.0024	-0.0005	0.0003	0.964	0.947	-	0.059	0.023	-
100	50	0.05	0.05	-0.0023	-0.0002	-0.0000	0.958	0.947	-	0.038	0.016	-
100	50	0.03	0.03	-0.0039	-0.0006	-0.0003	0.909	0.946	-	0.022	0.010	-
100	75	0.07	0.07	-0.0034	-0.0013	0.0003	0.959	0.954	-	0.073	0.032	-
100	75	0.05	0.05	-0.0034	0.0002	0.0004	0.944	0.941	-	0.046	0.022	-
100	75	0.03	0.03	-0.0076	-0.0002	-0.0001	0.829	0.936	-	0.026	0.015	-

True marker distribution in the  $N_0$  non-diseased subjects: Gaussian distribution (mean = -0.3, standard deviation =  $\sigma_0$ )

True marker distribution in the  $N_1$  diseased subjects: Gaussian distribution (mean = -0.25, standard deviation =  $\sigma_1$ )

\* Relative bias of the mode, the median, and the mean estimates of the optimal threshold.

† Coverage probability and credible interval (CI) mean width found with the quantile and the Highest Posterior Density (HPD) region method.

**Relative bias of the optimal threshold using the empirical, boxcox, and kernel methods, with the coverage probability and the mean width of the 95% credible interval (Design 2)**

$\nu$	Relative bias <sup>*</sup>			Coverage probability <sup>†</sup>			CI mean width <sup>†</sup>		
	Empirical	Boxcox	Kernel	Empirical	Boxcox	Kernel <sup>‡</sup>	Empirical	Boxcox	Kernel <sup>‡</sup>
1	0.0035	- <sup>§</sup>	0.0302	0.965	- <sup>§</sup>	-	0.052	- <sup>§</sup>	-
4	-0.0009	0.0281	0.0055	0.972	0.888	-	0.050	0.029	-
8	-0.0016	0.0073	0.0022	0.970	0.935	-	0.050	0.023	-
12	-0.0025	0.0034	0.0009	0.971	0.947	-	0.050	0.022	-

True marker distribution in the non-diseased group: Gaussian distribution (mean = -0.3, standard deviation = 0.05)

True marker distribution in the diseased group: Student-*t* distribution (mean = -0.25, standard deviation = 0.05,  $\nu$  degrees of freedom)

<sup>\*</sup> Relative bias of the optimal threshold estimate.

<sup>†</sup> Coverage probability and credible interval (CI) mean width.

<sup>‡</sup> Not estimated since time consuming.

<sup>§</sup> Not assessed due to the difficulty to estimate the boxcox transformation parameter for this example.

**Relative bias of the optimal threshold using the empirical, boxcox, and kernel methods, with the coverage probability and the mean width of the 95% credible interval (Design 3)**

$\sigma_2$	$p$	Relative bias <sup>*</sup>			Coverage probability <sup>†</sup>			CI mean width <sup>†</sup>		
		Empirical	Boxcox	Kernel	Empirical	Boxcox	Kernel <sup>‡</sup>	Empirical	Boxcox	Kernel <sup>‡</sup>
0.10	0.3	-0.0029	0.0165	0.0059	0.971	0.930	-	0.054	0.028	-
0.10	0.2	-0.0037	0.0106	0.0026	0.970	0.940	-	0.053	0.026	-
0.10	0.1	-0.0016	0.0048	0.0014	0.971	0.942	-	0.052	0.023	-
0.075	0.3	-0.0030	-0.0006	0.0025	0.970	0.946	0.850	0.054	0.024	0.031
0.075	0.2	-0.0020	-0.0004	0.0019	0.970	0.946	0.849	0.052	0.022	0.029
0.075	0.1	-0.0005	-0.0003	0.0018	0.967	0.947	0.842	0.051	0.021	0.028

True marker distribution in the non-diseased group: Gaussian distribution (mean = -0.3, standard deviation = 0.05)

True marker distribution in the diseased group: mixture of two Gaussian distributions  $(p \times N(-0.25, \sigma_2^2) + (1-p) \times N(-0.25, 0.05^2))$

<sup>\*</sup> Relative bias of the optimal threshold estimate.

<sup>†</sup> Coverage probability and credible interval (CI) mean width.

<sup>‡</sup> Not estimated since time consuming.

**Part 2 - Complementary simulations or results relative to section “Heterogeneity in the mean and the variance of biomarker measurements”**

**Relative bias of the optimal threshold using the empirical, boxcox, and kernel methods, with the coverage probability and the mean width of the 95% credible interval (Design 4)**

N	$\sigma_1$	$\sigma_2$	Relative bias <sup>*</sup>			Coverage probability <sup>†</sup>			CI mean width <sup>‡</sup>		
			Empirical	Boxcox	Kernel	Empirical	Boxcox	Kernel <sup>‡</sup>	Empirical	Boxcox	Kernel <sup>‡</sup>
200	0.07	0.07	-0.0071	-0.0728	0.0662	0.971	0.290	-	0.092	0.025	-
200	0.08	0.05	0.0394	0.0467	0.1493	0.983	0.630	-	0.111	0.025	-
200	0.10	0.05	0.0289	0.0432	0.1397	0.984	0.685	-	0.103	0.025	-
100	0.07	0.07	-0.0133	-0.0741	0.0768	0.963	0.597	-	0.106	0.035	-
100	0.08	0.05	0.0398	0.0465	0.1658	0.982	0.857	-	0.122	0.035	-
100	0.10	0.05	0.0294	0.0413	0.1554	0.985	0.886	-	0.115	0.035	-
50	0.07	0.07	-0.0312	-0.0750	0.0879	0.937	0.777	-	0.116	0.049	-
50	0.08	0.05	0.0343	0.0451	0.1803	0.980	0.945	-	0.128	0.049	-
50	0.10	0.05	0.0268	0.0400	0.1723	0.980	0.960	-	0.123	0.049	-
30	0.07	0.07	-0.0490	-0.0743	0.0968	0.909	0.864	-	0.122	0.064	-
30	0.08	0.05	0.0224	0.0424	0.1905	0.972	0.970	-	0.127	0.063	-
30	0.10	0.05	0.0194	0.0384	0.1807	0.969	0.974	-	0.126	0.063	-

True marker distribution in the non-diseased group: Gaussian distribution (mean = -0.3, standard deviation = 0.07)

True marker distribution in the diseased group: mixture of two Gaussian distributions  $(0.5 \times N(0.05, \sigma_1^2) + 0.5 \times N(-0.25, \sigma_2^2))$

<sup>\*</sup> Relative bias of the optimal threshold estimate. <sup>†</sup> Coverage probability and credible interval (CI) mean width. <sup>‡</sup> Not estimated since time consuming.  
N: number of subjects in each group.