



CMS-B2G-21-002



CERN-EP-2021-253

2021/12/30

Search for resonances decaying to three W bosons in the hadronic final state in proton-proton collisions at $\bar{s} = 13 \text{ TeV}$

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Abstract

A search for Kaluza–Klein excited vector boson resonances, W_{KK} , decaying in cascade to three W bosons via a scalar radion R, $W_{KK} \rightarrow WR \rightarrow WWW$, with two or three massive jets is presented. The search is performed with proton-proton collision data recorded at $\bar{s} = 13 \text{ TeV}$, collected by the CMS experiment at the CERN LHC, during 2016–2018, corresponding to an integrated luminosity of 138 fb^{-1} . Two final states are simultaneously probed, one where the two W bosons produced by the R decay are reconstructed as separate, large-radius, massive jets, and one where they are merged in a single large-radius jet. The data observed are in agreement with the standard model expectations. Limits are set on the product of the W_{KK} resonance cross section and branching fraction to three W bosons in an extended warped extra-dimensional model and are the first of their kind at the LHC.

Submitted to Physical Review D

1 Introduction

The search for physics beyond the standard model (SM) is one of the most important elements of the research program at the CERN LHC. Direct searches performed at the LHC have not yet found any compelling evidence for such new physics. However, novel ideas and recently developed techniques expand the potential for discovery. For example, in the CMS Collaboration, deep machine learning techniques for tagging Lorentz-boosted resonances decaying hadronically [1] have been developed and exploited extensively for both searches beyond the SM and measurements of the properties of the Higgs boson (H) [2]. New physics scenarios involving yet-unprobed signatures of resonant triboson final states through a two-step cascade decay of heavy resonances in extended warped extra-dimensional models [3–8] have recently been proposed. These models provide an attractive extension of the SM, which addresses the Planck-electroweak scale difference and flavor hierarchy problems simultaneously. The theory model probed assumes a Randall–Sundrum scenario with an extended bulk consisting of two extra branes other than the one on which the SM resides [3]. Only the electroweak gauge fields can propagate into the extended bulk. The size of the extra dimension is stabilized with a mechanism introducing a potential with a modulus field [9], resulting in a bulk scalar boson, the radion, for each additional brane. Such extended models can also incorporate heavy resonances that have enhanced decays into triboson final states as compared with direct decays into dibosons and top quark-antiquark pairs. Thus, a set of new final states emerges with a discovery potential within LHC reach.

In this paper, we report on a search for massive resonances decaying in a cascade into three W bosons, through $W_{\text{KK}} \rightarrow WR$ and $R \rightarrow WW$, where W_{KK} is a Kaluza–Klein (KK) massive excited gauge boson and R is a scalar radion. The analysis is based on proton-proton (pp) collision data at $\sqrt{s} = 13$ TeV collected by the CMS experiment at the LHC during 2016–2018, corresponding to an integrated luminosity of 138 fb^{-1} . Since the W_{KK} excitation has a mass of the order of several TeV, the W bosons typically have transverse momenta (p_T) of several hundred GeV.

In general, the W boson not originating from the radion decay is highly boosted and its decay products are contained in a single large-radius jet. However, depending on the relative masses of the W_{KK} and R resonances, the two W bosons from the R decay can either produce two large-radius jets (“resolved” case), or one single large-radius jet containing both W bosons (“merged” case). These two possibilities are illustrated in Fig. 1; the merged case is predominant in the case when $m_R \ll 0.2 m_{W_{\text{KK}}}$, where m_R and $m_{W_{\text{KK}}}$ are the masses of the R and W_{KK} bosons, respectively. As a result, the final states considered here require two or three massive jets and no isolated charged leptons. However, nonisolated leptons are allowed to be present inside the jets formed by merged radion decay products $R \rightarrow WW \rightarrow qq$. It is also possible to have additional jets in the “compressed mass” scenario, $m_R \gtrsim 0.8 m_{W_{\text{KK}}}$ (depending on the specific value of $m_{W_{\text{KK}}}$), which can feature at least one W boson with a low boost, whose decay is resolved as two individual small-radius jets. Such events are not explicitly targeted by this analysis as their production rate is much smaller than the ones of the standard scenarios described above. This is the first search of this kind in the all-hadronic final state.

In both cases, merged and resolved, dedicated techniques are applied to exploit the substructure of the W boson jets. For the merged case, apart from the case in which a nonisolated charged lepton overlaps with the hadronically decayed W boson, it is also possible that the decay products of a quark from the fully hadronic decay $R \rightarrow WW \rightarrow qqqq$ are not clustered into the same jet. Events identified as hadronically decaying W bosons can also include cases where the decay $W \rightarrow \ell\nu$ is followed by a hadronic decay of the tau lepton. These effects lead

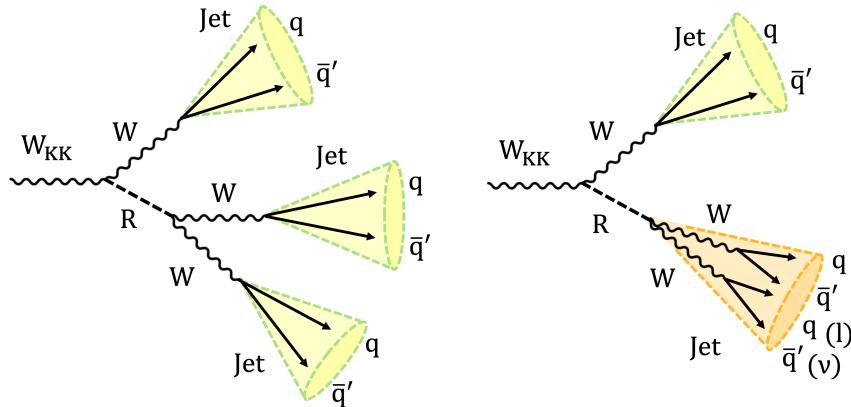


Figure 1: Schematic diagrams of the decay of a KK excitation of a W boson (W_{KK}) to the final states considered in this analysis. Left: three individually reconstructed W bosons; right: one individually reconstructed W boson and two W bosons reconstructed as a single large-radius jet, which is predominant for $m_R = 0.2m_{W_{KK}}$.

to a complicated jet mass spectrum from the merged radion that requires the design of a hybrid discriminant (“tagger”). Events with a single isolated charged lepton in the final state are considered in a similar, separate analysis with orthogonal event selection, described in Ref. [10].

While the search is by design optimized for a WWW signal, it is also partly sensitive to signals with similar decay topologies. In particular, heavy resonances decaying into WW , WZ , ZZ , WWZ , WZZ , ZZZ , Wt , Zt , WH , ZH , WX , or ZX , where X denotes an unknown particle with mass above 70 GeV whose decay products can be identified using jet substructure techniques, can be detected through this search.

This paper is organized as follows: Section 2 provides a description of the CMS detector. Section 3 describes the data sets and simulation samples used in the analysis. The triggers used for data collection and the event reconstruction are discussed in Section 4. The massive jet tagging is described in Section 5. The event selection and event categorization are presented in Section 6. The jet tagger calibration is described in Section 7. Section 8 describes the estimation of the SM background. Systematic uncertainties are discussed in Section 9. The results and their interpretation are given in Section 10. A summary is presented in Section 11. Tabulated results are provided in the HEPData record for this analysis [11].

2 The CMS detector

The central feature of the CMS detector is a superconducting solenoid of 6 m internal diameter, providing a magnetic field of 3.8 T. A silicon pixel and strip tracker, a lead tungstate crystal electromagnetic calorimeter (ECAL), and a brass and scintillator hadron calorimeter (HCAL), each composed of a barrel and two endcap sections resides within the solenoid volume. Forward calorimeters extend the coverage provided by the barrel and endcap detectors up to pseudo-rapidities of 5. Muons are measured in gas-ionization detectors embedded in the steel flux-return yoke outside the solenoid.

Events of interest are selected using a two-tiered trigger system. The first level, composed of custom hardware processors, uses information from the calorimeters and muon detectors to select events at a rate of around 100 kHz within a fixed latency of about 4 μ s [12]. The second level, known as the high-level trigger (HLT), consists of a farm of processors running a version of the full event reconstruction software optimized for fast processing, and reduces the event

rate to around 1 kHz before data storage [13]. A more detailed description of the CMS detector, together with a definition of the coordinate system and kinematic variables, can be found in Ref. [14].

3 Data samples and event simulation

The data samples analyzed in this search correspond to a total integrated luminosity of 138 fb^{-1} . They were recorded in pp collisions at $\sqrt{s} = 13 \text{ TeV}$ in the years 2016, 2017, and 2018, comprising 36.3, 41.5, and 59.7 fb^{-1} , respectively [15–17].

The signal is simulated at leading order (LO) using the MADGRAPH5_aMC@NLO 2.4.2 generator [18], covering a wide range of W_{KK} and R masses ($m_{W_{\text{KK}}}$ from 1.5 to 5.0 TeV, and m_R from 6 up to 90% of $m_{W_{\text{KK}}}$), together with the parameters recommended by the authors of Refs. [3–6], i.e., a KK coupling to the radion and a W boson $g_{\text{grav}} = 6$, KK gauge couplings $g_{W_{\text{KK}}} = 3$ and $g_{Z_{\text{KK}}} = 6.708$, and a confinement parameter $\Lambda = 0.5$. The branching fraction for the decay $W_{\text{KK}} \rightarrow W R \rightarrow WW$ can reach values above 50%.

Top quark pair and single top quark production are modeled at next-to-LO (NLO) using the POWHEG 2.0 generator [19–24]. Events composed uniquely of jets produced through the strong interaction are referred to as quantum chromodynamics (QCD) multijet events. These processes, along with background from $W+\text{jets}$ and $Z+\text{jets}$ production, are simulated at LO with MADGRAPH5_aMC@NLO, and matched to parton showers with the MLM [25] algorithm. The other, less important backgrounds, including processes with two or three vector bosons $V = W, Z$ (diboson and triboson production, respectively) and $t\bar{t}Z/W$ production, are simulated either with MADGRAPH5_aMC@NLO or POWHEG, at NLO and LO, respectively.

All background and signal samples for the 2016 data-taking conditions are generated with the NNPDF3.0 NLO or LO parton distribution functions (PDFs) [26], with the order matching that in the matrix element calculations. In 2017 and 2018, the NNPDF3.1 next-to-next-to-LO PDFs [27] are used for all samples. Parton showering, fragmentation, and hadronization for all samples are performed using PYTHIA 8.230 [28] with the underlying event tune CUETP8M1 [29] for the 2016 analysis, and CP5 [30] for the 2017 and 2018 analyses. The CMS detector response is modeled using the GEANT4 package [31, 32]. A tag-and-probe procedure [33] is used to derive corrections for data-to-simulation differences in reconstruction and selection efficiencies. The simulated events include additional pp interactions in the same and neighboring bunch crossings, referred to as pileup (PU). The simulated events are weighted so the PU vertex distribution matches the one from the data.

4 Event reconstruction

The candidate vertex with the largest value of summed physics-object p_T^2 is taken to be the primary pp interaction vertex. The physics objects used for this determination are the jets, clustered using the anti- k_T jet finding algorithm [34, 35] with the tracks assigned to candidate vertices as inputs, and the associated missing transverse momentum (p_T^{miss}), taken as the negative vector sum of the p_T of those jets.

A particle-flow (PF) algorithm [36] aims to reconstruct and identify each individual particle in an event, with an optimized combination of information from the various elements of the CMS detector. The energy of electrons is determined from a combination of the track momentum at the primary interaction vertex, the corresponding ECAL cluster energy, and the energy sum of all bremsstrahlung photons attached to the track. The energy of muons is obtained from the

curvature of the corresponding track. The energy of charged hadrons is determined from a combination of their momentum measured in the tracker and the matching ECAL and HCAL energy deposits, corrected for the response function of the calorimeters to hadronic showers. Finally, the energy of neutral hadrons is obtained from the corresponding corrected ECAL and HCAL energies.

For each event, hadronic jets are clustered from these reconstructed particles using the infrared and collinear safe anti- k_T algorithm [34, 35]. The clustering algorithm is run twice over the same inputs, once with a distance parameter of 0.4 (AK4 jets) and once with 0.8 (AK8 jets). Jet momentum is determined as the vectorial sum of all particle momenta in the jet, and is found from simulation to be, on average, within 5 to 10% of the true momentum over the entire p_T spectrum and detector acceptance. Pileup interactions can contribute additional tracks and calorimetric energy depositions to the jet momentum.

The pileup per particle identification algorithm (PUPPI) [37, 38] is used to mitigate the effect of PU at the reconstructed particle level. Using this algorithm, the momenta of charged and neutral particles are rescaled. Jet energy corrections are derived from simulation to bring the measured response of jets to that of particle-level jets on average. In situ measurements of the momentum balance in dijet, photon+jet, Z+jet, and multijet events are used to account for any residual differences in the jet energy scale between data and simulation [39]. The jet energy resolution amounts typically to 15–20% at 30 GeV, 10% at 100 GeV, and 5% at 1 TeV [39]. Additional selection criteria are applied to each jet to remove jets potentially dominated by anomalous contributions from various subdetector components or reconstruction failures [40].

Jets originating from the hadronization of b quarks are identified using a deep neural network algorithm (DEEPCSV) that takes as input: tracks displaced from the primary interaction vertex, identified secondary vertices, jet kinematic variables, and information related to the presence of soft leptons in the jet [41]. Working points (WPs) are used that yield either a 1% (medium WP) or a 10% (loose WP) probability of misidentifying a light flavor quark or a gluon (udsg) jet with $p_T > 30$ GeV as a b quark jet. The corresponding average efficiencies for the identification of the hadronization products of a bottom quark as a b quark jet are about 70 and 85%, respectively.

The vector p_T^{miss} is computed as the negative vector sum of the transverse momenta of all the PF candidates in an event, and its magnitude is denoted as p_T^{miss} [42]. The p_T^{miss} is modified to account for corrections to the energy scale of the reconstructed jets in the event. Anomalous high- p_T^{miss} events can be due to a variety of reconstruction failures, detector malfunctions, or noncollision backgrounds. Such events are rejected by event filters that are designed to identify more than 85–90% of the spurious high- p_T^{miss} events with a mistagging rate of less than 0.1% [42].

Hadronic decays of W/Z bosons are identified with the groomed jet mass (m_j), and a novel deep learning algorithm with the PF candidates and secondary vertices as inputs [1]. The groomed jet mass is calculated after applying a modified mass-drop algorithm [43, 44], known as the *soft-drop* algorithm [45], to AK8 jets, with parameters $\eta_{\text{cut}} = 0$, $z_{\text{cut}} = 0.1$, and $R_0 = 0.8$. The variables are calibrated in a top quark-antiquark sample enriched in hadronically decaying W bosons [46]. Further details on the calibration method used for this analysis are given in Section 7.

Muon (μ) and electron (e) candidates are reconstructed in order to veto events containing such energetic leptons. Muon candidates, within the geometrical acceptance of the muon detectors ($| \eta | < 2.4$), are reconstructed by combining the information from the silicon tracker and the muon chambers [47]. These candidates are required to satisfy a set of quality criteria based on

the number of hits measured in the silicon tracker and in the muon system, the properties of the fitted muon track, and the impact parameters of the track with respect to the primary vertex of the event. Electron candidates within $\Delta R < 2.5$ are reconstructed using an algorithm that associates fitted tracks in the silicon tracker with electromagnetic energy clusters in the ECAL [48]. To reduce the misidentification rate, these candidates are required to satisfy identification criteria based on the shower shape of the energy deposit, the matching of the electron track to the ECAL energy cluster, the relative amount of energy deposited in the HCAL detector, and the consistency of the electron track with the primary vertex. Because of nonoptimal reconstruction performance, electron candidates in the transition region between the ECAL barrel and endcaps, $1.44 < \eta < 1.57$, are discarded. Electron candidates identified as coming from photon conversions in the detector are also rejected. Identified muons and electrons are required to be isolated from hadronic activity in the event. The isolation sum is defined by summing the p_T of all the PF candidates in a cone of radius $R = \sqrt{\Delta\eta^2 + \Delta\phi^2}$ around the muon (electron) track, where $\Delta\phi$ is the azimuthal angle, and is corrected for the contribution of neutral particles from PU interactions [47, 48].

5 Massive jet tagging

The signal event signatures include two types of massive jets ($m_j > 60$ GeV) originating from the merged decay products of either W or R bosons. We consider three main cases for the merged R boson decay, designated and defined as follows:

R^{4q} , where the two daughter W bosons decay hadronically ($R \rightarrow WW \rightarrow qqqq$) with all four final-state quarks contained in the reconstructed jet

R^{3q} , similar to the former but with one quark leaking outside of the jet cone, producing a three-prong jet

R^{qq} , where one of the two daughter W bosons decays leptonically ($R \rightarrow WW \rightarrow qq$), resulting in a jet containing an energetic, charged, nonisolated lepton

All these types of R candidate jets are reconstructed as AK8 jets.

Both W and R boson candidates are tagged using the DEEPAK8 jet classification framework [1]. This modular tagging framework has been designed by the CMS Collaboration to identify hadronically decaying top quarks as well as W, Z, and Higgs bosons. The algorithm uses machine learning techniques based on PF candidates, secondary vertices, and other inputs to classify the AK8 jets into 17 categories. These categories include jets arising from $W \rightarrow qq$, $Z \rightarrow qq$, $t \rightarrow bqq$, $H \rightarrow 4q$, and gluon or light-quark decay. To remove a potential mass dependence from the classifier output, a generative adversarial neural network is used to create “mass-decorrelated” outputs. The final output is a set of 17 “raw scores” per jet, where each one gives the likelihood of the jet originating from a particular decay. Discriminants can be developed by combining sums in ratios of these raw scores to select a particular type of jet, while rejecting others.

Two particular discriminants are used for this analysis. The first, “deep-W”, aims to identify W boson candidates through the $W \rightarrow qq$ and QCD multijet raw scores, selecting and rejecting compatible jets, respectively. The second, “deep-WH”, is used to identify merged R boson candidates of types R^{qq} , R^{3q} , and R^{4q} . This is achieved by making use of the $W \rightarrow qq$ and $H \rightarrow 4q$ raw scores, which select radion-like jet types while rejecting QCD multijet candidates.

The corresponding formulae are as follows:

$$\text{deep-W} = \frac{\text{raw score W}}{\text{raw score W}} \frac{\text{qq}}{\text{raw score(QCD)}}, \quad (1)$$

used for tagging W boson candidates with mass m_j in the range 60–100 GeV, and

$$\text{deep-WH} = \frac{\text{r.s. W}}{\text{r.s. W}} \frac{\text{qq}}{\text{r.s. H}} \frac{\text{r.s. H}}{\text{4q}} \frac{\text{4q}}{\text{r.s.(QCD)}}, \quad (2)$$

where “r.s.” denotes the raw score, used for tagging radion candidates with mass $m_j > 100$ GeV.

For both taggers, the mass-decorrelated version is used to avoid distorting the mass distribution (mass sculpting) and to retain the sensitivity to radions with mass greater than those of the W and the Higgs bosons. The tagger discriminant distributions are presented in Fig. 2 (lower row) using a loose selection that will be defined in Section 6.2.

6 Event selection

6.1 Trigger

The analysis uses events that are selected by a range of different HLT paths. One set of paths requires H_T , the scalar sum of the p_T of all AK4 jets in the event, to be greater than 800, 900, or 1050 GeV, depending on the data collection year. In addition, events with $H_T > 650$ GeV and a pair of jets with invariant mass above 900 GeV and a pseudorapidity separation < 1.5 are also selected for the 2016 data set. A different set of paths selects events where the p_T of the leading AK8 jet is greater than 500 GeV, or the p_T is greater than 360 GeV and the “trimmed mass” of an AK8 jet is above 30 GeV. The jet trimmed mass is obtained after removing remnants of soft radiation with the jet trimming technique [49], using a subjet size parameter of 0.3 and a subjet-to-AK8 jet p_T fraction of 0.1. The trigger selection efficiency is measured to be greater than 99% for events with $H_T > 1.1$ TeV, using a sample of data events collected with an orthogonal single-muon trigger.

6.2 Preselection and signal region

Events are selected in two stages; the first, “preselection”, is initially applied to explore kinematic features of the signal compared to the SM background. A tighter selection, the signal region (SR) selection, is then applied to further improve the background rejection. The final analysis uses the SR events, while the preselected events are used to calibrate and validate the DEEPAK8 discriminants deep-W and deep-WH. In the following, we simply use the term “jets” to indicate massive AK8 jets if not stated differently.

The following kinematic conditions define the preselection:

- number of jets $N_j = 2$ or 3
- highest- p_T jet $p_T^{j1} > 400$ GeV, and for others $p_T^{j2,j3} > 200$ GeV
- mass of the two highest- p_T jets $m_{j1,j2} > 40$ GeV
- no isolated lepton ($N_e = 0$) with $p_T > 20$ –35 GeV and $\eta < 2.4$ –2.5 for (e)

The triboson signal is expected to show a peak in the distribution of the invariant mass of the jets, m_{jj} in dijet events and m_{jjj} in trijet events. These distributions are used for the statistical analysis. Figure 2 (upper row) shows the m_{jj} (m_{jjj}) spectra after preselection. The signal processes are scaled to 500 times their theoretical cross section.

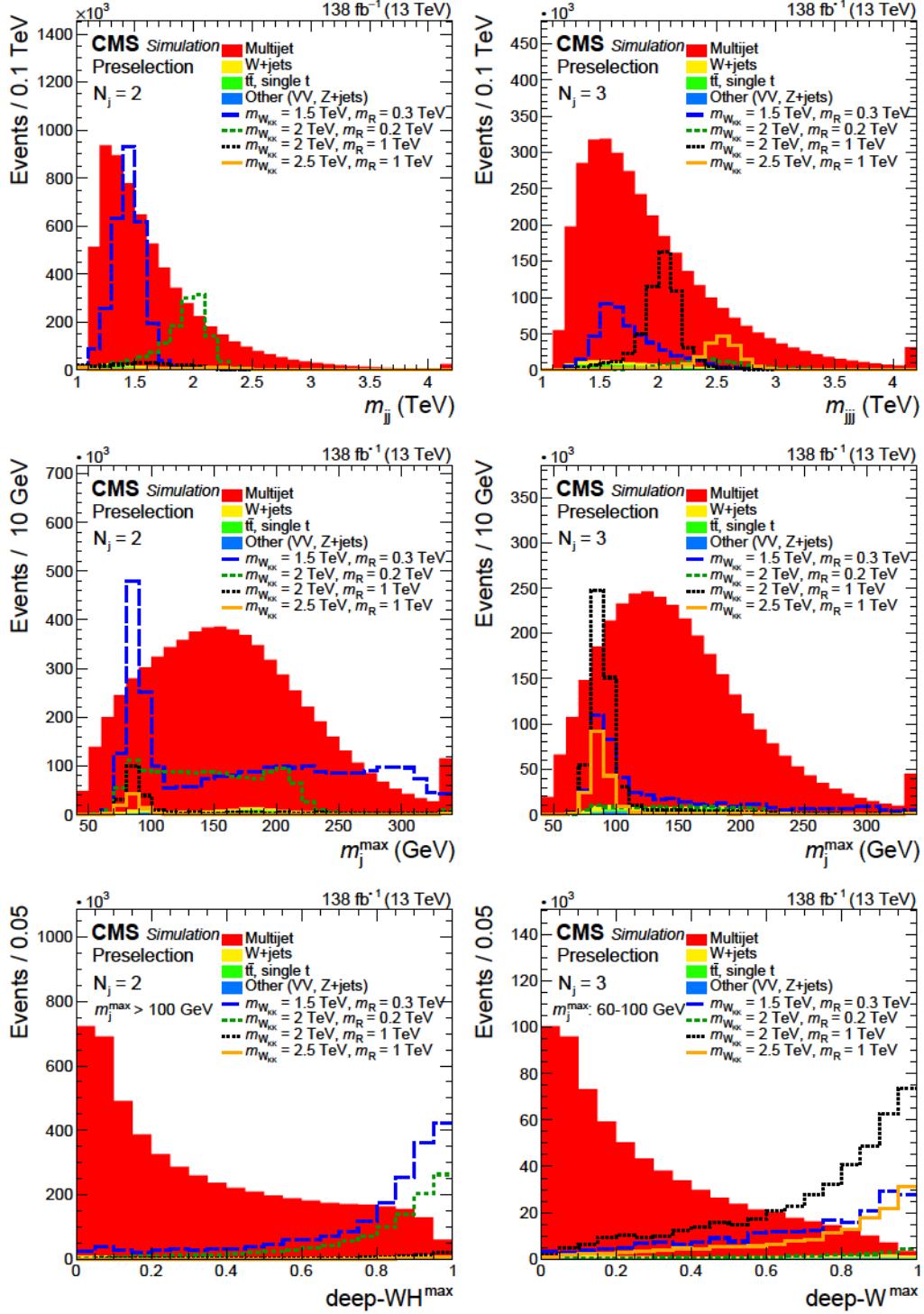


Figure 2: Variables discriminating between signal and background in simulation. Left column, upper to lower rows: the distributions of m_{jj} , m_j^{\max} , and deep-WH (for highest-mass jet with $m_j^{\max} > 100$ GeV) for preselected events with $N_j = 2$. Right column, upper to lower rows: the distributions of m_{jj} , m_j^{\max} , and deep-W (for highest-mass jet with $60 < m_j^{\max} < 100$ GeV) for preselected events with $N_j = 3$. The signal processes are scaled to 500 times their theoretical cross section for visibility.

To define the SR selection, we add the following conditions to the preselection criteria. In the case of $N_j = 2$ events, the higher and lower jet masses are designated as m_j^{\max} and m_j^{\min} , respectively. The higher-mass jet is taken to be the radion candidate, and the lower-mass jet to be the W boson candidate. Therefore, we require $m_j^{\max} > 70 \text{ GeV}$ and $70 < m_j^{\min} < 100 \text{ GeV}$. In the case of events with $N_j = 3$, m_j^{\max} and m_j^{\min} are defined as above, with m_j^{mid} designating the jet intermediate in mass. The two highest-mass jets are considered as W boson candidates, and we demand $70 < m_j^{\text{mid}}, m_j^{\max} < 100 \text{ GeV}$. The lowest-mass jet can correspond to either a merged W boson or to a quark from the W boson decay and its mass m_j^{\min} is always less than 100 GeV. Therefore, we allow at most one of the three W bosons to be resolved as a pair of low-mass jets ($m_j < 60 \text{ GeV}$), while one of these daughter jets still must have a p_T above the 200 GeV threshold. Figure 2 (middle row) shows the m_j^{\max} distributions.

Jets in the mass range 60–100 (< 100) GeV, as W boson (radion) candidates, are further selected using the deep-W(WH) discriminant, which is not required for jets with $m_j < 60 \text{ GeV}$. Figure 2 (lower row) presents the deep-W(WH) distributions for the highest-mass jets after preselection. The conditions $\text{deep-W} > 0.8$ and $\text{deep-WH} > 0.8$ are required for events with two massive jets, while the less stringent requirement of at least two massive jets with $\text{deep-W} > 0.6$ is imposed for events with three jets.

In order to select Lorentz-boosted final states, we additionally require that S_T , the scalar sum of the transverse momenta of the selected jets and the p_T^{miss} , is greater than 1.3 TeV. The p_T^{miss} in the S_T sum enhances signal separation for the cases where a hadronic lepton decay is present, or where the decay products from a merged radion decay include a nonisolated lepton, since in these cases the p_T^{miss} arises from the undetected neutrino. To suppress $t\bar{t}$ background, events are vetoed that contain a b-tagged AK4 jet not overlapping with any AK8 jet ($R > 0.8$). The DEEPCSV discriminant at the medium working point [41] is used for this veto. As the signal region explored corresponds to $m_{W_{KK}} > 1.5 \text{ TeV}$, we also impose the condition $m_{jj} > m_{jjj} > 1.1 \text{ TeV}$ to probe only the high-mass region, although this condition has minimal impact on top of the S_T and H_T constraints.

The SR selection criteria, which are applied on top of preselection, can be summarized as:

- Number of additional b-tagged jets (nonoverlapping with the AK8 jets) $N_b = 0$
(medium WP)
- Sum of p_T^{miss} and the p_T of the selected jets: $S_T > 1.3 \text{ TeV}$
- Dijet (trijet) invariant mass $m_{jj} > m_{jjj} > 1.1 \text{ TeV}$ for $N_j = 2$ (3)
- For $N_j = 2$: $m_j^{\max} > 70 \text{ GeV}$, $70 < m_j^{\min} < 100 \text{ GeV}$, with $\text{deep-W} > \text{WH} > 0.8$ for $70 < m_j < 100 \text{ GeV}$ ($m_j > 100 \text{ GeV}$)
- For $N_j = 3$: $70 < m_j^{\max}, m_j^{\text{mid}} < 100 \text{ GeV}$ and $m_j^{\min} > 100 \text{ GeV}$, with $\text{deep-W} > 0.6$ (0.8) for three (two) massive jets

6.3 Signal region definition

Six different SRs are defined in the following and are summarized in Table 1. In addition, Fig. 3 illustrates these SRs in two-dimensional (2D) and 3D diagrams of the jet mass.

The SR events with $N_j = 2$ are split into three samples based on the value of m_j^{\max} : SR1, SR2, and SR3 correspond to m_j^{\max} values of 70–100, 100–200, and > 200 GeV, respectively. This categorization serves as a binning over the unknown radion mass. As Fig. 2 (middle row) illustrates, the merged radion jet mass has a broad distribution populating the m_j^{\max} range of 70 GeV to m_R .

Table 1: Summary of the selection requirements for each of the signal regions.

Region	N_j	m_j^{\max} (GeV)	m_j^{mid} (GeV)	m_j^{\min} (GeV)	Jet tagging conditions		
SR1	2	70–100	—	70–100	Both with deep-W	0.8	
SR2	2	100–200	—	70–100	Higher with deep-WH	0.8, lower with deep-W	0.8
SR3	2	200	—	70–100	Higher with deep-WH	0.8, lower with deep-W	0.8
SR4	3	70–100	70–100	60–100	All three with deep-W	0.6	
SR5	3	70–100	70–100	60–100	Exactly two with deep-W	0.6	
SR6	3	70–100	70–100	0–60	Two highest with deep-W	0.8	

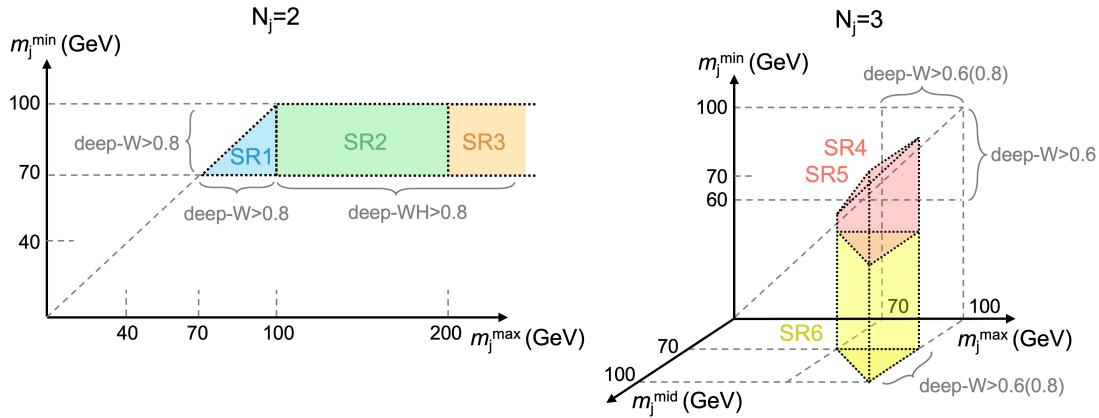


Figure 3: Schematic of the 2D jet mass regions for two-jet events (left) and 3D jet mass regions for three-jet events (right), indicating the location of the six orthogonal signal regions SR1–6, indicated by the colored areas. The SR4 and SR5 differ by the requirement of exactly three and two W-tagged jets, respectively.

Signal events in SR2 and SR3 (i.e., with $m_j^{\max} = 100$ GeV) generally contain a merged radion jet (R^{qq}, R^{3q}, R^{4q}), and the deep-WH discriminant separates these jets from the SM background.

Events in SR1 have both jets in the 70–100 GeV mass window. The merged radion jet lies in SR1 either for cases where the higher-mass jet is in the R^{qq} category and the neutrino acquires most of the parent W boson momentum, or when the higher-mass jet is a W boson jet (when the decay products of $R \rightarrow WW$ receive imbalanced Lorentz boosts and the softer W boson is not merged). Resolved radion events can lie in SR1 if the softest hadronically decaying W boson is resolved (events near the “compressed mass” scenario). In addition, SR1 is sensitive to any diboson resonant signal that might be present. Any jet of SR1–3 with a mass in the range 70–100 GeV is required to satisfy the $\text{deep-W} > 0.8$ requirement to be tagged as a W (or R^{qq}) boson candidate.

The SR events with $N_j = 3$ are split into three samples SR4–6 as follows. In case of $m_j^{\min} \geq 60$ GeV, we demand all three jets to be W-tagged satisfying the condition $\text{deep-W} > 0.6$, which defines the SR4 region; events with exactly two W-tagged jets are placed in SR5. Events with $m_j^{\min} \leq 60$ GeV and the other two massive jets satisfying $70 \leq m_j^{\text{mid}}, m_j^{\max} \leq 100$ GeV and $\text{deep-W} > 0.8$ constitute SR6. These three regions are sensitive only to the resolved radion signal, with SR4 being the most sensitive among them, as it demands three W-tagged jets.

The six different regions provide complementary sensitivity to different regions of the $m_{W_{KK}} - m_R$ plane. Signal scenarios with radion masses producing jets in the mass range 100–200 GeV are predominantly probed in SR2; for m_R in the range 200–300 GeV, the signal events predominantly lie in SR2 and SR3; while for $m_R = 300$ GeV (if the radion remains merged), SR3 provides most of the sensitivity.

7 Calibration of the DEEPAK8 tagger

The deep-W(WH) discriminants are not fully reproduced in simulation, especially at low and high scores. This section describes the calibration procedure followed to correct the deep-W(WH) spectra for each type of jet in two bins of p_T^j and m_j . The correction is quantified using scale factors (SFs), which are applied to all simulated events (signal and background).

Events in the preselected sample are dominated by QCD multijet background (99%). In SR1–6, QCD multijet events make up 50–75% of the expected background. The rest of the events are from $t\bar{t}$ and single t quark processes (10–25%), W+jets processes (10–20%), and other (e.g., WW, WZ, $t\bar{t}W/Z$, or tribosons, making up less than 15%). Therefore, massive jets ($m_j > 60$ GeV) produced by SM processes selected in the SRs comprise a mixture of:

- hadronically decaying W bosons producing merged W boson jets
- light quarks or gluons (q/g), with radiation or fragmentation, which are reconstructed as massive q/g jets
- three types of jets from hadronically decaying t quarks, $t \rightarrow bW \rightarrow bqq$:
 - jets including the b quark and only one of the quarks from the W boson decay, designated “ t^2 ”
 - jets including the b quark and both of the quarks from the W boson decay, designated “ t^3 ”
 - jets including the b quark, both of the quarks from the W boson decay, and an additional quark or gluon inside the jet cone, designated “ t^4 ”

Compared to the t^3 category, the t^4 category requires an additional q/g with $p_T > 50$ GeV inside the jet cone. These two categories are difficult to distinguish experimentally and the tagger response is similar. Thus, t^3 and t^4 jets are treated together and designated $t^{3,4}$ in the following. Jets not included in these four categories constitute less than 6 (5)% of the SR (preselection) events. In simulation, jets are placed into these categories, as well as signal categories, by matching the reconstructed jets to the generator-level partons in R . The matching criteria are summarized in Table 2. The matching is very efficient, and the number of jets not matched to any of these categories is negligible.

The calibration of the W, t^2 , and $t^{3,4}$ jets requires samples enriched in those jets. Therefore, dedicated calibration samples are defined, and the calibration for these jets is summarized in Section 7.1. The q/g jets are calibrated using preselection jets, and this procedure is described in Section 7.2. The calibration of signal jets is presented in Section 7.3.

7.1 Calibration of W boson and top quark jets with a matrix method

For the calibration of the taggers, a control sample similar to the preselected one, but enriched in W boson and top quark jets is used, which we refer to as “sideband”. The sideband is defined by requiring one isolated lepton (μ or e), $p_T^{\text{miss}} > 40$ –80 GeV for (e), and one or two massive jets. The neutrino p_z is reconstructed under the assumptions that the invariant mass of the system is equal to the W boson mass $m_W = 80$ GeV and the transverse momentum of the system is required to satisfy $p_T < 200$ GeV. This means that for the sideband one of the massive jets used for the preselection is effectively replaced by a leptonically decaying W boson candidate.

The highest-mass jets in these sideband events with $m_j > 60$ GeV are used for the calibration. These jets are categorized by the matching to the W, t^2 , $t^{3,4}$, and q/g categories described

Table 2: Matching criteria used to place a jet in one of the SM jet categories (left four columns) or merged radion jet categories (right two columns). Each column lists the R conditions demanded between the reconstructed jet (j) and the generator-level parton in order to match a jet with a particular jet substructure. Lower indexes enumerate partons and indicate the particle from whose decay they originate (e.g., $t \rightarrow b_t q_1 W q_2 W$). Schematic diagrams for each jet type are shown below each column.

q/g	W		t^2		$t^{3,4}$		$R^{3,4q}$		R_{qq}		
W, j	0.6	W, j	0.6	t, j	0.6	t, j	0.6	R, j	0.6	R, j	0.6
—	—	q_{1W}, j	0.8	b_t, j	0.8	b_t, j	0.8	q_1, j	0.8	q_1, j	0.8
—	—	q_{2W}, j	0.8	q_{1W}, j	0.8	q_{1W}, j	0.8	q_2, j	0.8	q_2, j	0.8
—	—	b_t, j	0.8	q_{2W}, j	0.8	q_{2W}, j	0.8	q_3, j	0.8	$, j$	0.8
—	—	—	—	—	For t^4 (t^3):	$q/g, j$	0.8	q_4, j	0.8	—	—

previously. We split the events into two m_j bins, one with $60 < m_j < 120\text{ GeV}$ (low mass), which contains primarily W , t^2 , and q/g ; and the other one with $m_j > 120\text{ GeV}$ (high mass) containing primarily the t^2 , $t^{3,4}$, and q/g categories. In addition, we split sideband events into two, based on the jet p_T^j . For low-mass jets, the bins used are $200\text{--}400$ and $>400\text{ GeV}$, while for high-mass jets the bins used are $200\text{--}500$ and $>500\text{ GeV}$. The resulting four categories are designated LL, LH, HL, and HH, where the first letter indicates low or high m_j and the second letter low or high p_T^j . The two SM processes ($W + \text{jets}$ and top quark production) are normalized in each of these four categories by scaling them to match the data separately for events with zero or one b -tagged jet(s). This corrects the simulation for an $\mathcal{O}(10\%)$ mismodeling of the cross section, and the residual data-to-simulation differences in the deep- W (WH) distribution can be attributed to the mismodeling of the discriminant.

Each of the LL, LH, HL, HH samples is dominated by exactly three jet types. Any other jet contribution or unmatched jets (collectively ~5%) can be ignored. For each of these jet types, we apply a set of kinematic conditions to split them further into three subsamples so that each sample is highly pure in a single jet type. Thus, for LL we form a W -pure, a t^2 -pure, and a q/g -pure subsample, and correspondingly for LH, HL, and HH. The splitting conditions include kinematic variables such as N -subjettiness [50], N_j , N_b , and m_j , as well as DEEPAK8 discriminants other than the calibrated one.

The deep- W (WH) distributions are formed for each of the three pure subsamples for LL. One equation is written for each pure subsample by equating the data yields $D_{i,k}$ for a jet type i in a deep- W (WH) bin k with the simulated jet yields for W , t^2 , and q/g (which we write as W , t , and g here), scaled by the scale factors SF_k^W , SF_k^t , and SF_k^g : $D_{i,k} = SF_k^W W_{i,k} + SF_k^t t_{i,k} + SF_k^g g_{i,k} - d_{i,k}$. The $d_{i,k}$ term accounts for the other types of jet yields; their contribution is small (amounting to ~5% for most of the bins), and these jet types are treated as not contributing to the mismodeling. A similar equation can be written for each of the three ($i = 1, 2, 3$) subsamples

W , t , and g to form a system of three equations:

$$\begin{array}{lllll} D_{1,k} & d_{1,k} & W_{1,k} & t_{1,k} & g_{1,k} \\ D_{2,k} & d_{2,k} & W_{2,k} & t_{2,k} & g_{2,k} \\ D_{3,k} & d_{3,k} & W_{3,k} & t_{3,k} & g_{3,k} \end{array} \quad \begin{array}{l} SF_k^W \\ SF_k^t \\ SF_k^g \end{array}, \quad (3)$$

in which the jet yields and the data are known, while the three SFs (SF_k^W , SF_k^t , SF_k^g) are unknown. We solve this 3×3 system per deep- W (WH) bin k to derive the SFs for each type of jet. The scale factors obtained with this matrix method SF_k^W , $SF_k^{t^2}$ and $SF_k^{t^{3,4}}$ are shown in Fig. 4 for LL, LH, HL, and HH. As the three subsamples are highly enriched in exactly one jet type, the matrix is nearly diagonal, and the derivation of the SFs is dominated by the data vs. simulation modeling in the corresponding pure subsamples. For example, the data/simulated yields in the W -pure subsample dominate the determination of SF_k^W . The method yields reliable SFs in the regime where subsamples are highly pure. Both deep- W and deep- WH are calibrated with this procedure for each of the LL, LH, HL, and HH bins separately.

All simulated events, based on the types of the selected jets they contain and their p_T^j and m_j , are corrected by the SFs for the respective deep- W (WH) bins. The discriminant distributions before and after corrections are shown in Fig. 5. Various validation tests performed showed good agreement between data and simulation. As the extracted SFs are found to depend on the choice of splitting conditions defining the pure subsamples, systematic uncertainties resulting from the selection criteria are assigned, as described in Section 9.

7.2 Calibration of quark and gluon jets

The quark and gluon jets are treated collectively as a single type of jet, q/g . Their calibration is performed using the preselected sample where SR events and events with b-tagged AK4 jets are vetoed. This sample consists of more than 13 million events, of which more than 97% are QCD multijet events. Similarly to the single-lepton sideband sample, we consider only the highest-mass jet with $m_j > 60$ GeV in each event, and define the same four LL, LH, HL, and HH bins in m_j and p_T^j . The QCD events in each bin are normalized to the data. The contribution from W , t^2 , and $t^{3,4}$ jets, amounting to less than 2%, is estimated using simulation and subtracted from the data. The result is divided by the q/g yields to define $SF_k^{q/g}$ in each deep- W (WH) discriminant value bin k . The resulting values of $SF_k^{q/g}$ are presented together with SF_k^W , $SF_k^{t^2}$, and $SF_k^{t^{3,4}}$ in Fig. 4. The relative fraction of quarks and gluons is the same for the preselection region where the SFs are defined, and the SRs and control regions (CRs). The only difference between the jets are therefore their p_T spectra.

Validation tests have shown a good post-correction performance, where the ratio of data to simulation is consistent with unity over the entire deep- W (WH) range. To perform these tests, we define CRs by using the SR1–6 selections with at least one of the deep- W (WH) conditions inverted. For SR4 and SR5, this inversion leads to the same sample with zero or one W -tagged jet. The five resulting CRs, associated with the SRs, are named CR1, CR2, CR3, CR45, and CR6. Figure 6 shows the deep- W (WH) distributions for the highest-mass jet in each CR after the SFs are applied. A similar, almost flat performance is exhibited by the middle and minimum mass jets. Validation tests in samples using other CR definitions lead to similar post-correction performance.

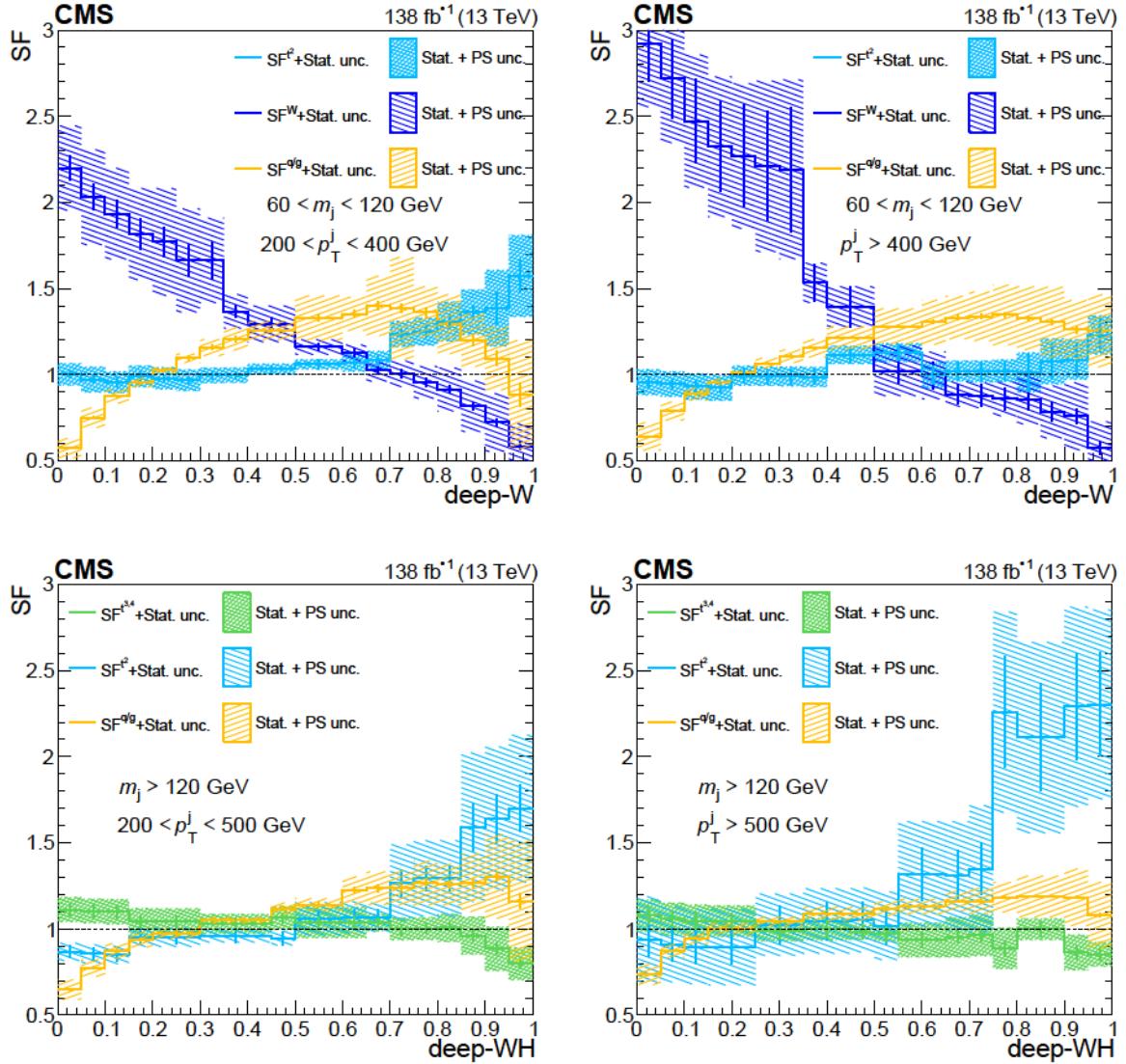


Figure 4: Measured scale factors (SFs) for the deep-W and deep-WH discriminants. Upper row: SFs for W (dark blue), t^2 (light blue), and q/g (yellow) matched jets in the low- m_j bins, LL (left) and LH (right), as functions of the deep-W discriminant value. Lower row: SFs for t^2 (light blue), $t^{3/4}$ (green), and q/g (yellow) matched jets in the high- m_j bins, HL (left) and HH (right), as functions of the deep-WH discriminant value. For each discriminant value bin, the sum of the SF-corrected jet yields is required to be equal to the observed data. The statistical and parton shower (PS) uncertainties are shown by the shaded bands.

7.3 Calibration of signal jets with SM proxy jets

The deep-W(WH) discriminant distributions for simulated signal events are also corrected using SFs. For resolved radion signal events ($N_j = 3$, SR4–6), the W-boson-matched jets are scaled by SF^W according to the p_T^j , m_j , and deep-W values for each jet.

Merged radion signal events ($N_j = 2$, SR1–3) contain jets of the form W, $R^{\ell qq}$, R^{3q} , and R^{4q} . Figure 7 (left) shows the relative contributions of each of these categories to the total as a function of m_j^{\max} . There are very few SM jets with the same substructure and flavor compositions as

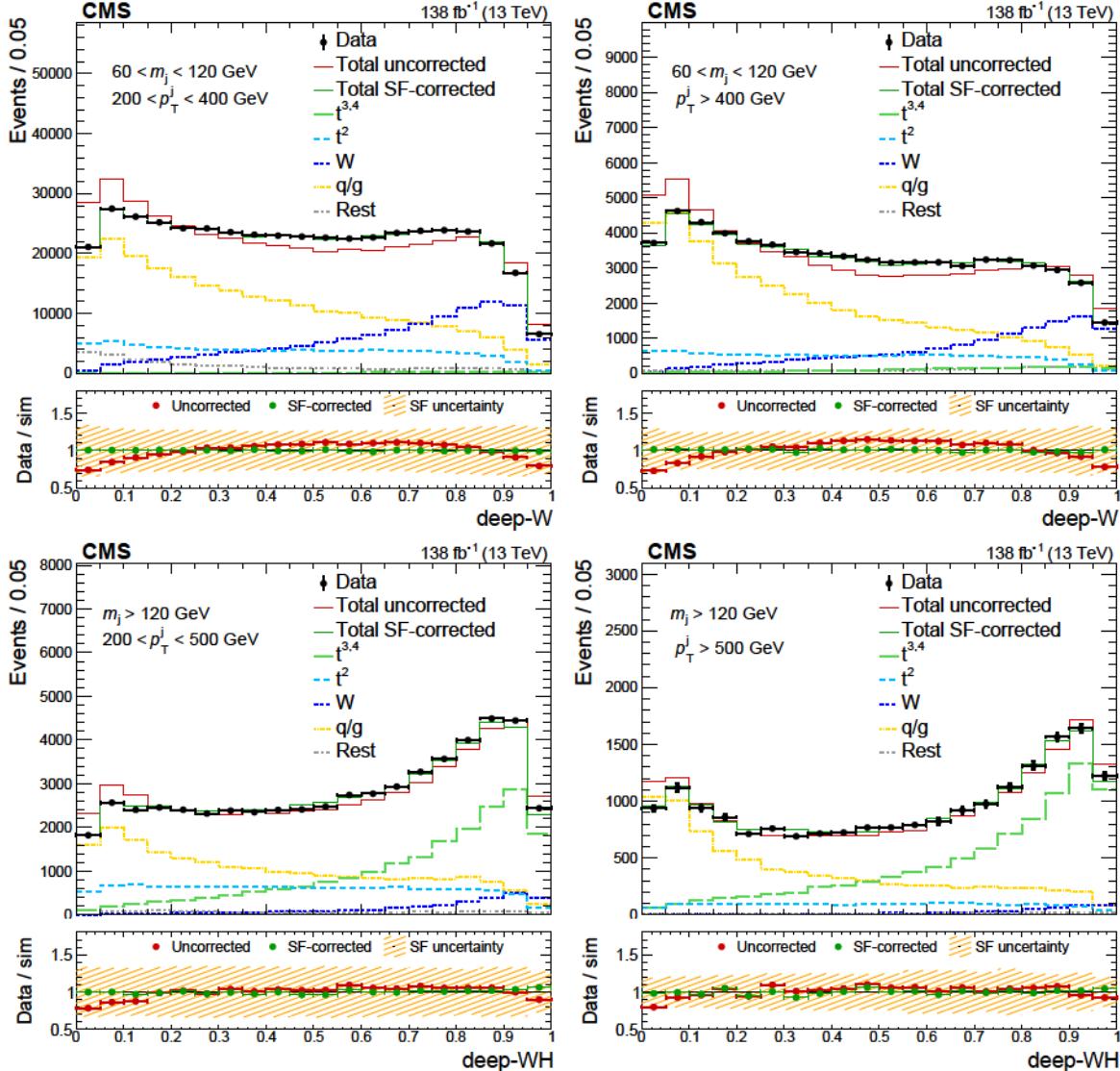


Figure 5: DEEPAK8 discriminants of the jet with highest mass in the single-lepton sideband. The deep-W spectra in the LL (upper left) and LH (upper right) samples are presented together with the deep-WH spectra in the HL (lower left) and HH (lower right) samples. The W boson jets are shown in dark blue, t^2 in light blue, $t^{3,4}$ in green, q/g in yellow, and the “Rest” jet types (jets not matching any of the categories) in gray. Before corrections (red), discrepancies between the prediction and the data can be observed, in particular at low and high discriminant values. The corrected distributions after application of the scale factors (SFs) are shown in dark green. The lower panels show the data-to-simulation ratios before and after corrections. The SF uncertainties are indicated by the shaded bands.

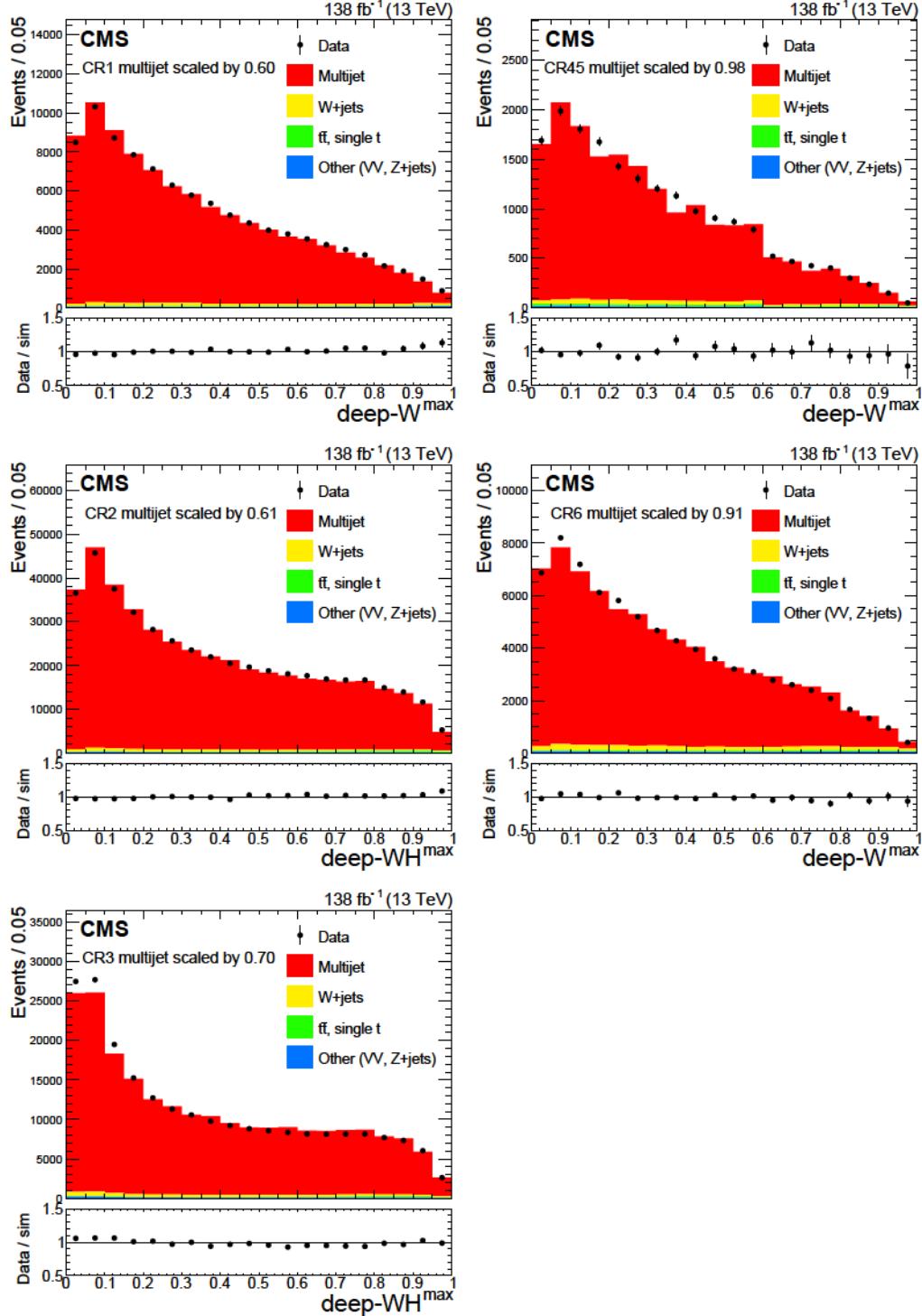


Figure 6: Comparison between data (black markers) and simulated background events (histograms) of the deep-W(WH) distributions for the highest-mass jet after SF application. The control regions CR1, CR2, CR3 are shown in the left column, upper to lower rows, while CR45 and CR6 are presented right column, upper and middle rows, respectively. The lower panels show the data-to-simulation ratio.

$R^{\ell qq}$, R^{3q} , and R^{4q} jets that can be directly used for calibration (considering that boosted Higgs bosons are not abundant). Instead, we calibrate these using SM jets that have similar prong substructure and deep-W(WH) response, which we call “proxy jets”.

The W boson jets exhibit highly similar deep-W and deep-WH distributions to $R^{\ell qq}$ jets. Thus, we use W boson jets as proxy jets for the $R^{\ell qq}$ calibration. The similarity of the two spectra can be seen in Fig. 7 for both the deep-W (used in SR1) and deep-WH (used in SR2–3) discriminants. This similarity results from the discriminant design, as the raw scores in both the numerator and denominator have not been derived for events with leptons inside jets, and so the deep-W and WH discriminants are largely blind to the presence of a lepton.

The closest abundant SM jets with substructure similar to R^{3q} and R^{4q} are fully merged top quark jets $t^{3,4}$. As Fig. 7 (right) shows, the deep-WH distributions of those three jet types are similar and thus the $t^{3,4}$ jets are used as proxy jets to calibrate signal R^{3q} and R^{4q} jets. Accordingly, the corresponding SF $t^{3,4}$ values derived in Section 7.1 are used to calibrate R^{3q} and R^{4q} jets. We find that the individual t^3 and t^4 components have an even better shape agreement with their corresponding signal jets R^{3q} and R^{4q} , respectively. This consistency suggests that despite their differences (in quark flavor, kinematics, and color recombination), the $t^{3,4}$ and $R^{3q,4q}$ jets have a largely similar response to the deep-WH discriminant. Systematic uncertainties are assigned to account for differences in this response and also to account for residual shape differences as discussed in Section 9.

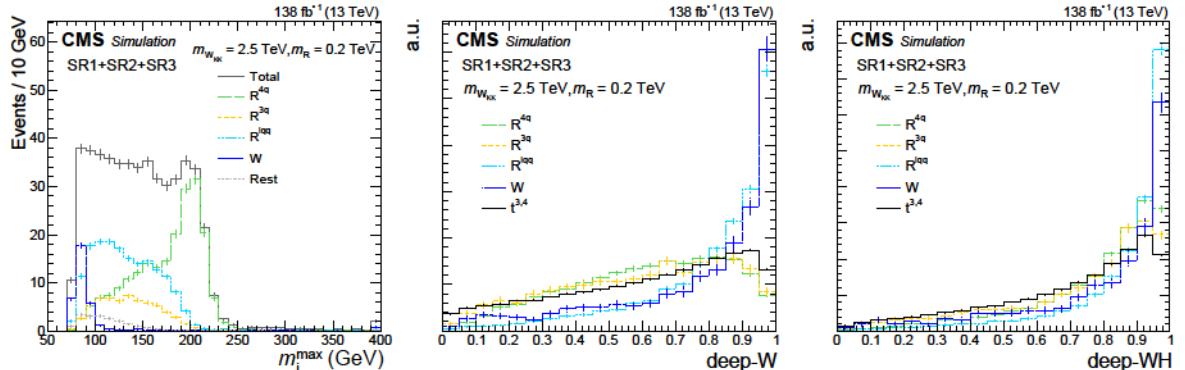


Figure 7: Shape comparison for different jet types in simulation. Left: the m_j^{max} distributions for SR1–3 events without deep-W(WH) constraints. Center and right: the deep-W and deep-WH distributions normalized to unity for the shown components, respectively. The $t^{3,4}$ jets from the preselected sample, normalized to unity, are superimposed to compare shapes with the R^{3q} and R^{4q} distributions.

8 Background estimation

The dominant background in all SRs consists of QCD multijet events, making up 60–80% of the total. As the DEEPAK8 tagger rejects the majority of these events, only a few of them remain in the SRs according to simulation. Thus, we estimate this background contribution directly from the data using CRs. The five CRs are defined by inverting at least one tagger condition, as described in Section 7.2. The selected jets in these regions possess similar kinematic properties to the ones in the corresponding SRs. The m_{jj} (m_{jjj}) distributions in CRs 1–6 are shown in Fig. 8, where the SF-corrected simulation is normalized to the data. After subtracting the other background processes estimated from simulated samples from the data, the resulting m_{jj} (m_{jjj}) distributions are used to predict the shape of the QCD multijet background in the correspond-

ing SRs. This shape compatibility has been validated in simulation in multiple selections, and the m_{jj} (m_{jjj}) distributions agree within the statistical uncertainties over the entire spectra. The a priori normalization in the SRs is taken from the SF-corrected simulation. All other smaller background contributions such as W+jets, $t\bar{t}$, single t quark, diboson, $t\bar{t}V$, and triboson production are taken from simulation.

9 Systematic uncertainties

Systematic uncertainties are taken into account in the background estimation and the signal prediction. For each source of uncertainty, a nuisance parameter is assigned, which is constrained by the data in the six SRs. These are summarized in Table 3.

Table 3: Sources of systematic uncertainties accounted for in the analysis. The first three sets of uncertainty sources originate from the tagger calibration. It is also indicated whether the uncertainties are evaluated for background (B) and/or signal (S), whether the uncertainty affects shape and/or rate, and the total number of nuisance parameters used per source.

Sources	B or S	Effect on	Magnitude	Nuisance parameters
Parton shower + selection bias for W, R^{qq}	B+S	Shape+rate	—	4, for LL, LH, HL, HH
Parton shower + selection bias for t^2	B	Shape+rate	—	8, for LL, LH, HL, HH
Parton shower + selection bias for $t^{3/4}, R^{3q,4q}$	B+S	Shape+rate	—	4, for LL, LH, HL, HH
Parton shower + selection bias for q/g	B	Shape+rate	—	8, for LL, LH, HL, HH
Proxy uncertainty for R^{qq}	S	Rate	10–35%	2, for deep-W(WH)
Proxy uncertainty for $R^{3q,4q}$	S	Rate	12–43%	2, for deep-W(WH)
Proxy uncertainty for unmatched	S	Rate	100%	2, for deep-W(WH)
High- p_T extrapolation for W	S	Rate	100%	2, for deep-W(WH)
High- p_T extrapolation for R^{qq}	S	Rate	23–30%	2, for deep-W(WH)
High- p_T extrapolation for R^{3q}	S	Rate	16–34%	2, for deep-W(WH)
High- p_T extrapolation for R^{4q}	S	Rate	24–33%	2, for deep-W(WH)
QCD multijet normalization	B	Rate	5–40%	5, common for SR4,5
$t\bar{t}$ normalization	B	Rate	15–30%	5, common for SR4,5
Other background normalization	B	Rate	30%	5, common for SR4,5
m_{jj}, m_{jjj} tail shape	B	Shape	—	6, one for each SR
$t\bar{t}$ shape	B	Shape	—	6, one for each SR
Pileup and integrated luminosity	S	Rate	1.7%	1, common for all SRs
PDFs, renormalization and factorization scales	S	Rate	1.4%	1, common for all SRs
Jet energy scale and resolution	S	Shape	—	2, common for all SRs
Jet mass scale	S	Shape	—	1, common for all SRs

9.1 Systematic uncertainties in the scale factor estimation

Systematic uncertainties in the signal and background rate and shape arise from the DEEPAK8 SF derivation. Two uncertainty sources common to signal and background jets are considered, and an additional two only for signal, which are described in Section 9.3. The common uncertainties are from parton shower variations, and the SF dependence on the jet subsample selection, referred to as the “selection bias” uncertainty in Table 3.

The SFs are derived using three different $t\bar{t}$ simulation samples: the nominal sample is generated using POWHEG with PYTHIA 8, a second one using POWHEG with HERWIG 7 [51], and a third one using MADGRAPH5_aMC@NLO with PYTHIA 8. Half of the maximum difference of the three resulting SFs is assigned as the parton shower uncertainty for the W , t^2 , and $t^{3/4}$ SFs. For the q/g SFs, the parameters controlling the parton shower behavior in the QCD multijet

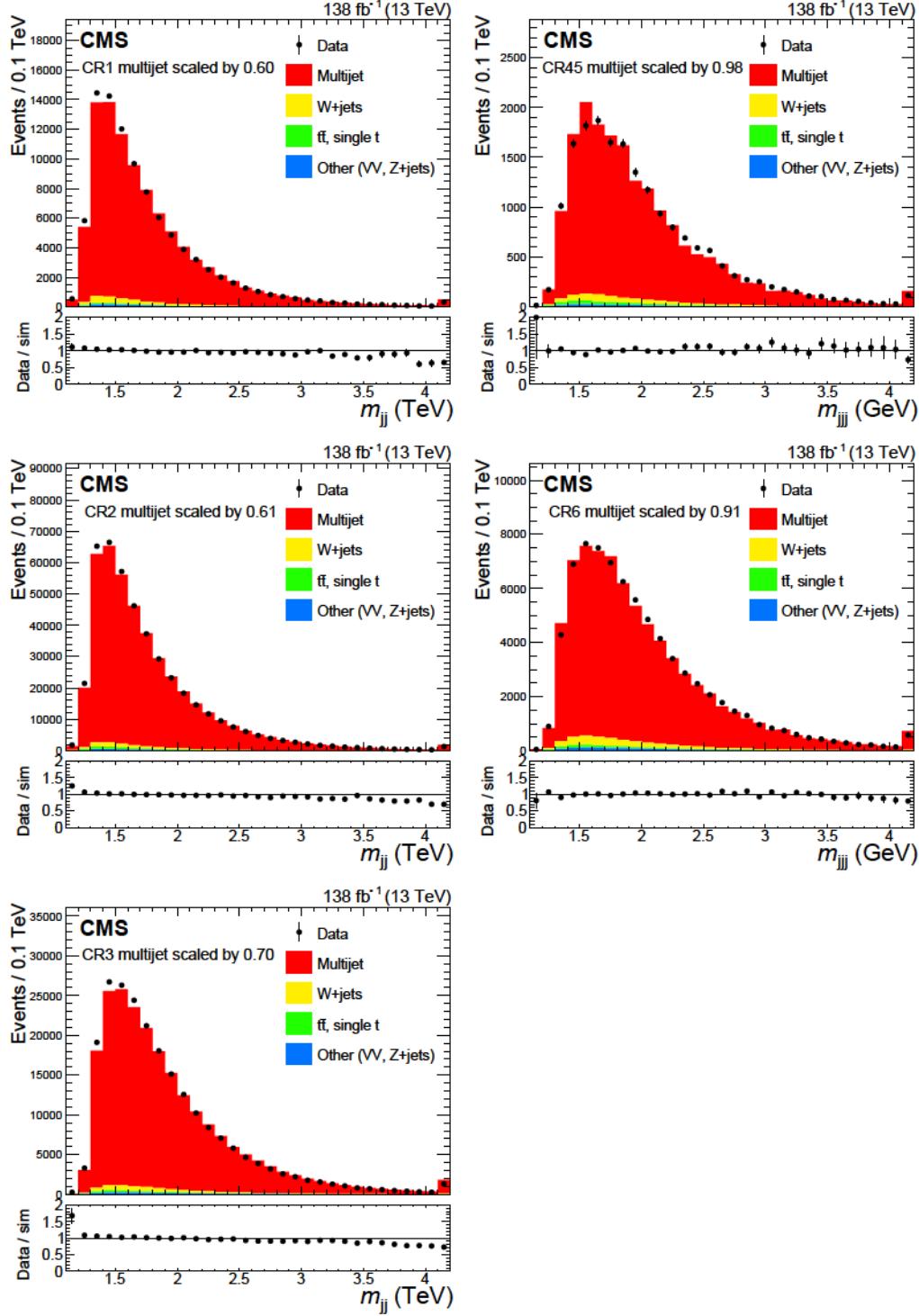


Figure 8: Invariant mass distributions of the reconstructed triboson systems for control regions in data (black markers) and simulated events (histograms). The m_{jj} distributions for CR1, CR2, CR3 are presented in the left column, upper to lower rows, respectively; the m_{jjj} distributions for control regions CR45 and CR6 are presented in the right column, upper and middle rows, respectively. The simulation is corrected by SFs, and the QCD multijet background is scaled to the data yields.

PYTHIA sample are varied to derive an uncertainty. The resulting uncertainty bands are shown in Fig. 4, combined with the significantly smaller statistical uncertainty.

The bias in the SF calculation due to the selection conditions defining the jet subsample is estimated by performing closure tests in several validation regions such as jet mass sidebands. The maximum nonclosure observed amounts to 10% for W , $t^3\bar{t}^4$, and q/g jets. Because of the limited numbers of events in the validation regions for t^2 jets and for jets not matching any of these categories, a 100% uncertainty is assigned to those. Uncertainties in the parton shower modeling and those arising from the selection bias are added in quadrature, and are assigned a single nuisance parameter for each matched jet in each LL, LH, HL, or HH bin. The per-jet variation is treated as fully correlated. Effects on both rate and shape of the m_{jj} (m_{jjj}) distributions are considered. The overall rate uncertainties due to this variation amount to about 35% for SRs 1–3 and SR6, 52% for SR4, and 45% for SR5. These values are driven by the SF uncertainty on q/g jets, which constitute 75–90% of the highest-mass jets in the SRs.

9.2 Systematic uncertainties in the background estimation

For the shape of the dominant QCD multijet background, we account for an additional uncertainty in the tail shape of the m_{jj} (m_{jjj}) distributions. This uncertainty is derived in the CRs by comparing the QCD multijet prediction in simulation to the data. A linear fit is performed to the ratio of the data and the simulation. The resulting ± 2 standard deviation bands are used as shape variations of the m_{jj} (m_{jjj}) distributions in the SRs. A single nuisance parameter with a Gaussian prior is used for each SR. This shape uncertainty allows the tails of the distributions to be adjusted by the data, accounting for effects that could lead to differences between CRs and SRs, e.g., a potential residual mass correlation of the taggers.

The uncertainty in the normalization of the QCD multijet background is taken as the normalization difference between data and SF-corrected simulation in the corresponding CRs. These differences range from 9 to 40% for SRs 1–3 and SR6, and 5% for SR4–5. For the top quark production rate, uncertainties in the normalization to NNLO and NLO predictions and missing higher orders are accounted for and are in the range 15–30%. In addition, uncertainties in the $t\bar{t}$ shape are derived by varying the top quark p_T spectrum based on the measurements in Refs. [52, 53]. For the other background processes, which are treated collectively, a 30% normalization rate uncertainty is assigned for all SRs. Because of their similarity, the same normalization nuisance parameters are used for SRs 4 and 5. All rate uncertainties are estimated using a log-normal prior.

9.3 Signal systematic uncertainties

The integrated luminosities of the 2016, 2017, and 2018 data-taking periods are individually known with uncertainties in the 1.2–2.5% range [15–17], while the total 2016–2018 integrated luminosity has an uncertainty of 1.6%. The simulated PU distribution is scaled to match data using an effective total inelastic cross section of 69.2 mb. The uncertainty in this procedure is evaluated by varying the total inelastic cross section by $\pm 4.6\%$ [54]. This results in a 0.5% uncertainty in the signal normalization in the SRs, which is combined with the integrated luminosity uncertainty for a total uncertainty of 1.7%, implemented with a lognormal prior.

Renormalization R and factorization F scales and PDF uncertainties affecting the signal selection efficiency are evaluated per SR and mass point. The scale uncertainties are obtained by varying the R and F independently by factors of 1/2 and 2 (without considering the extreme cases of the opposite-direction variations). The maximum value of these variations is taken as the prefit uncertainty. For the overall scale uncertainty, a single nuisance parameter is used. Its

typical magnitude is up to 1.4% for signal with $m_{W_{KK}} = 4 \text{ TeV}$.

The jet energy scale is varied by its uncertainty and the impact on the m_{jj} (m_{jjj}) distributions is taken to be the associated shape uncertainty. Similarly, for the uncertainties in the jet energy and jet mass resolution, shape uncertainties are considered by varying the jets selected by the respective uncertainties. All three uncertainty sources are implemented as nuisance parameters using Gaussian priors.

All of the above signal uncertainties only have a small impact on the final result. The largest signal uncertainty source lies in the DEEPAK8 tagger SF correction procedure. Four different uncertainties are considered for this. The uncertainties in the parton shower and selection bias are evaluated together with those of the background processes described in Section 9.1, using the same nuisance parameters for signal and background, and are constrained using the data in the SRs. The SFs of the signal jets categorized as W, R^{qq}, R^{3q}, and R^{4q} are considered as correlated with the SFs of the corresponding W and t^{3,4} SM proxy jets. The other two SF uncertainty sources are due to the difference between signal and proxy jets (proxy uncertainty), and to account for the significantly higher p_T that signal jets have compared to the SM jets (high- p_T extrapolation uncertainty).

Although the signal jets share similar substructures with the corresponding SM proxies and also have similar deep-W(WH) distributions, they are, with the exception of W boson jets, not the same objects. For example, the flavor of the most energetic quarks might differ, the color flow structure might not be the same, and overall jet substructure kinematic properties could be different. To account for all these differences, the shape difference of proxy and signal jets in six deep-W(WH) bins above the 0.7 discriminant selection value (0.7–1.0 in 0.05 bins) is evaluated in simulation. For each of these six bins, the relative difference between the proxy and the signal jets is taken as an uncertainty. For signal jets categorized as R^{3q,4q}, for which the corresponding proxy jet category is t^{3,4}, an additional uncertainty due to the difference observed between t³ and t⁴ is assigned. It amounts to 5 and 10% for the deep-WH and deep-W discriminants, respectively. The total resulting proxy uncertainty for R^{qq}, R^{3q}, and R^{4q} signal jets lies in the ranges 10–35%, 13–34%, and 12–43%, respectively. This source of uncertainty has the largest effect on the rate for the merged signal. Signal jets not matching any of these categories are assigned a 100% proxy uncertainty. The proxy uncertainty is evaluated separately for deep-W (used in SR1) and deep-WH (used in SR2–3), and is different for each signal mass scenario.

The high- p_T extrapolation uncertainty accounts for the fact that the SFs are derived in events containing jets with transverse momenta of a few hundred GeV, while the signal jets often have $p_T > 1 \text{ TeV}$. To account for this effect, the difference in the signal selection efficiency when using HERWIG++ [55] to perform the parton shower is evaluated with respect to the default PYTHIA 8 parton shower. The uncertainty is evaluated separately for each of the four types of signal jets (W, R^{qq}, R^{3q}, and R^{4q}) for the deep-W and deep-WH discriminants. It lies in the ranges 20–30 and 5–40% for the merged and resolved signal, respectively. The four DEEPAK8 tagger SF uncertainties are considered as uncorrelated and result in a total uncertainty ranging from 53–63% and 10–45% for merged and resolved signal, respectively.

10 Statistical analysis and results

The final m_{jj} (m_{jjj}) distributions for the SRs after performing a binned maximum likelihood fit in all six SRs simultaneously are shown in Fig. 9. No signal-like excess over the background expectation is observed in the data. Upper limits at 95% confidence level (CL) are set on the production cross section of a potential resonance signal as functions of the W_{KK} and R reso-

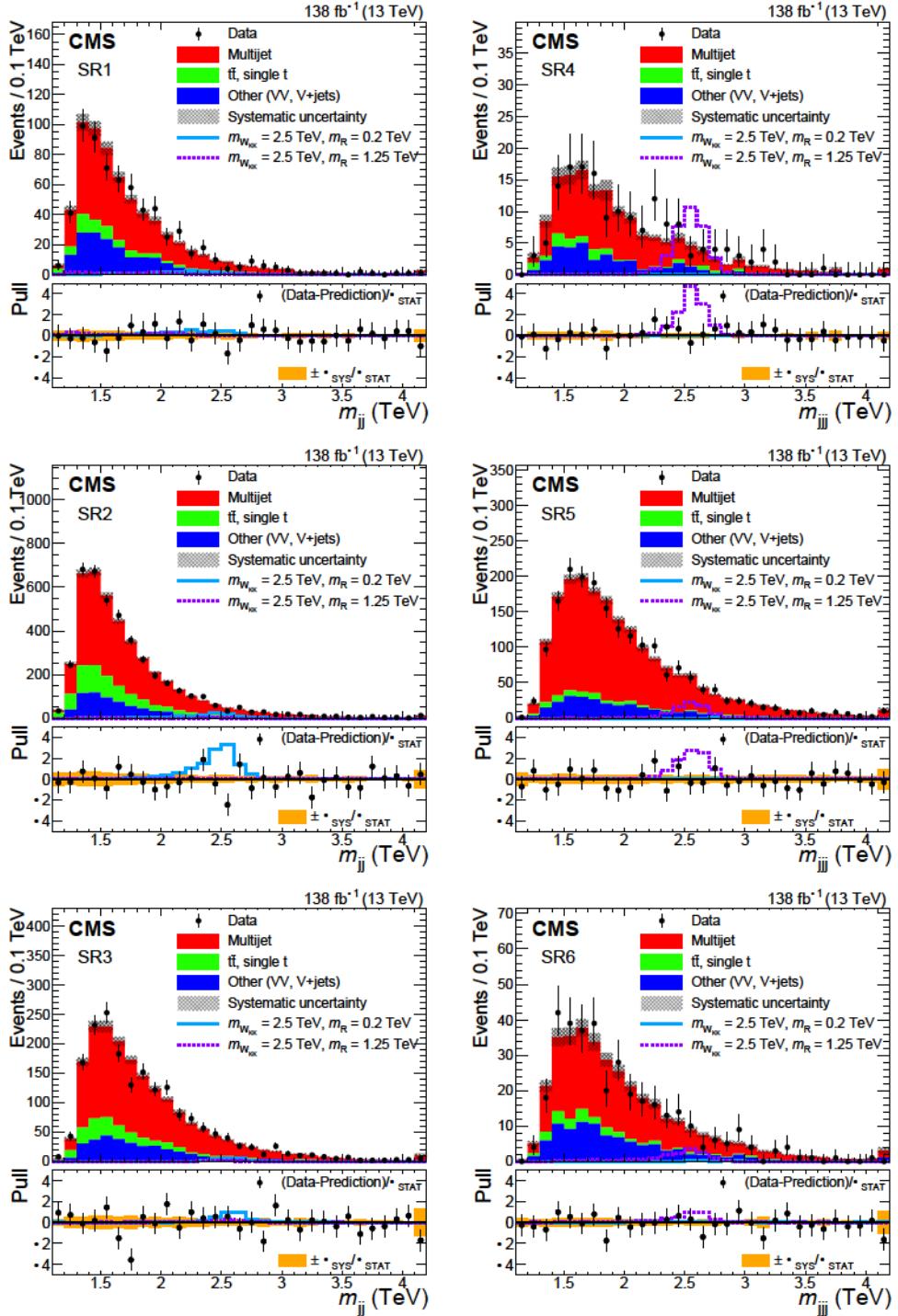


Figure 9: Post-fit distributions of the invariant mass of the reconstructed triboson system (m_{jj} , m_{tribo}) in data (black markers) and simulation (histograms) for all SRs (SRs 1–3 in the left column and SRs 4–6 in the right column). Systematic uncertainties are indicated by the shaded bands. Signal examples are superimposed, normalized to the theoretical prediction for the production cross section of $m_{W_{KK}} = 2.5 \text{ TeV}$ with $m_R = 0.2 \text{ TeV}$ (solid light blue line) and 1.25 TeV (dashed purple line). The bottom panels show the pull distributions, indicating the difference between the data and background prediction, divided by the statistical uncertainty in the background, with error bars representing the statistical uncertainty and shaded bands showing the one standard deviation systematic uncertainty, normalized by the statistical uncertainty.

nance masses. The limits are set following the modified frequentist approach as described in Refs. [56, 57] and the definition of the profile likelihood test statistic as in Ref. [58] using an asymptotic approximation [59]. Figure 10 shows the limits on the product of the W_{KK} production cross section and the branching fraction to three W bosons.

We exclude W_{KK} resonances decaying in cascade via a scalar radion R to three W bosons at 95% CL with $m_{W_{KK}}$ up to 3 TeV for the lowest m_R of 200 GeV probed using the model provided in Refs. [3–6]. The highest m_R value excluded is 1.5 TeV for $m_{W_{KK}} = 2.3$ TeV. The lower limits set on the production cross sections range from 70 fb at $m_{W_{KK}} = 1.5$ TeV down to 0.5 fb at $m_{W_{KK}} = 5$ TeV.

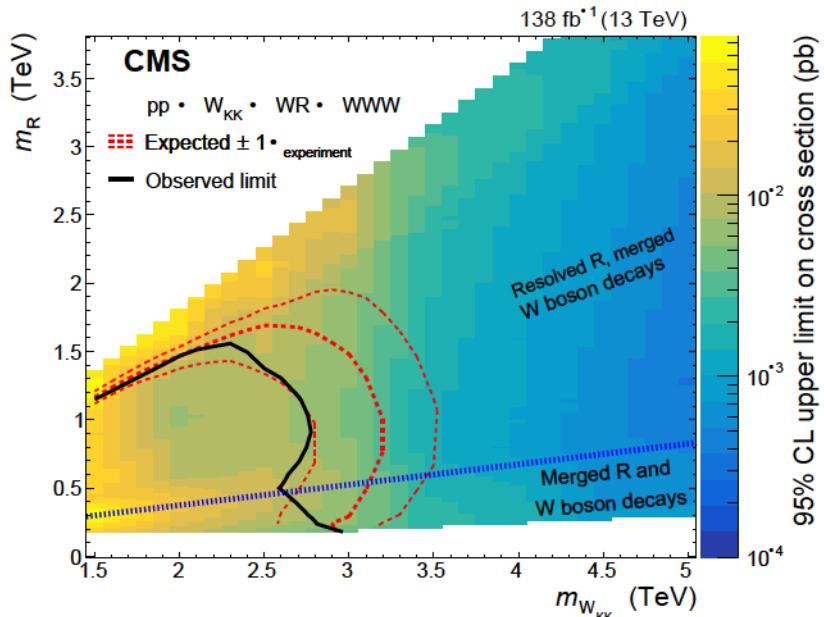


Figure 10: Expected (red dashed lines) and observed (solid black line) lower limits at 95% CL on the W_{KK} and R resonance masses for the particular parameters of the explored model. The colored area indicates the observed upper limit on the product of the signal cross section and the branching fraction to three W bosons. The blue dashed line indicates the border between the merged and resolved decay topologies probed. A signal with m_R lower than 180 GeV is not considered in this search to maintain on-shell W bosons, while for $m_{W_{KK}} > 3$ TeV, we only consider $m_R > 0.06 m_{W_{KK}}$.

For the resolved case, most of the sensitivity originates from SR4, complemented by SR5. For the merged case, SR2 and SR3 contribute to a similar extent. The SR1 and SR6 recover sensitivity to events where one W boson has relatively low p_T or mass.

11 Summary

A search for resonances decaying in cascade via a radion R to three W bosons, $W_{KK} \rightarrow WR \rightarrow WWW$, in the all-hadronic final state has been presented. The search is performed in proton-proton collision data at a center-of-mass energy of 13 TeV, corresponding to a total integrated luminosity of 138 fb^{-1} . The final states include two or three massive, large-radius jets containing the decay products of the hadronically decaying W bosons. The two-jet case corresponds to events where the radion decay products are reconstructed as a single merged jet. The three-jet case corresponds to events where each W boson from the radion decay is reconstructed as

a single merged jet. In this analysis and the analysis in the single-lepton channel reported in Ref. [10], previously unexplored signatures are probed, using novel jet substructure techniques. In particular, a dedicated radion tagger based on a neural network, targeting simultaneously three different radion decay topologies, has been developed. This tagger has been calibrated with a novel “matrix method”. These techniques are also applicable to the identification of $H \rightarrow 4q$ and $H \rightarrow qq$ decays of Lorentz-boosted Higgs bosons. Exclusion limits are set on the product of the production cross section and the branching fraction to three W bosons in an extended warped extra-dimensional model. This result, together with an analysis in the single-lepton channel [10], are the first of their kind, and constrain the parameters of this model for the first time.

Acknowledgments

We congratulate our colleagues in the CERN accelerator departments for the excellent performance of the LHC and thank the technical and administrative staffs at CERN and at other CMS institutes for their contributions to the success of the CMS effort. In addition, we gratefully acknowledge the computing centers and personnel of the Worldwide LHC Computing Grid and other centers for delivering so effectively the computing infrastructure essential to our analyses. Finally, we acknowledge the enduring support for the construction and operation of the LHC, the CMS detector, and the supporting computing infrastructure provided by the following funding agencies: BMBWF and FWF (Austria); FNRS and FWO (Belgium); CNPq, CAPES, FAPERJ, FAPERGS, and FAPESP (Brazil); MES and BNSF (Bulgaria); CERN; CAS, MoST, and NSFC (China); MINCIENCIAS (Colombia); MSES and CSF (Croatia); RIF (Cyprus); SENESCYT (Ecuador); MoER, ERC PUT and ERDF (Estonia); Academy of Finland, MEC, and HIP (Finland); CEA and CNRS/IN2P3 (France); BMBF, DFG, and HGF (Germany); GSRI (Greece); NKFIH (Hungary); DAE and DST (India); IPM (Iran); SFI (Ireland); INFN (Italy); MSIP and NRF (Republic of Korea); MES (Latvia); LAS (Lithuania); MOE and UM (Malaysia); BUAP, CINVESTAV, CONACYT, LNS, SEP, and UASLP-FAI (Mexico); MOS (Montenegro); MBIE (New Zealand); PAEC (Pakistan); MSHE and NSC (Poland); FCT (Portugal); JINR (Dubna); MON, RosAtom, RAS, RFBR, and NRC KI (Russia); MESTD (Serbia); MCIN/AEI and PCTI (Spain); MOSTR (Sri Lanka); Swiss Funding Agencies (Switzerland); MST (Taipei); ThEPCenter, IPST, STAR, and NSTDA (Thailand); TUBITAK and TAEK (Turkey); NASU (Ukraine); STFC (United Kingdom); DOE and NSF (USA).

Individuals have received support from the Marie-Curie program and the European Research Council and Horizon 2020 Grant, contract Nos. 675440, 724704, 752730, 758316, 765710, 824093, 884104, and COST Action CA16108 (European Union); the Leventis Foundation; the Alfred P. Sloan Foundation; the Alexander von Humboldt Foundation; the Belgian Federal Science Policy Office; the Fonds pour la Formation à la Recherche dans l’Industrie et dans l’Agriculture (FRIA-Belgium); the Agentschap voor Innovatie door Wetenschap en Technologie (IWT-Belgium); the F.R.S.-FNRS and FWO (Belgium) under the “Excellence of Science – EOS” – be.h project n. 30820817; the Beijing Municipal Science & Technology Commission, No. Z191100007219010; the Ministry of Education, Youth and Sports (MEYS) of the Czech Republic; the Deutsche Forschungsgemeinschaft (DFG), under Germany’s Excellence Strategy – EXC 2121 “Quantum Universe” – 390833306, and under project number 400140256 - GRK2497; the Lendület (“Momentum”) Program and the János Bolyai Research Scholarship of the Hungarian Academy of Sciences, the New National Excellence Program ÚNKP, the NKFIH research grants 123842, 123959, 124845, 124850, 125105, 128713, 128786, and 129058 (Hungary); the Council of Science and Industrial Research, India; the Latvian Council of Science; the Ministry of Science and Higher Education and the National Science Center, contracts Opus

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