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Measurements of π^- production in ${}^7\text{Be}+{}^9\text{Be}$ collisions at beam momenta from $19A$ to $150A$ GeV/ c in the NA61/SHINE experiment at the CERN SPS

The NA61/SHINE Collaboration

The NA61/SHINE collaboration studies at the CERN Super Proton Synchrotron (SPS) the onset of deconfinement in hadronic matter by the measurement of particle production in collisions of nuclei with various sizes at a set of energies covering the SPS energy range. This paper presents results on inclusive double-differential spectra and mean multiplicities of π^- mesons produced in the 5% most *central* ${}^7\text{Be}+{}^9\text{Be}$ collisions at beam momenta of $19A$, $30A$, $40A$, $75A$ and $150A$ GeV/ c obtained by the so-called h^- method which does not require any particle identification.

The shape of the transverse mass spectra differs from the shapes measured in central Pb+Pb collisions and inelastic $p+p$ interactions. The normalized width of the rapidity distribution decreases with increasing collision energy and is in between the results for inelastic nucleon-nucleon and central Pb+Pb collisions. The mean multiplicity of pions per wounded nucleon in *central* ${}^7\text{Be}+{}^9\text{Be}$ collisions is close to that in central Pb+Pb collisions up to $75A$ GeV/ c . However, at the top SPS energy the result is close to the one for inelastic nucleon-nucleon interactions.

The results are discussed in the context of predictions for the onset of deconfinement at the CERN SPS collision energies.

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1 Introduction

This paper presents measurements of inclusive spectra and mean multiplicities of π^- mesons produced in *central* ${}^7\text{Be}+{}^9\text{Be}$ collisions at beam momenta of 19A, 30A, 40A, 75A and 150A GeV/c ($\sqrt{s_{NN}} = 6.1, 7.6, 8.8, 11.9$ and 16.8 GeV) performed by the NA61/SHINE collaboration. These results are part of the strong interactions studies proposed by the NA61/SHINE collaboration [1] to investigate the properties of the onset of deconfinement and to search for the possible existence of a critical point in the phase diagram of strongly interacting matter. The first goal of the programme is motivated by the observation of rapid changes of hadron production properties in central Pb+Pb collisions at about 30A GeV/c by the NA49 experiment [2, 3] - a sharp peak in the kaon to pion ratio ("horn"), the start of a plateau in the inverse slope parameter for kaons ("step"), and a steepening of the increase of pion production per wounded nucleon with increasing collision energy ("kink"). These findings were predicted and interpreted as the onset of deconfinement [4, 5]. They were recently confirmed by the RHIC beam energy scan programme [6], and the interpretation is supported by the LHC results (see Ref. [7] and references therein). Experimentally the goals of the NA61/SHINE strong interaction programme are pursued by a two dimensional scan in collision energy and nuclear mass number of colliding nuclei. The scan allows to explore systematically the phase diagram of strongly interacting matter [1]. In particular, the analysis of the existing data within the framework of statistical models suggests that by increasing collision energy one increases temperature and decreases baryon chemical potential of strongly interacting matter at freeze-out [8], whereas by increasing nuclear mass number of the colliding nuclei one decreases the temperature [9, 8, 10].

Within this programme NA61/SHINE recorded data on $p+p$, Be+Be, Ar+Sc, Xe+La and Pb+Pb collisions. Further high statistics measurements of Pb+Pb collisions are planned with an upgraded detector starting in 2021 [11]. Results on particle spectra and multiplicities have already been published from $p+p$ interactions [12, 13, 14] which represent the basic reference. This paper reports NA61/SHINE results from the next step in size of the collision system namely measurements of π^- production for the 5% most *central* ${}^7\text{Be}+{}^9\text{Be}$ collisions. The data were recorded in 2011, 2012 and 2013 using a secondary ${}^7\text{Be}$ beam produced by fragmentation of the primary Pb beam from the CERN SPS [15]. The ${}^7\text{Be}+{}^9\text{Be}$ collisions play a special role in the NA61/SHINE scan programme. First, it was predicted within the statistical models [16, 17] that the yield ratio of strange hadrons to pions in these collisions should be close to those in central Pb+Pb collisions and significantly higher than in $p+p$ interactions. Second, the collision system composed of a ${}^7\text{Be}$ and a ${}^9\text{Be}$ nucleus has eight protons and eight neutrons, and thus is isospin symmetric. Within the NA61/SHINE scan programme the ${}^7\text{Be}+{}^9\text{Be}$ collisions serve as the lowest mass isospin symmetric reference needed to study collisions of medium and large mass nuclei. This is of particular importance when data on proton-proton, neutron-proton and neutron-neutron are not available to construct the nucleon-nucleon reference [18].

In this paper the so-called h^- method is used for determining π^- production since it provides the largest phase space coverage. This procedure utilizes the fact that negatively charged particles are predominantly π^- mesons with a small admixture (of order 10%) of K^- mesons and anti-protons which can be subtracted reliably.

The paper is organized as follows: after this introduction the experiment is briefly described in Sec. 2. The analysis procedure is discussed in Sec. 3. Section 4 describes the results of the analysis. In Sec. 5 the new measurements are discussed and compared to model calculations. A summary closes the paper.

The following variables and definitions are used in this paper. The particle rapidity y is calculated in the collision center of mass system (cms), $y = 0.5 \cdot \ln[(E + p_L)/(E - p_L)]$, where E and p_L are the particle energy and longitudinal momentum, respectively. The transverse component of the momentum is denoted as p_T , and the transverse mass m_T is defined as $m_T = \sqrt{m^2 + (cp_T)^2}$ where m is the particle mass. The momentum in the laboratory frame is denoted p_{lab} and the collision energy per nucleon pair in the center of mass by $\sqrt{s_{NN}}$.

Be+Be collisions can be characterized by the energy detected in the region populated by projectile spectators. Low values of this forward energy are referred to *central* collision and a selection of collisions based on the forward energy is called a *centrality* selection. Although for Be+Be collisions the forward energy is not tightly correlated with the impact parameter of the collision, the terms *central* and *centrality* are adopted following the convention widely used in heavy-ion physics.

2 Experimental setup

2.1 Detector

The NA61/SHINE experiment is a multi-purpose facility designed to measure particle production in nucleus-nucleus, hadron-nucleus and $p+p$ interactions [19]. The detector is situated at the CERN Super Proton Synchrotron (SPS) in the H2 beamline of the North experimental area. A schematic diagram of the setup during Be+Be data taking is shown in Fig. 1. The main components of the produced particle detection system are four large volume Time Projection Chambers (TPC). Two of them, called Vertex TPCs (VTPC), are located downstream of the target inside superconducting magnets with maximum combined bending power of 9 Tm. The magnetic field was scaled down in proportion to the beam momentum in order to obtain similar phase space acceptance at all energies. The main TPCs (MTPC) and two walls of pixel Time-of-Flight (ToF-L/R) detectors are placed symmetrically to the beam line downstream of the magnets. The fifth small TPC (GAP-TPC) is placed between VTPC1 and VTPC2 directly on the beam line. The TPCs are filled with Ar:CO₂ gas mixtures in proportions 90:10 for the VTPCs and the GAP-TPC, and 95:5 for the MTPCs.

The Projectile Spectator Detector (PSD), which covers the region into which the projectile spectators are emitted is positioned 20.5 m (16.7 m) downstream of the MTPCs at 75A and 150A GeV/c (19A, 30A, 40A GeV/c) centered in the transverse plane on the deflected position of the beam. The PSD allows to select the *centrality* of the collision by imposing an upper limit on the measured forward energy.

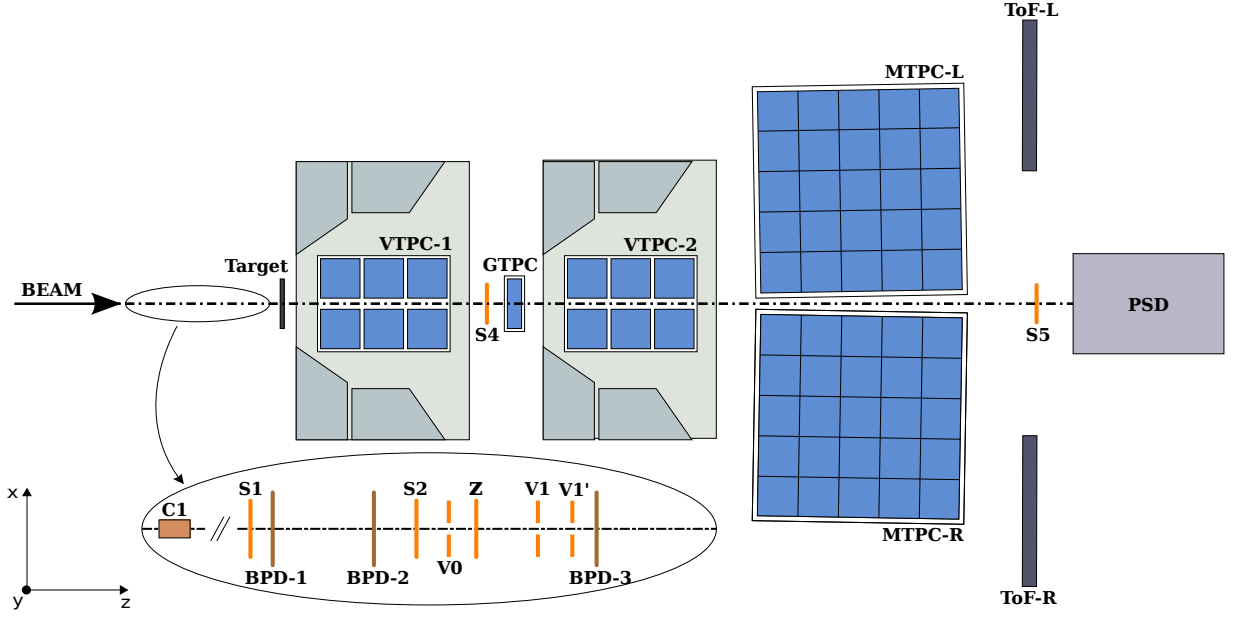


Figure 1: The schematic layout of the NA61/SHINE experiment at the CERN SPS [19] showing the components used for the Be+Be energy scan (horizontal cut, not to scale). The beam instrumentation is sketched in the inset (see also Fig. 2 below). Alignment of the chosen coordinate system as shown in the figure; its origin lies in the middle of VTPC-2, on the beam axis. The z axis is along the nominal beam direction. The magnetic field bends charged particle trajectories in the x-z (horizontal) plane. The drift direction in the TPCs is along the y (vertical) axis.

The beam line instrumentation is schematically depicted in Fig. 2. A set of scintillation counters as well as beam position detectors (BPDs) [19] upstream of the target provide timing reference, selection, identification and precise measurement of the position and direction of individual beam particles.

The target was a 12 mm thick plate of ^9Be placed ≈ 80 cm upstream of VTPC1. Mass concentrations of impurities in the target were measured at 0.3% resulting in an estimated increase of the produced pion multiplicity by less than 0.5% [20]. No correction was applied for this negligible contamination. Data were taken with target inserted (denoted I, 90%) and target removed (denoted R, 10%).

2.2 ^7Be Beam

The beam line of NA61/SHINE experiment is designed to provide good momentum resolution and particle identification even with secondary ion beams. The beam instrumentation (see Fig. 2) consists of scintillator counters (S) used for triggering and beam particle identification, veto scintillation counters (V) with a hole in the middle for rejection of upstream interactions and beam halo particles, and a Cherenkov charge detector Z built based on quartz glass radiator for the measurement of the secondary beam charge. Additionally the three Beam Position Detectors (BPDs) are used for determination of the charge of individual beam particles.

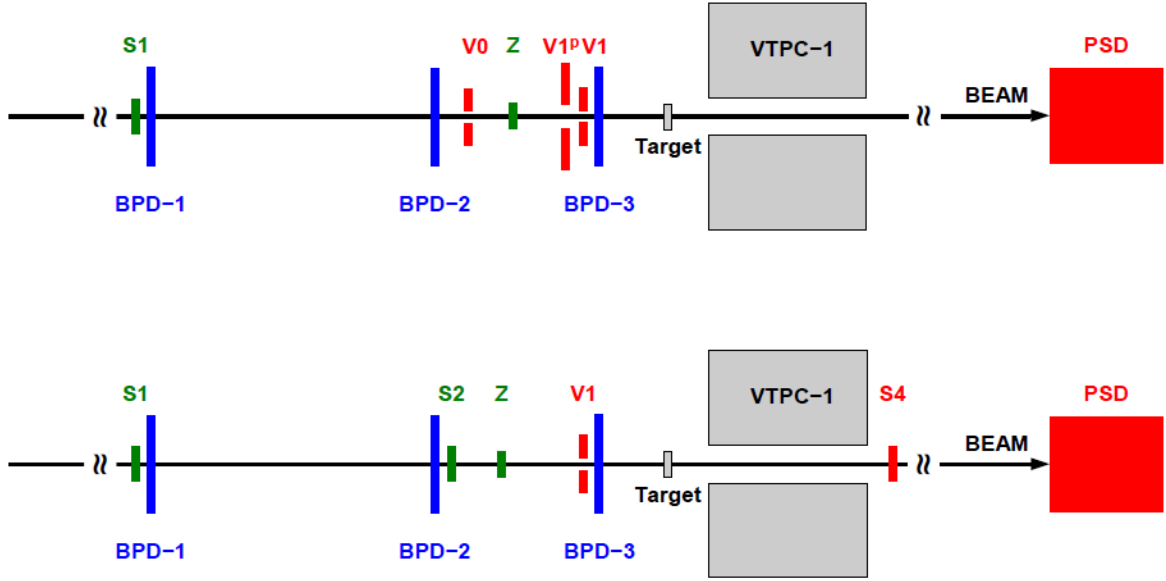


Figure 2: The schematic of the placement of the beam and trigger detectors in high-momentum (*top*) and low-momentum (*bottom*) data taking configurations showing scintillation counters S, veto counters V, charge Cherekov counter Z and beam position detectors BPD.

This paragraph provides a brief description of the ${}^7\text{Be}$ beam properties (see [15]). Primary Pb^{82+} ions extracted from the SPS were steered toward a 180 mm long beryllium fragmentation target placed 535 m upstream of the NA61/SHINE experiment. An interaction of a Pb-ion with the fragmentation target produces a mixture of nuclear fragments with a large fraction of so-called spectator nucleons which originate from the Pb nucleus but did not participate in the collision. Their momenta per nucleon p_N are equal to the beam momentum per nucleon smeared by Fermi motion. The field strength in the bending magnets of the beam line define the rigidity of the transported charged particles: $B\rho = 3.33 \cdot p_{\text{beam}}/Z$, where $B\rho$ can be adjusted by setting the current in the dipole magnets and $p_{\text{beam}} = A \cdot p_N$ is the beam momentum and Z the charge of the beam particle. Thus the beam line selects particles with the wanted A/Z ratio. Figure 3 shows the charge spectrum of a fragment beam with a rigidity corresponding to fully stripped ${}^7\text{Be}$ ions with a momentum of $150 A \text{ GeV}/c$ measured by the Z detector. A well separated peak for charge Z equal 4 is visible. In a special run taken at beam momentum of $13.9 A \text{ GeV}/c$ it was possible to also measure the time-of-flight of the beam particles. As demonstrated in Fig. 4 the selected Be fragments are pure ${}^7\text{Be}$.

2.3 Trigger

The schematic of the placement of the beam and trigger detectors can be seen in Fig. 2. The trigger detectors consist of a set of scintillation counters recording the presence of the beam particle (S1, S2), a set of veto scintillation counters with a hole used to reject beam particles passing far from the centre of the beamline (V0, V1), and a charge detector (Z). Beam particles were defined by the coincidence $T1 = S1 \cdot S2 \cdot \overline{V1} \cdot Z(\text{Be})$ and $T1 = S1 \cdot \overline{V0} \cdot \overline{V1} \cdot \overline{V1}' \cdot Z(\text{Be})$ for

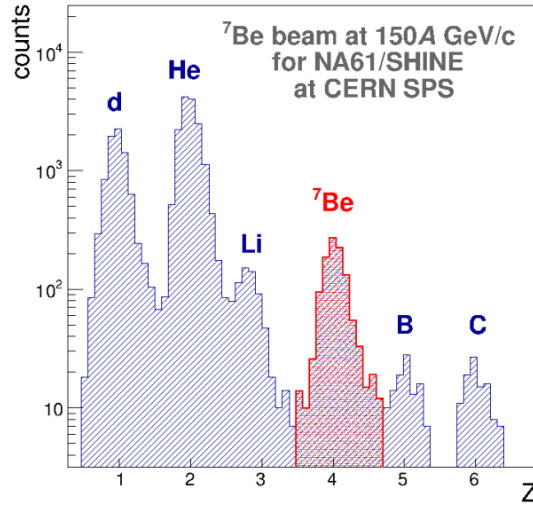


Figure 3: Charge of the beam particles measured by the Z detector.

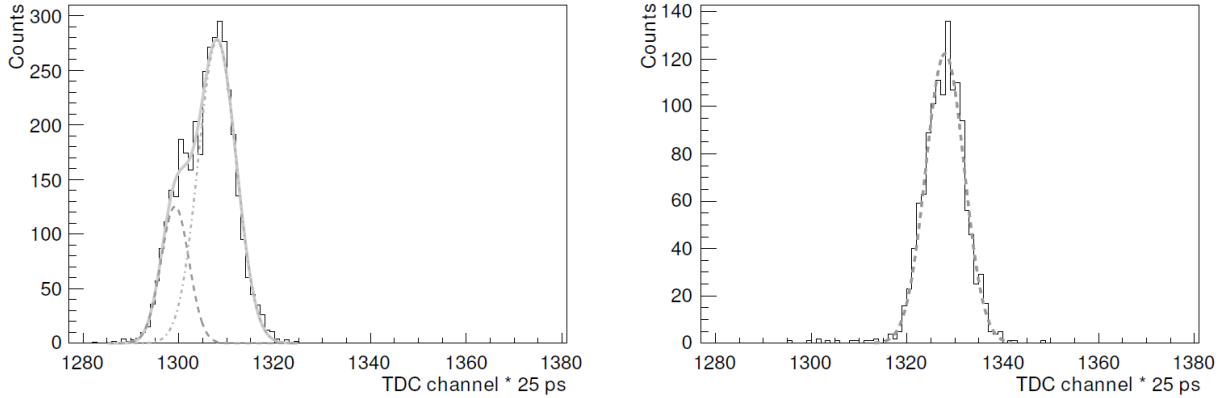


Figure 4: Mass of fragments of Z/A with momentum of $13.9A \text{ GeV}/c$. Left: carbon ions show double Gaussian structure due to two isotopes of carbon in the beam. Right: beryllium ions show single Gaussian distribution, indicating isotopic purity of the beryllium in the beam. Charge of the beam particle was selected by the measurement of scintillation counters.

low and high momentum data taking respectively. In addition, for the two lower energies an interaction trigger detector (S4) was used to check whether the beam particle changed charge after passing through the target. *Central* collisions were selected by requiring an energy signal below a set threshold from the 16 central modules of the PSD. The event trigger condition thus was $T2 = T1 \cdot S4 \cdot \overline{\text{PSD}}$ and $T2 = T1 \cdot \overline{\text{PSD}}$ for the lower and higher energies, respectively. The PSD threshold was set to retain from $\approx 70\%$ to $\approx 40\%$ of inelastic interactions at beam momenta from $19A$ to $150A \text{ GeV}/c$, respectively. The statistics of recorded events are summarised in Tab. 1.

Table 1: Basic beam properties and number of events recorded and used in the analysis for ${}^7\text{Be}+{}^9\text{Be}$ interactions of 5 % most *central* collisions at incident momenta of 19A, 30A, 40A, 75A and 150A GeV/c.

p_{beam} (A GeV/c)	$\sqrt{s_{NN}}$ (GeV)	Recorded event triggers	Number of events after quality cuts
19	6.1	$3.46 \cdot 10^6$	$0.33 \cdot 10^5$
30	7.6	$5.41 \cdot 10^6$	$0.37 \cdot 10^5$
40	8.8	$3.42 \cdot 10^6$	$0.99 \cdot 10^5$
75	11.9	$5.24 \cdot 10^6$	$1.00 \cdot 10^5$
150	16.8	$2.93 \cdot 10^6$	$0.81 \cdot 10^5$

3 Analysis procedure

This section starts with a brief overview of the data analysis procedure and the applied corrections. It also defines to which class of particles the final results correspond. A description of the calibration and the track and vertex reconstruction procedure can be found in Ref. [12].

The analysis procedure consists of the following steps:

- (i) application of event and track selection criteria,
- (ii) determination of spectra of negatively charged hadrons using the selected events and tracks,
- (iii) evaluation of corrections to the spectra based on experimental data and simulations,
- (iv) calculation of the corrected spectra and mean multiplicities,
- (v) calculation of statistical and systematic uncertainties.

Corrections for the following biases were evaluated:

- (i) contribution from off-target interactions,
- (ii) bias of selection procedure of *central* collisions,
- (iii) geometrical acceptance,
- (iv) contribution of particles other than *primary* (see below) negatively charged pions produced in Be+Be interactions,
- (v) losses of produced negatively charged pions due to their decays and secondary interactions.

Correction (i) was not applied due to insufficient statistics of the target removed data. The contamination of the target inserted data was estimated from the z distribution of fitted vertices (see Fig. 8) and found to be very small ($\approx 0.35\%$) for the selected *central* interactions. Correction (ii) was estimated to be small and was therefore included in the systematic uncertainty (see Sec. 3.1). Corrections (iii)-(v) were estimated by simulations, see Sec. 3.3 below.

The final results refer to π^- produced in *central* Be+Be collisions by strong interaction processes and in electromagnetic decays of produced hadrons. Such hadrons are referred to as *primary* hadrons. The definition and the selection procedure of *central* collisions is given in Sec. 3.1.

The analysis was performed independently in (y, p_T) bins. The bin sizes were selected taking into account the statistical uncertainties and the resolution of the momentum reconstruction [12]. Corrections as well as statistical and systematic uncertainties were calculated for each bin.

3.1 *Central collisions*

The term *centrality* of the collision is related in the simplest models to the impact parameter b or the number of wounded nucleons W . Neither quantity is experimentally measurable and one uses instead the number N of produced particles or the energy emitted into the forward spectator region to characterise the *centrality* of the collision. The first choice may bias the measurements of particle production probabilities whereas such a bias is avoided by the second choice. Therefore final results presented in this paper refer to the 5% of Be+Be collisions with the lowest value of the forward energy E_F (*central collisions*). The quantity E_F is defined as the total energy in the laboratory system of all particles produced in a Be+Be collision via strong and electromagnetic processes in the forward momentum region defined by the acceptance map in Ref. [21]. Results on *central* collisions defined as above allow a precise comparison with predictions of models without any additional information about the NA61/SHINE setup and used magnetic field. Using this definition the mean number of wounded nucleons $\langle W \rangle$ and the mean collision impact parameter $\langle b \rangle$ were calculated within the Wounded Nucleon Model [22] implemented in EPOS, see Sec. 3.1.3.

Negatively charged pion production was studied in event ensembles the centrality of which was selected by upper limits of the energy E_{PSD} measured by a subset of PSD modules. This subset was optimised for best sensitivity to projectile spectators (see Sec. 3.1.1 for details). For each collision energy the upper limit value was adjusted to select 5% of all inelastic interactions. The forward momentum acceptance in the definition of E_F corresponds to the acceptance of the optimised subset of PSD modules. Based on simulations the results for the E_{PSD} selected collisions were corrected to correspond to the E_F selected results.

The details of the described procedures are given below.

3.1.1 Event selection based on the PSD energy

In order to optimize the sensitivity to projectile spectators, only a subset of PSD modules was included in the calculation of E_{PSD} [23]. Figure 5 (*top*) shows the impact points of projectile spectator nucleons on the front face of the PSD obtained from the internal Glauber model of EPOS [24] including Fermi motion. Figure 5 (*bottom*) depicts the modules selected for the summation of E_{PSD} . Online event selection by the hardware trigger (T2) used a threshold on the sum of energies over the 16 central modules of the PSD.

Measured distributions of E_{PSD} for minimum-bias and T2 trigger selected events, calculated in the offline analysis, are shown in Fig. 6 at beam momenta of 19A GeV/c and 150A GeV/c, respectively. Also drawn are vertical lines which define the E_{PSD} corresponding to the 5% and 20% of events with the lowest E_{PSD} values. A minimum-bias distribution was obtained using the data from the beam trigger T1 with offline selection of events by requiring an event vertex in the target region and a cut on the ionisation energy detected in the GTPC to exclude Be beams. A properly normalized spectrum for target removed events was subtracted.

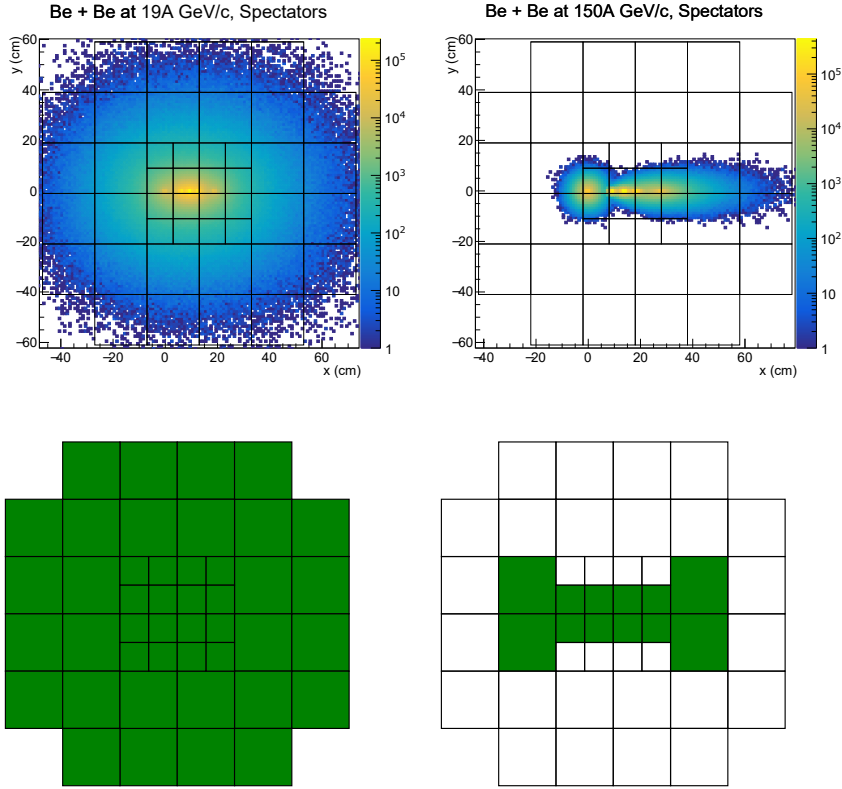


Figure 5: *Upper row*: Simulated impact points of particles on the front face of the PSD for beam momentum of 19A GeV/c (*left*) and 150A GeV/c (*right*). *Lower row*: PSD modules included in the calculation of the projectile spectator energy E_{PSD} used for event selection for beam momenta of 19A, and 30A GeV/c (*left*) and for 40A, 75A and 150A GeV/c (*right*)

3.1.2 Scaling to E_F selected results

Comparison of presented experimental results with other data require a realistic implementation of described centrality selection. This is more easily realized using a quantity "forward energy" (E_F) instead of E_{PSD} , since the latter requires detailed knowledge of its response. The acceptance map provided in Ref. [21] gives the recipe for the computation of E_F . Both E_F and E_{PSD} were calculated in simulations using the EPOS model, which employed a dedicated software package which tracks particles through the magnetic fields and simulates the response of the PSD modules. A global factor c_{cent} was then calculated as the ratio of mean multiplicities of negatively charged pions obtained with the two selection procedures in the 5% most *central* events. A possible dependence of the scaling factor on rapidity and transverse momentum was neglected. The resulting factors c_{cent} range between 1.00 and 1.03 corresponding to only a small correction compared to the systematic uncertainties of the measured π^- multiplicities. The correction was therefore not applied but instead included as a contribution to the systematic uncertainties.

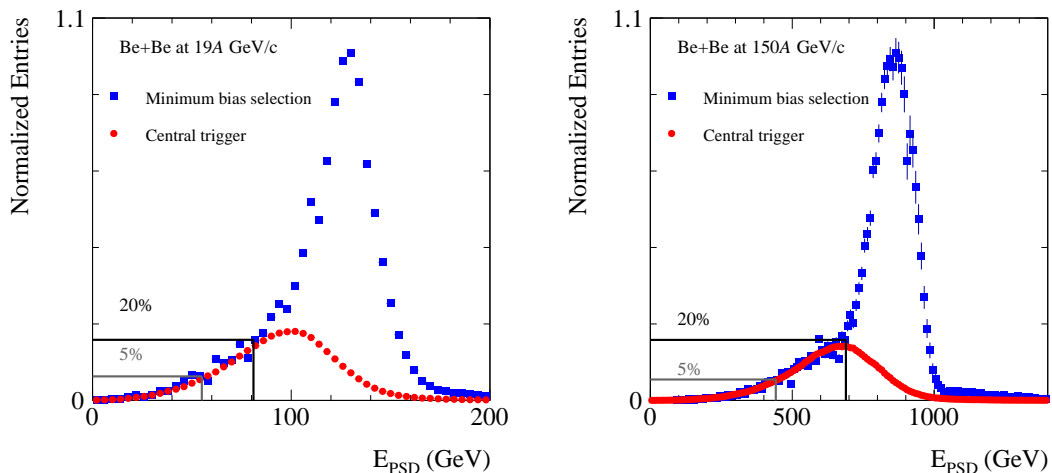


Figure 6: Two examples of the measured E_{PSD} distribution for minimum-bias selected (blue data points) and T2 selected (red data points) events at $19A$ GeV/c (*left*) and $150A$ GeV/c (*right*) beam momentum. Histograms are normalized to agree in the overlap region. The limits used to select events are shown by black lines and they correspond to $\approx 5\%$ and $\approx 20\%$ of inelastic collisions.

3.1.3 Mean number of wounded nucleons and collision impact parameter

Comparisons of particle yields in collisions of different size nuclei usually employs the average number of wounded nucleons $\langle W \rangle$ in the respective reactions. For estimating the average number of wounded nucleons corresponding to the selected *central* collisions EPOS 1.99 (version CRMC 1.5.3) [25] was employed which uses the Glauber model and a parton ladder mechanism to generate the interactions. EPOS was modified [24] to provide the values of W of its internal Glauber model calculation. The results on $\langle W \rangle$ for the 5% most *central* collisions from the EPOS model are listed in Table 2. Fluctuations of the listed values are due to the integer nature of W . As EPOS simulates all particles of the final state a more realistic estimate of $\langle W \rangle$ is obtained by selecting *central* collisions based on the energy E_F . The resulting mean number of wounded nucleons and the mean impact parameter are also listed in Table 2. Values of $\langle W \rangle$ for the two selection procedures differ by about two units. Examples of the distributions of W and b for the 5% most *central* collisions are shown in Fig. 7. As the nucleon density is low in the Be nucleus these distributions are quite broad. This emphasises that for model comparisons it is important to use equivalent *centrality* selection procedures for a meaningful comparison.

3.2 Event and track selection

3.2.1 Event selection

For the analysis Be+Be events were selected using the following criteria:

- (i) four units of charge measured in S1, S2, and Z counters as well as BPD3 (this requirement also rejects most interactions upstream of the Be target),

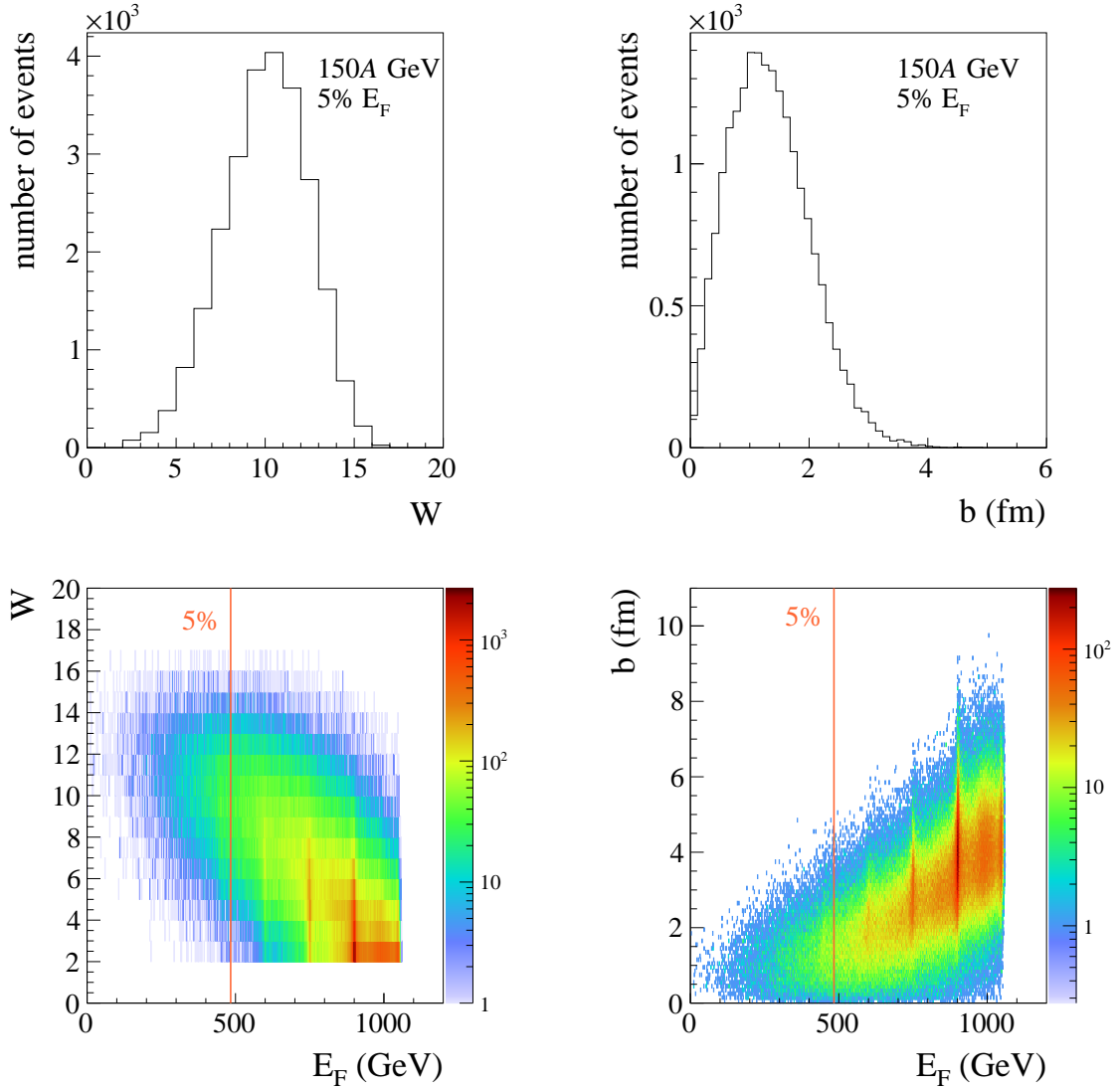


Figure 7: Examples of the distribution of the number of wounded nucleons W (*top, left*) and impact parameter b (*top, right*) for events with the 5% smallest forward energies E_F and E_F versus W (*bottom, left*) and E_F versus b (*bottom, right*) at beam momentum of $150A$ GeV/ c simulated with EPOS using the acceptance map provided in Ref. [21].

- (ii) no off-time beam particle detected within a time window of $\pm 4.5 \mu\text{s}$ around the trigger particle,
- (iii) no other event trigger detected within a time window of $\pm 25 \mu\text{s}$ around the trigger particle,
- (iv) beam particle trajectory measured in at least three planes out of four of BPD-1 and BPD-2 and in both planes of BPD-3,
- (v) charge measured in the GTPC smaller than that of Be (applied at $40A$, $75A$ and $150A$ GeV/ c),
- (vi) a well reconstructed interaction vertex with z position (fitted using the beam trajectory and TPC tracks) not farther away than 15 cm from the center of the Be target (see Fig 8; the

Momentum (A GeV/ c)		19	30	40	75	150
EPOS WNM	$\langle W \rangle$	11.8	11.8	11.8	11.8	11.8
	σ	1.0	1.0	1.0	1.0	1.0
EPOS E_F	$\langle W \rangle$	9.54	9.44	9.67	9.61	9.51
	σ	2.4	2.4	2.3	2.4	2.4
	$\langle b \rangle$	1.44	1.54	1.32	1.26	1.32
	σ	0.7	0.8	0.7	0.6	0.7

Table 2: Average number of wounded nucleons $\langle W \rangle$ and average impact parameter $\langle b \rangle$ in the 5% most *central* Be+Be collisions estimated from simulations using the EPOS [25] model. The values of σ denote the widths of the distributions of W and b . Results EPOS WNM are for *centrality* selection using the smallest number of spectators, EPOS E_F using the forward energy E_F within the acceptance map in Ref. [21]

cut removes less than 0.4% of *central* interactions),

- (vii) the energy E_{PSD} measured in the subset of the PSD modules smaller than an upper limit (55, 73, 104, 165, 442 GeV for collisions at 19A, 20A, 30A, 40A, 75A and 150A GeV/ c , respectively) in order to select the 5% most *central* collisions (see discussion in Sec. 3.1).

The event statistics after applying the selection criteria are summarized in Table 1.

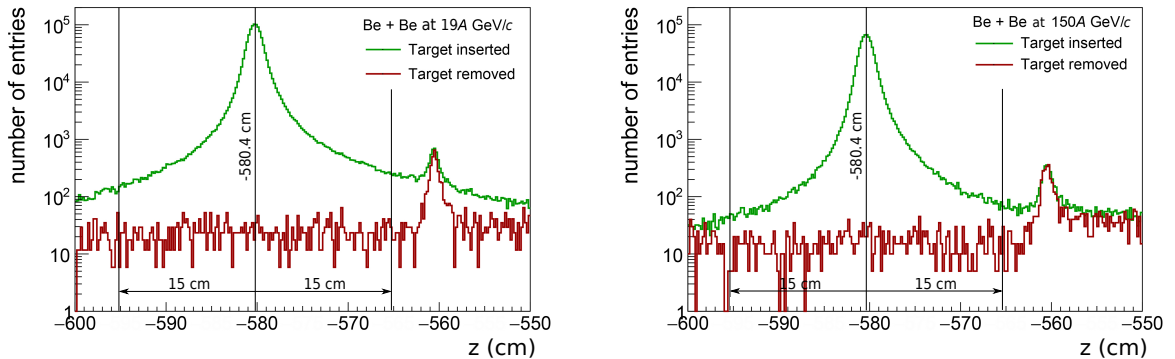


Figure 8: Distribution of fitted vertex z coordinate for the 20% most *central* ${}^7\text{Be}+{}^9\text{Be}$ interactions with target inserted (green histogram) and target removed (red histogram). (*Left*): 19A GeV/ c . (*Right*): 150A GeV/ c . Target position and cut values are marked. Target is installed in the box filled with He gas to minimise background interactions. Smaller peak on the right hand side of the plots corresponds to interactions with a target holder window.

3.2.2 Track selection

In order to select tracks of primary charged hadrons and to reduce the contamination of tracks from secondary interactions, weak decays and off-time interactions, the following track selection criteria were applied:

- (i) track momentum fit at the interaction vertex should have converged,

- (ii) fitted x component of particle rigidity at the vertex ($p_{\text{lab},x}/q$) is positive. This selection minimizes the angle between the track trajectory and the TPC pad direction for the given magnetic field direction, reducing uncertainties of the reconstructed cluster position, energy deposition and track parameters,
- (iii) total number of reconstructed points on the track should be greater than 15,
- (iv) sum of the number of reconstructed points in VTPC-1 and VTPC-2 should be greater than 15 or greater than 4 in the GTPC,
- (v) the distance between the track extrapolated to the interaction plane and the interaction point (track impact parameter) should be smaller than 4 cm in the horizontal (bending) plane and 2 cm in the vertical (drift) plane,
- (vi) electron tracks were excluded by a cut on the measured particle energy loss dE/dx in the TPCs.

3.3 Corrections

In order to determine the mean multiplicity of *primary* π^- mesons produced in *central* Be+Be collisions a set of corrections was applied to the extracted raw results. The main effects are detector acceptance, loss of events due to the cut on reconstructed vertex position, reconstruction efficiency, contributions of particles from weak decays (feed-down), and contribution of *primary* hadrons other than negatively charged pions (mostly K^- mesons). The contamination of events occurring outside the target was negligible.

A simulation of the NA61/SHINE detector is used to correct the data for acceptance, reconstruction efficiency and contamination. Only Be+Be interactions in the target material were simulated and reconstructed. The EPOS model [25, 24] was selected to generate the primary interactions as it best describes the NA61/SHINE measurements. A GEANT3 based program chain was used to track particles through the spectrometer, generate decays and secondary interactions and simulate the detector response (for more detail see Ref. [12]). Simulated events were then reconstructed using the NA61/SHINE reconstruction chain and reconstructed tracks were matched to the simulated particles based on the cluster positions. The same event selection procedure was used as for data (cut on the summed energy in the subset of PSD modules used to select the 5% most *central* collisions). Particles which were not produced in the primary interaction can amount to a significant fraction of the selected track sample. Thus a careful effort was undertaken to evaluate and subtract this contribution.

The correction factor c_{yp_T} for primary π^- , based on the event and detector simulation was calculated for each y and p_T bin as:

$$c_{yp_T} = n[\pi^-]_{\text{gen}}^{\text{MC}} / n[h^-]_{\text{sel}}^{\text{MC}} \quad (1)$$

where $n[h^-]_{\text{sel}}^{\text{MC}}$ is the mean multiplicity of reconstructed negatively charged particles after the event and track selection criteria and $n[\pi^-]_{\text{gen}}^{\text{MC}}$ is the mean multiplicity of *primary* negatively charged pions from the E_{PSD} -selected Be+Be collisions generated by the EPOS model.

The corrected multiplicities were then calculated as:

$$n[\pi^-]^{corr} = c_{yp_T} \cdot n[\pi^-]^{raw} \quad (2)$$

The final results in bins of y and p_T are shown in Fig. 9.

3.4 Statistical uncertainties

Statistical uncertainties of the yields receive contributions from the finite statistics of both the data and the simulated events used to obtain the correction factors. The dominating contribution is the uncertainty of the data which were calculated assuming a Poisson probability distribution for the number of entries in a bin. Compared to the statistics of the data the statistics of the simulation were much higher and the statistical uncertainties of the latter were neglected.

3.5 Systematic uncertainties

Systematic uncertainties presented in this paper were calculated taking into account contributions from the following effects.

- (i) Possible biases due to track cuts which are not corrected for. These are:
 - (a) a possible bias due to the dE/dx cut applied to remove electrons,
 - (b) a possible bias related to the removal of events with off-time beam particles close in time to the trigger particle.

Their magnitude was estimated by varying the values of the corresponding cut for data selection. The possible bias due to the dE/dx cut was changed by ± 0.01 dE/dx units (where 1 corresponds to a minimum ionising particle, and 0.04 is a typical width of the dE/dx distribution for π^-), and the off-time interactions cut was varied from a ± 3.5 μs to a ± 5.5 μs time window. The assigned systematic uncertainty was calculated as the maximum of the absolute differences between the results obtained for lower and upper values. The estimated bias is on the level of 1-3%.

This uncertainty is listed in the tables including numerical values and it is visualised by a shaded band around the data points in plots presenting the results. Systematic biases in different bins are correlated, whereas statistical fluctuations are almost independent.

- (ii) Uncertainty related to the track cuts which were corrected for. It was estimated by varying the track selection cuts used for data and Monte Carlo events: removing the impact parameter cut and decreasing the minimum number of required points to 12 (total) and 10 (in VTPCs). The potential bias is below 2%.
- (iii) Uncertainty of the correction for contamination of the primary π^- mesons. There was no data available to adjust the simulated spectra. To estimate a possible bias the simulated spectra were instead adjusted to preliminary NA61/SHINE data on the K^-/π^- ratio [26], and the difference between the results with adjusted and standard correction of order 2% was assigned as relative potential systematic uncertainty. Since K^- are the main contribution to

the h^- correction and the absolute correction is small, this contribution was finally neglected in the systematic uncertainty estimate.

The total systematic uncertainty was calculated by adding in quadrature the contributions (i) - (iii):

$$\sigma_{\text{sys}} = \sqrt{\sigma_{\text{i}}^2 + \sigma_{\text{ii}}^2 + \sigma_{\text{iii}}^2}. \quad (3)$$

This uncertainty is listed in the tables including numerical values and it is visualised by a shaded band around the data points in plots presenting the results. Systematic biases in different bins are correlated, whereas statistical fluctuations are almost independent.

4 Experimental results

This section presents results on negatively charged pion spectra at 19A, 30A, 40A, 75A and 150A GeV/c beam momentum in the 5% most *central* ${}^7\text{Be}+{}^9\text{Be}$ collisions (see Sec. 3.1 for definition of *central* collisions). The results refer to primary pions produced by strong interaction and decay processes and in electromagnetic decays of neutral hadrons.

4.1 Double-differential (y, p_T) and ($y, m_T - m_\pi$) yields

Figure 9 shows fully corrected double-differential (y, p_T) distributions $\frac{d^2n}{dydp_T}$ of π^- measured in Be+Be interactions and illustrates the wide phase space acceptance of the detector. Rapidity bins with limited acceptance ($y < -0.6$ for 19A GeV, $y < -0.8$ for 30A GeV, $y < -0.8$ for 40A GeV, $y < -1.2$ for 75A GeV and $y < -1.4$ for 150A GeV/c) are not used in the subsequent analysis. for

4.2 Transverse momentum and transverse mass spectra

Spectra of transverse momentum p_T in slices of rapidity y are plotted in Fig. 10. Superimposed curves show the results obtained from fitting the function

$$f(p_T) = C \cdot p_T \cdot \exp\left(\frac{-\sqrt{(cp_T)^2 + m^2}}{T}\right), \quad (4)$$

motivated by the thermal model, where the inverse slope parameter T and the normalisation constant C are the fit parameters.

A summary of the fitted values of the inverse slope parameter T are shown in Fig. 11 plotted versus rapidity divided by beam rapidity. The decrease of T towards larger rapidities and the obtained values are close to those found for inelastic $p+p$ interactions [12]. Numerical values of T at $y \approx 0$ are given in Table 3.

Spectra of transverse mass $m_T - m_\pi$ at mid-rapidity ($0 < y < 0.2$) are shown in Fig. 12 for the 5% most *central* Be+Be collisions and for inelastic $p+p$ interactions [12] as well as central Pb+Pb collisions [2, 3]. The $p+p$ data follow exponential distributions as shown by the lines fitted in

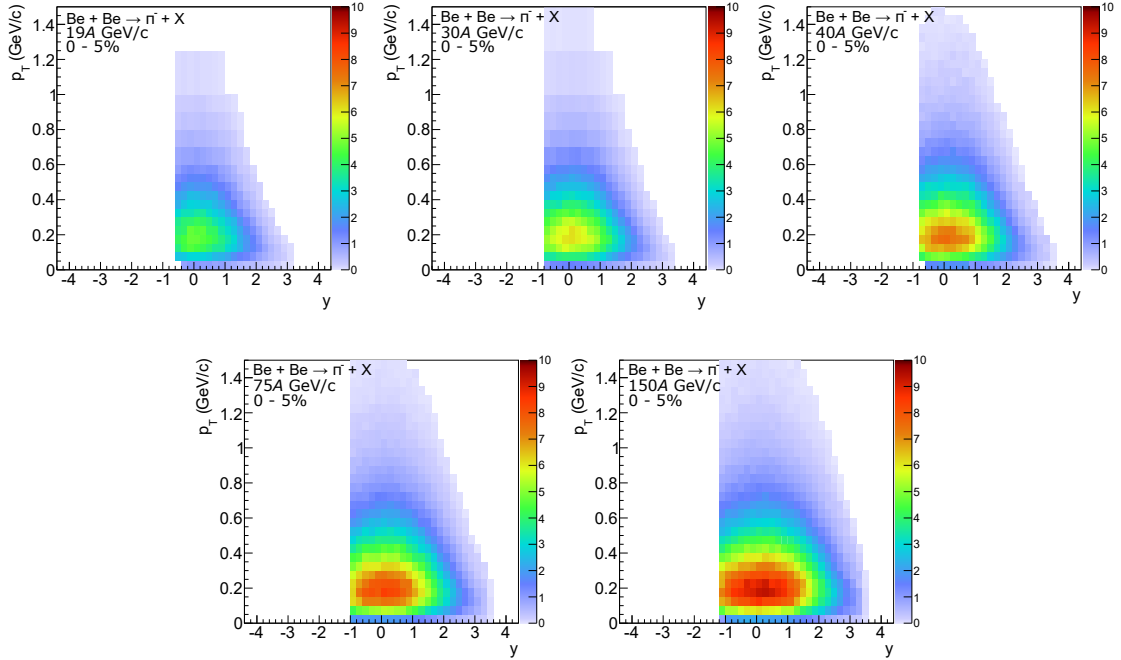


Figure 9: Double-differential spectra $\frac{d^2n}{dydp_T}$ of negatively charged pions produced in the 5% most *central* Be+Be collisions at beam momenta of 19A, 30A, 40A, 75A and 150A GeV/c.

Table 3: Inverse slope parameter T near mid-rapidity fitted in the interval $0.2 < m_T - m_\pi < 0.7$ GeV and mid-rapidity yield dn/dy of π^- mesons in the 5% most *central* Be+Be collisions. For comparison inverse slope parameter T_{p+p} near mid-rapidity fitted in the same interval of π^- mesons in the $p+p$ interactions at close beam momenta [12].

p_{beam} (A GeV/c)	T (MeV)	$dn/dy_{(y=0)}$	T_{p+p} (MeV)
19	$150 \pm 1 \pm 6$	$2.00 \pm 0.06 \pm 0.12$	$149.1 \pm 5.0 \pm 4.8$
30	$158 \pm 1 \pm 7$	$2.57 \pm 0.08 \pm 0.16$	$153.3 \pm 2.2 \pm 1.2$
40	$160 \pm 1 \pm 6$	$3.02 \pm 0.09 \pm 0.19$	$157.7 \pm 1.7 \pm 2.1$
75	$163 \pm 1 \pm 8$	$3.44 \pm 0.10 \pm 0.21$	$159.9 \pm 1.5 \pm 4.1$
150	$167 \pm 1 \pm 8$	$3.80 \pm 0.10 \pm 0.23$	$159.3 \pm 1.3 \pm 2.6$

the range $0.24 < m_T - m_{\pi^-} < 0.72$ using Eq. 4 expressed in m_T . Interestingly, nucleus-nucleus interactions show enhancements at low and high transverse mass. To compare in more detail the transverse mass spectra between systems, each spectrum was normalized to the integral of the spectrum in the range of $0.24 < m_T - m_{\pi^-} < 0.72$. The normalized Be+Be spectra were then divided by the corresponding $p+p$ and Pb+Pb spectra used as a reference. The resulting ratios of the normalised spectra are presented in Fig. 13.

The shape of m_T spectra in *central* Be+Be collisions is significantly different from the one observed in inelastic $p+p$ interactions (Fig. 13 *left*). However, it is important to note that the Be+Be system is isospin symmetric whereas $p+p$ has $I_3 = 1$. Comparing Be+Be to Pb+Pb (Fig. 13 *right*) reveals that both shapes are similar with a relative inclination in favor of the pion yield

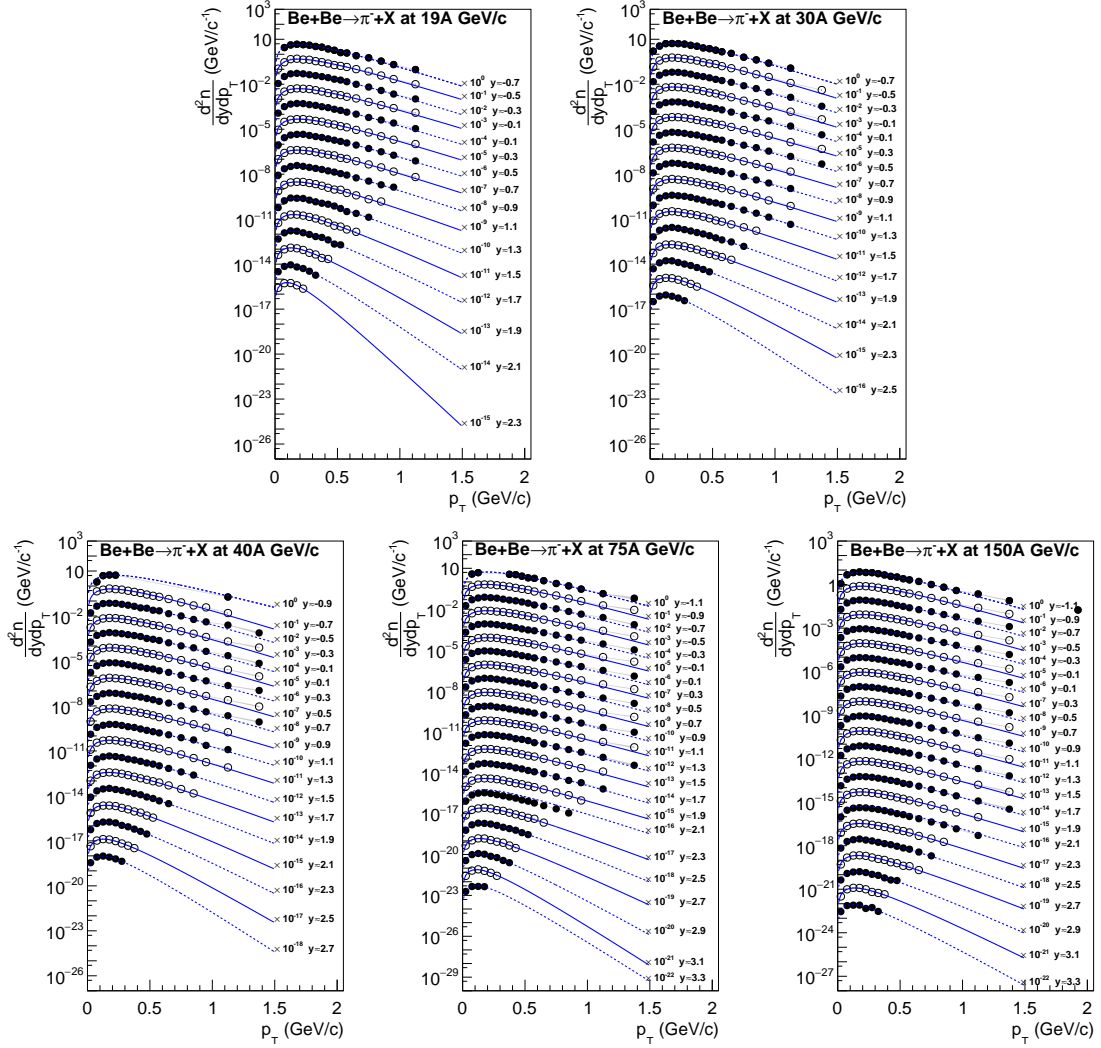


Figure 10: Transverse momentum spectra of π^- in rapidity slices produced in the 5% most *central* Be+Be collisions. Rapidity values given in the legends correspond to the middle of the corresponding interval. Data points for consecutive rapidity slices are scaled down by factors of 10. Shaded bands show systematic uncertainties. Curves depict thermal model motivated fits with Eq. 4.

at low m_T . Note that Pb+Pb is to a large extent isospin neutral. The quantitative comparison between Be+Be and Pb+Pb data are limited by large statistical uncertainties of the latter.

4.3 Rapidity spectra and mean multiplicities

To extract one-dimensional rapidity spectra from the two-dimensional y - p_T spectra the contribution from the missing high p_T acceptance has to be accounted for. The transverse momentum spectrum for each rapidity bin was parametrized with Eq. 4. An additional constraint was added to the fit to ensure that the integral of the fitted function agrees with the integral (sum) of the measurements

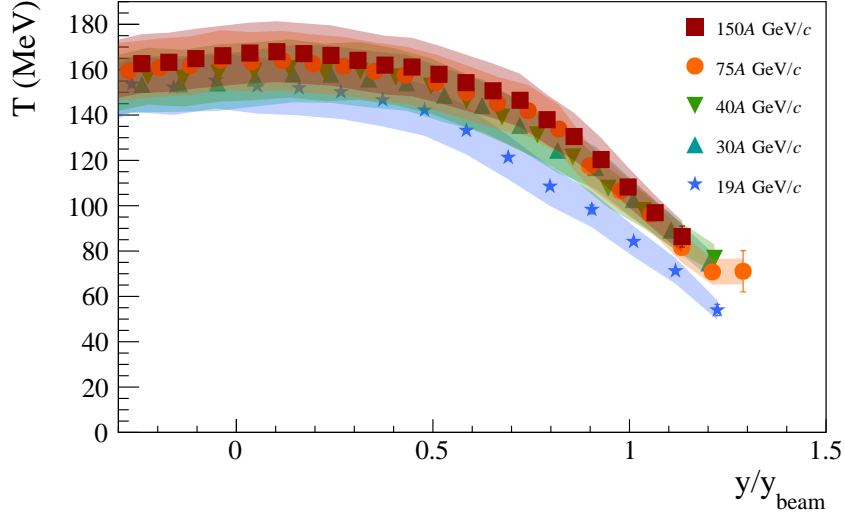


Figure 11: The inverse slope parameter T of the transverse mass spectra of negatively charged pions in *central* Be+Be collisions at the SPS energies as a function of rapidity divided by the beam rapidity. The fit range is $0.2 < m_T - m_\pi < 0.7$ GeV. Statistical uncertainties are mostly smaller than marker size, systematic uncertainties are indicated by shaded bands.

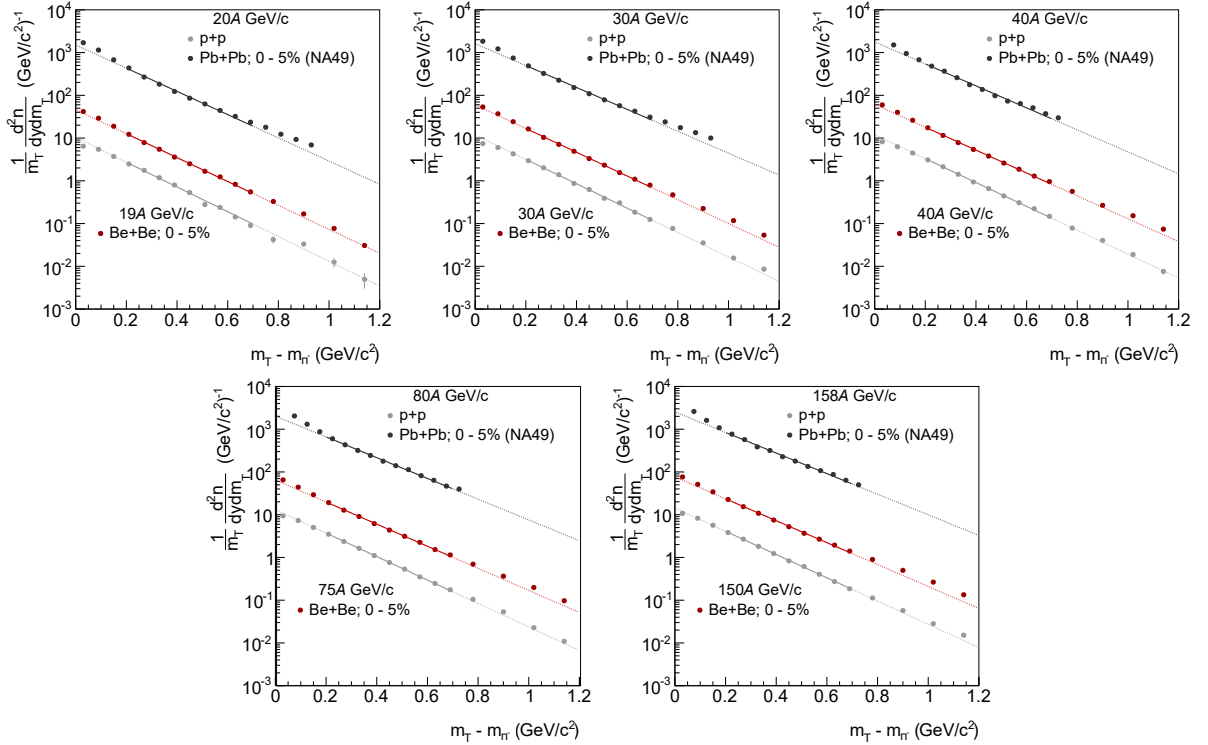


Figure 12: Transverse mass spectra $\frac{1}{m_T} \frac{d^2n}{dy dm_T}$ of negatively charged pions produced in *central* Be+Be collisions at the SPS energies. Statistical errors are smaller than the size of the points. Results from inelastic $p+p$ interactions [12] and central Pb+Pb interactions [2, 3] are shown for comparison. Lines show exponential fits with Eq. 4.

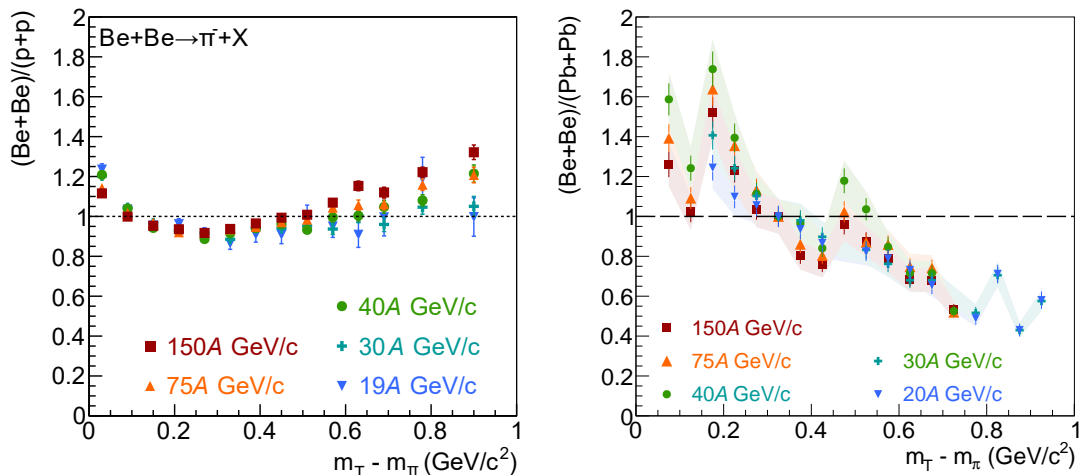


Figure 13: Ratio of normalized transverse mass spectra: Be+Be/ $p+p$ (left) and Be+Be/Pb+Pb (right) at the SPS energies.

over the interval where data are available. The p_T extrapolation increases the value of the summed measurements by $\approx 0.1\%$. Only for $y > 3$ the extrapolation effect rises to around 1%.

The rapidity spectra are plotted in Fig. 14. A closer look reveals an asymmetry of the spectra with respect to mid-rapidity. To quantify the amount of asymmetry the spectra were parametrized with the sum of two Gaussian functions with the same width and mean value displaced from mid-rapidity by the same amount:

$$g(y) = \frac{A \cdot A_{\text{rel}}}{\sigma\sqrt{2\pi}} \exp\left(-\frac{(y - y_0)^2}{2\sigma^2}\right) + \frac{A_0}{\sigma\sqrt{2\pi}} \exp\left(-\frac{(y + y_0)^2}{2\sigma^2}\right), \quad (5)$$

where A is the normalization parameter, A_{rel} is the relative amplitude of the Gaussian distributions, σ is the common width and y_0 is the displacement from mid-rapidity. Results for the fitted functions are presented in Fig. 14. Numerical values of the fitted parameters A_{rel} , y_0 as well as the RMS width σ_y of the rapidity distribution calculated from

$$\sigma_y = \sqrt{\sigma^2 + y_0^2} \quad (6)$$

are listed in Table 4.

The relative amplitude of the Gaussian distributions decreases slowly with increasing beam momentum, i.e the asymmetry increases. This deviation of A_{rel} from unity signals a forward-backward asymmetry of the rapidity distribution which may be explained by the asymmetry of the collision system and the event selection procedure:

- (i) Asymmetric collisions of a ${}^7\text{Be}$ beam with a larger mass ${}^9\text{Be}$ target may lead to enhanced particle production at backward rapidity,
- (ii) a larger number of neutrons in the ${}^9\text{Be}$ target nuclei might result in a difference in the ratio of π^- to π^+ in the backward and forward rapidity regions,

Momentum (A GeV/ c)	19	30	40	75	150
A_{rel}	0.975	0.919	0.858	0.828	0.837
$\delta(A_{\text{rel}})$	0.0319	0.0172	0.0172	0.0100	0.0076
y_0	0.659	0.667	0.720	0.778	0.891
$\delta(y_0)$	0.0032	0.0065	0.0078	0.0062	0.0047
σ_y	1.025	1.067	1.148	1.265	1.385
$\delta(\sigma_y)$	0.048	0.052	0.061	0.059	0.057

Table 4: Fitted parameters A_{rel} , y_0 of the double Gaussian fit and RMS width σ_y of the rapidity distribution calculated from Eq. 6.

Momentum (A GeV/ c)	19	30	40	75	150
$\langle \pi^- \rangle$	5.33	7.61	8.75	11.98	14.32
$\delta_{\text{stat}}(\langle \pi^- \rangle)$	± 0.11	± 0.08	± 0.09	± 0.07	± 0.09
$\delta_{\text{sys}}(\langle \pi^- \rangle)$	± 0.63	± 0.90	± 0.95	± 1.20	± 1.37
$\langle \pi^- \rangle / \langle W \rangle$	1.66	2.39	2.69	3.70	4.48

Table 5: Mean π^- multiplicities in the 5% most *central* Be+Be collisions with statistical and systematic uncertainties as well as ratios of mean π^- multiplicities to average number of wounded nucleons.

(iii) selection of *central* collisions by requiring the forward energy E_F below a cut value.

The asymmetry was studied using the Wounded Nucleon Model (WNM) [22], where production of particles in the backward hemisphere is proportional to the number of wounded nucleons in the target and production of particles in the forward hemisphere is proportional to the number of wounded nucleons in the projectile. In the WNM the effect of the asymmetric system leads to a small enhancement of the particle yield below mid-rapidity, which is opposite to what is seen in the data. On the other hand, the effect of the *centrality* selection based only on the forward energy is enhancing particle production at forward rapidity. The data show that the latter effect dominates.

Rapidity spectra in *central* Be+Be collisions are compared to results from inelastic $p+p$ interactions [12] in Fig. 15. Mean negative pion multiplicities $\langle \pi^- \rangle$ were obtained by summing the measured data points and adding a contribution from the fitted function Eq. 5 for the unmeasured region. Half of the contribution added based on the fit is added to systematic uncertainty. The results are listed in Table 5.

The widths of the rapidity distributions were calculated from Eq.6 and are listed in Table 4. The beam energy dependence of the width of the rapidity distribution divided by the beam rapidity σ_y/y_{beam} is presented in Fig. 16. For Be+Be and Pb+Pb interactions the ratio was calculated for π^- mesons. Since the $p+p$ collision system is not isospin symmetric the isospin average $(\pi^- + \pi^+)/2$ was plotted for comparison. These results are referred to as results for nucleon-nucleon ($N+N$) collisions [18]. For all system sizes the relative width decreases monotonically with beam energy and system size.

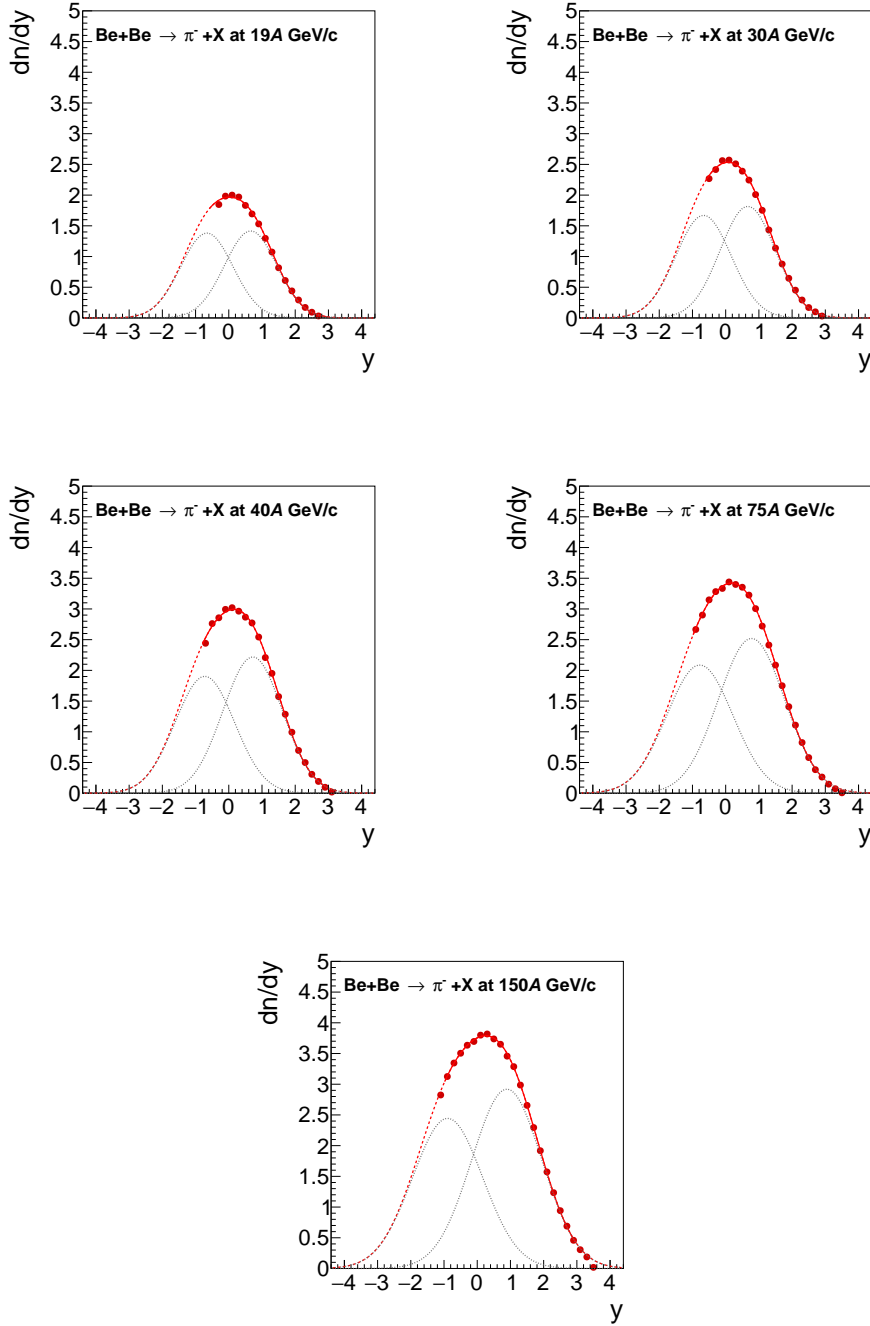


Figure 14: Rapidity distributions of negatively charged pions in *central* Be+Be collisions at the SPS energies. The parametrization of the spectra by Eq. 5 is shown. The solid line shows the fitted function in the range of the fit, and the red dashed line depicts the extrapolation of the fitted function. The two Gaussian functions constituting the fitted function are represented by the black dashed lines.

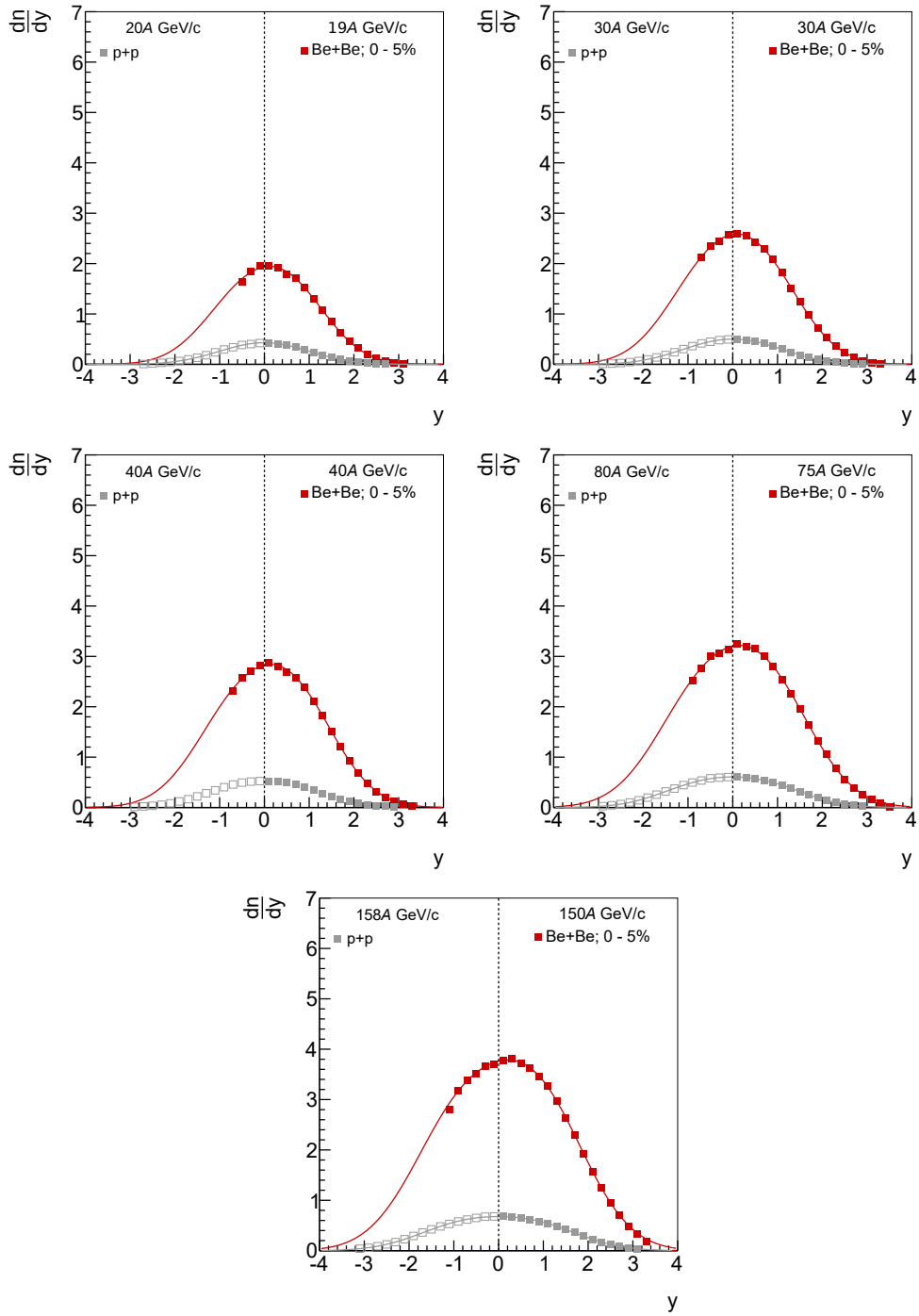


Figure 15: Rapidity spectra of π^- produced in the 5% most *central* Be+Be collisions at the SPS energies. Results from inelastic $p+p$ interactions [12] are shown for comparison. Statistical errors are smaller than the size of the markers.

5 Discussion

Several features of π meson production were predicted to be sensitive to the onset of deconfinement, namely the energy dependence of the transverse mass distribution, the width of the rapidity

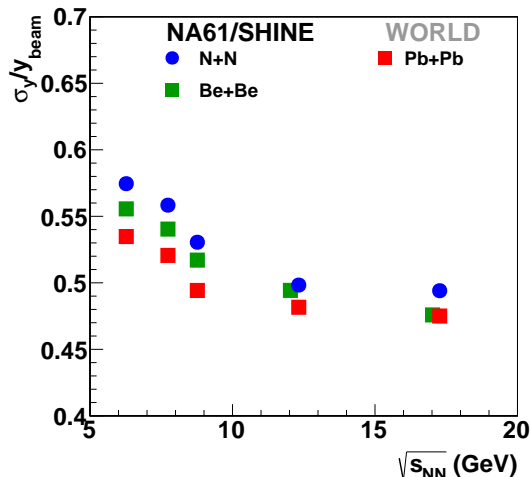


Figure 16: Collision energy dependence of the ratio of the width σ_y of the rapidity distribution to the beam rapidity y_{beam} for *central* Be+Be and Pb+Pb collisions and inelastic $N+N$ interactions.

distribution - both due to the softening of the equation of state [27, 28, 29] - and the mean multiplicity due to the increasing entropy during the transition from the hadronic to the partonic phase [30]. The data presented in this paper are discussed in the context of these predictions in the following.

In the collision energy range in which the mixed hadron and parton matter is created a stalling of the expansion of the system is expected [31]. This results in a slowing of the increase of radial flow of the produced particles and in a step-like structure in the energy dependence of the inverse slope parameter of the transverse mass spectra T [4]. This feature was clearly observed for K mesons in *central* Pb+Pb collisions and was interpreted as one of the indications of the onset of deconfinement [2, 3].

Pion transverse mass spectra deviate significantly from the exponential function Eq. 4 used to fit the inverse slope parameter. This is attributed to a large contribution of pions from resonance decays and possible effect of transverse collective flow [31]. Thus in order to avoid model-dependence of results π transverse mass spectra are characterized by the mean transverse mass $\langle m_T \rangle - m$. Figure 17 shows the "step" plot for π^- in *central* Be+Be collisions compared to *central* Pb+Pb interactions and inelastic $p+p$ reactions. The values and energy dependence measured in Be+Be collisions are surprisingly similar to those in inelastic $p+p$ interactions and there is only a small increase towards *central* Pb+Pb collisions. This suggests that the average transverse mass of π^- mesons is only weakly sensitive to the transverse flow and thus it is not a discriminating observable for the onset of deconfinement.

The Landau hydrodynamical model of high energy collisions [35, 36] predicts rapidity distributions of Gaussian shapes. In fact this prediction is approximately confirmed by the experimental data, see Ref. [37] and references therein. Moreover, the collision energy dependence of the width was derived by Shuryak [38] from the same model under simplifying assumptions and reads:

$$\sigma_y^2(\pi^-) = \frac{8}{3} \frac{c_s^2}{1 - c_s^4} \ln \left(\frac{\sqrt{s_{NN}}}{2m_p} \right), \quad (7)$$

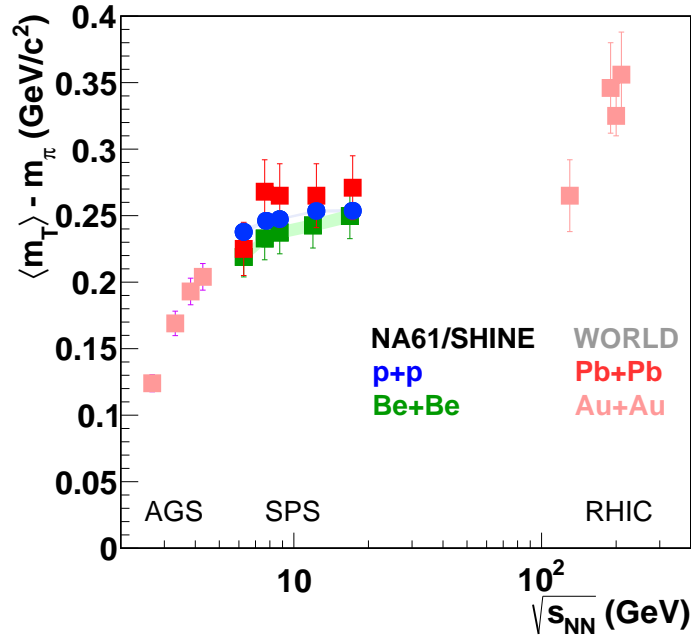


Figure 17: Energy dependence of the mean transverse mass of π^- measured at mid-rapidity in *central* Be+Be, Pb+Pb [2, 3] and Au+Au [32, 33] collisions and inelastic $p+p$ interactions [34].

where c_s denotes the speed of sound, and $c_s^2 = 1/3$ for an ideal gas of massless particles.

The above prediction is compared with the experimental data on the width σ_y of the rapidity distributions of π^- mesons produced in central nucleus-nucleus collisions and inelastic nucleon-nucleon interactions in Fig. 18 (*left*)¹. The model calculations are close to the measured dependence on the beam rapidity y_{beam} . However, linear increase with y_{beam} provides a better fit to the measurements as shown by the straight line fit. The deviations were attributed to the changes in the equation of state [39, 40], which can be effectively parametrised by allowing the speed of sound to be dependent on collision energy. Clearly the measured values of σ_y differ very little between the studied reactions in the SPS energy range.

By inverting Eq. 7 one can express c_s^2 in the medium as a function of the measured width of the rapidity distribution. The energy dependence of the sound velocities extracted from the data are presented in Fig. 18 (*right*). The energy range for results from Be+Be collisions and inelastic $p+p$ reactions is too limited and the fluctuations in the data too large to allow a significant conclusion about a possible minimum. Data on *central* Pb+Pb and Au+Au collisions cover a much wider energy range. Here the sound velocity exhibits a clear minimum (usually called the softest point) at $\sqrt{s_{NN}} \approx 10$ GeV consistent with the reported onset of deconfinement [2, 3].

Pions are the most copiously produced hadrons ($\approx 90\%$) in collisions of nucleons and nuclei at SPS energies. Their multiplicity is closely related to the entropy produced in such interactions [41]. Within the Fermi and Landau models the entropy is expected to increase as

$$S \sim F, \quad (8)$$

¹ For $p+p$ interactions the figure shows isospin symmetrised values denoted as $N+N$ [12]

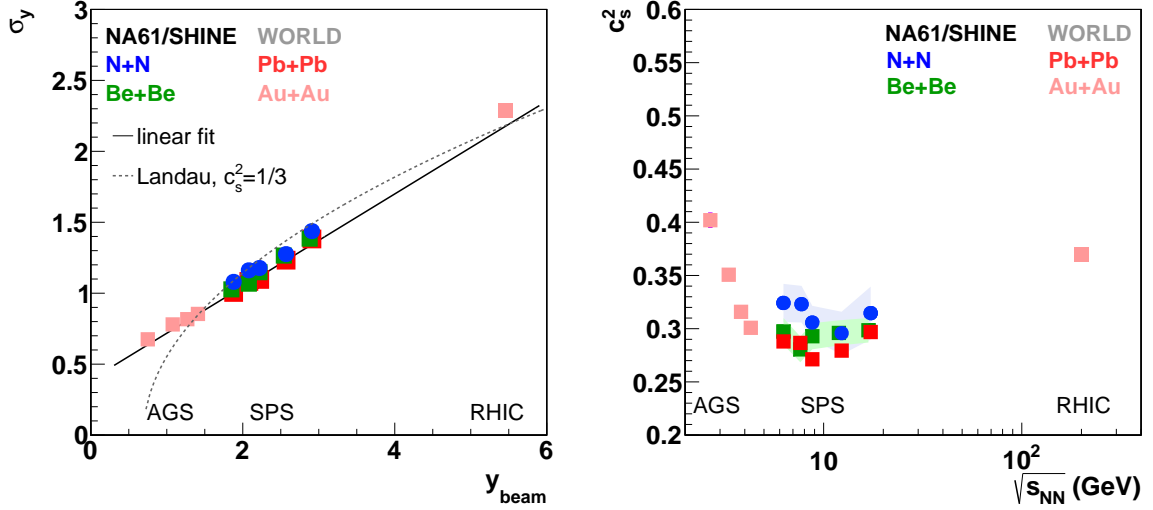


Figure 18: Comparison of the Landau hydrodynamical model with rapidity distributions of charged pions produced in central nucleus-nucleus collisions and inelastic nucleon-nucleon interactions. *Left:* The width σ_y of the rapidity distributions of negatively charged pions in *central* Be+Be, Pb+Pb [2, 3] (Au+Au [32, 33]) reactions and the width σ_y of the average of rapidity distributions of positively and negatively charged pions in $p+p$ [13, 34] (denoted as $N+N$) as a function of the beam rapidity y_{beam} . The dotted line indicates the Landau model prediction with $c_s^2 = 1/3$, while the full line shows a linear fit through the data points. *Right:* The speed of sound as a function of beam energy as extracted from the data using Eq. 7.

where the Fermi collision energy measure is defined as

$$F = \left[(\sqrt{s_{NN}} - 2m_N)^3 / \sqrt{s_{NN}} \right]^{1/4}. \quad (9)$$

Since the number of degrees of freedom g is higher for the quark-gluon plasma than for confined matter, it is also expected that the entropy density of the produced final state at given energy density should also be higher in the first case. The following simple relation describes the expected dependence [30]:

$$S/V \sim g^{1/4} F. \quad (10)$$

Therefore, the entropy and information regarding the state of matter formed in the early stage of a collision should be reflected in the number of produced pions normalized to the volume of the system. This intuitive argument was quantified in the Statistical Model of the Early Stage (SMES) [4]. The increase with collision energy of the mean number of produced pions $\langle \pi \rangle$, normalized to the number of wounded nucleons $\langle W \rangle$ [22] is expected to be linear when plotted against F . The rate of increase is related to the number of degrees of freedom as given by Eq. 10. This simple prediction is modified at low collision energies when absorption of pions in the hadronic matter is expected to significantly decrease the final pion yield [4].

Figure 19 displays the ratio of mean pion multiplicities² to the number of wounded nucleon as a function of F .

² The mean number of produced pions $\langle \pi \rangle$ is calculated as $\langle \pi \rangle = 3 \cdot \langle \pi^- \rangle$ for nucleus-nucleus collisions and $\langle \pi \rangle = 1.5 \cdot (\langle \pi^+ \rangle + \langle \pi^- \rangle)$ for $N+N$ interactions

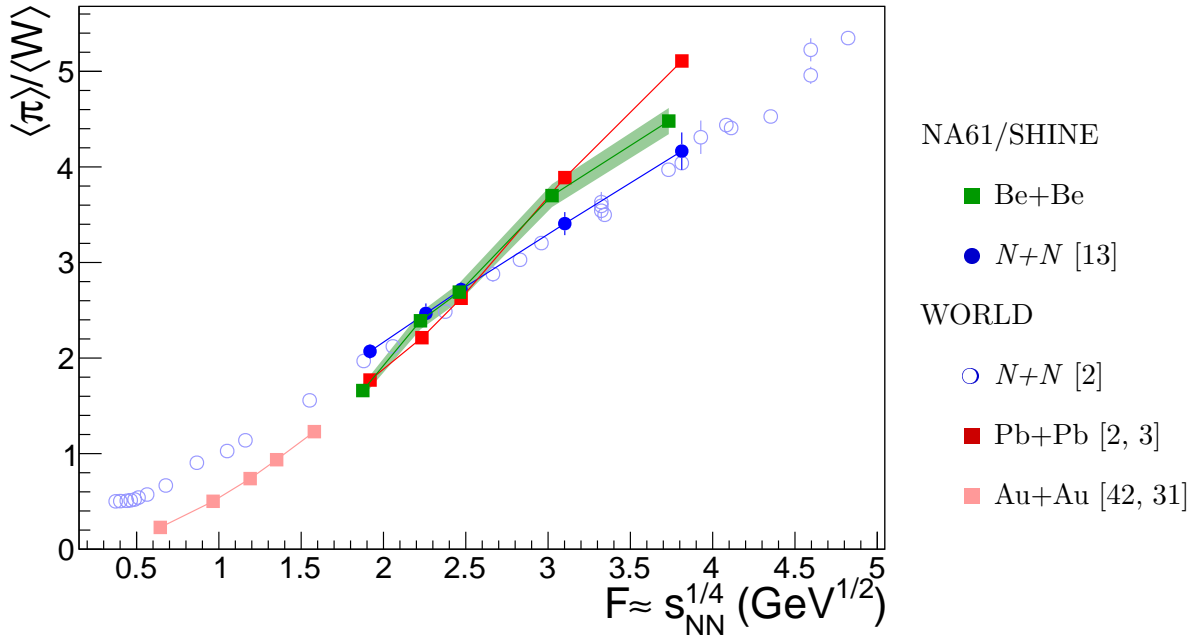


Figure 19: The "kink" plot showing the ratio of pion multiplicity $\langle\pi\rangle$ to number of wounded nucleons $\langle W\rangle$ versus the Fermi energy variable $F \approx s_{NN}^{1/4}$. Results from *central* Be+Be collisions are compared to measurements in for inelastic nucleon-nucleon reactions and *central* collisions of heavier nuclei. Results of Be+Be collisions are shown with statistical (vertical lines) and systematic (shaded band) uncertainties. All other results are presented with total uncertainty.

The new measurements of the $\langle\pi\rangle/\langle W\rangle$ ratio in *central* Be+Be collisions are compared to a compilation of results from central Pb+Pb (Au+Au) collisions and inelastic nucleon-nucleon interactions. Above $F \approx 2$ GeV $^{1/2}$ the slope of the Pb+Pb dependence is about a factor 1.3 higher than for nucleon-nucleon interactions. The ratio in *central* Be+Be collisions follows the ratio for central Pb+Pb collisions up to $F \approx 3$ GeV $^{1/2}$, whereas at the top collision energy the Be+Be ratio is close to the ratio for *N+N* interactions. Note, that W was derived using the EPOS model (see Sec. 3.1.3) and therefore depends on the details of the model. Using other models may lead to 5 - 10% differences. New results on Ar+Sc and Xe+La collisions from NA61/SHINE will be available soon and are expected to clarify the energy and system size dependence of $\langle\pi\rangle/\langle W\rangle$ which is a measure of the entropy of the produced fireball.

6 Summary and conclusions

The NA61/SHINE experiment at the CERN SPS measured spectra and multiplicities of π^- mesons produced in the 5% most *central* ${}^7\text{Be}+{}^9\text{Be}$ collisions at beam energies of 19A, 30A, 40A, 75A and 150A GeV/c using the so-called h^- method. This is the first step in the systematic study of the phase diagram of hadronic matter and the first such measurement in Be+Be collisions.

The normalized width of the rapidity distribution σ_y/y_{beam} decreases with increasing collision energy and the values lie between the results for inelastic nucleon-nucleon and central Pb+Pb collisions. The average transverse mass $\langle m_T \rangle - m$ versus collision energy shows a plateau in the

SPS energy range at a similar level like in inelastic nucleon-nucleon and central Pb+Pb collisions. The mean multiplicity of pions per wounded nucleon in *central* ${}^7\text{Be}+{}^9\text{Be}$ collisions rises linearly with the Fermi energy variable F and is close to the one in *central* Pb+Pb collisions expect for the top SPS energy, where it is closer to the $N+N$ ratio.

The results are discussed in the context of predictions for the onset of deconfinement at the CERN SPS collision energies.

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