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Proton distribution radii of $16-24$ O : signatures of new shell closures and neutron skin

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The root mean square radii of the proton density distribution in $16-24$ O derived from measurements of charge changing cross sections with a carbon target at ∼900A MeV together with the matter radii portray thick neutron skin for $22-24$ O despite $22,24$ O being doubly magic. Imprints of the shell closures at $N = 14$ and 16 are reflected in local minima of their proton radii that provide evidence for the tensor interaction causing them. The radii agree with ab initio calculations employing the chiral NNLO_{sat} interaction, though skin thickness predictions are challenged. Shell model predictions agree well with the data.

Nuclear shell structure has profound impact in shaping the elemental abundance in the universe. Nuclei with filled proton and/or neutron shells, i.e. magic numbers, play a significant role. Doubly magic nuclei are key benchmarks for constraining the nuclear force and nuclear models. Oxygen isotopes have closed proton shell $(Z = 8)$. The doubly magic nature of ¹⁶O leads to its copious abundance hence enabling sustaining life in the universe. The rare isotopes are unveiling new nuclear shells and exotic neutron skin and halo structures. At the edge of neutron binding, the neutron drip-line, a new magic number has surfaced at $N = 16$ making the heaviest oxygen isotope ²⁴O an unexpected doubly magic nucleus. A sub-shell closure at $N = 14$ also emerges in ²²O. Do these neutron shell closures impact the proton distribution? Does the doubly-magic nature of $22,24$ O hinder neutron skin formation?

This Letter addresses the questions above through experimental determination of the root mean square radii of the point proton density distributions, henceforth referred to as point proton radii, in $16,18-24$ O.

The signature of shell closures $N = 50$ and 82 is seen from a local dip in the proton radius for isotopes [1]. In neutron-rich light nuclei a new sub-shell gap at $N =$ 6 shows prominent minimum in the proton radii for He to B isotopes [1]. The proton radii of nitrogen isotopes hinted a dip at $N = 14$ [2]. If the possible origin of this sub-shell closure is due to the attractive isospin $(T) = 0$ $p - n$ tensor interaction it would be reflected also in the proton radii of neutron-rich oxygen isotopes.

The new shell closure at $N = 16$ is seen in the high excitation energy of the first excited state [3] of ²⁴O and from the large $2s_{1/2}$ orbital [4] occupancy of the valence neutrons, reflected in the neutron removal momentum distribution. Proton inelastic scattering of ²⁴O shows a small quadrupole deformation of 0.15(4) confirming a spherical shell closure at $N = 16$ [5].

A sub-shell closure at $N = 14$ for ²²O is discussed from

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high energy of its 2^+ first excited state [6] and a small quadrupole deformation parameter 0.26(4) [7] compared to ²⁰O. Quasifree (p, pn) neutron knockout [8] and neutron removal with carbon target [9] from 22O result in a wider momentum distribution reflecting knockout of $1d_{5/2}$ neutrons, consistent with $N = 14$ sub-shell gap. A narrower momentum distribution for ${}^{21}N$ suggests reduction of $N = 14$ shell gap in nitrogen. The quenching is derived from unbound states in ^{22}N [10]. It is predicted that a $2s_{1/2}$ - $1d_{5/2}$ level inversion may occur in ²⁰C. Proton knockout via $(p, 2p)$ reactions show a larger cross section for ^{22,23}O than ²¹N [8] interpreted being due to more protons in the $1p_{1/2}$ orbital in oxygen isotopes. The wider proton removal momentum distribution for ^{22}O is qualitatively suggested to be due to its compact nature from filled valence shell for protons. However, that for 23 O is indicated to be narrow, which remains to be understood.

The large matter radii for ^{23}O [11] and ^{24}O [12, 13] from interaction cross section (σ_I) measurements signal the possibility of a thick neutron surface. The large σ_I of 23 O is explained by ²²O core + neutron in the $2s_{1/2}$ orbital [11]. This is consistent with its narrow one-neutron removal longitudinal momentum distribution [9, 14] and its large Coulomb dissociation cross section [15]. The neutron removal momentum distribution of ²⁴O shows predominant valence neutron occupancy in the $2s_{1/2}$ orbital [4]. The matter radii derived from low-energy proton elastic scattering [16] is systematically higher than from the σ_I measurements. At energies below 100A MeV medium modification effects of the nuclear interaction can lead to large uncertainty in the extraction of the radii.

Ab *initio* calculations with chiral interactions as introduced in Ref.[16] predicted the radii of oxygen isotopes. In-medium similarity renormalization group (IM-SRG) and Gorkov self-consistent Green's function theory (GGF) with the Entem-Machleidt (EM) chiral interaction resulted in smaller radii than with the $NNLO_{sat}$ interaction [16]. An increase of charge radius ∼ 0.03 - 0.05 fm is predicted between ¹⁶O and ²⁴O using the SRG evolved chiral interaction [17] and the Δ -full interaction at N^2LO [18]. The $NN+3N(lnl)$ chiral Hamiltonian and the $NNLO_{sat}$ interactions in the Gorkov self-consistent Green's function theory [19] predicts a continuous increase of the charge radii with increasing mass number. In the relativistic mean field framework an ansatz simulating the pairing effect [20] predicts charge radii with odd-even staggering. For neutron-rich isotopes they predict $20,220$ having a larger charge radius. There is no experimental information on the proton distribution radii beyond 18 O.

In this article, we present the first determination of root mean square point proton radii for ¹⁹−²⁴O and those for the stable isotopes $16,18$ O derived from measurements of charge changing cross sections (σ_{CC}). The experiment was performed using the Fragment Separator FRS [21] at GSI. The $16-24$ O isotopes were produced by fragmentation of ⁴⁰Ar accelerated to 1A GeV which interacted

FIG. 1: (a) Schematic view of the experiment setup at the FRS with detector arrangement at the final focus F4. (b) Particle identification before C target at F4. (c) Z identification using MUSIC detector behind C target. The red / blue histogram shows data without / with C target.

with a Be target of thickness 6.3 g/cm^2 . The fragments produced were separated and identified using the FRS by employing the event-by-event determination of mass to charge ratio (A/Q) and atomic number Z information derived from the magnetic rigidity $(B\rho)$, time-offlight (TOF) and energy-loss (ΔE) . The isotopes were fully stripped hence $Q = Z$. A schematic of the detector placement is shown in $Fig1(a)$ and the particle identification is shown in Fig.1(b). The energy-loss of the fragments in a multi-sampling ionization chamber (MU-SIC) [22] provided the Z information. The time of flight was measured between the dispersive mid-focal plane F2 and the achromatic final focal plane F4 using the fast plastic scintillators. Position sensitive Time Projection Chamber (TPC) detectors placed at these focal planes were used for beam tracking. The position information and the magnetic field provided the $B\rho$ determination of the incoming beam.

The σ_{CC} was measured with a 4.010 g/cm² thick C target placed at F4. The measurement was done using the transmission technique, where the ratio of the particles transmitted through the target without any loss of protons to the number of incoming particles gives the desired cross section for determining the root mean square radius of the point proton distribution, hereafter referred to as the proton radius. For this measurement the number (N_{in}) of the incident nuclei ${}^{A}Z_{in}$ before the reaction target is identified and counted event-by-event. Behind the reaction target, the nuclei with charge $Z_{out} \geq Z_{in}$ are identified and counted on an event-by-event basis $(N_{Z>Z_{in}})$. The charge changing cross section is given

by $\sigma_{CC} = t^{-1} \ln(R_{T_{out}}/R_{T_{in}})$. Here $R_{T_{in}}$ and $R_{T_{out}}$ are the ratios of $N_{Z\geq Z_{in}}/N_{in}$ with and without the reaction target, respectively and t is the target thickness. Data without the reaction target was collected in order to account for losses due to interaction with the non-target materials. There is no uncertainty in N_{in} due to freedom of any incident beam event selection in the event-by-event counting.

In order to eliminate beam particle losses due to the restricted acceptance of the target and/or detectors the incident beam events were chosen with a restricted phase space. This reduces the systematic uncertainty in the transmission ratio. A veto scintillator with a central aperture was placed in front of the target to reject beam events incident on the edges of the target scattered by matter upstream and multi-hit events that can cause erroneous reaction information in the MUSIC detector placed after the target. In the incident beam identification the estimated contamination from $Z = 7$ and 9 are 6×10^{-5} and 2×10^{-5} , respectively.

In order to count the ^AO beam events that did not undergo proton removal reactions in the target, the spectrum of the MUSIC detector placed after the target was used with the condition of the selected incoming ${}^{A}O$ beam events for the $Z_{out} \geq 8$ identification (Fig.1c). The limits are chosen to be the 3.5σ ends of the $Z = 8$ and 9 peaks. The $Z = 9$ peak is included in the unreacted event counting because proton pickup or (p, n) reactions leading to higher Z do not involve interaction with protons in the projectile. Hence, for determining the proton radius these are unreacted proton events. The energyloss in the TPC and plastic scintillator detectors placed further downstream of the target provided additional information to confirm the Z identification as well as determine the detection efficiency of the MUSIC detector. The MUSIC detector resolution for Z was ~ 0.1 (σ). The estimated $Z_{out} = 7$ contamination in the selection region of unreacted Z_{out} is $\sim 5 \times 10^{-5}$ which leads to an average uncertainty of ± 0.07 mb in the σ_{CC} .

The measured cross sections and their one standard deviation total uncertainties are given in Table 1. This includes the target thickness uncertainty of ∼0.1%. The systematic uncertainty from contaminants vary for the different isotopes ranging from 0.05 mb - 1 mb. The cross section for 16 O aligns with the value 813(8) mb reported in Ref.[23] at a slightly higher energy of 903A MeV. The cross sections reported in Ref. [24] at $930\pm44A$ MeV are systematically higher as found also for other isotopic chains and have larger uncertainties making them unsuitable to accurately derive the proton radii.

To extract the root mean square radii the measured σ_{CC} are compared to cross sections calculated (σ_{CC}^{cal}) using the Glauber model framework [25]. The formalism uses harmonic oscillator density profiles for the protons and neutrons in the projectile nucleus and the carbon target. The variation of the harmonic oscillator width yields projectile proton densities with different root mean square proton radii (R_p) which give different σ_{CC}^{cal} . The

FIG. 2: (a) R_p^{ex} (filled circles), blue open squares show $R_p^{e^-}$. (b) R_m^{ex} (Table 1) σ_I from Ref.[12] (open circles), Ref.[11] (filled circles). The curves show predictions with coupled cluster theory for $NNLO_{sat}$ interaction (red curves). The dotted curves represent the \pm 3% uncertainty of the theory. The predictions with $NNLO_{sat}$ interaction and the IMSRG model are shown by the star symbols. The pink squares show shell model predictions. The green bars and dashed lines show mean field results.

consistency of the measured σ_{CC} and σ_{CC}^{cal} determines the range of R_p^{ex} that agrees with the data. The derived R_p^{ex} are listed in Table 1. A good agreement of R_p^{ex} and the root mean square point proton radii derived from electron scattering $(R_p^{(e^-)})$ is seen for ^{16,18}O. This supports the successful determination of R_p^{ex} from the measured σ_{CC} . The gradual filling of neutrons in the $1d_{5/2}$ orbital is found to decrease the R_p^{ex} progressively for ^{20–22,24}O (Table 1 and Fig. 2). This is consistent with lower $B(E2)$) values [26]. A local minimum seen at $N = 14$ is reflecting this new sub-shell closure. The consistent decrease in the proton radius for both ^{21}N [2] and ^{22}O shows the $N = 14$ sub-shell gap arises from the attractive $T = 0$ monopole tensor interaction between the protons in the $1p_{1/2}$ orbital and neutrons in the $1d_{5/2}$ orbital.

The proton radius of 23 O increases due to its extended neutron density distribution where the valence neutron is

TABLE I: Secondary beam energies at the entrance of the C target, measured σ_{cc} and the root mean square proton and matter radii derived from the data for the oxygen isotopes.

Isotope	\rm{E}/\rm{A}	σ_{cc}^{ex}	R_p^{ex}	$R_p^{(e^-)}$	R_m^{ex}
	(MeV)	(mb)	(f _m)	(f _m)	(f _m)
$\overline{16}$ O	857	848(4)	2.54(2)	2.55(1)	2.57(2)
18 O	872	879(5)	2.67(2)	2.66(1)	2.64(8)
19 O	956	852(7)	2.55(3)		2.71(3)
20 O	880	846(4)	2.53(2)		2.71(3)
21 \bigcirc	937	847(6)	2.53(2)		2.73(3)
22 O	937	837(3)	2.50(2)		$2.78(6)^{a}$
22 O					$2.90(5)^{b}$
23 O	871	857(8)	2.58(3)		$2.99(10)^{a}$
23 O					$3.20(4)^{b}$
24 O	866	839(11)	2.51(4)		3.18(12)

^a σ_I [11]

occupying predominantly the $2s_{1/2}$ orbital. The proton radius of ²⁴O is found to be smaller than ²³O but similar to that of ²²O. This suggest the center-of-mass of the two valence neutrons in ²⁴O is not greatly separated spatially from that of the core. The filling of the $2s_{1/2}$ orbital also leads to stronger neutron binding of the two-valence neutrons in 24 O due to pairing.

Using the R_p^{ex} determined in this work we find the point matter radius by analyzing the interaction cross sections (σ_I) reported in Refs.[11, 12]. At the high energies inelastic scattering cross section to bound excited states is negligible. Therefore, $\sigma_I = \sigma_R$, the reaction cross section. The nucleon-target profile function in the Glauber model (NTG) [27] with the profile function given in Ref.[28] is used for calculating σ_R^{cal} , for which harmonic oscillator densities of protons and neutrons for ${}^{A}O$ are adopted. The densities that result in σ_R^{cal} agreeing with the measured σ_I yield the point matter radii (R_m^{ex}) that are listed in Table 1. The R_m^{ex} of $19-22$ Q shows a small gradual increase, trend that is broken at ²³O which shows a larger increase in R_m^{ex} . We note that the later measurement of interaction cross section of $22,23$ O [11] yield matter radii that agree with the description of ^{23}O in a ^{22}O core plus neutron model with large spectroscopic factor for the neutron in the $2s_{1/2}$ orbital. This is consistent with the observations from knockout reactions [14] and Coulomb dissociation [15].

Ab-initio coupled-cluster and valence-space (VS) IM-SRG computations are performed employing the chiral $NN+3N$ interaction $NNLO_{sat}$ [29], which generally reproduces absolute and relative trends in radii across isotopic chains in both the sd [30] and pf shells [31, 32]. For the coupled-cluster calculations we employ the singlesand-doubles (CCSD) approximation [33], and start from an axially deformed Hartree-Fock reference state (assuming a prolate shape) following Refs. [34, 35]. In the VS-IMSRG, an approximate unitary transformation is constructed to decouple a core and effective valence-space Hamiltonian [36–38] diagonalized with the KSHELL code [39]. Applying the same transformation to the point proton radius operator we further construct an effective valence-space operator consistent with the Hamiltonian. Other details of the ab initio radii calculations can be found in Ref. [32]. Combining the effects from neglected many-body correlations, model-space truncations, and symmetry breaking we estimate an uncertainty of $\pm 3\%$ on the coupled-cluster computations which is correlated for the point nucleon radii, hence negligible for relative quantities.

The R_p^{ex} are compared (Fig. 2a) with the CCSD predictions (red curves). The $NNLO_{sat}$ interaction reproduces binding energies of oxygen isotopes [29, 40]. It reproduces also the trends of R_p^{ex} reasonably well for neutron-rich isotopes predicting a radius dip at $N = 14$ consistent with the data. The IMSRG (star symbols) results with the $NNLO_{sat}$ interaction from Ref.[16], are within the uncertainty band of the CCSD results and also show a local minimum at $N = 14$. In contrast, Ref.[20] predicts an increase in the charge radius of 22° O. The NN+3N(lnl) chiral interaction predictions [19] are smaller than the data showing an improved description of the nuclear interaction by $NNLO_{sat}$. Within the data uncertainties the R_p^{ex} of the doubly closed shell nuclei ¹⁶O and ²⁴O are similar, with an indication, from the central values, of a possible reduction in 24 O due to its stronger proton binding.

Shell model calculations with the YSOX Hamiltonian [41] are shown in Fig. 2 and 3 (filled squares). Occupation numbers for the orbits obtained with the YSOX are used to evaluate the proton and matter radii as well as the neutron skin thickness. The proton orbits are obtained in a Woods-Saxon potential with the standard parameters [42], the resulting proton radii (Fig. 2a filled pink squares) are in fair agreement with the data. Using these proton radii, the matter radii are computed using harmonic oscillator functions for neutron orbits with $\hbar\omega$ = $45/A^{1/3}$ -25/ $A^{2/3}$ except for the $2s_{1/2}$ orbital in $2s_{3/2}$. which are obtained by the three-body model with an inert ²²O core plus $2s_{1/2}$ valence neutron description [43]. Use is made of a low-energy limit of the valence neutronneutron interaction, which can reproduce the known NN scattering length and effective range [43].

Mean-field Hartree-Fock calculations with Sk3, SLy4 and SKM forces (Fig. 2 green bars and dashed lines) show proton radii of 22 O and 24 O larger than that of 16 O, independent of the Skyrme forces. This is contrary to the data trend. Inclusion of the coupling to the monopole resonances and improvements of proton-neutron interaction need to be considered in future for the study of neutronrich nuclei in the mean-field approximation.

The point matter radii are compared to the model predictions in Fig. 2b. The coupled cluster theory predictions with \pm 3% uncertainty band is shown by the red solid and dotted curves, respectively. The IMSRG calculations performed in this work are shown by the star symbols. An overall good agreement with the data af-

 b σ_I [12]

FIG. 3: Neutron skin thickness data from R_p^{ex} and R_m^{ex} filled circles. The red solid (dotted) curves represent the predictions $(\pm 3\%$ uncertainty) from coupled cluster theory using the $NNLO_{sat}$ interaction. The star symbols represent predictions from the IMSRG calculations. The pink filled squares are shell model results. Green bars show mean-field results.

firms the $NNLO_{sat}$ interaction to be successful in predicting the radii from stable isotopes to the drip-line. The shell model predictions also agree well with the data (Fig. 2b filled pink squares). The mean field model predictions are shown by the green bars and dashed lines. The predicted radii align better with the data for $22,23$ O from Ref.[11] which are also consistent for a core + neutron($2s_{1/2}$) model for ²³O. We therefore, use these data to derive the neutron skin thickness shown in Fig.3. The neutron skin thickness is found by $R_n - R_p$ $=\sqrt{(A/N)R_m^2-(Z/N)R_p^2}-R_p$, where A, N, Z are the mass number, neutron number and proton number, respectively. R_m , R_n and R_p are the point matter, point neutron and point proton rms radii, respectively. The data reveal a thick neutron surface for ²²−24O. The skin thickness predicted by the coupled cluster model and the IMSRG are similar but underestimate the data beyond ²¹O. The shell model predictions of neutron skin thickness (Fig.3 filled squares) successfully describe the large neutron surface for $22,23$ O.

In summary, the point proton radii of ¹⁶,18−24O derived from measurements of charge changing cross sections show an extended radius for 23 O and local minimum for ²²O that relates to the $N = 14$ sub-shell closure due to the tensor force. The doubly magic nature of $22,24$ O does not hinder neutron skin development, which rapidly increases for ²²−24O. Shell model predictions reproduce the observed neutron skin. Ab initio predictions with the $NNLO_{sat}$ chiral interaction agree within theoretical uncertainty with R_p^{ex} showing a dip for ²²O as observed in the data. The predictions for neutron skin thickness of ²²−24O underestimate the data. The data therefore open new avenues for refining the chiral interaction.

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- [1] I. Angeli and K. Marinova, Atomic Data and Nuclear Data Tables 99, 69 (2013).
- [2] S. Bagchi et al., Phys. Lett. B **790**, 251 (2019).
- [3] C. Hofman et al., Phys. Lett. B **672**, 17 (2009).
- [4] R. Kanungo et al., Phys. Rev. Lett. **102**, 152501 (2009).
- [5] K. Tshoo et al., Phys. Rev. Lett **109**, 022501 (2012).
- [6] M. Stanoiu et al., Phys. Rev. C 69, 034312 (2004).
- [7] E. Becheva et al., Phys. Rev. Lett. 96, 012501 (2006).
- [8] P. Díaz Fernández et al., Phys. Rev. C **97**, 024311 (2018).
- [9] E. Sauvan et al., Phys. Rev. C 69, 044603 (2004).
- [10] M. Strongman et al., Phys. Rev. C **80**, 021302(R) (2009).
- [11] R. Kanungo et al., Phys. Rev. C 84, 061304(R) (2011).
- [12] A. Ozawa et al., Phys. Rev. Lett. 84, 5493 (2000).
- [13] A. Ozawa, T. Suzuki, and I. Tanihata, Nucl. Phys. A 691, 599 (2001).
- [14] D. Cortina-Gil et al., Phys. Rev. Lett. **93**, 062501 (2004).
- [15] C. Nociforo et al., Phys. Lett. B **605**, 79 (2005).
- [16] V. Lapoux et al., Phys. Rev. Lett. **117**, 052501 (2016).
- [17] S. Binder et al., Phys. Rev. C 98, 014002 (2018).
- [18] J. Hoppe et al., Phys. Rev. C 100, 024318 (2019).
- [19] V. Som/'ea et al., Phys. Rev. C 101, 014318 (2020).
- [20] R. An, L.-S. Geng, and S.-S. Zhang, Phys. Rev. C 102, 024307 (2020).
- [21] H. Geissel et al., Nucl. Instrum. Methods Phys. Res.,

Sect. B 70, 286 (1992).

- [22] A. Stolz et al., Phys. Rev. C 65, 064603 (2002).
- [23] W. Webber, J. Kish, and D. Schrier, Phys. Rev. C 41, 520 (1990).
- [24] L. Chulkov et al., Nucl. Phys. A 674, 330 (2000).
- [25] Y. Suzuki et al., Phys. Rev. C **94**, 011602(R) (2016).
- [26] S. Raman, C. J. Nestor, and P. Tikkanen, At. Data and Nucl. Data Tables 78, 1 (2001).
- [27] B. Abu-Ibrahim and Y. Suzuki, Phys. Rec. C 62, 051601(R) (2000).
- [28] B. Abu-Ibrahim, W. Horiuchi, A. Kohama, and Y. Suzuki, Phys. Rev. C 77, 034607 (2008).
- [29] A. Ekström, G. R. Jansen, K. A. Wendt, G. Hagen, T. Papenbrock, B. D. Carlsson, C. Forssén, M. Hjorth-Jensen, P. Navrátil, and W. Nazarewicz, Phys. Rev. C 91, 051301 (2015), URL https://link.aps.org/doi/ 10.1103/PhysRevC.91.051301.
- [30] H. Heylen, C. S. Devlin, W. Gins, et al., Phys. Rev. C 103, 014318 (2021).
- [31] R. de Groote et al., Nature Phys. 16, 620 (2020).
- [32] S. Malbrunot-Ettenauer et al., Phys. Rev. Lett. 128, 022502 (2022).
- [33] R. J. Bartlett and M. Musiał, Rev. Mod. Phys. $79, 291$ (2007).
- [34] S. J. Novario, G. Hagen, G. R. Jansen, and T. Papenbrock, Phys. Rev. C 102, 051303 (2020), URL https: //link.aps.org/doi/10.1103/PhysRevC.102.051303.
- $[35]$ A. Koszorús, X. F. Yang, W. G. Jiang, S. J. Novario, S. W. Bai, J. Billowes, C. L. Binnersley, M. L. Bissell,

T. E. Cocolios, B. S. Cooper, et al., Nat. Phys. 17, 439 (2021), ISSN 1745-2481, URL https://doi.org/10. 1038/s41567-020-01136-5.

- [36] S. R. Stroberg, S. K. Bogner, H. Hergert, and J. D. Holt, Ann. Rev. Nucl. Part. Sci. 69, 307 (2019).
- [37] S. R. Stroberg, A. Calci, H. Hergert, J. D. Holt, S. K. Bogner, R. Roth, and A. Schwenk, Phys. Rev. Lett. 118, 032502 (2017).
- [38] T. Miyagi, S. R. Stroberg, P. Navrátil, K. Hebeler, and J. D. Holt, Phys. Rev. C 105, 014302 (2022).
- [39] N. Shimizu, T. Mizusaki, Y. Utsuno, and Y. Tsunoda, Comput. Phys. Commun. 244, 372 (2019), URL https://doi.org/10.1016/j.cpc.2019.06.011https: //linkinghub.elsevier.com/retrieve/pii/ S0010465519301985.
- [40] A. Ekström, G. Baardsen, C. Forssén, G. Hagen, M. Hjorth-Jensen, G. R. Jansen, R. Machleidt, W. Nazarewicz, T. Papenbrock, J. Sarich, et al., Phys. Rev. Lett. 110, 192502 (2013), URL http://link.aps. org/doi/10.1103/PhysRevLett.110.192502.
- [41] C. Yuan *et al.*, Phys. Rev. C **85**, 064324 (2012).
- [42] A. Bohr and B. Mottelson, Nuclear Structure (W. A. Benjamin Inc, New York, 1969).
- [43] T. Suzuki, T. Otsuka, C. Tuan, and N. Alahari, Phys. Lett. B 753, 199 (2016).
- [44] S. R. Stroberg, https://github.com/ragnarstroberg/imsrg, URL https://github.com/ragnarstroberg/imsrg.