LEARNING REPRESENTATIONS OF SEQUENCES

WITH APPLICATIONS TO MOTION CAPTURE AND VIDEO ANALYSIS

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OVERVIEW: THIS TALK

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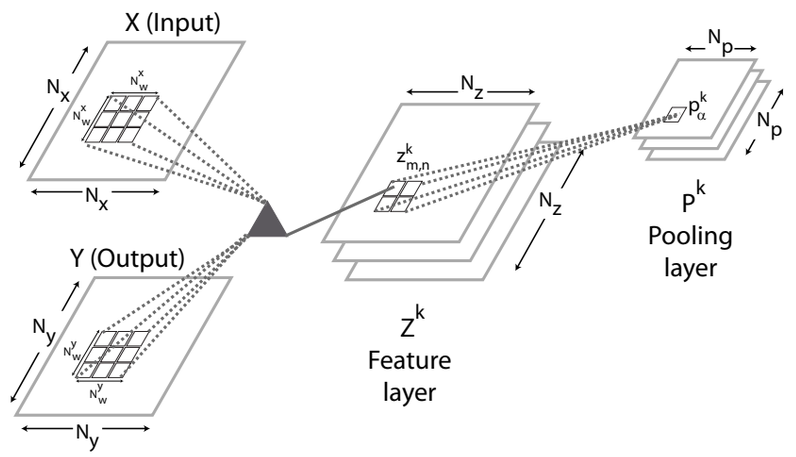
- Learning representations of temporal data:
  - existing methods and challenges faced
  - recent methods inspired by “deep learning”



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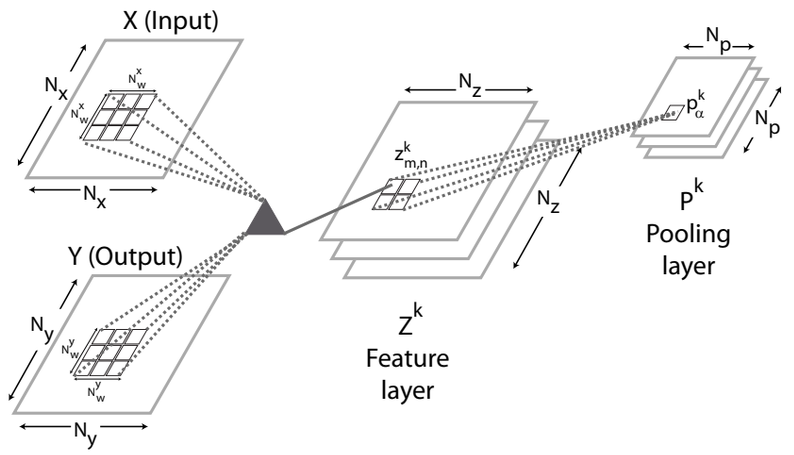
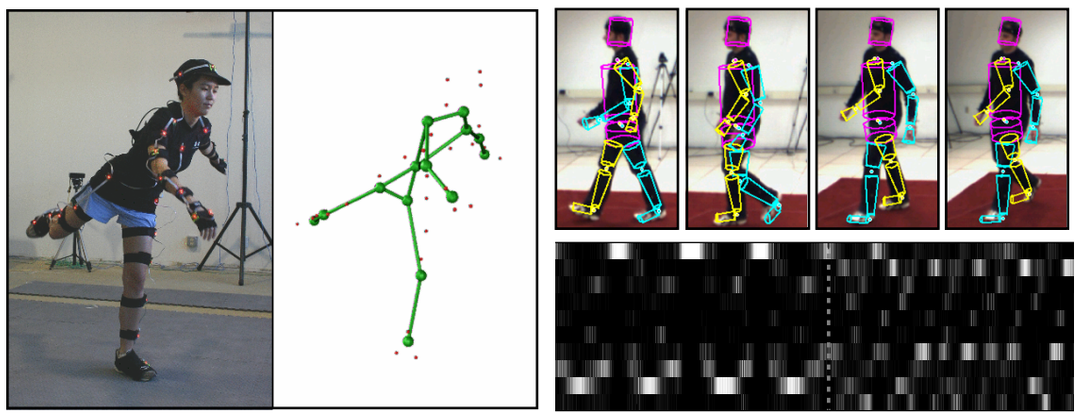


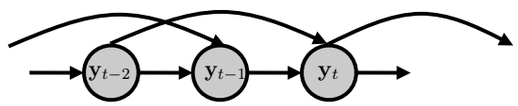
- Applications: in particular, modeling human pose and activity
  - highly structured data: e.g. motion capture
  - weakly structured data: e.g. video



OUTLINE

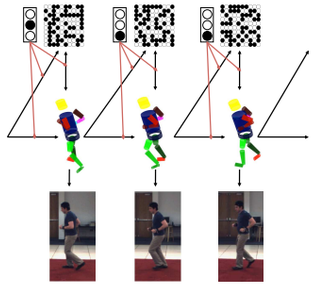
Learning representations from sequences

Existing methods, challenges



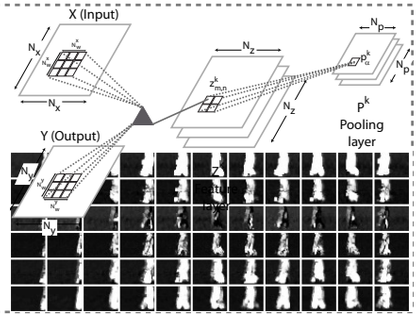
Composable, distributed-state models for sequences

Conditional Restricted Boltzmann Machines and their variants



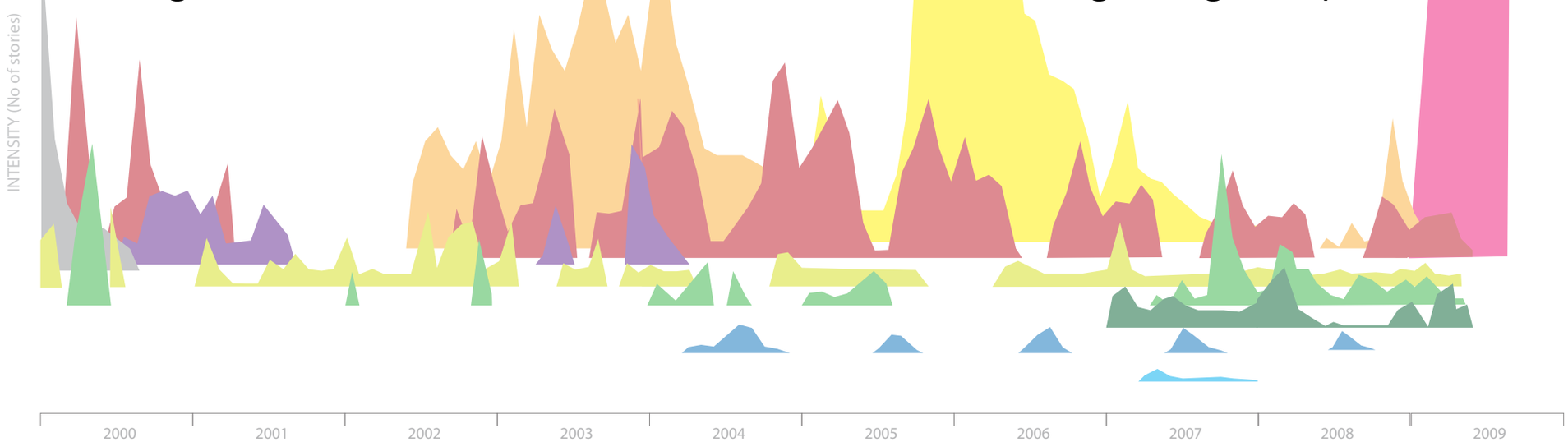
Using learned representations to analyze video

A brief and (incomplete survey of deep learning for activity recognition



TIME SERIES DATA

- Time is an integral part of many human behaviours (motion, reasoning)
- In building statistical models, time is sometimes ignored, often problematic
- Models that **do** incorporate dynamics fail to account for the fact that data is often high-dimensional, nonlinear, and contains long-range dependencies



Graphic: David McCandless, informationisbeautiful.net

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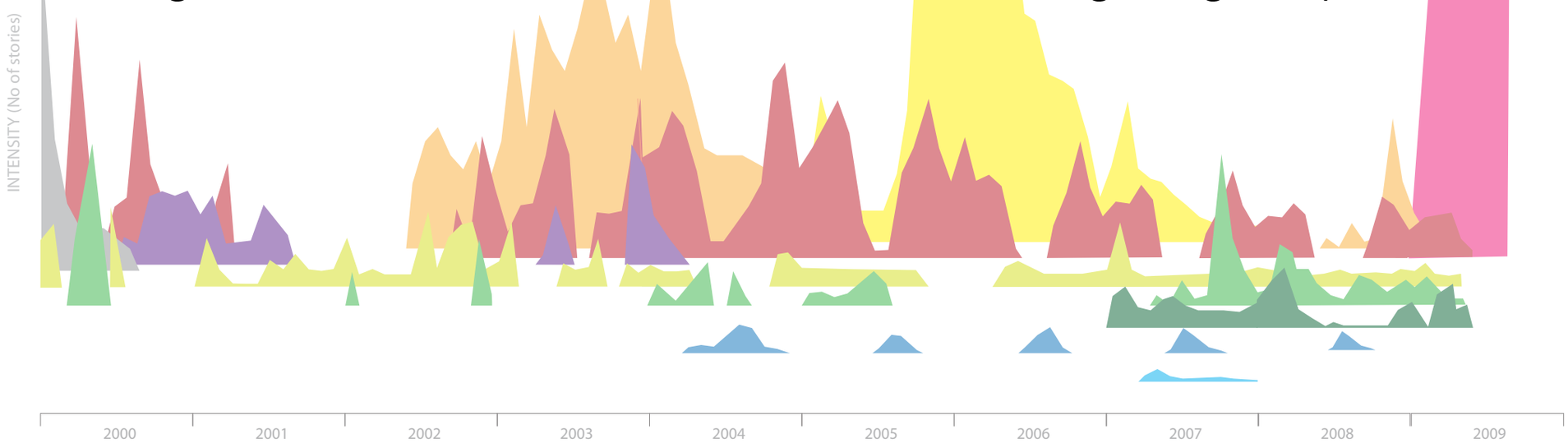


Today we will discuss a number of models that have been developed to address these challenges

Graphic: David McCandless, informationisbeautiful.net

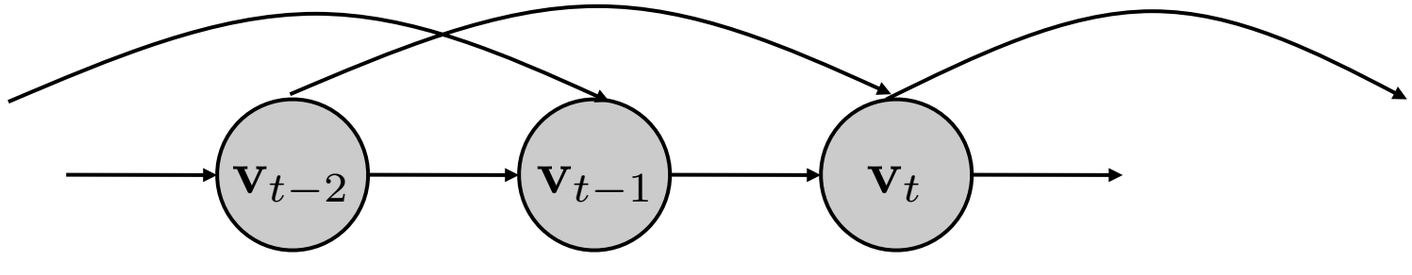
VECTOR AUTOREGRESSIVE MODELS

$$\mathbf{v}_t = \mathbf{b} + \sum_{m=1}^{M} A_m \mathbf{v}_{t-m} + \mathbf{e}_t$$

- Have dominated statistical time-series analysis for approx. 50 years
- Can be fit easily by least-squares regression
- Can fail even for simple nonlinearities present in the system

  - but many data sets can be modeled well by a linear system
- Well understood; many extensions exist

MARKOV ("N-GRAM") MODELS



- Fully observable
- Sequential observations may have nonlinear dependence
- Derived by assuming sequences have Markov property:

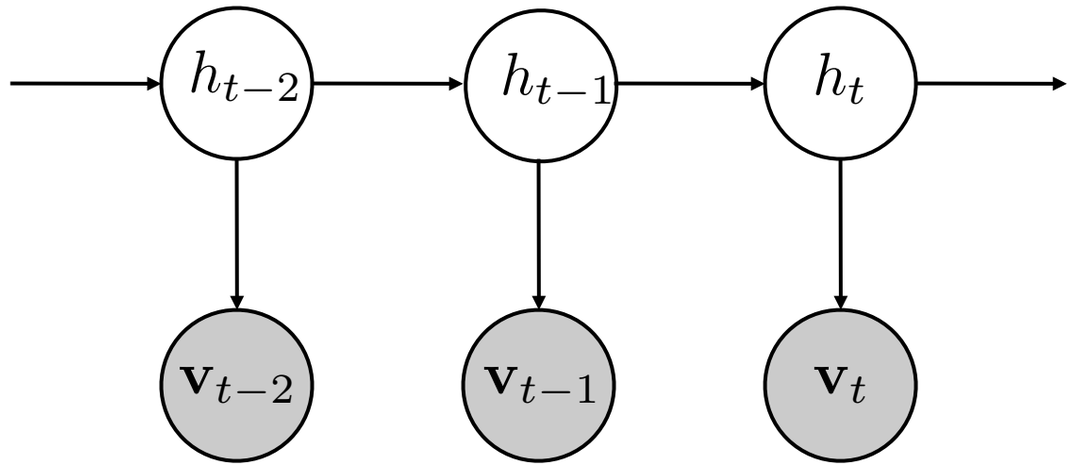
$$p(\mathbf{v}_t|\{\mathbf{v}_1^{t-1}\}) = p(\mathbf{v}_t|\{\mathbf{v}_{t-N}^{t-1}\})$$

- This leads to joint:

$$p(\{\mathbf{v}_1^T\}) = p(\{\mathbf{v}_1^N\}) \prod_{t=N+1}^{T} p(\mathbf{v}_t|\{\mathbf{v}_{t-N}^{t-1}\})$$

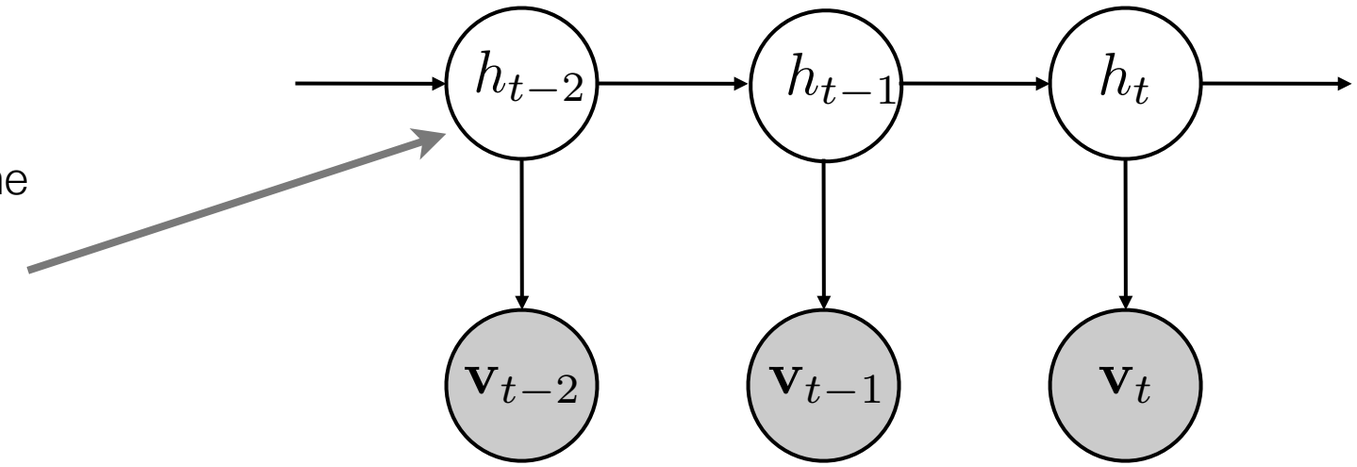
- Number of parameters exponential in N !

HIDDEN MARKOV MODELS (HMM)



HIDDEN MARKOV MODELS (HMM)

Introduces a hidden state that controls the dependence of the current observation on the past



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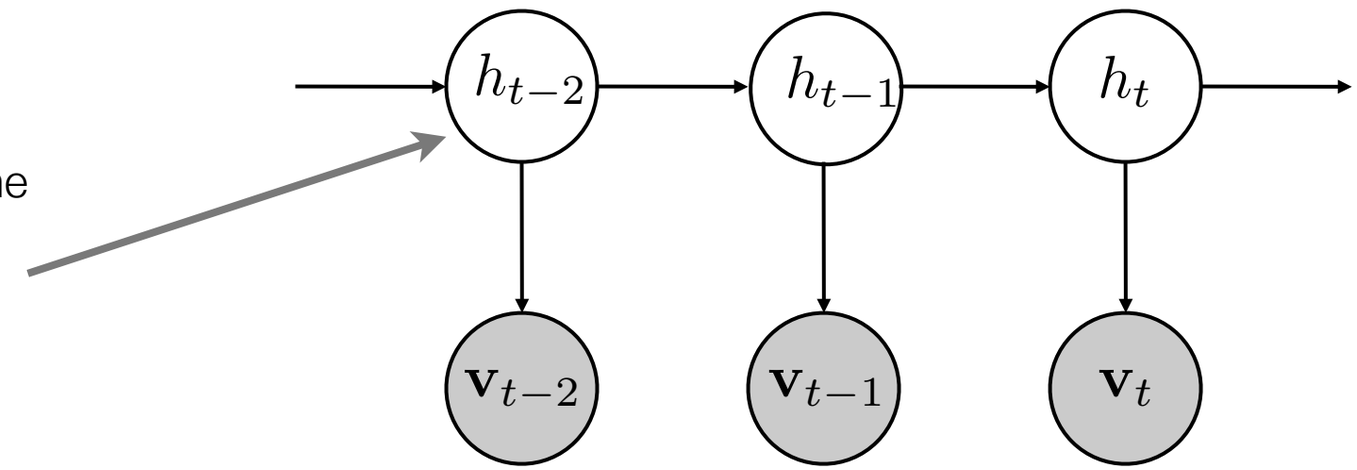

- Successful in speech & language modeling, biology
- Defined by 3 sets of parameters:
  - Initial state parameters, π
  - Transition matrix, A
  - Emission distribution, $p(\mathbf{v}_t|h_t)$
- Factored joint distribution: $p(\{h_t\},\{\mathbf{v}_t\}) = p(h_1)p(\mathbf{v}_1|h_1)\prod_{t=2}^{T} p(h_t|h_{t-1})p(\mathbf{v}_t|h_t)$

HMM INFERENCE AND LEARNING

- Typically three tasks we want to perform in an HMM:
  - Likelihood estimation
  - Inference
  - Learning
- All are exact and tractable due to the simple structure of the model
- Forward-backward algorithm for inference (belief propagation)
- Baum-Welch algorithm for learning (EM)
- Viterbi algorithm for state estimation (max-product)

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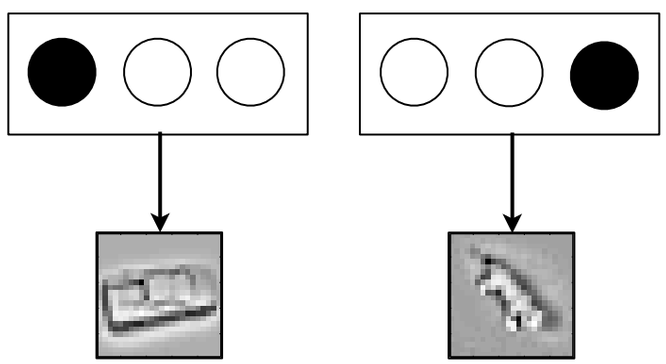

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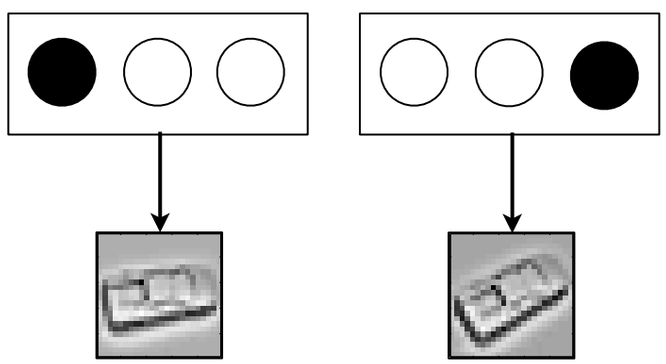

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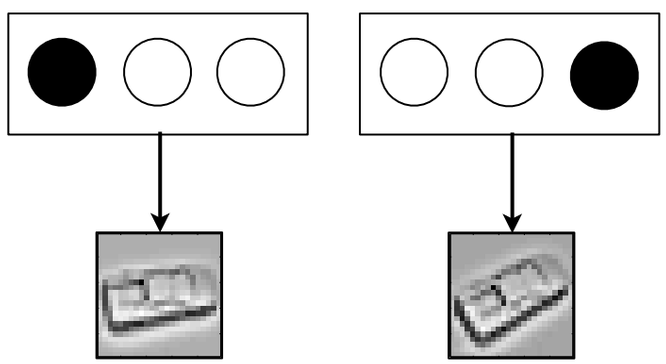

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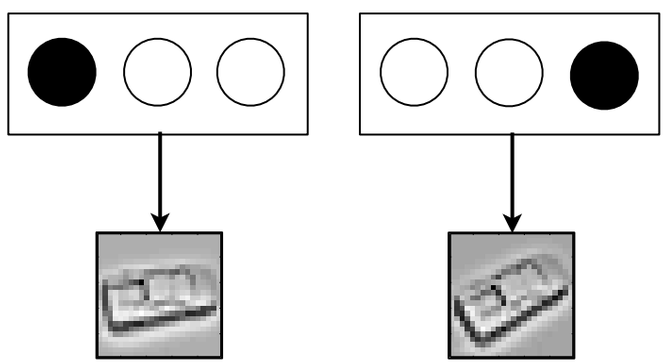

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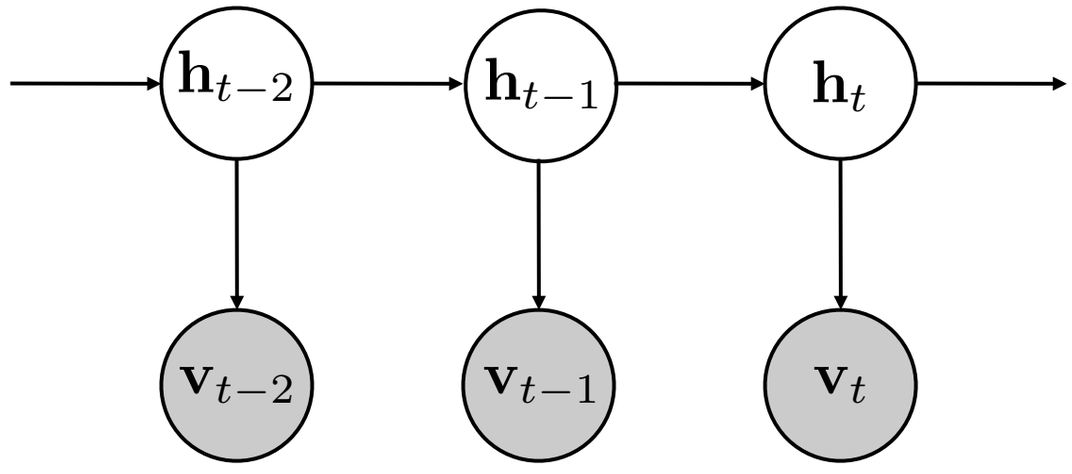
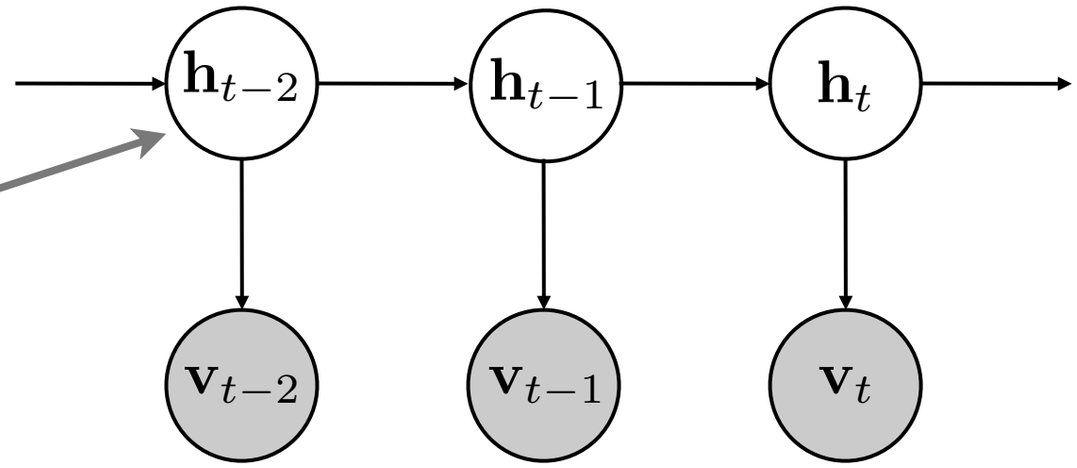
LINEAR DYNAMICAL SYSTEMS



LINEAR DYNAMICAL SYSTEMS

Graphical model is the same as HMM but with real-valued state *vectors*



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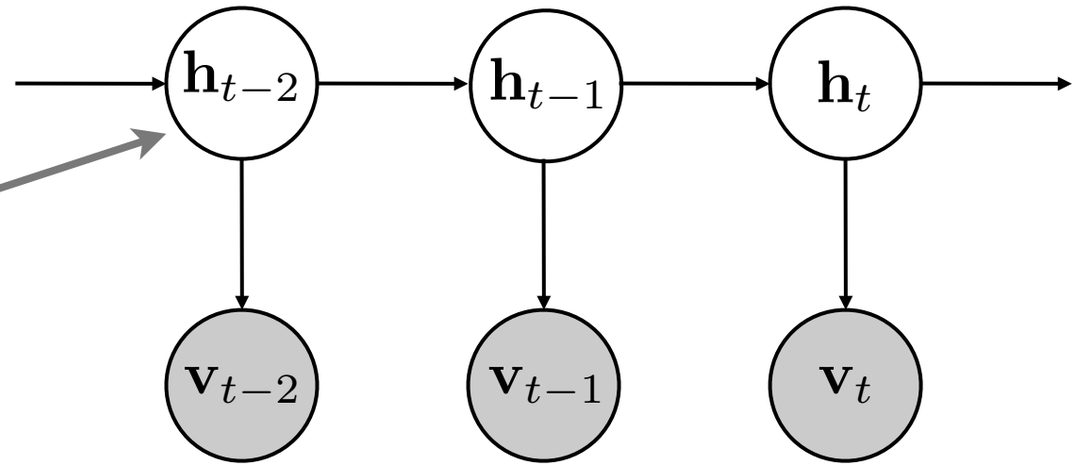


- Characterized by linear-Gaussian dynamics and observations:

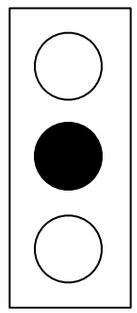
$$p(\mathbf{h}_t|\mathbf{h}_t - 1) = \mathcal{N}(\mathbf{h}_t; A\mathbf{h}_{t-1}, Q) \qquad p(\mathbf{v}_t|\mathbf{h}_t) = \mathcal{N}(\mathbf{v}_t; C\mathbf{h}_t, R)$$

- Inference is performed using Kalman smoothing (belief propagation)
- Learning can be done by EM
- Dynamics, observations may also depend on an observed input (control)

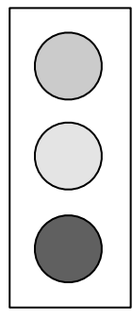
LATENT REPRESENTATIONS FOR REAL-WORLD DATA

Data for many real-world problems (e.g. motion capture, finance) is high-dimensional, containing complex non-linear relationships between components

<u>Hidden Markov Models</u>
Pro: complex, nonlinear emission model
Con: single K-state multinomial represents entire history



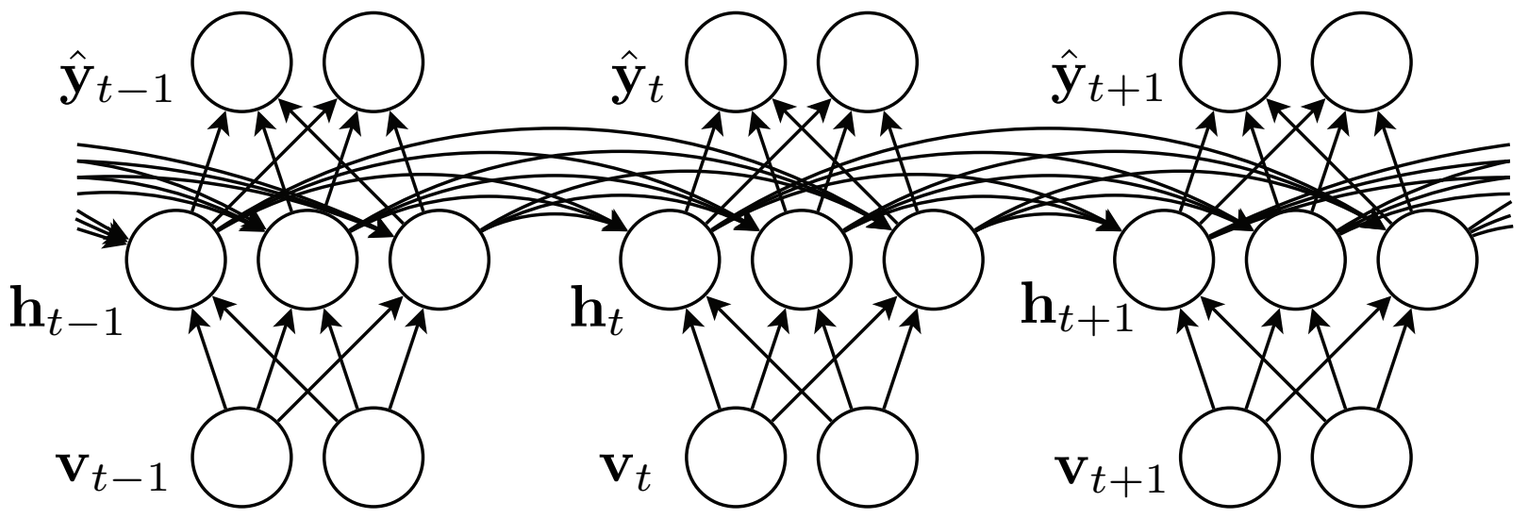
<u>Linear Dynamical Systems</u>
Pro: state can convey much more information
Con: emission model constrained to be linear



LEARNING DISTRIBUTED REPRESENTATIONS

- Simple networks are capable of discovering useful and interesting internal representations of static data
- Perhaps the parallel nature of computation in connectionist models may be at odds with the serial nature of temporal events
- Simple idea: spatial representation of time
  - Need a buffer; not biologically plausible
  - Cannot process inputs of differing length
  - Cannot distinguish between absolute and relative position
- This motivates an **implicit** representation of time in connectionist models where time is represented by its effect on processing

RECURRENT NEURAL NETWORKS



(Figure from Martens and Sutskever)

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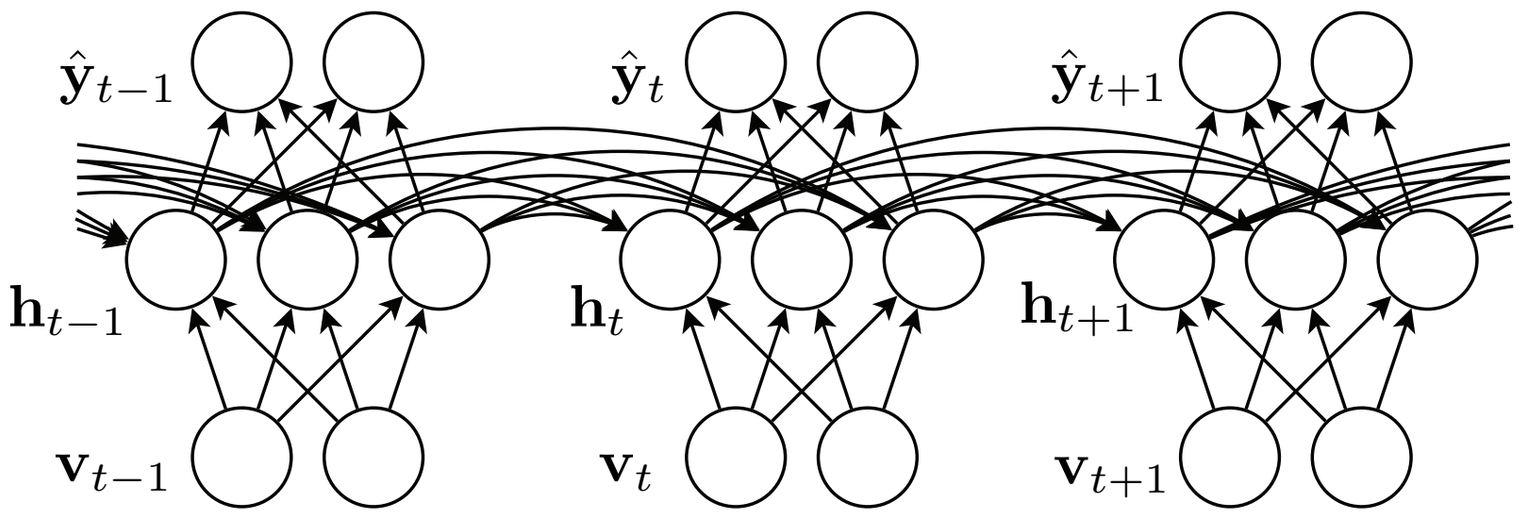

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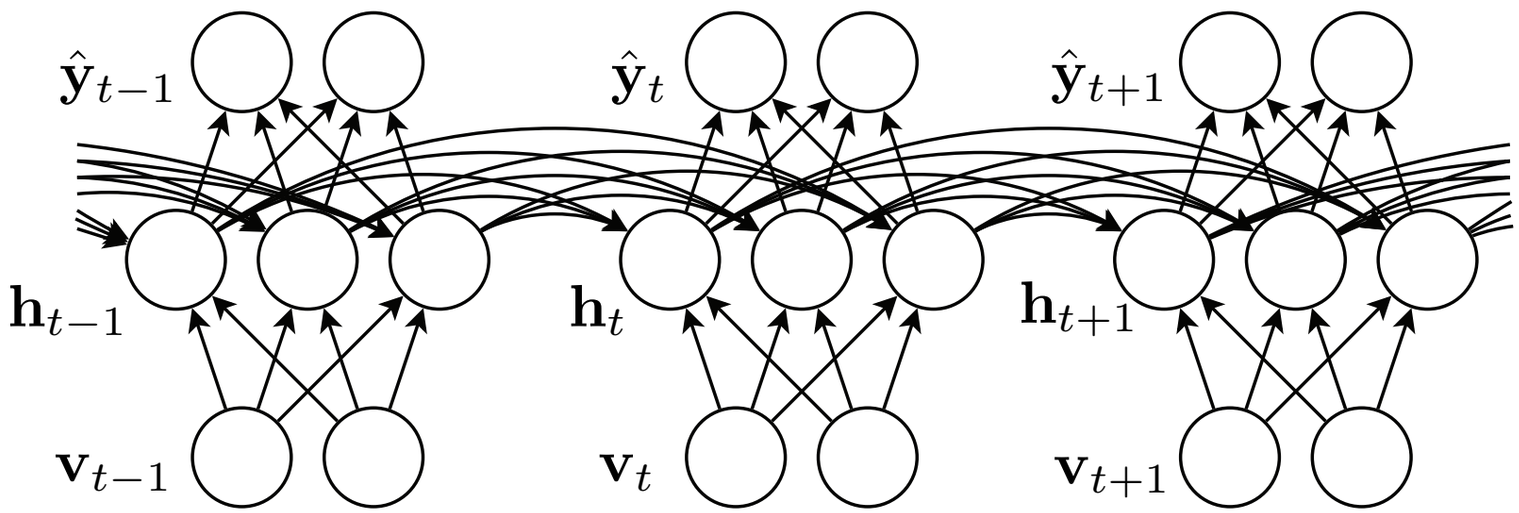

- Neural network replicated in time
- At each step, receives input vector, updates its internal representation via nonlinear activation functions, and makes a prediction:

$$
\begin{aligned}
\mathbf{v}_t &= W^{hv}\mathbf{v}_{t-1} + W^{hh}\mathbf{h}_{t-1} + \mathbf{b}_h \\
h_{j,t} &= e(v_{j,t}) \\
\mathbf{s}_t &= W^{yh}\mathbf{h}_t + \mathbf{b}_y \\
\hat{y}_{k,t} &= g(y_{k,t})
\end{aligned}
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- Exact gradients can be computed exactly via Backpropagation Through Time
- It is an interesting and powerful model. What's the catch?
  - Training RNNs via gradient descent fails on simple problems
  - Attributed to "vanishing" or "exploding" gradients
  - Much work in the 1990's focused on identifying and addressing these issues: none of these methods were widely adopted

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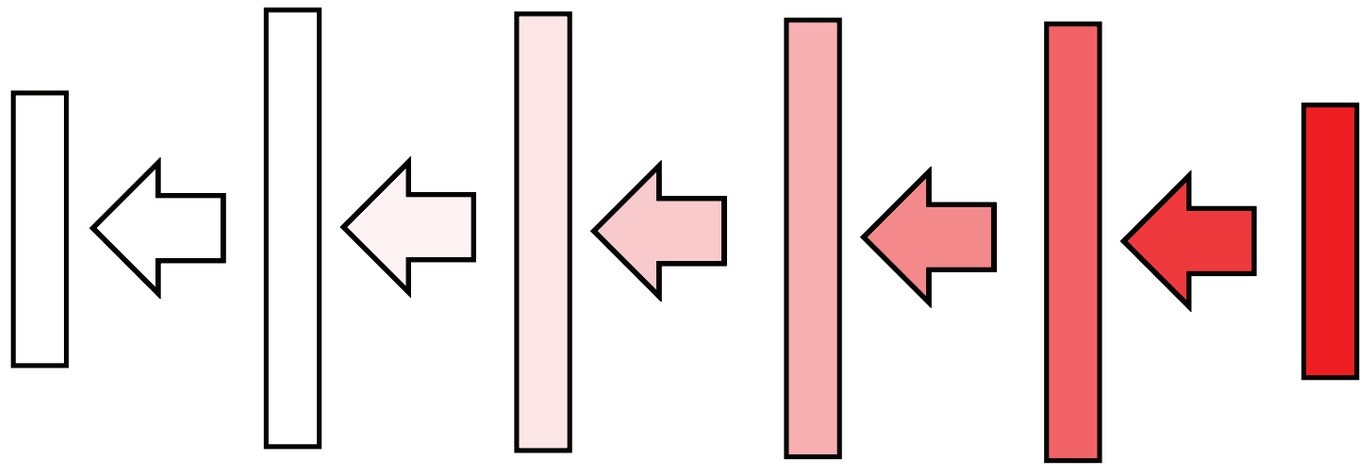

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  - Attributed to "vanishing" or "exploding" gradients
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- Best-known attempts to resolve the problem of RNN training:
  - Long Short-term Memory (LSTM) (Hochreiter and Schmidhuber 1997)
  - Echo-State Network (ESN) (Jaeger and Haas 2004)

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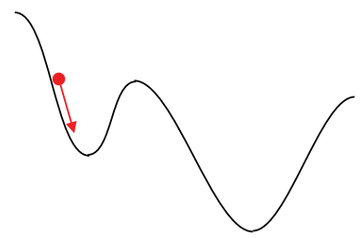


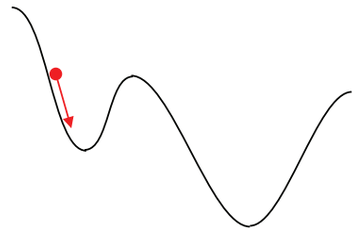
(Figures from James Martens)

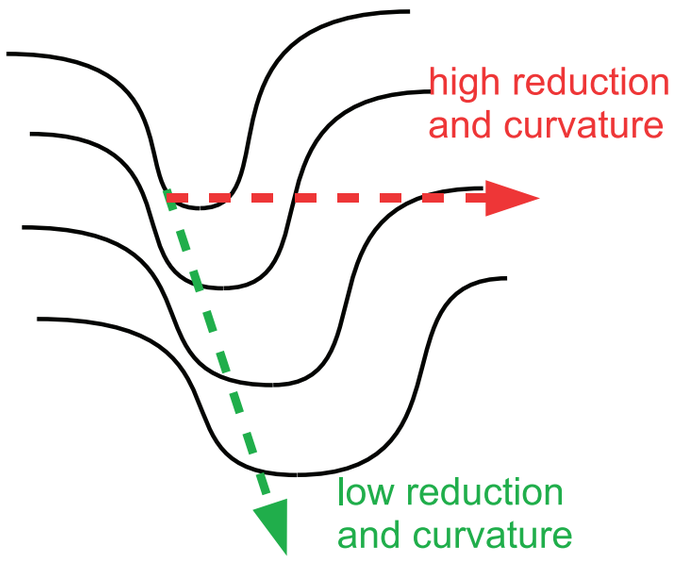
FAILURE OF GRADIENT DESCENT

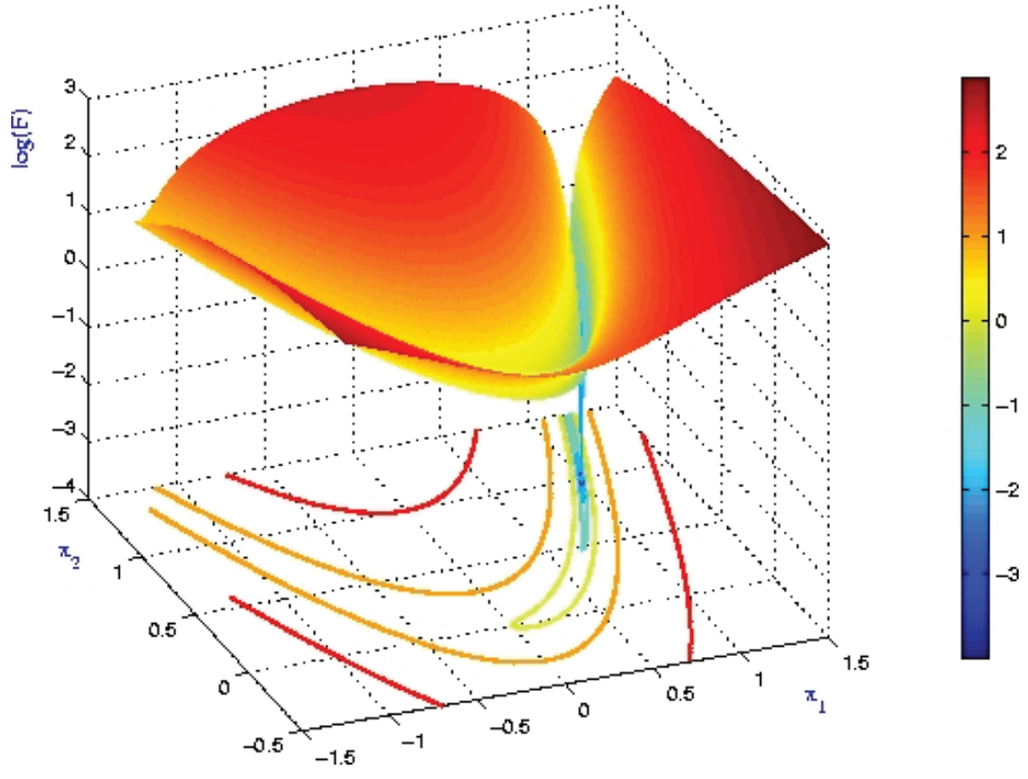
Two hypotheses for why gradient descent fails for NN:

- increased frequency and severity of bad local minima
- pathological curvature, like the type seen in the Rosenbrock function:

$$f(x, y) = (1 - x)^2 + 100(y - x^2)^2$$







(Figures from James Martens)

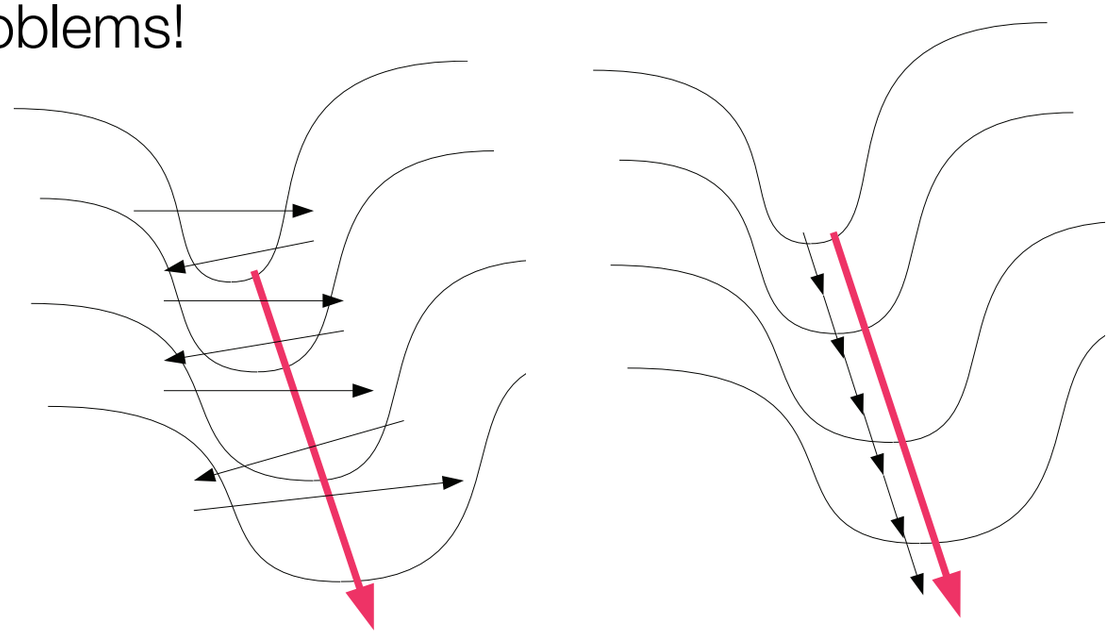
SECOND ORDER METHODS

- Model the objective function by the local approximation:

$$f(\theta + p) \approx q_\theta(p) \equiv f(\theta) + \Delta f(\theta)^T p + \frac{1}{2} p^T B p$$

  where p is the search direction and B is a matrix which quantifies curvature

- In Newton's method, B is the Hessian matrix, H
- By taking the curvature information into account, Newton's method "rescales" the gradient so it is a much more sensible direction to follow
- Not feasible for high-dimensional problems!



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This method was shown to effectively train RNNs in the pathological long-term dependency problems they were previously not able to solve (Martens and Sutskever 2011)

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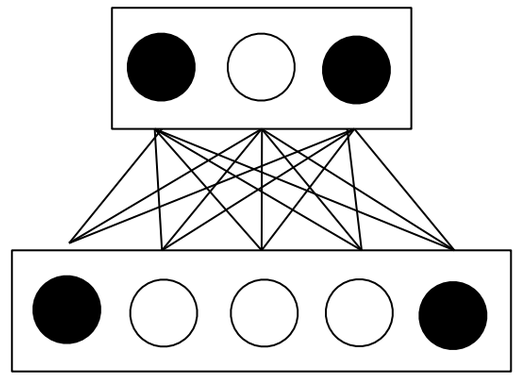
- Generative models (like Restricted Boltzmann Machines) can express the negative log-likelihood of a given configuration of the output, and can capture complex distributions
- By using binary latent (hidden) state, we gain the best of both worlds:
  - the nonlinear dynamics and observation model of the HMM without the simple state
  - the representationally powerful state of the LDS without the linear-Gaussian restriction on dynamics and observations

DISTRIBUTED BINARY HIDDEN STATE

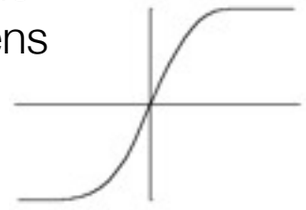
- Using distributed binary representations for hidden state in directed models of time series makes inference difficult. But we can:
  - Use a Restricted Boltzmann Machine (RBM) for the interactions between hidden and visible variables. A factorial posterior makes inference and sampling easy.
  - Treat the visible variables in the previous time slice as additional **fixed** inputs

Hidden variables (factors) at time t



Visible variables (observations) at time t

One typically uses binary logistic units for both visibles and hiddens

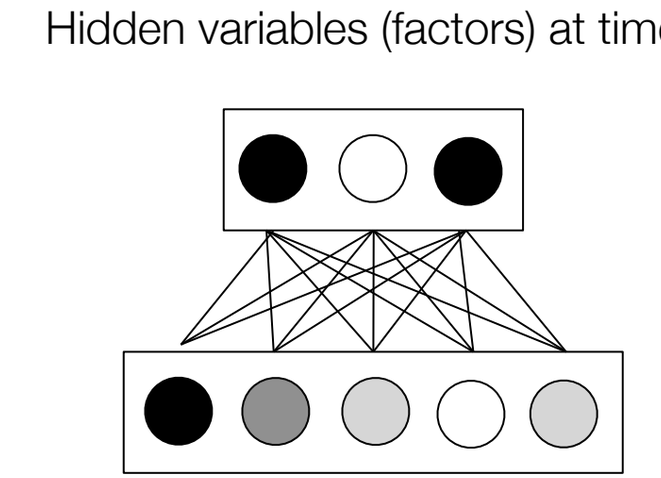


$$p(h_j = 1|\mathbf{v}) = \sigma(b_j + \sum_i v_i W_{ij})$$

$$p(v_i = 1|\mathbf{h}) = \sigma(b_i + \sum_j h_j W_{ij})$$

MODELING OBSERVATIONS WITH AN RBM

- So the distributed binary latent (hidden) state of an RBM lets us:
  - Model complex, nonlinear dynamics
  - Easily and exactly infer the latent binary state given the observations
- But RBMs treat data as static (i.i.d.)



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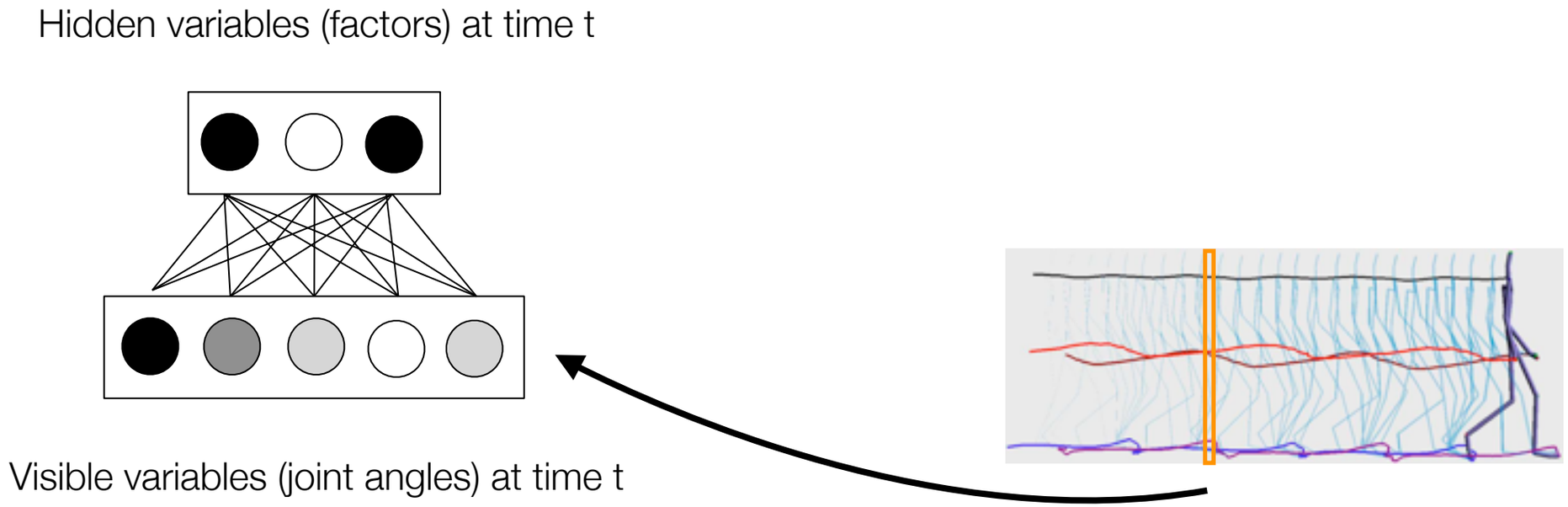

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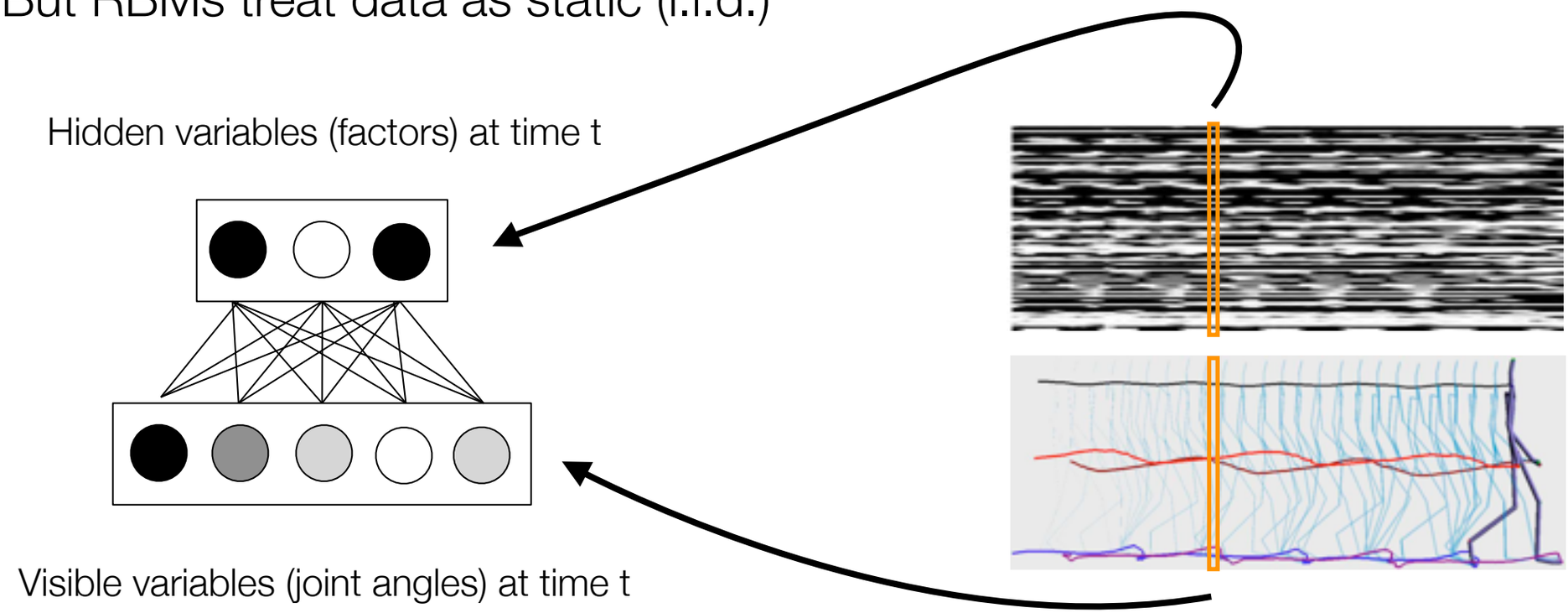

CONDITIONAL RESTRICTED BOLTZMANN MACHINES

(Taylor, Hinton and Roweis NIPS 2006, JMLR 2011)

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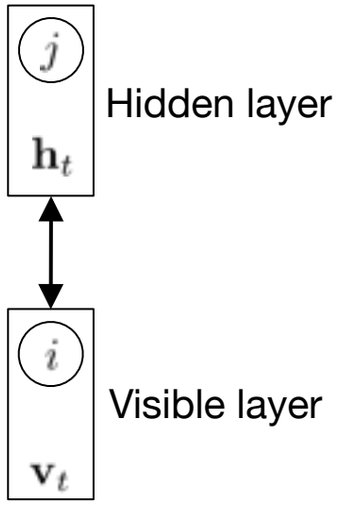

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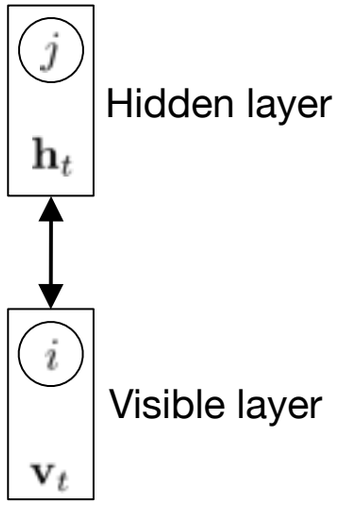
- Start with a Restricted Boltzmann Machine (RBM)

- Add two types of directed connections



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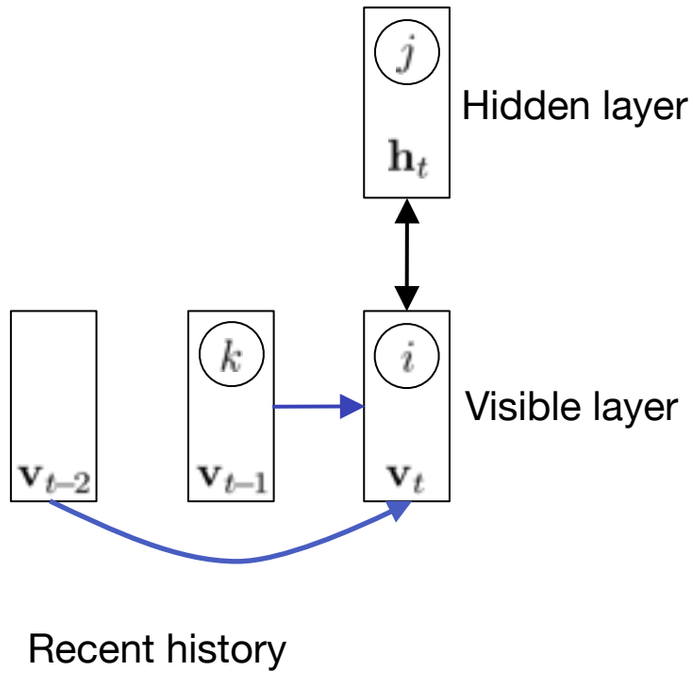

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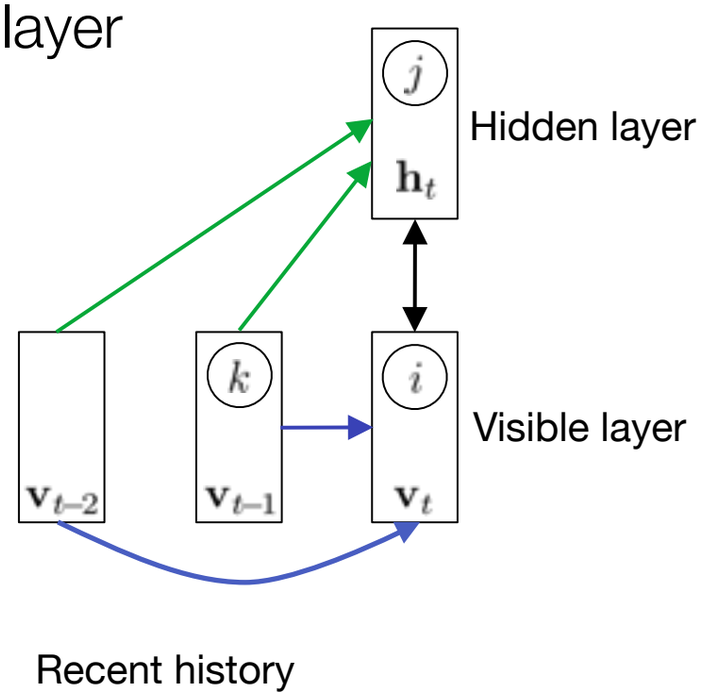

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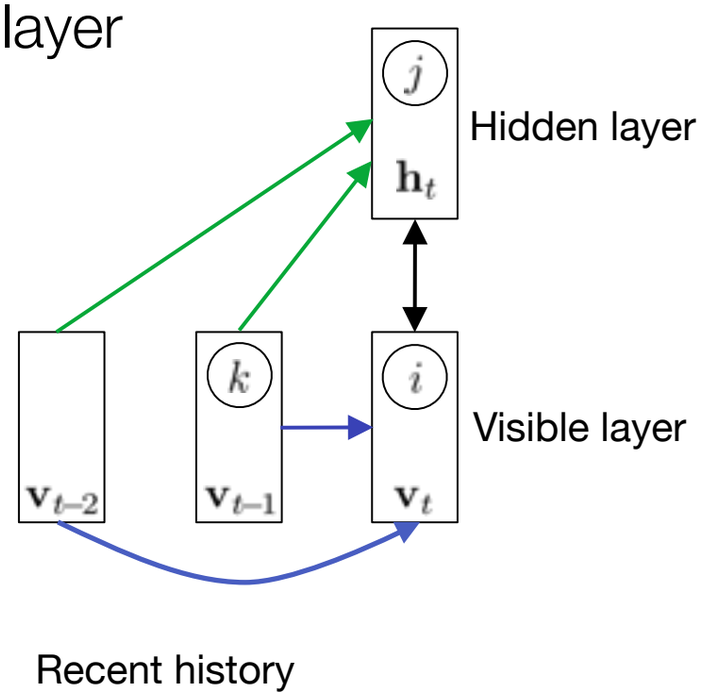
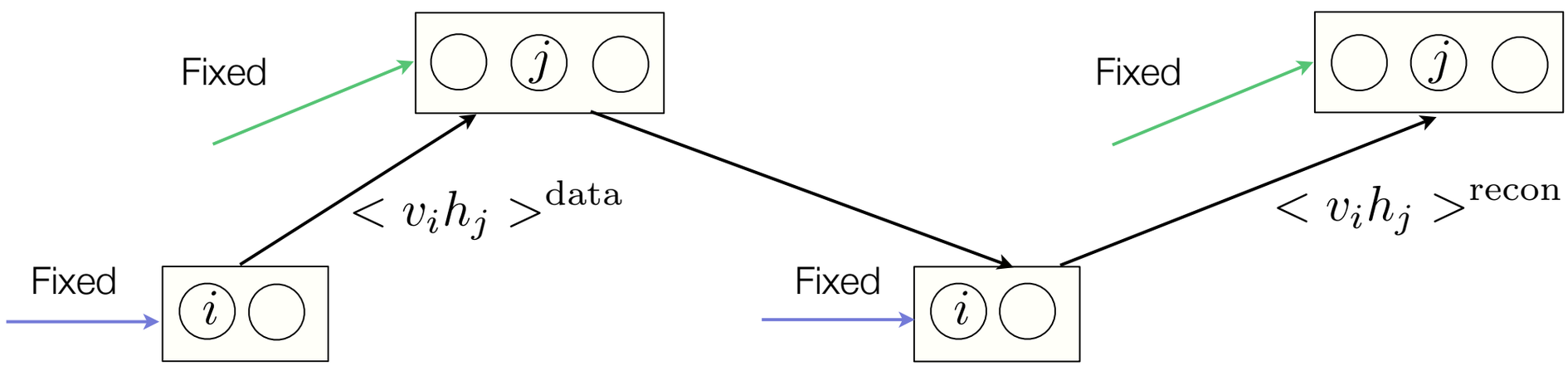
- Conditioning does not change inference nor learning



CONTRASTIVE DIVERGENCE LEARNING



- When updating visible and hidden units, we implement directed connections by treating data from previous time steps as a dynamically changing bias
- Inference and learning do not change

STACKING: THE CONDITIONAL DEEP BELIEF NETWORK

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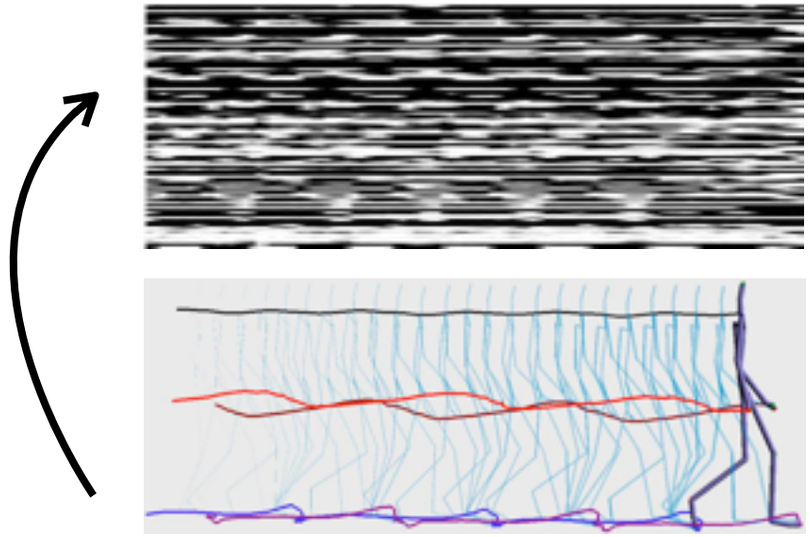
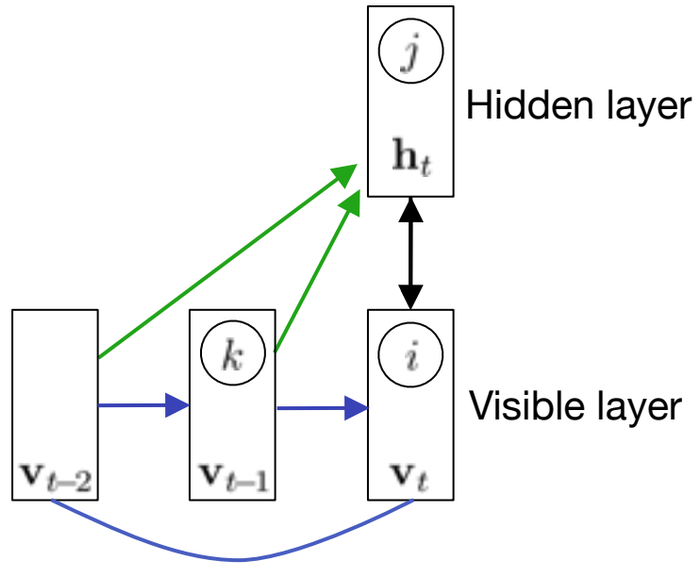
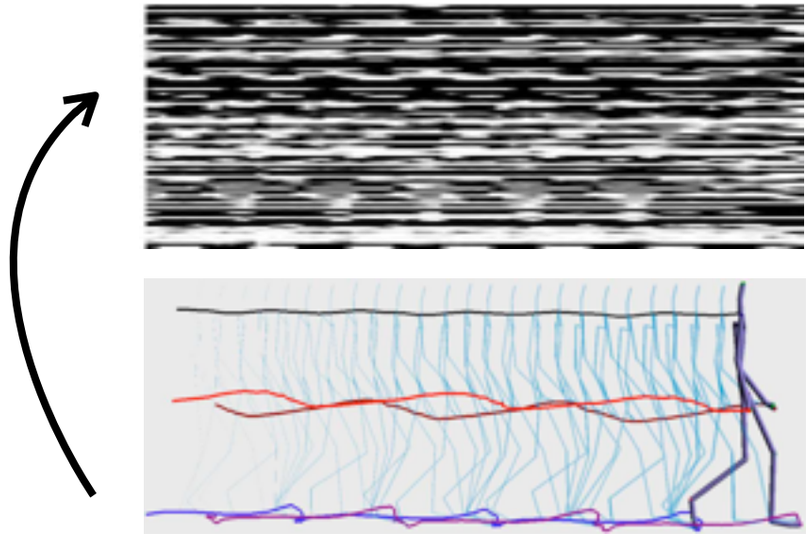
- Learn a CRBM

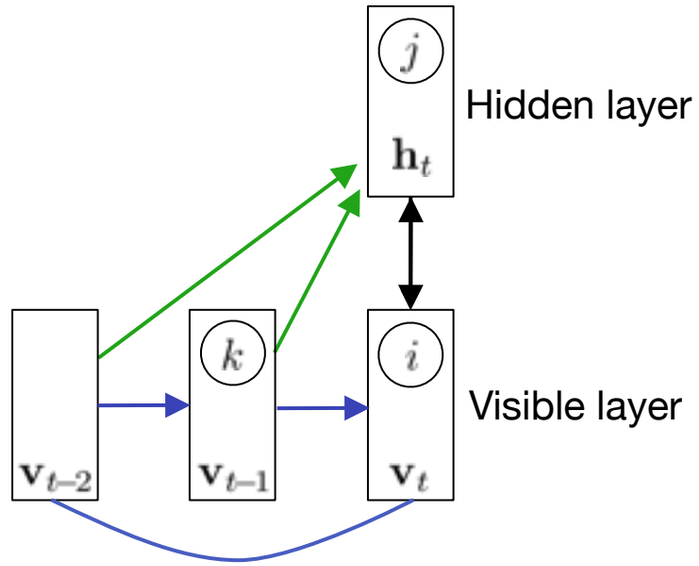




STACKING: THE CONDITIONAL DEEP BELIEF NETWORK

- Learn a CRBM
- Now, treat the sequence of hidden units as “fully observed” data and train a second CRBM





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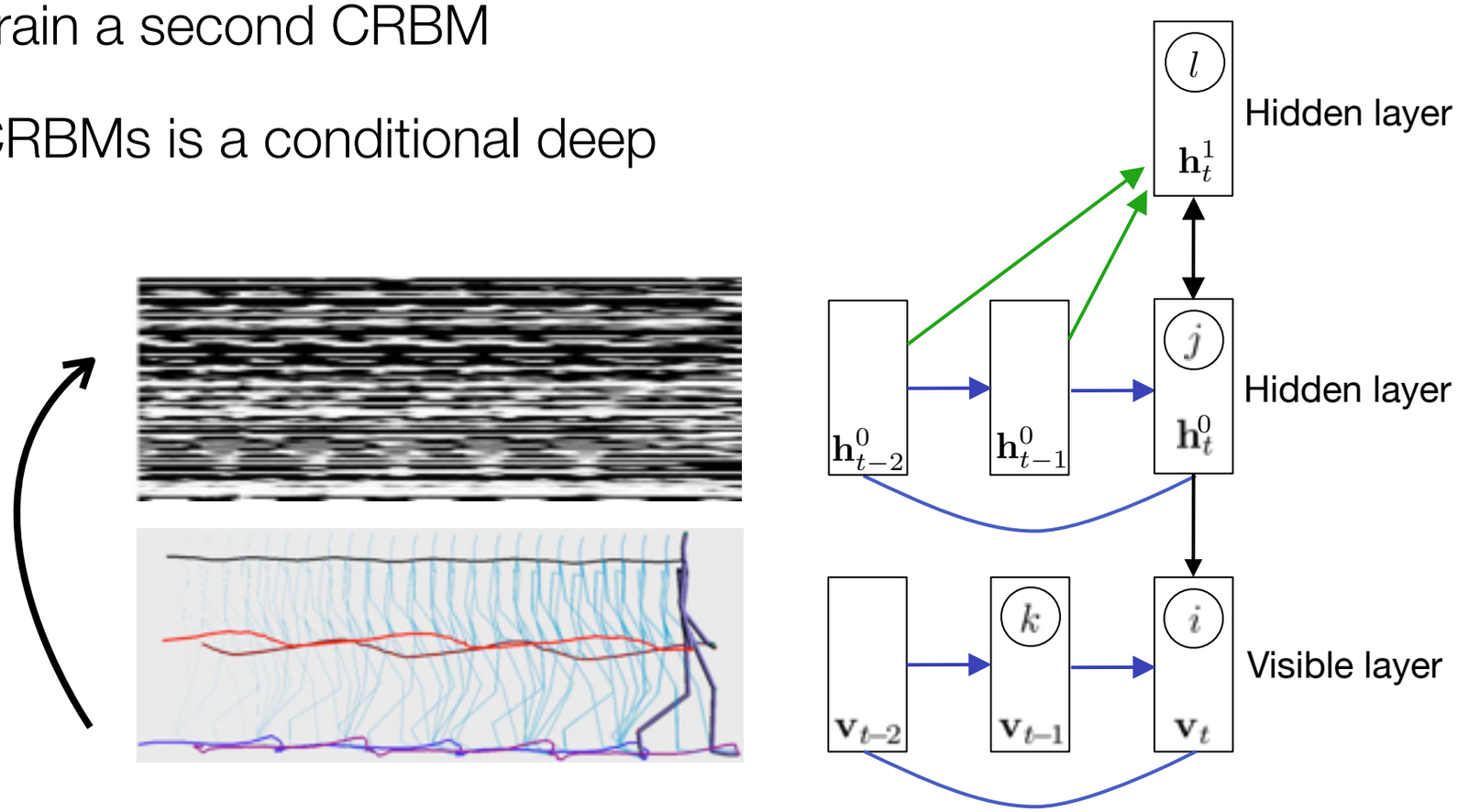
- The composition of CRBMs is a conditional deep belief net



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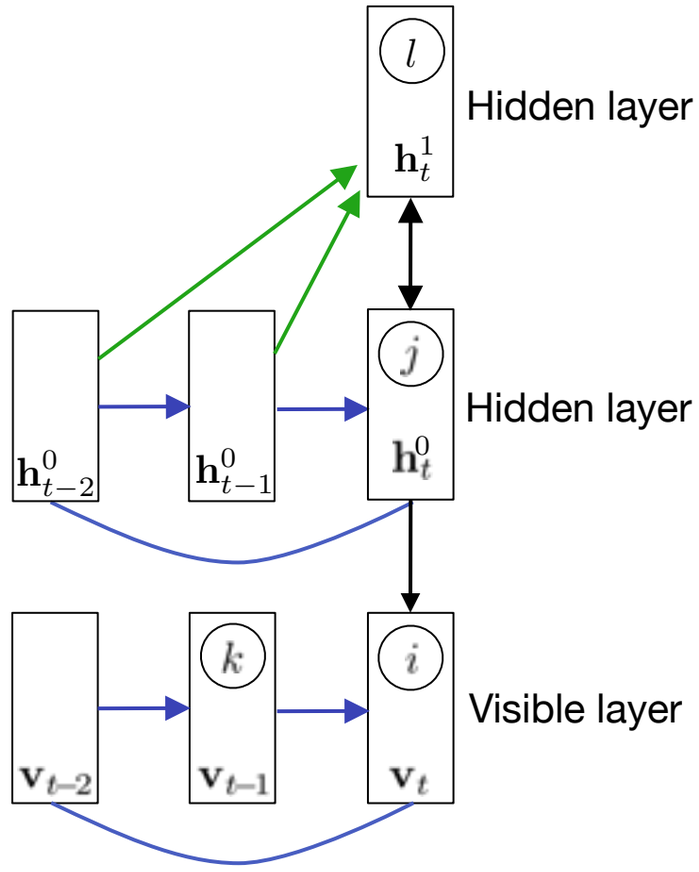
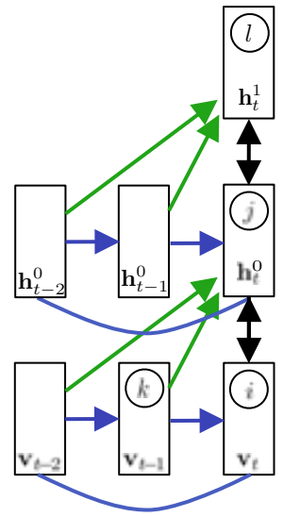
- The composition of CRBMs is a conditional deep belief net
- It can be fine-tuned generatively or discriminatively



MOTION SYNTHESIS WITH A 2-LAYER CDBN



- Model is trained on ~8000 frames of 60fps data (49 dimensions)
- 10 styles of walking: cat, chicken, dinosaur, drunk, gangly, graceful, normal, old-man, sexy and strong
- 600 binary hidden units per layer
- < 1 hour training on a modern workstation

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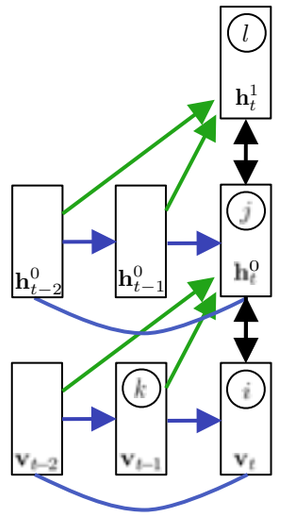

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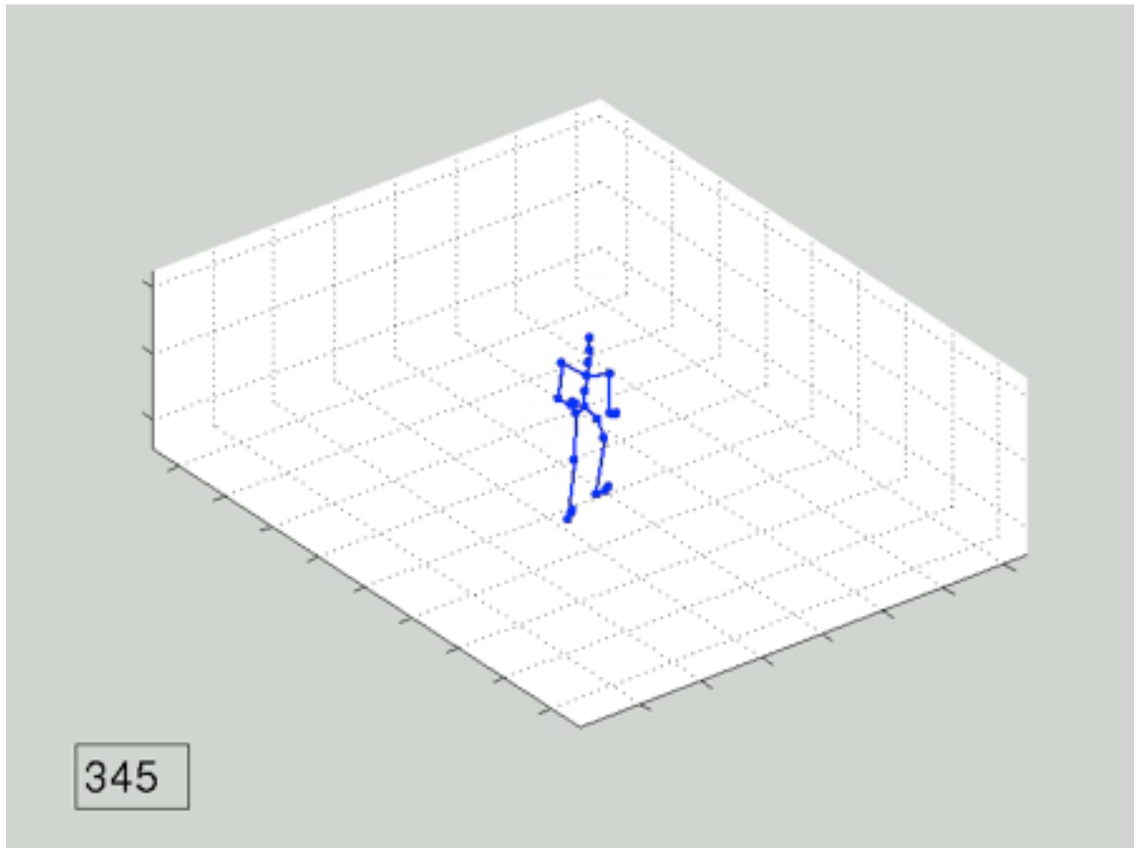
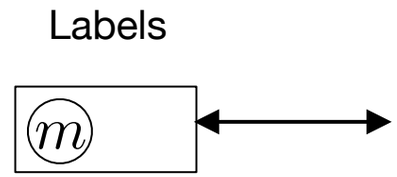


MODELING CONTEXT

- A single model was trained on 10 “styled” walks from CMU subject 137
- The model can generate each style based on initialization
- We cannot prevent nor control transitioning
- How to blend styles?
- Style or person labels can be provided as part of the input to the top layer



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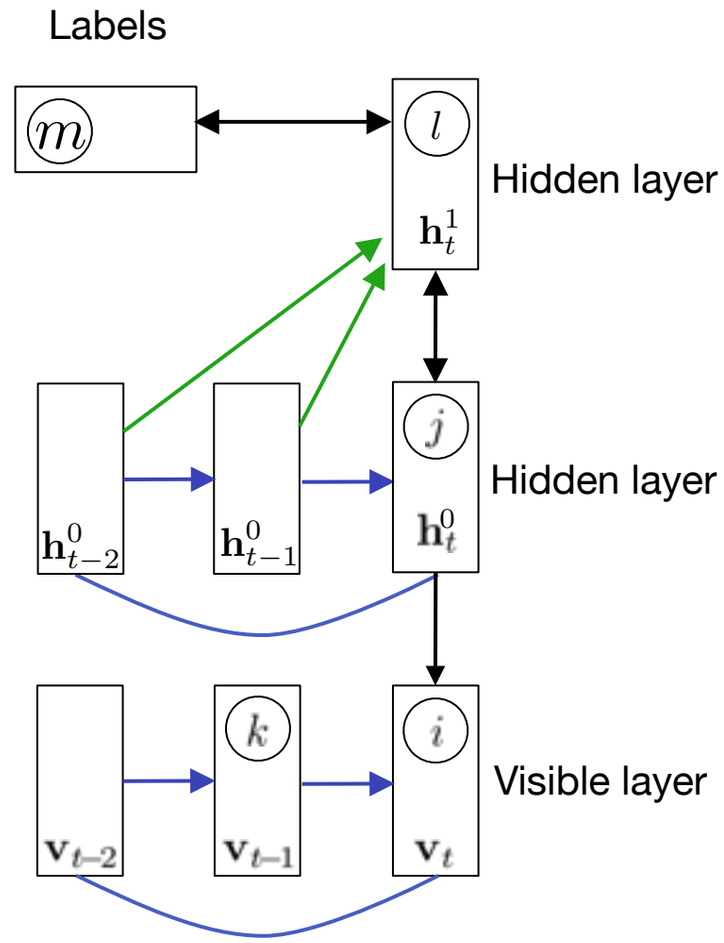
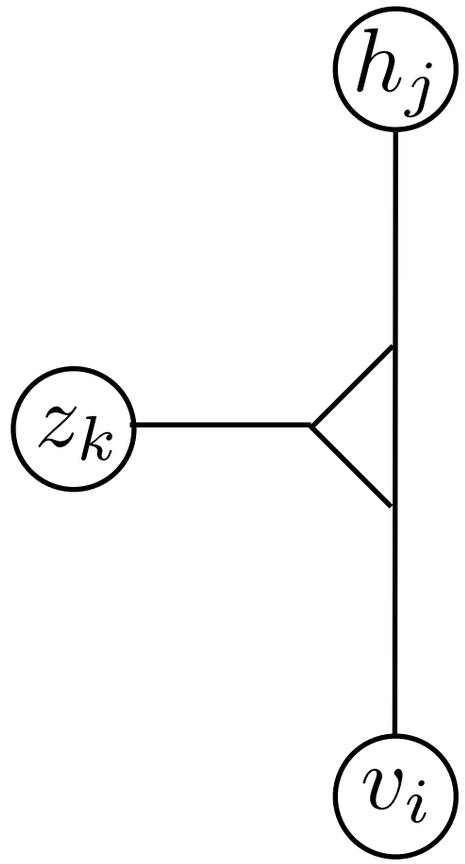


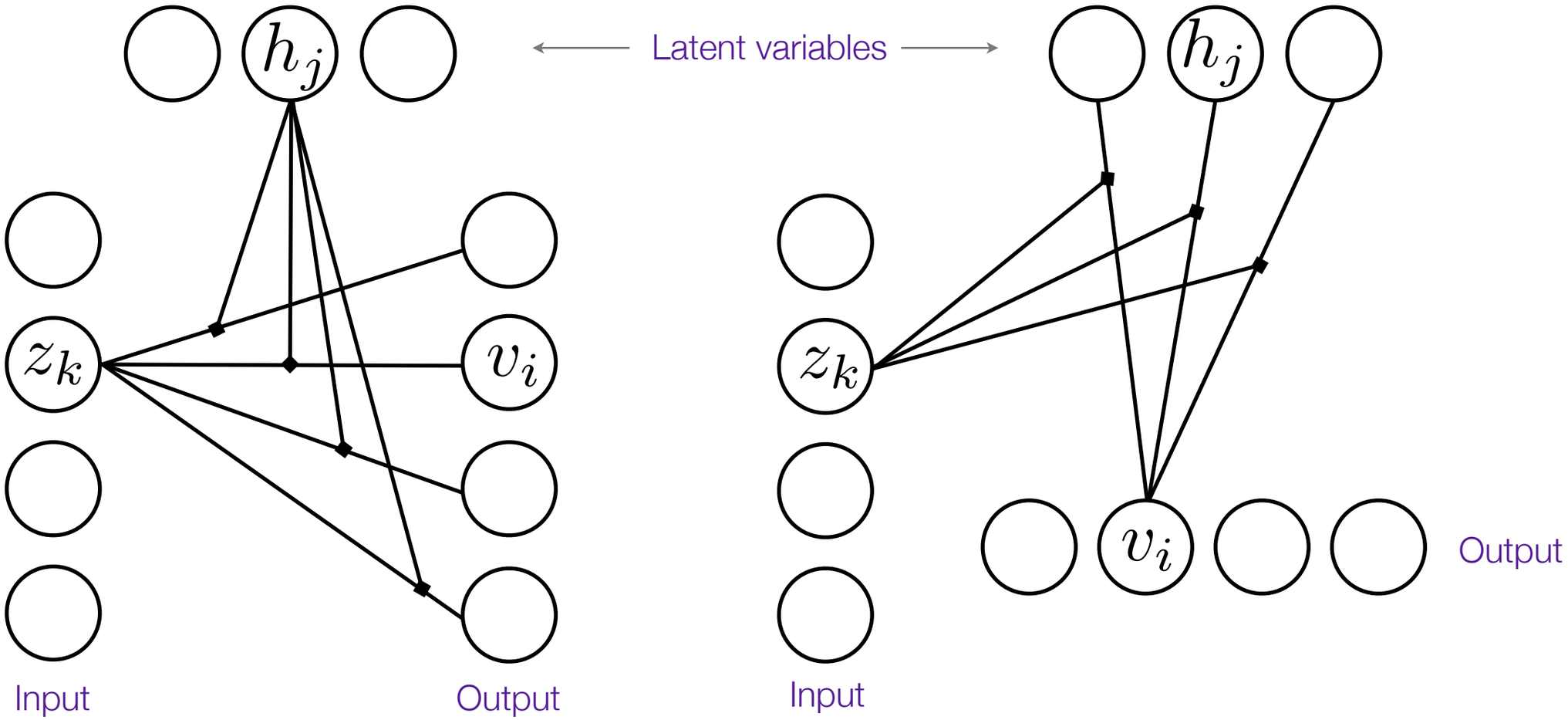
MULTIPLICATIVE INTERACTIONS

- Let latent variables act like *gates*, that dynamically change the connections between other variables
- This amounts to letting variables multiply connections between other variables: *three-way multiplicative interactions*
- Recently used in the context of learning *correspondence* between images (Memisevic & Hinton 2007, 2010) but long history before that



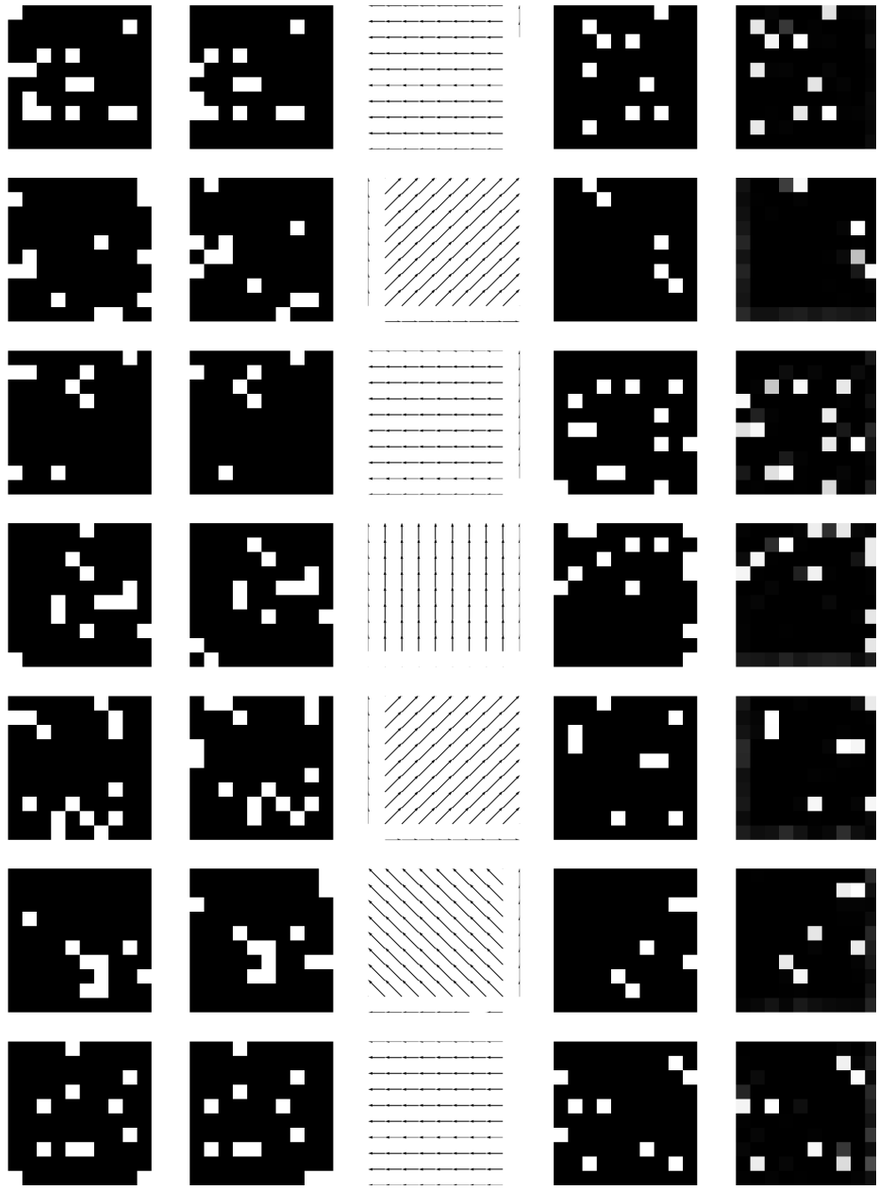
GATED RESTRICTED BOLTZMANN MACHINES (GRBM)

Two views: Memisevic & Hinton (2007)



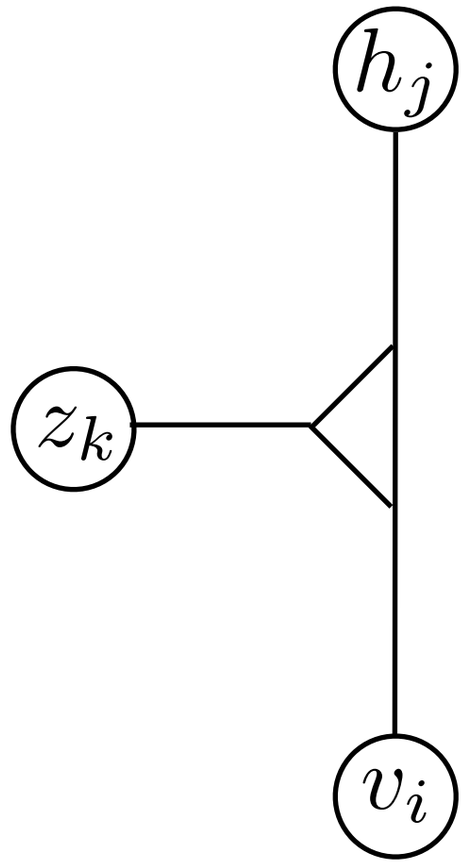
INFERRING OPTICAL FLOW: IMAGE “ANALOGIES”

- Toy images (Memisevic & Hinton 2006)
- No structure in these images, only *how they change*
- Can infer optical flow from a pair of images and apply it to a random image



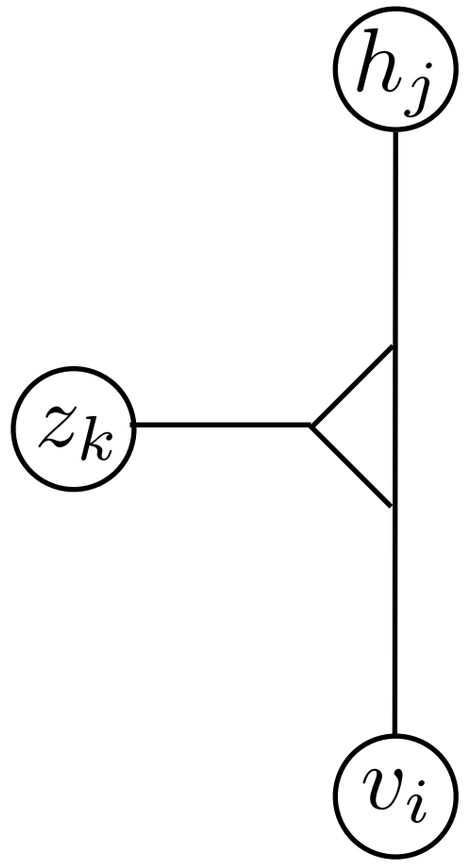
BACK TO MOTION STYLE

- Introduce a set of latent “context” variables whose value is known at training time
- In our example, these represent “motion style” but could also represent height, weight, gender, etc.
- The contextual variables gate every existing pairwise connection in our model



LEARNING AND INFERENCE

- Learning and inference remain almost the same as in the standard CRBM
- We can think of the context or style variables as "blending in" a whole "sub-network"
- This allows us to share parameters across styles but selectively adapt dynamics



SUPERVISED MODELING OF STYLE

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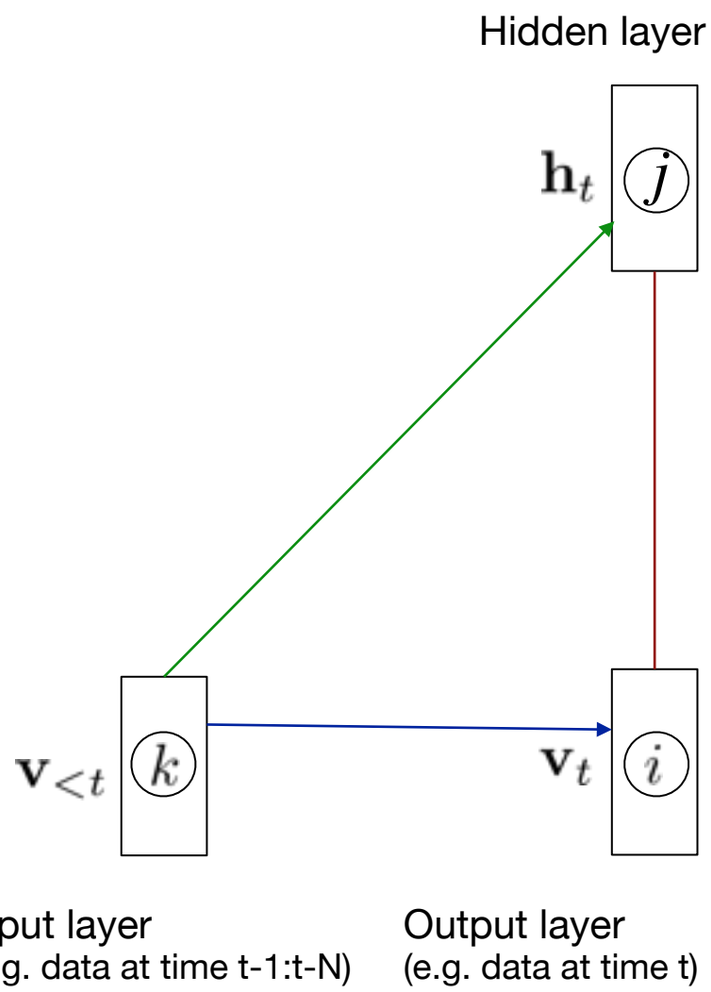

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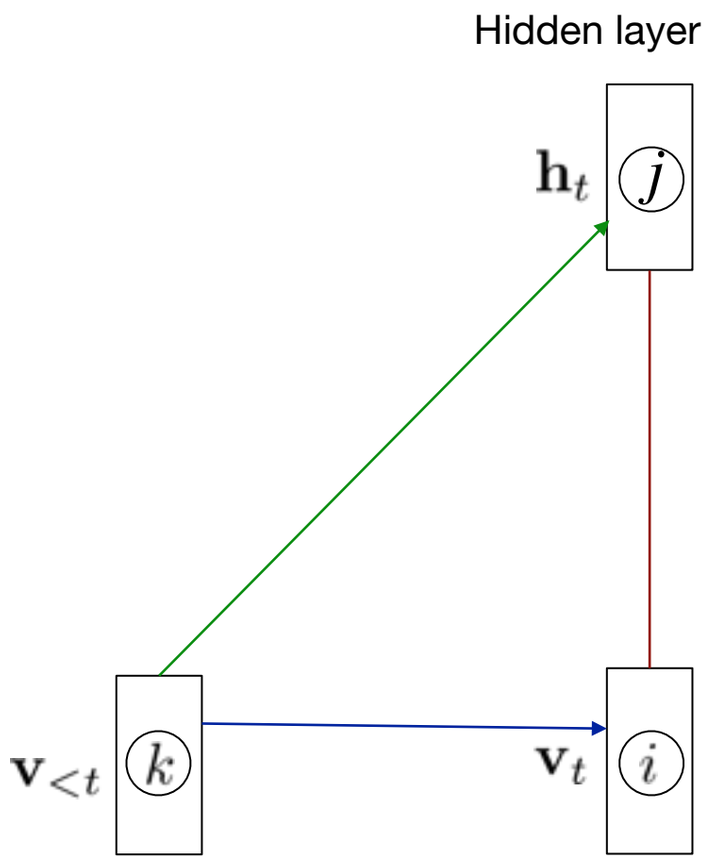

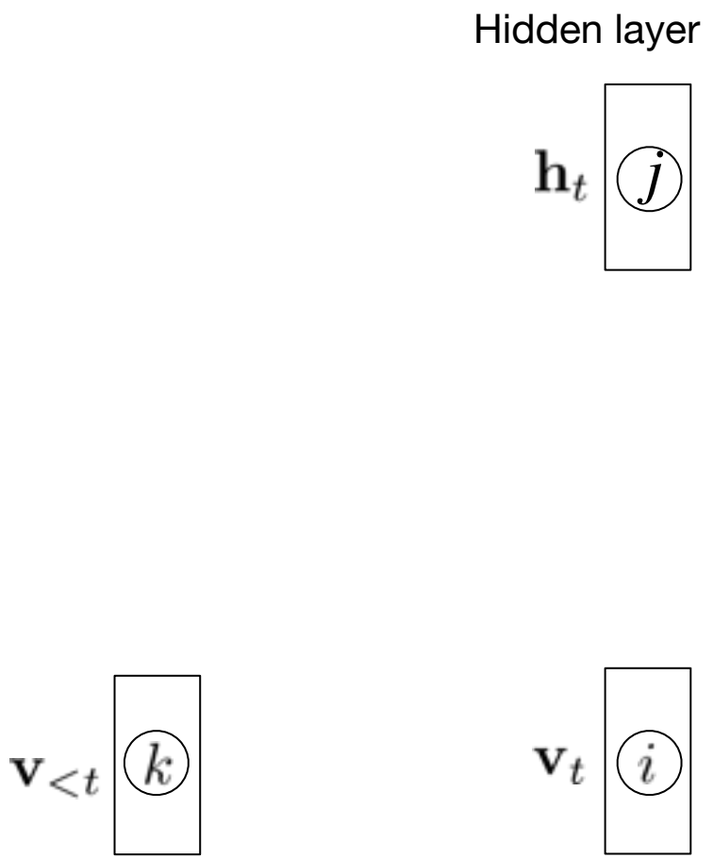

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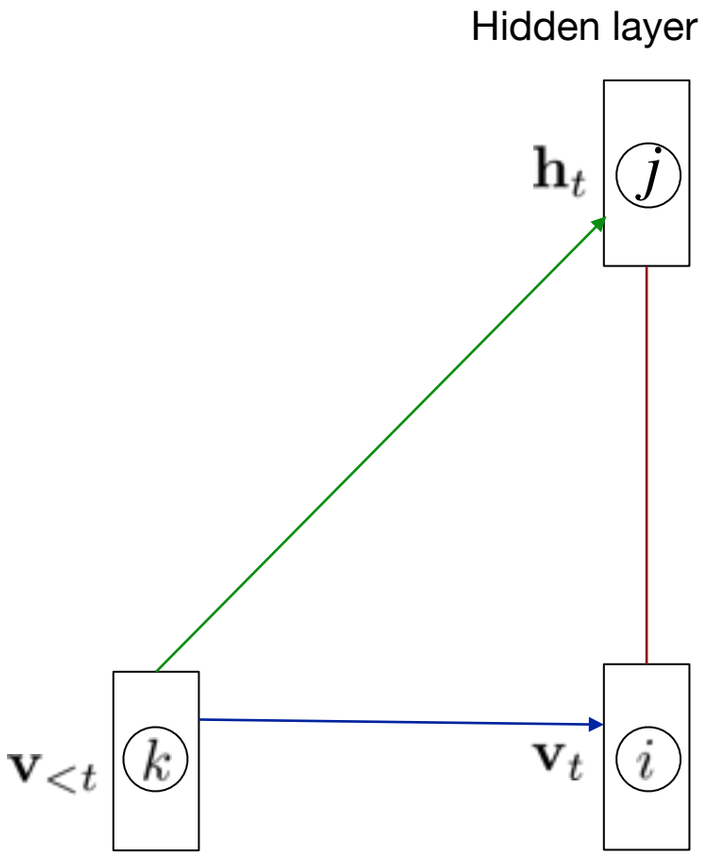

Input layer
(e.g. data at time t-1:t-N)

Output layer
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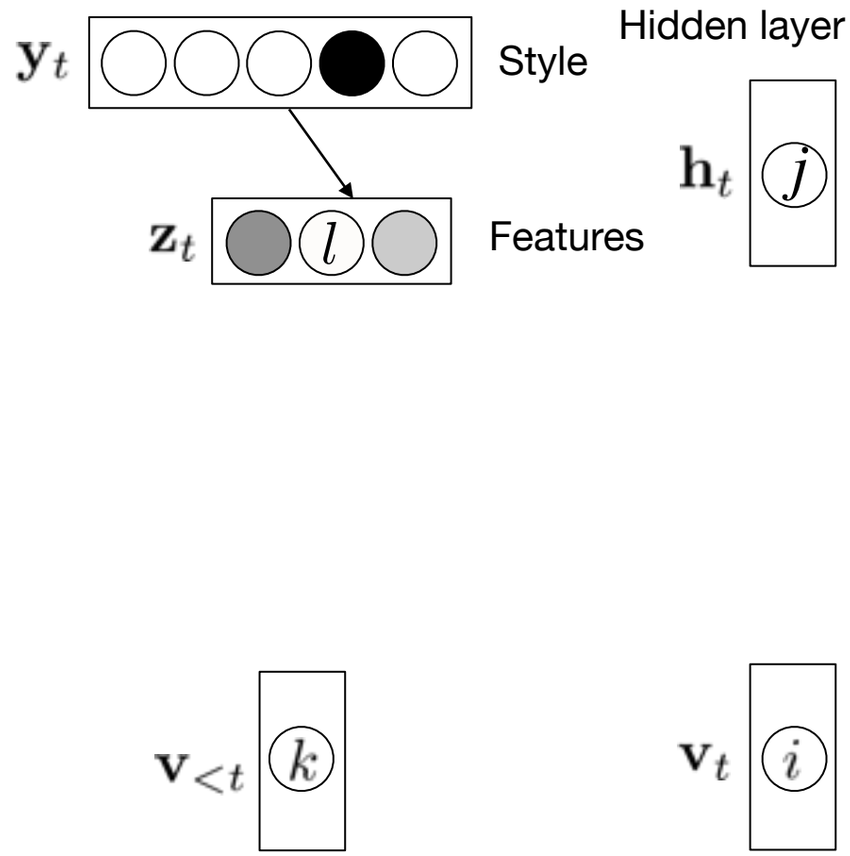

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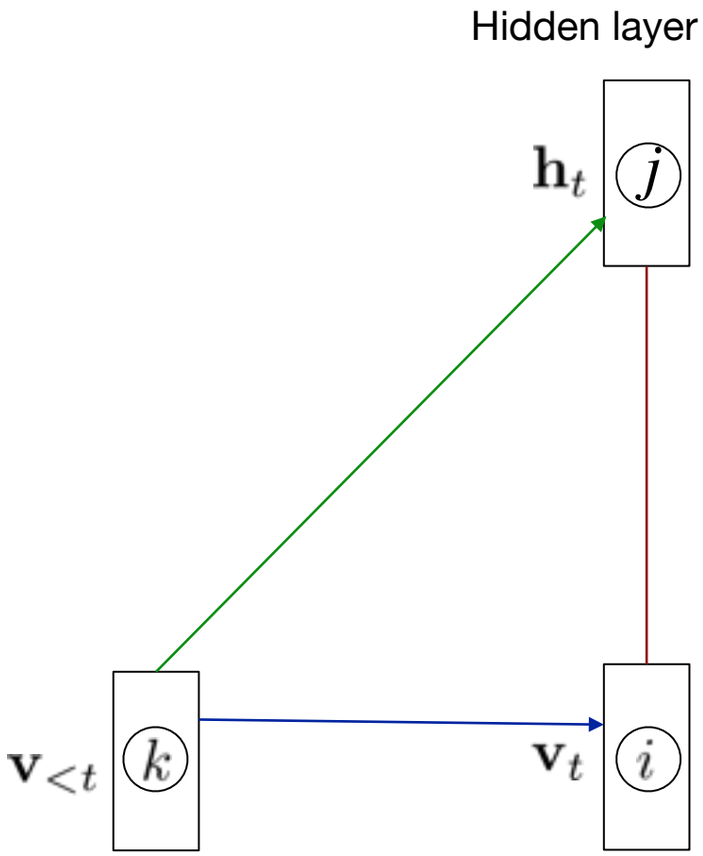

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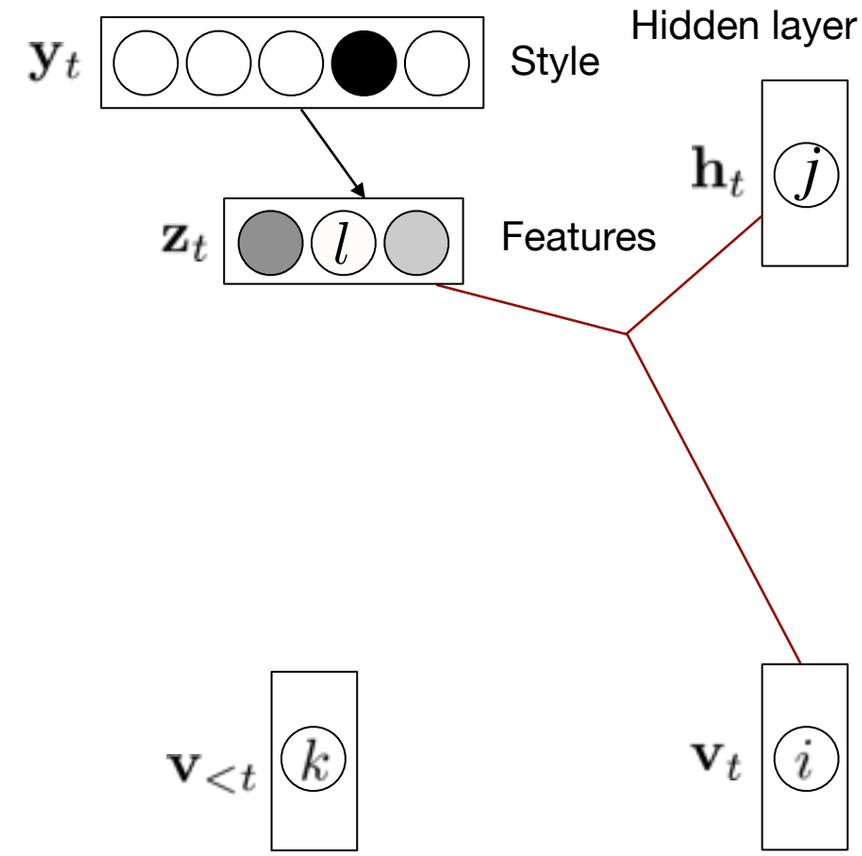

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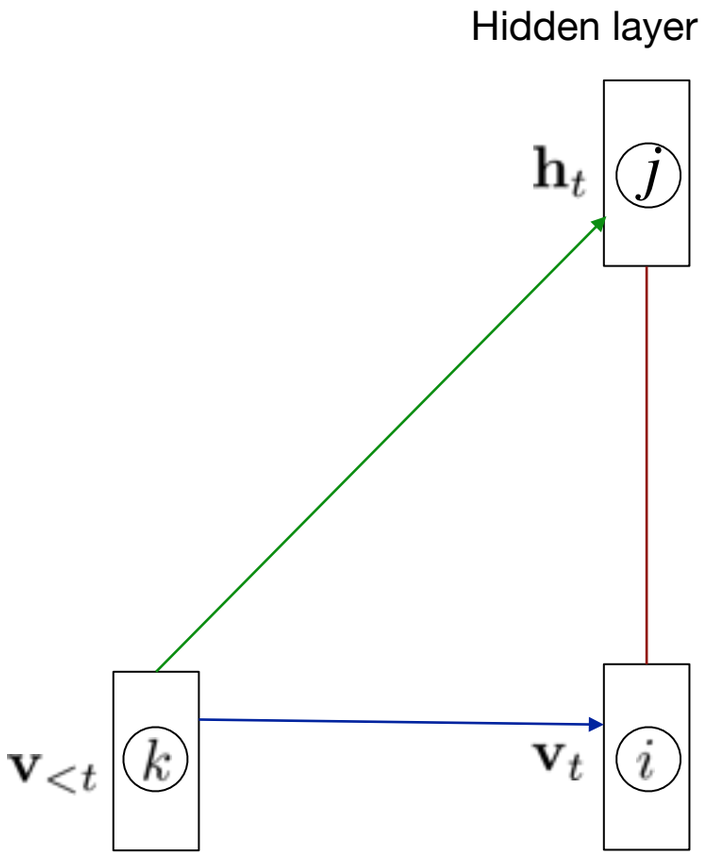

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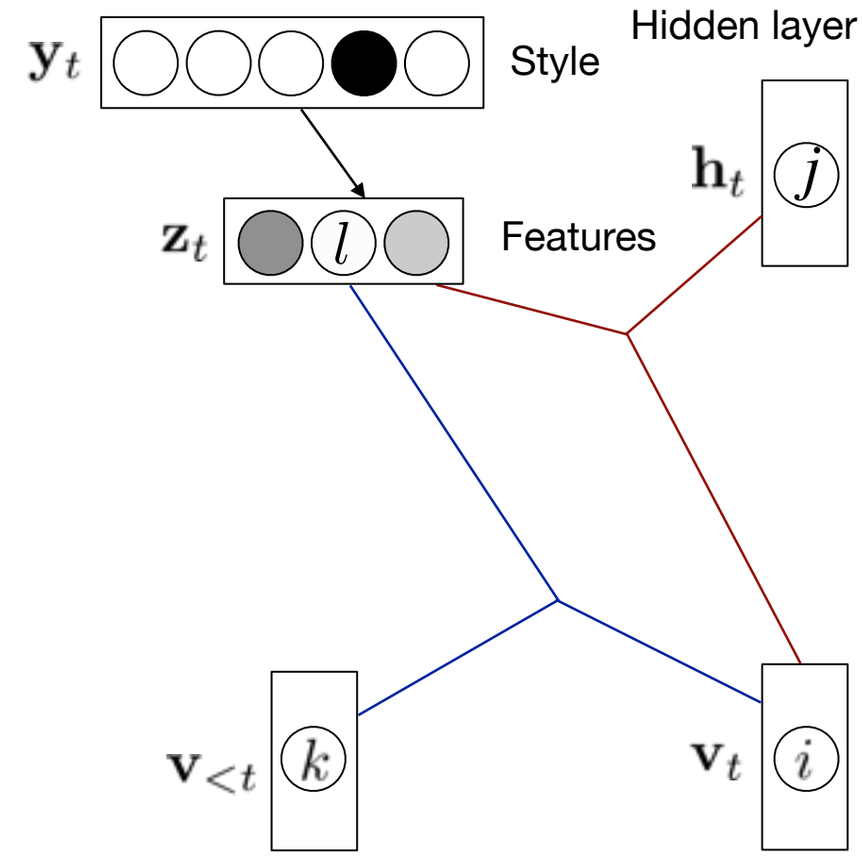

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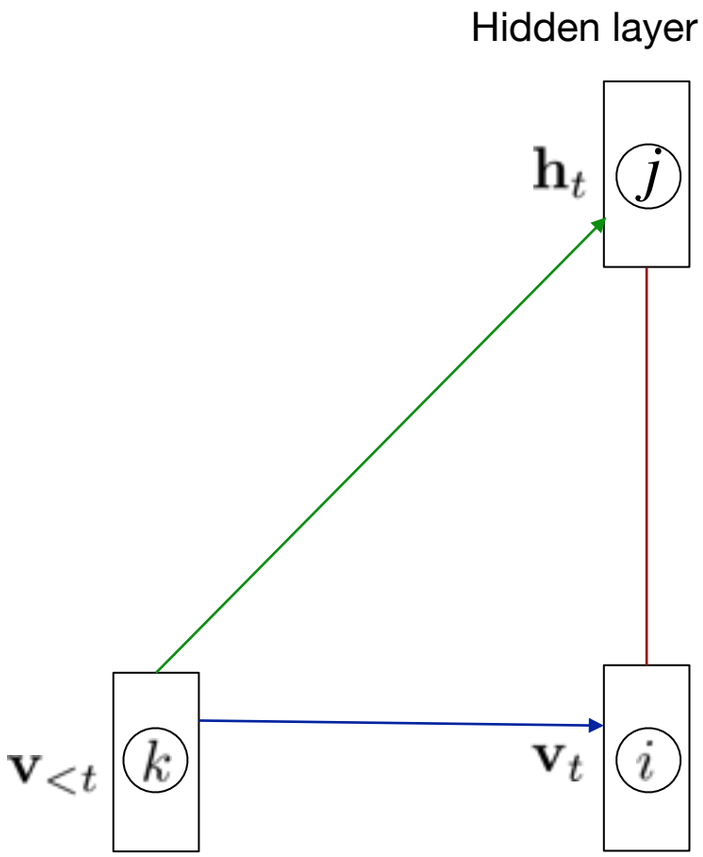

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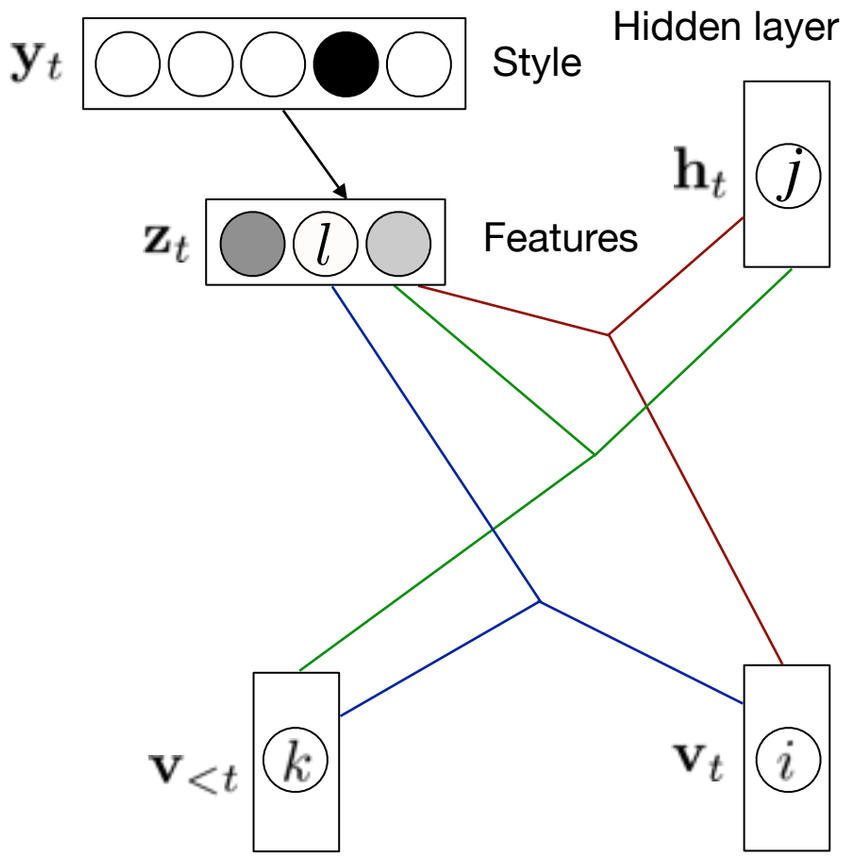

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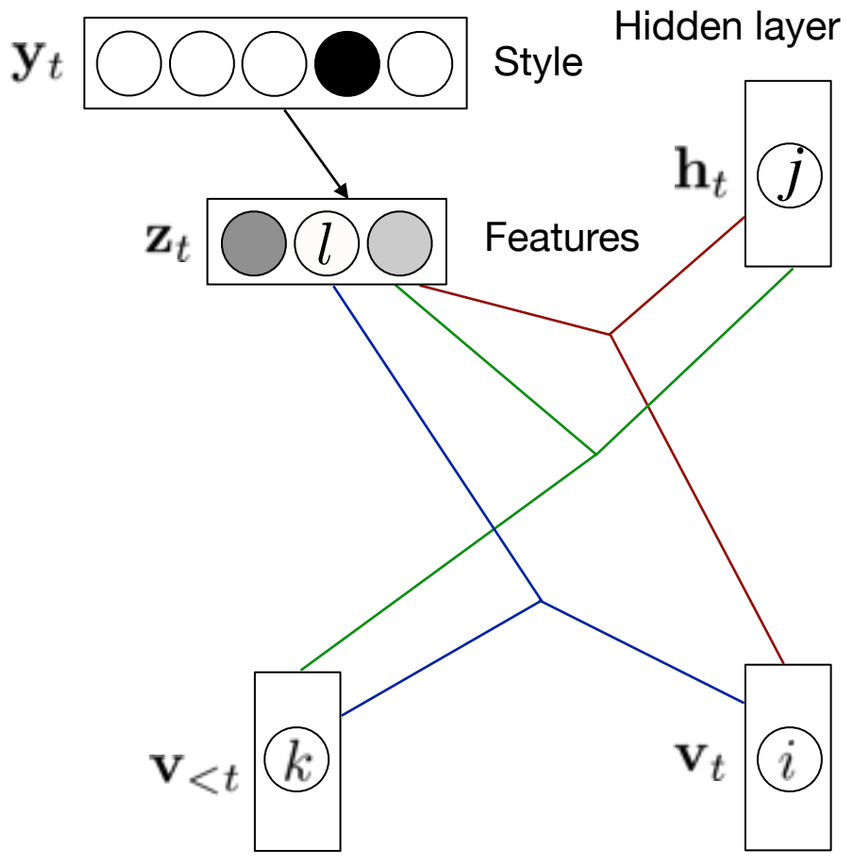
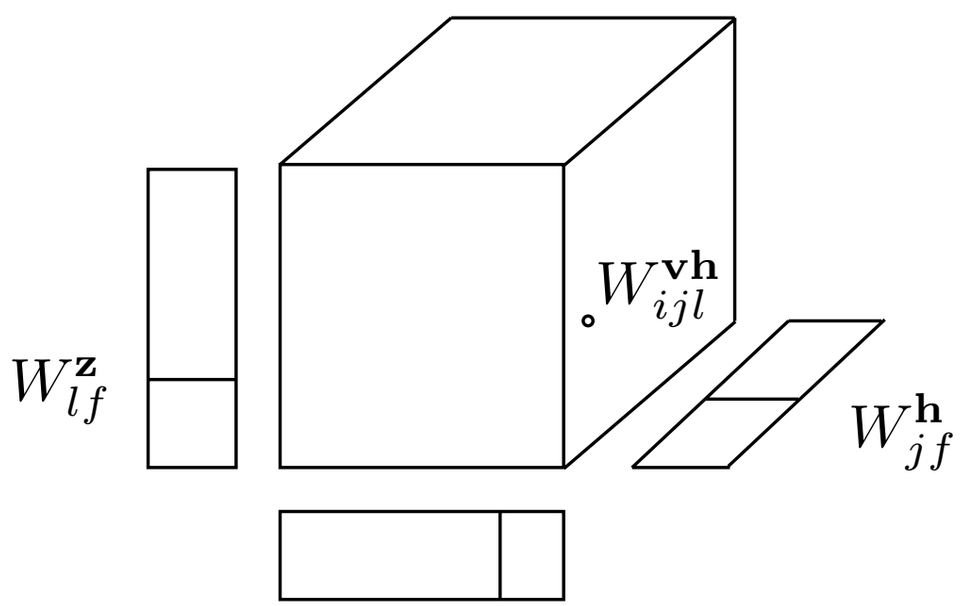
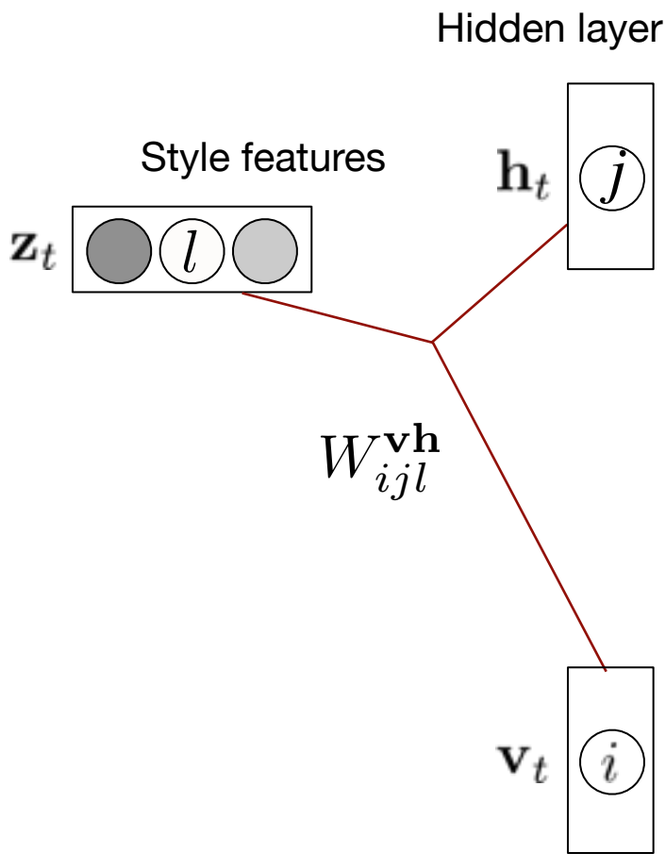
OVERPARAMETERIZATION

- Note: weight Matrix $W^{\mathbf{v},\mathbf{h}}$ has been replaced by a tensor $W^{\mathbf{v},\mathbf{h},\mathbf{z}}$! (Likewise for other weights)
- The number of parameters is $O(N^3)$ - per group of weights
- More, if we want sparse, overcomplete hiddens
- However, there is a simple yet powerful solution!



FACTORING





$$W^{\mathbf{vh}}_{ijl} = \sum_f W^{\mathbf{v}}_{if} W^{\mathbf{h}}_{jf} W^{\mathbf{z}}_{lf}$$

(Figure adapted from Roland Memisevic)

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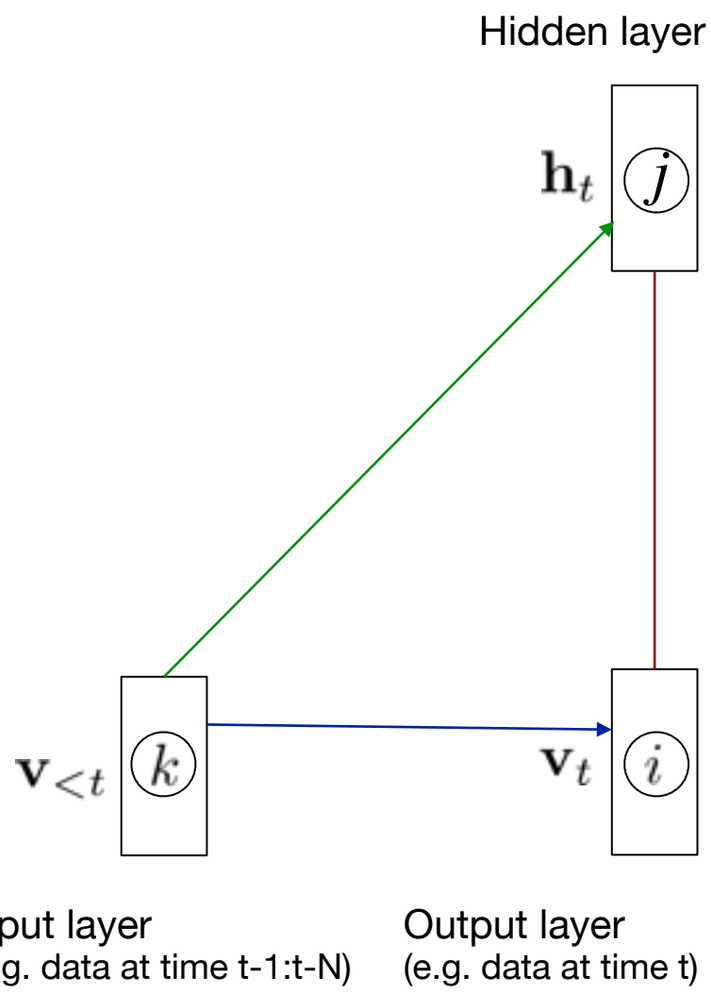

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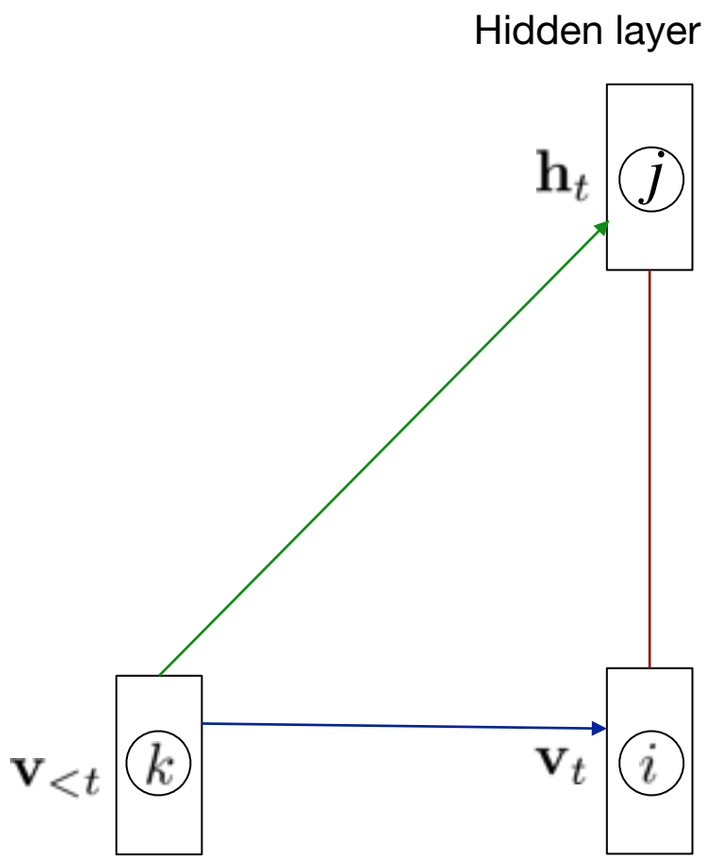

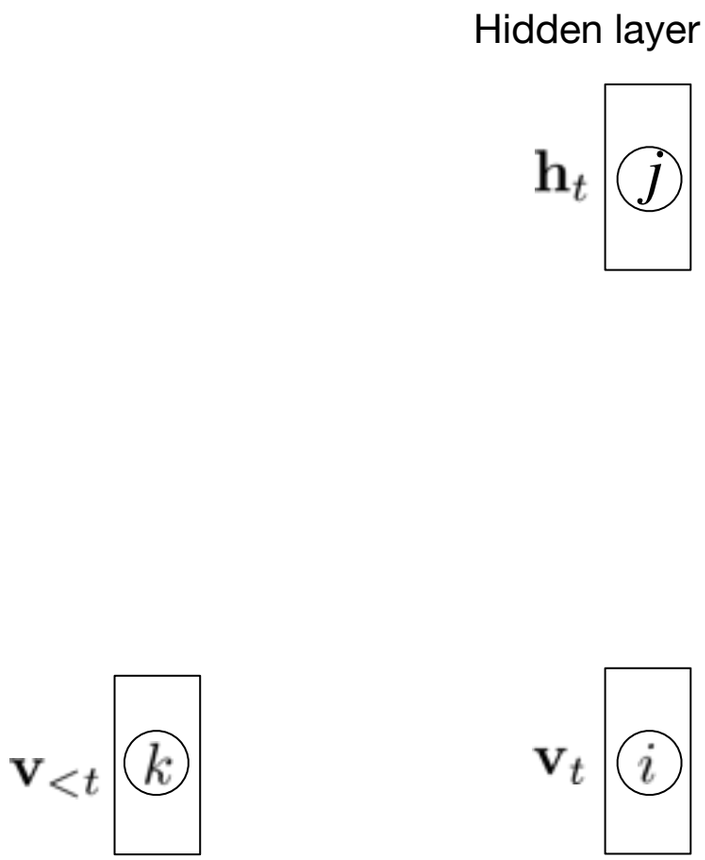

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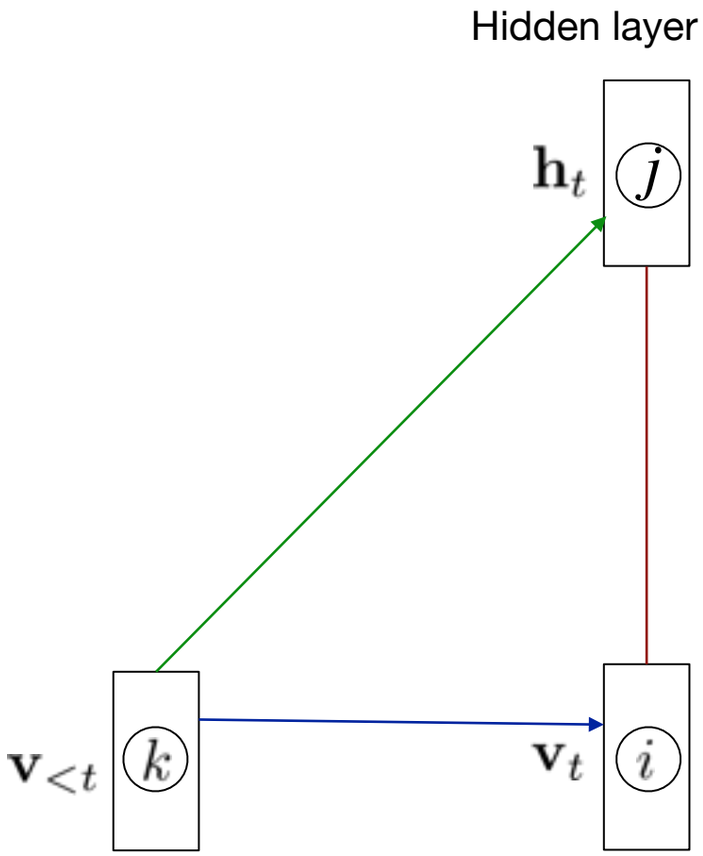
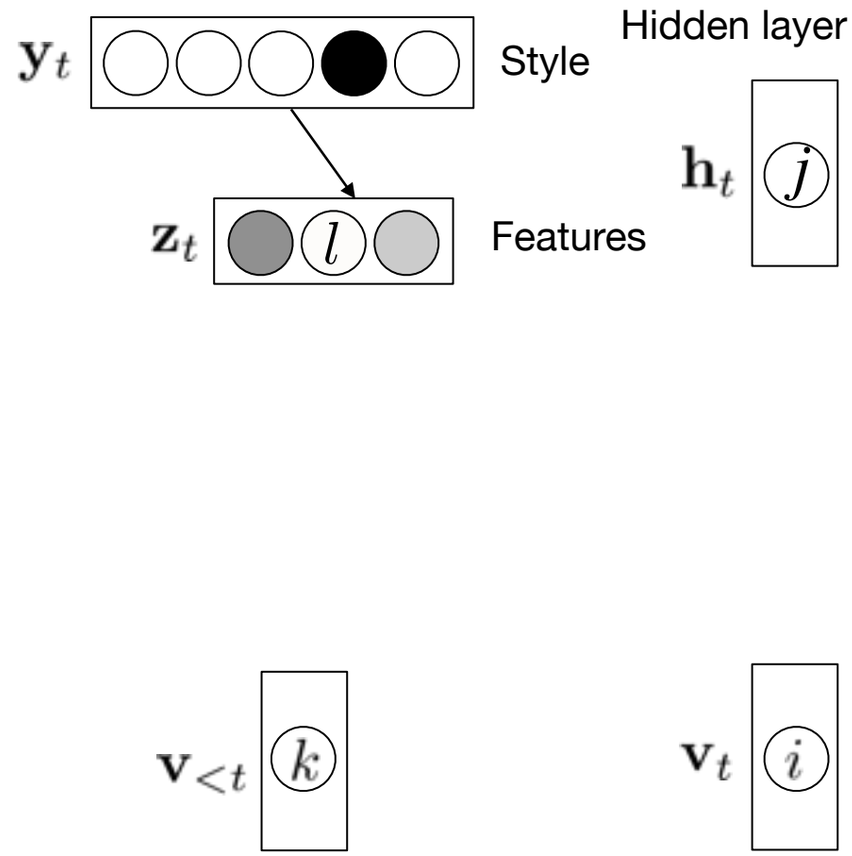


Input layer
(e.g. data at time t-1:t-N)

Output layer
(e.g. data at time t)



Input layer
(e.g. data at time t-1:t-N)

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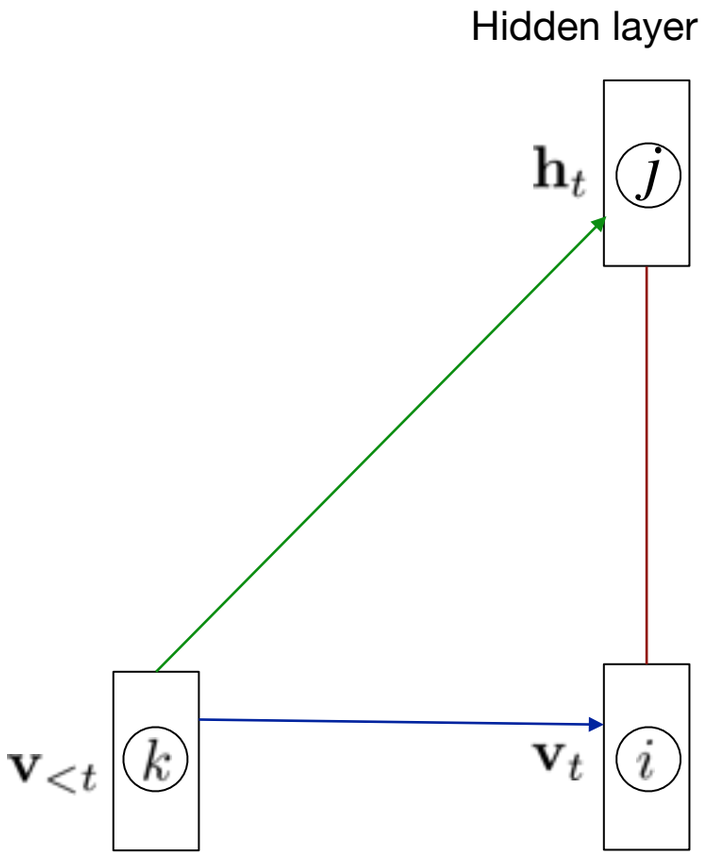

Input layer
(e.g. data at time t-1:t-N)

Output layer
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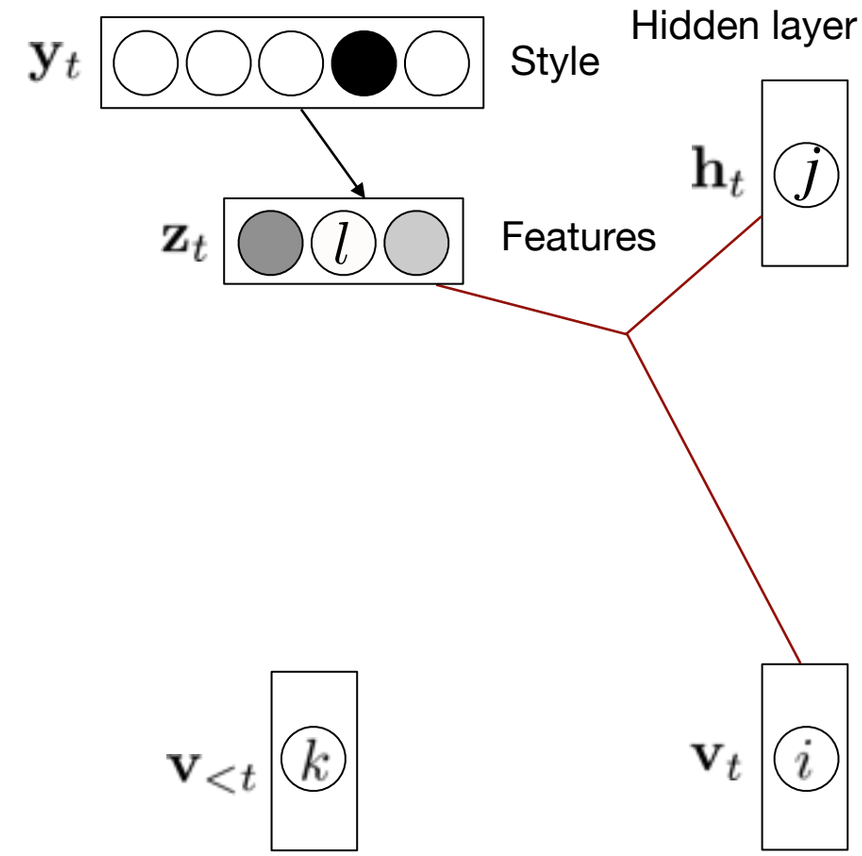

Input layer
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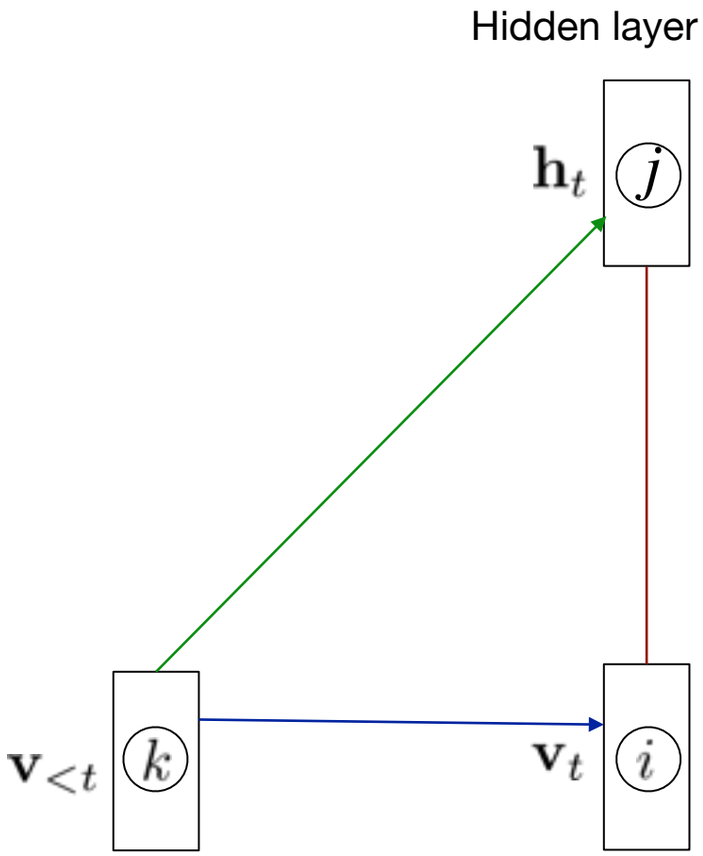

Input layer
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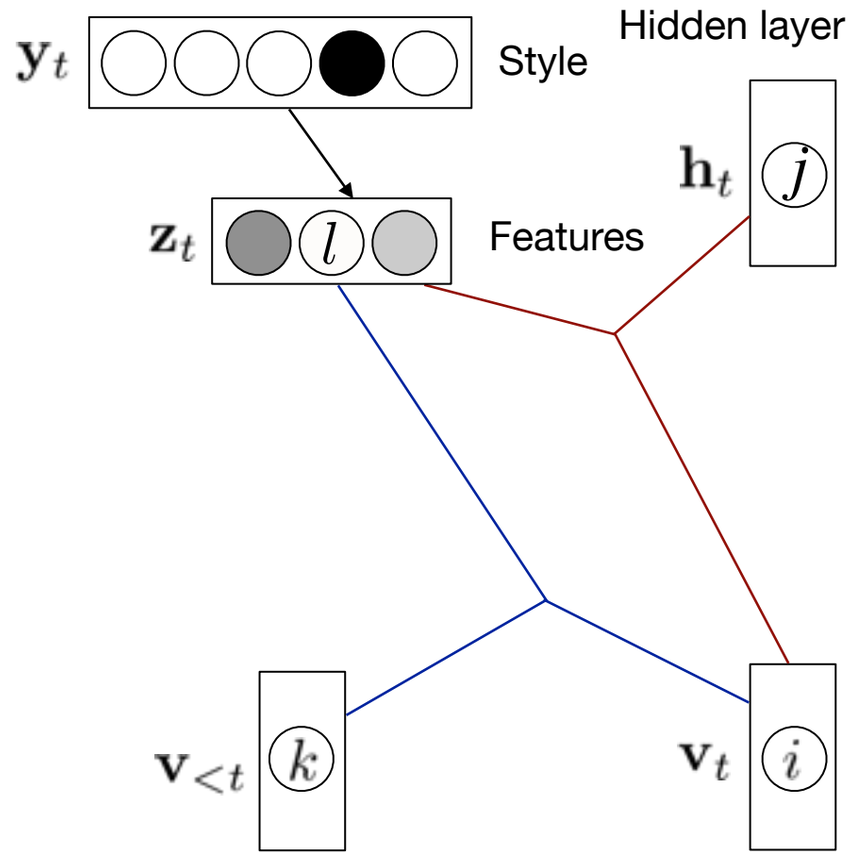

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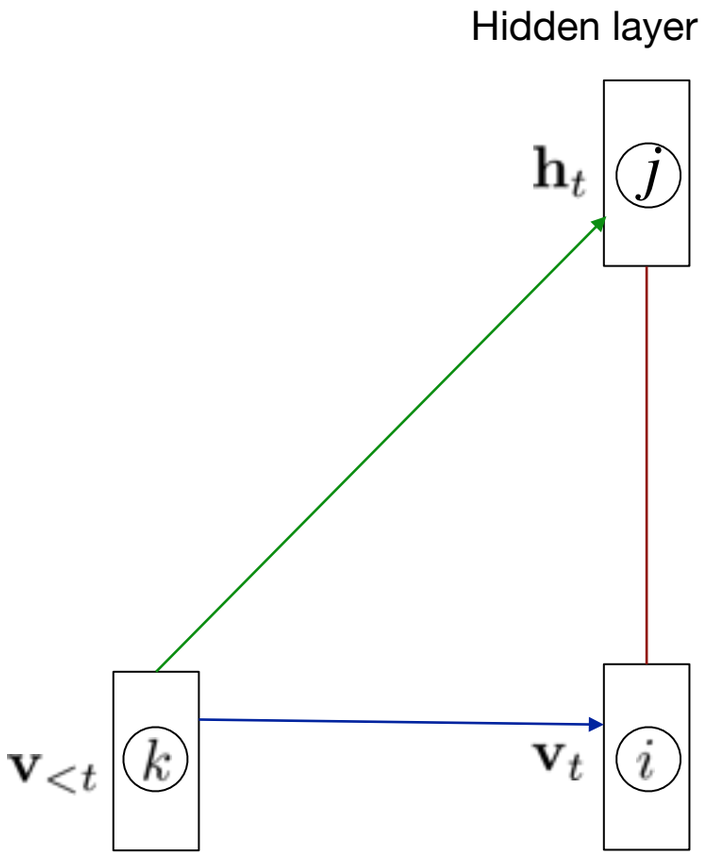

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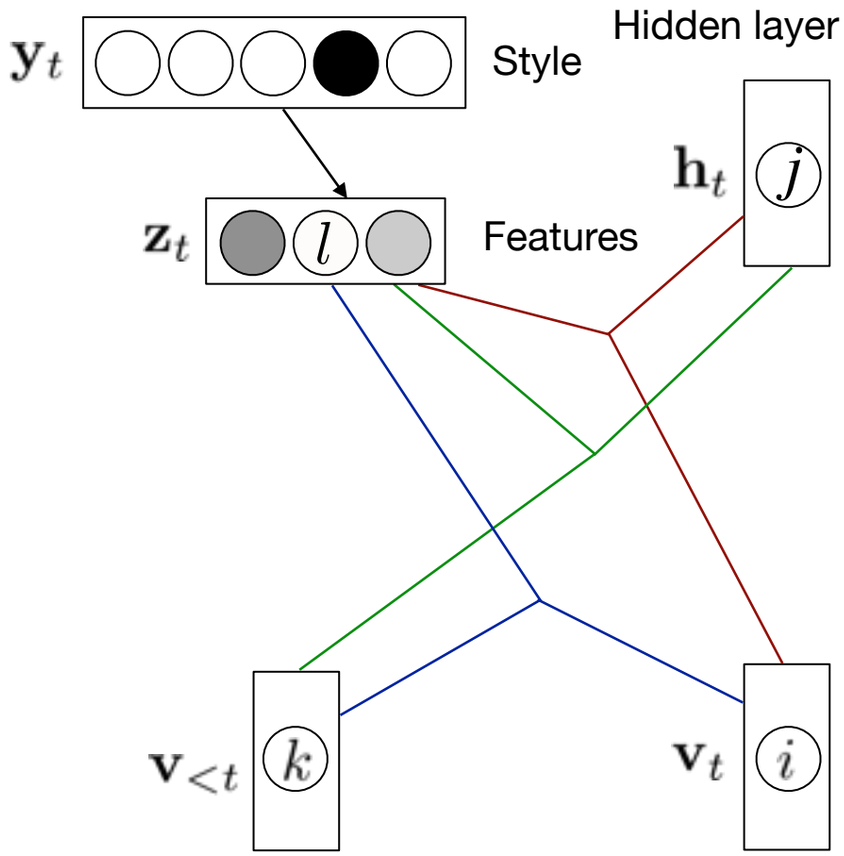

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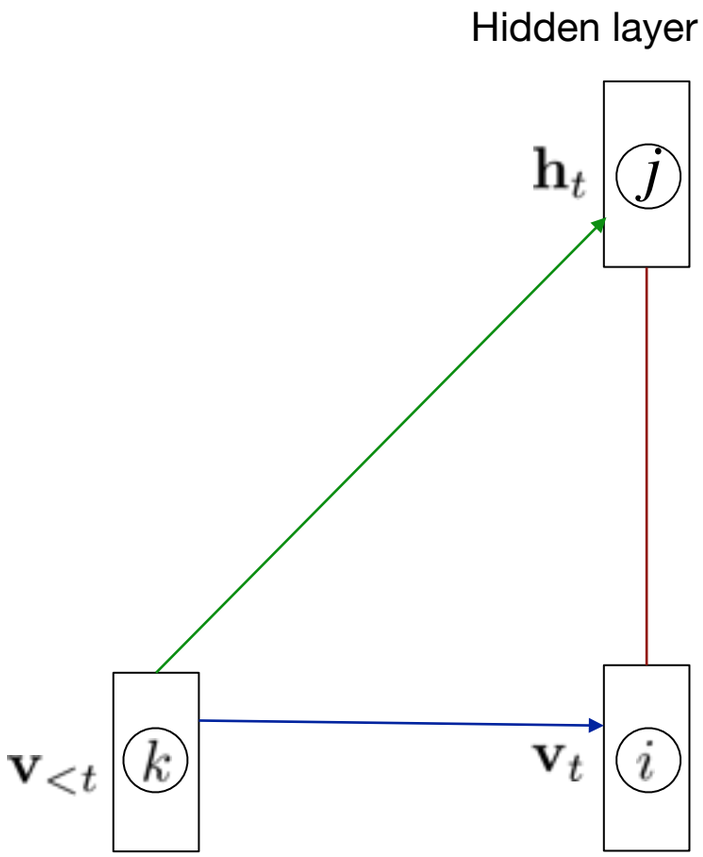

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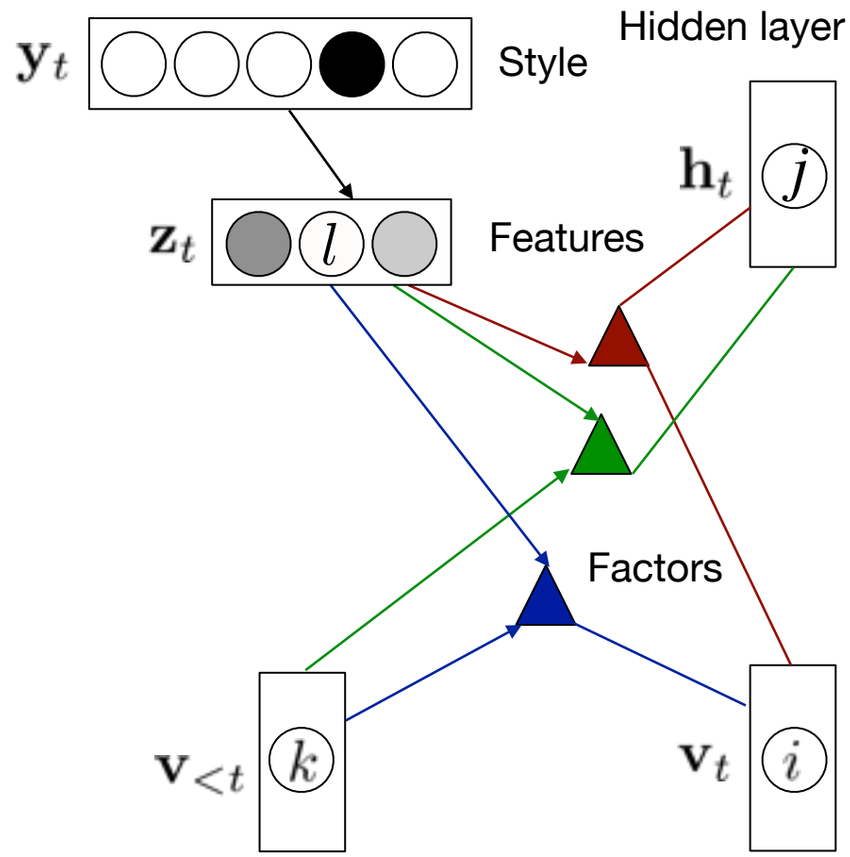

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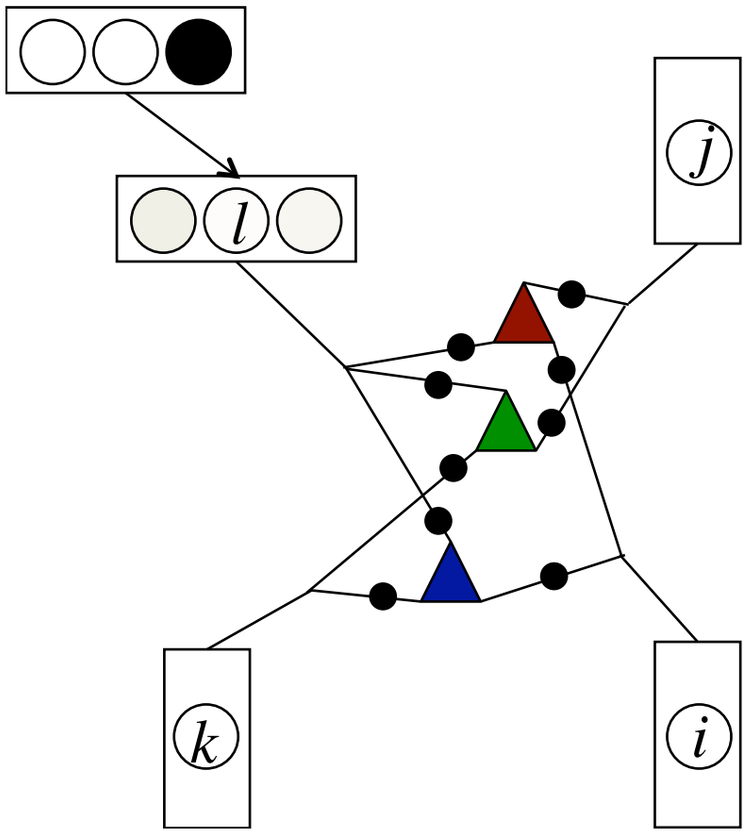
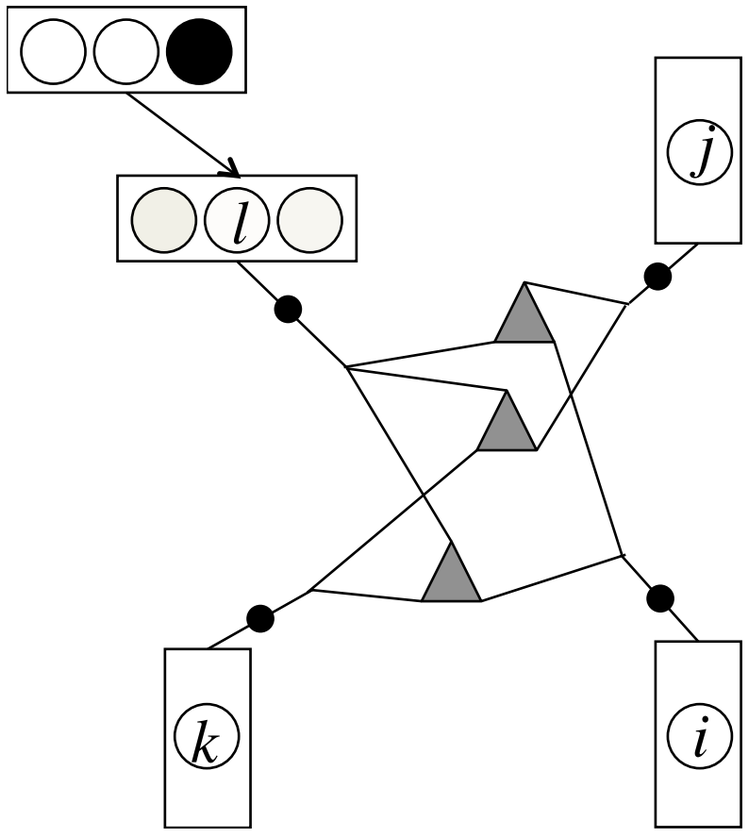
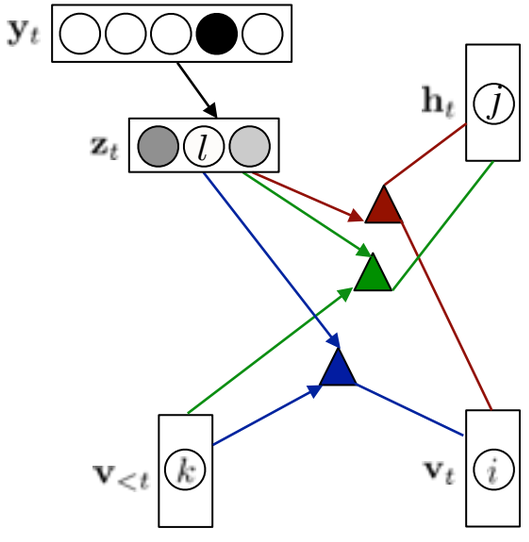
PARAMETER SHARING





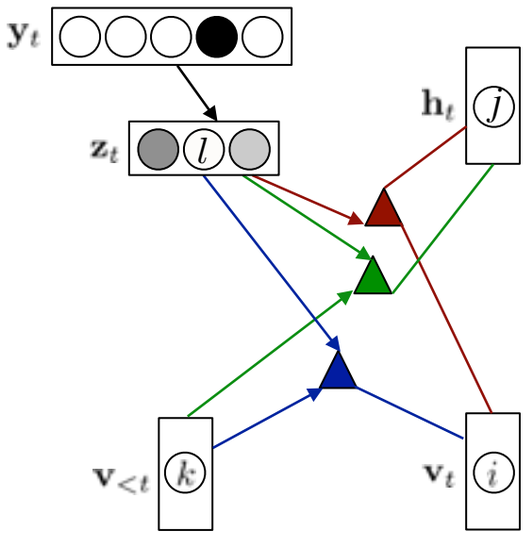
MOTION SYNTHESIS: FACTORED 3RD-ORDER CRBM



- Same 10-styles dataset
- 600 binary hidden units
- 3×200 deterministic factors
- 100 real-valued style features
- < 1 hour training on a modern workstation
- Synthesis is real-time

Summary

MOTION SYNTHESIS: FACTORED 3RD-ORDER CRBM



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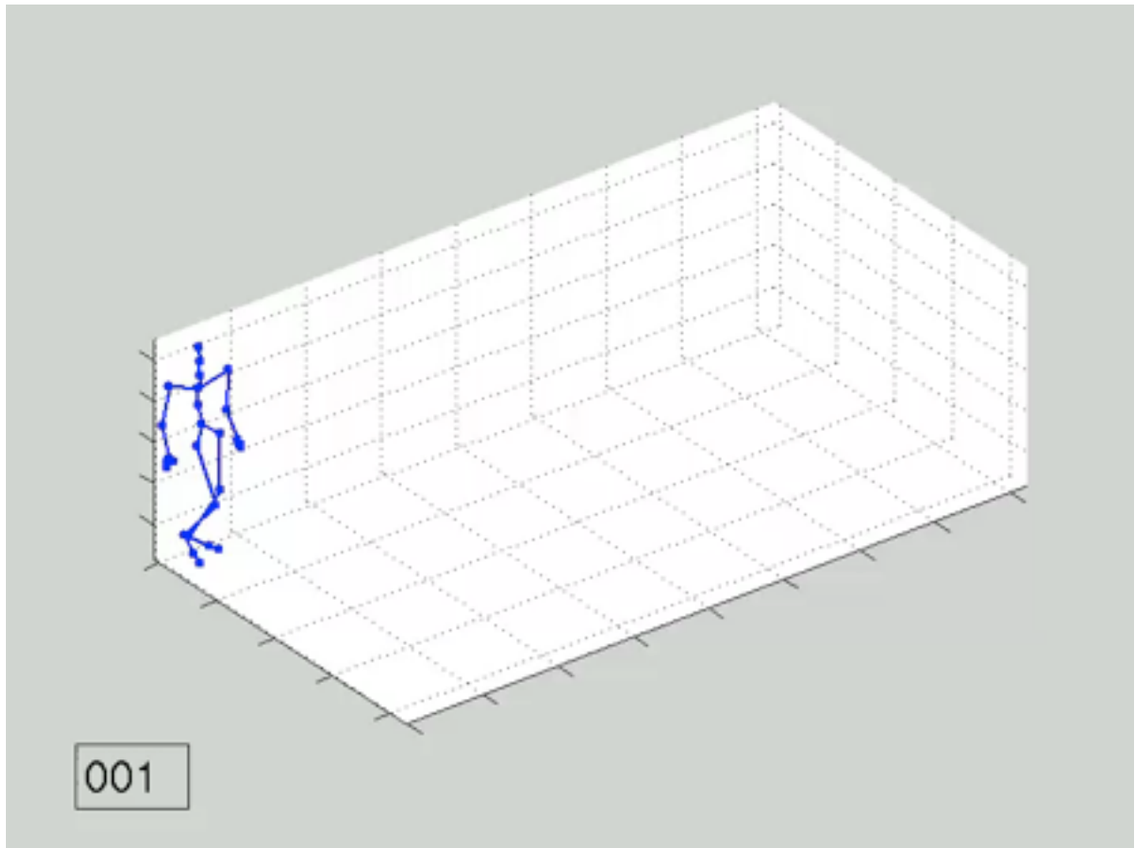
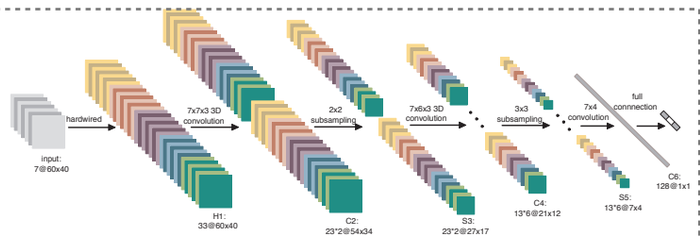


Summary

ACTIVITY RECOGNITION

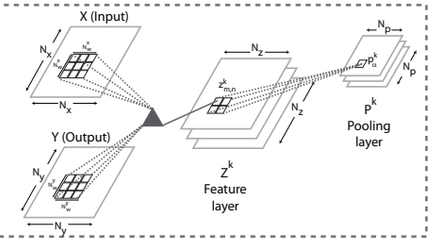
3D convolutional neural networks

Shuiwang Ji, Wei Xu, Ming Yang, and Kai Yu (2010)



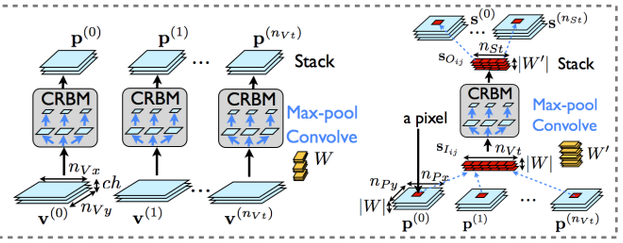
Convolutional gated restricted Boltzmann machines

Graham Taylor, Rob Fergus, Yann LeCun, and Chris Bregler (2010)



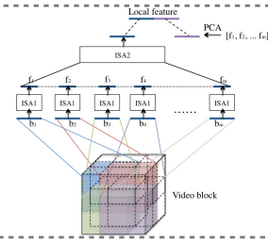
Space-time deep belief networks

Bo Chen, Jo-Anne Ting, Ben Marlin, and Nando de Freitas (2010)



Stacked convolutional independent subspace analysis

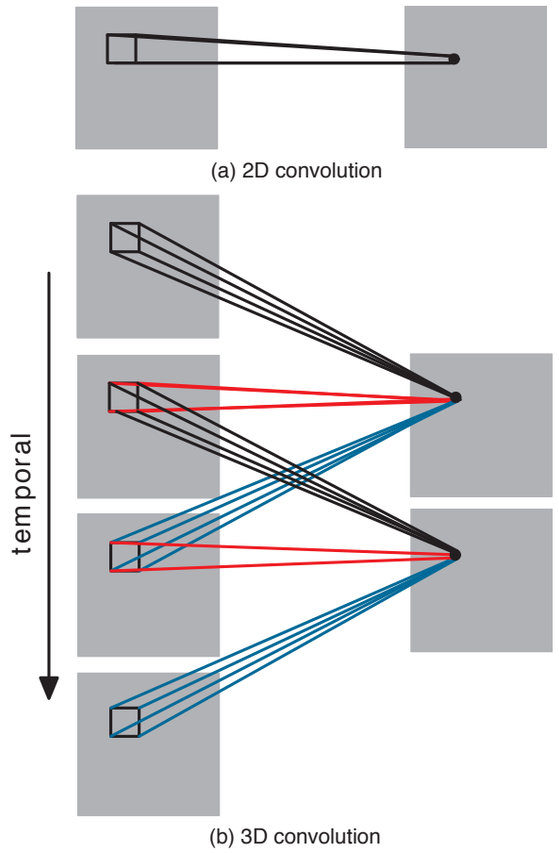
Quoc Le, Will Zou, Serena Yeung, and Andrew Ng (2011)

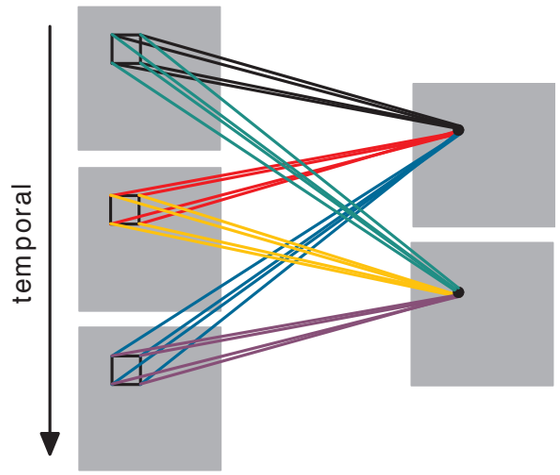


3D CONVNETS FOR ACTIVITY RECOGNITION

Shuiwang Ji, Wei Xu, Ming Yang, and Kai Yu (ICML 2010)

- One approach: treat video frames as still images (LeCun et al. 2005)
- Alternatively, perform 3D convolution so that discriminative features across space and time are captured





Multiple convolutions applied to contiguous frames to extract multiple features

Images from Ji et al. 2010

3D CNN ARCHITECTURE

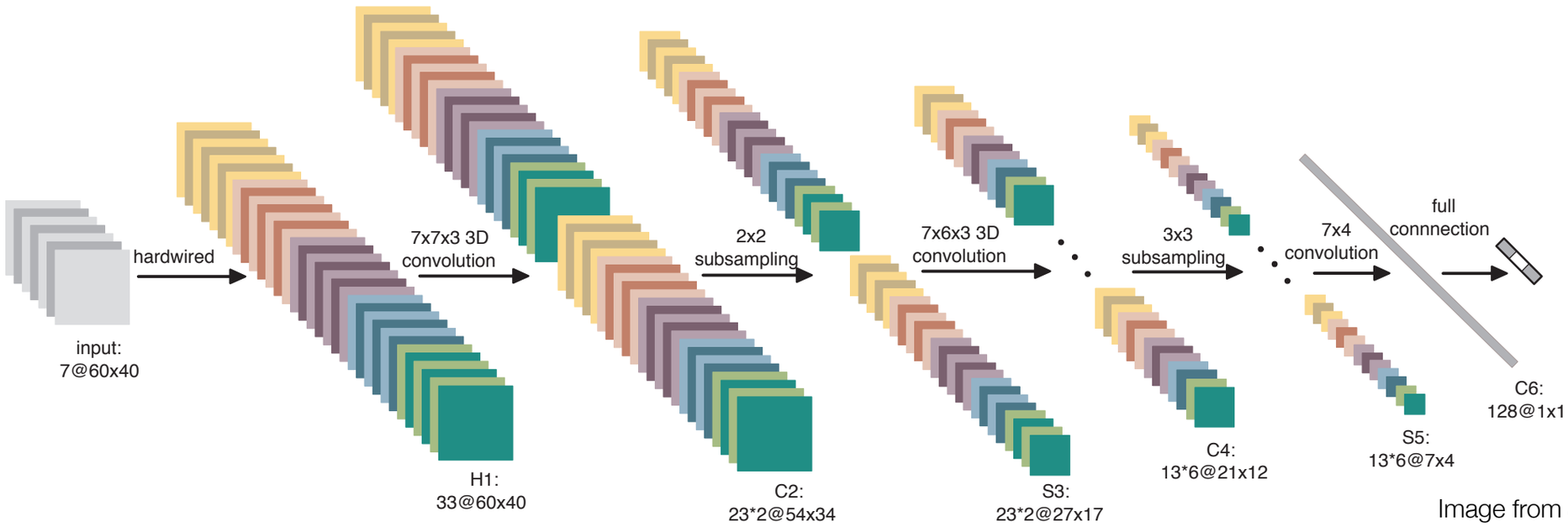


Image from Ji et al. 2010

Hardwired to extract:
1)grayscale
2)grad-x
3)grad-y
4)flow-x
5)flow-y

2 different 3D filters applied to each of 5 blocks independently

Subsample spatially

3 different 3D filters applied to each of 5 channels in 2 blocks

Two fully-connected layers

Action units

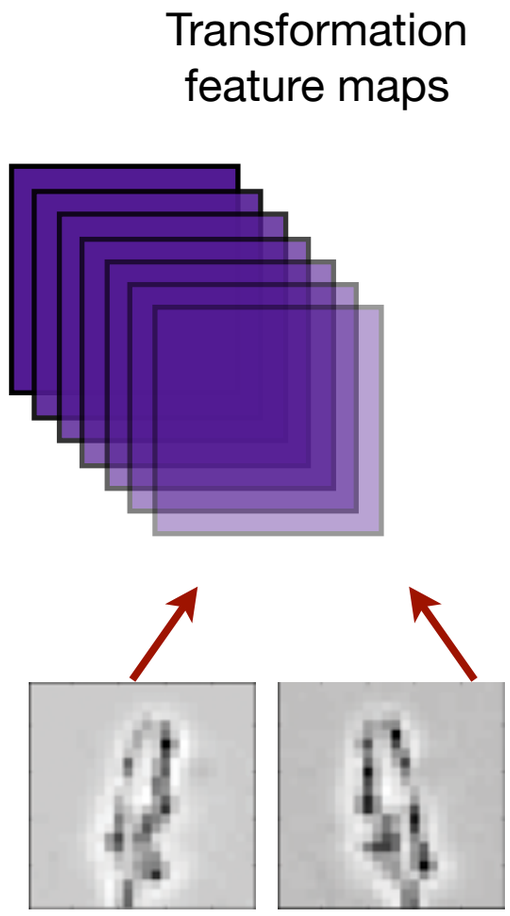
3D CONVNET: DISCUSSION

- Good performance on TRECVID surveillance data (*CellToEar, ObjectPut, Pointing*)
- Good performance on KTH actions (*box, handwave, handclap, jog, run, walk*)
- Still a fair amount of engineering: person detection (TRECVID), foreground extraction (KTH), hard-coded first layer

Image from Ji et al. 2010

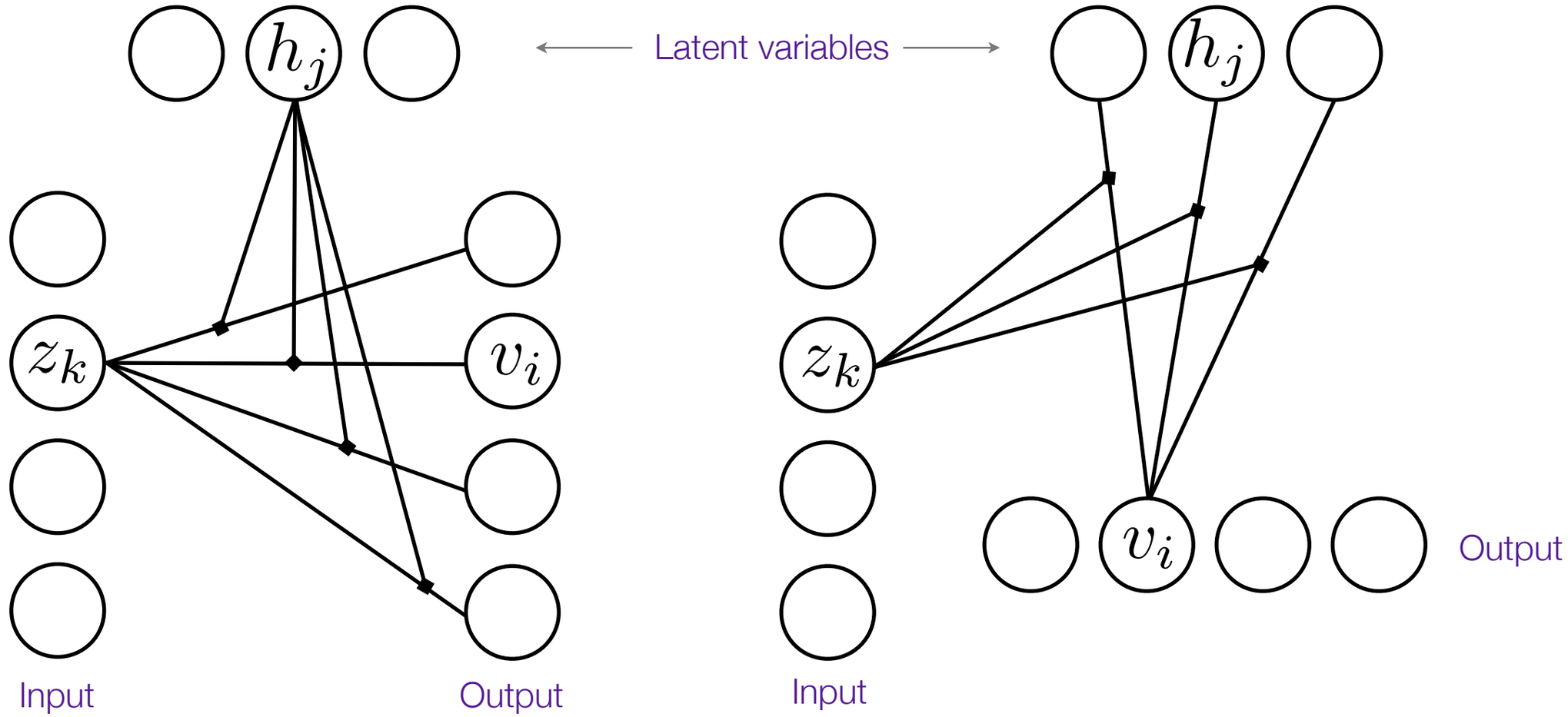
LEARNING FEATURES FOR VIDEO UNDERSTANDING

- Most work on unsupervised feature extraction has concentrated on *static images*
- We propose a model that extracts motion-sensitive features from *pairs of images*
- Existing attempts (e.g. Memisevic & Hinton 2007, Cadieu & Olshausen 2009) ignore the *pictorial* structure of the input
- Thus limited to modeling small image patches



GATED RESTRICTED BOLTZMANN MACHINES (GRBM)

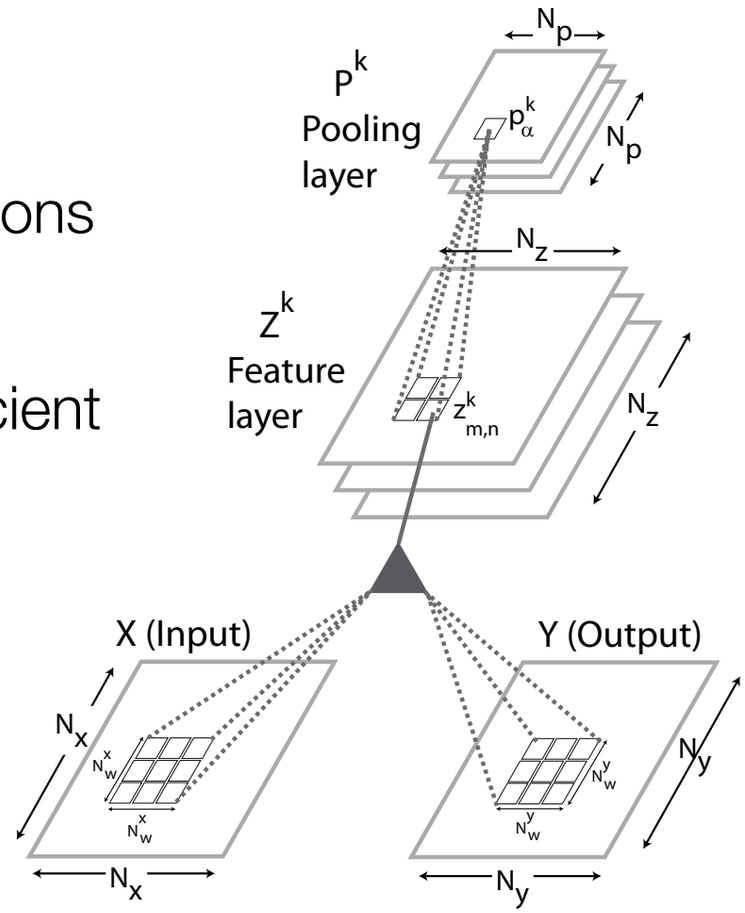
Two views: Memisevic & Hinton (2007)



CONVOLUTIONAL GRBM

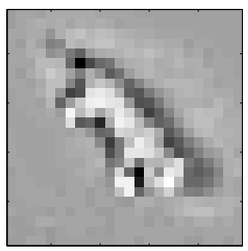
Graham Taylor, Rob Fergus, Yann LeCun, and Chris Bregler (ECCV 2010)

- Like the GRBM, captures third-order interactions
- Shares weights at all locations in an image
- As in a standard RBM, exact inference is efficient
- Inference and reconstruction are performed through convolution operations

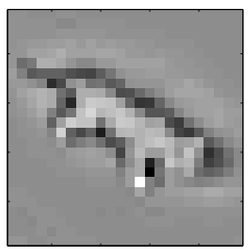


MORE COMPLEX EXAMPLE OF “ANALOGIES”

(Taylor et al. ECCV 2010)



Input

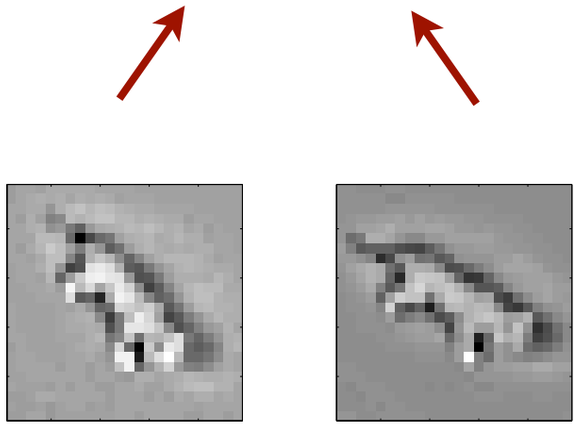


Output

MORE COMPLEX EXAMPLE OF “ANALOGIES”

(Taylor et al. ECCV 2010)

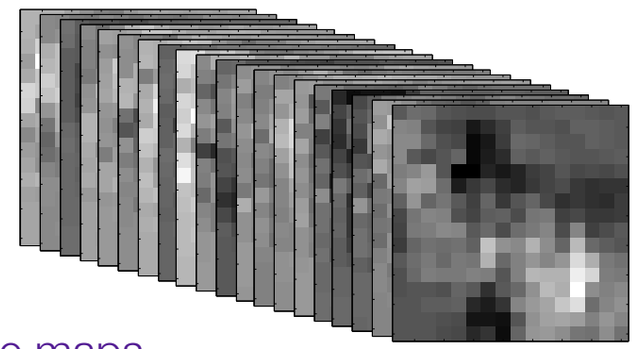
Feature maps



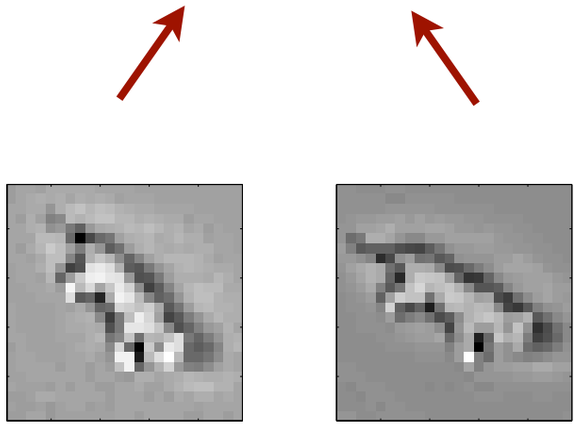
Input Output

MORE COMPLEX EXAMPLE OF “ANALOGIES”

(Taylor et al. ECCV 2010)



Feature maps



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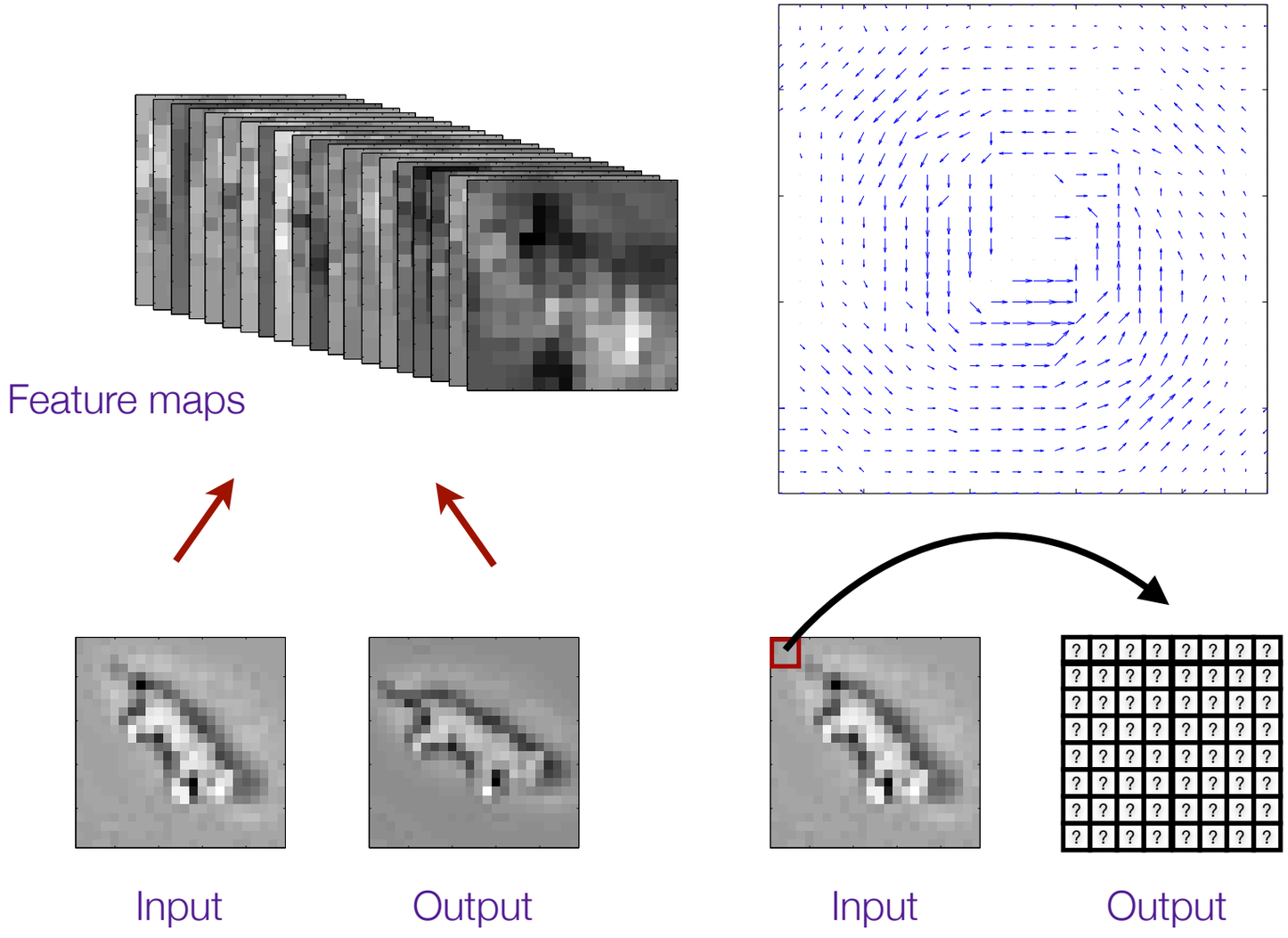

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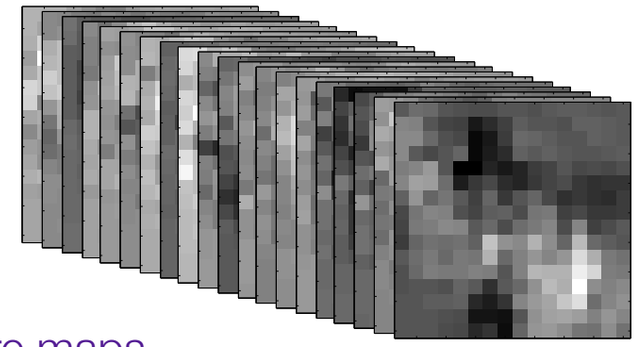

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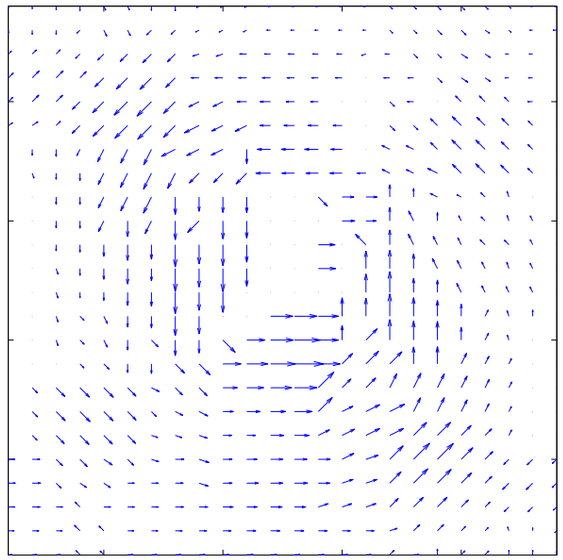
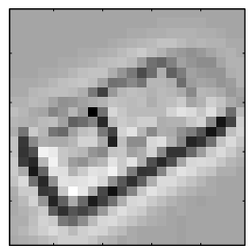
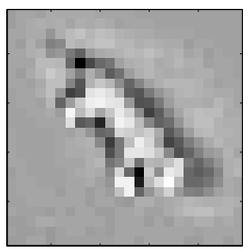
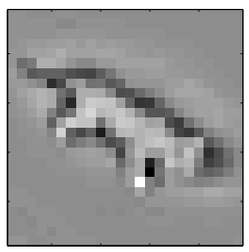


Ground truth





Input



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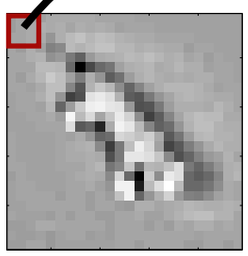
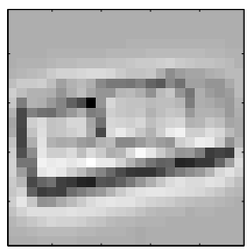
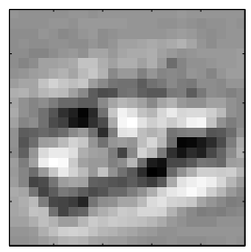


Input

Output



Novel input

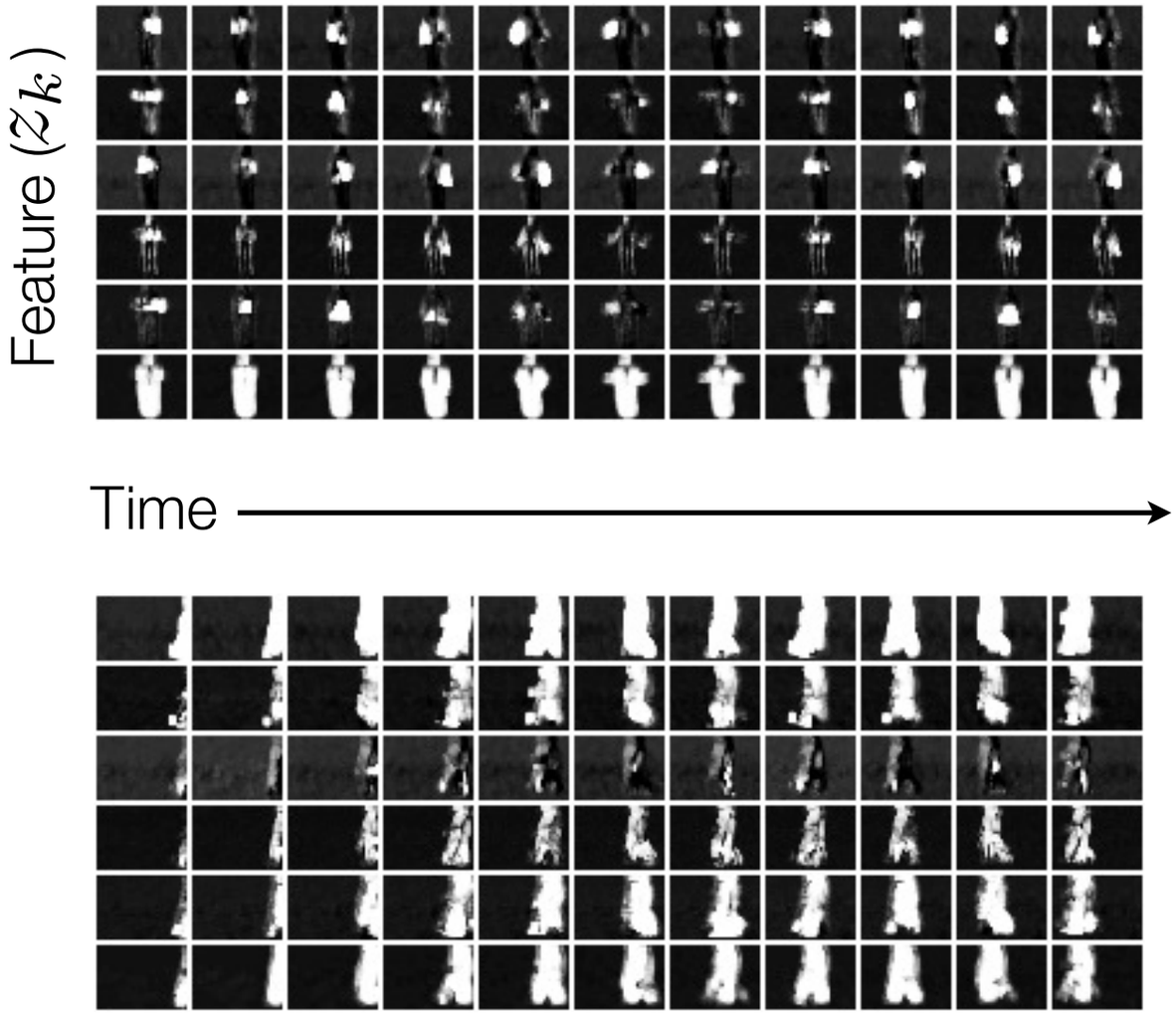


Transformation (model)

HUMAN ACTIVITY: KTH ACTIONS DATASET

- We learn 32 feature maps
- 6 are shown here
- KTH contains 25 subjects performing 6 actions under 4 conditions
- Only preprocessing is local contrast normalization

- Motion sensitive features (1,3)
- Edge features (4)
- Segmentation operator (6)



Hand clapping (above); Walking (below)

ACTIVITY RECOGNITION: KTH

Prior Art	Acc (%)	Convolutional architectures	Acc. (%)
HOG3D+KM+SVM	85.3	convGRBM+3D-convnet+logistic reg.	88.9
HOG/HOF+KM+SVM	86.1	convGRBM+3D convnet+MLP	**90.0**
HOG+KM+SVM	79.0	3D convnet+3D convnet+logistic reg.	79.4
HOF+KM+SVM	88.0	3D convnet+3D convnet+MLP	79.5

- Compared to methods that do not use explicit interest point detection
- State of the art: 92.1% (Laptev et al. 2008) 93.9% (Le et al. 2011)
- Other reported result on 3D convnets uses a different evaluation scheme

ACTIVITY RECOGNITION: HOLLYWOOD 2

- 12 classes of human action extracted from 69 movies (20 hours)
- Much more realistic and challenging than KTH (changing scenes, zoom, etc.)
- Performance is evaluated by mean average precision over classes

Method	Average Prec.
Prior Art (Wang et al. survey 2009):	
HOG3D+KM+SVM	45.3
HOG/HOF+KM+SVM	**47.4**
HOG+KM+SVM	39.4
HOF+KM+SVM	45.5
Our method:	
GRBM+SC+SVM	**46.8**

SPACE-TIME DEEP BELIEF NETWORKS

Bo Chen, Jo-Anne Ting, Ben Marlin, and Nando de Freitas (NIPS Deep Learning Workshop 2010)

- Two previous approaches we saw used discriminative learning
- We now look at a generative method, opening up more applications
  - e.g. in-painting, denoising
- Another key aspect of this work is demonstrated learned invariance
- Basic module: Convolutional Restricted Boltzmann Machine (Lee et al. 2009)

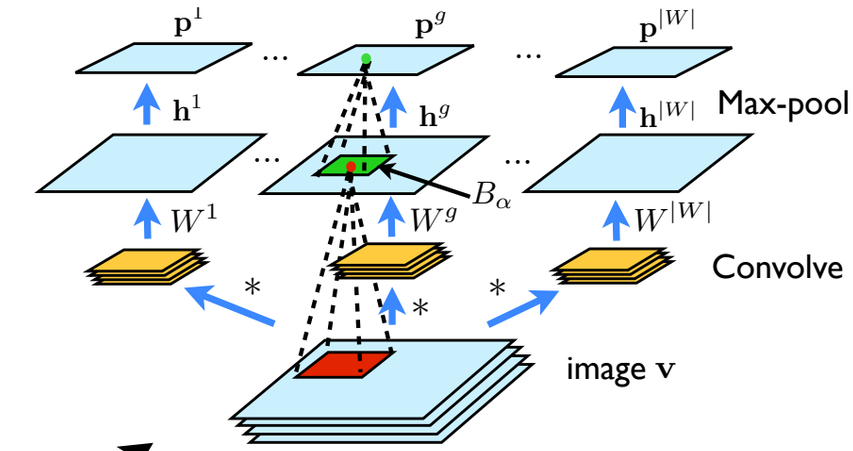
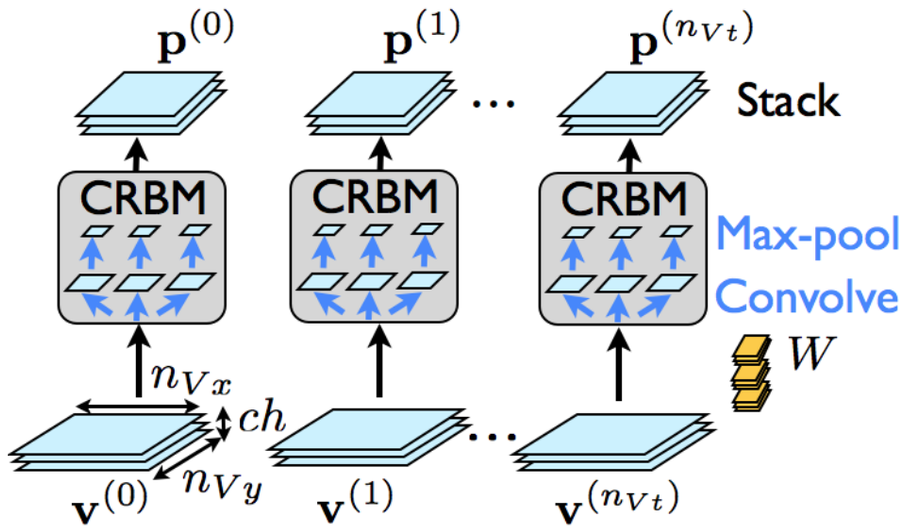


Image from Chen al. 2010

ST-DBN

- Key idea: alternate layers of spatial and temporal Convolutional RBMs
- Weight sharing across all CRBMs in a layer
- Highly overcomplete: use sparsity on activations of max-pooling units



Spatial pooling layer

Images from Chen al. 2010

ST-DBN

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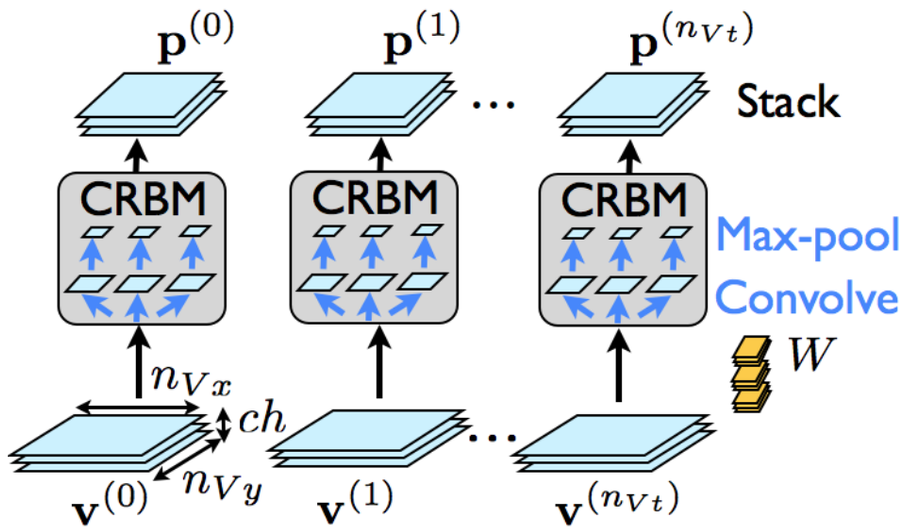
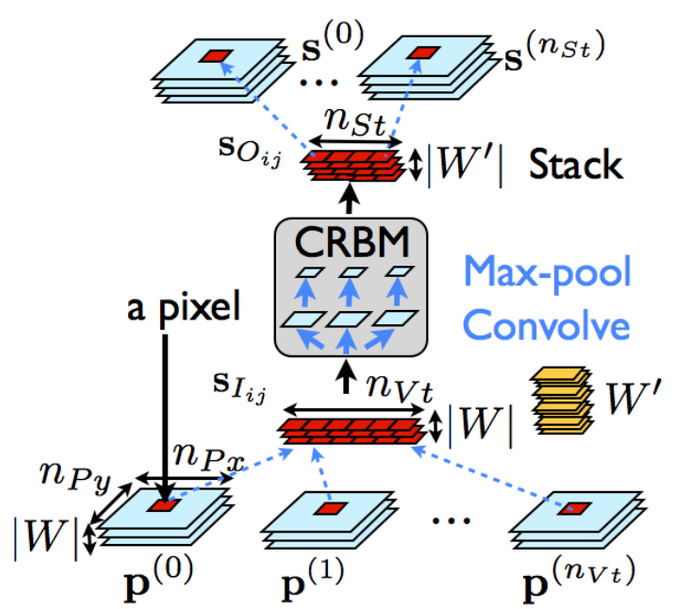


Spatial pooling layer

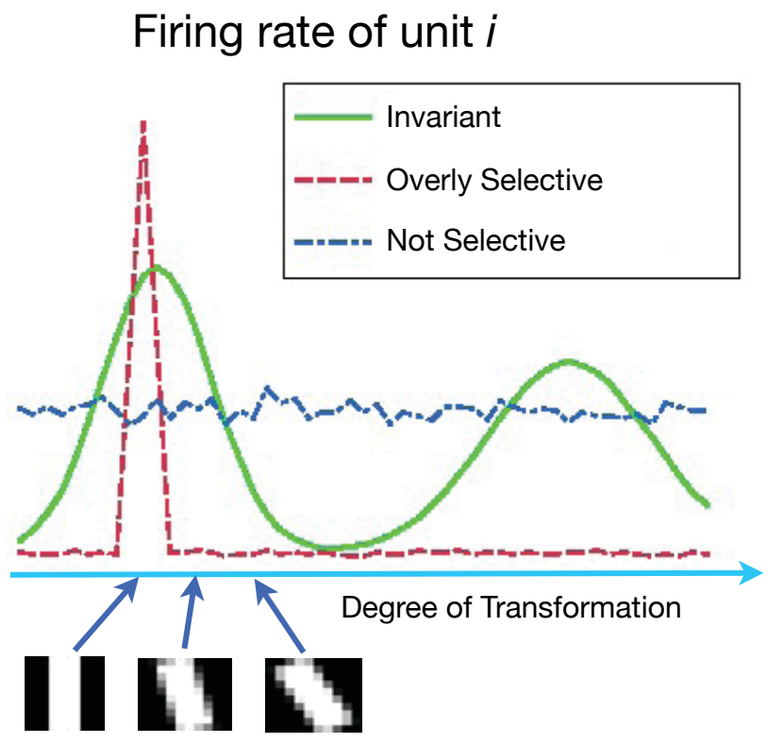


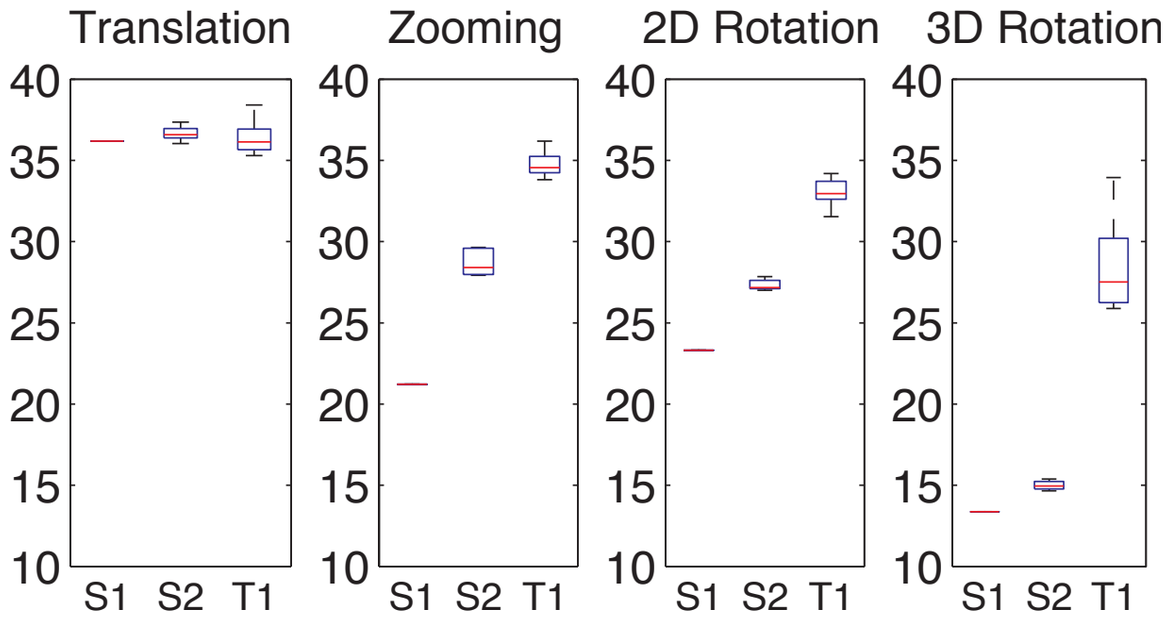
Temporal pooling layer

Images from Chen al. 2010

MEASURING INVARIANCE

- Measure invariance at each layer for various transformations of the input
- Use measure proposed by Goodfellow et al. (2009)



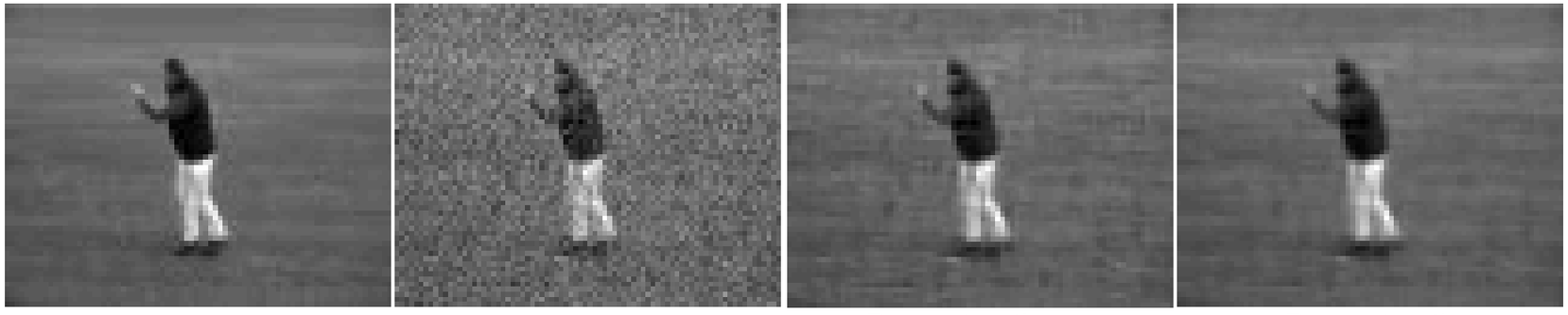


Invariance scores computed for Spatial Pooling Layer 1 (S1), Spatial Pooling Layer 2 (S2) and Temporal Pooling Layer 1 (T1).
Higher is better.

Images from Chen al. 2010

DENOISING AND RECONSTRUCTION

- Operations not possible with a discriminative approach



Test frame | Corrupted test frame | Reconstruction: 1 layer ST-DBN | Reconstruction: 2 layer ST-DBN

Observed gazes

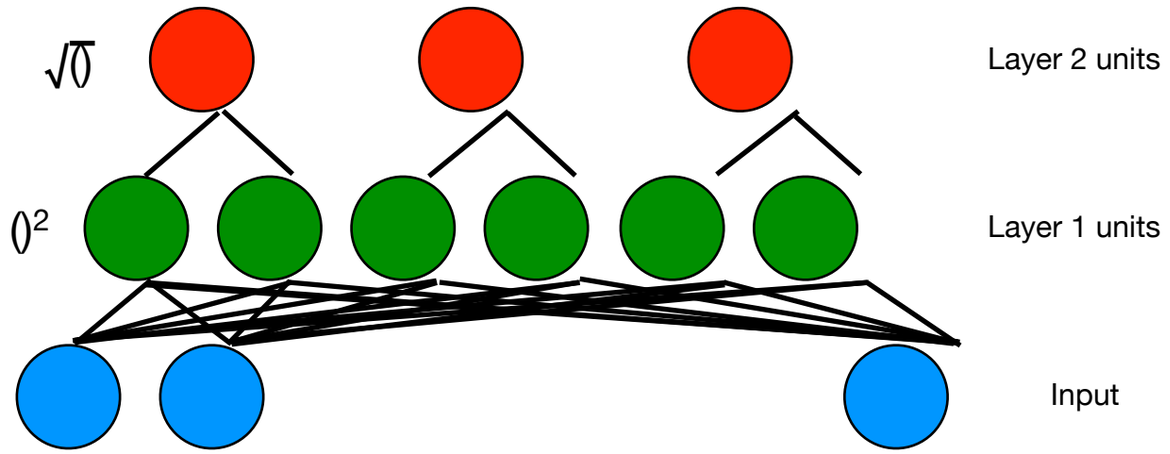
Reconstructions

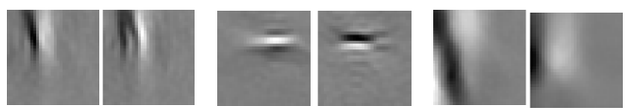
Images from Chen al. 2010

STACKED CONVOLUTIONAL INDEPENDENT SUBSPACE ANALYSIS (ISA)

Quoc Le Will Zou, Serena Yeung, and Andrew Ng (CVPR 2011)

- Use of ISA (right) as a basic module
- Learns features robust to local translation; selective to frequency, rotation and velocity
- Key idea: scale up ISA by applying convolution and stacking





Typical filters learned by ISA when trained on static images
(organized in pools - red units above)

Images from Le et al. 2010

SCALING UP: CONVOLUTION AND STACKING

- The network is built by “copying” the learned network and “pasting” it to different parts of the input data
- Outputs are then treated as the inputs to a new ISA network
- PCA is used to reduce dimensionality

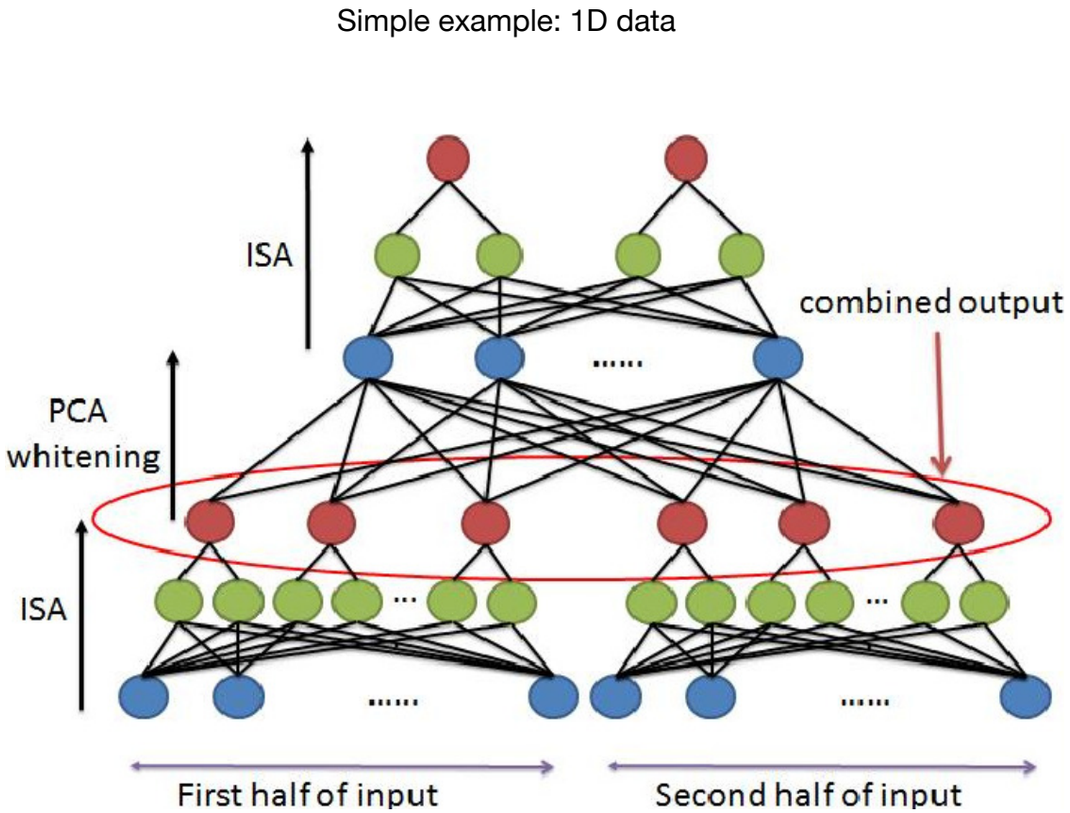
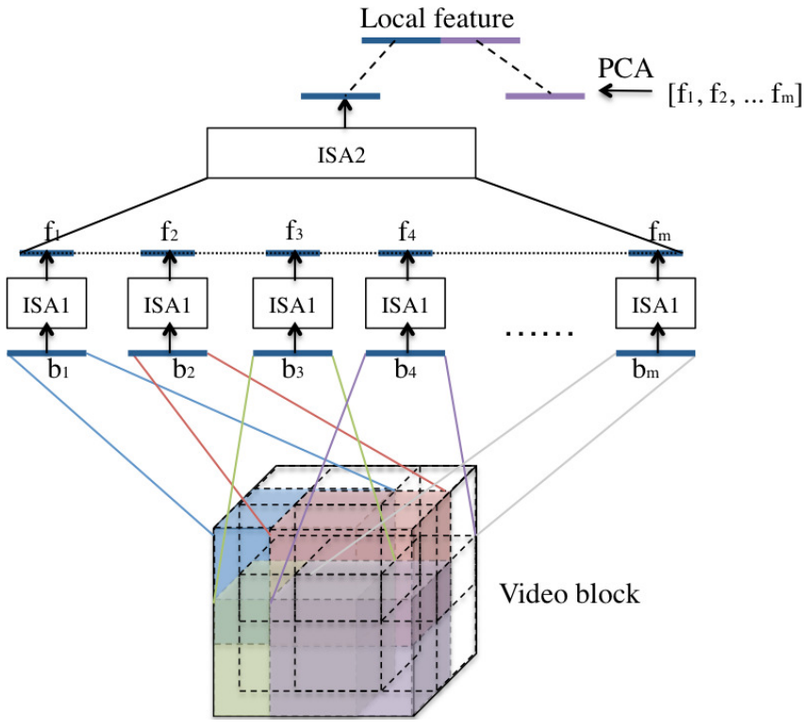


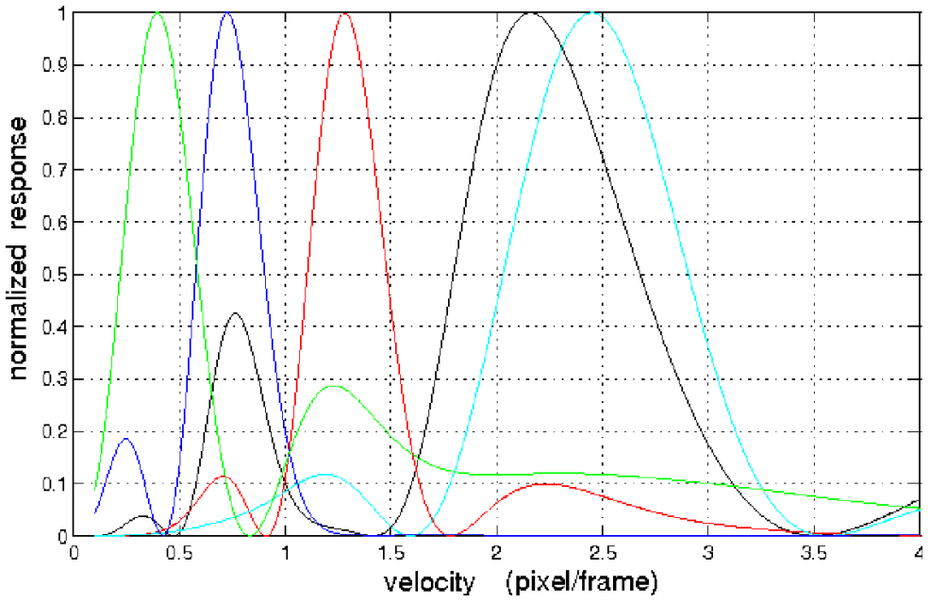
Image from Le et al. 2010

LEARNING SPATIO-TEMPORAL FEATURES

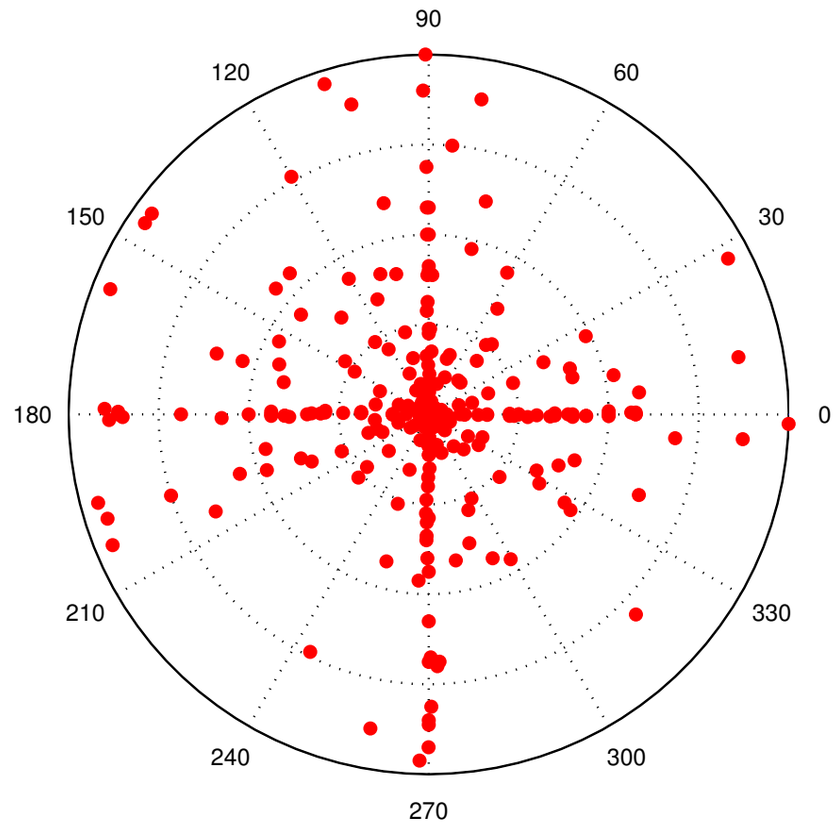
- Inputs to the network are blocks of video
- Each block is vectorized and processed by ISA
- Features from Layer 1 and Layer 2 are combined prior to classification



VELOCITY AND ORIENTATION SELECTIVITY



Velocity tuning curves for five neurons in an ISA network trained on Hollywood2 data



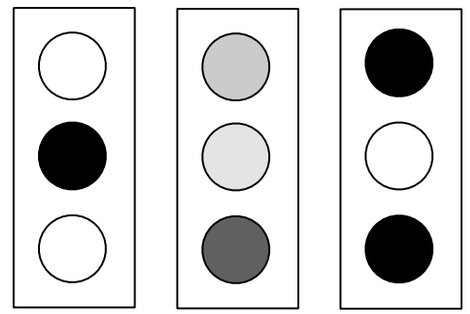
Edge velocities (radius) and orientations (angle) to which filters give maximum response
Outermost velocity: 4 pixels per frame

SUMMARY

18 May 2012 / 56
Learning Representations of Sequences / G Taylor

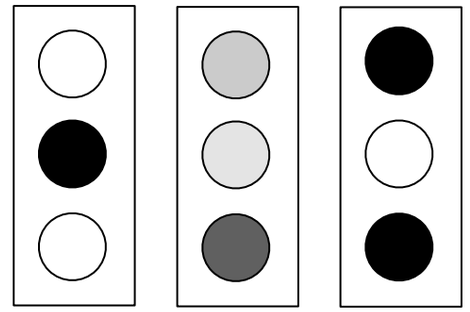
SUMMARY

- Learning distributed representations of sequences

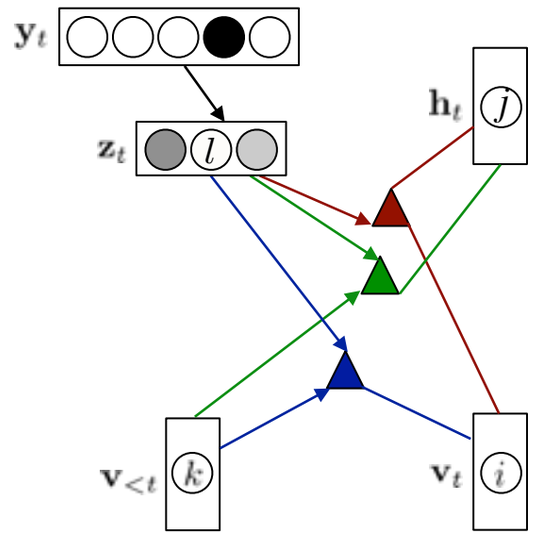


SUMMARY

- Learning distributed representations of sequences

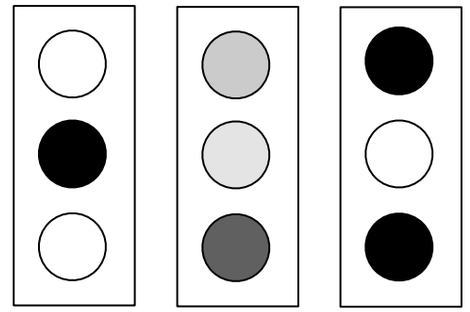


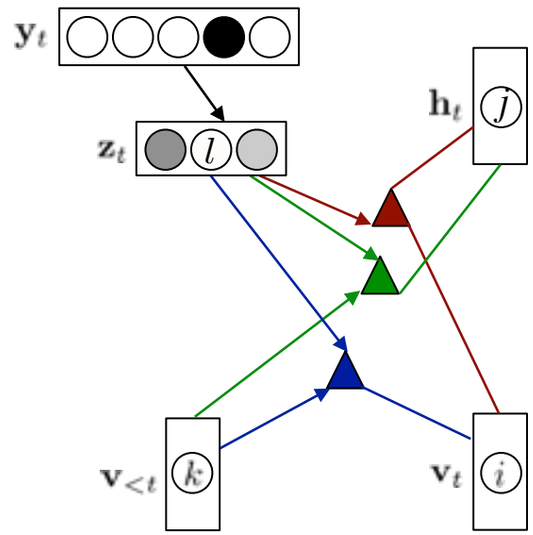
- For high-dimensional, multi-modal data: CRBM, FCRBM



SUMMARY

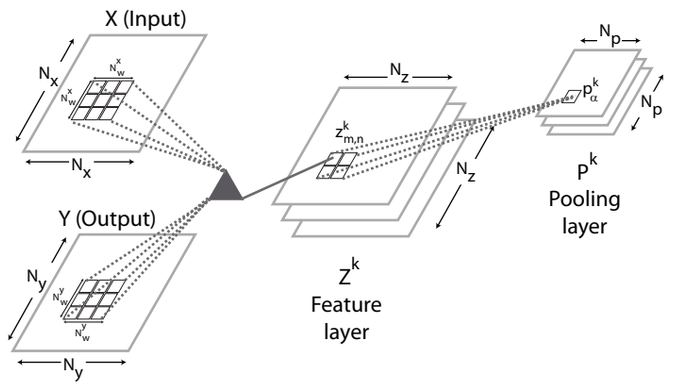
- Learning distributed representations of sequences





- For high-dimensional, multi-modal data: CRBM, FCRBM

- Activity recognition: 4 methods



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