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4.4.1974

M E M O R A N D U M

TO: S.P.S.C.

FROM: Bari-CAEN-CERN(NP/TC)-Liverpool-Milan Collaboration

RE: Addendum to "Proposal for a detailed study of high -  
 $p_t$  events at the SPS". (SPSC/P4)

I. INTRODUCTION

Having taken note of the points raised during our presentation of the proposal to the open session of the SPSC, we give here our present ideas as regards the trigger along with more detailed information on the various parts of the apparatus. The following points will be discussed.

Sec. II : The time schedule and the manpower needed to be on the SPS floor by September 1976.

Sec. III : The modified trigger system (the scintillator hodoscope and the Cerenkov system is now backed up by two calorimeters so as to allow an independent selection on the momentum of the wanted particles while reducing the background of unwanted triggers).

Sec. IV : The Cerenkov counter design.

Sec. V : The vertex detector design (details on the MWPC's).

Sec. VI : The forward detector design (details on the drift chambers).

Sec. VII : The data acquisition system.

Sec. VIII : The pattern recognition.

This completes our White Book on the specific apparatus needed to study in detail the high transverse momentum phenomena at the SPS.

II. THE SCHEDULE AND MANPOWER

According to the project schedule (Table I) the year 1974 will be devoted to studies, tests and fabrication of prototypes. Production should start at the beginning of 1975 and be completed by 1976.

Installation at the SPS will commence somewhat earlier than July 1976. The achievement of such a schedule requires the technical support listed below.

Mechanical construction of the vertex MWPC's, forward drift chambers and Cerenkov counters

MAN-YEARS

|   | 1974 | 1975 | 1976 |    |
|---|------|------|------|----|
| 1. Designers and laboratory technicians<br>for design, development, tests,<br>production control, assembly,etc.....   | 6    | 4    | 3    |    |
| 2. Machinists (CERN).....   | 2    | 2    | 2    |    |
| 3. Cablers for MWPC's and drift chambers<br>(Regie).....  | 1    | 3    | 2    |    |
| Total   | 9    | 9    | 7    | 25 |
| 4. Technicians (Regie). These will be necessary for the fabrication and assembly. Their importance will vary depending on the division of work in the CERN and outside workshops. The estimated total cost of the MWPC and drift chamber system includes the cost of all sources of manpower. |      |      |      |    |

Electronics

MAN-YEARS

|   | 1974 | 1975 | 1976 |    |
|---|------|------|------|----|
| 1. Engineers and technicians                      |      |      |      |    |
| a) MWPC's and drift chambers.....                 | 4    | 4    | 3    |    |
| b) Fast electronics and trigger.....              | 1    | 1    | 1    |    |
| c) Reading and coding logic and<br>interface..... | 1    | 1    | 1    |    |
| d) Software for data acquisition.....             | ½    | 1    | ½    |    |
| 2. Cablers (Regie)                                | 3    | 5    | 5    |    |
| 3. Designers for printed circuits                 | ½    | 1    | ½    |    |
| Total   | 10   | 13   | 11   | 34 |

Cerenkov optics

|  |   |   |   |   |
|--|---|---|---|---|
| 1. Study and design (Engineer) and assembly  | ½ | ½ | ½ |   |
| 2. Fabrication of mirrors and light catchers | ¼ | ½ | ¼ |   |
| 3. Mirror coating                            | ¼ | 1 | ¼ |   |
| Total  | 1 | 2 | 1 | 4 |

Counters

|   |   |     |   |   |
|---|---|-----|---|---|
| 1. Scintillators: fabrication and assembly<br>of hodoscopes (West Workshop) | 0 | ¼   | ¼ |   |
| 2. Calorimeters (West Workshop) *)  | ½ | 1½  | ½ |   |
| Total   | ½ | 1 ¾ | ¾ | 3 |

\*) Scintillators and light guides will be purchased from  
outside sources.

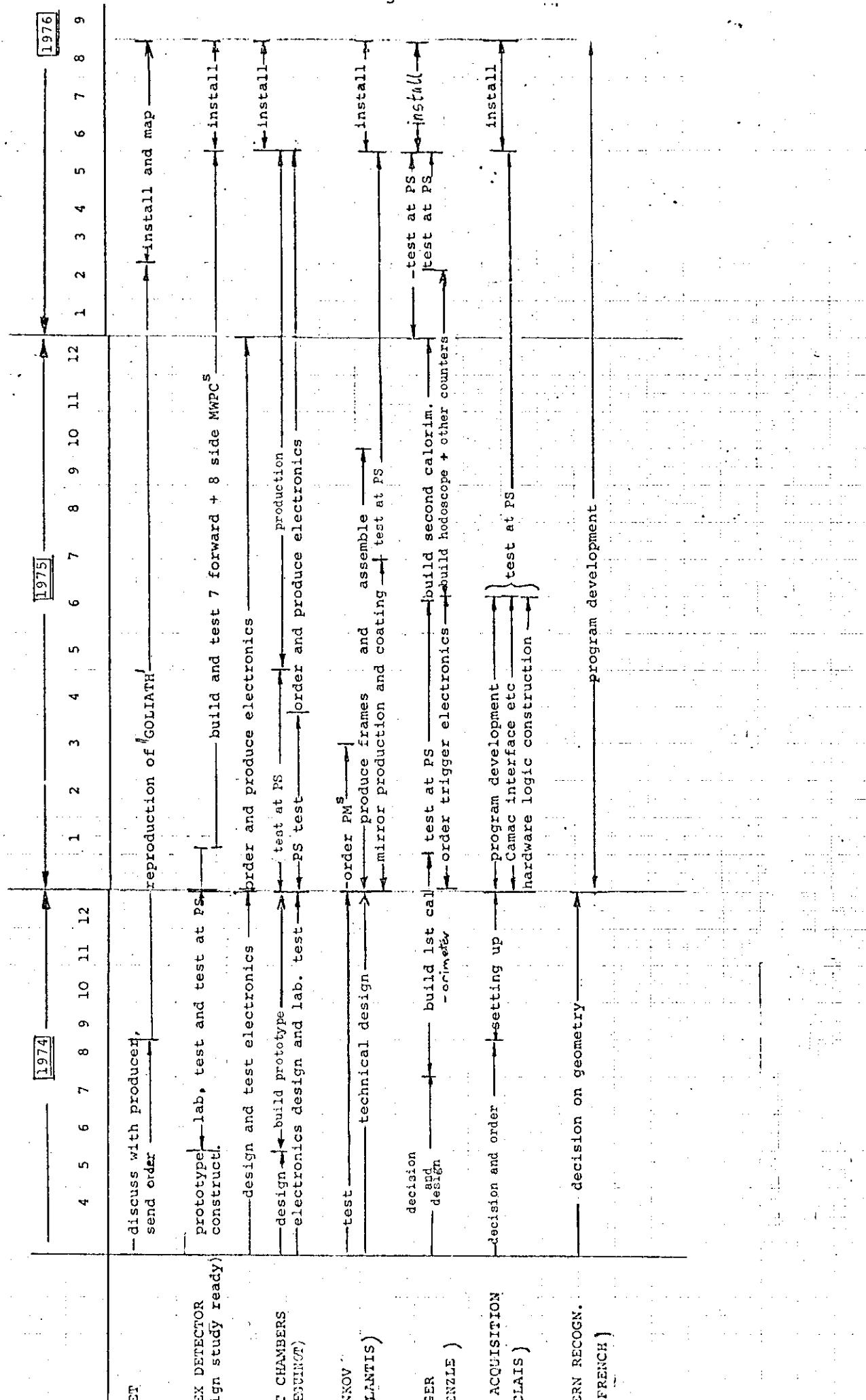
Hence we arrive at a grand total of 66 man-years. Of these, 19 are from outside regie and 47 from CERN. The CERN load would then amount to a total of 18 men over  $\sim$  2.5 years.

Magnet

The possibility of building a copy of the Saclay magnet "GOLIATH" has been examined during a visit to ALSTHOM (Belfort) on 3/4/1974. The company confirms that the construction schedule given in Table I is realistic provided an order for the coils is submitted not later than September 1st, 1974.

TABLE I

Time schedule of the project. The names of the persons responsible for the various items are shown in parenthesis.



### III. TRIGGER

In order to improve the selectivity of the system for the very low cross section of the high- $p_t$  events, a more flexible multi-level trigger system has been designed by introducing calorimeters. We still require, as before, one high- $p_t$  charged particle emitted near  $90^\circ$  in the c.m. However, we now perform the selection by means of three independent requirements : (a) the coincidence of the scintillation hodoscope, (b) the required combination of signals from the Cerenkov system and (c) the indication that a particle with momentum equal or larger than a pre-set value has entered one of two calorimeters situated downstream of the scintillation hodoscope.

These three components of the trigger signal are discussed below. They are followed by a re-examination of the expected trigger rates and by an analysis of the possible backgrounds.

#### 1. Scintillation hodoscopes.

A first definition of  $p_t$  is done with the set of hodoscopes  $M_{12}^{M_1 M_2}$  consisting of vertical slabs of scintillators used in fast coincidence (fig. 1). One pair of hodoscopes is above and one below the beam, at an angle of  $\sim 6^\circ$  with respect to the target. Each hodoscope has a rectangular shape (fig. 2) and covers the c.m. angle  $80^\circ - 100^\circ$  (fig. 3) over the azimuthal interval  $-45^\circ \leq \phi \leq +45^\circ$ . The total solid angle covered by the hodoscope is  $\sim 1$  sr.

The reason for having the  $M_{12}^{M_1 M_2}$  hodoscopes in the up-down regions only, rather than in the circular arrangement quoted in the original proposal, comes from a more extensive study of the peripheral events distribution. Fig. 4 shows the spread of track intersections at 10 m from the target (position of the calorimeter; see sect. 3) as obtained from Monte Carlo events after deflection through the magnet. Fig. 4 also shows the position of  $M_3$  which defines the solid angle of the trigger. The peripheral Monte Carlo events have been plotted in Fig. 5 to show the correlation between the vertical coordinate Z in a plane 10 m from

the target and their momentum; the trigger acceptance region can be seen to be well outside the peripheral spread.

By cabling suitable combinations of the hodoscope elements one can adjust the acceptance, selecting for example a lower cut-off in  $p_t$ . A situation that can be obtained if a uniform  $p_t$  acceptance is desired above  $p_t \sim 3.5$  GeV/c appears in fig. 6; introducing the known  $d\sigma/dp_t$  distribution at 150 GeV/c the acceptance function becomes as in Fig. 7. More details about  $M_{12}$  correlations can be found in the original proposal.

## 2. Cerenkov counters

As described in the proposal, the four Cerenkov counters  $C_1 - C_4$  are used in the trigger in the following combinations according to the particle selection requirement :

$C_1 C_2 C_3 C_4$  for  $\pi$ 's

$C_1 C_2 C_4$  for  $K$ 's

$C_1 C_3 C_4$  for  $p$  and  $\bar{p}$ 's.

One can notice that the trigger condition is quite tight for  $\pi$ 's, less so for  $K$ 's and somewhat loose for  $p$  and  $\bar{p}$ 's ( $C_1$  accepts  $\pi$ 's already from  $\sim 2.5$  GeV/c).

## 3. Calorimeters

In order to further improve the selectivity of our trigger and thus avoid certain backgrounds discussed below we have added calorimeters to the original set-up. In addition to reducing the background they give an independent definition of  $p_t$ .

We propose to use two calorimeters, positioned as in Fig. 1, covering the solid angle of the  $M_{12}$  hodoscope. Their position with respect to the peripheral events at 10 m from the target is shown in figs. 4 and 5.

Their design is a straightforward extrapolation of the existing STAC developed by Engler et al<sup>(1)</sup>. Each calorimeter consists of 6 equal modules and is 9 collision lengths deep (see Fig. 8). The construction of one module is illustrated in Fig. 9. It consists of 8 plastic scintillators (1 cm thick) sandwiched between 8 iron sheets (3 cm thick). The area is  $1 \times 2 \text{ m}^2$  and the thickness per module corresponds to 1.5 collision lengths ( $200 \text{ gr/cm}^2$ ). Each module is viewed from both sides by a large area fast photomultiplier (60 DVP) to assure uniform light collection and fast response (5 ns by mean-timer method) for use in the fast logic.

The expected energy resolution is  $\pm 8\%$  at 30 GeV (Fig. 10) with good linearity (Fig. 11). The drift in amplitude quoted by ref. (1) is less than 10% per week; however, this drift is continuously monitored and corrected by means of calibrated photodiode pulses thus ensuring permanent stability. Fig. 12 shows the expected cut-off efficiency of the calorimeters for a setting at  $p_t = 2.5 \text{ GeV/c}$  (the corresponding lab. momentum at 150 GeV/c incident momentum is  $\sim 22 \text{ GeV/c}$ ). We then arrive, for instance, at a rejection efficiency larger than 100 for  $p_t \leq 1.5 \text{ GeV/c}$ . This efficiency should be folded into the hodoscope triggering function of Fig. 6 thus greatly improving the overall rejection. The relative adjustment between the hodoscope acceptance and the calorimeter rejection is obtained by the discriminator setting of the latter.

Each calorimeter is triggered by the counter  $M_3$  located in front of it and which also defines the sensitive area.  $M_3$  consists of vertical scintillator strips which can be used as an additional hodoscope system to check and reinforce the  $M_1 M_2$  coincidence. An anticounter  $\bar{S}$  can be placed at the back of the calorimeter to ensure that the hadron shower has been contained. The effects of shower leakage and containment are illustrated in Fig. 13.

If we require that in the first 3 collision lengths the hadron shower has started to develop (by using module No. 3 of the calorimeter as a

(1) J. Engler et al., Nucl. Instr. and Meth. 106, (1973) 189 and measurements by the same authors at Serpukhov (1973), private communication.

probe counter) and that after another 6 collision lengths it is contained, then we expect a calorimeter efficiency larger than 90% (see Fig. 14).

Noticing that 1 collision length is approximately equivalent to 10 radiation lengths, we can use the first module of each calorimeter for an efficient rejection of the electromagnetic showers introducing a pulse height discrimination, (thus suppressing the  $\gamma$  background).

We would like to point out a further possible gain in rejection power if such need should arise. Calorimeter No. 2 can be shifted into the beam line and used as an antiperipheral trigger. This is shown as cal. 2'dashed in Fig. 1. Thus one could, for example, reject events where more than 100 GeV out of 150 GeV incident have been absorbed by cal. 2. For this "missing energy" trigger operation we could easily insert additional iron plates between the modules (each plate would have a small hole in the center to allow the passage of the beam). Rejections of the order of 10 or larger would be provided by this mode of triggering. At this stage, however, we cannot prove that such an anticalorimeter alone would give enough rejection (see, for example the NAL proposal No. 222 by Frisch et al, 1973). Thus the reason for starting by triggering on one high- $p_t$  particle.

The effects of backscattering from the calorimeters into the trigger hodoscopes are, according to measurements by ref. (1), of the order of 10%. They can be avoided, in our case, by introducing a sufficient distance between  $M_2$  and the calorimeters. The solid angle available to the backscattered particles would then be reduced. Also, a time-of-flight separation may become feasible.

In order to keep the rate of accidental triggers due to backscattering of beam-halo particles at an acceptable level, some shielding may be necessary beside that provided by the iron of the magnet (which already shadows most of the calorimeter volume). We require that the flux of the hadronic halo at 1 m from the beam and with energy larger than  $\sim 25$  GeV should not exceed  $10^5$  particles  $\times m^{-2} \times sec^{-1}$ .

Finally, we estimate the cost of each calorimeter module to be 50 KSF as indicated by up-to-date information from various manufacturers. A total of 0.6 MSF is thus necessary for the 50-ton complete calorimeter system.

#### 4. Rates.

The rates expected with the new geometry at 150 GeV/c incident momentum have been calculated using the "universal CCR fit" of the ISR data :

$$E \frac{d\sigma}{dp_t^3} = 1.54 \times 10^{-26} p_t^{-8.24} e^{-26.1 p_t/\sqrt{s}} [\text{mb/GeV}^2]$$

The above refers to the  $\pi^0$  of the inclusive reaction  $pp \rightarrow \pi^0 + \text{anything}$ . Applying this to our conditions ( $10^7$  incident particles per burst,  $10^4$  bursts per day, 30 cm liquid hydrogen target) and triggering on all charged particles in our solid angle, we expect the following rates :

| $p_t$ (GeV/c) | 2.5 - 3.5 | 3.5 - 4.5 | 4.5 - 5.5 |
|---------------|-----------|-----------|-----------|
| events/day    | 22400     | 975       | 44        |

These rates could probably be improved substantially if, as discussed earlier, one succeeds in triggering on the missing energy alone, i.e. with the calorimeter No. 2 in the anticoincidence position (the gain could be a factor  $p_t^4$  and would result in  $\sim 600$  times more events at  $p_t = 5 \text{ GeV}/c$ ).

#### 5. Background.

Three possible sources of background have been estimated. They are all strongly suppressed by the use of the calorimeters. They are :

- i) A single charged particle of low momentum (less than 9 GeV/c) impinges on the first hodoscope  $M_1$ , interacts and gives rise to a particle going into the second hodoscope  $M_2$  satisfying the  $M_1 M_2$  correlation condition. From a sample of Monte Carlo

events we find a 2% probability for one such particle to enter  $M_1$ . The interaction rate in the  $M_1$  scintillators being  $\sim 1\%$ , we see that at most (i.e. with the secondary particle entering the correct  $M_2$  section each time) the probability for such a background is  $2 \times 10^{-4}$ . With  $5 \times 10^5$  interactions per burst in the target this results in 100 background triggers per burst. The calorimeter trigger condition rejects them all. It should be noticed that - in the absence of a calorimeter - this background could also be rejected by an on-line rough straight track reconstruction on the PDP 11 computer (the computational capacity is of the order of 2000 per second).

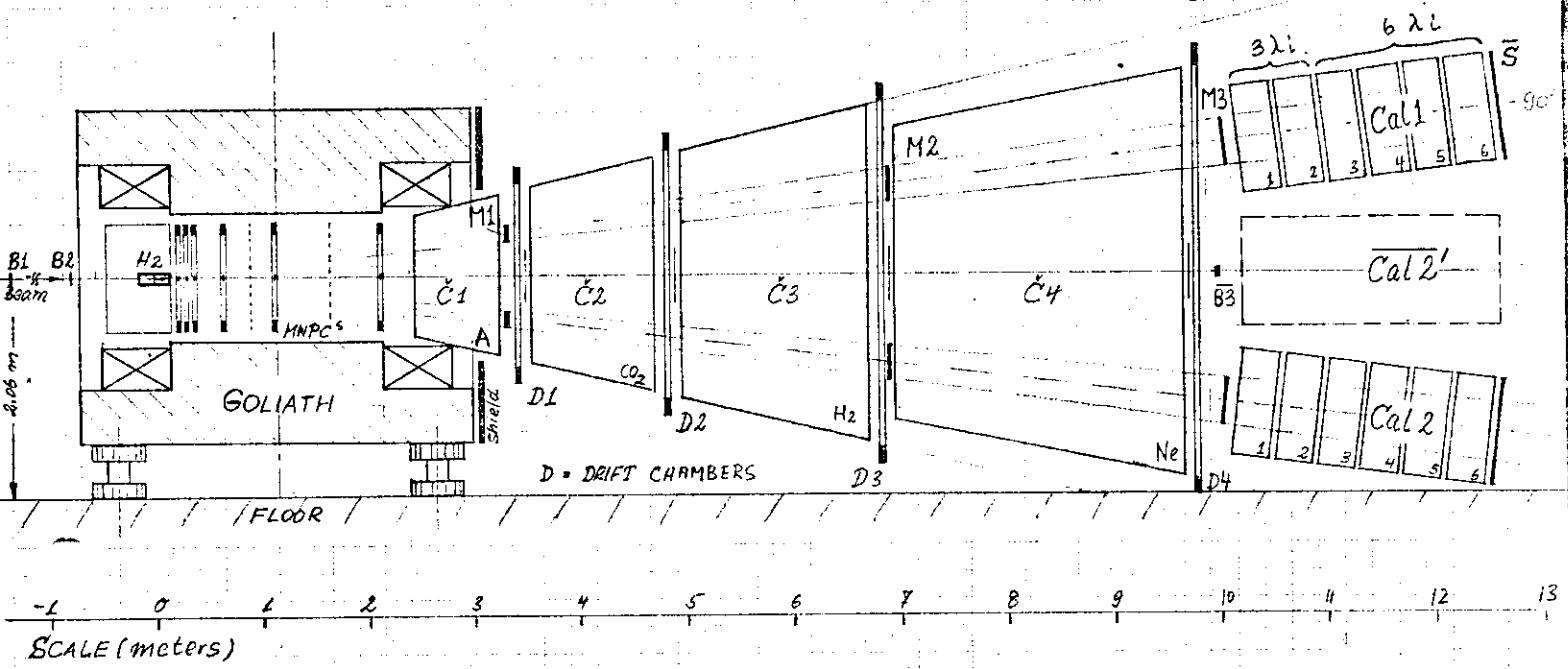
- ii) Two charged particles of low momentum, one hitting  $M_1$  the other hitting  $M_2$ , can simulate a good trigger. This background occurs with a probability of  $2 \times 10^{-4}$  and is also eliminated by the calorimeter. Alternatively, a fast reconstruction on the on-line computer could also take care of it.
- iii) The  $\gamma$ -rays emitted by the  $\pi^0$ 's which are produced in large number ( $5 \times 10^5$  per burst of  $10^7$  incident particles) among the peripheral events are an important source of background. They materialise in a region before, or just inside, the first Cerenkov counter ( $C_1$  in fig. 1). In this region the influence of the magnetic field is minimal and the electrons from the  $\gamma$  conversion can simulate charged tracks of high momentum - and hence high- $p_t$  - in the  $M_1 M_2$  hodoscope. We have estimated the size of this background by generating Monte Carlo events of a peripheral type with 8 charged tracks and 4  $\pi^0$ 's. The  $\gamma$ 's from the  $\pi^0$ 's have been allowed to materialise with a 40 m radiation length. The effective amount of material which is responsible for the conversion is  $3 \times 10^{-3}$  radiation lengths, mainly concentrated in the region of the 6th MWPC of the vertex detector. We find a total of 600 simulated high- $p_t$  events per burst. Most of them are rejected by the calorimeter. An independent reduction

can also be achieved by interrogating specific sets of wires in the 5th MWPC so as to insure that a charged track is already present inside the magnet (one could probably gain a factor 10 in this way thus reducing the false triggers to only 60 per burst). A check on the above estimates has been done by using real events as observed in the OMEGA spectrometer. Fig. 15a shows the correlation observed in two hodoscopes for events with one track in the spark chambers: these are the good triggers. Fig. 15b shows instead the same hodoscope correlation for 2750 background triggers, i.e. events which had no charged track in the spark chambers. From the density on the latter plot and scaling to the size of our hodoscopes we find a background of 700 triggers per  $5 \times 10^5$  interactions, to be compared to the 600 estimated above.

We conclude by stressing that, although alternative or complementary methods such as those originally proposed can also be construed, the use of the calorimeter by itself will eliminate all sources of background.

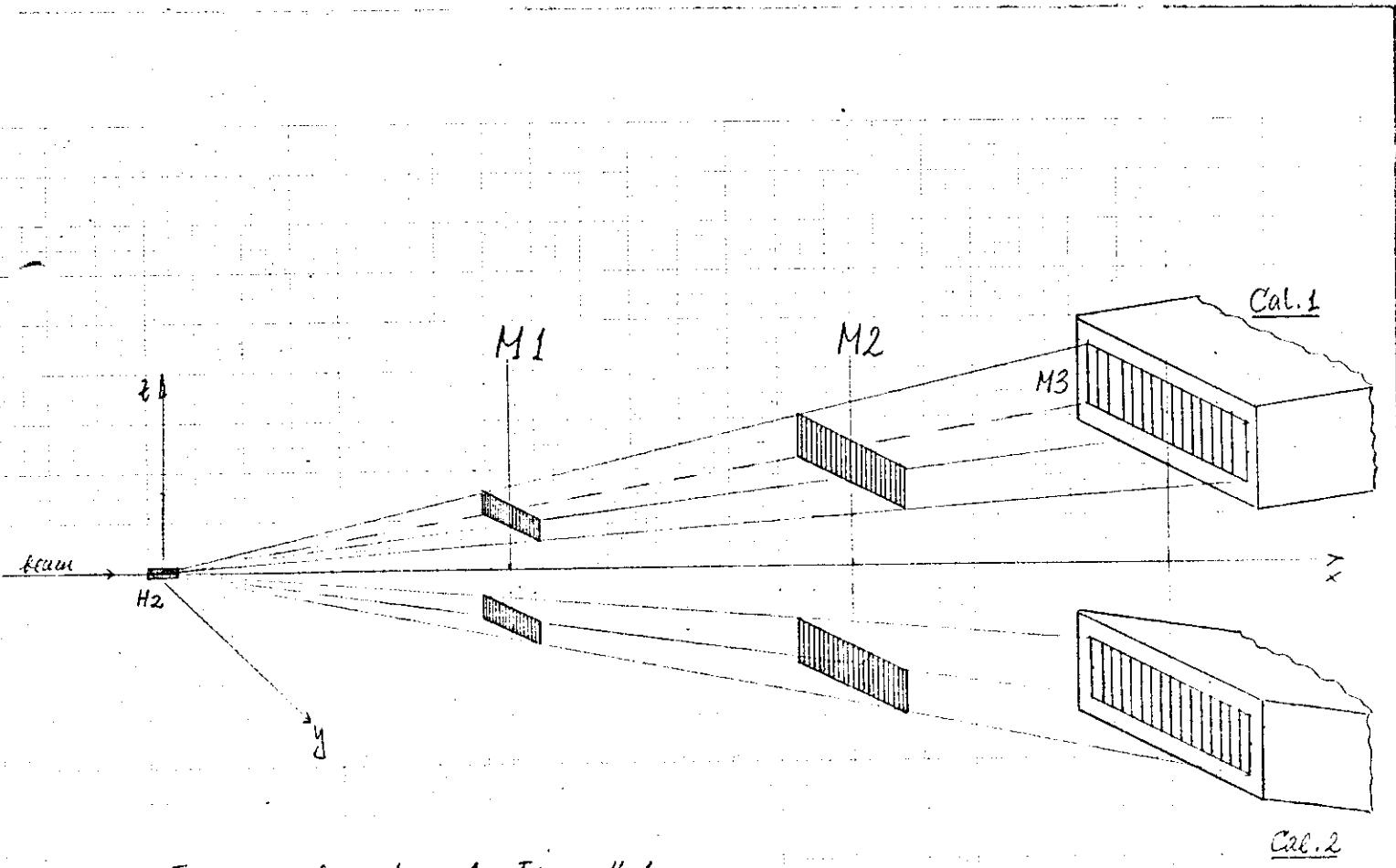
114, 7-11.

$\theta^* - 130^\circ$



TRIGGER:  $B1B2\bar{B}_3$ ,  
 $H1H_2C$ ,  
 $Cal1/Cal2$ ,  
OR:  $Cal1\bar{Cal}2'$

Fig.1: HIGH  $P_t$  SPECTROMETER  
(elevation)



Cal.2

Fig. 3: Acceptance of trigger mask shape  
in CMS. ( $\Theta^*$  = polar angle).

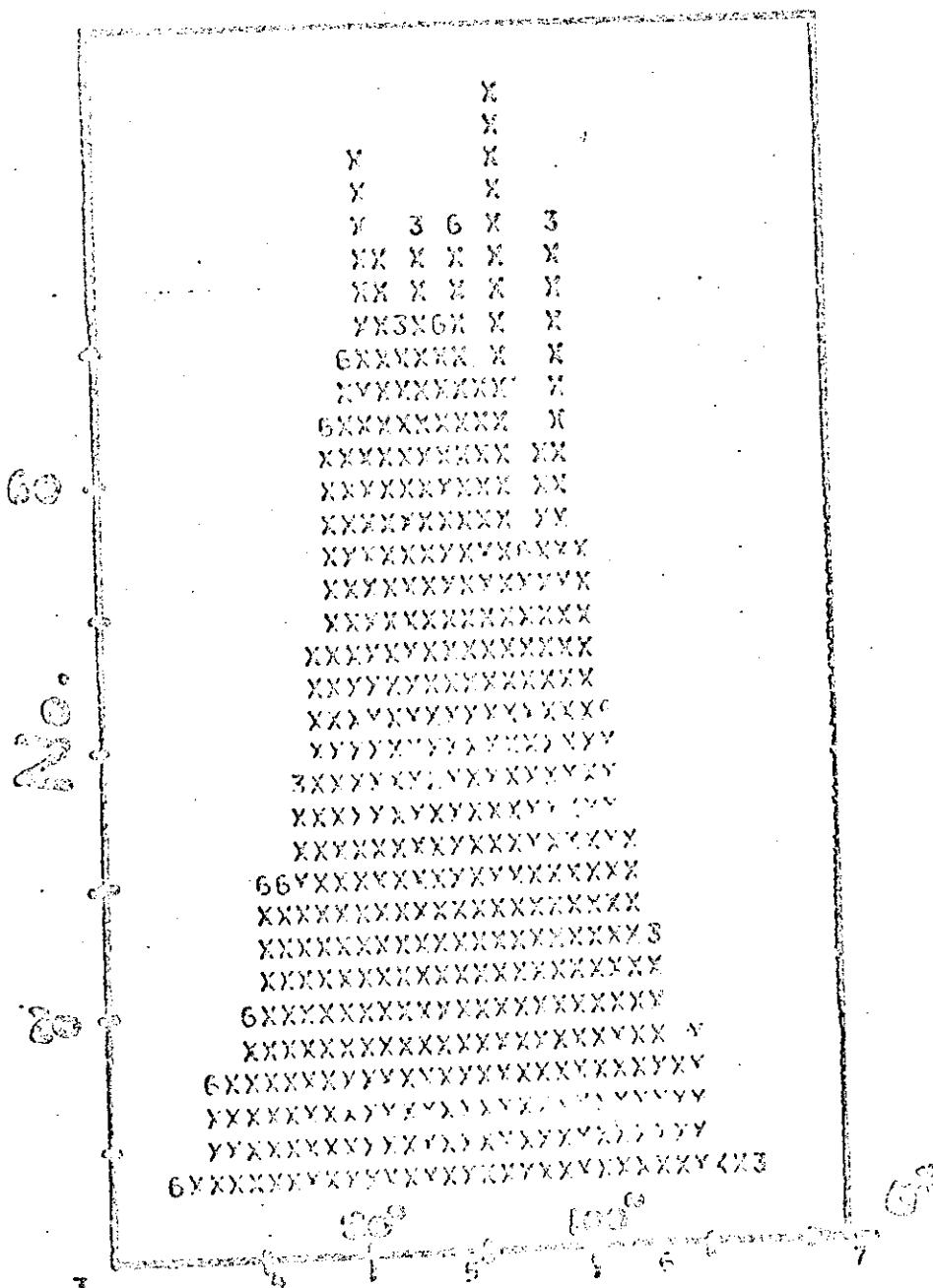


Fig 4: Segmentation of the plane

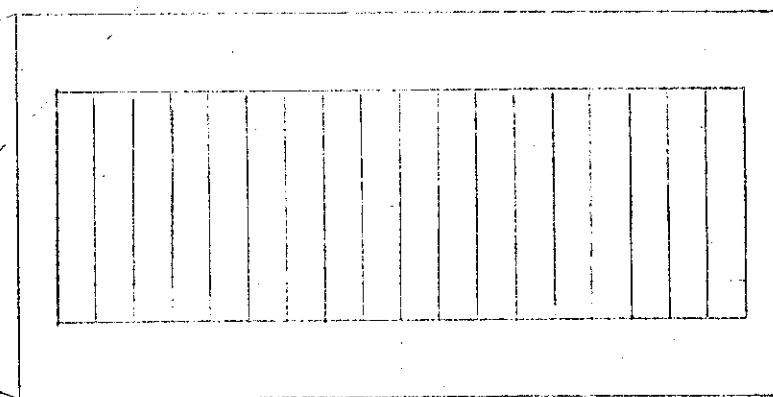
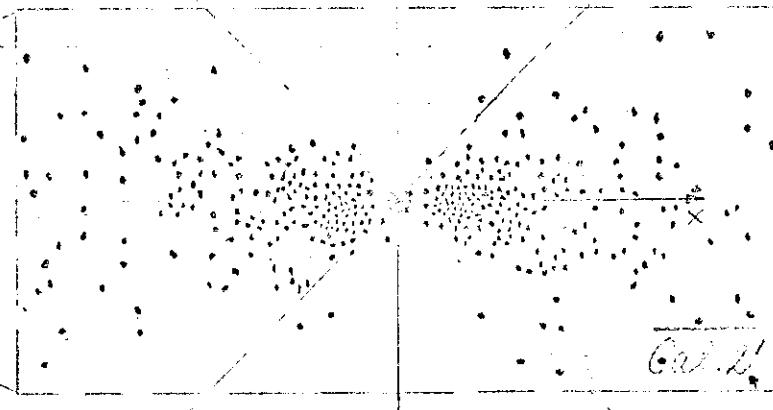
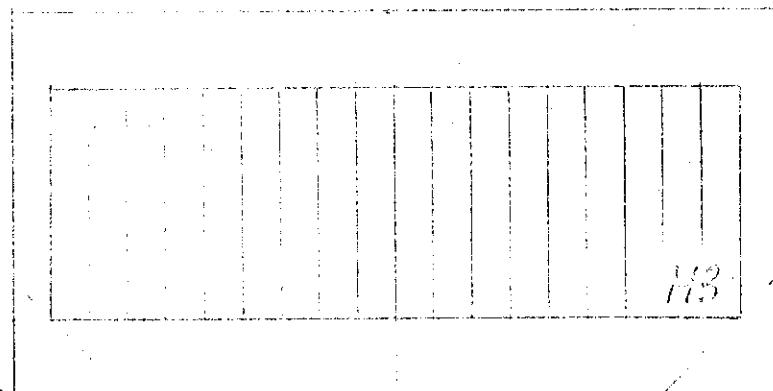
RESPECT TO PELTIER 2.46 ELEMS

(at 10 m/s from origin)

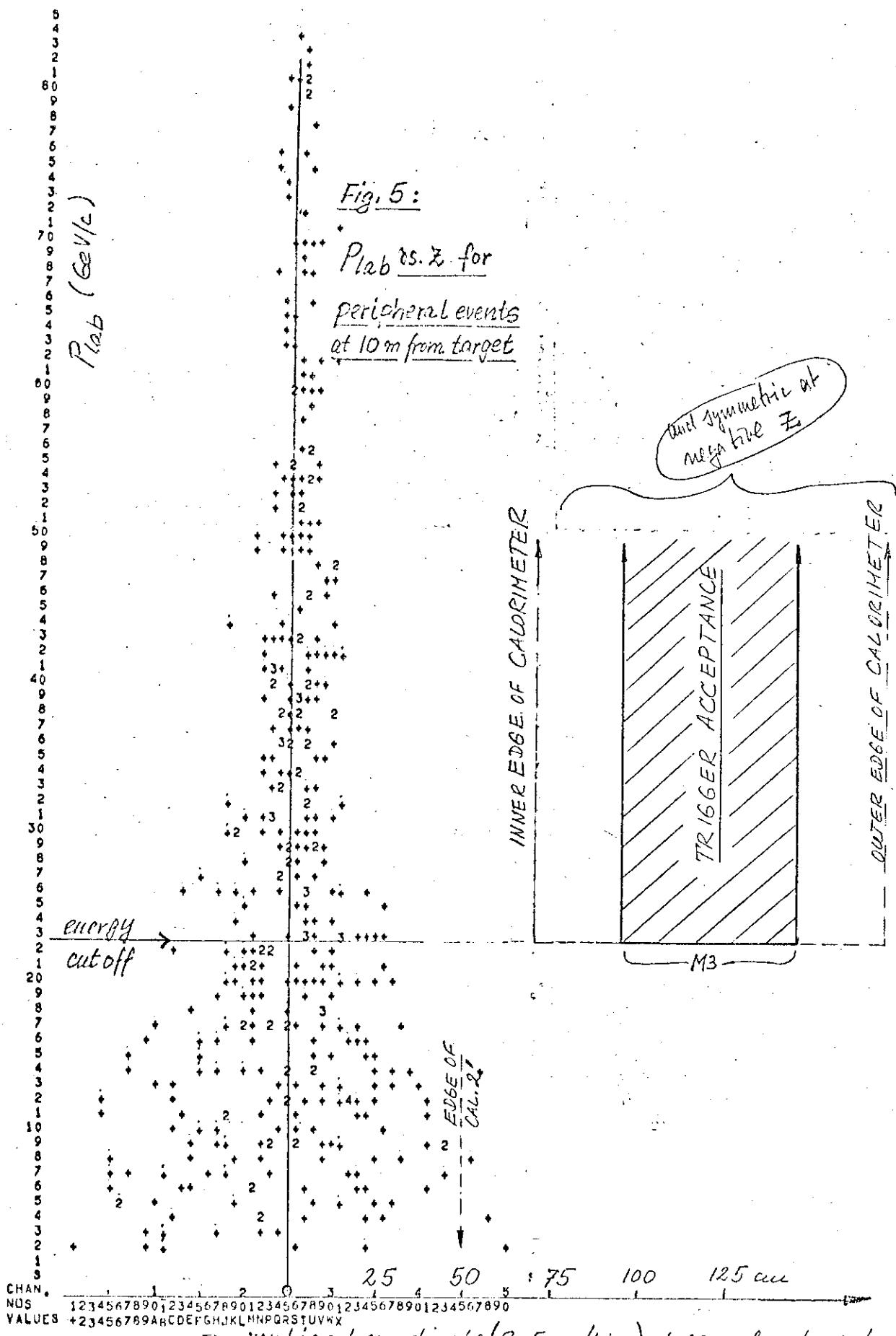
$\varphi = -45^\circ$

Cell 1

$\varphi = +45^\circ$



Mean flow = 1 m/s



$Z = \text{vertical coordinate (2.5 cm/bin) at 10 m from target}$

Fig. 7:  
Acceptance of  $NW^2$   
trigger histograms  
folded into original  
 $d\sigma/dp_t$  distribution

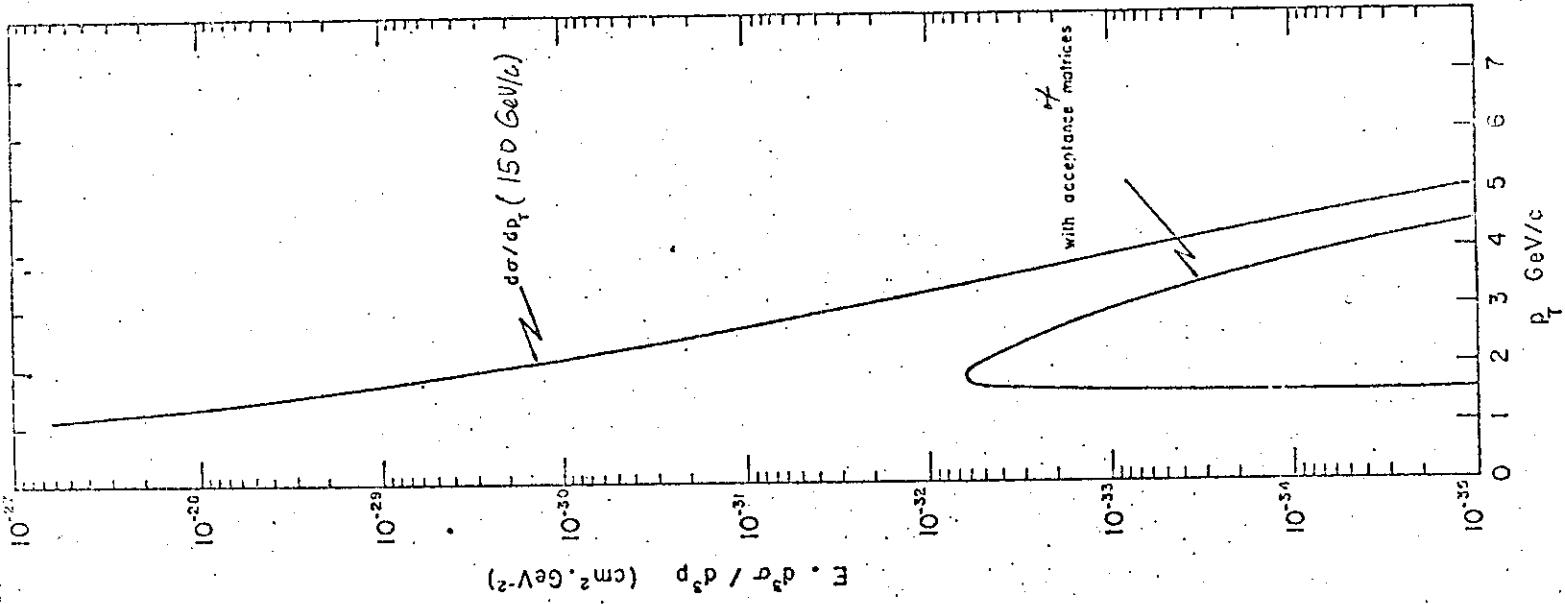


Fig. 6: Acceptance of trigger hodo-  
scopes vs.  $p_t$

$\Delta\phi = \pm 45^\circ$   
 $80^\circ < \theta^* < 100^\circ$  } 1 sterad

(EVENTS GENERATED UNIFORMLY IN  $x_1, x_{11}$ )

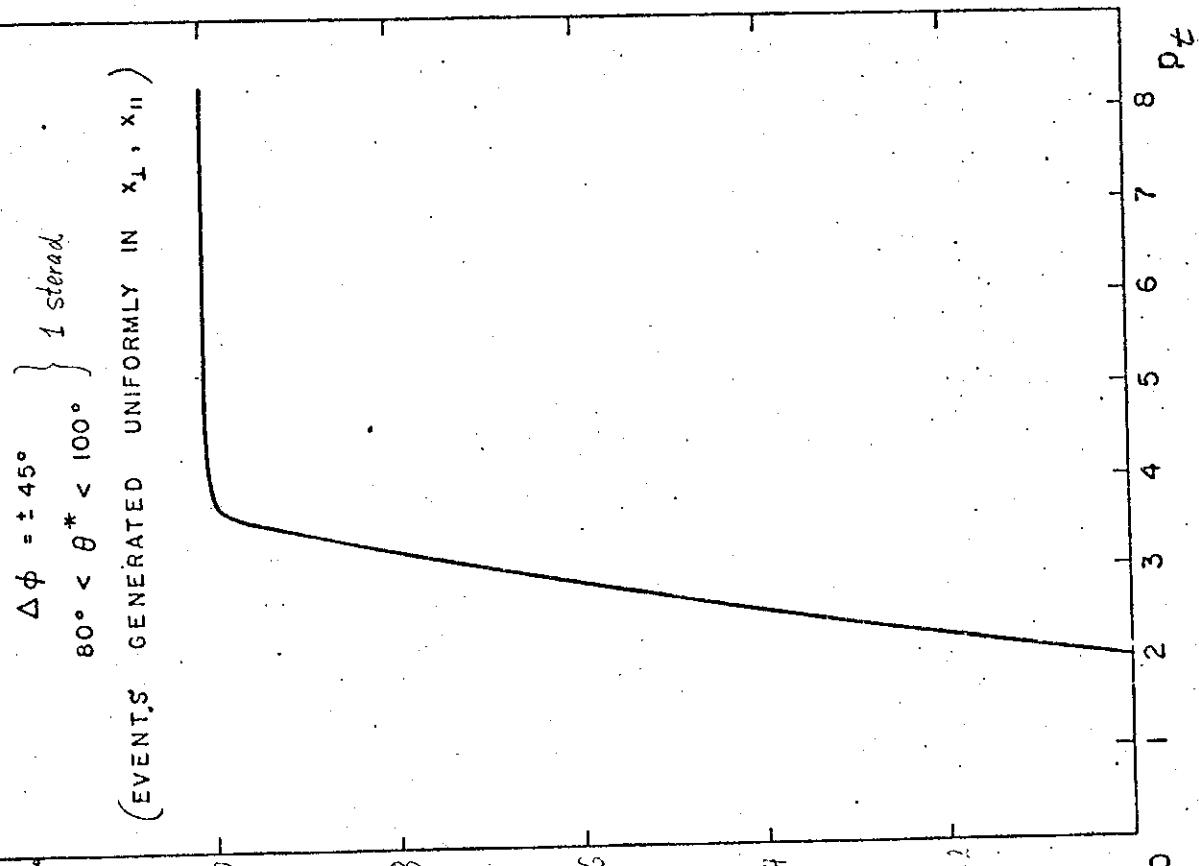
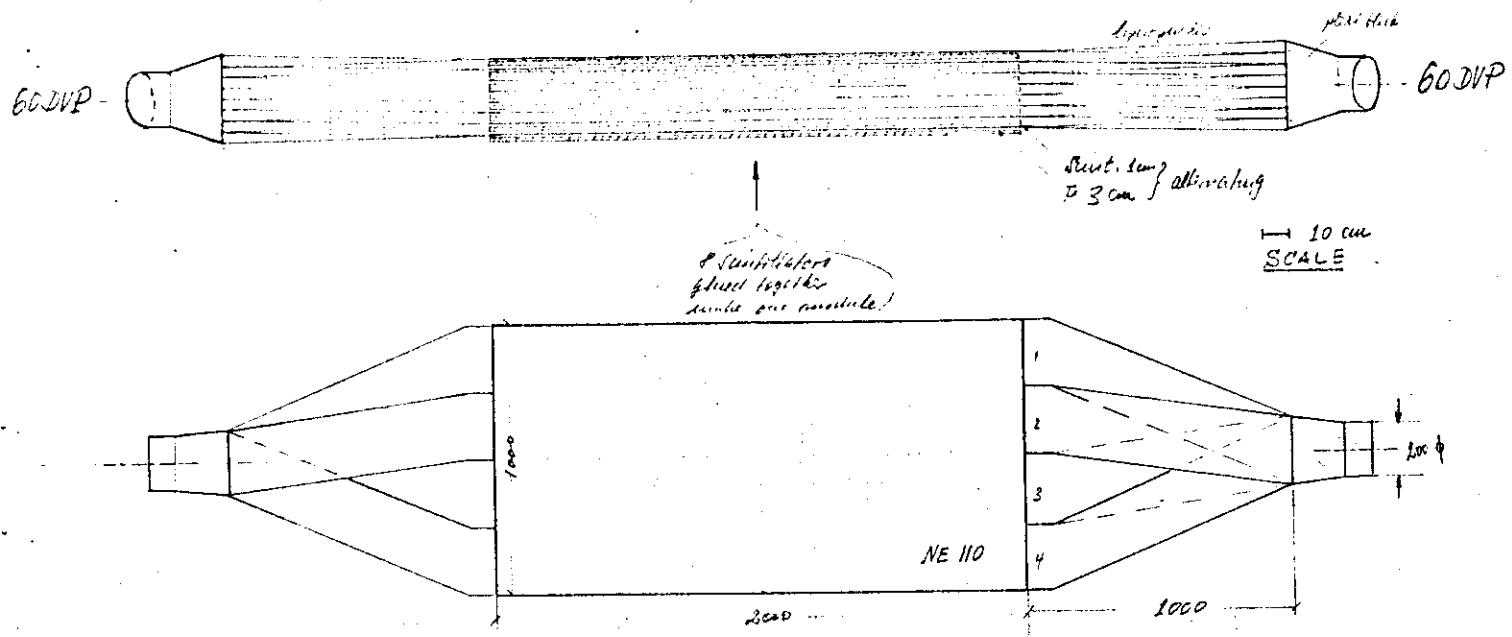
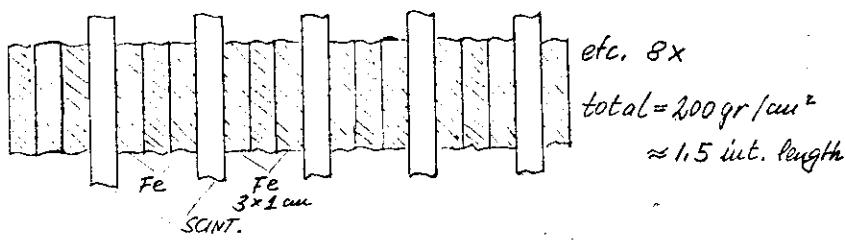


Fig. 9  
Calorimeter Module

21/3 '74 MK



Sequence of Fe-scintillator blocks (scale 1:2):



External light guides:

Each module sheet  
seen by a bundle  
of  $250 \times 10 \text{ mm}^2$   
cables, from both  
ends (surface light  
collection + fast timing).

Fig. 8  
Calorimeter Unit (=6 modules)

22/3 '74  
MK

$$\text{total depth} = 3 \lambda_{\text{int}} (\text{mod. 1+2}) + 6 \lambda_{\text{int.}} (\text{mod. 3-6}) = 9 \lambda_i$$

$$\text{overall dim.} = 2 \times 1 \times 2.5 \text{ m}^3$$

$$\text{weight} \approx 25 \text{ tons}$$

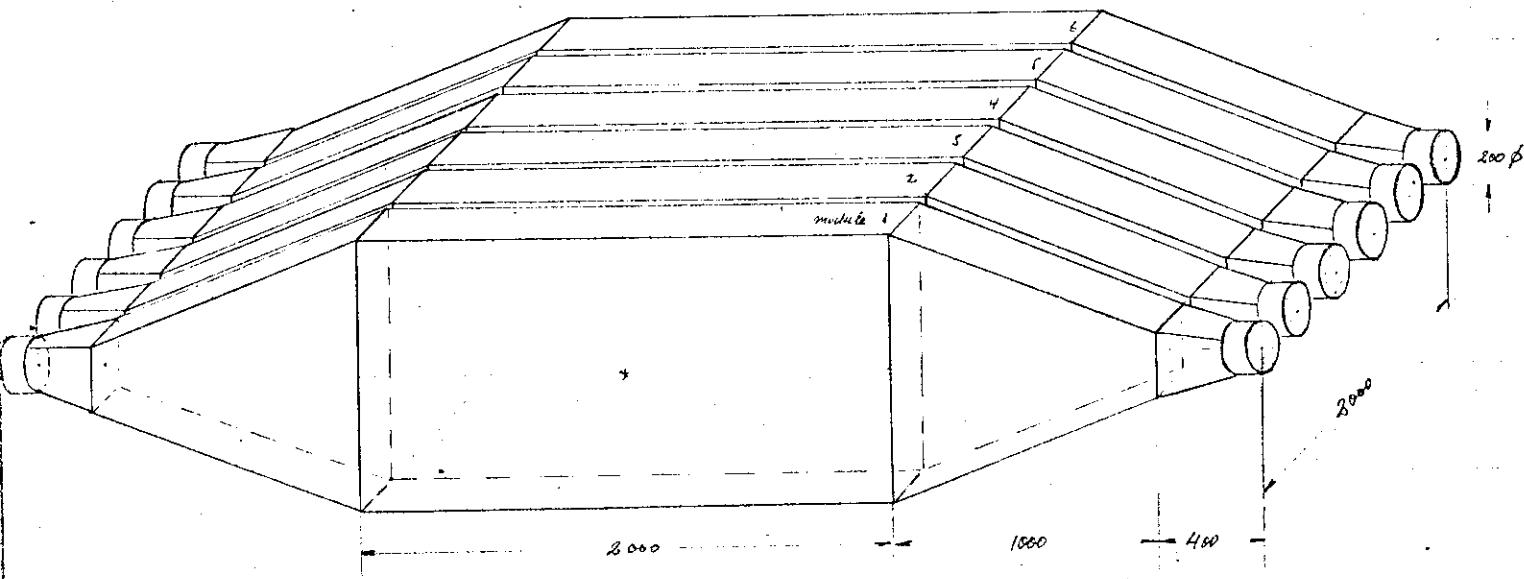
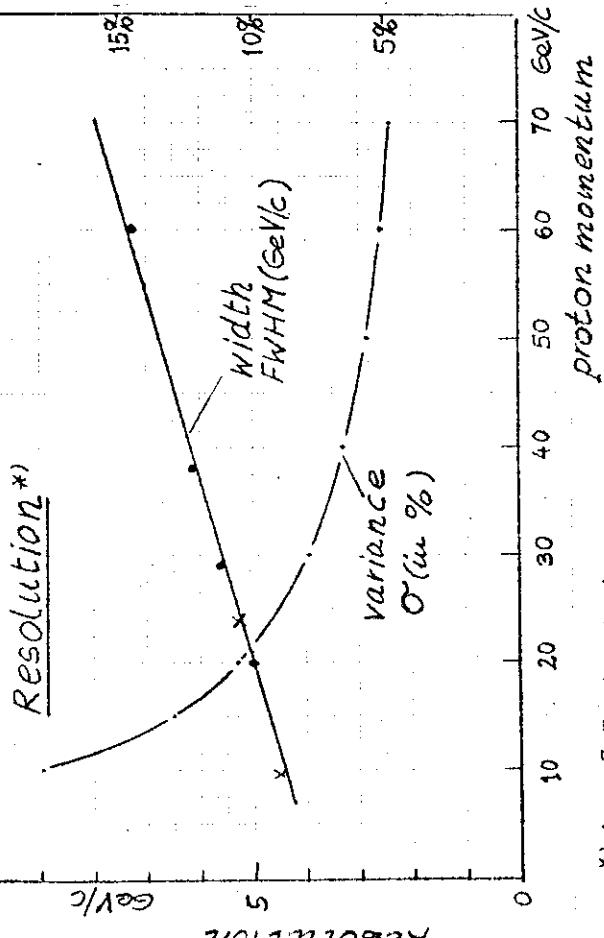
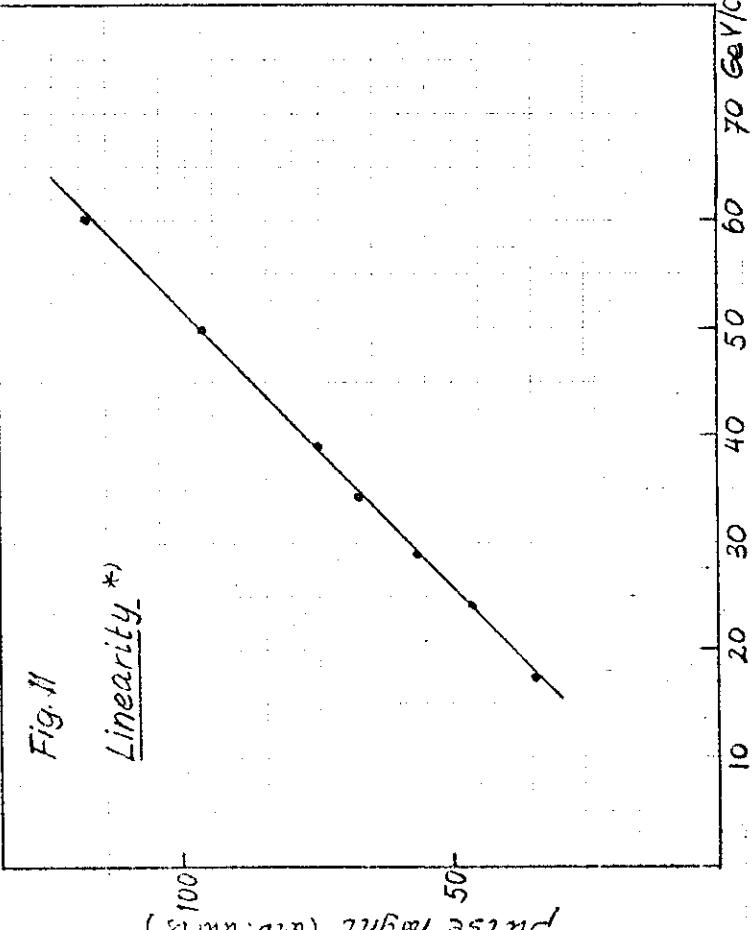


Fig. 10



\* from J. Engler et al.

Fig. 11



calorimeter setting  $R = 2.5$

calorimeter effective efficiency

~95% at  $P_T = 3$

Fig. 12: Expected cut-off function

of the calorimeters ( $R = 150 \text{ cm}$ )

Fig.14: Shower containment (without 6' unit)

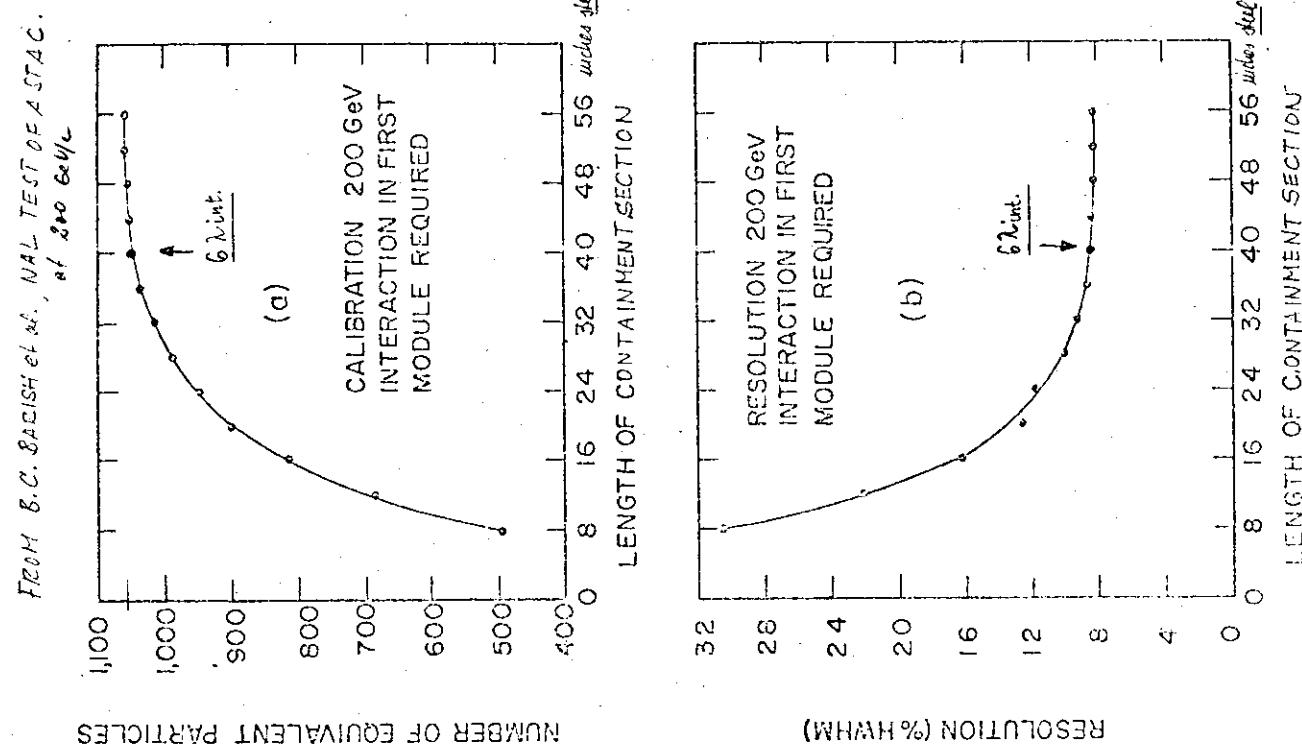
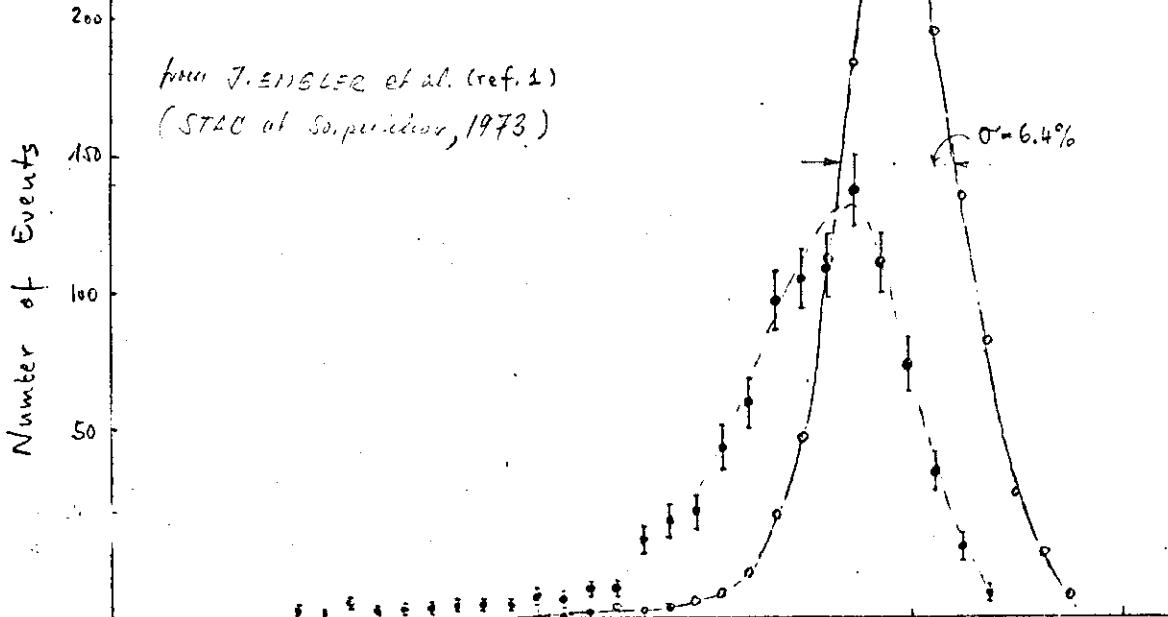


Fig.13: Response of STAC

for 30 GeV Protons

- o- No shower leakage (anticounter on)
- o-- Big shower leakage (anticounter off)



# MEGA MATRIX CORRELATION FOR EVENTS WITH TRACKS IN THE SPARE CHAMBERS

OMEGA MATRIX - CORRELATION  
FOR BACKGROUND EVENTS

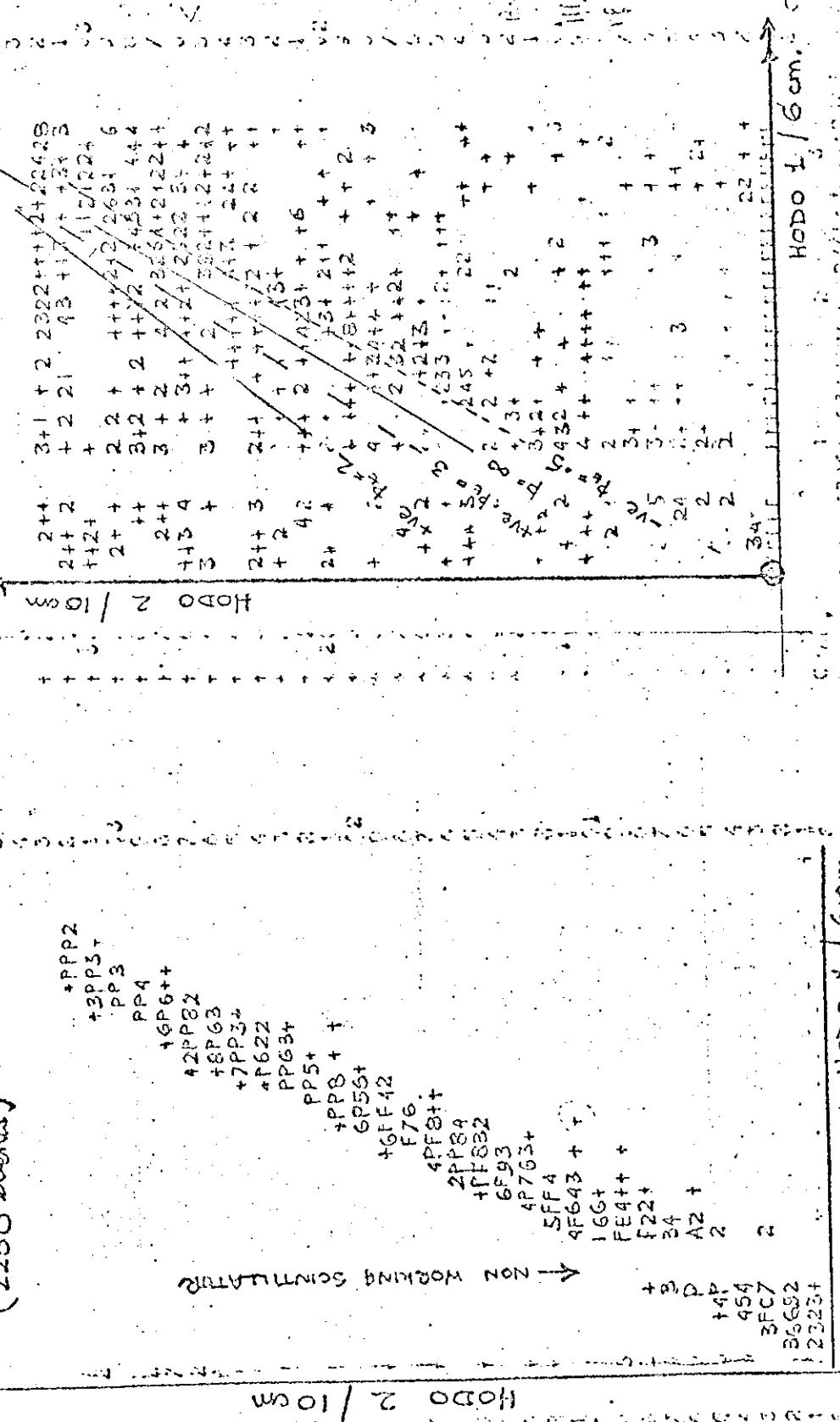


FIG 15a

FIGURE 15b

IV. CERENKOV COUNTERS

1. Capability and performance

Our Cerenkov counters have been designed in order to provide good particle identification together with minimum length. The Cerenkov radiation formula gives the number of photons ( $dN_\gamma$ ) emitted in a medium with index of refraction  $n$  over a given wave length interval  $d\lambda$  as

$$dN_\gamma = \frac{2\pi}{137} L \sin^2 \theta \frac{d\lambda}{\lambda^2}$$

where  $L$  is the counter length and  $\theta$  is the Cerenkov angle ( $\cos\theta = 1/n\beta$ ). In the limit  $\beta = 1$ ,  $\sin^2 \theta = 2(n-1)$  and

$$dN = \frac{2\pi}{137} L 2 \alpha \frac{d\lambda}{\lambda^2} \epsilon_{PC}(\lambda)$$

where  $\alpha = n-1$ ,  $\epsilon_{PC}(\lambda)$  is the photocathode conversion efficiency and  $dN$  is the number of produced photo electrons. Upon integrating one gets

$$N = N_o L 2 \alpha$$

where

$$N_o = \frac{2\pi}{137} \int_{\lambda_2}^{\lambda_1} \epsilon_{PC}(\lambda) \frac{d\lambda}{\lambda^2}$$

In a given counter,  $L$  and  $2\alpha$  are fixed by the length and nature of the gas, so  $N$  is maximum when  $N_o$  is maximum. The value of  $N_o$  is governed by three factors

- a) gas transmittivity  $\epsilon_T(\lambda)$
- b) mirror reflectivity  $\epsilon_R(\lambda)$
- c) photo cathode conversion efficiency  $\epsilon_{PC}(\lambda)$  of photomultiplier (PM)

In the sections which follow each of these factors will be considered.

In terms of these factors we have

$$N_o = \frac{2\pi}{137} \int_{\lambda_2}^{\lambda_1} \epsilon_T(\lambda) \epsilon_R(\lambda) \epsilon_{PC}(\lambda) \frac{d\lambda}{\lambda^2}$$

and for  $\lambda$  in units of  $10^3 \text{ \AA}^\circ$  (i.e.  $10^{-5} \text{ cm}$ )

$$N_o = 4586 \int_{\lambda_2}^{\lambda_1} \epsilon_T(\lambda) \epsilon_R(\lambda) \epsilon_{PC}(\lambda) \frac{d\lambda}{\lambda^2}$$

If for example one takes  $\epsilon_T = 0.9$ ,  $\epsilon_R = 0.8$  and  $\epsilon_{PC} = 0.25$  for the interval  $\lambda_2 = 5.5$  ( $5500 \text{ \AA}^\circ$ ) and  $\lambda_1 = 2.0$  ( $2000 \text{ \AA}^\circ$ ) we get

$$N_o = (4586)(0.9)(0.8)(0.25) \left( \frac{1}{2} - \frac{1}{5.5} \right) = 263 \text{ cm}^{-1}$$

Thus, for light collection through a quartz window PM ( $\lambda \geq 2000 \text{ \AA}^\circ$ ) and reasonably good reflectivity and good transmissivity gases (He, Ne, A,  $\text{CO}_2$ ,  $\text{H}_2$ ,  $\text{CH}_4$  and others) one might expect  $N_o$  values  $\approx 260 \text{ cm}^{-1}$ . In actual practice most Cerenkov systems have values of  $N_o$  of  $100 \text{ cm}^{-1}$  or less because one or several of these factors have not been optimized.

One experiment is reported<sup>(1)</sup> where  $N_o$  of  $160 \text{ cm}^{-1}$  was obtained. In this measurement they used a Quartz window PM (RCA 31000 M), He gas radiator and Al mirror coated with  $250 \text{ \AA}^\circ$  thick protective layer of  $\text{Mg F}_2$ .

It will be the purpose of a test run (in a PS test beam starting at end April) to pinpoint those factors which limit the performance of Cerenkov counters so as, hopefully, to use such an improved system for the proposed experiment. Our presently proposed system is summarized in table 1 and  $N$  versus momentum is plotted in fig. 1.

TABLE 1

| COUNTER | GAS                            | $\alpha$             | L(cm) | $N_o (\text{cm}^{-1})$ | $N (\text{p.e., } \beta = 1)$ |
|---------|--------------------------------|----------------------|-------|------------------------|-------------------------------|
| C1      | N-pentane                      | $18 \cdot 10^{-4}$   | 50    | 100                    | 17.95                         |
| C2      | $\text{CO}_2$ or $\text{CH}_4$ | $4.5 \cdot 10^{-4}$  | 110   | 160                    | 15.80                         |
| C3      | H <sub>2</sub>                 | $1.38 \cdot 10^{-4}$ | 180   | 160                    | 7.95                          |
| C4      | Ne                             | $0.67 \cdot 10^{-4}$ | 300   | 160                    | 6.43                          |

It is clear that our proposed system is well within the optimal limits given above and represents simply an attempt to build a Cerenkov system up to the presently achieved levels. In fact, from the discussion which follows, we have good reasons to believe that values of  $N$  even higher

a) Mirror Reflectivity.

In this domain advances in vacuum evaporation methods<sup>(2)</sup> for deposition and protection of Al mirrors with Mg F<sub>2</sub> or LiF films show that  $\epsilon_R = 0.8$  can be achieved from infrared to far ultra violet (i.e. from 6000 Å to 1100 Å). The reflectivity curves for Al (Mg F2) and unprotected Al mirrors are shown in figure 2. It was found that such protected mirrors Al (Mg F2) did not deteriorate with age. A mirror stored in a air filled box for up to two years lost 1-2% in reflectance even though no dessicant was present during storage. We have found that such mirrors can be obtained commercially in Europe at reasonable prices (~ 130 DM/ 50 x 40 cm<sup>2</sup> mirror) so we envision no problem here. From figure 2 one sees that even down to 1200 Å<sup>o</sup>  $\epsilon_R = .80$  and falls to 20% at 1000 Å<sup>o</sup> so one may take the effective lower limit at about 1100 Å<sup>o</sup>. Above this value,  $\epsilon_R = 0.8$  and constant seems a reasonable representation of the data. Figure 3 shows Al mirrors with Li F protective films. They have a lower low wave length limit but the average reflectivity seems to be worse in the above 1200 Å<sup>o</sup> region. It seems unlikely that any gain can be had by using Li F protected mirrors.

b) Transmission of U.V. in gases.

In this area we have rather fragmentary data<sup>(3), (4)</sup> which is summarized in Table 2. In most cases the transmission  $\epsilon_T$  (through 1 meter of gas) is not known directly but can be inferred from the position of the absorption edge.

TABLE 2

| CHEMICAL NAME | GAS            | $(10^{-4})$<br>$\alpha = n-1$ | ABSORPTION<br>EDGE (Å <sup>o</sup> ) | $\epsilon_T (\lambda)$    |
|---------------|----------------|-------------------------------|--------------------------------------|---------------------------|
|               | He             | .35                           | 584                                  |                           |
|               | Ne             | .67                           | 744                                  |                           |
|               | H <sub>2</sub> | 1.38                          | 1215                                 |                           |
|               | O <sub>2</sub> | 2.72                          | 1971                                 |                           |
|               | A              | 2.84                          | 1066                                 |                           |
|               | N <sub>2</sub> | 2.97                          | 1400                                 | .95(1875 Å <sup>o</sup> ) |

Table 2 (Cont'd)

| NAME                 | GAS                                 | $\alpha (10^{-4})$ | ABSORPTION<br>EDGE (Å) | $\epsilon_T(\lambda)$           |
|----------------------|-------------------------------------|--------------------|------------------------|---------------------------------|
| Methane              | Kr                                  | 4.27               | 1236                   |                                 |
|                      | $\text{CH}_4$                       | 4.40               | 1640                   |                                 |
|                      | $\text{CO}_2$                       | 4.50               | 1920                   | .47(1860), .81(1930), .91(2000) |
| Methyl Alcohol       | $\text{CH}_3\text{OH}$              | 5.86               |                        |                                 |
| Sulfur dioxide       | $\text{SO}_2$                       | 6.86               |                        | .67(3200)                       |
| Ethylene             | $\text{C}_2\text{H}_4$              | 6.96               |                        |                                 |
|                      | Xe                                  | 7.02               | 1470                   |                                 |
| Ethane               | $\text{C}_2\text{H}_6$              | 7.06               |                        |                                 |
|                      | $\text{SF}_6$                       | 7.85               | 1473                   | .95(1875 Å)                     |
| Freon 13             | $\text{CCl}_3\text{F}_3$            | 7.99               | 1970                   |                                 |
| Propane              | $\text{C}_3\text{H}_8$              | 10.05              | 1850                   |                                 |
| Freon 13 Bl          | $\text{CBr}_3\text{F}_3$            | 10.07              | 2600                   |                                 |
| Freon 12             | $\text{CCl}_2\text{F}_2$            | 11.52              | 2220                   |                                 |
| Butane               | $\text{C}_4\text{H}_{10}$           | 14.37              | 1960                   |                                 |
| Chloroform           | $\text{CHCl}_3$                     | 14.55              |                        |                                 |
| Ethyl Ether          | $(\text{C}_2\text{H}_5)_2\text{OH}$ | 15.20              |                        |                                 |
| Carbon Tetrachloride | $\text{CCl}_4$                      | 17.70              |                        |                                 |
| N-pentane            | $(\text{CH}_3)_4\text{C}$           | 18.0               |                        |                                 |

One may infer from Table 2 that He, Ne, A, should be essentially transparent down to 1100 Å, H<sub>2</sub> down to about 1250 Å and Kr down to about 1300 Å.

If one takes  $\epsilon_R = 0.8$  and  $\epsilon_T = 0.9$  for the wave length limits given above we find

TABLE 3

| GAS            | $N_O / \bar{\epsilon}_{PC}$ | $N_O (\bar{\epsilon}_{PC} = .25)$ |
|----------------|-----------------------------|-----------------------------------|
| He             | 2400                        | 600                               |
| Ne             | 2400                        | 600                               |
| A              | 2400                        | 600                               |
| H <sub>2</sub> | 2040                        | 510                               |
| Kr             | 1940                        | 485                               |

So we see that if photocathode efficiencies average 25% over the whole wave length interval ( $1100 \text{ \AA}$  to  $5500 \text{ \AA}$ ) then values of  $N_o$  between 485 and 600 should be possible.

c) Photomultipliers and photocathode efficiencies.

We have investigated existing P.M.'s on the market and find that EMI 9821Q<sup>\*)</sup> 5" diameter (110 mm effective) seems to be the tube best suited to our needs. It has a spectrosil window (fused  $\text{SiO}_2$ ) whose transmission is 50% at  $1700 \text{ \AA}$ , 80% at  $1730 \text{ \AA}$  and 90% at longer wave lengths as shown in Fig. 4a. The various photocathode efficiencies (which include window transmission)  $\epsilon_{PC}(\lambda)$  are shown in Fig. 4b. We will use the tube with bialkali (K-Cs) or possibly the S-20 photocathode. Taking  $\epsilon_T = 0.9$  and  $\epsilon_R = 0.8$  one gets

$$N_o = (4586)(0.9)(0.8) \int_{\lambda_1}^{\lambda_2} \epsilon_{PC}(\lambda) \frac{d\lambda}{\lambda^2} = 3302 \int_{\lambda_1}^{\lambda_2} \epsilon_{PC} \frac{d\lambda}{\lambda^2}$$

which for the (K-Cs) photocathode integrates to

$$N_o = 300 \text{ cm}^{-1}$$

This value should obtain for all gases whose absorption edge is below about  $1650 \text{ \AA}$ . With this tube and using good reflecting mirrors and proper transmitting gases we can certainly achieve the conservative design values given in Table 1.

Another possible way of achieving the largest  $\bar{\epsilon}_{PC}$  over the largest wave length interval is to utilize wave length shifters<sup>(4)</sup> as is common in the field of U.V. spectroscopy<sup>(5)</sup>. The most commonly used material is a thin film of  $\approx 3 \text{ mg/cm}^2$  of Sodium Salicylate deposited on the PM entrance window. This material has the unique property of absorbing all U.V. photons between  $600 \text{ \AA}$  and  $3600 \text{ \AA}$  and emitting an equal number of photons at  $4300 \text{ \AA}$  which is near the peak of the P.M. response. It emits half the photons forward (with  $\cos\theta$  distribution) and half backward so assuming none of the backward photons are utilized one can expect values of  $N_o$  exactly half of that listed in table 3 (i.e.  $N_o = 300 \text{ cm}^{-1}$  for He, Ne, A 255 for  $\text{H}_2$  and 240 for Kr). These values could probably be increased even further by constructing proper reflectors about the P.M. which allow detection of some fraction of the backward emitted

is that it has a 10 ns decay time. Other wave length shifters are available (with shorter decay times) such as p-terphenyl, p-quaterphenyl, diphenylstilbene PPO, POPOP and perhaps most interesting  $\text{Ca WO}_4$ : 7% Pb which has been reported<sup>(6)</sup> to give more than one visible photon for each U.V. photon absorbed.

2. Test Program.

We are constructing apparatus for a run in a PS test beam (electrons) to measure  $N_o$  for various gases, photomultipliers (with and without wave length shifters) and mirrors. The method which we will use to measure  $N_o$  follows closely the technique used Yovanovitch et al<sup>(1)</sup> with a slight variation. From the relation  $N = N_o L 2 \alpha$  we can write  $\alpha = \alpha_o P$  where  $\alpha_o = (n - 1)_{P=1}$  and P is the pressure in atmospheres. Thus

$$N = N_o L 2 \alpha_o P$$

The inefficiency of a counter is  $e^{-N} = 1 - \epsilon$  where  $\epsilon$  = efficiency. The method of Yovanovitch et al<sup>(1)</sup> was to plot  $- \ln(1 - \epsilon)$  vs P and determine the slope  $N_o L 2 \alpha_o$ . Since L and  $\alpha_o = (n - 1)_{P=1}$  were known then  $N_o$  was determined. In the measurements the plot of  $- \ln(1 - \epsilon)$  vs P was linear over several decades indicating that the above formulation is reasonable. In our case we wish to determine  $N_o$  without varying the gas pressure so we will vary the effective length L by moving a baffle in the C gas region.

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FIGURE CAPTIONS

- 1 Number of photoelectrons versus momentum ( $P_K$ ,  $P_\pi$ ,  $P_P$ ). Threshold of  $C_1$  set at 6 photoelectrons to avoid counting  $\pi$ 's as  $K$ 's because of  $C_1$  inefficiency.
- 2 Reflectivity of Al ( $Mg F_2$ ) mirrors vs wave length.
- 3a Reflectivity of Al ( $Li F$ ) mirrors vs wave length.
- b Reflectivity of Al ( $Mg F_2$ ) mirrors vs angle of incidence.
- 4a Transmission of various photomultiplier window materials vs wave length.
- b Photocathode efficiencies  $\epsilon_{PC}$  for various photocathodes vs wave length.

22.8 26.6 30.4 34.2 45.6 49.4 53.2 57.0 60.8 64.6 68.4 72.2 76.0 79.9 83.6 87.4 91.2 95.0 98.8 102.6 106.4 110.2 114 117.9 121.6 125.4 129.2  
 3.4 4.0 4.5 5.1 5.7 6.2 6.8 7.4 8.1 8.5 9.1 9.6 10.2 10.7 11.3 11.9 12.0 12.6 14.1 14.7 15.3 15.8 16.4 17.0 17.5 18.1  
 $\Sigma 2, \beta=1$

ELECTRONIC N

$\Sigma 2, \beta=1$

FIG. 1

$\Sigma 3, \beta=1$

$\Sigma 4, \beta=1$

THRESHOLD

THRESHOLD

THRESHOLD

THRESHOLD

$\Sigma 5$

THRESHOLD

THRESHOLD

THRESHOLD

THRESHOLD

THRESHOLD

THRESHOLD

$\Sigma 2$

$\Sigma 3$

$\Sigma 4$

$\Sigma 5$

$P_e (\text{GeV}/c)$

$e^+$

$e^-$

$e^+$

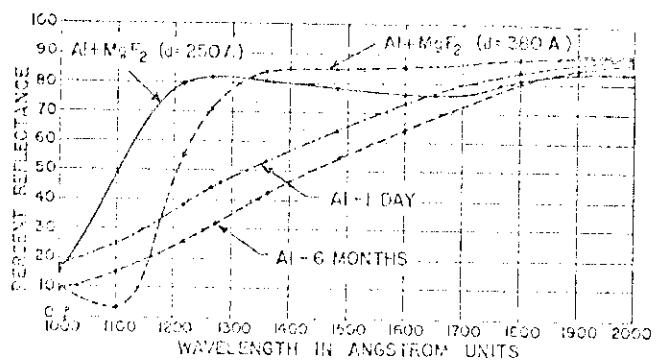


FIG. 2 Vacuum ultraviolet reflectance of evaporated aluminum with and without protective layers of MgF<sub>2</sub> of two different thicknesses (250 and 380 Å). The reflectance of unprotected aluminum films is shown after 1 day and after 6 months of normal aging.

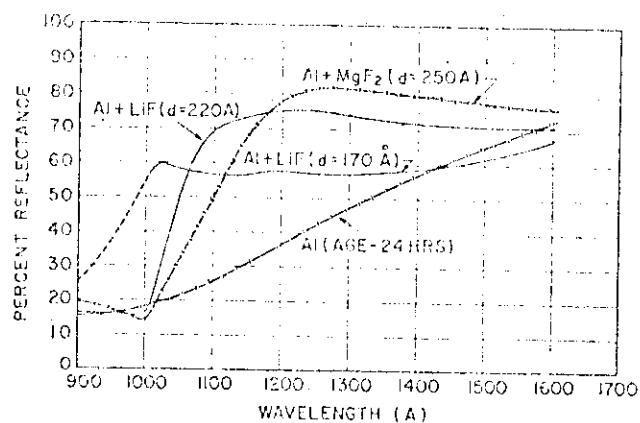


FIG. 3 (a) Vacuum ultraviolet reflectance of evaporated aluminum with and without protective layers of LiF of two different thicknesses (170 and 220 Å). The reflectance of aluminum protected with 250 Å of MgF<sub>2</sub> is also shown.

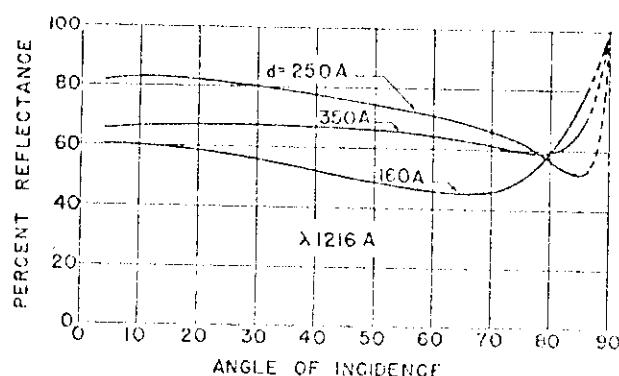


FIG. 3 (b) Reflectance of MgF<sub>2</sub> protected aluminum films as a function of incidence angle for various thicknesses of MgF<sub>2</sub>. (Wavelength: 1216 Å.)

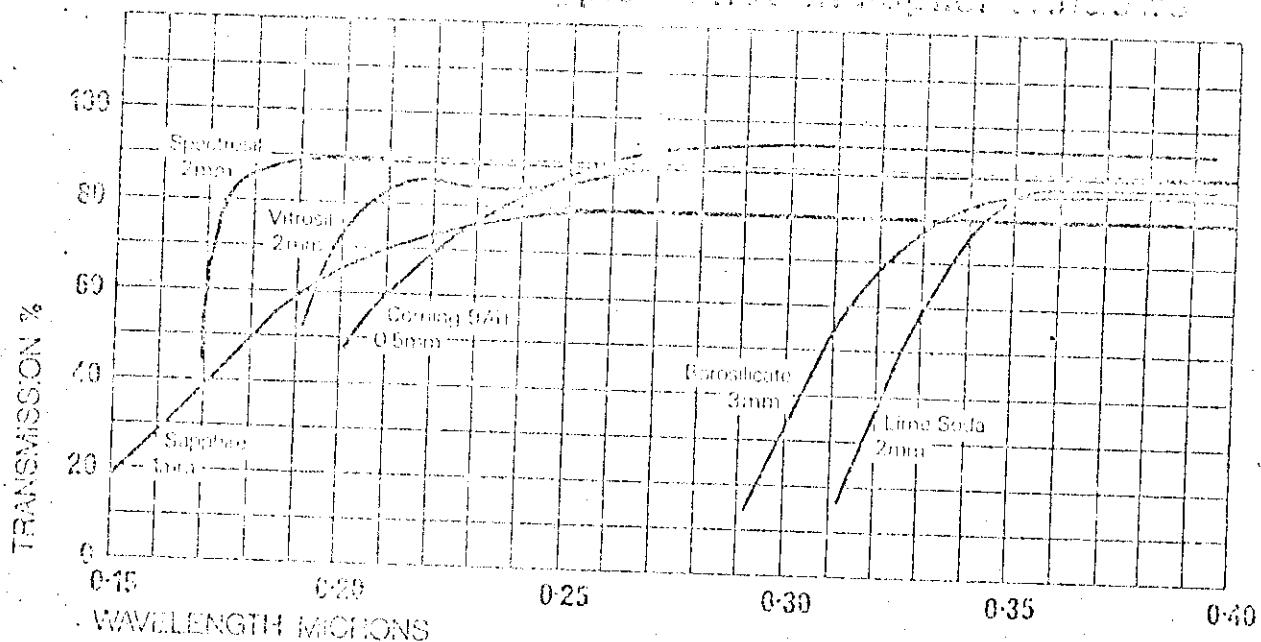
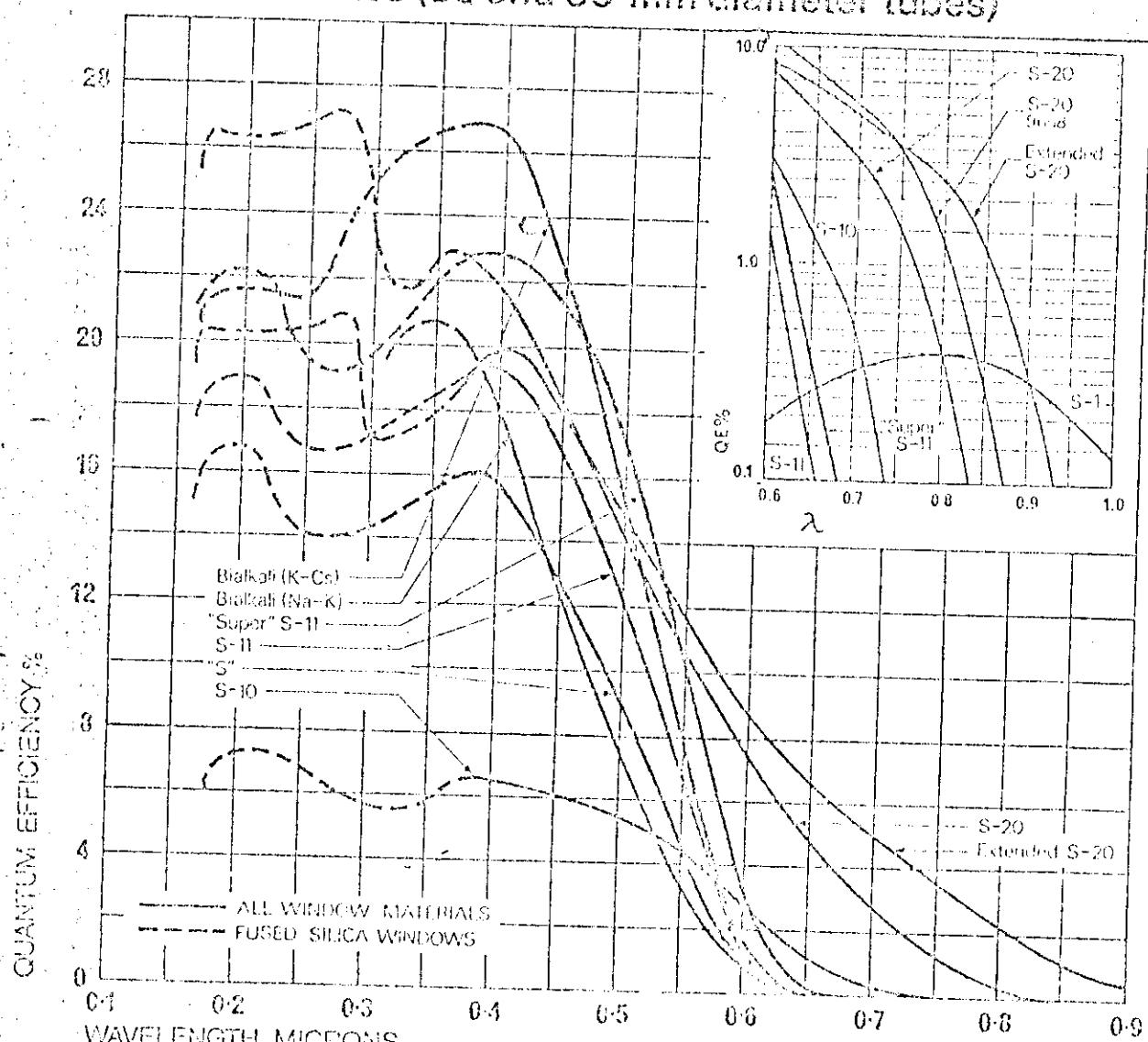


FIG. 4a

### Typical Spectral Response Curves for ENI Photocathodes (50 and 30 mm diameter tubes)



V. VERTEX DETECTOR

The vertex detector is made up of modules of MWPC's with three planes per module. The chambers are positioned inside the gap of a magnet such as "GOLIATH" of Saclay (Fig. 1) which has 2 m diameter pole pieces, 1.2 m gap and consumes 2.7 MW at 17 K gauss.

The number of modules and their disposition has been specifically designed to optimize the pattern recognition programs discussed in section VIII.

We distinguish forward and side modules, the former being perpendicular and the latter parallel to the beam direction. Each forward module (area  $1.0 \times 0.8 \text{ m}^2$ ) consists of one plane of vertical wires and two planes of inclined wires ( $\pm 25^\circ$  with respect to the vertical). Each side module (area  $0.6 \times 0.8 \text{ m}^2$ ) consists of one vertical plane, one horizontal and one plane of wires inclined at  $5^\circ$ . The sense wires are made of tungsten (gold plated), 20  $\mu\text{m}$  diameter and stretched at 35 gm. The wire spacing is 2 mm at a distance of 3 mm from the high voltage planes (50  $\mu$  diameter Cu-Be wires at a tension of 100 gm). The total number of wires in the vertex detector is of the order of 16000.

The mechanical conception of the ensemble has been studied in detail to satisfy the following conditions:

- a) To obtain a precision of 0.2 mm or better in the positioning of wires within the same module and in the relative positioning of the modules.
- b) To guarantee good precision and stability of the ensemble relative to the SPS floor and to insure interchangeability amongst modules.
- c) To limit the amount of material per module so as to minimize the multiple scattering for low energies particles,

to reduce the  $\delta$ -ray production (which limits the detection efficiency and complicates the pattern recognition by multiplying the number of wires hit) and to limit the conversion of  $\gamma$  rays from  $\pi^0$ 's (which contribute to the background of the experiment).

The present design achieves the figure of 1 radiation length per 100 m of particle path.

The frame which supports the modules is made of stainless steel and will be fixed such as to minimize the displacement of the system when the magnet is energised. The standardised modules are positioned on the frame, with the precision mentioned above, by ball bearing rollers which provide guidance when setting the modules in place (Fig. 2). In fig. 3 we show the prototype of a side module partially wired. The frame has the form of a C with the horizontal wires being attached at the open end to a 3 mm diameter Cu-Be wire under a tension of 60 Kg. This method of frameless support of the horizontal wires has been tested with success. The lower part of the frame is hinged so that when transferring the module from inside the magnet to an external frame any slight difference in the two supporting frames can be adjusted. The forward modules will be desensitised in the region of the primary beam ("beam-killers" technique). Fig. 4 shows details of the wire mounting. The wires are clamped, not soldered, in copper tubes at their ends. If a wire breaks in a given module it can be replaced without disassembling the module in a relatively short time ( $\sim 1/2$  hour). The new wire is introduced through the outside frame by a stainless steel needle and guided to the corresponding hole by means of a magnetized shaft.

Various solutions are under study for the associated electronics and the final choice depends on how much real time pre-treatment of the data is required in order to reduce the rate of data taking to a manageable level.

The amplifiers, placed outside the magnet, are connected to the wires by "twisted pairs" of 3 to 4 meters length. The prototype, now under test, has a threshold of 1  $\mu$ A (which is necessary for a chamber functioning with a classical gas mixture of Argon-Isobutane). It has a 40 MHz band-width and the dead-time of a wire is 150 ns. Two or three stages of buffer memory will be available in order to be able to make logical decisions on data retention without increasing the dead-time of the system.

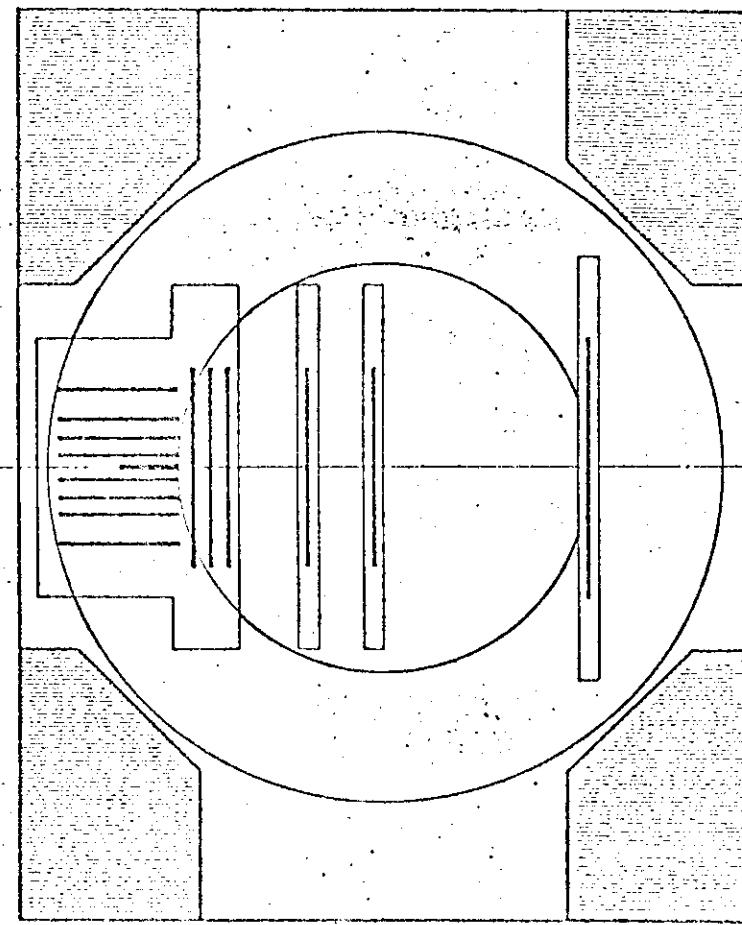
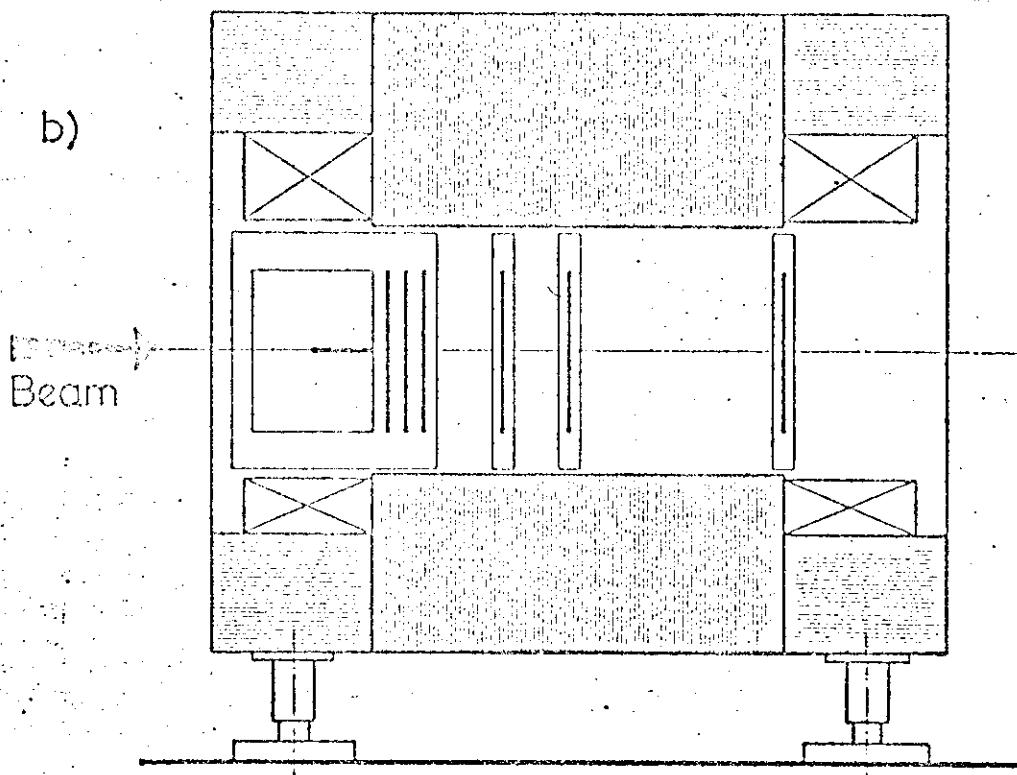
A side module will be completely tested in a particle beam by the end of the summer. During this period a forward module will be completed; testing of this module will go on to the end of the year (1974). The serial production of both side and forward modules could then start at the beginning of 1975.

FIG.1

VERTEX DETECTOR

a) plan view

b) elevation



1m

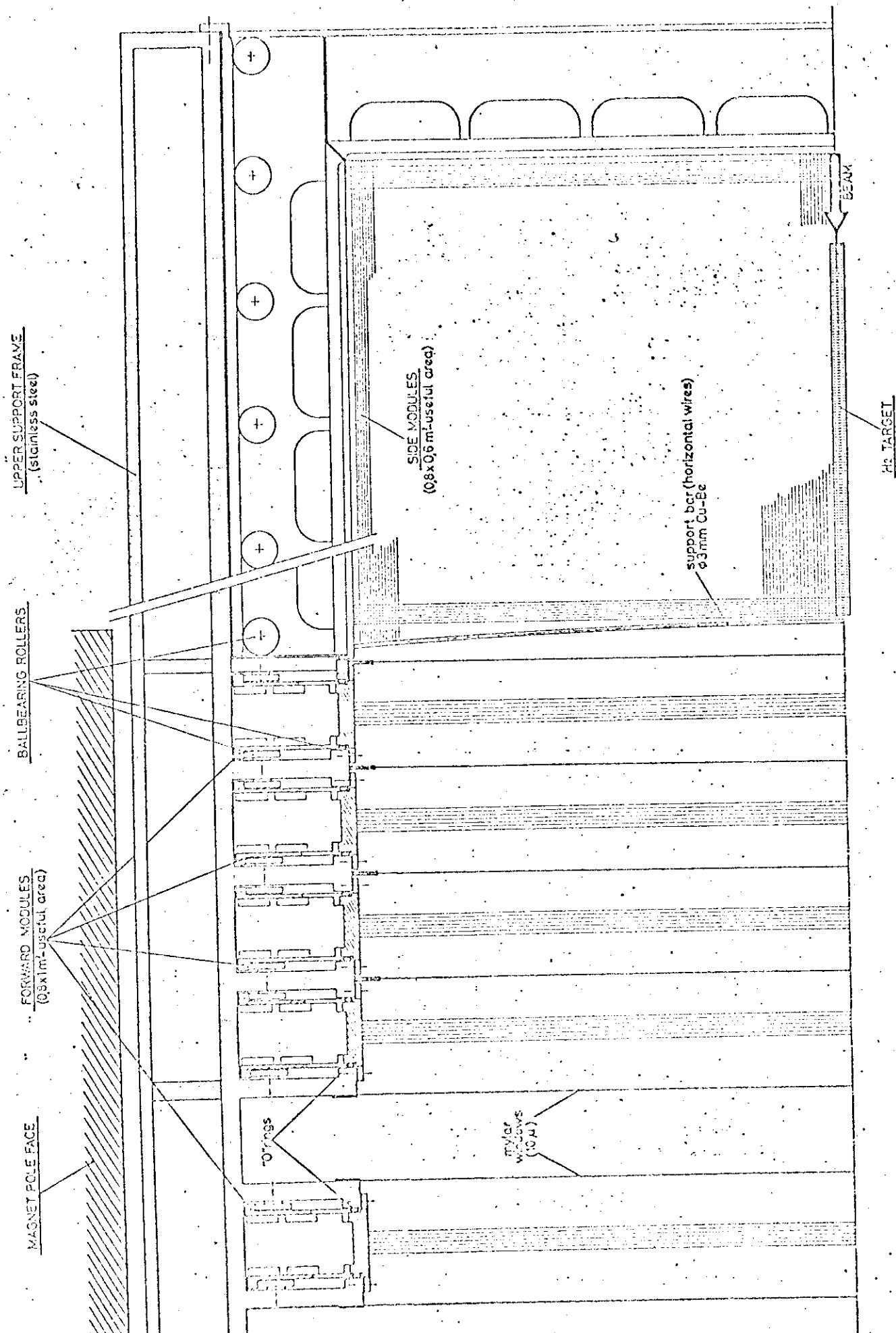


FIG. 2

VERTEX DETECTOR (ASSEMBLY OF UPPER HALF)

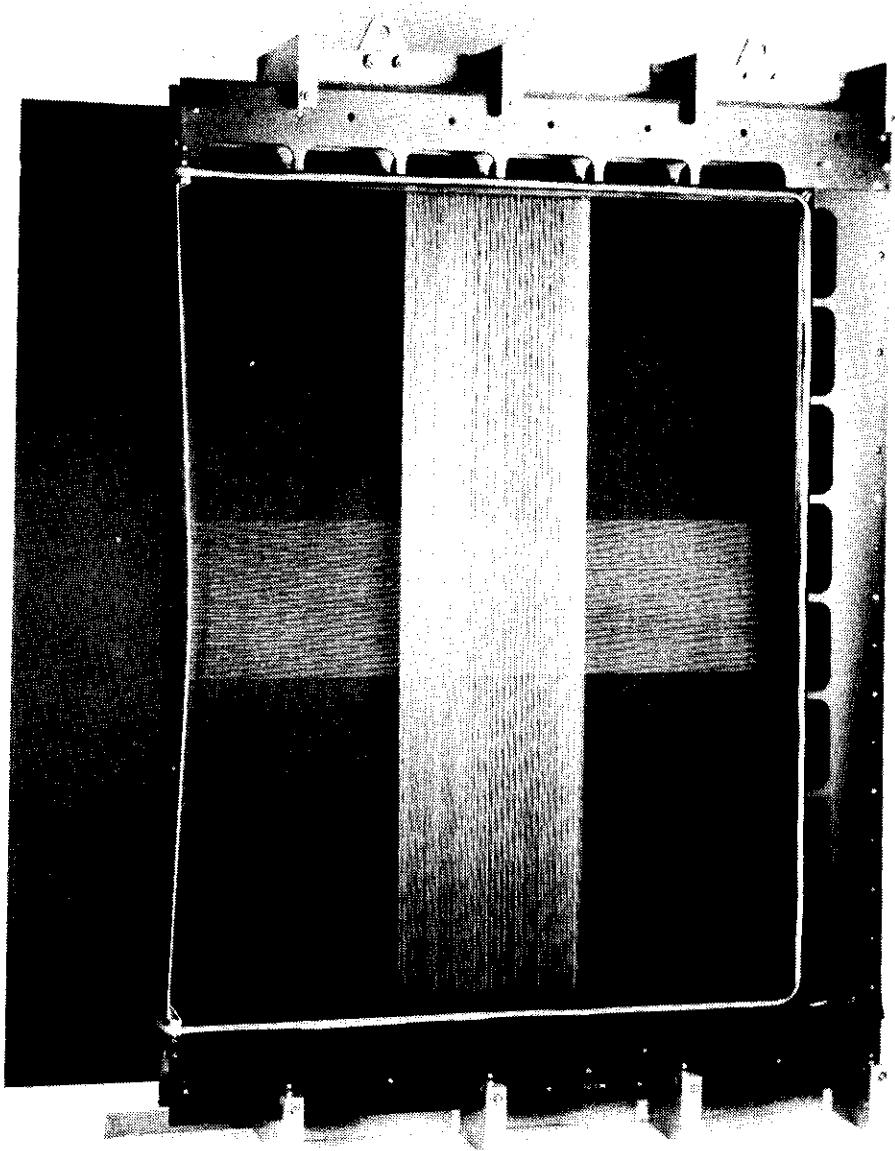
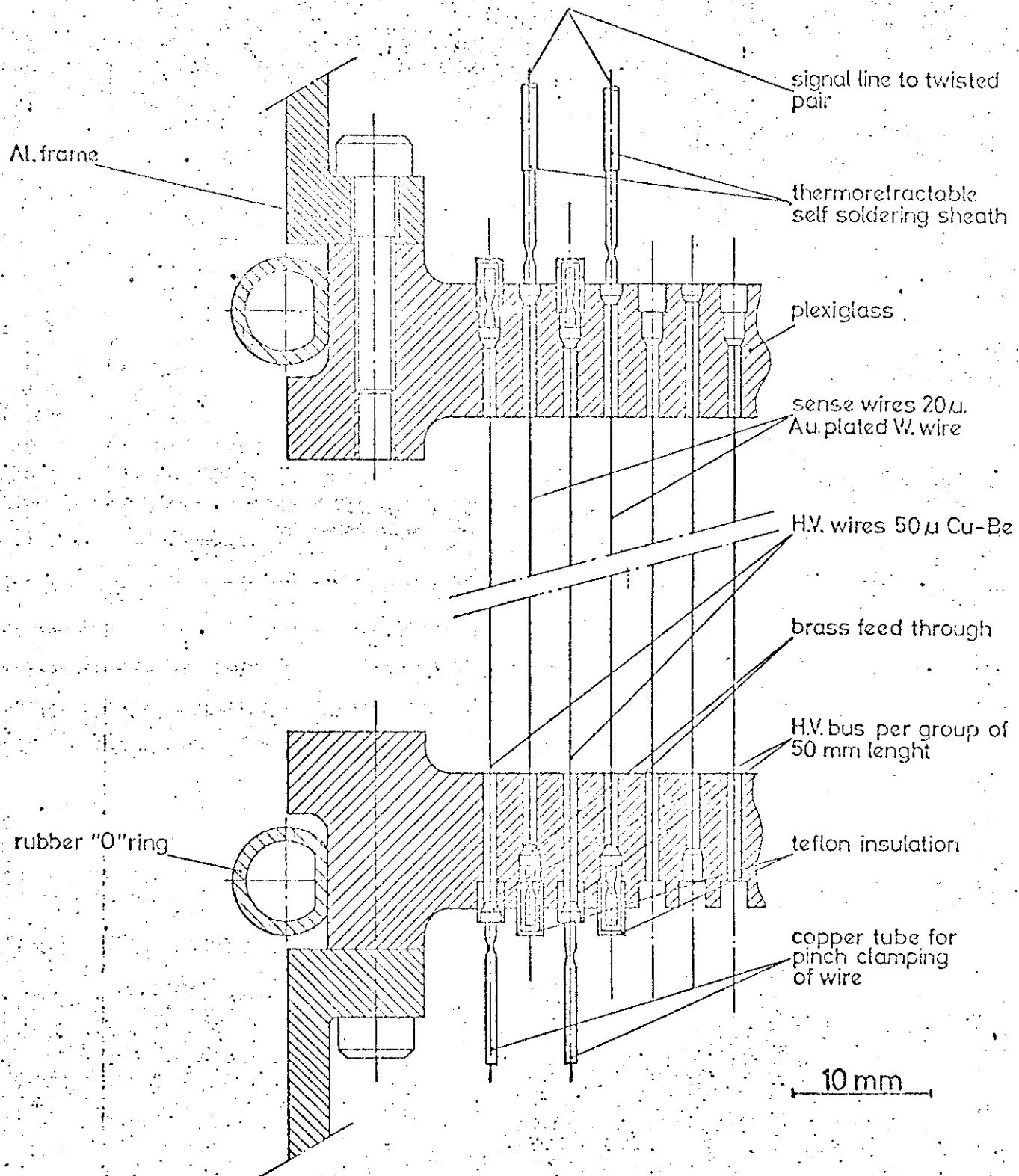


FIG. 3 SIDE MODULE



-FIG.4-

DETAILS: WIRES FIXATION AND ELECTRIC CONNECTION

VI. FORWARD DETECTOR

The choice of drift chambers for the lever arm situated outside the magnetic field appears the only realistic possibility to obtain the necessary experimental space precision of  $\pm 0.3$  mm and  $\pm 0.6$  mm over the required dimensions of  $2 \times 2 \text{ m}^2$  and  $4 \times 4 \text{ m}^2$  respectively.

The wire separation is fixed at 2 cm due to considerations of cost, resolution time (300 nsec) and multitrack resolution necessary within the forward diffraction cone. We are also studying a MWPC design to cover the central region in an angular interval  $\Delta\theta = \pm 3^\circ$  with respect to the beam.

The rate of accidental tracks coming from interactions occurring during the resolution time of the chambers will be eliminated by paralysing the trigger during an equivalent time after each detected interaction. This procedure reduces the effective beam intensity by 20% for a beam flux of  $10^7$  particles/second. The number of background tracks per event due to beam-halo muons is estimated to be  $\sim 0.3/\text{m}^2$ .

In order to overcome the left-right ambiguity in locating the particle position with respect to the sensitive wire we use two planes displayed by 1/2 of the sensitive wire spacing. The sensitive wires are of gold plated tungsten, 50  $\mu\text{m}$  in diameter spaced 2 cm apart and at positive HV. Field wires, at negative HV are placed regularly in between the sensitive wires in order to linearise to a good degree the drift speed. These wires are of Cu-Be and have a 100  $\mu\text{m}$  diameter.

The cathode planes are at ground potential and are made of mylar strips, 10 cm wide, 25  $\mu\text{m}$  thick aluminised on both sides. The strips are stretched by means of springs (see figure 6). An anode-cathode distance of 1 cm. establishes a near radial structure for the electric field.

The position measurement is achieved by measuring the difference in the collection time of the two sensitive wires touched. The correction due to the incident angle of the track is relatively easy, and the linearity of the drift velocity is sufficient for the required spatial accuracy. No ambiguities in reconstruction occur since the angle of incidence is  $< \pm 15^\circ$ . The method of measuring the difference in the drift time has the advantage of reducing the errors coming from uncertainties of the drift velocity (the time difference is zero when the two collection times are equal).

Each chamber (see figures 1 and 2) consists of 2 modules (each module having 2 displaced planes) with horizontal and vertical coordinates and 1 plane of wires at  $30^\circ$  in order to resolve point ambiguities (2 cm spacing between wires). In order to reduce the effects of thermal expansion the points of support are placed on the axes of symmetry (Figure 1). The study of the mechanical construction is well advanced and a prototype of  $2 \times 2 \text{ m}^2$  can be constructed, following the planning, for the end of the year.

The chamber electronics does not pose any serious technical problem and is more one of choosing the cheapest method capable of giving the accuracy required. The amplifiers attached to each wire have been designed and tested. The sensitivity is  $2 \mu\text{A}$  for a maximum slewing time of 3.5 nsec. They contain two fast transistors (BSX27) and an amplifier (MC 10116).

The time coding system is not yet frozen. Several solutions are possible (time-stretcher or analogue system associated to each wire). Within the limits of precision desired, counting frequencies of 100 and 50 MHz are in principle sufficient for the chambers of  $2 \times 2 \text{ m}^2$  and  $4 \times 4 \text{ m}^2$  respectively and pose no problems. We have developed a method which consists in passing the signals of the wires onto a delay line. The delay of each cell, coupling 2 sensitive wires relative to the next, is 360 nsec. This is achieved by means of 3 monostables of

120 nsec each placed in series in order to reduce the dead-time; it will assure a precision on the propagation time of the cell of  $\sqrt{3} \times (0.02 \times 120) = 4$  nsec. The pulses are synchronised in phase at the end of each cell by a 100 MHz voltage. The accuracy of the time between two successive pulses (taken as a multiple of the period) becomes, in this way, independent of the delay line length; this is a gain over the quadratic sum of the fluctuations of each cell. Such a system is the fast equivalent of the magneto-strictive delay lines attached to wire spark chambers. In this way we need only a number of counters equal to twice the maximum number of particles expected if the measurement is done with respect to an external time reference. The method reduces to a minimum the number of counters. By dividing the chambers into lengths of 1 meter, the dead-time due to the propagation of the line will be 36  $\mu$ sec; this is acceptable if we compare it with the total decoding time of 400-500  $\mu$ sec.

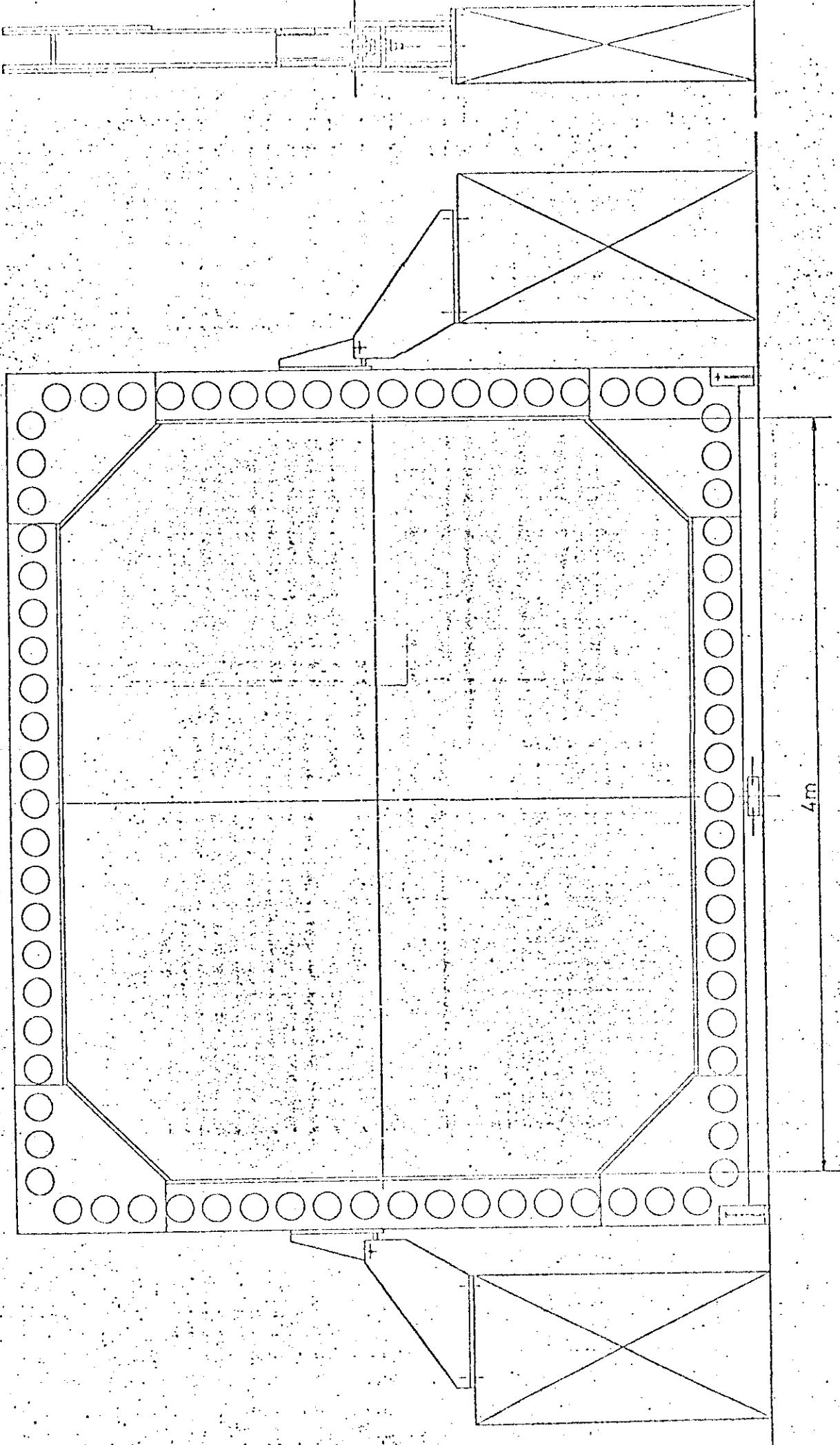
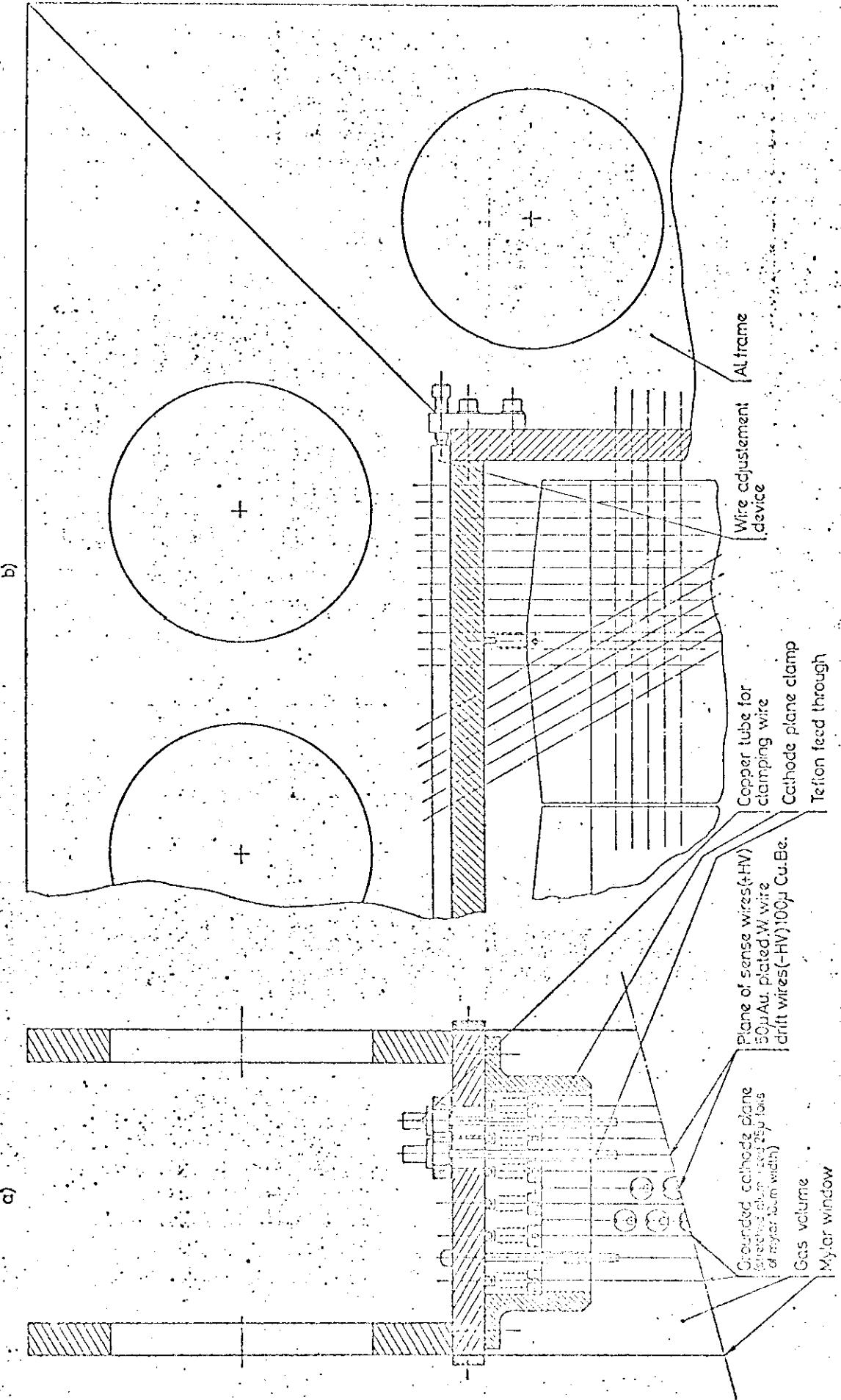


FIG. 1  
DRIFT CHAMBER —  
General construction principle.



VII. DATA ACQUISITION

The information coming from the apparatus is read, decoded and stored by the system described below.

The number of events to be recorded per accelerator cycle is  $\sim 100$ . Each event consists of 800 words of 16 bits for a charged particle multiplicity of 8. The duration of the data acquisition is  $\sim 0.5$  seconds every 4 or 8 seconds. If we wish to reduce the loss of events due to the system dead-time to less than 20%, the recording speed must be at least  $10^6$  words/second. The storing of this information must then be done at a speed of 20000 words/second; these must then be written onto magnetic tape at  $5 \times 10^7$  words/hour (i.e. 3 tapes per hour).

The computer needed for these operations must have a minimum memory of 64000 words. The computer will control the data acquisition, memorise the information during the bursts and perform a certain number of technical controls. The following peripheral equipment will be needed:

- (i) A CAMAC interface adapted to the 0.8  $\mu$ sec fast memory access time; it should have direct access to the computer memory.
- (ii) A high performance tape unit: it should be capable of working at a speed of 75 inches/sec with a density of 1600 bytes/inch.

Two types of control will be performed by the computer. First, an efficiency check of all the detectors for each event. Second, a stability check of the detectors (e.g. voltages, multiplier amplifications, magnet currents and fields, gas flows, etc..) to be done between bursts.

In addition to this computer, it would be an advantage to be connected to a more powerful computer. This would allow a detailed study of the operation of each detector, the calibration of the geometry with straight tracks and all the operations usually performed during the debugging stage of the apparatus. During data-taking it would allow the complete analysis of a sample of events. An IBM 360-40 would be suitable for this role. Alternatively, one could have a data link to one of the larger CERN computers.

Much of the equipment mentioned above is already available to the collaborating laboratories, viz:

- PDP 11/40 computer with 8K memory and basic peripherals.
- Fast electronics.
- CAMAC chassis and CAMAC modules, scalers, pattern units, digital voltmeter, display and its interface.

The missing equipment is:

- 4 blocks of 16K words.
- 2 magnetic tape units (1600 bpi, 75 ips).
- 1 magnetic tape controller.
- 1 CAMAC interface for PDP 11.
- 1 read-out logic for digital MWPC.

#### VIII. PATTERN RECOGNITION

As described in the original proposal we have chosen a disposition for the MWPC's and drift chambers which should enable us to attack the problem of reconstructing high multiplicity events. The philosophy which we arrived at, after some study, is as follows.

The lever arm, which comprises four drift chambers, is in a field free region. At 150 GeV/c about 60% of all charged secondaries, be it a peripheral or high  $p_t$  type of event, go into the lever arm. The ambiguities in the pattern recognition of these tracks (as shown below) is essentially zero. They have been well spread out by the magnetic field and the track points lie on a straight line. All pattern recognition is done in space. This means, for example, that in a 10-charged-track event 6 have been already identified.

Then, by knowing the origin (which is well determined by the beam direction and the high- $p_t$  track or a single wide angle track), the points in the MWPC system inside the magnet can be associated to these tracks by back-tracking. Ambiguities of association there will be, as we show below, but this does not matter as the momenta and angles are determined by the lever arm and the origin alone.

We are then left with the problem of recognising the 40% (or 4) charged tracks of momenta  $< 10$  GeV/c in the MWPC vertex system in the magnetic field. Now we know from the OMEGA spectrometer, where pattern recognition is done in projection, that 4 tracks of  $< 10$  GeV/c present no problems. We believe pattern recognition in space, which is much emptier than its projection, will allow us to go to higher multiplicities than 4 (in principle one might guess at  $4^2 = 16$  tracks as a possibility, due to another dimension).

Our choice of vertex detector layout was arrived at by our wish to obtain, as a minimum, the possibility of measuring a good fraction of the events containing tracks over the entire region of phase space (momentum and angle) in the c.m. For example, among the 4 remaining tracks to be

identified, we found that only 5% of high- $p_t$  type generated events have a track with momentum  $< 1 \text{ GeV}/c$  and  $< 3$  points (hence non identifiable) in the geometry of fig. 1a. In the case of peripheral-type generated events this figure becomes 72%, and is worse (see Table 6) if we do not add the chambers on each side of the target.

Below we describe :

- 1) The acceptance and track recognition properties of the vertex-detector shown in fig. 1a.
- 2) The track recognition capabilities of the complete set-up for peripheral and high- $p_t$  type of events.
- 3) Characteristics of the lost particles.

As a result of this work we reduced the number of MWPC's in the vertex detector to those indicated by an arrow in fig. 1a. The total complement of MWPC's of fig. 1a will be constructed but will only be equipped with read-out electronics depending on the experience gained during initial running.

#### I. Low momentum tracks in the vertex detector

##### i) Simulation of low momenta.

We have studied acceptances and track recognition for simulated tracks with momenta less than  $1 \text{ GeV}/c$ . The chamber layout and the two target positions that are considered are shown in figs. 1b, c. The chamber dimensions and positions are summarised in table 1. For the simulation, uniform distributions in the track parameters (momentum, azimuth, dip as defined in fig. 2, and vertex position) have been used and the ranges of these parameters are given in table 2.

The particles are tracked in the two-coil magnetic field of the Omega spectrometer - but with the spatial dimensions scaled by a factor 2/3. Two target positions are considered: "back", positioned symmetrically

with respect to the side chambers (fig. 1b) and "forward", with the front end of the target level with the front edge of the side chambers (fig. 1c). For the forward target position, the side chambers are decreased in width to give the same acceptance in the backward direction as for the target back configuration.

In the tracking, each chamber gives a space point with a random error of  $\pm 0.7$  mm. Tracks are followed from the side chambers into the forward chambers and vice versa, but with a cut-off on a turning angle of more than  $180^\circ$ .

ii) Acceptance for single tracks.

The minimum number of space points to define a track in a magnetic field is three. In table 3 we give the percentage of tracks with momentum greater than 100 MeV/c that fulfil this requirement in the forward and side cones for the two target positions. Extra points obtained by a track passing through the same plane twice are not included. In the following we give figures for the forward target position, which gave the best results.

The dip-azimuth and momentum-azimuth correlations of the tracks in the side cone which are lost (i.e. have less than 3 points) are shown in figs. 2 and 3. The dip-azimuth and momentum-dip correlation for the forward cone are shown in figs. 4 and 5a. We see that except for large dip angles the  $\phi$  vs  $\lambda$  plot is fairly uniformly populated. The momentum projection (fig. 5b) shows no particular biases or loss, except that expected at lower momenta due to the small curvature.

As can be seen from table 3, the target position does not greatly affect the overall acceptance for tracks less than 1 GeV/c. However, the effect is more noticeable for the higher momenta ( $> 1$  GeV/c) in the forward cone, where tracks of larger dip are accepted with the target forward than with the target back. Acceptances are given in table 3 for the forward cone in a momentum range of 1-10 GeV/c. The momentum-angle correlations for the tracks from this sample with less than 3 space points are shown in figs. 6 and 7.

iii) Track recognition.

For tracks with three points or more we have the problem of associating the points to tracks i.e. track recognition. This has been studied in detail for the side cone and the conclusions checked in the forward cone. The conclusions may be summarised as follows:

- 1) For 5 or more space points (in the same geometry) good linear constraints are obtained from the principal component method (see ref. 1). Thus tracks may be identified using certain linear combination of the measurements.
- 2) For 3 or 4-point tracks the number of measurements results in insufficient redundancy for the solution to become unique, so that track recognition by linear tests is very inefficient (many ambiguities). This also applies to tracks having 5 or 6 points, but with only 2 or 3 points in a given set of chambers i.e. the tracks linking the two geometries. For these tracks it is necessary to use a non-linear constraint for track recognition. We have used a quintic spline fit for each track (see ref. 2). This fit incorporates the non uniformity of the magnetic field and is therefore more time-consuming than the linear constraints - but it includes a better momentum estimate at the same time.
- 3) In order to test the track recognition procedures described above, two prong pseudo events were simulated by grouping tracks in the side cone. No kinematics or physics was included. Track recognition was done by the brute force approach-looking at all possible combinations of the track points in an "event", and using linear or spline constraints to identify track combination. The program was set up to find all true tracks, and in table 4 we give typical "contamination" figures for two-track events i.e. the percentage of extra tracks found. Similar figures were obtained for the low momentum tracks in the forward cone.
- 4) Typical times for track identification using linear and spline methods are given in table 5, both for single tracks and for the two-track pseudo-events where all combinations are tested for tracks.

References

1. H. Wind, Function Parametrisation, CERN 72-22.
2. H. Wind, Nuclear Inst. and Methods (submitted) NP-DHG 73/5.
2. Results on simulated peripheral and high  $p_t$  type of events.
  - i) Generation :- We have generated two kinds of events.
    - a) 100 "peripheral" Van-Hove longitudinal phase space type at 150 GeV/c,  $\pi^- p \rightarrow p 3\pi^+ 4\pi^- \pi^0$ .
    - b) 100 high  $p_t$  (so called "explosive") events in which two mass  $M_5^0$  of 5 GeV each, produced isotropically along with one  $\pi^0$ ,  $\pi^- p \rightarrow M_5^0 M_5^0 \pi^0$ , are allowed to decay isotropically to 4 charged particles each, viz.  $\pi^- p \rightarrow p 3\pi^+ 4\pi^- \pi^0$ .

ii) Pattern recognition.

Each track point was randomised with an error of  $\pm 0.7$  mm as before, and we then went through a large number of exercises using existing pattern recognition programs. These are the "principal component" method and spline fit as mentioned above. We give here some results which give us a certain confidence that the pattern recognition problems associated with the higher multiplicity events occurring can be overcome in the proposed layout.

Thus fig. 8 shows the distribution of what is essentially a measure of the "mean residual" for the possible track combinations, using the linear test on the 5 points occurring in the chambers 1, 3, 5, 7 and 9 of fig. 1a for each "explosive" event. The full line histogram shows the distribution for the true tracks. In order to retain all true tracks we see we have also 16% extra spurious tracks. If we then take these candidates and repeat the spline fit on them the contamination falls to 12% (see fig. 9). This is not a very happy result. Fig. 10 and 11 display similar results for the peripheral events where track separation in space is smaller. Here a contamination factor of 3.88 falls to 2.77 by using the spline fit. The results clearly demonstrate the impossibility of pattern recognition of tracks with this spatial separation and point error over such a distance

from the target. Figs. 12 and 13 which repeat the exercise on chambers 6 to 10, where the tracks are best separated in the vertex magnet, show a net amelioration for the "explosion" events but the situation for peripheral events (fig. 14 and 15) is still bad - 26% background tracks.

However, when we move further downstream from the target and consider the 3 lever arm chambers 11, 12 and 13 the track background has completely disappeared (fig. 16). Hence our insistence on first performing pattern recognition on the tracks in the lever arm chambers.

We then looked at all the tracks  $< 10 \text{ GeV}/c$  having  $\geq 5$  points and find, after removing all points from the tracks  $> 10 \text{ GeV}/c$  (assumed found in the lever arm), that the background tracks were reduced to 1% for explosive events (fig. 17 and 18) and 2% for peripheral events which we consider acceptable. (figs. 19 and 20).

For the tracks with less than 5 points which then remain and are mainly  $< 1 \text{ GeV}/c$  we used the spline fit and found no contamination for these tracks. This is reasonable since there are less of them and they are well separated in space.

Figs. 21 - 25 show the spread in  $\Delta p/p$  obtained from the spline fit along with the correlation lines calculated using the formula of Gluckstern<sup>(1)</sup>, with an R.M.S. error of  $\pm 0.4 \text{ mms}$ .

The results of this section are summarised briefly in table VI along with the timings (Table VI.3) which indicate about 0.5 sec. 6600 CP time/event of 8 prongs. Note that the complete calculation is necessary only for those events in which a high  $p_t$  track occurs.

### 3. Characteristics of lost particles.

As we see from table 6 (1) there are 72 tracks from peripheral events with  $P < 1 \text{ GeV}/c$  lost from the original 249. The  $P, \phi$  correlation of these tracks is shown in figs. 26 and 27 and no obvious bias is seen. On the contrary figs. 28 and 29 showing the  $\lambda, \phi$  correlation, show that tracks with large dip are preferentially lost, as expected for this geometry. If, as could be the case, there are few tracks of this peripheral nature  $< 1 \text{ GeV}/c$  in the high  $p_t$  events then we have a good

chance of obtaining a sample where all tracks are seen. In the regions above and below the target (large dip) we will place scintillation counters to know that a track passed in this region.

For the tracks  $> 1 \text{ GeV/c}$  and  $< 10 \text{ GeV/c}$  the  $P, \lambda$  of the actual tracks for the peripheral and explosion events is compared to the  $P, \lambda$  distribution for the lost tracks in the uniform simulation in figs. 30 to 32. No track lies in the lost region.

- 1) R.L. Gluckstern Nucl. Instr. and Meth. 24 (1963), 381.

TABLE 1

| REGION  | TARGET CENTRE (x) | CHAMBER DIMENSIONS |           | CHAMBER POSITION (cm)       |
|---------|-------------------|--------------------|-----------|-----------------------------|
|         |                   | WIDTH (y or x)     | DEPTH (z) |                             |
| Side    | -80.0             | 60.0               | 80.0      | y = + 6,+12,+18,+24,+36,+48 |
| Forward | -80.0             | 110.0              | 80.0      | x = - 45,-39,-33,-27,-15,-3 |
| Side    | -65.0             | 45.0               | 80.0      | y = + 6,+12,+18,+24,+36,+48 |
| Forward | -65.0             | 110.0              | 80.0      | x = - 45,-39,-33,-27,-15,-3 |

TABLE 2

| REGION       | P (GeV/c) | $\phi$        | $\lambda$    | TARGET DIMENSIONS   |
|--------------|-----------|---------------|--------------|---------------------|
| Forward Cone | 0 to 1    | -60° to +60°  | -60° to +60° | 30 cm x 2 cm x 2 cm |
| Side Cone    | 0 to 1    | +30° to +150° | -60° to +60° | 30 cm x 2 cm x 2 cm |
| Forward Cone | 1 to 10   | -60° to +60°  | -60° to +60° | 30 cm x 2 cm x 2 cm |

TABLE 3

| REGION               | MOMENTUM RANGE   | TARGET CENTRE | ACCEPTANCE (%) |
|----------------------|------------------|---------------|----------------|
| Forward              | { 0.1 to 1 GeV/c | -80           | 81             |
|                      |                  | -65           | 87             |
| Side                 | { 0.1 to 1 GeV/c | -80           | 85             |
|                      |                  | -65           | 83             |
| Forward              | { 1 to 10 GeV/c  | -80           | 79             |
|                      |                  | -65           | 86             |
| Forward<br>+<br>Side | { 0 to 1 GeV/c   | -80           | 81             |
|                      |                  | -65           | 80             |

TABLE 4

| No. of Tracks/"Event" | No. of Points per Track | No. of Extra Tracks (%) | Method Used |
|-----------------------|-------------------------|-------------------------|-------------|
| 2                     | 3                       | ~ 12                    | Spline      |
| 2                     | 4                       | ~ 1                     | Spline      |
| 2                     | 5                       | ~ 3                     | Linear      |
| 2                     | 6                       | ~ 3                     | Linear      |

TABLE 5

Timings (in msec of CDC 7600)

| No. of Points/Track | 3   | 4    | 5   | 6   |                    |
|---------------------|-----|------|-----|-----|--------------------|
| Linear              | .3  | .4   | .5  | .7  | { 1 Track/"Event"  |
| Spline              | 2.4 | 2.8  | 3.5 | 4.3 |                    |
| Linear              | .7  | 1.2  | 3.3 | 7.0 | { 2 Tracks/"Event" |
| Spline              | 5.0 | 13.5 | -   | -   |                    |

TABLE 6

SIMULATION RESULTS                    150 GeV/c                    EXPLOSION + PERIPHERAL

| All P<br>Total No. Tracks | 0 to 1 GeV/c<br>Total < 3 Pts. | 1 < P < 10<br>Total < 3 Pts. | > 10 GeV/c<br>Total < 3 pts. |
|---------------------------|--------------------------------|------------------------------|------------------------------|
| Explosion : 800           | 36      4                      | 360      0                   | 404      0                   |
| Peripheral : 800          | 249      72                    | 198      0                   | 353      0                   |

2. Track Recognition Results

a) 0 to 1 GeV/c. Peripheral (Worst Case)

Spline : No contamination for 3, 4, 5 and 6 point tracks  
 Linear : ~ 2% Contamination for 5 or 6 point tracks

b) 0 to 100 GeV/c.

| No. of points<br>in forward chambers | 0   | 1  | 2  | 3  | 4  | $\geq 5$<br>p > 10 | p < 10 GeV/c |
|--------------------------------------|-----|----|----|----|----|--------------------|--------------|
| Explosion :                          | 10  | 0  | 2  | 1  | 2  | 404                | 381          |
| Peripheral :                         | 122 | 16 | 12 | 13 | 21 | 353                | 263          |

Recognition : Linear tests;  $\geq 5$  PTS/TRK ; p < 10 GeV/c.

| No. of Tracks | Efficiency | Contamination | Time/Track (7600) |                     |
|---------------|------------|---------------|-------------------|---------------------|
|               |            |               | Lin +             | Spline              |
| Explosion :   | 381        | 99.5%         | ~ 2%              | ~ 1%      ~ 3 msecs |
| Peripheral :  | 263        | 99.0%         | ~ 6%              | ~ 2%      ~ 3 msecs |

3. Time/Event (8-Prongs) (7600 Time)

| Fraction > 10 GeV/c | Fraction<br>0 to 10 GeV/c | $\geq 5$ pts.      | Fraction<br>0 to 10 GeV/c | < 5 pts. | Total                 |
|---------------------|---------------------------|--------------------|---------------------------|----------|-----------------------|
| Explosion :         | .50<br>(x 5 msecs)        | .48<br>(x 3 msecs) | .02<br>(x 5 msecs)        | ~30msecs | Point<br>-find<br>ing |
| Peripheral :        | .44<br>(x 5 msecs)        | .33<br>(x 3 msecs) | .23<br>(x 20 msecs)       | ~60msecs | Over<br>-head         |



Fig. 1b : TARGET BACK

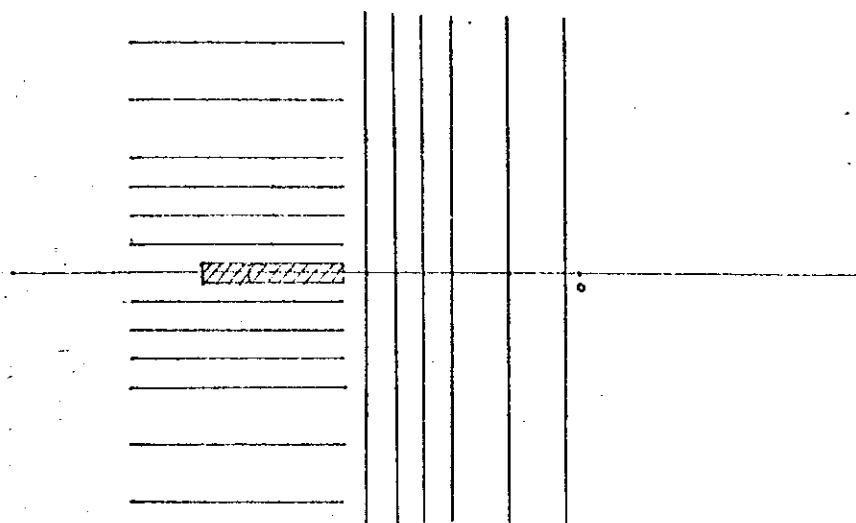


Fig. 1c : TARGET FORWARD.

Scale : 1 mm = 1 cm.

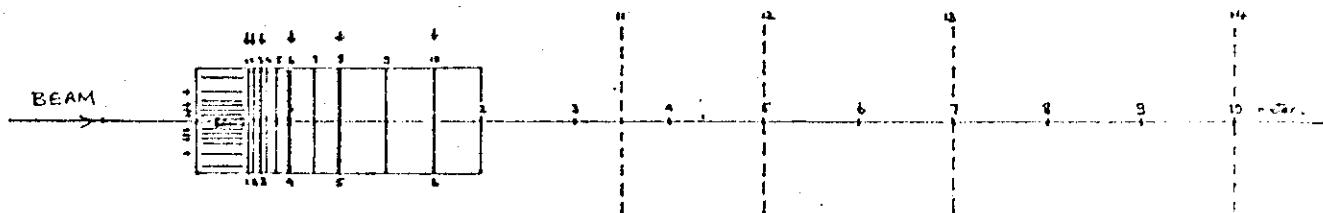


FIGURE 1a (PLAN VIEW)



&lt; 3 PTS / TRK.

## FORWARD + SIDE TRACKING.

17

|                | 0            | 1           | 2           | 3           | 4           | 5           | 6              |
|----------------|--------------|-------------|-------------|-------------|-------------|-------------|----------------|
| 0.             | 01234567890  | 12345678901 | 23456789012 | 34567890123 | 45678901234 | 56789012345 | 67890123456    |
| FORWARD + SIDE |              |             |             |             |             |             |                |
| TRACKING.      |              |             |             |             |             |             |                |
|                |              |             |             |             |             |             |                |
| 0° - X         | 2            | + 2         | +           | +           | +           | 2           | ++             |
| X              | 3 2          | + +         | +           | +           | +           | 22          | ++             |
| X              | + + +        | +           | +           | +           | +           | 3 2         |                |
| X              | + + + +      | +           | +           | 2           | +           |             |                |
| X              | 2 +          | ++          | +           | +           | 2           | 2 2         | 23             |
| X              | + +          | +           | +           | +           | +           | +           | 3 +            |
| X              | + + + 2      | +           | +           | +           | +           |             | 22             |
| X              | 32 + 2       | ++          | +           | +           | +           | +           | ++ 2           |
| X              | 2 + 2 + 2    | +           | +           | +           | +           | +           | 3 +            |
| X              | 2 +          | +           | +           | +           | +           |             | 2              |
| X              | + 3 + 2      | +           | +           | +           | +           | +           | 2 2            |
| X              | 32 +         | ++          | +           | +           | +           | 2           | ++             |
| X              | + 3 + 3 +    | +           | 2           | +           | +           | +           | 3 + 3          |
| X              | 2 2 + 3      | +           | ++          | +           | +           | +           | 22             |
| X              | + 3 22 +     | +           | +           | +           | +           | +           | ++ 2 + 2       |
| X              | + 42         | +           | +           | +           | +           | +           | ++ 2 ++        |
| X              | 3 +          | ++ 2        | ++          | +           | +           | +           | ++ 2 + 2 +     |
| X              | + + 2 + 2    | +           | +           | +           | +           | +           | 2 22           |
| X              | 22 +         | +           | ++          | +           | +           | +           | +              |
| X              | + + 2 +      | +           | +           | +           | +           | +           | ++ 2 + 2 2 + 2 |
| X              | + + 2 + 4    | +           | +           | +           | +           | +           |                |
| X              | 3222         | +           | +           | +           | +           | +           | ++ + + +       |
| X              | 22 +         | ++ +        | +           | +           | +           | +           | 322 3          |
| X              | 23           | ++ +        | +           | +           | +           | +           | ++ + + + 4     |
| X              | + + 3        | +           | +           | +           | +           | +           | ++ + + + 23    |
| X              | 324          | 3 +         | ++          | +           | 2           | +           | ++ 22 222      |
| X              | 3 2 + 3      | ++          | +           | +           | +           | +           | ++ 224 +       |
| X              | + 2 + 2      | +           | +           | +           | +           | +           | 2 + 33         |
| X              | ++ + 2 + 2 + | +           | +           | +           | +           | +           | 4 + 5 + 2      |
| X              | 2 + 2 +      | +           | +           | +           | +           | +           | 3              |
| X              | 3 + 25       | ++          | 2           | +           | +           | +           | ++ 3 +         |
| X              | + 2 + 2      | +           | +           | ++          | +           | +           | 32 23          |
| X              | + + + + +    | +           | +           | 2           | +           | +           | 2 + + + 4 + 23 |
| X              | + + 2 2      | +           | +           | +           | +           | +           |                |
| X              | 24 + 3       | +           | 2 +         | +           | +           | +           | 3 + + 32       |
| X              | 3 + 2        | +           | ++          | +           | +           | +           | ++ + + 32      |
| X              | + + + 2 +    | +           | +           | +           | +           | +           | ++ 2 + +       |
| X              | 2 + 2 + 2    | +           | +           | +           | +           | +           | 2 +            |
| -20° - X       | + + 2 2 2 +  | 2           | +           | +           | +           | +           | 2 + 2 + 24     |
| X              | + 2 + + + +  | 2           | +           | +           | +           | +           |                |
| X              | + + + + +    | +           | +           | +           | +           | +           | 4 + + 23 + 3   |
| X              | + 22 + 2 + + | +           | +           | +           | +           | +           |                |
| X              | 2233         | 2           | +           | 2           | +           | 2           | 2 2 +          |
| X              | + + + +      | +           | +           | +           | +           | +           | ++ + + 2 4     |
| X              | 2 + 2 + + 23 | +           | +           | +           | +           | +           | ++ + + 2 +     |
| X              | + + + +      | +           | +           | +           | +           | +           | ++ + +         |
| X              | 22 + + 2 + + | +           | +           | +           | +           | +           | 2 + +          |
| X              | 2 + +        | +           | +           | +           | +           | +           | 222            |
| -40° - X       | + 2 22 + +   | +           | +           | +           | 2           | 3           | ++ 22 + + 2    |
| X              | + + + +      | 2           | +           | ++          | +           | 2 +         | ++ 2 +         |
| X              | + + 2 +      | +           | +           | +           | +           | +           | 2 + +          |
| X              | 5 +          | +           | +           | ++ +        | +           | +           | 2 + 2          |
| X              | 2 + +        | 2           | +           | +           | +           | +           | 23             |
| X              | + + +        | 2           | +           | +           | +           | +           | ++ +           |
| X              | 2 + +        | +           | +           | 2           | +           | +           | ++ 3           |
| X              | + + 2        | +           | +           | 2           | +           | +           | ++ +           |
| X              | + + + +      | 2           | +           | ++          | +           | +           | ++ +           |
| X              | 33           | ++          | +           | +           | 2           | +           | 2 + 2          |

$T_c = -65 \text{ cm}$

DIP ANGLE  $\lambda$ 

100 Movie

ANGLES  $-60^\circ$   $-40^\circ$   $-20^\circ$  0  $+20^\circ$   $+40^\circ$   $+60^\circ$ 

FIG 4









04

1-DIMENS. HISTOGRAM NR. 4

**IDENT**

DATE 11/02/74

96  
93  
90  
87  
84  
81  
78  
75  
72  
69  
66  
63  
60  
57  
54  
51  
48  
45  
42  
39  
36  
33  
30  
27  
24  
21  
18  
15  
12  
9  
6  
3  
F

**EXPLOSION**

RLL P. LINEAR TEST

CHAMBERS 1 6 → 10

No. of tracks = 579

No. under peak = 615 (1 : 1.06)

FIG. 12

MANUEL

0 0 1 2 3 4 5 6 7 8 9 0  
0 1 2 3 4 5 6 7 8 9 0 1 2 3 4 5 6 7 8 9 0 1 2 3 4 5 6 7 8 9 0 1 2 3 4 5 6 7 8 9 0  
0 1 2 3 4 5 6 7 8 9 0 1 2 3 4 5 6 7 8 9 0 1 2 3 4 5 6 7 8 9 0 1 2 3 4 5 6 7 8 9 0 1 2 3 4 5 6 7 8 9 0

## CONTENTS

1, D1

1-DIMENS. HISTOGRAM NR. 1

IDENT

DATE 11/02/74

|     |    |
|-----|----|
| 340 | X  |
| 330 | X  |
| 320 | X  |
| 310 | X  |
| 300 | X  |
| 290 | X  |
| 280 | 4X |
| 270 | XX |
| 260 | XX |
| 250 | XX |
| 240 | XX |
| 230 | XX |
| 220 | XX |
| 210 | XX |
| 200 | XX |
| 190 | X  |
| 180 | XX |
| 170 | X  |
| 160 | X  |
| 150 | X  |
| 140 | X  |
| 130 | X  |
| 120 | X  |
| 110 | X  |
| 100 | X  |
| 90  | X  |
| 80  | X  |
| 70  | XX |
| 60  | XX |
| 50  | XX |
| 40  | XX |
| 30  | XX |
| 20  | XX |
| 10  | XX |

PERIPHERAL

ALL P. CHAMBERS : 1,3,5,7,9

## SPLINE CONSTRAINT

AFTER LINEAR TEST.

No. of. Tracks = 470

No. under Peak = 1301 (1:2.44)

· ANNEX

→ D (mm)

Fig 11







D 1

1-DIMENS. HISTOGRAM NR. 1

IDENT

DATE 06/02/74

|    |        |
|----|--------|
| 90 | 3      |
| 87 | X      |
| 84 | X      |
| 81 | X      |
| 78 | X      |
| 75 | XX     |
| 72 | XX     |
| 69 | XX     |
| 66 | XX     |
| 63 | XX     |
| 60 | XX     |
| 57 | XX     |
| 54 | XX     |
| 51 | XX     |
| 48 | 6XX    |
| 45 | XXX    |
| 42 | XXX    |
| 39 | XXX    |
| 36 | XXX    |
| 33 | XXX    |
| 30 | XXX3   |
| 27 | XXXX   |
| 24 | XXXXX  |
| 21 | XXXXX  |
| 18 | XXXXX  |
| 15 | XXXXX  |
| 12 | 6XXXXX |
| 9  | XXXXXX |
| 6  | XXXXXX |
| 3  | XXXXXX |

PERIPHERAL

$0 \leq p \leq 10$  Gev/c.       $\geq 5$  PTS/TRACK.

### SPLINE CONSTRAINT AFTER LINEAR TEST

## 2% BACKGROUND

ANNELS

FIG. 20

CONTENTS

04

1-DIMENS. HISTOGRAM NR. 4

**IDENT**

DATE 05/02/74

|    |      |       |
|----|------|-------|
| 44 |      | 4     |
| 42 | X    |       |
| 40 | X    |       |
| 38 | X    |       |
| 36 |      | XXXX4 |
| 34 | XXX  |       |
| 32 | XXX  |       |
| 30 |      | XXXXX |
| 28 | XXX  |       |
| 26 | XXX  |       |
| 24 | XXX  |       |
| 22 | XXX  |       |
| 20 | XXXX |       |
| 18 | XXXX |       |
| 16 | XXXX |       |
| 14 | XXXX |       |
| 12 | XXXX |       |
| 10 | XXXX |       |
| 8  | XXXX |       |
| 6  | XXX  |       |
| 4  | XXX  |       |
| 2  | XX   |       |

**PERIPHERAL**

$0 \leq p \leq 10$  GeV/c ;  $\geq 5$  pbs/track.

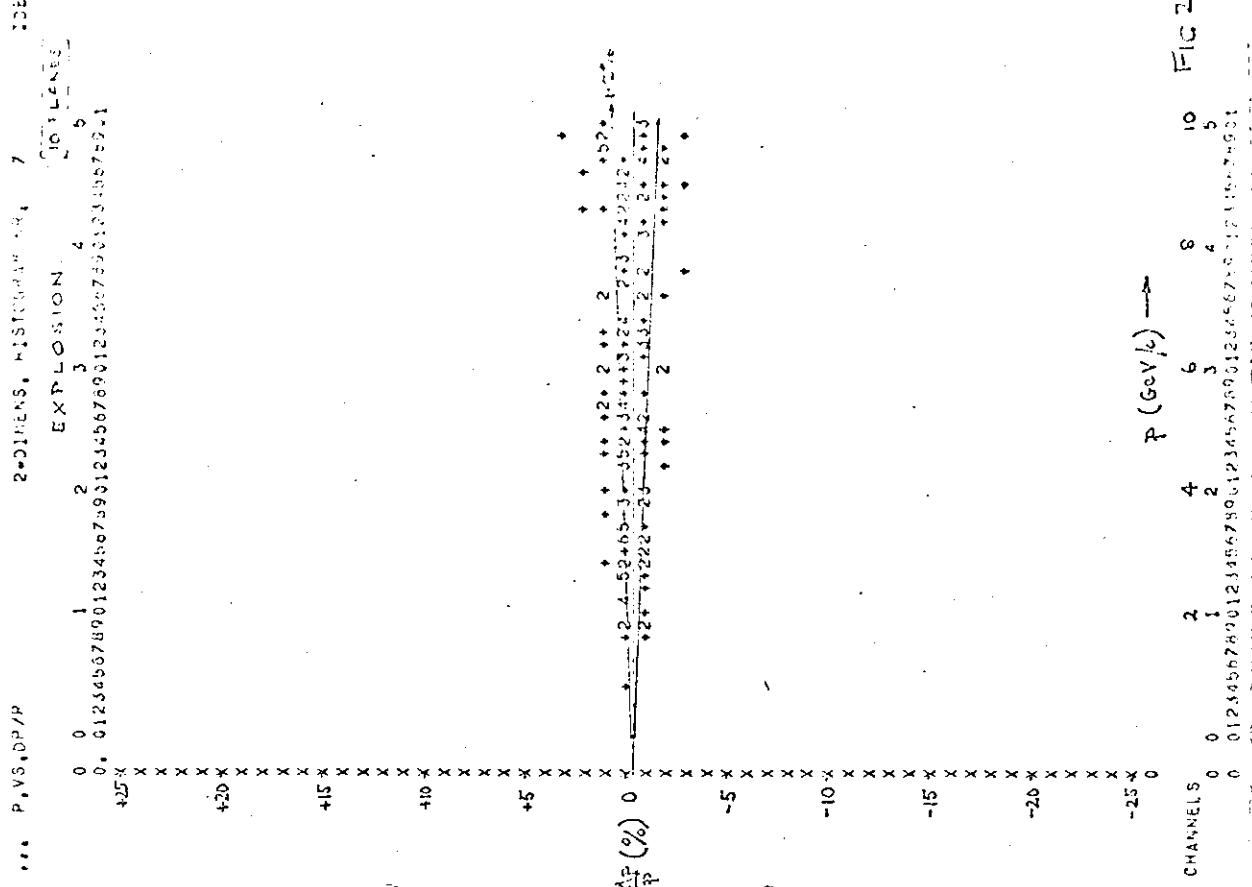
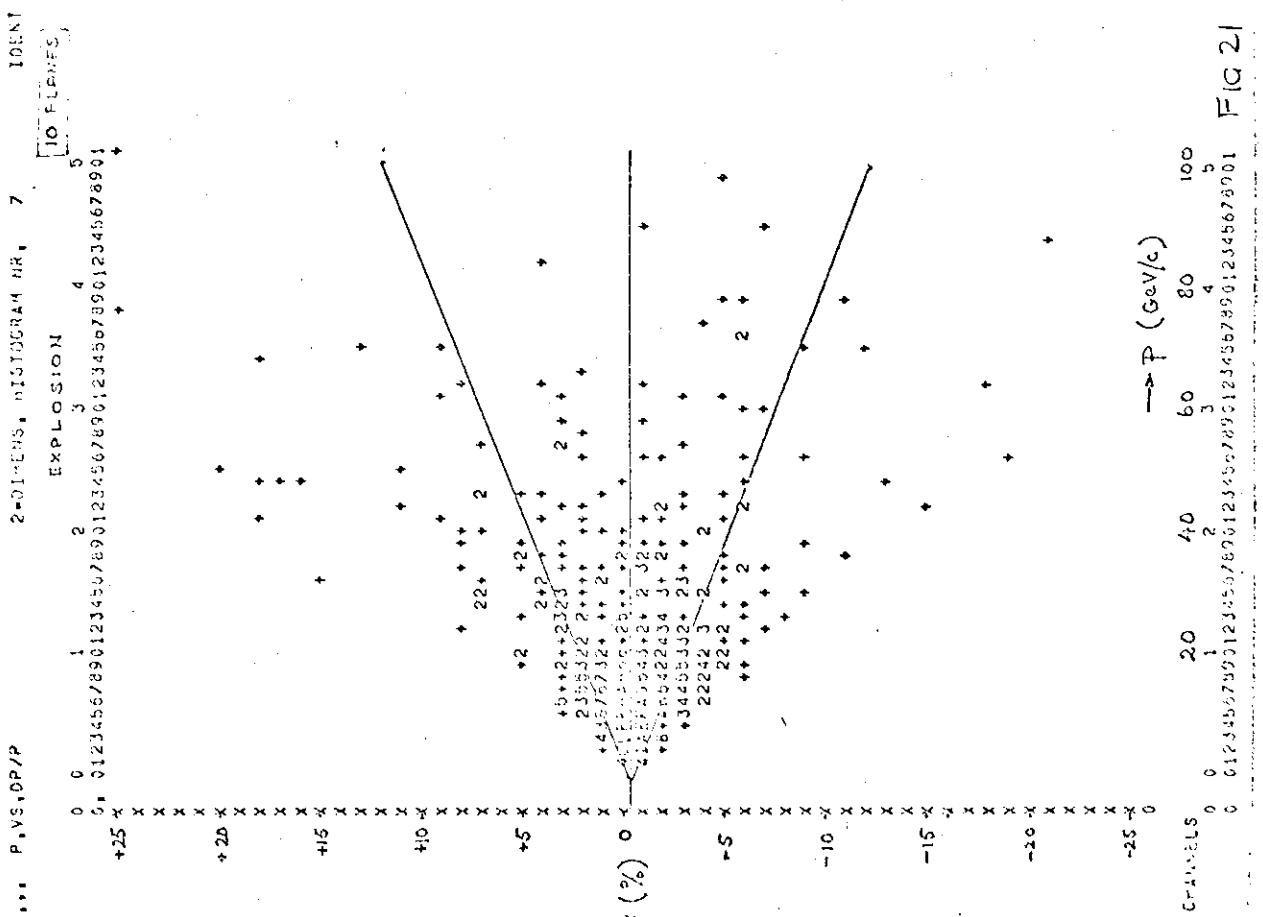
No. of tracks = 263

No. under peak = 280 ( $1:1.06$ )

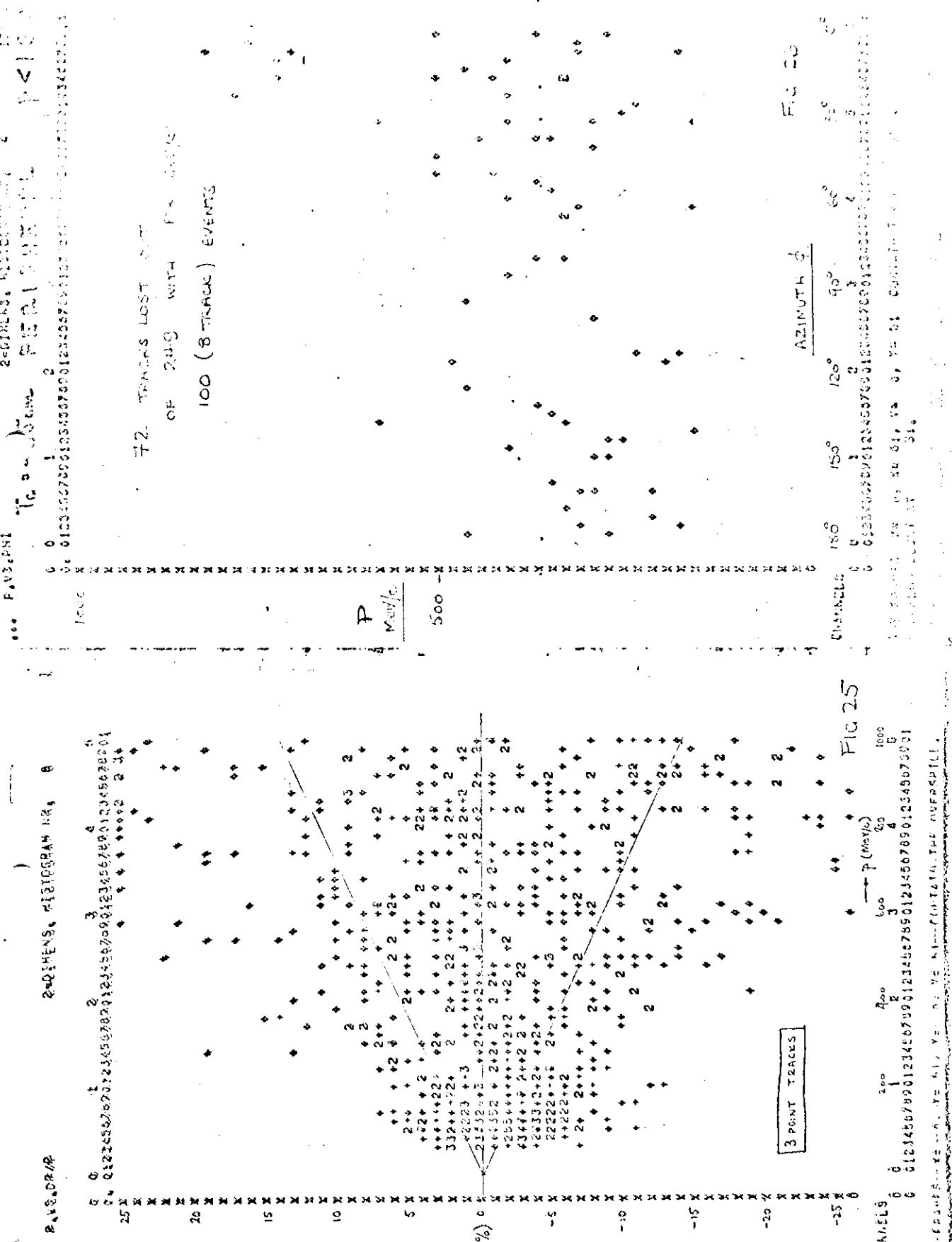
## ANNELS

| S | 0 | 0 | 1  | 2  | 3  | 4  | D (mm) |
|---|---|---|----|----|----|----|--------|
|   | 0 | 0 | 1  | 2  | 3  | 4  |        |
|   | 1 | 2 | 3  | 4  | 5  | 6  | 7      |
|   | 8 | 9 | 10 | 11 | 12 | 13 | 14     |

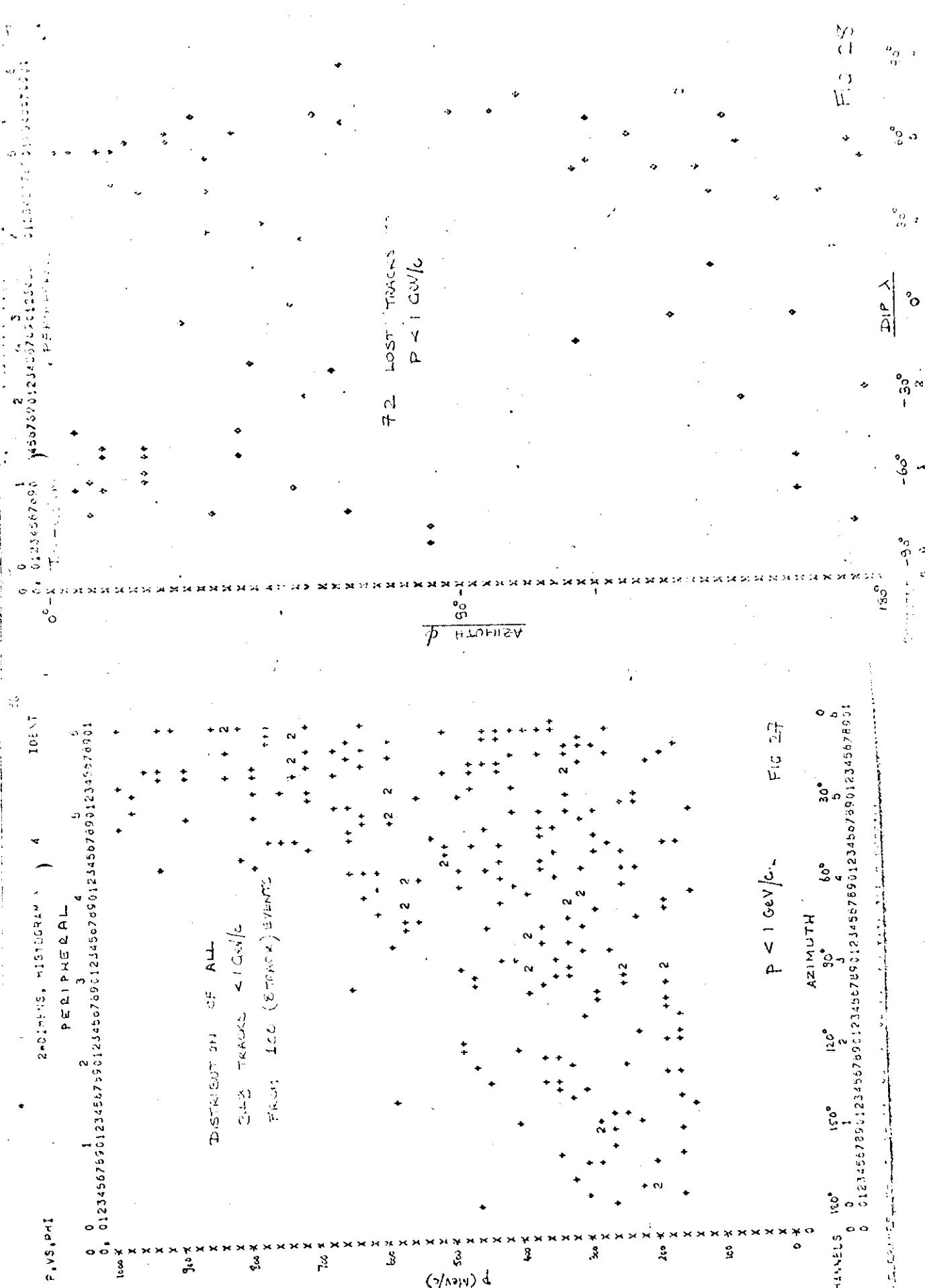
W\_EOCG

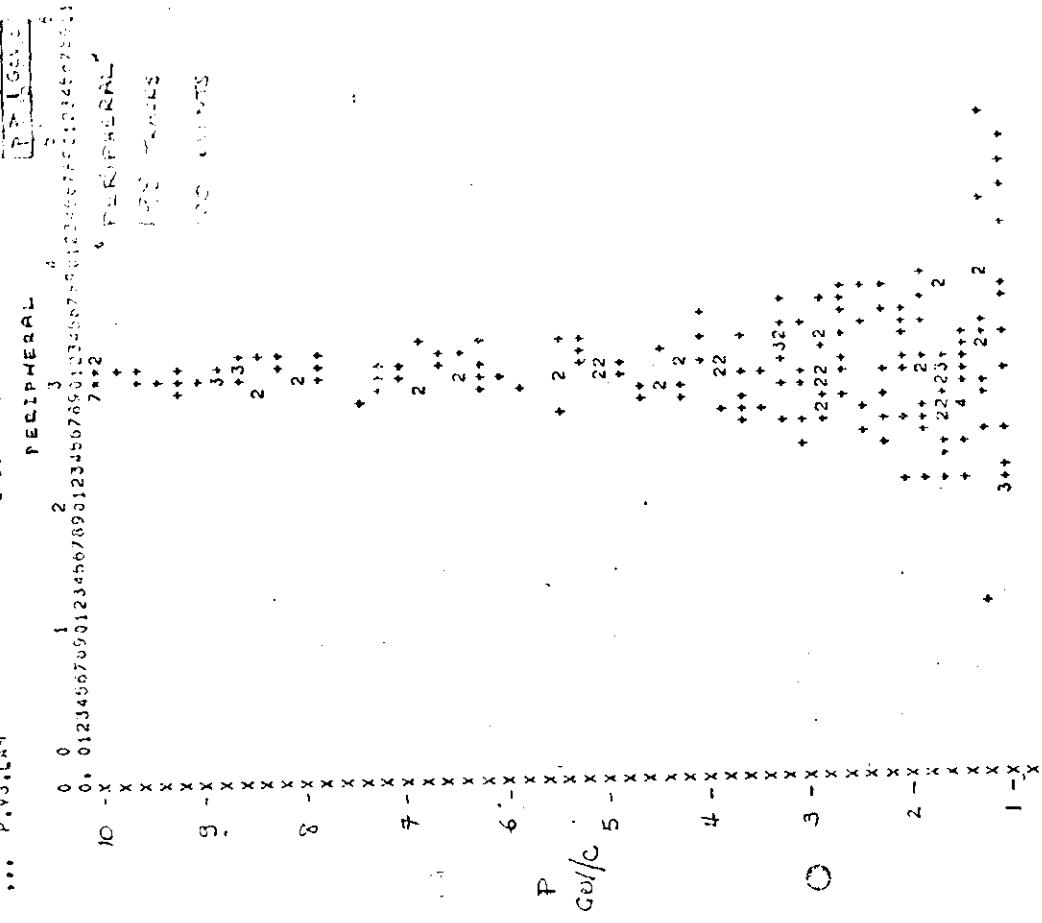
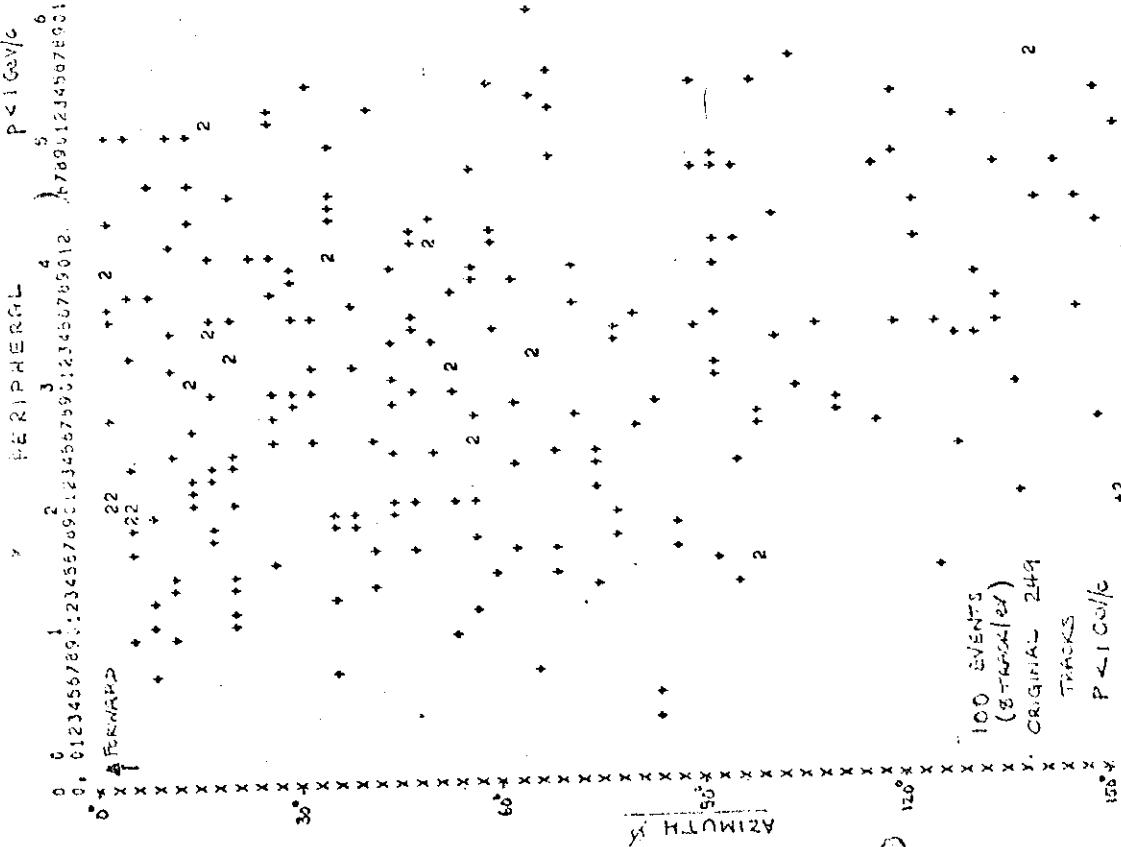






1718 DEPARTMENT OF THE ARMY

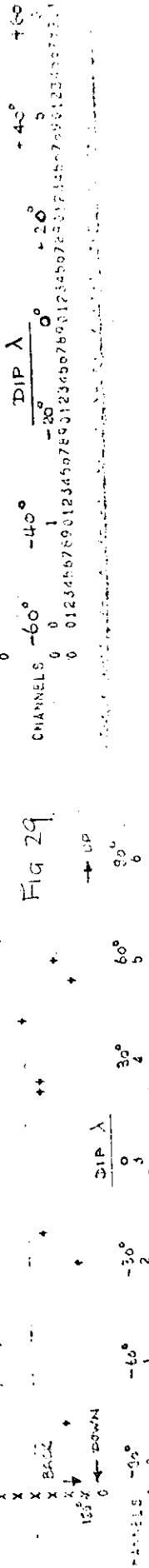


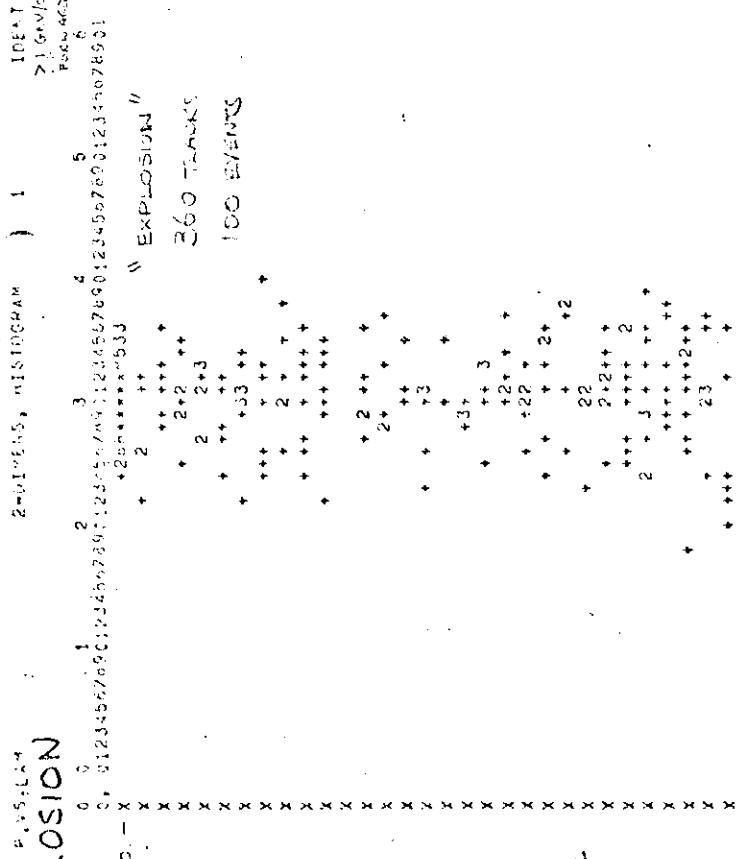


Precipitation

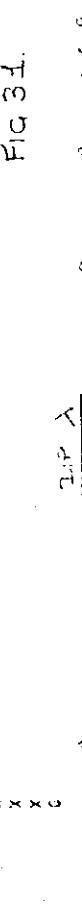
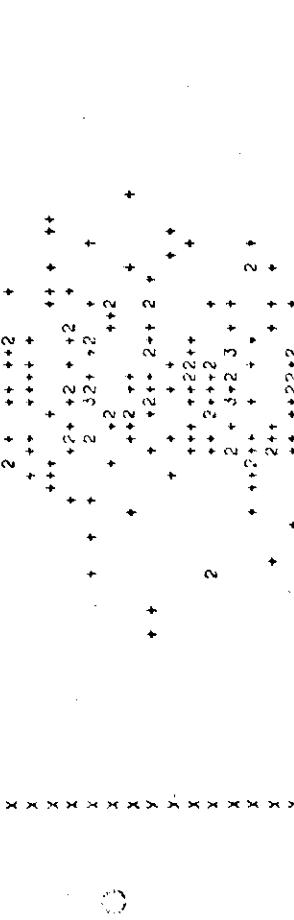
Precipitation

| Symbol | Approximate Range (cm/year) |
|--------|-----------------------------|
| +      | 0 - 20                      |
| ++     | 20 - 40                     |
| +++    | 40 - 60                     |
| ++++   | 60 - 80                     |
| +++++  | 80 - 100                    |
| ++++++ | 100 - 120                   |
| ++++++ | 120 - 140                   |
| ++++++ | 140 - 160                   |
| ++++++ | 160 - 180                   |
| ++++++ | 180 - 200                   |

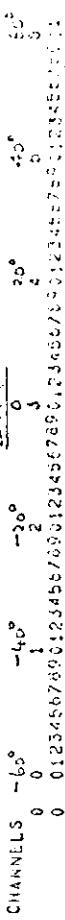




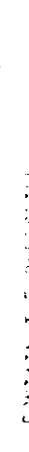
EXPOSITION 2010



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THE ECONOMIC POSITION OF THE STATEMENT



C. J. H. & A. G. 199