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PUBLICATION

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Zhang, P (The University of Manchester; DESY; The Cockcroft Institute of Accelerator Science and Technology) *et al*

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Study of Beam Diagnostics with Trapped Modes in 3rd Harmonic SC Cavities at FLASH

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IPAC'11, San Sebastian, Spain

Sep 08th, 2011



FLASH and ACC39

Free-electron LASer in Hamburg (FLASH)

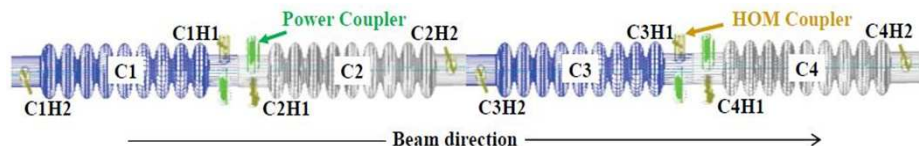
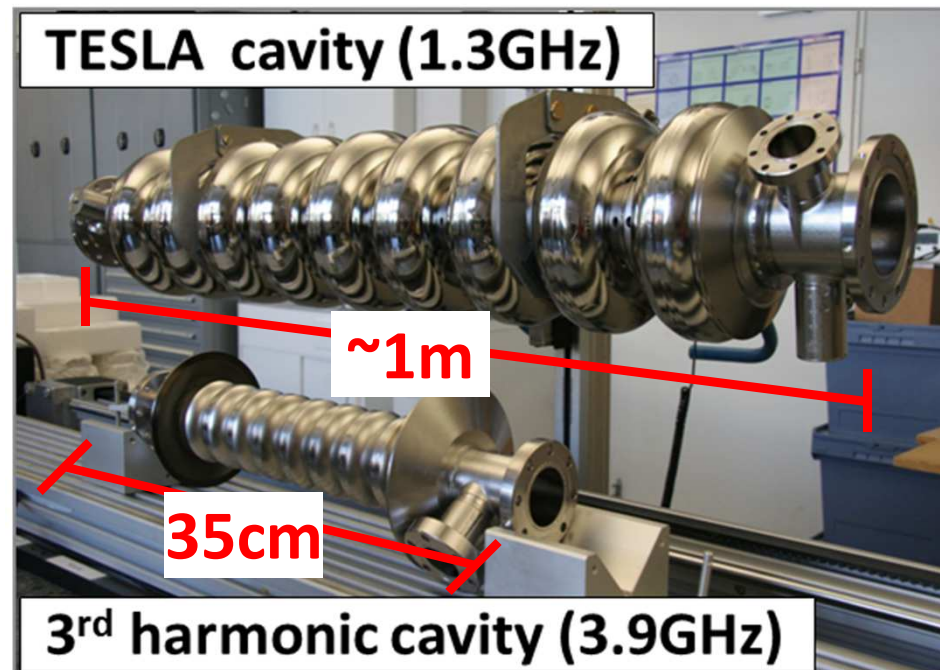
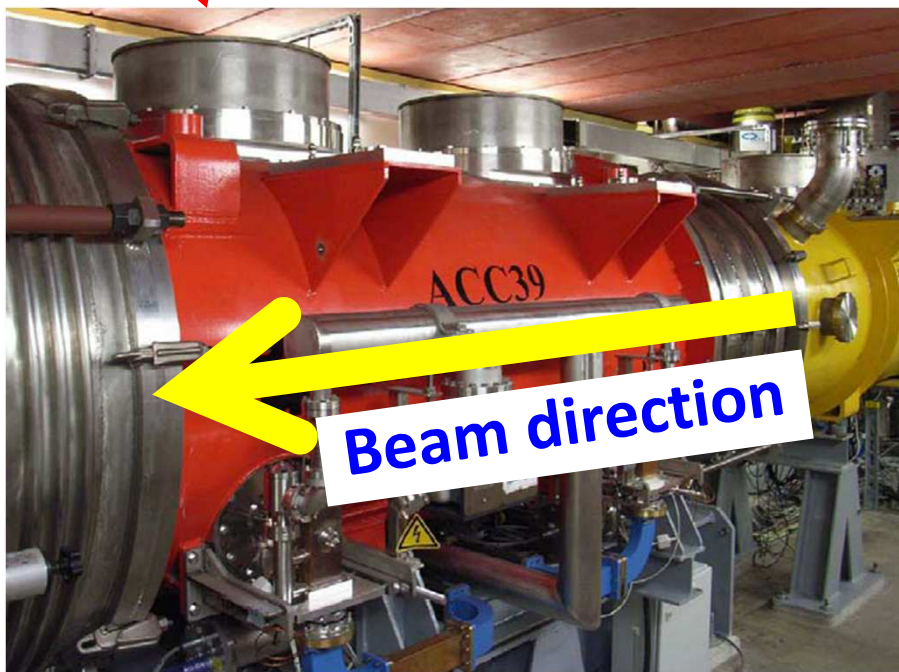
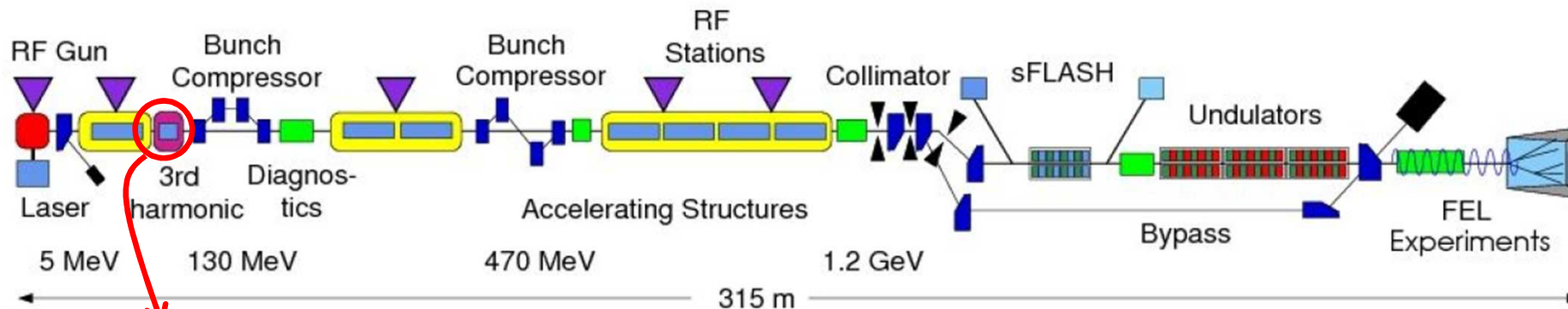


Photo courtesy E. Vogel & DESY

Motivation

- Higher order modes (HOMs) are excited by charge particles in cavities
- **Dipole** modes dominate transverse wakefields

$$W_{\perp} \approx \hat{x} \left(\frac{r'}{a} \right) \sum_n \frac{2k_{1n}}{\omega_{1n} a/c} \sin \frac{\omega_{1n} S}{c} \quad \begin{array}{l} r': \text{beam offset of excitation particle} \\ a: \text{iris radius} \end{array}$$

- **Use HOMs (non-monopole modes) to**
 - align the beam to the electric axis
 - monitor beam position (HOM-BPM)
- **Principle proved in 1.3GHz Tesla cavity**

[1] G. Devanz et al., EPAC2002, WEAGB003

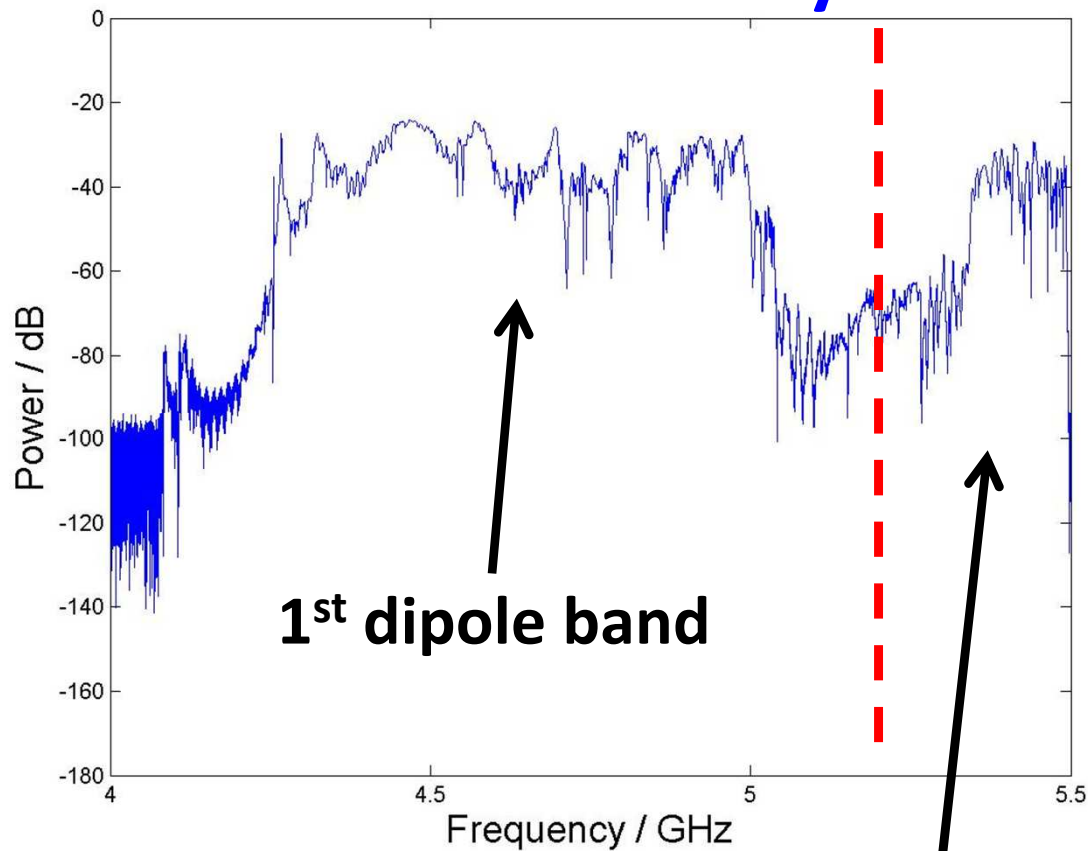
[2] N. Baboi et al., LINAC2004, MOP36

[3] S. Molloy et al., Phys. Rev. ST-AB 9, 112802 (2006)

Challenge

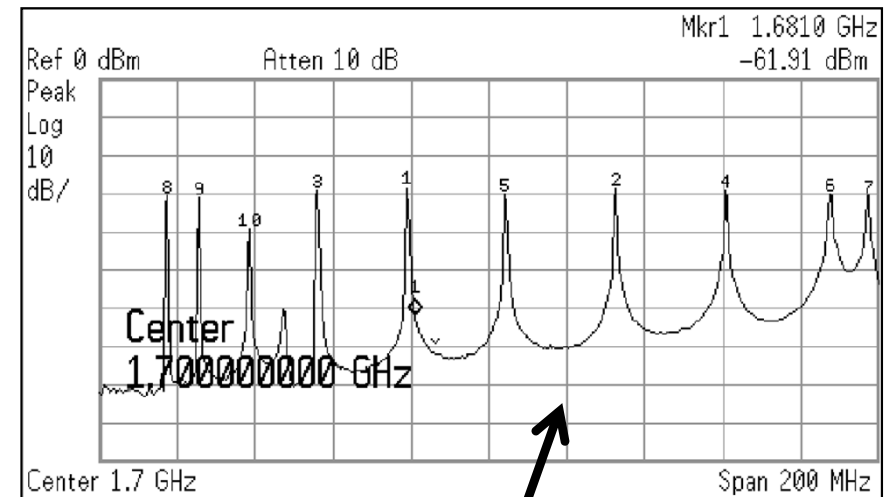
- Most dipole modes propagate through attached beam pipes

3.9 GHz Cavity

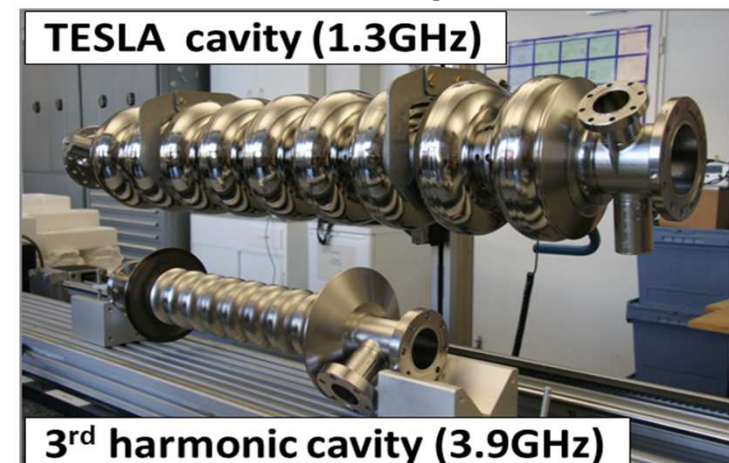


2nd dipole band

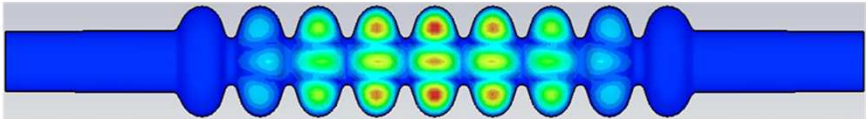
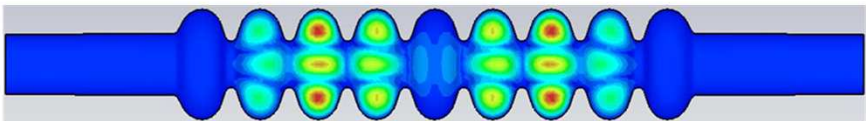
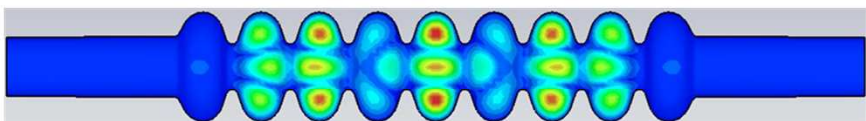
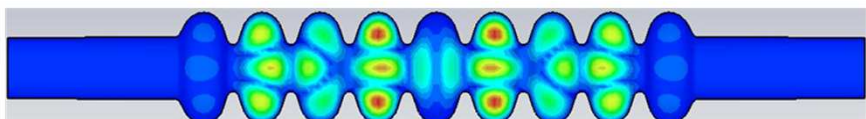
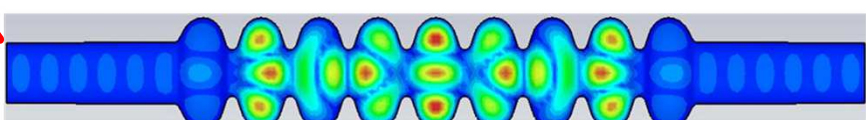
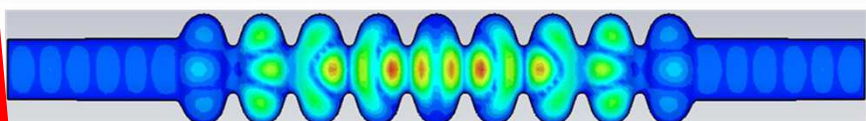
1.3 GHz Cavity



1st dipole band

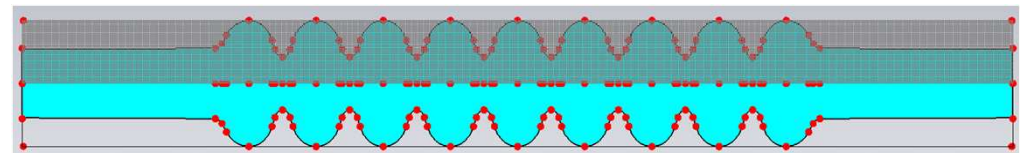


Simulation

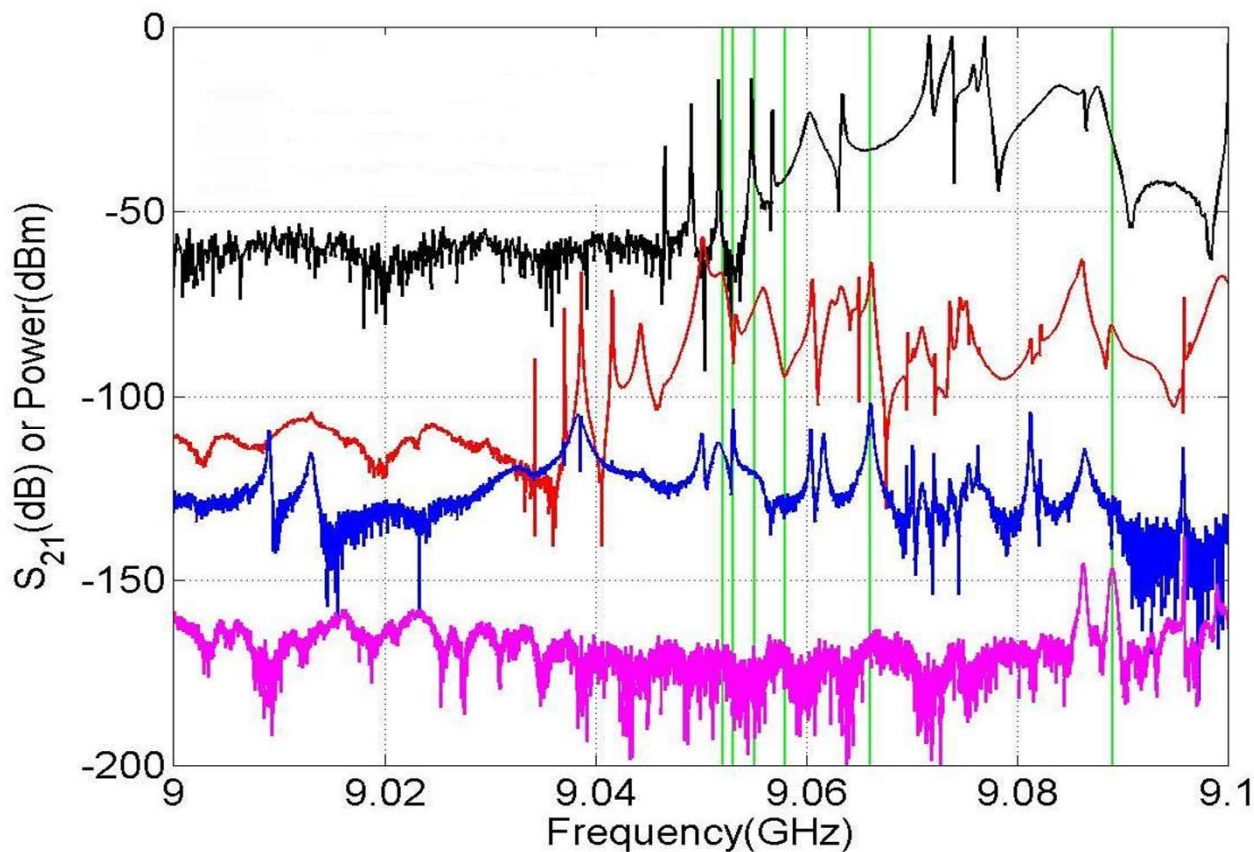
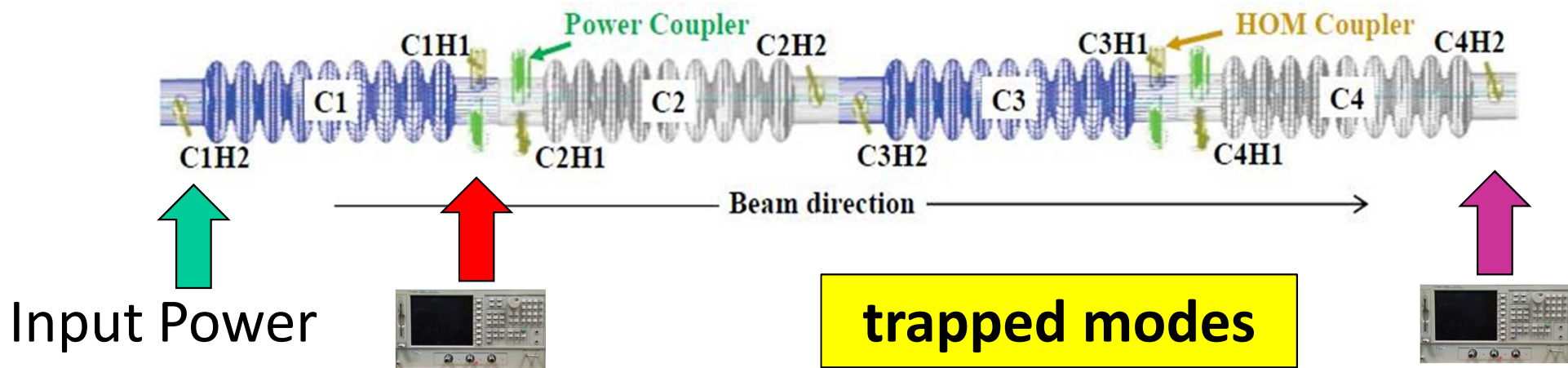
Electric Field	f (GHz)	R/Q (Ω/cm^2)
	9.052	0.00
	9.053	0.05
	9.055	0.06
	9.058	2.17
	9.066	4.12
	9.089	0.58

- Look like trapped

- Also seen in other simulations: I.R.R. Shinton, [WEPC125](#)

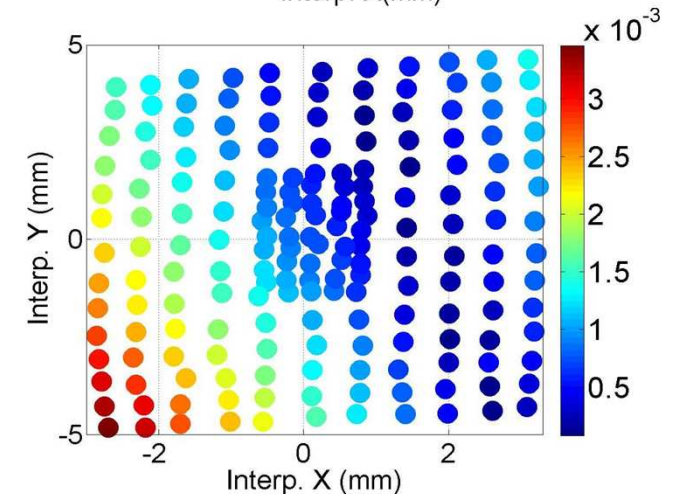
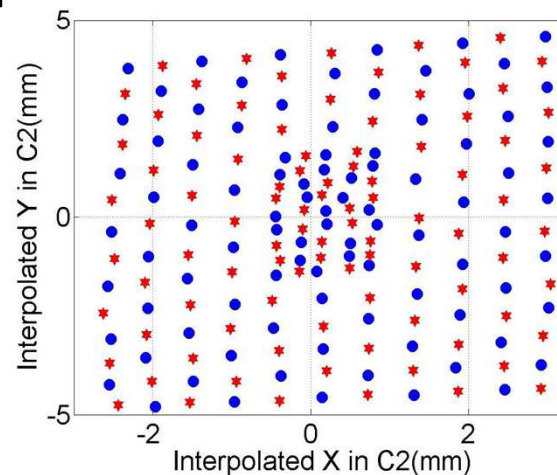
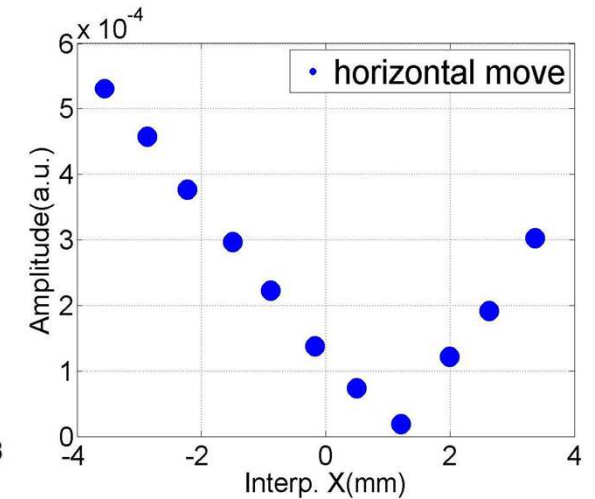
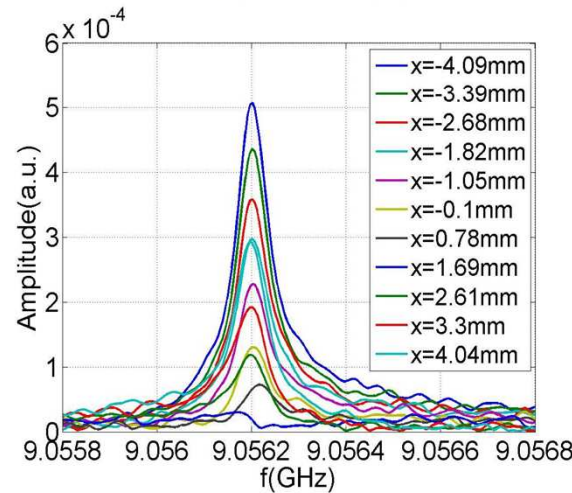
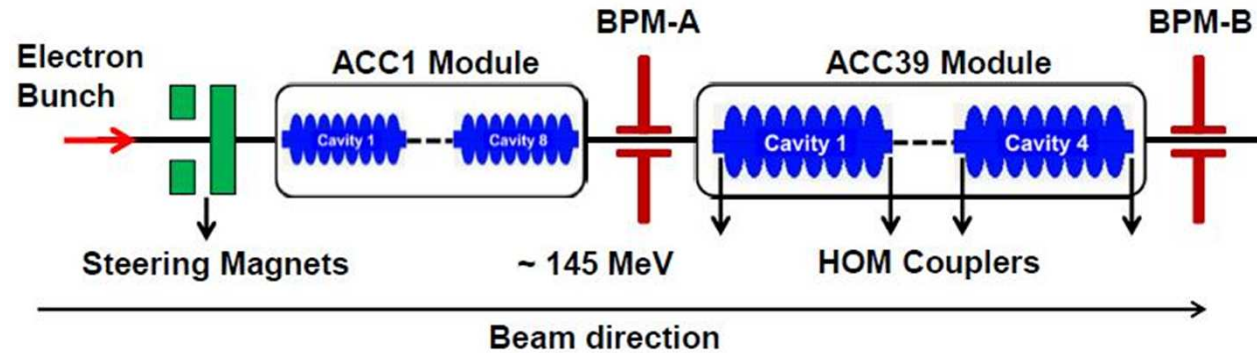


Measurements



- ← Isolated cavity (across C1)
- ← S_{21} (across C1)
- ← Beam-excited (C1H1)
- ← S_{21} (across 4-cavity string)

Dipole-like Behavior



- Move the beam horizontally
- Grid-like move: polarization



trapped dipole modes

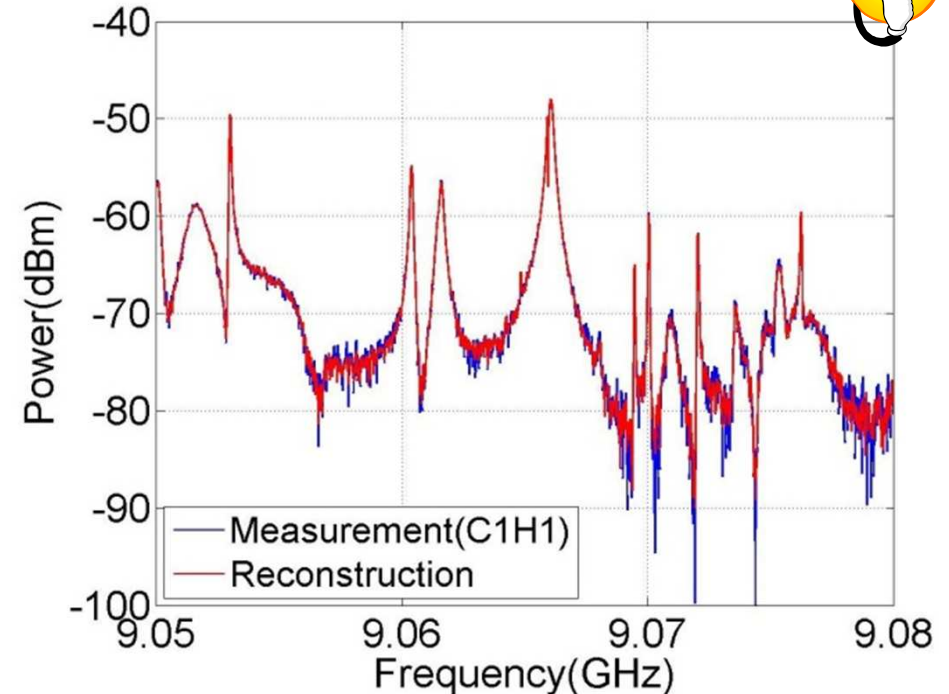
One mode is not enough

Electric Field	f (GHz)	R/Q (Ω/cm^2)
	9.052	0.00
	9.053	0.05
	9.055	0.06
	9.058	2.17
	9.066	4.12
	9.089	0.58

too small



Use more modes



1.3 GHz TESLA cavity

Dipole passband	Mode #	f (GHz)	R/Q (Ω/cm^2)
Band 1 (TE-like)	6	1.7129	5.5366
	7	1.7391	7.7833

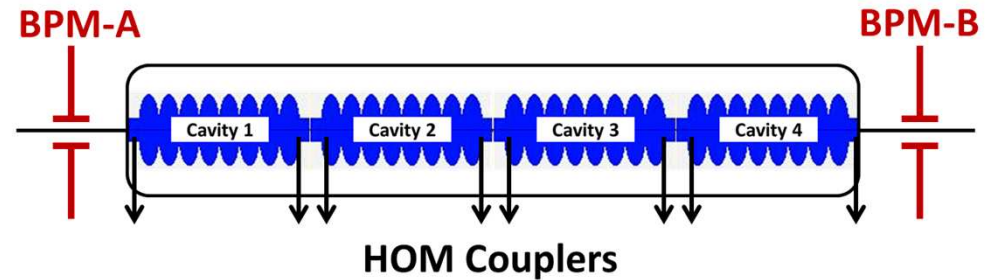
Direct Linear Regression (DLR)

$$A = \begin{pmatrix} \text{spectrum}_1 \\ \vdots \\ \text{spectrum}_N \end{pmatrix}$$

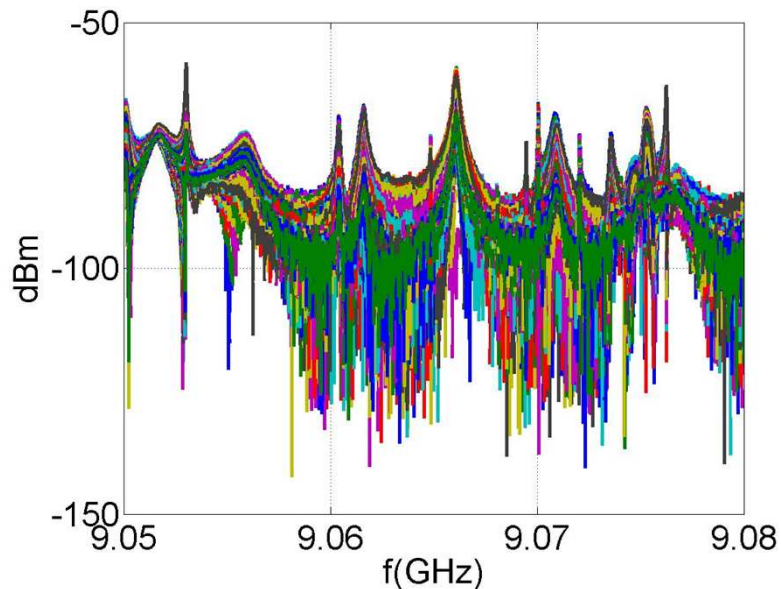
Coefficient matrix

$$B = \begin{pmatrix} x_1 & y_1 \\ \vdots & \vdots \\ x_N & y_N \end{pmatrix}$$

$$A \cdot M = B$$

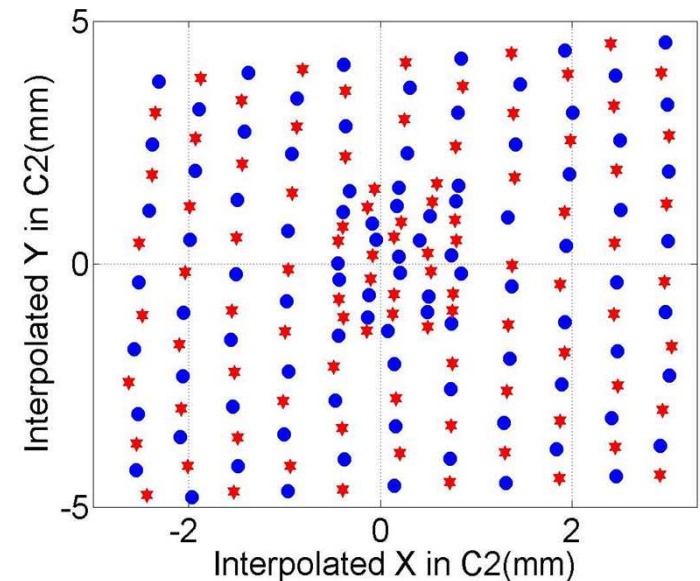


184 spectra



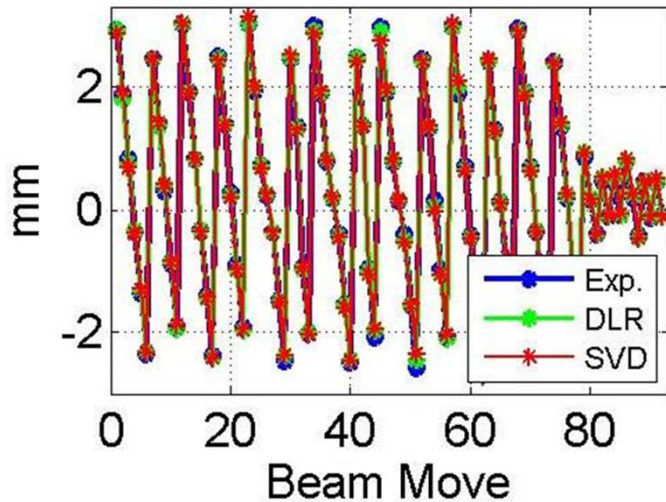
Two steps:

1. Calibration ●
2. Validation ★

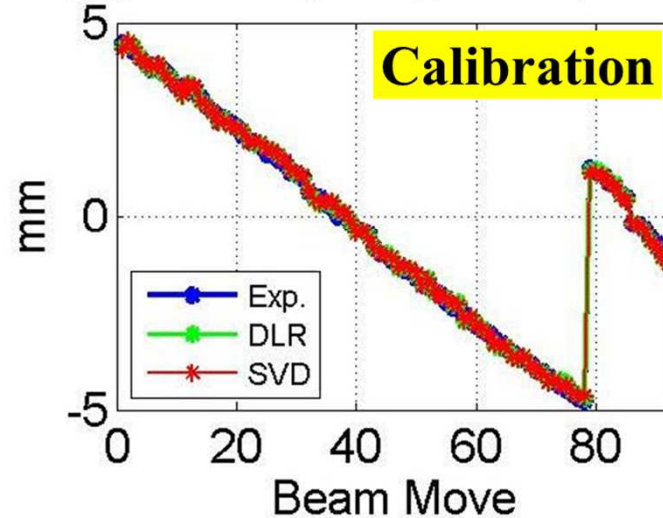


Performance (DLR)

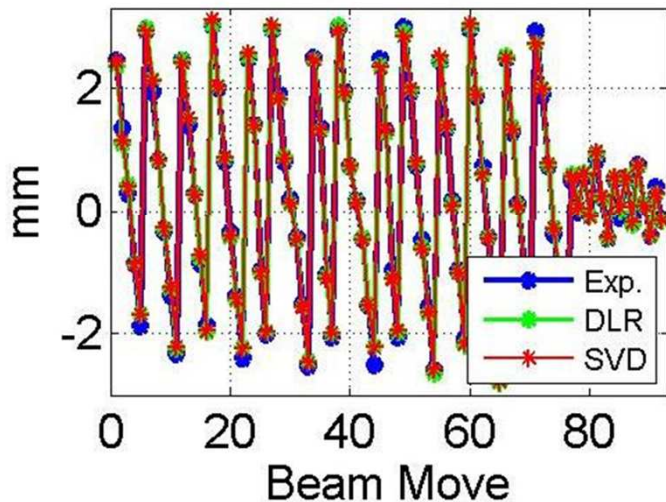
x (r^2 : 0.999(DLR), 0.998(SVD))



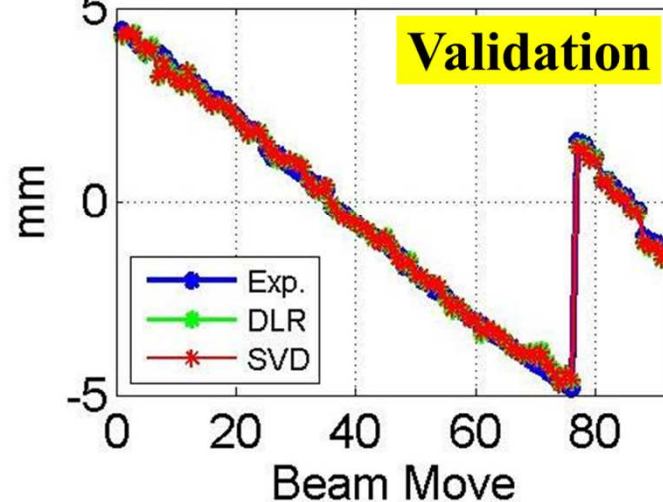
y (r^2 : 0.999(DLR), 0.999(SVD))



x (r^2 : 1(DLR), 0.996(SVD))



y (r^2 : 1(DLR), 0.997(SVD))



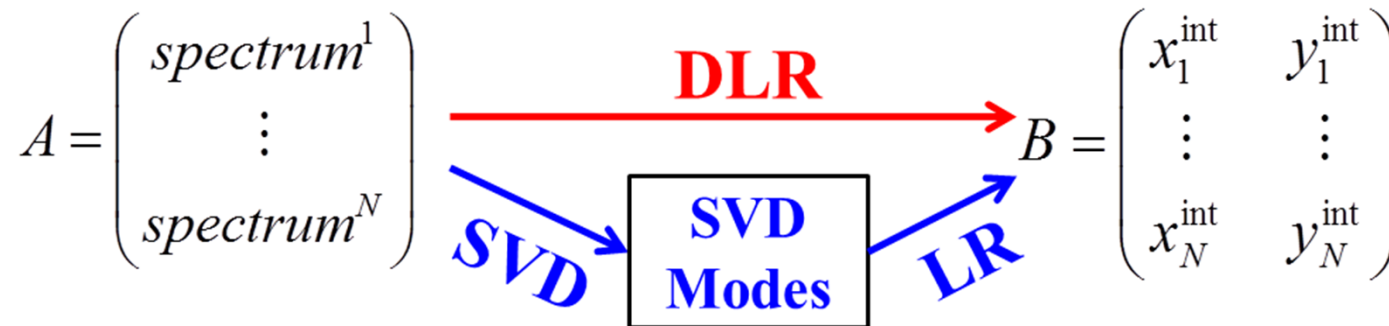
$$r^2 = 1 - \frac{\sum_{i=1}^n (B_i^{pre} - B_i)^2}{\sum_{i=1}^n (B_i - \bar{B})^2}$$

$r^2 = 1$, perfect fit
 $r^2 = 0$, bad fit

Singular Value Decomposition (SVD)



$$A \cdot M = B \quad \rightarrow \quad \text{Too many coefficients}$$



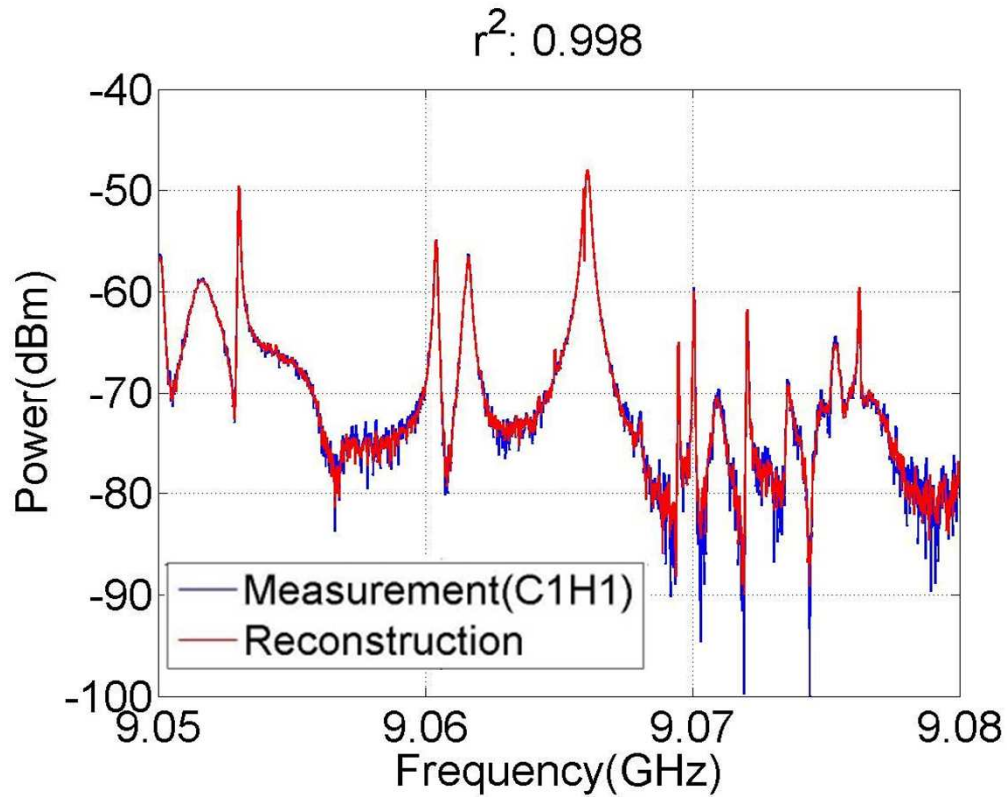
$$A = U \cdot S \cdot V^T \quad \longrightarrow \quad A_S \quad \text{Size}(A) = 1000\text{'s}$$

$$\text{Size}(A_S) = 10\text{'s}$$

$$A_S \cdot M_S = B$$

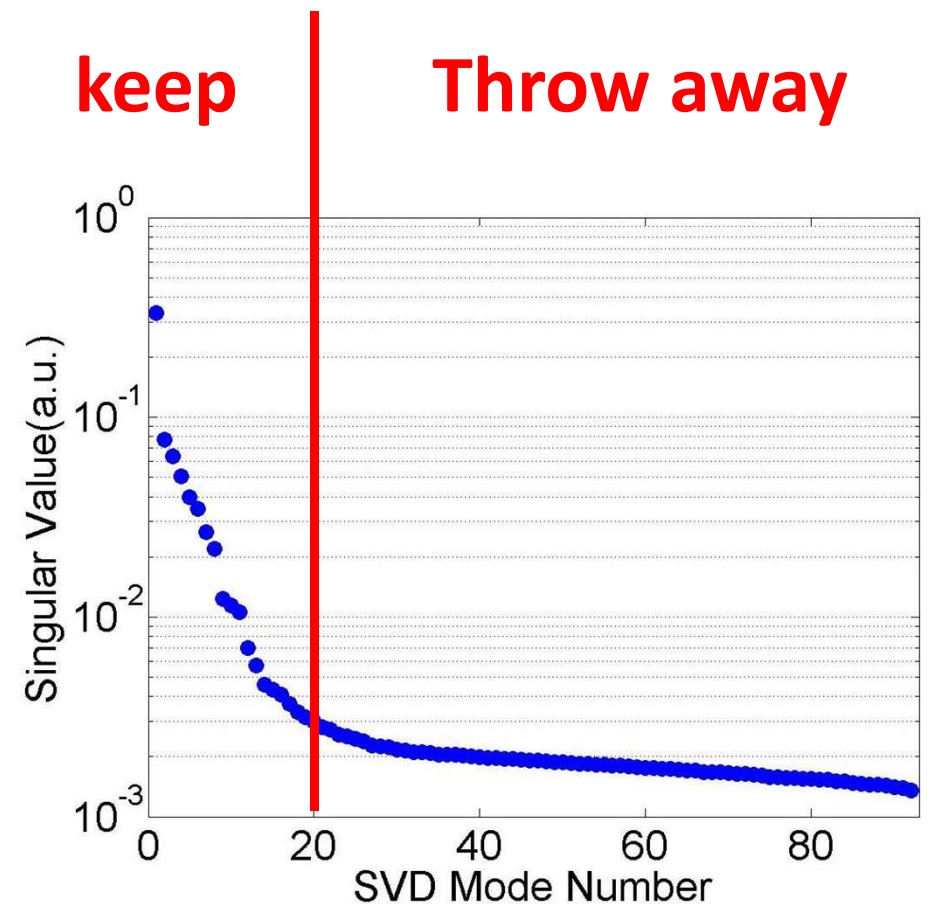
\rightarrow Much fewer coefficients

SVD Modes

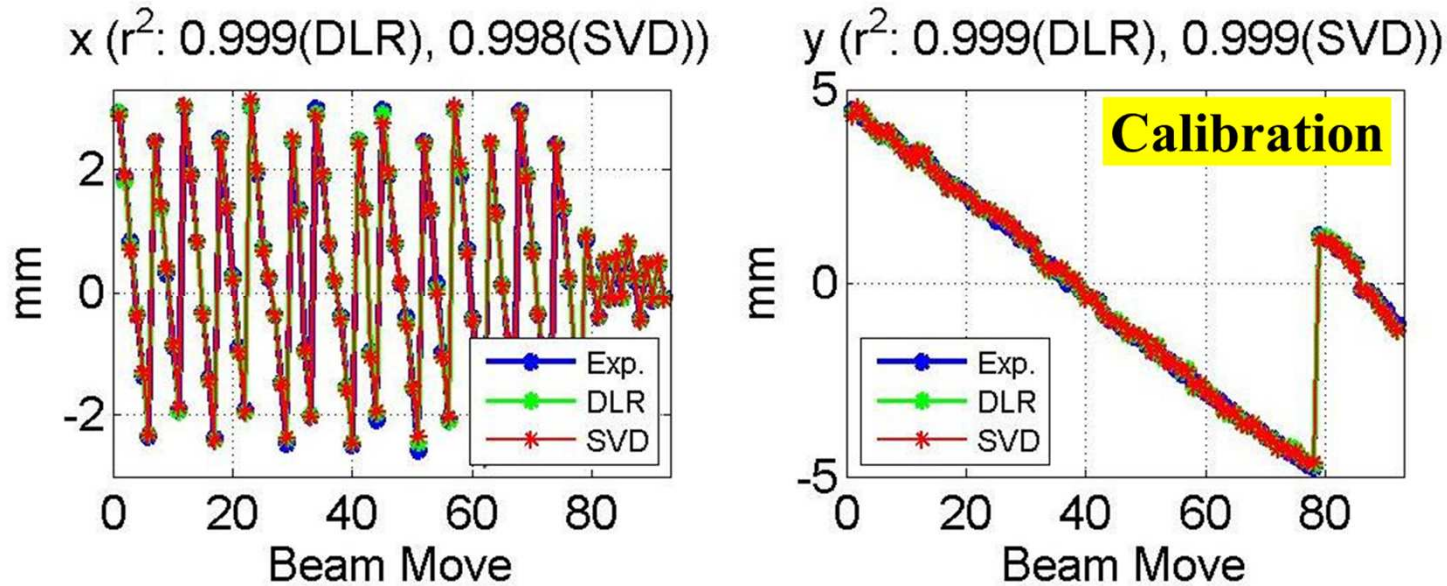


Dimension reduction

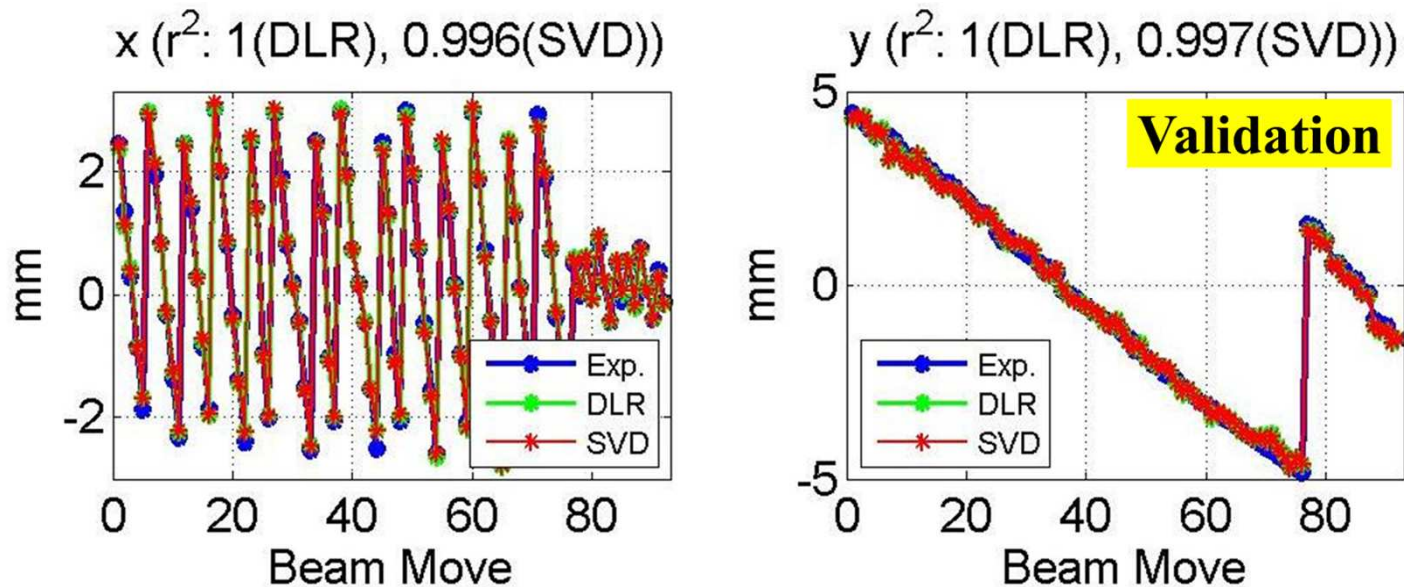
$$A_{reco} = \sum_{i=1}^{20} U_i \cdot S_{ii} \cdot V_i^T$$



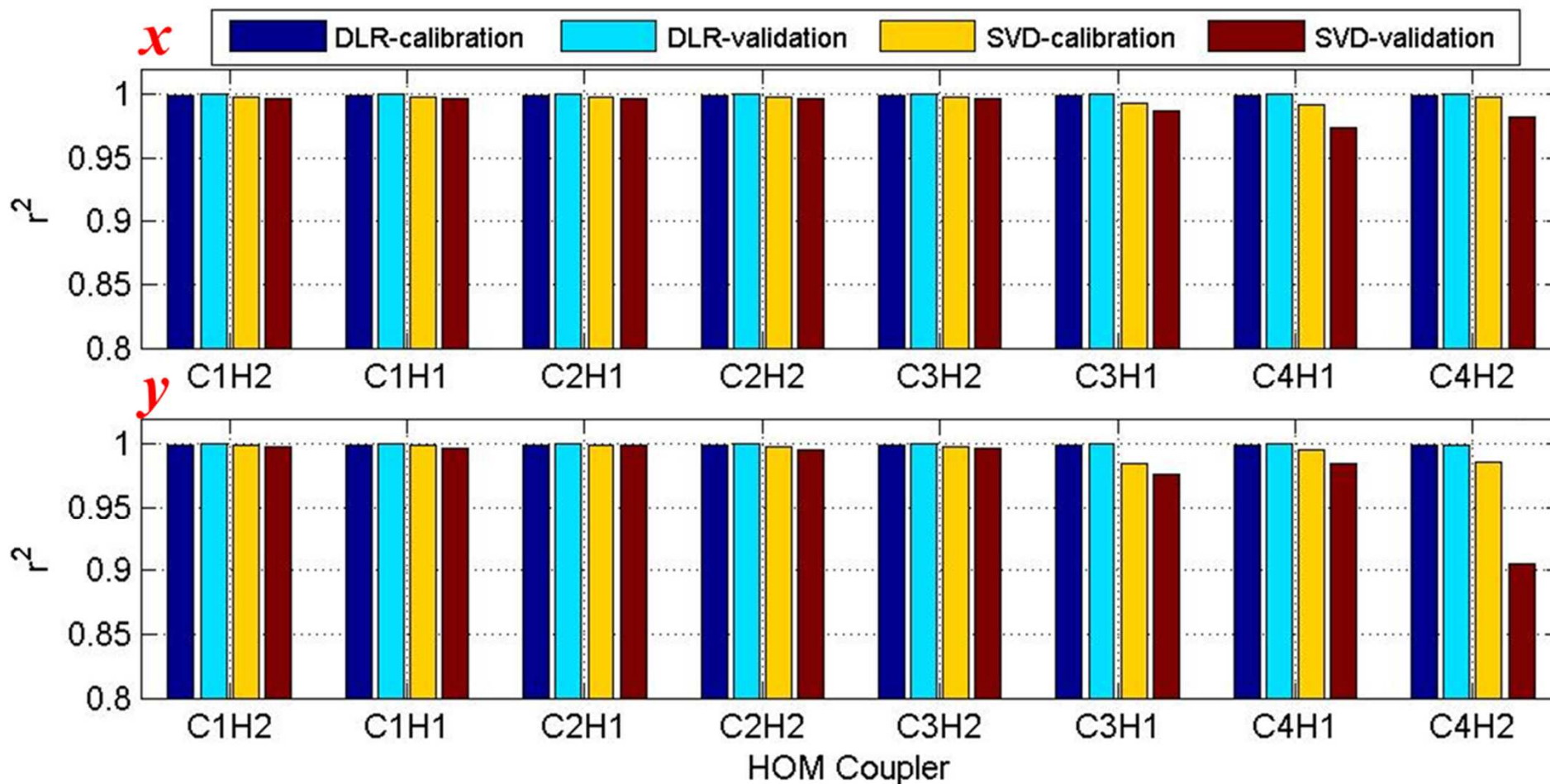
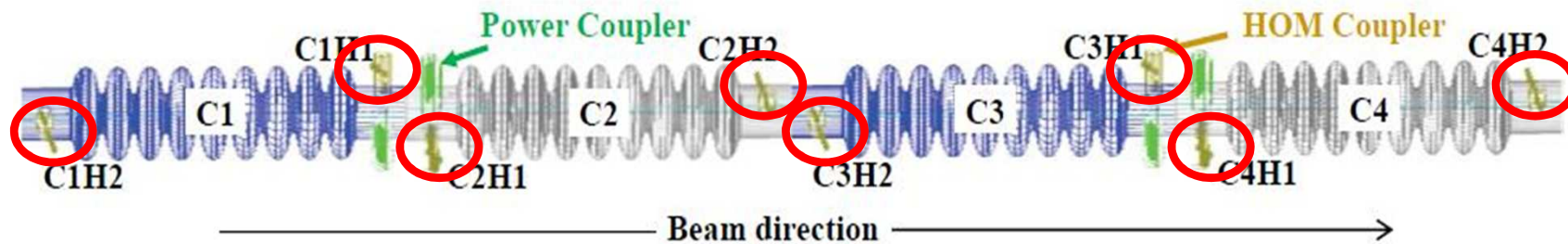
Performance (SVD)



Direct compare of SVD and DLR for the first time.



Extend to all 8 HOM Couplers



Summary

- **Trapped dipole modes** found in the 5th dipole band
- **Linear dependence** of HOMs on the transverse beam offset observed
- One mode to **a small band of modes**
- SVD and DLR are compared for **the first time**
- **Dedicated electronics are under design by collaborations of DESY and Fermilab**

Dipole Candidates	f range	Based-on
Beampipe modes†	~ 4 GHz	beam pipe
1 st or 2 nd cavity band†	~ 4-6 GHz	module
5 th cavity band	~ 9 GHz	cavity

†P. Zhang, *et al.*, DIPAC2011, Hamburg, Germany, 2011, MOPD17

- A PRSTAB paper is in prepare on HOM diagnostics