# Synthetic Aperture Radar Signal Processing

with Matlab Algorithms

Mehrdad Soumekh

#### Acknowledgements

The work reported in this book was supported by the following government agencies and private industries: National Science Foundation, Grant #MIP-9004996, P. Ramamoorthy, Program Director; Bell Aerospace (Textron), William Zwolinski, Technical Coordinator; Space Computer Corporation, Alan Stocker, Technical Coordinator; Summer Faculty Fellowships at Naval Research and Development (SPAWAR Systems Center), Robert Dinger (1992-95) and Lawrence Hoff (1995), Technical Coordinators; Summer Faculty Fellowship at Rome Laboratory, Air Force Office of Scientific Research, Michael Wicks, Technical Coordinator; Naval Research and Development, Grants #N66001-95-M-1383 and #N66001-7052-7595, Michael Pollock, Technical Coordinator; MITRE Corporation, Richard Perry, Technical Coordinator; Office of Naval Research, Grants #N00014-96-1-0586 and #N00014-97-1-0966, William Miceli, Program Officer; and Air Force Office of Scientific Research, Grant #F49620-99-1-0140, Jon Sjogren, Program Officer. Their generous support of this work is greatly appreciated.

# Contents

#### PREFACE

#### INTRODUCTION

Synthetic Aperture Radar The Book Organization SAR and ISAR Databases List of Figures

### CHAPTER 1 RANGE IMAGING

- 1.0 Introduction Outline Mathematical Notations and Symbols
- 1.1 System Model
- 1.2 Reconstruction via Matched Filtering
- 1.3 Range Resolution
- 1.4 Data Acquisition and Signal Processing *Time Domain Sampling Time Interval of Sampling Number of Time Samples*
- 1.5 Reconstruction Algorithm
- 1.6 Reconstruction via Pulse Compression for Chirp Signals Signal Model Reconstruction Range Resolution Time Domain Sampling Residual Video Phase Error Upsampling to Recover Alias-Free Echoed Signal Electronic Counter-Countermeasure (ECCM) Via Amplitude Modulation of Chirp Signals
- 1.7 Frequency-Dependent Target Reflectivity Reconstruction via Target Signature Matched Filtering
- 1.8 Matlab Algorithms

### CHAPTER 2 CROSS-RANGE IMAGING

- 2.0 Introduction Outline Mathematical Notations and Symbols
- 2.1 System Model
- 2.2 Spherical PM Signal within an Infinite Aperture
- 2.3 Reconstruction via Matched Filtering: Infinite Aperture
- 2.4 Spherical PM Signal within a Finite Aperture Instantaneous Frequency Slow-Time Fourier Transform Slow-Time Angular Doppler Spectrum
- 2.5 Reconstruction via Matched Filtering: Finite Aperture
- 2.6 Cross-Range Resolution
- 2.7 Data Acquisition and Signal Processing Synthetic Aperture Sampling for a Broadside Target Area Synthetic Aperture Sampling for a Squint Target Area Reducing PRF via Slow-Time Compression Cross-Range Gating via Slow-Time Compression
- 2.8 Reconstruction Algorithm
  - Baseband Conversion of Target Area Zero-Padding in Synthetic Aperture Domain Slow-Time Doppler Domain Subsampling Reducing Bandwidth of Reconstructed Image
- 2.9 Synthetic Aperture-Dependent Target Reflectivity
  - AM-PM Signal Model
  - Slow-Time Fourier Transform of AM-PM Signal
  - Example 1: Spotlight SAR
  - Example 2: Stripmap SAR
  - Reconstruction
  - Representation in Slow-Time Angular Doppler Domain
- 2.10 Reconstruction via Target Signature Slow-time Matched Filtering Type 1: Generalization of Spotlight SAR Type 2: Generalization of Stripmap SAR Type 3: Partial Observability
- 2.11 Matlab Algorithms

### CHAPTER 3 SAR RADIATION PATTERN

3.0	Introduction
	Outline
	Mathematical Notations and Symbols
3.1	Transmit Mode Radar Radiation Pattern
	Example 1: Planar Radar Antenna
	Example 2: Parabolic Radar Antenna
	Example 3: Circular Radar Antenna
	Synthetic Aperture (Slow-Time) Dependence
3.2	Radiation Pattern in Three-Dimensional Spatial Domain
	Radar Footprint
	Slant-Range

- 3.3 Transmit-Receive Mode Radar Radiation Pattern
- 3.4 Transmit-Receive Mode Radar-Target Radiation Pattern
- 3.5 Polarization
- 3.6 Matlab Algorithms

### CHAPTER 4 GENERIC SYNTHETIC APERTURE RADAR

- 4.0 Introduction Outline Mathematical Notations and Symbols
- 4.1 System Model
- 4.2 Fast-Time Fourier Transform
- 4.3 Slow-Time Fourier Transform
- 4.4 Reconstruction
- 4.5 Digital Reconstruction via Spatial Frequency Interpolation Baseband Conversion of Target Area Interpolation from Evenly Spaced Data Interpolation from Unevenly Spaced Data
- 4.6 Digital Reconstruction Via Range Stacking Algorithm 1: Fast-Time Slow-Time Matched Filtering Algorithm 2: Slow-Time Fast-Time Matched Filtering

- 6 Contents
  - 4.7 Digital Reconstruction Via Time Domain Correlation and Backprojection *Time Domain Correlation Algorithm Backprojection Algorithm*

#### 4.8 Frequency and Synthetic Aperture-Dependent Target Reflectivity

- 4.9 Motion Compensation Using Global Positioning System Spatial Frequency Modeling of Motion Errors Narrow-Beamwidth Motion Compensation Wide-Beamwidth Motion Compensation Three-Dimensional Wide-Beamwidth Motion Compensation Motion Compensation for Backprojection
- 4.10 Motion Compensation Using In-Scene Targets Narrow-Beamwidth Motion Compensation Wide-Beamwidth Motion Compensation Three-Dimensional Wide-Beamwidth Motion Compensation

4.11 Polar Format Processing

Plane Wave Approximation-Based Reconstruction Narrow-Beamwidth Approximation Narrow-Bandwidth and Narrow-Beamwidth Approximation Wavefront Curvature Compensation Motion Compensation Using Global Positioning System

#### 4.12 Conventional ISAR Modeling and Imaging

ISAR Modeling Slow-Time Compression or Motion Compensation Polar Format Processing

#### 4.13 Range-Doppler Imaging

Fresnel Approximation-Based Reconstruction Narrow-Bandwidth and Narrow-Beamwidth Approximation

4.14 Three-Dimensional Imaging With Two-Dimensional Azimuth and Elevation Synthetic Apertures System Model Reconstruction

#### 4.15 Electronic Counter-Countermeasure Via Pulse Diversity

## CHAPTER 5 SPOTLIGHT SYNTHETIC APERTURE RADAR

5.0	Introduction
	Outline Mathematical Notations and Symbols
5.1	Mechanically Beam-Steered Spotlight SAR Mechanical Beam Steering System Model Reconstruction
5.2	Electronically Beam-Steered Spotlight SAR Electronic Beam Steering System Model Reconstruction
5.3	Bandwidth of Spotlight SAR Signal Single Target Target Area
5.4	Resolution and Point Spread Function
5.5	Data Acquisition and Signal Processing Fast-Time Domain Sampling and Processing Slow-Time Domain Sampling and Processing Reducing PRF via Slow-Time Compression Digital Spotlighting Subaperture Digital Spotlighting
5.6	Reconstruction Algorithms and SAR Image Processing Digital Reconstruction via Spatial Frequency Interpolation Reconstruction in Squint Spatial Coordinates Slow-Time Doppler Domain Subsampling Reducing Bandwidth of Reconstructed Image Digital Reconstruction via Range Stacking Digital Reconstruction via Time Domain Correlation and Backprojection Effect of Slow-time Doppler Filtering Effect of Motion Errors in Slow-time Doppler Spectrum
5.7	Matlab Algorithms

#### 8 Contents

### CHAPTER 6 STRIPMAP SYNTHETIC APERTURE RADAR

- 6.0 Introduction Outline Mathematical Notations and Symbols
- 6.1 System Model Radar Radiation Pattern Stripmap SAR Signal Model
- 6.2 Reconstruction
- 6.3 Bandwidth of Stripmap SAR Signal Planar Radar Antenna Curved Radar Antenna
- 6.4 Resolution and Point Spread Function
- 6.5 Data Acquisition and Signal Processing Fast-Time Domain Sampling and Processing Slow-Time Domain Sampling and Processing Slow-time Compression and Processing Subaperture Digital Spotlighting Reducing Side Lobes Doppler Aliasing via Slow-Time Upsampling
- 6.6 Reconstruction Algorithms and SAR Image Processing Digital Reconstruction via Spatial Frequency Interpolation Slow-Time Doppler Domain Subsampling Reducing Bandwidth of Reconstructed Image Digital Reconstruction via Range Stacking Digital Reconstruction via Time Domain Correlation and Backprojection Effect of Beamwidth (Slow-time Doppler) Filtering Effect of Motion Errors in Slow-time Doppler Spectrum Subpatch "Mosaic" Digital Reconstruction with Subaperture Data

6.7 Moving Target Detection and Imaging SAR Signal Model for a Moving Target with a Constant Velocity Three-Dimensional Imaging in Motion-Transformed Spatial Domain and Relative Speed Domain Moving Target Indicator: SAR Ambiguity Function

6.8 Matlab Algorithms

Contents 9

### CHAPTER 7 CIRCULAR SYNTHETIC APERTURE RADAR

7.0	Introduction
	Outline
	Mathematical Notations and Symbols
7.1	System Model
	CSAR Signal Model
	Fourier Properties of Slant Plane Green's Function
7.2	Reconstruction
	Slant Plane to Ground Plane Transformation
	Ground Plane CSAR Reconstruction
7.3	Bandwidth of CSAR Signal
7.4	Resolution and Point Spread Function
	Full Rotation Aspect Angle Measurement
	Partial Rotation Aspect Angle Measurement
7.5	Data Acquisition and Signal Processing
	Fast-Time Domain Sampling and Processing
	Slow-Time Domain Sampling and Processing
	Digital Spotlighting and Clutter Filtering
7.6	Reconstruction Algorithms and CSAR Image Processing
	Digital Reconstruction via Spatial Frequency Interpolation
	Reducing Bandwidth of Reconstructed Image
	Digital Reconstruction via Time Domain Correlation and Backprojection
7.7	Three-Dimensional Imaging
7.8	Target Resolvability from Single Tone Fringe Patterns
7.9	Three-Dimensional Imaging With Two-Dimensional Circular
	and Elevation Synthetic Apertures
	System Model
	Reconstruction
	Digital Reconstruction

### CHAPTER 8 MONOPULSE SYNTHETIC APERTURE RADAR

8.0 Introduction

Outline Mathematical Notations and Symbols 8.1 Along-Track Moving Target Detector Monopulse SAR Along-Track Monopulse SAR System Geometry Monostatic SAR Signal Model Bistatic SAR Signal Model Synthesis of Monostatic SAR Signal from Bistatic SAR Signal Moving Target Indicator Effect of Variations in Altitude and Nonlinear Motion 8.2 Effect of Uncalibrated and Unstable Radars Amplitude Patterns of Monopulse Radars Instability of Monopulse Radars Wide-Beamwidth Monopulse Radars 8.3 Signal Subspace Registration of Uncalibrated SAR Images System Model Signal Subspace Processing Estimating Calibration Error Impulse Function Application in MTD Monopulse SAR Application in Automatic Target Recognition SAR 8.4 Slant Plane Topographic Mapper Monopulse SAR Slant Plane Monopulse SAR System Geometry Monostatic and Bistatic SAR Signal Models Narrow-Bandwidth and Narrow-Beamwidth Approximation: Interferometric SAR (IF-SAR) Wide-Bandwidth and Wide-Beamwidth Model Estimating Slant-Range Shift via Signal Subspace Processing

- 8.5 Multistatic Monopulse ISAR Multistatic ISAR Model Motion Tracking via Signal Subspace Processing
- 8.6 Matlab Algorithms

### **BIBLIOGRAPHY**

INDEX