

# LOOKING THROUGH THE “GLASS CEILING”: A CONCEPTUAL FRAMEWORK FOR THE PROBLEMS OF SPECTRAL SIMILARITY

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## ABSTRACT

Spectral similarity measures have been shown to exhibit good performance in several Music Information Retrieval (MIR) applications. They are also known, however, to possess several undesirable properties, namely allowing the existence of hub songs (songs which frequently appear in nearest neighbor lists of other songs), “orphans” (songs which practically never appear), and difficulties in distinguishing the farthest from the nearest neighbor due to the concentration effect caused by high dimensionality of data space. In this paper we develop a conceptual framework that allows connecting all three undesired properties. We show that hubs and “orphans” are *expected* to appear in high-dimensional data spaces, and relate the cause of their appearance with the concentration property of distance / similarity measures. We verify our conclusions on real music data, examining groups of frames generated by Gaussian Mixture Models (GMMs), considering two similarity measures: Earth Mover’s Distance (EMD) in combination with Kullback-Leibler (KL) divergence, and Monte Carlo (MC) sampling. The proposed framework can be useful to MIR researchers to address problems of spectral similarity, understand their fundamental origins, and thus be able to develop more robust methods for their remedy.

## 1. INTRODUCTION

The notion of audio-based music similarity is generally considered to be complex, subjective, and context dependent [13]. However, spectral similarity measures [2, 10] are receiving a growing interest and have been shown to exhibit good performance in several Music Information Retrieval (MIR) applications [14]. These measures describe aspects related to timbre and model the “global sound” of a musical signal based on features called Mel Frequency Cepstrum Coefficients (MFCCs).

Despite the advantages of spectral similarity measures, related research has also reported a number of undesired properties, summarized as follows:

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- The existence of hub songs (also called “always similar”) [2], which are close neighbors of many other pieces to which they hold no perceptual similarity, thus increasing the rate of false positives.
- The existence of “orphans” (also called “never similar”) [12], which are songs that rarely become close neighbors of any other piece (despite possibly having perceptual similarity to a large number of songs), increasing therefore the rate of true negatives.
- Songs are represented in a feature space whose dimensionality is determined by the number of features (MFCCs). As the dimensionality grows, it is becoming hard to identify meaningful nearest neighbors, since all songs tend to be at nearly the same distance from each other. This property was identified in other research areas [1, 5, 8], but was also examined in the contexts of MIR [6] and audio speech data (based on MFCCs) [18].

These undesired properties constitute some of the main causes for the empirically demonstrated upper limit for the performance of spectral similarity measures, referred to as the “glass ceiling” [2]. Recent research has focused mostly on the amelioration of hubness (the attribute of being a hub song), by proposing techniques for normalizing the distances between songs in a way that reduces the influence of hubs [11, 14, 15], whereas other works [9, 17, 19] developed measures that try to avoid hubness.

Our motivation is to develop a conceptual framework that allows for relating all three aforementioned undesired properties, and explains the mechanisms that create them. Aucouturier and Pachet [3] have focused on the analysis of hubness and concluded that the creation of *homogenized* models (i.e., models that ignore the least likely mixture components) are responsible for creating hubs. Despite this detailed conclusion, our emphasis is to disclose a more fundamental reason that causes all three undesired properties, which is the high dimensionality of the feature space that originates from the need to use multiple MFCCs in order to capture the “global sound”.

A conjecture about the role of high dimensionality has been stated by Berenzweig in his thesis [4]. This conjecture was drawn from two synthetic data sets that follow multivariate Gaussian distributions. In particular, a main conclusion of this thesis [4, page 99] was: “First, hubness

seems to be a natural consequence of the curse of dimensionality, at least for the points distributed according to a Gaussian in a space up to 32 dimensions. In high dimensions these points tend to be spread around the shell of the space with very few points near the center; this implies that any points that do happen to remain near the center will be extreme hubs.” However, this work neither generalized the conclusion to real audio music data, nor even to other settings besides simple synthetic data. More importantly, it did not provide a clear explanation of the mechanism that creates hubness, leaving this question unresolved [4, question 1 on page 99]. A more thorough examination of hubness has been performed by Radovanović et al. [16], wherein using real vector-space data the authors relate hubness with the *intrinsic* dimensionality of data, and show that in (intrinsically) high-dimensional data sets hubs tend to appear in the proximity of cluster centers. However, [16] focused primarily on general vector spaces and  $l_p$  norms, with the results not directly applicable for MIR purposes.

In this paper, we propose a conceptual framework to provide a clear explanation of the mechanism that creates hubness and show that hubs are *expected* to appear in high-dimensional spaces (i.e., they are not points that just *happen* to remain near the center). Moreover, the framework helps to understand the connection between all three undesired properties: hubs, “orphans” and the problem of finding meaningful neighbors. Also, our conclusions are verified with real audio music data. The proposed conceptual framework can be useful to MIR researchers to address the problems of spectral similarity in relation to each other, understand their fundamental reasons, and thus be able to develop more robust methods for their remedy.

In the rest of this article, Section 2 reviews related work. Section 3 presents the proposed framework, whereas Section 4 provides empirical evidence for verifying the conclusions of the proposed framework in the MIR domain. Finally, Section 5 concludes the paper.

## 2. RELATED WORK

Research by Aucouturier and Pachet [3] focuses on the nature and causes of hub songs. They propose methods to detect hubs and infer that hubs are distributed along a scale-free distribution. Moreover, in their work they deduce that hubs neither exist due to the spectral features, nor are they a property of a feature representation or a given modeling strategy but rather tend to occur with any type of model that uses agglomeration of multiple frames of a sound texture. Furthermore, they establish that hubness is not a characteristic of certain songs, as different algorithms distribute hubs differently in a database. In addition, they also establish that the class of algorithms studied is irrelevant to hubs which appear only for data with a given amount of heterogeneity. Finally, they conclude that hubness can be localized to certain parts of the distribution of a song.

Berenzweig [4] offers insight as to the understanding of hubs and arrives to the conclusion that their existence is a natural result of the curse of dimensionality. Additionally, in his work, the possibility of hubs being derived from sim-

ilarity to a universal background is proven invalid through experimentation, that is by showing that the discriminating power of specific frames is not ameliorated by weighting based on their shared information.

As mentioned in Section 1, unlike Aucouturier and Pachet [3] our motivation is to provide high dimensionality as a more fundamental reason for hubness, and for the other two undesired properties (see Section 1) as well. Differentiating also from the work of Berenzweig [4], we develop a thorough conceptual framework that links all three properties and clearly explains the mechanisms through which they originate.

Other related work includes techniques to ameliorate or try to avoid hubness [9, 11, 14, 15, 17, 19]. We hope that our proposed framework will assist in this direction, by allowing MIR researchers to further analyze the causes of all examined undesired properties (not just hubness), and develop solutions that take into account all of them.

## 3. PROPOSED CONCEPTUAL FRAMEWORK

We commence the description of the proposed conceptual framework by demonstrating the property of *concentration* [8] that is exhibited by spectral similarity measures due to the high dimensionality of their feature space. Next, we examine how the generation of hubs and “orphans” can be explained as a consequence of high dimensionality, in relation with the concentration phenomenon. The conclusions (in this and the following section) are verified with real data. Since our description involves some empirical measurements, we start by detailing the employed settings.

### 3.1 Settings for Empirical Measurements

We focus on two characteristic spectral similarity measures that have been widely used in related research. The first is proposed by Logan and Salomon [10], and uses Earth Mover’s Distance (EMD) in combination with Kullback-Leibler (KL) divergence to compute the distance between groups of frames generated by a GMM approach. The second is proposed by Aucouturier and Pachet [2], and uses Monte Carlo (MC) sampling to measure the similarities of GMMs. Henceforth, the first measure is denoted as EMD-KL, whereas the second as GMM-MC. We based our implementation of both measures on the MA toolbox [12].

The main parameter examined for both measures is the number of MFCCs, denoted as  $d$ , which corresponds to the dimensionality of the feature space, since each frame of the audio signal is mapped to a point in a  $d$ -dimensional space.

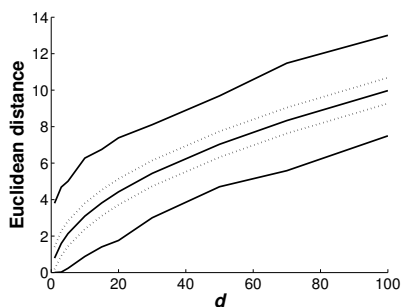
The default value for the number of clusters used in Gaussian mixture modeling performed by GMM-MC and EMD-KL is equal to one, since measures like GIC [12] have demonstrated the efficacy of this option. In our experiments we also examined other values in order to verify that this factor does not have any impact on our conclusions. For brevity we therefore present results only for the default number of clusters. Regarding other parameters (sampling rate, frame size, etc.), empirical evidence in related work [3], and our experiments, indicates that they are not related with the examined issues. For this reason, we

keep the remaining parameters at the default values from the MA toolbox, which correspond to commonly used values in most related works. The sampling frequency of the input wav file is 11025, the FFT window size is 512 samples and the FFT window hop size is 256 samples. Finally, we used the MIREX'04 audio collection for the reasons that it is widely used by the MIR community, has been involved in all related work (e.g., [3]), and is publicly available, allowing reproducibility of the presented results.

### 3.2 The Property of Concentration

The concentration property of a distance (similarity) measure refers to the tendency of all points in a high-dimensional feature space to be almost equally distant from (similar to) each other. Concentration has been studied in vector spaces for Euclidean distance and other  $l_p$  norms (including fractional distances) [1, 8], and was also analyzed in the MIR context [6], but not explicitly for the spectral similarity measures we are focusing on in this work.

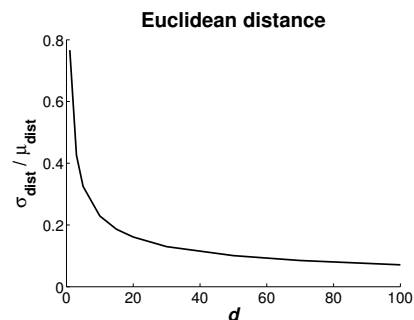
To ease comprehension, we first consider iid Gaussian random data with  $d$ -dimensional points, the components of which are independently drawn from  $\mathcal{N}(0, 1)$ . Figure 1 illustrates the concentration of Euclidean distance that incurs with high dimensionality. In particular, the figure depicts from top to bottom: the maximal observed value, mean value plus one standard deviation, the mean value, mean value minus one standard deviation, and minimal observed value of distances of all data points to the origin. It can be seen that the mean value steadily increases with increasing dimensionality, while the standard deviation remains constant, and that the observed minimal and maximal values become constrained to a narrow interval as dimensionality increases. This means that distances of all points to the origin (i.e., the norms) become very similar to each other as dimensionality increases, with the same behavior also extending to all pairwise distances within a data set [8], thus making it harder to distinguish between the farthest and the nearest neighbor in high dimensions [1]. It is important to note that this property of distances was proven to hold for *any* iid random data distribution [8].



**Figure 1.** Concentration of Euclidean distance for iid Gaussian random data ( $n = 2000$  points).

Concentration is usually expressed as the ratio between some measure of spread, like the standard deviation, and some measure of magnitude, like the mean value, of distances of all points in a data set to some arbitrary reference point [1, 8]. If this ratio converges to 0 as dimensionality

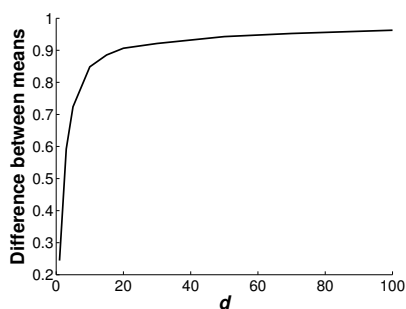
goes to infinity, it is said that distances concentrate. Regarding the aforementioned synthetic data set, if the origin is selected as the reference point, Fig. 2 illustrates the ratio between the standard deviation ( $\sigma_{\text{dist}}$ ) and mean value ( $\mu_{\text{dist}}$ ) of distances of all points to the origin, showing that it tends to 0 as dimensionality increases. Moreover, theoretical results by François et al. [8] indicate that the same asymptotic behavior holds with any other point selected as the reference, and also extends to all pairwise distances in a data set. In the case of Euclidean distance, the mean value  $\mu_{\text{dist}}$  behaves asymptotically as  $\sqrt{d}$ , whereas the standard deviation  $\sigma_{\text{dist}}$  remains asymptotically constant.



**Figure 2.** Ratio between the standard deviation and mean value of the distribution of distances to the origin, for iid Gaussian random data.

The property of concentration can be used to explain the generation of hubs and “orphans” as follows. Existing theoretical and empirical results [1, 5] specify that concentration can be viewed as causing points in a high-dimensional data set to approximately lie on the surface of a hypersphere centered at an arbitrary point. In addition, further results [7, 8], as illustrated in Fig. 1, indicate that the distribution of distances to any reference point has a finite variance for any given  $d$ . If the data distribution center is taken to be the reference point (as, coincidentally, is the case in the previously used random data example), it can be said that it is *expected* for points closer to the data center to exist in high dimensions, since for any finite  $d$  the standard deviation of the distribution of distances to the data set center is finite (in this case, constant). However, in higher dimensions, the points closer to the center have the tendency to become closer, on average, to all other points, thus having increased probability of becoming hubs by being near neighbors of many remaining points. On the other hand, it is also expected to have a non-negligible number of points farther from the data set center. Consequently, these points, which are the “orphans”, become farther from all other points and more difficult to be near neighbors of any other point. The aforementioned connection between concentration and hubs/“orphans” has been initially proposed by Radovanović et al. [16] using experimentation on iid uniform random data, in contrast to Gaussian random data which pertains to real musical data utilized in this paper. Still, it is important to note that based on the results in [8], the reasoning followed in [16] can be applied to *any* iid random data distribution.

In order to clarify the mechanism through which the “centrality” of a point close to the data center, i.e. its proximity to all other points, becomes amplified in high dimensions, let us return to the iid Gaussian random data example and observe as reference points (instead of the origin) two points with the following properties: point  $x_0$ , which is at the expected distance from the data center for a given dimensionality  $d$ , and point  $x_2$ , which is two standard deviations closer to the center than  $x_0$ .<sup>1</sup> Next, we compute the distributions of distances of  $x_0$  and  $x_2$  to all other points, and denote the means of these distributions  $\mu_{x_0}$  and  $\mu_{x_2}$ , respectively. Figure 3 plots the difference between  $\mu_{x_0}$  and  $\mu_{x_2}$ . It can be seen that this difference increases with increasing dimensionality, meaning that  $x_2$  becomes closer, on average, to all other points, solely by virtue of increasing dimensionality. According to the results by François et al. [8], verified by our empirical measurements, both  $\mu_{x_0}$  and  $\mu_{x_2}$  asymptotically behave as  $\sqrt{d}$ . However, convergence does not occur at the same *speed*, giving rise to the differences shown in Fig. 3 which ultimately result in the emergence of hubs. Similar arguments hold when, for example, point  $x_2$  is taken to be two standard deviations *farther* from the center than  $x_0$ , explaining the formation of “orphans.”



**Figure 3.** Difference between means of distance distributions to points at analogous positions wrt the data center, for iid Gaussian random data.

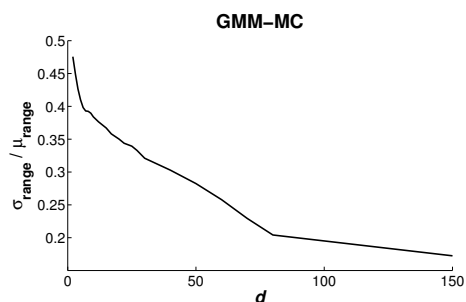
### 3.3 Concentration in Real Audio Data

The preceding discussion suggests that concentration can help explain the generation of hubs and “orphans” for audio music data and spectral similarity measures. However, the aforementioned conclusions were drawn with respect to distances between single points, whereas spectral similarities are computed between Gaussian Mixture Models (GMMs). Moreover, in this case of spectral similarity, we can only consider pairwise distances and not a point of reference like the center. Therefore, to examine the concentration of spectral similarity, we perform the following measurement. We vary the dimensionality of the feature space (number of MFCCs). For each examined dimensionality, we define for each song in the examined collection its *neighbor-range* by computing the difference between the

<sup>1</sup> Roughly speaking, for every  $d$  point  $x_0$  has the same “probability” of occurrence with regards to the distance from the data distribution center, and the same can be said for  $x_2$ .

distances to its farthest and nearest neighbor. To characterize the distribution of neighbor-range for each dimensionality, as explained before, we follow the approach of related work [8] and compute the ratio between the standard deviation  $\sigma_{\text{range}}$  and the mean  $\mu_{\text{range}}$  of the neighbor-ranges of all songs.

Figure 4 illustrates this ratio as a function of dimensionality, for the two examined spectral similarity measures. The fact that the examined ratio reduces with increasing dimensionality indicates that the neighbor-range is narrowing as dimensionality increases, making it more difficult to separate the closest from the farthest neighbor. Asymptotically, as dimensionality tends to infinity, the examined ratio is expected to become equal to zero, denoting that the closest and the farthest neighbor of any song will tend to coincide. This means that asymptotically all points tend to become equidistant. However, for the high but finite dimensionality values used in MIR applications, the standard deviation in the examined ratio will be small but nonzero, causing an analogous amplification of “centrality” to that described above.



**Figure 4.** Ratio of standard deviation and mean value of neighbor-range as a function of dimensionality.

## 4. DIMENSIONALITY: ROLE & IMPACT ON MIR

The proposed framework allows for explaining the emergence of hubs and “orphans” principally as a consequence of high dimensionality of the feature space, in relation with the concentration it incurs. In this section we will verify with the examined real audio music data that the high dimensionality of the feature space creates the hubs and “orphans” according to the mechanism described in the previous section. Additionally, we examine the resulting impact of high dimensionality on MIR specific applications.

### 4.1 Verifying the Role of Dimensionality

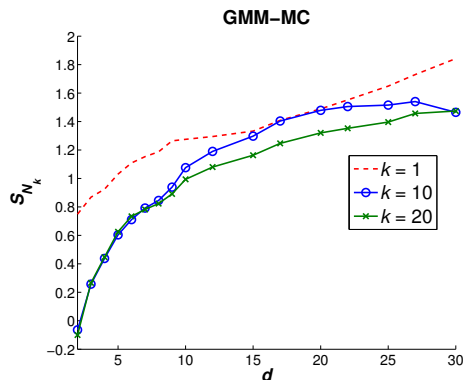
Let  $N_k(x)$  denote the number of  $k$ -occurrences of each song  $x$  in a collection, i.e., the number of times  $x$  occurs among the  $k$  nearest neighbors of other songs. Following the approach in [16], we express the asymmetry of  $N_k$  (i.e., the skewness) using the standardized third moment:

$$S_{N_k} = E(N_k - \mu_{N_k})^3 / \sigma_{N_k}^3,$$

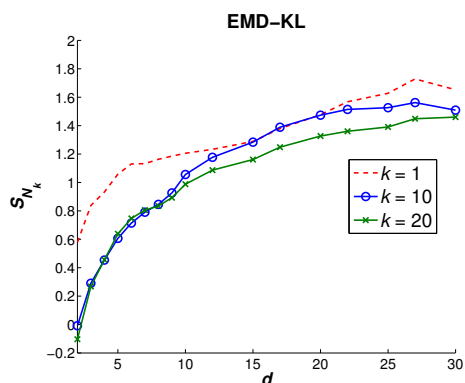
where  $\mu_{N_k}$  and  $\sigma_{N_k}$  are the mean and standard deviation of  $N_k$ .<sup>2</sup> For the examined real audio data, and for the two

<sup>2</sup> An  $S_{N_k}$  value of 0 signifies that the distribution of  $N_k$  is symmetrical, positive (negative) values indicate skewness to the right (left).

similarity measures GMM-MC and EMD-KL, Figures 5 and 6, respectively, depict skewness as a function of dimensionality (three different values of  $k$  are examined in each case). As dimensionality increases, the increase of skewness, for all values of  $k$ , indicates that the distribution of  $N_k$  becomes considerably skewed to the right, resulting in the emergence of *hubs*, i.e., points which appear in many more  $k$ -nearest neighbor lists than other points.



**Figure 5.** Skewness of  $N_k$  as a function of dimensionality for the GMM-MC measure.



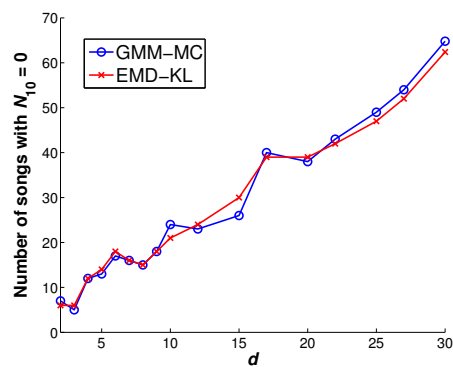
**Figure 6.** Skewness of  $N_k$  as a function of dimensionality for the EMD-KL measure.

Regarding “orphans,” Figure 7 depicts, for both examined measures, the number of songs with  $N_k$  equal to zero as a function of dimensionality ( $k$  was set to 10). As expected, with increasing dimensionality, the number of such songs increases, demonstrating the relation of “orphans” with dimensionality.

All the above results show that dimensionality is the fundamental reason for the emergence of hubs and “orphans.” In the next section we examine the relevance of this result to the objectives of MIR.

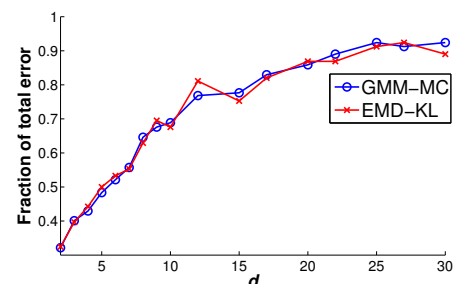
#### 4.2 Impact on MIR

In order to study how our main conclusion, concerning the role of high dimensionality, affects MIR applications, we rely on external labels, such as the genre, to characterize the similarity between songs. This assumption is being widely applied in MIR (e.g., in MIREX contests), since results in related work [13] indicate that this assumption is reasonable.



**Figure 7.** Number of songs with  $N_k$  equal to 0 ( $k = 10$ ).

In this context, we measure the impact of hubs by examining the number of times they mismatch in label with the songs to which they are close neighbors. In this sense, we can measure how much of the total error (in terms of label mismatches) can be attributed to hubs. Figure 8 depicts, as a function of dimensionality, the fraction of total error due to the 10% of the strongest hubs, i.e., songs with the largest  $N_k$  values ( $k$  was set to 1). For low dimensionality values, when according to previous measurements hubs are not strong, their responsibility for the total error is much smaller compared to the case of larger dimensionality. It is worth to note that, for the largest examined dimensionality value, the strongest hubs are responsible for about 90% of the total error.



**Figure 8.** Fraction of total error due to 10% of the strongest hubs ( $k = 1$ ).

## 5. CONCLUSIONS

In this paper we propose a conceptual framework that relates the known shortcomings of spectral similarity measures for music data: the existence of hubs, “orphans” and the distance concentration phenomenon, with the high dimensionality of underlying data space. The framework presents a unifying view of the three examined problems of music similarity measures, offering an explanation of their fundamental origins, which will hopefully help MIR researchers develop robust methods for their remedy.

The issue of high dimensionality is significant for spectral similarity measures because small dimensionality usually leads to poor discriminating capability, while high dimensionality produces the described negative effects pertaining to hubs, “orphans,” and distance concentration.

In future work we will take into consideration more theoretical aspects of the hub/“orphan” properties and similarity concentration, providing a sounder theoretical backing for the described relationships. Furthermore, it would be interesting to examine why some approaches [9, 17, 19] tend to produce less hubs, by relating to the intrinsic dimensionality of the space they produce (i.e., to consider the proposed framework in explaining these approaches and understanding their reported properties). We also plan to conduct an extended experimental evaluation involving more similarity measures and data collections, giving more precise quantification of relationships between high dimensionality and the aforementioned properties of (spectral) similarity measures. Finally, we will develop novel mitigation methods for the problems induced by the existence of excessive hubs and “orphans”. In particular, we will examine machine learning methods that apply correction to spectral similarity measures in order to take into account that retrieval error may not be distributed uniformly (as exemplified in Section 4.2), thus focusing on hubs as the main source of error, and in order to enable “orphans” to participate more prominently as nearest neighbors.

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