

# Analysis of One Scheme for Enabling Cloud Storage Auditing with Verifiable Outsourcing of Key Updates

Zhengjun Cao<sup>1</sup>, Lihua Liu<sup>2</sup>, Olivier Markowitch<sup>3</sup>

(Corresponding author: Zhengjun Cao)

Department of Mathematics, Shanghai University<sup>1</sup>

No.99, Shangda Road, Shanghai, China

(Email: caozhj@shu.edu.cn)

Department of Mathematics, Shanghai Maritime University<sup>2</sup>

No.1550, Haigang Ave, Pudong New District, Shanghai, China

Computer Sciences Department, Université Libre de Bruxelles<sup>3</sup>

Boulevard du Triomphe CP 212, 1050 Bruxelles, Belgique

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## Abstract

Cloud computing supports a paradigm shift from local to network-centric computing and enables customers with limited computational resources to outsource large-scale computational tasks to the cloud, such as linear equations and linear programming. Recently, Yu et al. [IEEE TIFS, 11(6), 2016, 1362-1375] have proposed a scheme for cloud storage auditing with verifiable outsourcing of key updates. In this note, we remark that Yu et al.'s scheme has two inherent weaknesses: 1) it does not truly mitigate the client's computational burden for key updates; 2) it does not ensure confidentiality since the files uploaded to the cloud by the client are eventually not encrypted at all.

*Keywords:* Cloud Computing; Cloud Storage Auditing; Confidentiality; Third-party Auditor

## 1 Introduction

Cloud computing making use of the tremendous resources of computing and storage systems via the Internet, supports a paradigm shift from local to network-centric computing [17, 19], and benefits scientific and engineering applications, such as data mining and many other computational and data-intensive activities. It enables customers with limited computational resources to outsource large-scale computational tasks to the cloud, including linear equations [21, 23], linear programming [9, 20, 22], bilinear pairing [1, 7, 8, 11], matrix inversion computation [14] and matrix multiplication computation [13]. Many researchers have studied the new computing paradigm and proposed a lot of schemes [2, 6, 10, 12, 15, 16]. But some

kinds of flaws in some outsourcing schemes [3, 4, 5] were found for security, efficiency or other reasons.

Key-exposure problem is a special one related to key management. A primary observation on the problem in the scenario of cloud storage auditing is that once the client's secret key for storage auditing is exposed to the cloud, the cloud is able to easily hide the data loss incidents for maintaining its reputation. More seriously, the cloud maybe discard the client's data rarely accessed for saving the storage space [24].

Very recently, Yu et al. [25] have proposed a scheme for cloud storage auditing with verifiable outsourcing of key updates. The scheme involves three entities, the client, the cloud infrastructure and a third-party auditor (TPA). The client uploads his files to the cloud. The TPA audits the integrity of the files stored in the cloud and regularly updates the encrypted secret keys of the client to prevent any secret key exposition. Upon receiving the returned encrypted secret key, the client decrypts it to get the real secret key.

In this note we would like to stress that in Yu et al.'s scheme the recovered secret key is only used to generate authenticators for the files instead of protecting these files. No secret key associated to a symmetric key encryption is dedicated to the protection of the files. Besides, the scheme does not truly mitigate the client's computational burden for key updates. In view of these weaknesses, we would like to point out that Yu et al.'s scheme could not be practically implemented.

## 2 Review of Yu et al.'s Scheme

The scheme [25] uses the following notations.  $G_1, G_2$  are two multiplicative groups with some prime order  $q$ .  $g$  is a generator of  $G_1$ .  $\hat{e} : G_1 \times G_1 \rightarrow G_2$  is a bilinear pairing.  $H_1 : G_1 \rightarrow G_1, H_2 : \{0, 1\}^* \times G_1 \rightarrow \mathbb{Z}_q^*$  and  $H_3 : \{0, 1\}^* \times G_1 \rightarrow G_1$  are three cryptographic hash functions.  $T$  is the total periods number of the whole lifetime for the files stored in the cloud.  $w_1 \cdots w_t$  is the binary string of the node  $w^j$  associated with period  $j$ .  $w^j|_k (k \leq t)$  is the  $k$ -prefix of  $w^j$ .  $w^{j_0}, w^{j_1}$  are the left child node and the right child node of  $w^j$ , respectively.  $w^j|_{\bar{k}}$  is the sibling node of  $w^j|_k$ .  $PK$  is the public key which is unchanged in the whole lifetime.  $ES_{w^j}$  is the encrypted node secret key.  $R_{w^j}$  is the verification value which is used to verify the validity of authenticators.  $ESK_j$  is the client's encrypted secret key in period  $j$ .  $X_j$  is the set composed by the key pairs.  $\Omega_j$  is a set composed by the verification values.  $(ES, R)$  is the key pair of the root node.  $F$  is a file which the client wants to store in cloud.  $m_i (i = 1, \dots, n)$  are  $n$  blocks of file  $F$ .  $DK$  is the decryption key to recover the encrypted secret key for cloud storage auditing.

It involves three entities, some clients, a third-party auditor (TPA), and the cloud. The client has a secret key associated to a signature  $SSig$  for ensuring the integrity of not only the file identifier  $name$  but also the time period  $j$ . The protocol consists of the following phases:

**SysSetup:** Given a security parameter  $k$  and the total time period  $T$ , the client picks a generator  $u$  of  $G_1$ ,  $\rho, \tau \in \mathbb{Z}_q^*$  and computes  $R = g^\rho, G = g^\tau, ES = H_1(R)^{\rho-\tau}$ . Set  $PK = (R, G, u)$ . Set  $X_0 = \{(ES, R)\}, \Omega_0 = \emptyset$  (where  $\emptyset$  is null set),  $DK = \tau$  and keep it himself. The client sends  $ESK_0 = (X_0, \Omega_0)$  to the TPA.

**EkeyUpdate:** Input  $ESK_j$ , the time period  $j$ , and the public key  $PK$ . The TPA parses  $ESK_j = (X_j, \Omega_j)$  where  $X_j$  is organized as a stack which consists of  $(ES_{w^j}, R_{w^j})$  and the key pairs of the right siblings of the nodes on the path from the root to  $w^j$ . The top element of the stack is  $(ES_{w^j}, R_{w^j})$ . Firstly, pop  $(ES_{w^j}, R_{w^j})$  off the stack. Then do as follows:

- If  $w^j$  is an internal node ( $w^{j+1} = w^{j_0}$  in this case), select  $\rho_{w^{j_0}}, \rho_{w^{j_1}} \in \mathbb{Z}_q^*$ . And then compute  $R_{w^{j_0}} = g^{\rho_{w^{j_0}}}, R_{w^{j_1}} = g^{\rho_{w^{j_1}}}, h_{w^{j_0}} = H_2(w^{j_0}, R_{w^{j_0}}), h_{w^{j_1}} = H_2(w^{j_1}, R_{w^{j_1}}), ES_{w^{j_0}} = ES_{w^j} \cdot H_1(R)^{\rho_{w^{j_0}} h_{w^{j_0}}}, ES_{w^{j_1}} = ES_{w^j} \cdot H_1(R)^{\rho_{w^{j_1}} h_{w^{j_1}}}$ . Push  $(ES_{w^{j_1}}, R_{w^{j_1}})$  and  $(ES_{w^{j_0}}, R_{w^{j_0}})$  onto the stack orderly. Let  $X_{j+1}$  denote the current stack and define  $\Omega_{j+1} = \Omega_j \cup \{R_{w^{j_0}}\}$ .
- If  $w^j$  is a leaf, define  $X_{j+1}$  with the current stack. If  $w_t = 0$  (the node  $w_{j+1}$  is the right sibling node of  $w^j$  in this case), then set  $\Omega_{j+1} = \Omega_j \cup \{R_{w^{j+1}}\} - \{R_{w^j}\}$  ( $R_{w^{j+1}}$  can be read from the new top  $(ES_{w^{j+1}}, R_{w^{j+1}})$  of the stack). If

$w_t = 1$  ( $w^{j+1} = w''1$  in this case, where  $w''$  is the longest string such that  $w''0$  is a prefix of  $w^j$ ), then set  $\Omega_{j+1} = \Omega_j \cup \{R_{w^{j+1}}\} - \{R_{w''0}, R_{w''01}, \dots, R_{w''t}\}$  ( $R_{w^{j+1}}$  can be read from the new top  $(ES_{w^{j+1}}, R_{w^{j+1}})$  of the stack).

- Erase key pair  $(ES_{w^j}, R_{w^j})$ , and return  $ESK_{j+1} = (X_{j+1}, \Omega_{j+1})$ .

**VerESK:** Input a client's encrypted secret key  $ESK_j = (X_j, \Omega_j)$ , the current period  $j$  and the public key  $PK$ . The client checks that

$$\hat{e}(g, ES_{w^j}) = \hat{e}\left(R/G \cdot \prod_{m=1}^t R_{w^{j_1}}^{h_{w^{j_1}}}, H_1(R)\right),$$

where  $h_{w^j} = H_2(w^j, R_{w^j})$ .

**DecESK:** The client computes  $S_{w^j} = ES_{w^j} \cdot H_1(R)^\tau$ . The real secret key is set as  $SK_j = (X'_j, \Omega_j)$ , where  $X'_j$  is the same stack as  $X_j$  except that the top element in  $X'_j$  is  $(S_{w^j}, R_{w^j})$  instead of  $(ES_{w^j}, R_{w^j})$  in  $X_j$ .

**AuthGen:** For a file  $F = \{m_1, \dots, m_n\}$  and the current period  $j$ , the client proceeds as follows.

- Parse  $SK_j = (X'_j, \Omega_j)$  and read the top element  $(S_{w^j}, R_{w^j})$  from the stack  $X'_j$ . Select  $r \in \mathbb{Z}_q^*$  and compute  $U = g^r$ ,

$$\sigma_i = H_3(name || i || j, U)^r \cdot S_{w^j} \cdot u^{r m_i}$$

( $i = 1, \dots, n$ ), where the  $name$  is chosen randomly from  $\mathbb{Z}_q^*$  as the identifier of the file  $F$ . Generate a file tag for  $F$  and  $j$  using the signature  $SSig$  in order to ensure the integrity of  $name$  and  $j$ . Denote the set of authenticators in time period  $j$  with  $\Phi = (j, U, \{\sigma_i\}_{1 \leq i \leq n}, \Omega_j)$ .

- Send the file  $F$  and the set of authenticators along with the file tag to cloud.

**ProofGen:** Input a file  $F$ , a set of authenticators  $\Phi = (j, U, \{\sigma_i\}_{1 \leq i \leq n}, \Omega_j)$ , a time period  $j$ , a challenge  $Chal = \{(i, v_i)\}_{i \in I}$  (where  $I = \{s_1, \dots, s_c\}$  is a  $c$ -element subset of set  $[1, n]$  and  $v_i \in \mathbb{Z}_q$ ) and the public key  $PK$ . The cloud calculates an aggregated authenticator  $\Phi = (j, U, \sigma, \Omega_j)$ , where  $\sigma = \prod_{i \in I} \sigma_i^{v_i}$ . It also computes  $\mu = \sum_{i \in I} v_i m_i$ . It then sends  $P = (j, U, \sigma, \mu, \Omega_j)$  along with the file tag as the response proof of storage correctness to the TPA.

**ProofVerify:** Input a proof  $P$ , a challenge  $Chal$ , a time period  $j$  and the public key  $PK$ . The TPA parses  $\Omega_j = (R_{w^j|_1}, \dots, R_{w^j|_t})$ . He then verifies the integrity of  $name$  and  $j$  by checking the file tag. After that, the client verifies whether the following equation holds:

$$\hat{e}(g, \sigma) = \hat{e}\left(R \cdot \prod_{m=1}^t R_{w^j|_m}^{h_{w^j|_m}}, H_1(R)^{\sum_{i \in I} v_i} \cdot \hat{e}(U, u^\mu \cdot \prod_{i \in I} H_3(name || i || j, U)^{v_i})\right),$$

Table 1: Yu et al.'s outsourcing scheme

Client	TPA	Cloud
<p>–<i>SysSetup</i>. Set <math>PK = (R, G, u)</math>,  <math>X_0 = \{(ES, R)\}, \Omega_0 = \emptyset</math>.  <math>DK = \tau, ESK_0 = (X_0, \Omega_0)</math>.</p>	<p><math>\xrightarrow{ESK_0}</math> –EkeyUpdate. Update  <math>\xleftarrow{ESK_1}</math> it as <math>ESK_1 = (X_1, \Omega_1)</math>.  <math>\vdots</math>  <math>\xleftarrow{ESK_j}</math></p>	
<p>–<i>VerESK</i>. Check <math>\hat{e}(g, ES_{\omega^j}) \stackrel{?}{=} \hat{e}(R/G \cdot \prod_{m=1}^t R_{\omega_{j_1}^{h_{\omega^j_1}}}, H_1(R))</math>.</p>		
<p>–<i>DecESK</i>. Compute  <math>S_{\omega^j} = ES_{\omega^j} \cdot H_1(R)^\tau</math>,  <math>SK_j = (X'_j, \Omega_j)</math>.</p>		
<p>–<i>AuthGen</i>. For a file <math>F = \{m_1, \dots, m_n\}</math>, compute <math>U = g^r, \sigma_i = H_3(name\ i\ j, U)^r \cdot S_{\omega^j} \cdot u^{r m_i}</math>  <math>i = 1, \dots, n</math>. Generate <i>tag</i> for <math>F, j</math> using the signature <i>SSig</i>.  Set <math>\Phi = (j, U, \{\sigma_i\}_{1 \leq i \leq n}, \Omega_j)</math>.</p>	<p>upload <math>F, \Phi, tag</math></p>	<p>→ Store <math>F, \Phi, tag</math>.</p>
	<p>–<i>Challenge</i>. Set  <math>Chal = \{(i, v_i)\}_{i \in I}</math>.</p>	<p><math>\xrightarrow{Chal}</math> –<i>ProofGen</i>.  <math>\sigma = \prod_{i \in I} \sigma_i^{v_i}</math>,  <math>\mu = \sum_{i \in I} v_i m_i</math>.</p>
	<p>–<i>ProofVerify</i>. Verify the integrity of <i>name</i> and <math>j</math> by checking the <i>tag</i>.  Check <math>\hat{e}(g, \sigma) \stackrel{?}{=} \hat{e}(R \cdot \prod_{m=1}^t R_{\omega^j   m}^{h_{\omega^j   m}}, H_1(R)^{\sum_{i \in I} v_i} \cdot \hat{e}(U, u^\mu \cdot \prod_{i \in I} H_3(name\ i\ j, U)^{v_i}))</math></p>	<p><math>\xleftarrow{P}</math> <math>P = \{j, U, \sigma, \mu, \Omega_j\}</math>.</p>

where  $h_{\omega^j} = H_2(\omega^j, R_{\omega^j})$ . If it holds, returns “True”, otherwise returns “False”.

time period  $j$ , the client’s main computational task is to calculate

We refer to the following Table 1 for a brief description of Yu et al.’s scheme [25].

$$\begin{aligned}
 U &= g^r, S_{\omega^j} = ES_{\omega^j} \cdot H_1(R)^\tau, \\
 \sigma_i &= H_3(name\|i\|j, U)^r \cdot S_{\omega^j} \cdot u^{r m_i}, \\
 & \quad i = 1, \dots, n
 \end{aligned}$$

### 3 Analysis of Yu et al.’s Scheme

The scheme [25] aims to deal with the key exposure problem. They proposed the paradigm of cloud storage auditing which enables a client to outsource the burden of key updates to the third party auditor. But we find the scheme has two inherent flaws.

- 1) *The scheme does not truly mitigate the client’s computational burden for key updates.* Concretely, in the

$$\hat{e}(g, ES_{\omega^j}) \stackrel{?}{=} \hat{e}(R/G \cdot \prod_{m=1}^t R_{\omega_{j_1}^{h_{\omega^j_1}}}, H_1(R)).$$

while the TPA’s main computational task is to calculate

$$\begin{aligned}
 R_{\omega^{j_0}} &= g^{\rho_{\omega^{j_0}}}, ES_{\omega^{j_0}} = ES_{\omega^j} \cdot H_1(R)^{\rho_{\omega^{j_0}} h_{\omega^{j_0}}}, \\
 R_{\omega^{j_1}} &= g^{\rho_{\omega^{j_1}}}, ES_{\omega^{j_1}} = ES_{\omega^j} \cdot H_1(R)^{\rho_{\omega^{j_1}} h_{\omega^{j_1}}},
 \end{aligned}$$

$$\hat{e}(g, \sigma) \stackrel{?}{=} \hat{e} \left( R \cdot \prod_{m=1}^t R_{\omega^j|_m}^{h_{\omega^j|_m}}, H_1(R)^{\sum_{i \in I} v_i} \right) \cdot \hat{e} \left( U, u^\mu \cdot \prod_{i \in I} H_3(\text{name} \| i \| j, U)^{v_i} \right).$$

It is easy to find that the computational task for the client is almost equal to that for the TPA. That means the client's computational burden is not truly alleviated.

- 2) *The scheme does not ensure any confidentiality since the files uploaded by the client to the cloud are in fact not encrypted at all.* In the phase *AuthGen*, it is specified that the client has to parse the file  $F$  as  $\{m_1, \dots, m_n\}$  and generate the authenticator  $\Phi$  by invoking these  $m_i$ . The client then sends  $\{F, \Phi, \text{tag}\}$  to the cloud. Clearly, the authors have forgotten to assign a symmetric key encryption to protect the file  $F$ . In practice, it is conventional to encrypt files using any symmetric key encryption, such as AES. Due to computing overhead [18], a public key encryption is usually just used to establish the secure channel needed to exchange the secret key of a symmetric-key system.
- 3) We would like to stress that if the uploaded file  $F$  is viewed as an encrypted file, then the scheme has to assign three groups of secret keys,  $SK_1$  for encrypting the file  $F$ ,  $SK_2$  for generating the authenticator  $\Phi$  for  $F$ , and  $SK_3$  for signing *name* and the timestamp  $j$  (it specifies that "the client has held a secret key for a signature *SSig*, which is used to ensure the integrity not only of the file identifier *name* but also of the time period  $j$ "). Obviously, both  $SK_1$  and  $SK_3$  held by the client could also be exposed (as  $SK_2$ ), but the authors [25] have not realized the main danger. The proposed method only solves the problem of updating  $SK_2$ . Therefore, *the proposed scheme does not solve correctly the client's key exposure problem.*
- 4) We think it seems impossible to revise the scheme such that it could simultaneously update the involved secret keys  $SK_1, SK_2$  and  $SK_3$ , because the client has to retrieve the file  $F$  stored previously on the cloud in order to update the symmetric key  $SK_1$ . In such case, it is totally unnecessary to introduce the key  $SK_2$  for generating the authenticator  $\Phi$  for the file  $F$ . Frankly speaking, this is an inherent flaw in the proposed model by Yu et al.

## 4 Conclusion

We show that there are two flaws in Yu et al.'s scheme for cloud storage auditing with verifiable outsourcing of key updates, and remark that the scheme cannot be practically implemented. We would like to stress that the proposed paradigm is somewhat artificial because the client is able to update his secret keys solely by himself.

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## Biography

**Zhengjun Cao** is an associate professor with the Department of Mathematics at Shanghai University. He received his Ph.D. degree in applied mathematics from Academy of Mathematics and Systems Science, Chinese Academy of Sciences. His research interests include applied cryptography, discrete algorithms and quantum computation.

**Lihua Liu** is an associate professor with the Department of Mathematics at Shanghai Maritime University. She received her Ph.D. degree in applied mathematics from Shanghai Jiao Tong University. Her research interests include combinatorics and cryptography.

**Olivier Markowitch** is an associate professor with the Computer Sciences Department at the Universite Libre de Bruxelles. He is also information security advisor of his University. He is working on the design and analysis of two-party and multi-party cryptographic protocols as well as on the design and analysis of digital signature schemes.