Monitoring Piecewise Continuous Behaviors by Refining Semi-Quantitative Trackers

Bernhard Rinner Institute for Technical Informatics Technical University Graz A-8010 Graz, AUSTRIA b.rinnerOcomputer.org

Abstract

We present a model-based monitoring method for dynamic systems that exhibit both discrete and continuous behaviors. MIMIC [Dvorak and Kuipers, 1991] uses qualitative and semiquantitative models to monitor dynamic systems even with incomplete knowledge. Recent advances have improved the quality of semi-quantitative behavior predictions, used observations to refine static envelopes around monotonic functions, and provided a semiquantitative system identification method. Using these, we reformulate and extend MIMIC to handle discontinuous changes between models. Each hypothesis being monitored is embodied as a tracker, which uses the observation stream to refine its behavioral predictions, its underlying model, and the time uncertainty of any discontinuous transitions.

keywords: model-based monitoring; model refinement, hybrid systems

1 Introduction

Benjamin Kuipers Department of Computer Sciences University of Texas at Austin Austin, TX 78712, U.S.A. kuipers@cs.utexas.edu

and coverage exactly when it is most important for the monitoring system to consider all possible scenarios.

The MIMIC framework [Dvorak and Kuipers, 1991] addresses this need, first by using qualitative and semiquantitative (SQ) models in the QSIM representation [Kuipers, 1994] to express incomplete knowledge with a guarantee that all possible real-valued behaviors are covered; and second, by tracking multiple qualitativelydistinct hypotheses in parallel. SQSIM [Kay, 1998] extends the semi-quantitative inference power of QSIM by deriving and reasoning with dynamic envelopes guaranteed to bound the real behaviors consistent with an SQ model SQUID [Kay, 1996; Kay *et a*/., 1999] is a semi-quantitative system identification method based on SQSIM that assimilates a set of observations to an SQ model over a single continuous mode.

Time uncertainty at a mode transition has a particularly explosive effect on the uncertainty of predictions from the SQ model after the transition. Therefore, we focus our attention first on getting the most out of SQUIDbased tracking of a continuous mode hypothesis, and second, on detecting the mode transition and refining its time uncertainty. In our approach, the monitoring system starts with a coarse description of the physical system and uses the observation stream to refine the behavior prediction, its underlying model, and the time uncertainty of any discontinuous transition. After presenting the details of our extension and reformulation of MIMIC, we present a non-trivial example and discuss related work.

Physical systems are by nature continuous. However, it is natural to simplify models by abstracting isolated regions of rapid change to instantaneous discontinuities separating regions of continuous behavior [lwasaki *et a*/., 1995; Nishida and Doshita, 1987]. Systems which exhibit both continuous and discrete behaviors are called *hybrid systems*, where a continuous segment of the system's behavior is called a *mode of operation* and a discontinuous change is called a *transition* between modes.

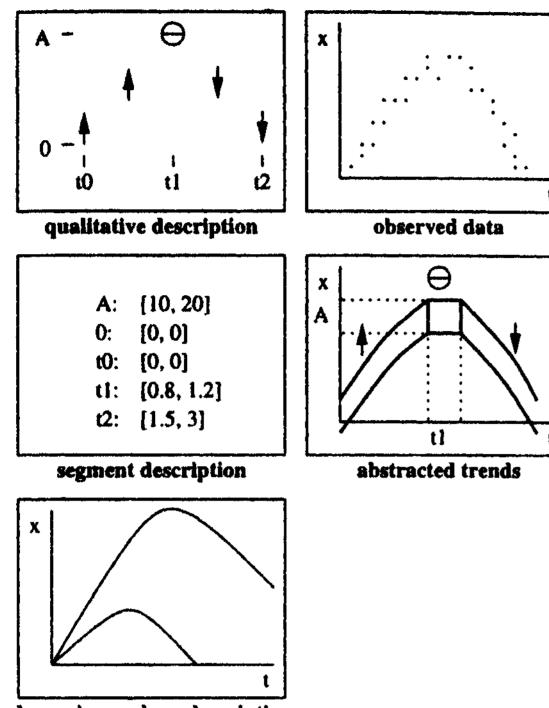
Model-based monitoring relies on a comparison between the predicted behavior of a model and the observed behavior of a physical system. Traditional monitoring approaches typically use a single precise model of the physical system. However, even if the system is behaving properly, precise parameter values and functional relationships are often not known. More importantly, monitoring systems are designed to detect unexpected events or faults, after which knowledge of the system is by definition incomplete. A reliance on precise models leads to overly-specific predictions, sacrificing accuracy

2 Tracking Piecewise Continuous Behaviors

A *tracker* embodies a continuous mode hypothesis and confirms or refutes the hypothesis by unifying its predictions with the observed behavior. When the observations provide sufficient new information, the tracker may be able to refine the imprecision in the underlying model, and thus make more precise predictions in the future.

2.1 SQ System Identification

A tracker is based on SQUID [Kay *et a*/., 1999], which refines an imprecise model (SQDE) by a process called



dynamic envelope description

Figure 1: Trend matching compares the prediction and the observation corresponding to the level of detail in the behavior prediction derived by SQSIM (qualitative, segment and dynamic envelope description). Trends describe the observed data at the same levels.

trend matching. Imprecision in the SQDE is represented by numerical intervals bounding possible values of unknown parameters, and by static envelopes - functions bounding the possible graphs of unknown monotonic functions.

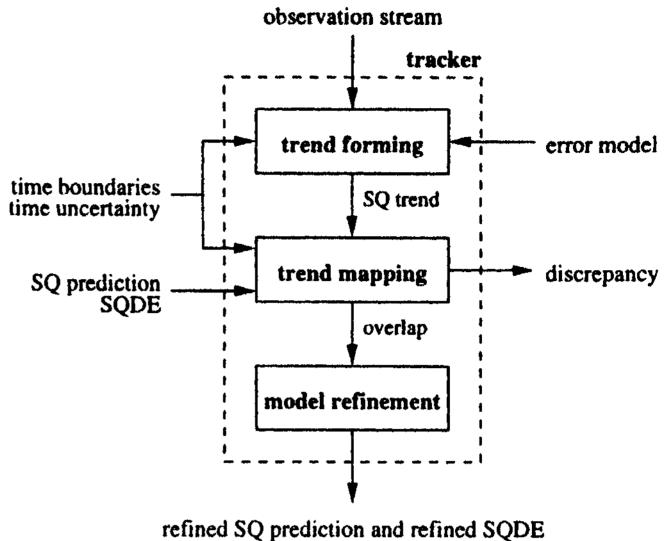


Figure 2: Tracker architecture.

2.2 Tracker Architecture

Figure 2 presents the architecture of a tracker. The tracker is initialized with the SQ prediction and the underlying SQDE of the current mode. Information about the time boundary and the time uncertainty of the current mode may be given. The tracker consumes an observation stream and it either produces a refined SQ prediction and SQDE, or detects a discrepancy between the observation and the prediction. The observation stream is a sequence of samples: numeric values for variables at specified times derived by possibly noisy sensors. Samples do not necessarily appear at a constant rate, and need not be synchronized across variables.

Trend forming generates an SQ trend describing each variable in the observation stream by breaking the samples into monotonic segments [Kay et o/., 1999]. The segments are determined by computing the slope of a linear least-squares fit to the data within a sliding window over the samples. Dynamic envelope descriptions for the t and I segments are generated by MSQUID, a neural network-based estimator for monotonic functions [Kay and Ungar, 1993; 1999], out to any given confidence bound. Each 8 segment is described by the segment's time interval and the minimum and maximum sample values over that interval. The goal is to detect the qualitative dynamics of the underlying signal in the noisy observation. In the current implementation it is assumed that Gaussian noise of fixed mean and variance is superimposed on the "pure" signal. Each observed variable has an error model that specifies bounds on mean and variance for noise. Trend mapping compares the SQ trend derived from the observations with the SQ prediction by stepping through both sequences. If an inconsistency is detected between the trend and the prediction, the current hypothesis is refuted, so the mapping process and the current tracker are aborted.

Trend matching compares semi-quantitative trajectory descriptions derived by SQSIM (the SQ prediction) and the corresponding properties of the observations (the SQ trend). To refine the underlying model, portions of the model space which cannot plausibly generate the observations are excluded.

There are three levels of abstracted properties of the trajectories, corresponding to the level of detail derived by the components of SQSIM: qualitative (QSIM), seqment (Q2), and dynamic envelope (NSIM) descriptions (Figure 1). The qualitative description is defined by a sequence of symbols $(\downarrow, \ominus \text{ and } \uparrow)$ representing the derivative's sign (qdir) of the trajectory at time points and intervals between time points. The segment description specifies intervals bounding the trajectory at particular time points, i.e., magnitude and time ranges. The dynamic envelope description bounds the trajectory by a lower and an upper envelope. A trend represents the abstracted properties of the observed data (Figure 1), i.e., symbols representing the qdir, bounding intervals on extrema and bounding envelopes for monotonic segments.

- Qualitative mapping generates a correspondence between the qdirs in the SQ prediction and the SQ trend. A successful correspondence may fail to be one-to-one because (i) the samples in the observation stream may end before some of the qualitative changes in the SQ prediction take place; (ii) the SQ prediction terminates with a mode change before the end of the current SQ trend, leaving data to correspond to the next mode; or (iii) the SQ prediction may include small qdir changes which are not detectable in a noisy observation stream.
- Segment mapping ensures consistency of corresponding behavior segments in the SQ trend and the SQ prediction, in the sense that their time and magnitude bounds overlap. Consistency of segments is checked by asserting the segment bounds of the SQ trend to the corresponding segments of the SQ prediction and propagating these bounds to the other variables in the SQDE using Q2's interval propagation [Kuipers, 1994].
- *Dynamic envelope mapping* ensures consistency by intersecting the dynamic envelopes for corresponding monotonic segments of the trend and the prediction.

Model refinement takes place when trend mapping decreases the bounds on some variables in the SQDE. Parameter imprecision is refined by using Q2 to derive bounds on independent variables from dependent ones. Q2 propagates intervals across model variables at time points and uses the (weak) Mean Value Theorem to propagate those bounds over time intervals. The dynamic envelopes in the SQ trend provide more information than just magnitude and time bounds over monotonic segments. Model refinement exploits this information by introducing several instantaneous "snapshots" over the monotonic trend segments and propagating the smaller magnitude bounds at these time instants to other model variables. The number of "snapshots" affects the achieved refinement and is specified by the user. Functional imprecision is refined by excluding portions from the static envelopes that are inconsistent with the (refined) variable bounds. The trend matching techniques guarantee that portions of the model space are ruled out only when they are inconsistent with the observations [Kay et al, 1999]. If a mode change is manifested by a discontinuous change of an observed variable or a sudden sign change of its slope, the change becomes explicit in the purely qualitative trend, and is easy to detect. Otherwise, segment and dynamic envelope trend mapping should eventually refute the current model, but excessive imprecision in the model and uncertainty in the data could prevent the change from being recognized. Once a mode change has been detected, the tracker for the next mode is initialized with the variable values at the transition point. The new tracker attempts to create a mapping between its SQ prediction and the remaining segments of the observed trend. Time uncertainty in the mode change affects the current tracker and more

dramatically the following tracker, in an important way.

3 Refining the Time Uncertainty of Discontinuous Changes

We assume that there are three possible causes for discontinuous changes in the model of a complex system: (i) the autonomous operation of the plant moves from one operating mode to another; (ii) the plant operator takes a known action; and (iii) an unexpected and externally caused event such as a failure takes place. In the first two cases, the current and following modes are known. In the third case, we assume that a separate diagnosis engine proposes a set of fault hypotheses, which MIMIC tracks in parallel.

A discontinuous change happens in an instant. Unfortunately, with imprecise models and noisy and finitely sampled observations, we may never be able to determine the precise instant when the change takes place. The best we can do is determine time bounds on the instant when the change occurred.

For matching a piecewise continuous model to a stream of observations, it is particularly important to make the time bounds on discontinuous changes as precise as possible. Time uncertainty on a mode change affects the entire correspondence between prediction and observation in the following mode, resulting in propagating uncertainty. Figure 6(c) shows how weak time bounds on a discontinuous change can result in extremely weak bounds on the prediction of the following mode. Therefore, we focus on improving these time bounds.

3.1 Intersecting Trend and Prediction

We focus here on refining time uncertainty of a mode change based on the intersection of SQ trend and SQ prediction. After semi-quantitative reasoning has provided bounds on the transition time, advanced filtering techniques based on statistical or digital signal processing may be applicable.

When there is time uncertainty, the mapping between the SQ trend and the SQ prediction is not fixed. The SQ prediction can be shifted relative to the SQ trend by any offset within the range of the time uncertainty.

However, a mapping is only valid if the SQ trend segment and the SQ prediction segment have a non-empty intersection for every time-point *t* in the SQ trend. This is exploited to derive refined bounds on the time uncertainty of discontinuous changes (Figure 3).

For | segments, the mapping is valid as long as (i) the upper envelope of the trend is above the lower envelope of the prediction and (ii) the lower envelope of the trend is below the upper envelope of the prediction. More formally, we can determine the lower bound t_{cmin} and the upper bound t_{cmax} , respectively, as follows:

$$t_{cmin} = min\{t_s : \forall t, \overline{x_{tr}}(t) \ge \underline{x_{pr}}(t-t_s)\}$$

$$t_{cmax} = max\{t_s : \forall t, \underline{x_{tr}}(t) \le \overline{x_{pr}}(t-t_s)\}$$

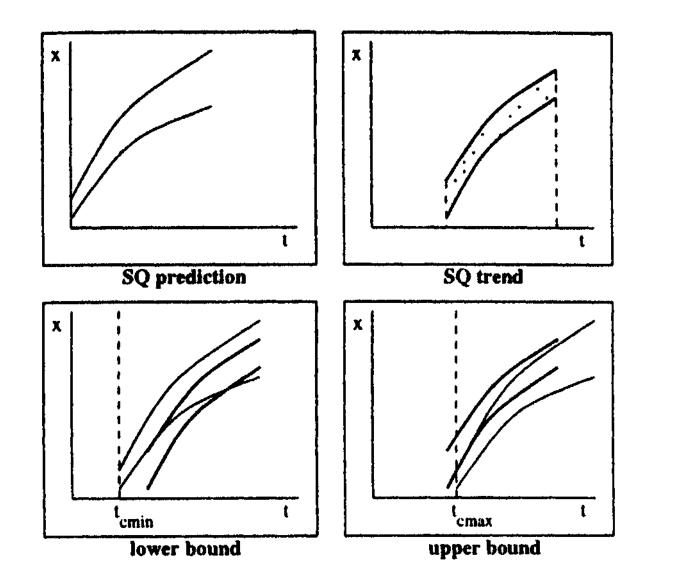


Figure 3: Deriving bounds on the time uncertainty by intersecting the SQ prediction and the SQ trend.

where $x_{tr}(t)$ is the observed trend x(t), $x_{pr}(t - t_s)$ s the prediction, shifted by t_s , Over- and under-bars represent the upper and lower dynamic envelopes, respectively. Similar conditions hold for \downarrow and \ominus segments.

This intersection process is applied to all segments of the mode. Improvements in time uncertainty propagate from segment to segment by interval arithmetic and intersection of bounding intervals.

3.2 Incremental Refinement

When there is a great deal of time uncertainty about the transition from one mode to another, many samples in the observation stream fall within the uncertainty interval, and thus cannot be unambiguously assigned to one of the adjacent segments of monotonic change. After time uncertainty is decreased, some samples can now be assigned to a definite adjacent segment. The additional information helps refine the mode the segment belongs to, and its underlying model. Improvements to the adjacent modes can, in turn, lead to further decreases in time uncertainty of the transition. And so on until no further improvement results. The algorithm for incremental refinement of the time uncertainty between two adjacent modes *i* and *j* is presented in Figure 4. The trend/prediction intersection (line 7) is performed for each behavior in the succeeding mode. If the trend is inconsistent with the behavior at the qualitative level or no valid mapping can be found for any time offset within the time uncertainty the behavior is refuted (line 9). Since each behavior is independently intersected with the trend this method results in different refinements on the uncertainty interval for each behavior of the succeeding mode.

```
refine-transition(t<sub>u</sub>, mode,-, mode<sub>i</sub>, SQtrend)
 1
2
      behs <- generate-behaviors(modej)
3
      for each behavior beh in behs do
4
        t < t_u
 5
        repeat
6
          refine 4- false
 7
          t<sub>n</sub> <- intersect(beh, SQtrend)
8
          if (t_n = 0) then
9
            refute beh
          elseif (t_n < t) then
10
11
            t < t_n
12
            refine <~ true
13
            re-assign samples to mode and mode,
14
            re-track mode,
15
            inherit refinements from mode to beh
          endif
16
        until not (refine)
17
```

```
18 endfor
```

Figure 4: Incremental refinement of the initial time uncertainty t_u between mode and mode_j.

4 Overall Monitoring System

The overall monitoring system tracks multiple hypotheses in parallel. The hypotheses may represent different nominal or fault models of the plant, or they may represent different qualitative behaviors predicted from semiquantitative simulation of a particular model.

A particular hypothesis is a sequence of mode hypotheses $[H_1(t_0, t_1); H_2(t_1, t_2); \cdots; H_n(t_{n-1}, t_n)]$. The monitoring system alternates between tracking a particular mode hypothesis $H_i(t_{i-1}, t_i)$ and refining the time uncertainty of the mode transition at t_i . Several trackers and their hypotheses may be refined in parallel (Figure 5). The achieved refinements (SQ prediction and SQDE) are passed to the tracker manager which instantiates new trackers and refines the time uncertainty of the

mode transition. As discussed in Section 3, we assume that the models for new modes are known. Information from the observation stream, such as the satisfaction of a condition that autonomously moves the system to another mode or a signal indicating an operator action, allows the tracker manager to choose the model(s) for the new mode. Fault models may also be proposed at any time by a separate diagnosis engine.

Model refinements such as improved variable bounds or static envelopes may be inherited from one model H_i to the next H_{i+1} across a mode transition. In the current implementation, the user specifies the variables and functional relations whose refinements can be inherited.

The degree of model precision is important for the fault detection performance of our monitoring system. However, with imprecise models, uncertain observation and limited observability we may never be able to detect all faults or distinguish between every possible hypothesis. In order to achieve a sufficiently precise prediction for fault detection, (i) our initial knowledge about the

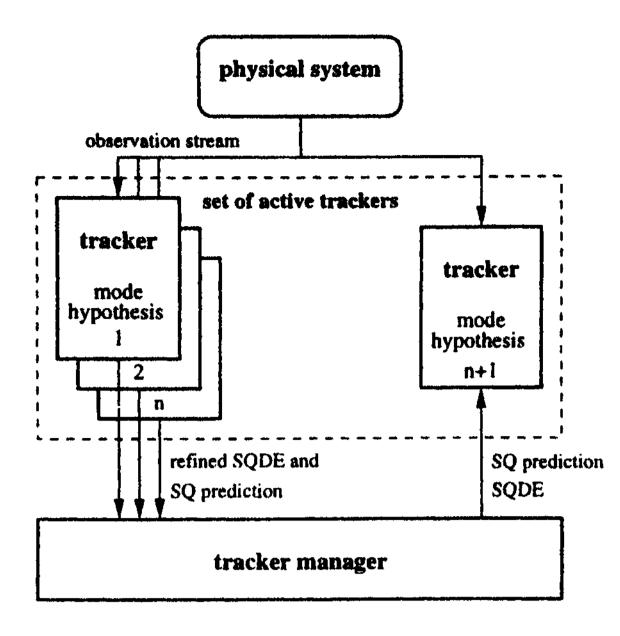


Figure 5: Overall monitoring system.

system must be precise enough or (ii) we must collect enough data from the "healthy" physical system to refine its model to the required degree of precision.

5 Experimental Results

We demonstrate the refinement capabilities of our monitoring system using a two tank system. In this example (Figure 6(a)), we start with a filled upper tank and an empty lower tank; the drains of both tanks are open and the upper tank is filled at a constant inflow rate. When the amount in the upper tank drops below a limit the inflow rate is increased. This scenario is modeled as a transition between two operating modes (Figure 6(b)). Only imprecise information is known about this scenario, i.e., intervals for variables and bounding envelopes for functional relations. Since both tanks remain unchanged, the refinements of the variables o and b as well as of the functional relations / and g are inherited from the first to the second mode. SQSIM predicts 9 different behaviors for the two tank scenario; 5 of them include the region transition. Only one is consistent with the SQ trend; the other trackers are refuted. Figure 6(c) shows the predicted dynamic envelopes for the amount in the lower tank for the surviving prediction. SQSIM predicts the time of the mode transition as [1.68, in/].

obs. vars.	a(t)	b(t)	f	g	tc
none	1	1	1	1	[1.68, inf]
Ь	1	0.53	1	1	2.70, 4.20
a, b	0.29	0.22	0.68	1	3.73, 4.14
a,b,ofa,ofb	0.26	0.18	0.28	0.40	3.78, 4.14

Table 1: Achieved refinements dependent on the observed variables including noise with $\mu = 0$ and var = 1.

obs. vars.	a(t)	b(t)	5	9	t _c
5	1	0.70	1		[2.50, 4.25]
a, b	0.64	0.56	0.96	1	2.87, 4.25
a,b,ofa,ofb	0.61	0.47	0.57	0.58	2.98, 4.25

Table 2: Achieved refinements dependent on the observed variables including noise with $\mu = 0$ and var = 2.

constructs the bounding envelopes around the observations to achieve a certainty of 95%. This figure also presents the final refinement achieved by the monitoring system. The dynamic envelopes for- b are refined to 18% of their initial area and the time uncertainty is refined to [3.78,4.14] after two iterations of the refinement algorithm¹. Observations for a, 6, *of a* and of b, with noise $\mu = 0$ and *var* = 1, are used in this case. Note the propagation of refinements through the SQDE, i.e., the dynamic envelopes in the first segment are narrower than the bounding envelopes of the observation of 6. Due to time uncertainty, the dynamic envelopes in the second mode are wider than the bounding envelopes of the observation.

The effect of observability is shown in Table 1. This table presents the achieved refinements dependent on the observed variables. The degree of refinement is defined by the ratio of the predicted and refined areas for variables and functional relations. For the variables *a* and 6, the area is specified by the dynamic envelopes over the observation time. For the functional relations / and *g*, the area is specified by the bounding functions (static envelopes) over the range of / and *g*. The achieved refinement of the time uncertainty is represented by *t_c*. As the number of observed variables increases the refinement improves and extends to more variables and functional relations. Table 2 presents the reduced refinements caused by an increase of noise in the observation.

The observations are generated by numeric simulation of an ODE, adding Gaussian noise with fixed mean and variance to the samples. The exact model for deriving the samples is given as $a' = ifa - 9\sqrt{a}$, $b' = 9\sqrt{a} - 8\sqrt{b}$ with $a(t_0) = 95$, $b(t_0) = 0$, c = 9 and an inflow rate *if* a = 25 before and *if* a = 60 after the transition. The samples are generated at a rate of 20 Hz.

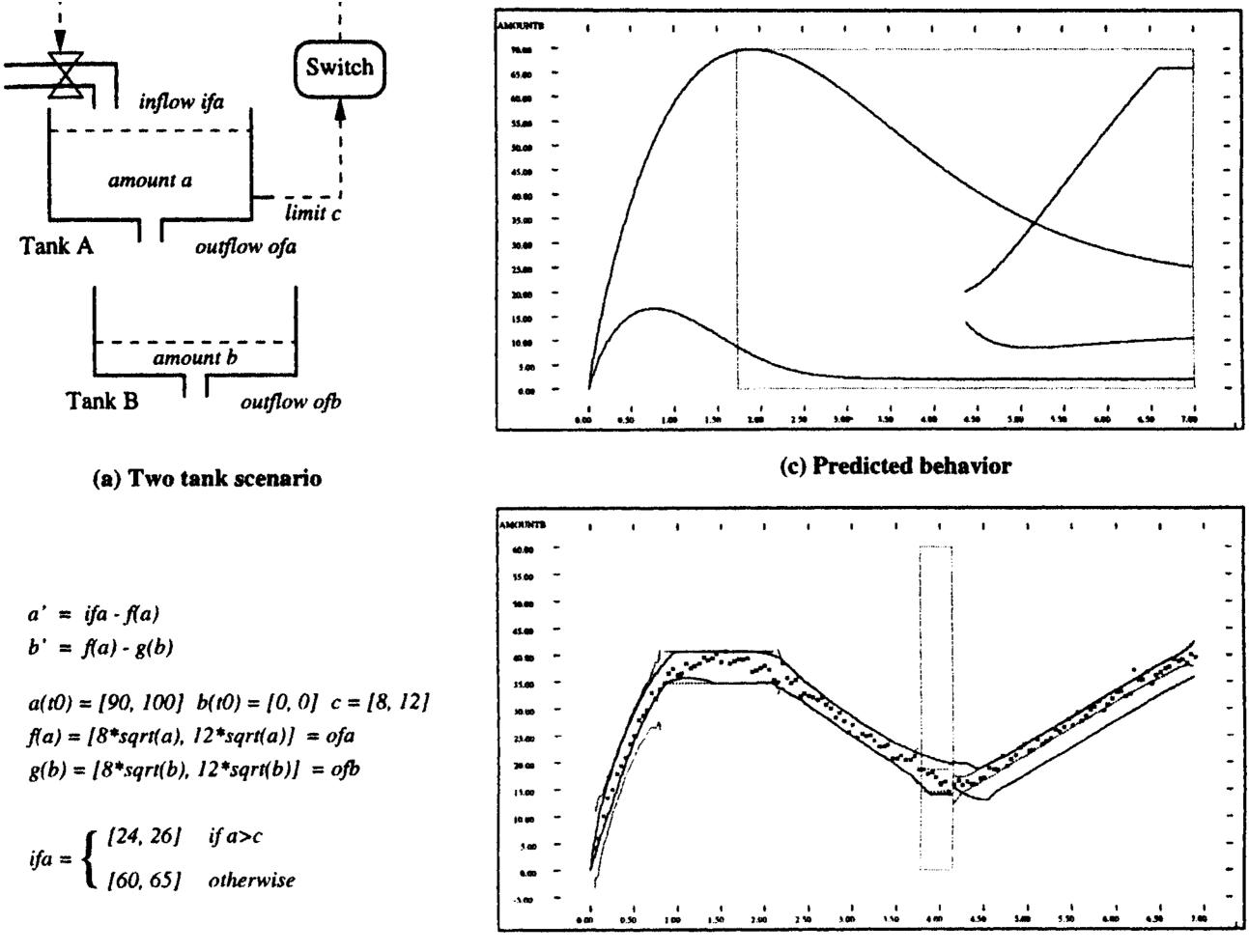
Figure 6(d) shows the samples and bounding envelopes derived by trend forming for the variable 6. MSQUID

6 Conclusion

We have presented a method for monitoring dynamic systems that exhibit both discrete and continuous behaviors. The monitoring system refines the behavior prediction, the underlying model and the time uncertainty of discontinuous changes. The hypothesis is refuted and pruned from the tracking set when refinement eliminates all possible values for any parameter.

Trend matching uses a statistical best fit to observed

¹In our experiments incremental refinement never required more than 3 iterations; it usually stopped after 1 or 2.



(b) Imprecise model with mode transition

(d) Refined behavior and time uncertainty

Figure 6: A two tank scenario (a), modeled as an autonomous mode transition (b), its prediction (c) of the upper and lower bounds (dynamic envelopes) for b, and the refined bounds and time uncertainty (d). In both graphs, the solid lines represent the predicted or refined dynamic envelopes. The dotted box represents the time uncertainty of the mode change; the dashed lines represent the bounding envelopes of the observations (d). Due to the time uncertainty of the discontinuous change the prediction of the second mode can start at any time within the dashed box. For the sake of readability, they start in the middle (c) and at the right end (d) of the dashed box, respectively.

data, plus bounding envelopes out to any desired confidence bound. Portions of the model space are removed only when they are inconsistent with these bounds. This gives a good (and adjustable) compromise between aggressiveness and robustness in handling noise and uninformative data.

Related work has been done by [Mosterman *et al.*, 1998]. In their framework for model-based diagnosis the physical system is modeled by a temporal causal graph. Qualitative candidate models are derived from this representation and parameter estimation techniques are applied to fit the candidate models to the observation. TrenDx [Haimowitz and Kohane, 1993] is a monitoring system which uses a semi-quantitative representation of a behavior and attempts to fit data to this behavior representation. Since TrenDx uses pre-

defined behavior templates no refinement can be performed. PRET [Bradley and Stolle, 1996] automatically constructs a precise ODE model of a physical system. PRET focuses on system identification and not on monitoring. Loiez and Taillibert [Loiez and Taillibert, 1997] use piecewise polynomial functions, so-called temporal band sequences, to bound the observation stream. The behavior of components in analog circuits is modeled by sums of temporal functions including derivatives of any order. This approach is only able to detect discrepancies but not to predict the behavior of the system. McIlraith et al. [McIlraith et a/., 1999] present an approach for diagnosing hybrid systems where all mode transitions, i.e., the history of executed actions, are known. Candidate generation and model estimation are based on the model-based diagnosis framework of [Mosterman et a/., 1998] and the tracker framework is adopted to refine multiple candidates.

Furthermore, our monitoring method is directly applicable to fault diagnosis in dynamic systems. Fault hypotheses can be proposed for monitoring based on initial weak information such as the signs of discrepancies between observations and predictions, by using existing methods such as [de Kleer and Williams, 1987; Ng, 1991]. Automatic model-building methods can select relevant model-fragments from a background knowledge base to express initially weak knowledge about a fault as an SQDE [Crawford *et al*, 1990; Rickel and Porter, 1994]. The observation stream is then used to refine or refute each proposed model.

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