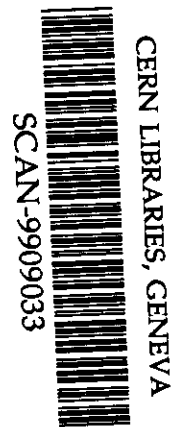
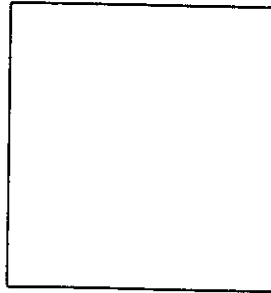


B_d^0 MIXING AND CP VIOLATION MEASUREMENTS AT THE TEVATRON

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We present six time-dependent B_d^0 mixing measurements of Δm_d from the CDF Run I data. The CDF average is $\Delta m_d = .494_{\pm .026}^{+ .026} (\text{ps})^{-1}$. We also present a measurement of the CP-violating asymmetry $\sin(2\beta)$ using a sample of $B^0/\bar{B}^0 \rightarrow J/\psi K_s^0$ decays and report $\sin(2\beta) = .79_{- .44}^{+ .41}$.

1 Introduction

In the context of the standard model, the mixing of $B_d^0 \leftrightarrow \bar{B}_d^0$ occurs through the charge current coupling between quarks. This can be described in the context of the Cabibbo-Kobayashi-Maskawa (CKM)¹ matrix which transforms the flavor eigenstates of the quarks into their mass eigenstates. The CKM rotation matrix can be completely determined from three angles and a phase. It is useful to write it in the Wolfenstein² parameterization as:

$$V_{CKM} \equiv \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} 1 - \frac{\lambda^2}{2} & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{\lambda^2}{2} & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + O(\lambda^4)$$

where $\lambda = \sin(\theta_C)$ and the three other parameters A , ρ , and η can be described by the remaining two weak rotation angles and the complex phase that introduces CP violation. Unitarity of the CKM matrix can be represented graphically as a triangle in the complex plane. The base of this triangle is scaled to unit length by $A\lambda^3$. This leaves three angles α , β , and γ and two sides which may be measured. $B_d^0 \leftrightarrow \bar{B}_d^0$ mixing constrains the element V_{td} which contributes to one of the triangle sides, while CP violation in the decay $B^0/\bar{B}^0 \rightarrow J/\psi K_s^0$ determines the angle β .

1.1 $B_d^0 \leftrightarrow \bar{B}_d^0$ Mixing

A neutral B_d^0 meson can oscillate into its anti-particle state, \bar{B}_d^0 through second-order weak processes with a probability equal to:

$$\mathcal{P}(B_d^0(t_0) \rightarrow \bar{B}_d^0(t)) = \frac{e^{-t/\tau_B}}{2\tau_B} (1 - \cos(\Delta m_d t)), \quad (1)$$

where Δm_d is the frequency of the oscillation and is equal to the mass difference ($\Delta m_d = m_H - m_L$) between the heavy and light mass eigenstates, τ_B is the mean lifetime of the two mass eigenstates, and t is the proper decay time of the B_d^0 in its rest frame. The asymmetry between the mixed and unmixed state is

$$\mathcal{A} = \frac{P(B_d^0 \rightarrow B_d^0) - P(B_d^0 \rightarrow \bar{B}_d^0)}{P(B_d^0 \rightarrow B_d^0) + P(B_d^0 \rightarrow \bar{B}_d^0)} = \cos(\Delta m_d t) \quad (2)$$

To measure the time-dependent mixing asymmetry, we need three measurements: (1) the flavor of the B at production, (2) the flavor of the B at decay, and (3) the proper decay time. At CDF, measuring (2) and (3) are relatively easy. The flavor is known by the B reconstruction, and the proper time is measured using the CDF silicon vertex detector (SVX) with a 2-D $\tau\phi$ resolution of $\sigma_d \approx (13 + 40/p_T)\mu m$. We use three algorithms for determining the B flavor at production. The soft lepton tagging (SLT) algorithm identifies the flavor of the opposite B through its decay to a lepton. The jet charge tagging algorithm (JetQ) uses a momentum-weighted charge average of particles in a b quark jet to infer the charge of the b quark. These two tagging algorithms are referred to as opposite side taggers (OST) since the production flavor is determined by the B opposite the B candidate of interest. The same side tagging algorithm (SST) uses charged tracks surrounding the B to determine its flavor. The effectiveness of a tagging algorithm is characterized by the efficiency, ϵ , which is the fraction of events that can be tagged and the dilution, D , which dilutes the asymmetry due to an imperfect detector, mistags, etc. The statistical accuracy of a sample of tagged events is proportional to $N\epsilon D^2$ where N is the number of events. Figure 1 shows six CDF B_d^0 -oscillation measurements of Δm_d , and the combined average. These measurements exploit all three of the tagging algorithms.

1.2 CP-Violation

To measure CP-violation, we use the CP eigenstate $B_d^0/\bar{B}_d^0 \rightarrow J/\psi K_s^0$. For the CP-asymmetry to be non-zero, the imaginary phase between the two decay paths leads to a difference in the decay rate. The CP asymmetry is described by

$$\mathcal{A}(t) = \frac{P(\bar{B}_d^0 \rightarrow J/\psi K_s^0) - P(B_d^0 \rightarrow J/\psi K_s^0)}{P(\bar{B}_d^0 \rightarrow J/\psi K_s^0) + P(B_d^0 \rightarrow J/\psi K_s^0)} = \sin(2\beta) \sin(\Delta m_d t) \quad (3)$$

The first measurements of $\sin(2\beta)$ were published by CDF³ and OPAL⁴ in 1998. OPAL measured $\sin(2\beta) = 3.2_{-2.0}^{+1.8} \pm 0.5$ using $J/\psi K_s^0$ events. CDF used a sample of ≈ 200 $J/\psi K_s^0$ events to measure $\sin(2\beta) = 1.8 \pm 1.1 \pm 0.3$. The CDF events required the J/ψ to be reconstructed in the SVX and used only one tagging method to identify the B at production.

In the present update, we have expanded the earlier result to include ≈ 200 additional events in which the J/ψ is reconstructed in the central tracker (CTC) thus having large uncertainty on the decay time. We have also allowed for multiple taggers for each event. To measure the time-dependent CP asymmetry, we measure the proper decay time and tag the flavor of the B at production. Each event can be tagged with either a SST, an OST or both. When multiple taggers are combined the effective dilution (D) is:

$$D_{eff} = \frac{D_{OST} \pm D_{SST}}{1 \pm D_{OST} D_{SST}} \quad (4)$$

Table 1: Efficiencies and Dilutions of tagging algorithms used for determining the flavor of $B_d^0/\bar{B}_d^0 \rightarrow J/\psi K_s^0$

Tag	Efficiency (%)	Dilution (%)
SST _{svz}	35.5 ± 3.7	16.6 ± 2.2
SST _{non}	38.1 ± 3.9	17.4 ± 3.6
SLT	5.6 ± 1.8	62.5 ± 14.6
JetQ	40.2 ± 3.9	23.5 ± 6.9
Combined	$\epsilon D^2 = 6.3 \pm 1.7$	

To calibrate the OST algorithms, we use the $B^\pm \rightarrow J/\psi K^\pm$ events which have similar kinematics to the $J/\psi K_s^0$ signal sample and have a known flavor. For the dilution of the SST, we use the result from our previous measurement of $\sin(2\beta)$ ³. Table 1 list the efficiencies and dilutions for the different tagging algorithms.

The tagged $J/\psi K_s^0$ events are fit using a negative log-likelihood function. The fit is described by the signal events, the prompt background and the long-lived background. Each component is broken down into a piece with precision lifetime information and a piece with less precise lifetime information. The probability function includes terms for lifetime, normalized mass (M_N) and the tagging efficiency functions. Background asymmetries are constrained by events far from the signal peak at $M_N = 0$, and detector asymmetries are accounted for in the fit using a large inclusive J/ψ sample.

The result for $\sin(2\beta)$ is shown in Figure 2a including systematic errors due to the dilutions, Δm_d , τ_{B^0} , and m_{B^0} . The left side of the figure shows the asymmetry versus lifetime using the precision lifetime sample. The solid curve shows the full likelihood fit with Δm_d fixed to the world average and the dashed curve shows the fit with Δm_d floating. The one data point on the right side of the figure is the value of $\sin 2\beta$ obtained from the CTC sample with low lifetime resolution. This result corresponds to a Feldman-Cousins frequentist limit of $0.0 < \sin(2\beta) < 1$ at 93% CL. Figure 2b shows the CDF result compared to indirect results in the $\rho - \eta$ plane⁵. The dotted lines correspond to the central values of β from $\sin(2\beta) = .79$. The solid lines represent the 1σ regions. The oval shaped region shows the 1σ and 2σ intervals from indirect measurements of the CKM parameters⁵.

2 Conclusion

We present six measurements of the mixing parameter Δm_d from the CDF Run I data and measure $\Delta m_d = .494_{\pm 0.026}^{\pm 0.026}(\text{ps}^{-1})$. Using the tagging algorithms developed for these mixing measurements, we measure the CP-violating asymmetry $\sin(2\beta)$ with a sample of $B^0/\bar{B}^0 \rightarrow J/\psi K_s^0$ decays. We report $\sin(2\beta) = .79_{-.44}^{+.41}$ which corresponds to a Feldman-Cousins frequentist limit of $0 < \sin(2\beta) < 1$ at 93% CL.

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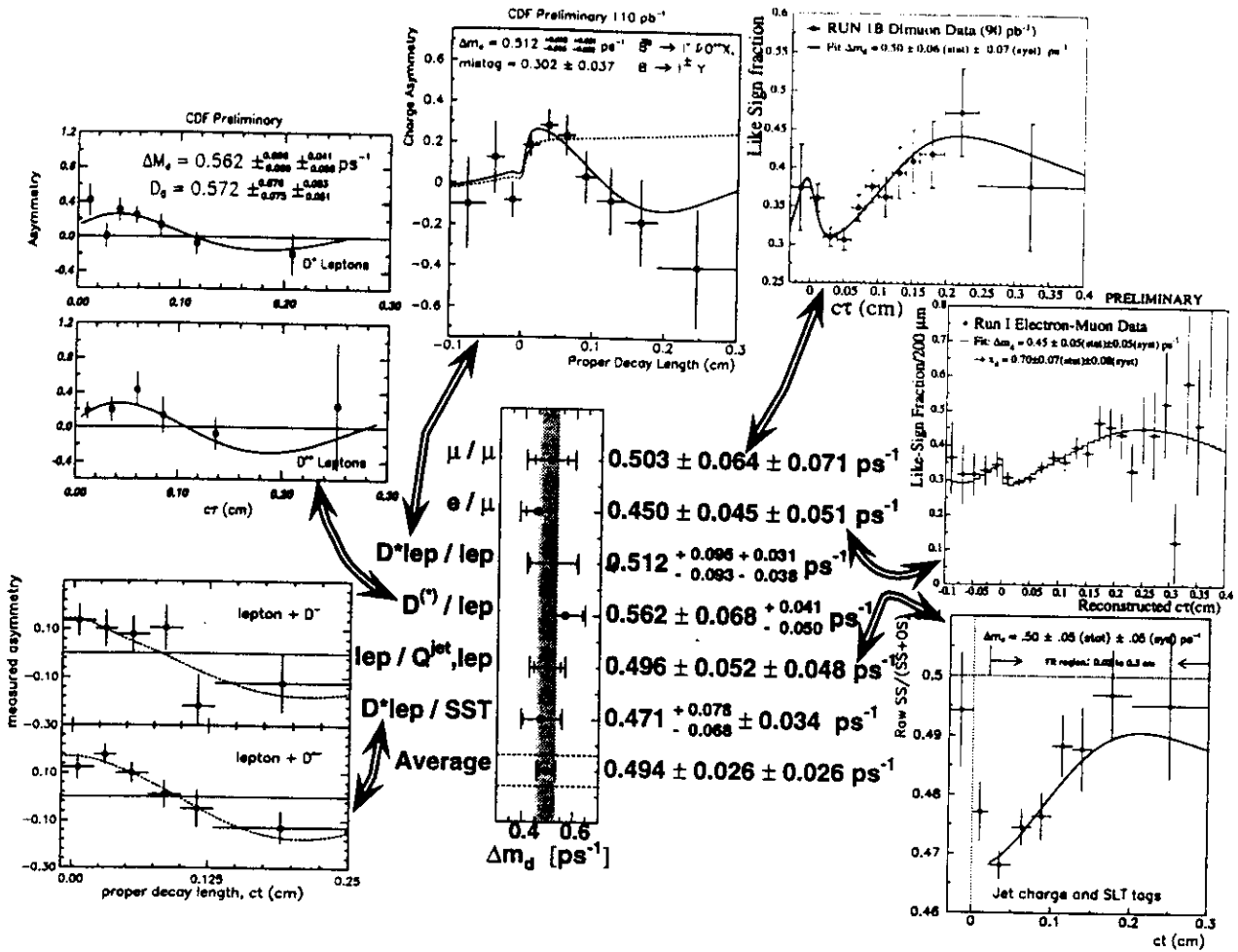


Figure 1: Six measurements of the mixing parameter Δm_d from the CDF Run I data.

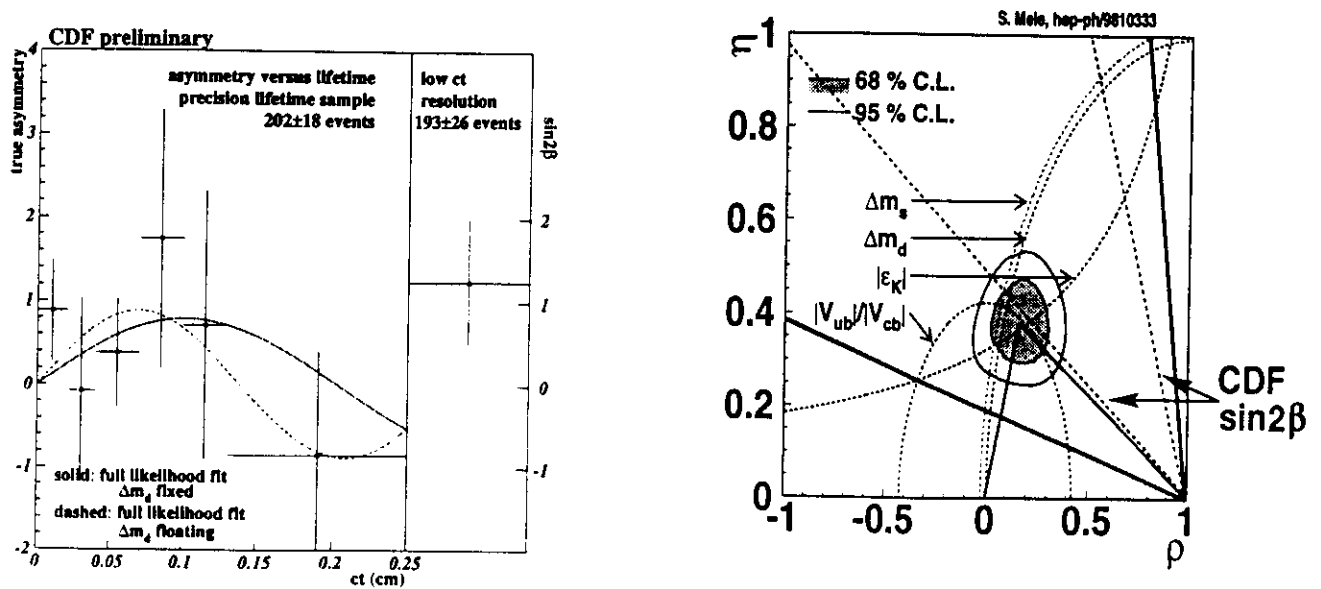


Figure 2: Left figure is the result of $\sin(2\beta)$ using a negative log-likelihood fit and multiple tags. The right figure shows the CDF result compared to indirect results in the $\rho - \eta$ plane.