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We study a possible relation between the neutron and electron electric dipole moments (EDM) in the framework of the Two-Higgs-Doublet Model which has been proposed to explain why the t-quark is much heavier than all other known quarks and leptons. If there is no especial fine-tuning between the CP-violating parameters of the model, the experimental limit on the neutron EDM,  $d_n^{EXP} \leq 1.1 \cdot 10^{-25}~e\cdot\text{cm}$ , implies  $d_e \leq 2 \cdot 10^{-28}~e\cdot\text{cm}$  for the electron EDM.

Fig. -3, ref. -11 name.

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#### 1 Introduction

It is commonly accepted [1]-[5] that in electroweak interaction theories, where mixing between the scalar and pseudoscalar components of two Higgs doublets takes place, the electric dipole moments (EDM) of the electron,  $d_e$ , and the neutron,  $d_n$ , could reach levels close to their respective experimental upper limits. In the particular case of the neutron EDM, such a conclusion follows from considering the two-loop diagram in Fig.1, which produces the so-called quark chromoelectric dipole moment. In turn, the latter generates a neutron EDM dominated, at least in principle, by the t-quark contribution in the upper loop of Fig. 1 which is of order (in e-cm)

$$d_n \sim d_n^{t-loop} \sim 6 \cdot 10^{-25} \{ f(t) (ImZ_0 - Im\bar{Z}_0) + g(t) (ImZ_0 + Im\bar{Z}_0) \}, \quad (1)$$

as recently discussed by Khriplovich [5]. In (1), f(t) and g(t) are the functions determined in Refs.[1, 3] with  $t \equiv m_t^2/m_H^2$  being the ratio between the squared masses of the t-quark and the lightest Higgs boson. These two functions satisfy the relation  $f(t) = (1-2t)g(t) + 2t + t \ln t$  and are both of order one at  $t \sim 1$  or, more precisely, f(1) = 0.828 and g(1) = 1.172. Finally,  $ImZ_0$  and  $Im\bar{Z}_0$  are the dimensionless CP-violating parameters of the model. In such a two Higgs doublet model, there are two different vacuum expectation values:  $v_1 \equiv \langle \Phi_1^0 \rangle_0$ and  $v_2 \equiv \langle \Phi_2^0 \rangle_0$ . This gives the possibility to adjust the model in such a way that it naturally explains why the t-quark is much heavier than the other elementary fermions. This simply occurs if the top quark becomes the only fermion getting its mass from  $v_2$ , which is then supposed to be much larger than  $v_1$ . A model of this kind has been proposed by Das and Kao (DK) [6], who explicitly assume that  $|v_2| / |v_1| \equiv \tan \beta \sim m_t/m_b \sim 40$ . If  $\tan \beta$ is really so large, some new, and considerable, contributions to the neutron EDM appear in addition to  $d_n^{t-loop}$  already given in Eq.(1). A first one,  $d_n^{b-loop}$ , comes from the diagram in Fig. 1 with the t-quark replaced by a b-quark in the upper loop. A second,  $d_n^{Fig\ 2}$ , comes from the diagram in Fig. 2, where the scalar, CP-even bosons,  $H_{1,2}$ , and the pseudoscalar, CP-odd one, A, are coupled "directly" to the nucleon. The quotation-marks mean that such a coupling arises at two-loop level with intermediate heavy quarks and gluons [7, 8].

The present paper is devoted to estimating these additional contributions to the neutron EDM in the framework of the DK model [6]. Comparing our results with the available experimental limit on the neutron EDM we shall

find considerably stronger restrictions on the parameters  $ImZ_0$  and  $Im\bar{Z}_0$  than those given by the unitarity constraints [9] at large  $\tan \beta$ 

$$|ImZ_0 + Im\bar{Z}_0| < 1/2$$
  
 $|ImZ_0 - Im\bar{Z}_0| < 1/2 |\tan \beta|$  (2)

In turn, this will mean that the expected value of the electron EDM,  $d_e$ , will be considerably smaller than the available experimental upper limits.

## 2 Model and notations

The initial doublets  $\Phi_1$  and  $\Phi_2$  can be transformed to the gauge eigenstates  $\Phi_1$  and  $\Phi_2$  through

$$\Phi_1 = \cos \beta \Phi_1 - \sin \beta \Phi_2, \quad \Phi_2 = (\sin \beta \Phi_1 + \cos \beta \Phi_2)e^{i\theta}, \quad (3)$$

where

$$\mathbf{\Phi_1} = \begin{pmatrix} G^+ \\ \frac{v + H_1 + iG^0}{\sqrt{2}} \end{pmatrix}, \mathbf{\Phi_2} = \begin{pmatrix} H^+ \\ \frac{H_2 + iA}{\sqrt{2}} \end{pmatrix} \tag{4}$$

with  $v = (v_1^2 + v_2^2)^{1/2} = (\sqrt{2}G_F)^{-1/2}$  and  $G^+$ ,  $G^0$  being the Goldstone states absorbed by the massive  $W^+$  and Z bosons.

The quark-Higgs interaction is described by the following Yukawa terms of the DK-lagrangian [6]

$$\mathcal{L}_{Y} = -\sum_{d=d,s,b} m_{d}\bar{d}d - \sum_{u=u,c,t} m_{u}\bar{u}u 
- \sum_{d=d,s,b} \frac{m_{d}}{v}\bar{d}d(H_{1} - \tan\beta H_{2}) - i\sum_{d=d,s,b} \frac{m_{d}}{v}\bar{d}\gamma_{5}d(G^{0} - \tan\beta A) 
- \left(\frac{m_{u}}{v}\bar{u}u + \frac{m_{c}}{v}\bar{c}c\right)(H_{1} - \tan\beta H_{2}) - \frac{m_{t}}{v}\bar{t}t(H_{1} + \cot\beta H_{2}) 
+ i\left(\frac{m_{u}}{v}\bar{u}\gamma_{5}u + \frac{m_{c}}{v}\bar{c}\gamma_{5}c\right)(G^{0} - \tan\beta A) + i\frac{m_{t}}{v}\bar{t}\gamma_{5}t(G^{0} + \cot\beta A)...$$
(5)

where the dots refer to further irrelevant terms.

CP violation proceeds through the mixing between the scalar and pseudoscalar neutral Higgs bosons, which can be parametrized in the form [9]:

$$\langle H_1 A \rangle_q = \frac{1}{2} \sin 2\beta \sum_n \frac{Im Z_{0n}}{q^2 - m_n^2} ,$$

$$\langle H_2 A \rangle_q = \frac{1}{2} \sum_n \frac{\cos 2\beta Im Z_{0n} - Im \bar{Z}_{0n}}{q^2 - m_n^2}$$
(6)

As a rule, it is assumed that the above sums are dominated by the lightest Higgs boson with mass  $m_0 = m_H$ . Then, the index n can be dropped in eqs.(6).

# 3 b-quark contribution to the neutron EDM

If the t-quark loop in Fig.1 is replaced by a b-quark one, the expression in the curly bracket of eq.(1) must be changed to

$$\tan^2 \beta [f(b) + g(b)] (ImZ_0 + Im\bar{Z}_0),$$
 (7)

where b now stands for the small ratio  $b \equiv m_b^2/m_H^2$ . The functions f(b) and g(b), at these small values of b, can be approximated by  $f(b) \sim g(b) \sim (b/2)(lnb)^2$  and they turn out to be some 50 times smaller than f(t) and g(t), at  $t \sim 1$  as in eq.(1). In spite of this, the value for  $d_n^{b-loop}$  turns out to be considerably larger than  $d_n^{t-loop}$  for  $\tan \beta > 10$ , provided that

$$|ImZ_0 + Im\bar{Z}_0| / |ImZ_0 - Im\bar{Z}_0| \ge 1$$

A little later we will come back to a more detailed comparison of the various contributions to the neutron EDM. But before that, let us consider one further contribution.

## 4 Contribution of the diagram in Fig. 2

Assuming that the t- and b-quarks are really the only heavy ones, the diagram in Fig. 2 gives a further contribution through the effective vertex

$$e\mu_{n}g_{N}^{A}g_{N}^{H}\epsilon_{\mu}^{\lambda}k_{\nu}\bar{u}_{N}(p_{2})\Gamma_{\mu\nu}u_{N}(p_{1}).$$

$$\frac{1}{2}\{(1+\cot^{2}\beta)(ImZ_{0}-Im\bar{Z}_{0})+(1+\tan^{2}\beta)(ImZ_{0}+Im\bar{Z}_{0})\},$$
(8)

where  $\mu_n$  is the anomalous magnetic moment of the neutron and

$$\Gamma_{\mu\nu} = im_{\sigma_0}^2 m_{\eta_0}^2 \int \frac{d^4q}{(2\pi)^4}.$$

$$\{ \gamma_5 (\not A + \not p_2 + m) \sigma_{\mu\nu} (\not A + \not p_1 + m) + (\not A + \not p_2 + m) \sigma_{\mu\nu} (\not A + \not p_1 + m) \gamma_5 \}.$$

$$[(q^2 - m_H^2)(q^2 + 2qp_1)(q^2 + 2qp_2)(q^2 - m_{\sigma_0}^2)(q^2 - m_{\eta_0}^2)]^{-1}$$
(9)

In this formula,  $\sigma_0$  and  $\eta_0$  are the SU(3)-singlet states of the scalar and pseudoscalar meson nonets. Their masses characterise the two form factors introduced in Eq.(9) for the vertices  $AN\bar{N}$  and  $HN\bar{N}$  to account for the fact

that A and H interact with the nucleon through the chains of transitions  $A \longrightarrow \bar{h}i\gamma_5 h \longrightarrow G^a_{\mu\nu}\tilde{G}^a_{\mu\nu} \longrightarrow \eta_0$  and  $H \longrightarrow \bar{h}h \longrightarrow G^2_{\mu\nu} \longrightarrow \sigma_0$ . Since the  $\sigma_0$  and  $\eta_0$  masses are close to  $m_N$ , we simplify the computation of the integral in (9) setting  $m_{\sigma_0} = m_{\eta_0} = m_N$ . One then obtains

$$\Gamma_{\mu\nu} = \gamma_5 \sigma_{\mu\nu} \frac{m_N^2}{16\pi^2 m_H^2} \int_0^1 \frac{2y^2 (1-y)(2-y)}{(1-y+y^2)^2} = \frac{1}{8\pi^2} (2 - \frac{\pi}{\sqrt{3}}) \frac{m_N^2}{m_H^2} \gamma_5 \sigma_{\mu\nu}$$
 (10)

The constants  $g_N^A$  and  $g_N^H$  in Eq.(8) correspond to the interactions of A and H with a nucleon-antinucleon pair through a single heavy quark loop with vertices  $A\bar{h}i\gamma_5h$  and  $H\bar{h}h$ . Both the specific interactions of A and H with t- and b-quarks described by the Lagrangian (5) and the mixing between A and  $H_{1,2}$ , as given in Eq.(6), are taken into account by the expression in the curly bracket in Eq.(8). From refs.[7] and [8] we take, respectively,

$$g_N^H = (\sqrt{2}G_F)^{1/2} 2m_N/27,$$
 (11)

$$g_N^A = (\sqrt{2}G_F)^{1/2}(-g_A)\frac{m_N}{3}\frac{g_A^{(0)}}{g_A},\tag{12}$$

where  $(-g_A) \approx 1.25$  and  $g_A^{(0)}$  is the isoscalar axial coupling constant. In the quark model one has  $g_A^{(0)}/g_A = 3/5$ . The final result for the contribution of Fig.2 to  $d_n$  is then (in  $e \cdot \text{cm}$ )

$$|d_n^{Fig.2}| = 6 \cdot 10^{-24} (m_N/m_H)^2$$
 (13)

$$\{(1+\cot^2\beta)(ImZ_0-Im\bar{Z}_0)+(1+\tan^2\beta)(ImZ_0+Im\bar{Z}_0)\}$$

This formula exhibits a crucial dependence of the  $d_n^{Fig.2}$  contribution on  $m_H$ ,  $\tan \beta$  and  $(ImZ_0 + Im\bar{Z}_0)$ .

As we do not see any reason to assume that the sum of  $ImZ_0$  and  $Im\bar{Z}_0$  must be much smaller than their difference, we shall consider the situation when

$$\tan^2 \beta \mid Im Z_0 + Im \bar{Z}_0 \mid / \mid Im Z_0 - Im \bar{Z}_0 \mid \gg 1 \tag{14}$$

as the natural one for  $\tan \beta \gg 1$ . In this case the values of  $d_n^{Fig.2}$  can exceed the contribution from  $d_n^{t-loop}$  given by Eq.(1), if  $\tan \beta \approx m_t/m_b \approx 40$  and  $m_H$  is near the generic lower limit  $m_H$ =66.7 GeV [11] found for this kind of Two-Higgs-Doublet models. But in this case, the dominant contribution comes from the *b*-quark upper loop in Fig.1 giving (in *e*-cm)

$$d_n \sim d_n^{b-loop} = 6 \cdot 10^{-25} [f(b) + g(b)] \tan^2 \beta (Im Z_0 + Im \bar{Z}_0)$$
 (15)

where  $[f(b) + g(b)]_{m_H=70GeV} \approx 0.12$ . For larger values of  $m_H$ , the  $d_n^{Fig.2}$  contribution becomes negligible even when compared to  $d_n^{t-loop}$ .

## 5 Relation between $d_n$ and $d_e$

It follows from Eq.(15) that the available experimental limit for the neutron EDM,  $d_n^{EXP} \leq 1.1 \cdot 10^{-25}$  e·cm, imposes a bound on  $(ImZ_0 + Im\bar{Z}_0)$  which is more restrictive than that coming from Eq.(2). Namely, for  $m_H = 70$  GeV one obtains  $(ImZ_0 + Im\bar{Z}_0) \leq 1/tan^2\beta$ . But the most interesting feature of the model under consideration is the possibility of relating the values of the neutron and electron EDM's,  $d_n$  and  $d_e$ . For  $\tan\beta \gg 1$ ,  $d_e$  is dominated by the contributions of the diagram in Fig.3 with a b-quark and a  $\tau$ -lepton circulating in the upper loop [6]

$$d_e \sim d_e^{b,\tau - loops} = -\frac{m_e \alpha \sqrt{2} G_F}{(4\pi)^3} \tan^2 \beta$$

$$\{ \frac{4}{3} [f(b) + g(b)] + 4 [f(\tau) + g(\tau)] \} (Im Z_0 + Im \bar{Z}_0)$$
 (16)

where  $\tau \equiv m_{\tau}^2/m_H^2$ . From Eqs.(15,16) and for  $\tan \beta \gg 1$  one finally finds

$$\mid d_e/d_n \mid \sim 2 \cdot 10^{-3} \tag{17}$$

or  $d_e \le 2 \cdot 10^{-28}$  e·cm, if  $d_n^{EXP} \le 1.1 \cdot 10^{-25}$  e·cm is used.

At present, the corresponding experimental upper limit is  $d_e^{EXP} = (1.8 \pm 1.6) \cdot 10^{-27} \ e \cdot \text{cm}$  [11].

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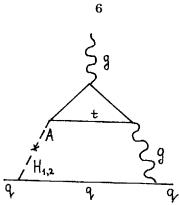


Fig. 1 t-quark loop contribution to the chromoelectric dipole moment of a q-quark.

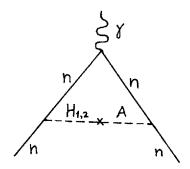


Fig. 2 A further contribution to the neutron EDM.

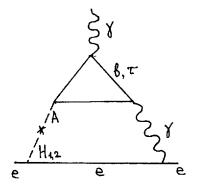


Fig. 3 & quark contribution to the electron EDM.

## References

- [1] S.Bar and A.Zee, Nucl. Phys. 65 (1990) 21; ibid 65 (1990) 2920(E).
- [2] J.F.Gunion and D.Wyler, Phys.Lett. B248 (1990) 170.
- [3] D.Chang, W.-Y.Keung and T.C.Yuan, Phys.Lett. B251 (1990) 608.
- [4] X.-G.He and B.H.J.McKellar, Phys.Lett.B254 (1991) 231.
- [5] I.B.Khriplovich, Phys.Lett. **B382** (1996) 145. A crucial point in this analysis is the introduction of the strange quark content in the neutron. This leads to values for  $d_n$  above the ones predicted in refs. [2, 3].
- [6] A.Das and C. Kao, Phys.Lett. B372 (1996) 106.
- [7] M.A.Shifman, A.I.Vainshtein and V.I.Zakharov, Phys.Lett. B78 (1978) 443.
- [8] A.A.Anselm et al., Phys.Lett. B152 (1985) 116.
- [9] S. Weinberg, Phys. Rev. **D42** (1990) 860.
- [10] The L3 Collaboration, preprint CERN-PPE/96-95, July 1996.
- [11] E.D.Commins et al., Phys.Rev. **D50** (1994) 2960.

## А.Брамон, Е.Шабалин

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