Beta delayed neutron emission of $N = 84^{132}$ Cd

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Using the time-of-flight technique, we measured the beta-delayed neutron emission of 132 Cd. From our large-scale shell model (LSSM) calculation using the $N³LO$ interaction [Z.Y. Xu et al., Phys. Rev. Lett. 131, 022501 (2023)], we suggest the decay is dominated by the transformation of a neutron in the $g_{7/2}$ orbital, deep below the Fermi surface, into a proton in the $g_{9/2}$ orbital. We compare the beta-decay half-lives and neutron branching ratios of nuclei with $Z < 50$ and $N \ge 82$ obtained with our LSSM with those of leading "global" models. Our calculations match known half-lives and neutron branching ratios well and suggest that current leading models overestimate the yet-to-be-measured half-lives. Our model, backed by the ¹³²Cd decay data presented here, offers robust predictive power for nuclei of astrophysical interest such as r-process waiting points.

Introduction. The *r*-process sensitivity studies [\[1\]](#page-4-0) have identified nuclei southeast of the doubly magic $Z = 50$ $N = 82^{132}$ Sn as crucial in calculating the *r*-process nucleosynthesis for almost all astrophysical environments. This is due to the robustness of the $N = 82$ and $Z = 50$ shell closures [\[2\]](#page-4-1), which causes a dramatic discontinuity in proton and neutron separation energy. This feature forces the *r*-process sequence of neutron capture to follow a path aligned with the $N = 82$ shell closure and a sharp turnoff towards more neutron-rich nuclei at $Z = 50$. This also results in the unique sensitivity of the *r*-process to nuclear properties of the nuclei below 132 Sn, even though the ¹³²Sn itself is not directly involved [\[1\]](#page-4-0). Despite the apparent simplicity of the nuclei in the vicinity of 132Sn , rich nuclear phenomena are expected due to the presence of highand low-*j* orbitals and large proton-neutron asymmetry [\[3\]](#page-4-2). This results in the emergence of nuclear isomers [\[4,](#page-4-3) [5\]](#page-4-4), early on set of collectivity in $Z > 50$ nuclei [\[6,](#page-4-5) [7\]](#page-4-6), or unexpectedly short half-lives (compared to leading calculations using "global" models [\[8,](#page-4-7) [9\]](#page-4-8)) for $Z < 50$, $N \geq 82$ nuclei [\[10\]](#page-4-9). Möller, Pfeiffer and Kratz identified the halflife problem in their seminal work on "speeding up the *r*-process" [\[11\]](#page-5-0). They observed that including first-forbidden (FF) beta decay together with allowed Gamow-Teller (GT) transitions decreased their calculated half-lives. However, their new calculations still do not align with experimental values [\[8,](#page-4-7) [10\]](#page-4-9), leaving the problem unresolved.

Both half-lives [\[10\]](#page-4-9) and neutron branching ratios [\[12,](#page-5-1) [13\]](#page-5-2) in the $Z < 50$ $N \geq 82$ region are of crucial importance to model the astrophysical *r*-process correctly [\[1\]](#page-4-0). The difficulty, mentioned above, of "global" models in reproducing known half-lives and branching ratios indicates that nuclear structure effects play a much more important role than initially assumed. In our recent investigation of the beta decay of $N = 84^{133}$ In, we provided the first piece of evidence to tackle this problem [\[14\]](#page-5-3). We showed that the decay strength, and thus the half-life, is dominated by the transformation of a neutron deep below the Fermi surface $(\nu-1g_{7/2} \rightarrow \pi-1g_{9/2})$. We postulated such transformation should be present and thus dominate the decay of all other $N = 84$ isotones. However, testing this hypothesis is hampered by the lack of complete spectroscopic studies. While the beta-delayed gamma spectrum has been studied in 133,134,135 In [\[15–](#page-5-4)[17\]](#page-5-5), 132,133 Cd [\[18,](#page-5-6) [19\]](#page-5-7), and 130 Ag [\[20\]](#page-6-0), no beta-delayed neutron spectroscopy has been done except for 133,134 In [\[14,](#page-5-3) [15,](#page-5-4) [21,](#page-6-1) [22\]](#page-6-2). Beta-delayed neutron spectroscopy has proved to be crucial, as the energy required to transform a neutron deep below the Fermi surface places the dominating transition well above the neutron separation energy [\[14\]](#page-5-3). Only by studying the betadelayed neutron emission of $Z < 50 N = 82, 84$ isotones can we detect the crucial fingerprint, the decay of a neutron deep below the Fermi surface, needed to validate nuclear models in the region.

In this Letter we report the measurement of the betadelayed gamma, and for the first time, neutron emission of 132 Cd. From the lack of observation of gamma transitions between states in 132 In, we deduce a neutron branching ratio of 100%, consistent with Taprogge et al. [\[18\]](#page-5-6) and Phong et al. [\[13\]](#page-5-2). As the beta-decay populates only neutronunbound states, we obtained the decay strength distribution from the neutron branching ratios. We calculated the 132 Cd decay strength using a large scale shell model (LSSM) and the $N³LO$ interaction, resulting in a good match to the experimental distribution. We tested our LSSM by calculating the half-lives of $N = 82, 84$ isotones with atomic number between 43 and 49 (waiting points of the astrophysical *r*-process), obtaining values as much as twice as short as the generally used predictions by FRDM-QRPA. We also calculated the neutron branching ratios of N=82 to N=85 cadmium isotopes, obtaining values systematically larger than global models. This highlights the importance of validating theoretical calculations with a variety of observables, and shows much work still needs to be done in reliably predicting the properties of nuclei relevant to the *r*-process. [\[1\]](#page-4-0).

Experiment. The nucleus of interest, ¹³²Cd, was produced at the ISOLDE facility at CERN using the Isotope Separation On-Line (ISOL) technique. A 1.4 GeV proton beam of $2\mu A$ intensity provided by the Proton Synchrotron Booster (PSB) induced fission in a UC_x target heated to 2200 degrees Celsius located at the ion source assembly at the HRS (High Resolution Separator) beam-line. We selectively ionized ¹³²Cd from other fission products using the Resonance Ionization Laser Ion Source (RILIS) [\[23\]](#page-6-3). The enhanced ionization rate afforded by the use of RILIS

FIG. 1. Gamma spectrum following the decay of 132 Cd. We observe no gamma transitions in 132 In and just one transition in 131 In at 988 keV, populated after beta-delayed neutron emission [\[18\]](#page-5-6). We observe two transitions following the decay of 131 In (*), and a variety of background lines corresponding to neutron scattering in Ge (\dagger) , ⁸⁴Rb contamination from a previous experiment (‡), and the 511 keV positron annihilation line (#). The top right inset shows a schematic of the ¹³²Cd beta-decay.

allowed for the use of the "cold" (room temperature) ion source transfer line in order to suppress highly volatile iodine and cesium mass 132 isobars. These two nuclides are at the high mass peak of 238 U fission yields, resulting in a potential source of background radioactivity in the 132 Cd beam. The combination of laser ionization, cold transfer line, and high resolution magnetic separation resulted in an almost complete suppression of background contaminants (see the gamma spectrum in Fig. [1\)](#page-1-0).

After isoberic separation at the HRS, a transfer beamline delivered ¹³²Cd ions to the ISOLDE Decay Station (IDS) for decay measurements. We implanted the 60-keV ions into a moving tape located in the middle of the β - γ neutron counting setup. The PSB operates in pulsed mode, delivering proton bunches 50 ms long, with 1.2 or 2.4 s between packets. We operated the tape in the take-away mode. It consisted of a 200 millisecond grow-in phase, followed by 400 millisecond decay cycle, and 500 ms transport time to the shielded section of the tape. The complete cycle finished before the next proton bunch is delivered. We observed a total number of $2.2 \, 10^5$ decays. The ISOLDE Decay Station consists of four high-purity Ge (HPGe) clover detectors used to detect gamma and x-ray radiation. The photo-peak efficiency of the array was 3.2% at 1 MeV. We measured the energies of the neutron using the Versatile Array of Neutron Detectors at Low Energy (VANDLE) [\[24\]](#page-6-4). The configuration used here consisted of $26.3\times6\times120$ cm³ plastic scintillator modules capped by photomultiplier tubes at both ends. The VANDLE modules were arranged in an arc of 104.5 cm radius, located in front of the implantation spot. Two plastic scintillators

FIG. 2. Beta-delayed neutron time-of-flight spectra from the decay of 132 Cd. The inset shows the neutron time-of-flight spectrum in coincidence with the 988 keV gamma line in 131 In (see the inset in Fig [1\)](#page-1-0). Similarly to our observation in the decay of ¹³³In [\[14\]](#page-5-3), a large fraction of the neutron intensity concentrates in a peak at around 2 MeV. Both spectra were fitted simultaneously using a self-consistent procedure that includes all possible decay channels in 131 In (see text for more details). The black transitions correspond to neutron emission populating the 1290 keV $3/2^-$ state, the blue to the first excited state (1/2[−]), and the red to the $9/2$ ⁺ ground state. The dashed line represents the background arising from the gamma-flash and uncorrelated events. Finally, the pink line corresponds to the sum of all transitions and background.

surrounding the implantation point detected beta particles, providing a start signal for VANDLE with 80% efficiency. The acceptance of the VANDLE array, taking into account shadowing from the support frame, was 12.0% of 4π , with a total detection efficiency 7.8% at 1 MeV.

Figure [1](#page-1-0) shows the beta-gated gamma spectrum following the decay of the implanted beam. The most prominent lines correspond to: the 988 keV gamma transition in 131 In observed by Taprogge et al. [\[18\]](#page-5-6); 131 Sn (331 and 2433 keV, $*$); one gamma line from long lived $84Rb$ implanted in the chamber in a previous experiment (881 keV, ‡); and the positron annihilation line at 511 keV (#). Daggers (†) mark several lines identified as inelastic neutron scattering on 74 Ge in the high purity germanium gamma detectors [\[25\]](#page-6-5). We did not observe any of the transitions in 132 In previously identified in the decay of 133 Cd [\[19\]](#page-5-7), nor any transition from the decay of 132In in 132Sn [\[26\]](#page-6-6). Our gamma spectrum suggests the neutron branching ratio of ¹³²Cd is close to 100%. A recent measurement at the RIBF (Rare Ion Beam Facility) facility, RIKEN, using ³He proportional counters reports a P_n of 100% [\[13\]](#page-5-2), supporting our observation.

Figure [2](#page-2-0) shows the singles and 988 keV gamma $(^{131}$ In) gated neutron spectra. The most prominent feature is a large peak at 54 ns. This indicates a large fraction of the neutron emission is concentrated at energies around 2.0 MeV. We obtained the neutron energy distribution using

FIG. 3. Cumulative decay strength as a function of the excitation energy in 132 In. We obtained the strength using the intensities from the fit of the neutron time-of-flight spectrum (Fig. [2\)](#page-2-0), the total number of 132 Cd decays (2.2 10^5), and assuming a neutron branching ratio of 100%. The large jump in strength at around 5 MeV corresponds to the most intense neutron transitions observed at 2 MeV in Fig. [2.](#page-2-0) The red line corresponds to the total decay strength calculated using the LSSM with $N³LO$ [\[14\]](#page-5-3), while the dashed red line is just the FF strength. The model reproduces very well the experimental decay strength, further supporting its consistency across $N = 82, 84$ nuclei with $Z < 50$.

the fitting procedure we developed for 133 In [\[14\]](#page-5-3). First, the response of the VANDLE detector to mono-energetic neutrons was obtained from a GEANT4 Monte Carlo simulation of the array, including all detectors and support structures. Then, the response function was calibrated using the beta-delayed neutron emission of ${}^{17}N$ [\[27\]](#page-6-7) and ${}^{49}K$ [\[28\]](#page-6-8).

Discussion. We obtained the cumulative decay strength distribution from the intensities obtained in the fit, the total number of ¹³²Cd decays, and assuming a total $P_n=100\%$, as per above (see black line in Fig. [3\)](#page-2-1). From the intensity of the two largest neutron transitions at 2 MeV (see Fig. [2](#page-2-0) in blue) populating the first $1/2^-$ state in ¹³¹In (E_x=0.3) MeV) and the neutron separation energy $(S_n=2.46 \text{ MeV})$ [\[29\]](#page-6-9)), we deduce that the largest GT transitions correspond to two states in 132 In at 4.8 and 4.9 MeV. They have B(GT) values of $0.14(2)$ and $0.18(2)$ respectively $(log(ft)=4.65(7))$ and 4.54(6)), well within the range of allowed GT transitions populating 1^+ states. 31(6)% of the strength below the main transition corresponds to log(ft) values larger than 5, which are therefore possible candidates to be First Forbidden (FF) transitions. All other transitions above 5 MeV have log(ft) values smaller than five and we propose they correspond to GT transitions to 1^+ states in 132 In.

The red line in Fig. [3](#page-2-1) corresponds to the LSSM calculation of the cumulative beta-decay strength S_β (for the GT transitions, $S_\beta = B(GT)/6144$ and quenching factor $q=0.6$) of ¹³²Cd decay into ¹³²In using N³LO [\[30\]](#page-6-10), and the dashed red line to the FF strength. The extended model space encompassed the $\pi 1p_{1/2}0g_{9/2}0g_{7/2}1d_{5/2}1d_{3/2}2s_{1/2}$ -

FIG. 4. Left: Decay half-lives of $N = 82$ isotones ([\[31\]](#page-6-11)) compared with our calculation using LSSM with $N³LO$ (red). We include calculations using FRDM-QRPA [\[8\]](#page-4-7) (dashed teal), DF3- CQRPA [\[9\]](#page-4-8) (dashed dark green, where available), D3C* [\[32\]](#page-6-12) (dashed green), and shell model calculations from Shimizu et al. [\[33\]](#page-6-13) (purple) and Zhi et al. [\[34\]](#page-6-14) (orange). Right panel: same for $N = 84$ isotones. Note that prior to our model no other LSSM calculations were available.

 $\nu 0g_{7/2}1d_{5/2}1d_{3/2}2s_{1/2}0h_{11/2}1f_{7/2}$ single particle orbitals (see Z. Xu et al. [\[14\]](#page-5-3) for more details). Our LSSM calculation predicts that 17.1% of the strength populates states through FF transitions, within two sigma of the experimental value. In our calculation, the main GT transition corresponds to a single 1^+ state at 4.9 MeV, with a transition strength of 0.35, matching well the observed B(GT)=0.32(3) of the two largest transitions combined. The neutron configuration of the 1^+ state is dominated ($>$ 60%) by the neutron $0g_{7/2}^{-1}1f_{7/2}^{+2}$ configuration, as expected from the large transition strength of the ν g_{7/2} $\rightarrow \pi$ g_{9/2} transformation.

To further test the LSSM with $N³LO$, we calculated the decay half-lives, including both GT and FF transitions, of $N = 82$ and $N = 84$ isotones between technetium ($Z = 43$) and indium $(Z = 49)$, see Fig. [4.](#page-3-0) For 131,133 In and ^{130,132}Cd, the Q_β is taken from experiment [\[29,](#page-6-9) [35\]](#page-6-15). For the rest $(Z \leq 47)$ that do not have measured atomic masses, we used the calculated Q_β from LSSM. An error band corresponding to varying Q_β by ±0.5 MeV was added to those nuclei to account for the uncertainty in their masses. We chose these two isotonic chains due to their impact in the *r*-process abundance pattern, as calculated by Mumpower et al. [\[1\]](#page-4-0). We predict that the low-energy GT strength built on the microscopic $\nu g_{7/2} \rightarrow \pi g_{9/2}$ transition dominates the beta decay of all isotones below $Z = 50$. We included for comparison calculations using "global models" FRDM-CQRPA [\[8\]](#page-4-7), DF3-CQRPA [\[9\]](#page-4-8), and D3C* [\[32\]](#page-6-12). For the $N = 82$ isotones, we also include previous shell-model calculations from Shimizu et al. [\[33\]](#page-6-13) and Zhi et al. [\[34\]](#page-6-14). The present model systematically pre-

FIG. 5. Beta-delayed neutron branching ratios of $N = 82$ to $N = 85$ cadmium isotopes [\[31\]](#page-6-11), compared to the model using LSSM with $N³LO$ (red). For comparison, we show neutron branching ratios from FRDM-QRPA [\[8\]](#page-4-7) (dashed teal), DF3- CQRPA [\[9\]](#page-4-8) (dashed dark green), and D3C* [\[32\]](#page-6-12) (dashed green). While the LSSM with $N³LO$ calculation reproduces well all neutron branching ratios, all "global models" substantially underpredict 132,133 Cd.

dicts shorter half-lives than the FRDM-CQRPA and DF3- CQRPA global models for even- Z parents, with similar results to D3C*. However, the FF transitions represent a much smaller fraction of the overall decay strength along N = 84, ranging between 5% in ¹²⁸Ru (31% in D3C*) and 26% in 133 In (48% in D3C*). The experimental value of 133 In is determined to be 33% [\[14\]](#page-5-3), more consistent with our calculation. The calculations agree with all known half-lives reasonably well. Due to the difficulty in modeling the interaction between nucleons in multiple major shells, calculating beta decays with LSSM had not been available beyond $N = 82$. We note the half-lives of $N =$ 84 even-even ¹²⁸Ru and ¹³⁰Pd have not yet been measured. Both nuclei are so-called waiting points of the astrophysical *r*-process, and have a critical effect in the overall abundance pattern in at least one of the astrophysical scenarios modeled in Ref. [\[1\]](#page-4-0). In these two cases, we predict mostly pure GT decays (\approx 95%) with half-lives about two times shorter than the generally accepted FRDM+CQRPA values [\[8\]](#page-4-7). Although D3C* gave similar half-lives as the LSSM in these particular cases, their predictive power in general is undermined by unrealistically strong FF strengths as shown above.

We also used our LSSM with $N³LO$ to calculate the the neutron branching ratios of cadmium isotopes between $N = 82$ and = 85. Figure [5](#page-3-1) shows the LSSM calculation compared with "global models" FRDM+QRPA [\[8\]](#page-4-7), DF3-CQRPA [\[36\]](#page-6-16), D3C* [\[32\]](#page-6-12), and recent experimental values by Phong et al. [\[13\]](#page-5-2). We note Phong et al. revised the neutron branching ratio of $N = 84$ ¹³²Cd from 60% [\[37\]](#page-6-17) to 100%, consistent with Taprogge et al [\[18\]](#page-5-6) and the present result. Our LSSM calculations reproduce well

all experimental values, including the neutron branching ratios of $N = 84,85^{132,133}$ Cd, which are consistently under-predicted by all other models. We propose that this discrepancy arises from the prediction in "global models" that a larger fraction of FF strength populates bound states compared to the LSSM calculations. For example, the large D3C* FF strength mentioned above [\[32\]](#page-6-12) results in underpredicting the neutron branching ratio of 132 Cd by a factor of two, while still being able to reproduce its half-life. This offers a clear warning against using a single experimental observation to validate theoretical calculations. On the other hand, the good agreement between the LSSM calculation of the neutron branching ratio and the experimental decay strength in 132 Cd, presented here, and for 133 In [\[14\]](#page-5-3) suggests that FF transitions play a smaller role than it had been proposed since the seminal work by Möller et al. [\[11\]](#page-5-0).

Conclusions. We measured the ¹³²Cd beta-delayed gamma and, for the first time, neutron emission. We used the time-of-flight technique to measure the neutron intensity distribution as a function of energy and obtained the GT strength populating unbound states in 132 In. We performed Large Scale Shell Model calculations of the GT strength using the $N³LO$ interaction, resulting in an excellent agreement with our experimental distribution. The model distinguishes itself, when compared to previous calculations using global models, by the smaller fraction of the total strength that goes to FF transitions populating bound states. This, in turn, results in our calculations predicting larger neutron branching ratios that better match known values. The model also reproduces well the known half-lives of $N = 82, 84$ isotones between technetium and indium, as well as the 133,134 In GT strength distributions previously presented in [\[14,](#page-5-3) [22\]](#page-6-2). Considering all these results together, we posit that our LSSM with $N³LO$, anchored by our measurement of the 132 Cd decay strength, is robust and applicable to the $Z < 50$ and $N \geq 82$ region of the chart of nuclei, of great interest to understand the nuclear structure of nuclei relevant to the astrophysical *r*-process.

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