Proposal to the ISOLDE and Neutron Time-of-Flight Committee

Study of the $N = 28$ shell closure in the argon isotopes

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Abstract: We propose to study the neutron-rich isotopes of Ar $(Z = 18)$ around the $N = 28$ shell closure through measuring the spins, nuclear moments and changes in mean-square charge radii for ⁴⁵−⁴⁸Ar. These isotopes lie two protons below the magic Ca nuclei. The moments and spins of $45,47$ Ar ($N = 27,29$) will shed light on the persistence of the $N = 28$ shell gap in Ar, investigating the potential onset of deformation along $N = 28$ as protons are removed from the $Z = 20$ shell. Charge radii across $N = 28$ will provide crucial data to study the characteristics of the shell gap in this region.

Requested shifts: 18 shifts with protons (+3 shifts without protons for setup).

1 Physics Motivation

Recent studies of nuclei in the vicinity of $Z = 20$ have focused on the evolution of shell and sub-shell closures for varying Z. A strong shell closure at $N = 28$ for Ca $(Z = 20)$ up to Ni $(Z = 28)$ isotopes is well documented through studies of the single-particle nature of isotopes along $N = 28$ [1–7]. This is the first shell closure that appears in the shell model due to the contribution of the spin-orbit interaction. Additionally, this region shows evidence of sub-shell gaps at $N = 32,34$ in the vicinity of $Z = 20$ [8– 10]. Experimentally, shell closures are signposted by the disruption of trends in nuclear properties along an isotopic chain, such as the charge radii [11], nuclear moments [12–14], or nuclear masses [15]. A strong shell closure at $N = 28$ is known to exist for the doubly magic ⁴⁸Ca nucleus, but this devolves to the complete disappearance of the shell closure in ⁴²Si. The disappearance of the $N = 28$ shell closure in Si ($Z = 14$) isotopes has been observed in lifetime measurements [16, 17] and measurements of the first 2^+ excitation energy [18–21]. Erosion of the $N = 28$ shell closure has been shown to already begin in isotopes of S $(Z = 16)$. Signatures of shape coexistence in ⁴⁴S have been observed with a deformed prolate ground state and a quasi-spherical $0₂⁺$ state [22–24]. Observations of the deformed ⁴⁴S ground-state strongly mixed with the excited spherical state provide evidence of the breakdown of $N = 28$ in this isotopic chain. This is further supported by shape coexistence seen in ⁴³S [25]. Collective behavior is thought to emerge gradually as the transition occurs from the spherical 48 Ca to the deformed 42 Si leading to the deformed mixed configuration of ⁴⁴S [23]. This progressive development of deformation can be described well with Shell-Model calculations using the SPDF-U interaction [3, 26, 27]. Ar $(Z = 18)$ lies directly between S and Ca and as such, measurements of Ar will study the progressive erosion of the $N = 28$ shell closure as protons are removed from the $d_{3/2}$ orbital. Existing mass measurements and resulting S_{2n} values indicate a strong shell gap at ^{46}Ar [28], although it was measured as $402(4)$ keV smaller than the shell gap in 48 Ca [15]. However, an elevation in correlation energy in 46,47 Ar suggests a description of the Ar ground states that diverges from the expected characteristics of a closed shell nucleus. This implies that the beginnings of collectivity are already appearing within the Ar isotopes [15]. Transfer reactions in 47 Ar observed large variations in the f and p spinorbit splittings which can be accounted for by the proton-neutron tensor force (f) and density dependence (p). This contrasts with previous understandings of the spin-orbit interaction as a purely surface term and can be further investigated with the nuclear moments of Ar isotopes [29]. Additionally, Coulomb excitation measurements [30] show that the shape coexistence in ⁴³S occurs suddenly, with little to no indication in the $N = 27$ isotone of ⁴⁵Ar. Quadrupole moment predictions using the SPDF-U interaction [31] and low energy Coulomb excitation measurements indicate a prolate shape of the ⁴⁴Ar nucleus [32]. Measurements of the nuclear moments of Ar via laser spectroscopy will yield additional information to help improve the description of $N = 28$ shell evolution for different values of Z.

1.1 Nuclear moments and spin measurements

Figure 1: Evolution of measured q -factors and quadrupole moments above $N = 20$ for both Ca [33] and Ar [34].

The magnetic moments of the odd-mass Ar isotopes near $N = 28$ are important for understanding the interplay between manybody correlations and the role of two-body currents in nuclei. The latter has recently been shown to be critical for describing the magnetic moments of medium and heavy mass nuclei, with ab-inito theory, without the need of effective operators adjusted to experimental data [35]. In Ref. [34, 36], the magnetic moments of Ar isotopes with unpaired neutrons in the $1\nu f_{7/2}$ shell up to $N = 25$ were shown to agree with effective single-particle values of $g^{\nu} = 0.8g^{\nu}_{free}$. In Figure 1, we plot the experimental g factors of the odd Ar and Ca isotopes between $N = 20$ and $N = 32$. This observable $(g = \frac{\mu}{l})$ $\frac{\mu}{I}$) is sensitive to the orbit occupied by the unpaired neutrons [11, 12] irrespective of spin. While all Ca isotopes between $N = 20$ and 28 have a groundstate spin of $I = 7/2$ consistent with an unpaired $\nu f_{7/2}^{-1}$ configuration, the groundstate spins of Ar are more diverse. For $39,41$ Ar $(N = 21, 23)$ the spin is 7/2, but ⁴³Ar ($N = 25$) has a spin 5/2, demonstrat-

ing a more complex/mixed wavefunction. However, its g-factor is found similar to that of Ca, which confirms this is a seniority-3 $f_{7/2}$ configuration and highlights the sensitivity of the g-factor to changes in nuclear structure. Its quadrupole moment is also significantly larger than that of the Ca isotone, confirming the seniority-3 configuration. Thus, both the g-factor and quadrupole moment are very sensitive probes to understand the evolution of structure in this region [13]. In this proposal, we wish to establish the spins (known only tentatively), g-factors and quadrupole moments of $45,47$ Ar in order to compare these to those of $47,49$ Ca. This will enable conclusions to be made on the effect that further emptying of the $\pi d_{3/2}$ shell has on the $N = 28$ shell gap.

Predictions place Ar at the boundary between the magic, spherical behaviour in ⁴⁸Ca and the onset of shape coexistence in the ground-state of ⁴⁴S. Calculations using the angular momentum projected generator coordinate method found the shape coexistent ⁴⁴S groundstate to have an absolute deformation of β_2 =0.12 [37]. The predicted deformation for ⁴⁶Ar amounts to β_2 =-0.08, suggesting that shape coexistence decreases in approach of the doubly magic ⁴⁸Ca [37]. Calculations of quadrupole moments in the $sp - df$ picture confirm this, the quadrupole moments increase considerably with the removal of two or more protons from $Z = 20$ [38]. Measurements of the quadrupole moments of Ar isotopes will further extend this picture and probe the onset of deformation towards $N = 28$ away from stability.

1.2 Mapping charge radii

Laser spectroscopy methods have been used to probe the structure of isotopes in the Ca region. A 'kink' in the measured $\delta \langle r^2 \rangle$ for isotones of $N = 28$ can be observed consistently in all isotopes from Ni to K (see Figure 2) [11]. This change in the gradient of $\delta \langle r^2 \rangle$ is a signature typically observed at a spherical shell closure [39], thus indicating the strength of the $N = 28$ shell gap around $Z = 20$. Beyond the $N = 28$ shell closure, the measured $\delta \langle r^2 \rangle$ for isotopes between $Z = 20$ and $Z = 28$ increase steeply and monotonically up to $N = 32$ with similar rates [40–43]. The K [41], Mn [42], Fe [43], and Ni [7] isotopic chains exhibit no observable $N = 32$ closure in the charge radii (Figure 2). It was suggested in Ref.[44] that an effective increase in size of shell-model valence p-wave neutron orbitals, influencing the proton radial extension, explains the observed increase of charge radius in Ca isotopes while maintaining the doubly-magic character of ${}^{52}Ca$. This was experimentally confirmed in Ref. [45] through a neutron-knockout reaction study. The charge radii of Ar isotopes are currently limited to $N = 28$ [34, 36] but are missing ⁴⁵Ar. Systematic measurements of the radii of Ar isotopes past $N = 28$ would provide additional information on the behaviour of the $N = 28$ shell gap and the onset of collectivity between Ca and S.

Figure 2: The measured trend in mean-square charge radii for Ar [34, 36] and regional systematics around $N = 28$ [7, 41].

Figure 3: Schematic diagram of the CRIS experiment that will be used to measure the neutron-rich Ar isotopes.

2 Experimental Details

The Collinear Resonance Ionization Spectroscopy (CRIS) experiment will be used to measure the hyperfine structure and isotope shifts of the neutron-rich Ar isotopes. This combines the high resolution of the collinear-beam method with the high sensitivity of RIS to measure elements with low production yields [46, 47]. We propose to use a uranium carbide (UC_x) target and cold plasma ion source. The resultant beam will be separated using the highresolution separator, HRS, bunched using ISCOOL, and then deflected into the CRIS beamline, schematically presented in Figure 3. The bunched ion beam will undergo neutralisation with K vapour inside the CRIS charge-exchange cell. Post chargeexchange, 40% of the Ar atoms will be in the $4s[3/2]_2$ metastable state for a 40keV beam [36, 48]. Any residual ions postneutralisation will be separated from the atomic beam before it enters the interaction region, where it is overlapped spatially

Figure 4: Three step resonant ionization scheme for Ar. First step transition has been previously used by [34].

and temporally with pulsed lasers. The resonantly-produced ions are then deflected by a 34◦ -bender and detected using either a MagneTOF detector or a decay spectroscopy station.

An illustration of the three-step ionization scheme can be found in Figure 4. The first step of the RIS scheme will use the $4s[3/2]_2 \rightarrow 4p[3/2]_2$ transition, which has previously been used to successfully measure nuclear moments and isotope shifts [34, 36]. A three-step RIS scheme will be used and can be produced with the available lasers at CRIS. The required three-step scheme relies on fundamental wavelengths, and as such will have sufficient power for the required transitions. The first step will be produced with a narrowband injection-seeded Ti:Sa cavity, which has a linewidth of ∼20 MHz [49]. A Pulsed Dye Laser (PDL) using Pyrromethene dye to produce 583.2 nm light will provide the second step. This will allow the atoms to be photoionized by a 1064 nm non-resonant step. The choice of a resonance scheme with a non-resonant laser step of 1064 nm in comparison to lower wavelengths will reduce the laser-induced background of our measurements. In addition to this, production of collisional ions through interactions of neutral atoms after the charge exchange process is reduced by the ultra-high vacuum achieved within the interaction region of the CRIS beamline. The interaction region is routinely operated with an ultra-high vacuum of 10[−]¹⁰ mbar. The beam time estimates have been made based on previous signal-to-noise measurements with the CRIS experiment and a 40% neutralization efficiency from previous fast-beam laser spectroscopy measurements at ISOLDE [36].

3 Beam Time Request

Table 1: Isotopes of interest, half-lives, measured and expected yields, number of shifts requested with a UCx target and protons on target. Yields with a * represent predicted values extrapolated from existing yield measurements and Ar half-lives with thanks to the Targets Team.

In total we request 18 shifts with protons using a UCx target and a low temperature, water-cooled transfer line to a FEBIAD-type plasma ion-source. By maintaining a low temperature on the transfer line, only species that are gaseous at room temperature will be ionized reducing isobaric contamination. The beams of Ar will be contaminated with Kr^{2+} and Xe^{3+} , by a factor of approximately 100 from $45Ar$ to $48Ar$. In addition to this, a large volume of stable contamination is expected. The CRIS technique has previously measured cases where the isobar has been produced with 4 orders of magnitude higher intensity. The beam time request has been estimated using the required shifts to measure 78 Cu [46], 52 K [41] and 131 In [47] with CRIS, considering the expected background rates and RIS efficiency. The shift request accounts for a reduced yield for all isotopes due to a short beam gate and frequency scanning synchronised with one step per super cycle to reduce the effects of isobaric contamination.

The requested shifts for ⁴⁸Ar accounts for the lack of hyperfine structure (a single resonance requires a smaller scanning region), the stable molecule contamination and reduced contamination from 2+ and 3+ species. In order to account for the voltage calibration of ISCOOL and other systematic effects, a total of 5 shifts are required for reference measurements across the previously-measured isotopes ³⁸−44,⁴⁶Ar. Additionally, 3 shifts without protons are requested to optimize the CRIS setup with stable Ar beams from the plasma ion source. This is essential to optimize the neutralization process and laser-atom overlap to maximise the sensitivity to the most radioactive cases.

References

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4 Details for the Technical Advisory Committee

4.1 General information

Describe the setup which will be used for the measurement. If necessary, copy the list for each setup used.

⊠ Permanent ISOLDE setup: CRIS

⊠ To be used without any modification

4.2 Beam production

• Requested beams:

- Full reference of yield information: ISOLDE Yield Database, ISOLTRAP [15], COLLAPS[34]. Yields with a * represent predicted values extrapolated from existing yield measurements and Ar half-lives with thanks to the Targets Team. Minimum required rate at experiment accounts for the short beamgate and synchronisation with the proton supercycle that will be used to limit contamination.
- Target ion source combination: UCx target and a low temperature, water-cooled transfer line to a FEBIAD-type plasma ion-source.
- RILIS? NO.
- Additional features? NO.
- Expected contaminants: We expect contamination from Kr^{2+} and Xe^{3+} . Additional stable contaminants were observed by ISOLTRAP in [15] such as the stable $34\text{S}^{12}\text{C}^+$ or ${}^{34}S^{12}C^+$ molecular ions.
- Acceptable level of contaminants: Contamination level will be limited using a short beamgate, synchronised witht the proton supercycle to only allow for data taking after a proton pulse.
- Can the experiment accept molecular beams: NO.
- Are there any potential synergies (same element/isotope) with other proposals and LOIs that you are aware of? NO.

4.3 Shift breakdown

Summary of requested shifts:

4.4 Health, Safety and Environmental aspects

4.4.1 Radiation Protection

- $\bullet\,$ If radioactive sources are required: N/A
- $\bullet\,$ For collections: N/A