EUROPEAN ORGANIZATION FOR NUCLEAR RESEARCH

Letter of Intent to the ISOLDE and Neutron Time-of-Flight Committee

Coulomb Excitation of a Triaxial Superdeformed "β-band" in [162]Yb

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Abstract

Relativistic Mean Field calculations predict that the 0_2^+ bands of Er and Yb isotopes around N=90 and 92 have a deformation of $\beta_2 \sim 0.45$ and $\gamma \sim 10°$. This is a rather fascinating prospect since the 0_2^+ bands, which are nominally β-vibrational bands, will have a similar deformation to bands at high-spin in this region, which have been identified as "triaxial superdeformed bands". The calculations are supported by the large observed moments-of-inertia of the "β-bands" in these nuclei. Coulomb Excitation measurements are proposed to give a measure of the deformation of these bands, including the triaxiality parameter γ. This proposal is a follow-on from Letter of Intent 226, which asked for the development of ^{160,162,164}Yb beams, to check the maximum achievable intensities, and beam contaminants, for Coulomb excitation and plunger measurements of the "β-bands".

Requested shifts: 21 shifts
Beamline: Miniball, IDS

Scientific Motivation

For many years, the 0_2^+ (or 0_β^+) bands of well-deformed nuclei were understood as "β-vibrations" following the seminal works of Bohr and Mottelson [Bo52, Bo53]. Nevertheless, it became clear that low-lying 0^+ bands could also arise due to other effects such as e.g. shape-coexistence [He11], and quadrupole pairing [Sh19]. Even the very existence of β-bands has been questioned some years ago [Ga01]. In nuclei with $R_{4/2} = E(4_1^+)/E(2_1^+) = 2.91$, such as those in the vicinity of N=90, there is also the opportunity to manifest the critical point symmetry X(5) [Ia01]. Here, we wish to explore the possibility that in the light Yb isotopes, in the N=90 region, the "β-band" could actually have a triaxial superdeformed (TSD) shape.

The proposal is motivated by our recent experimental results and calculations around N=90 [Ma19]. In Fig.1, the level energies of the so-called β- and γ-bands for the N=90, 92 nuclei ^{156}Dy and ^{160,162}Yb are presented, where the energies of a rigid rotor have been subtracted. The data are compared to calculations based on potential energy surfaces (PES's) calculated with the Relativistic Mean Field (RMF) and a 5-dimensional collective Hamiltonian (a modern version of the Bohr-Hamiltonian).

In both the experiment and theory, there is a striking difference in behavior of the 0_2^+ bands between ^{156}Dy and ^{160}Yb. In the former, the 0_2^+ band runs parallel to both the ground and γ-bands, while in the latter, the 0_2^+ band crosses the γ-band, as they have a larger moment-of-inertia than either the ground or γ-bands. Like ^{160}Yb, the 0_2^+ band of ^{162}Yb has a much higher moment-of-inertia than the ground band. These features can be explained by the RMF PES's (RMF+BCS with PC-PK1 density functional [Ma19]) shown in Fig. 2. In ^{156,158}Dy, a single prolate minimum is calculated near β=0.3, and as a result, two β-vibrational bands are predicted. The 0_2^+ and 0_3^+ bands are spaced equally to the spacing between ground band and 0_2^+ bands, as expected for a first and second β-vibrational band. However, in ^{160,162}Yb, a second, triaxial, highly-deformed minimum is visible in the PES at $(\beta,\gamma) \sim (0.45,10°)$ which is absent in the surfaces of the Dy isotopes. So, in the model, the 0_2^+ bands of ^{160,162}Yb are shape-coexisting TSD bands, while the 0_3^+ band is the band based on the first β-phonon. (These bands mix strongly below spin 4 in the calculations for ^{160}Yb). Interestingly, these TSD "β-bands" are predicted in a region where TSD bands have been reported at *high spin* e.g. in Lu isotopes [Sc95, Ød01] and in ^{160}Yb itself [Ag08].
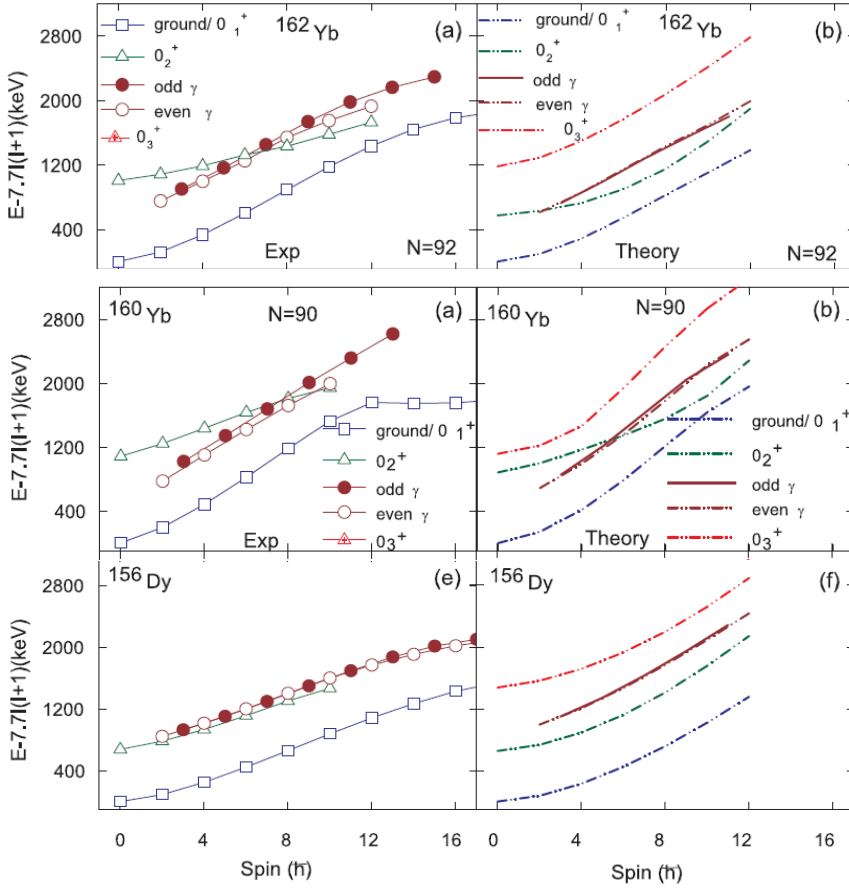
Figure. 1. *Experimental ground, β- and γ-bands (left) compared with calculation (right) [Ma19].*

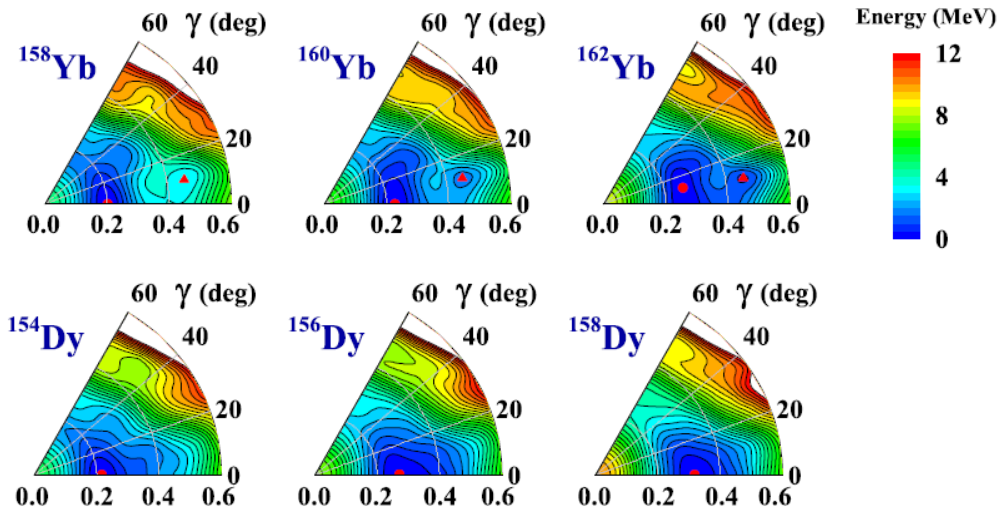**Figure. 2.** *PES's of N=88, N=90 and N=92 Dy and Yb isotones in the β-γ-plane. Minima are marked with red symbols, circles and triangles represent the global and secondary minima, respectively. The energy spacing in the contour lines is 0.25 MeV [Ma19]. RMF PES around N=90 [Ma19].*

Although lifetimes have been measured in the ground band in even-even nuclei in this region [e.g. Fe88, Mc06], the higher-spin members of the β- and γ-bands in the Yb isotopes have only recently been reported, following measurements at iThemba LABS [Ma19, Md18]. No data on level lifetimes of yrare low-spin states and transition strengths from such states are known so far for the nuclei of interest, which hampers a clear interpretation of the structure of the β-bands and motivates this work.

Experiments

In our Letter of Intent (LOI226), two methods were proposed to obtain transition rates related to the "β"-band – an RDDS plunger measurement and Coulomb Excitation. Time was granted to test the yields and purity of ^{160,162,164}Yb beams; the ^{160}Yb beam was found to have high (50%) contamination while ^{162}Yb and ^{164}Yb had yields of over 10^9 pps/μC with 10% and 5% contamination, respectively. Since the"β"-band of ^{164}Yb is not confirmed above spin 2 [Si18], we have chosen to measure transition rates in ^{162}Yb, where the band members and their decay branching ratios are better understood (see Fig. 2). With an upper limit of 2×10^8 particles for charge breeding, and a 2.3% transport efficiency to Miniball, up to 5×10^6 pps can be expected on target.

While much is known about the level scheme of ^{162}Yb [Mc04, Md18], the $4_β \rightarrow 2_β$ and $2_β \rightarrow 0_β$ γ-ray transitions have not been reported. We also propose to search for these transitions using the IDS.
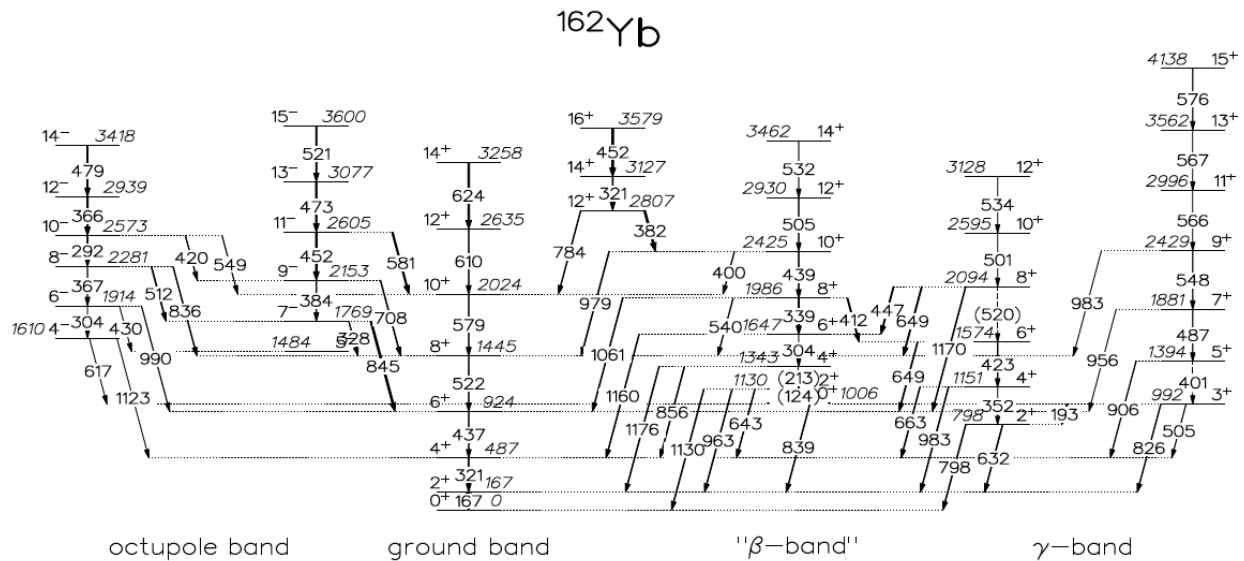

Figure. 2. *Low-lying levels of ^{162}Yb, from the in-beam work of [Md18] and the decay work of [Mc04], including the ground, "β", γ-bands and octupole vibrational bands. Transitions in parenthesis have not been observed.*

Coulomb Excitation

Transition matrix elements will be measured so that the quadrupole moment and the triaxiality parameter γ can then be deduced using Kumar-Cline sum rules [Cl86]. In Figure 3, integrated p-γ yields for the ^{194}Pt(^{162}Yb,^{162}Yb) reaction, as a function of spin, have been calculated using GOSIA, with the QQQ2 charged particle detector array (CD detector) subtending the forward angles between 18° and 52°, and assuming an energy-independent 7% γ-ray detection efficiency for the Miniball array. Matrix elements were derived from known lifetimes for the ground band [Mc06], and calculated [Ma19] B(E2) values for the 0_2^+ and γ-band. The calculated p-γ counts for members of the 0_2^+ band, (summed over all γ-decays per level), obtained for a beam of 5×10^6 pps on a 2 mg/cm^2 ^{194}Pt target, are up to 10^4 counts per level to the 8_2^+ state. The calculated and experimental branching ratios differ

for decays from the β-band, so in Table 1, *experimental* branching ratios [Md18, Re07] are used to estimate p-γ yields for individual transitions depopulating the 0_2^+ band. Note that each level in the 0_2^+ band typically decays via a single strong transition, of energies around 1 MeV. Under this scenario, these would accumulate up to 10000 counts in 4 days of beam time.
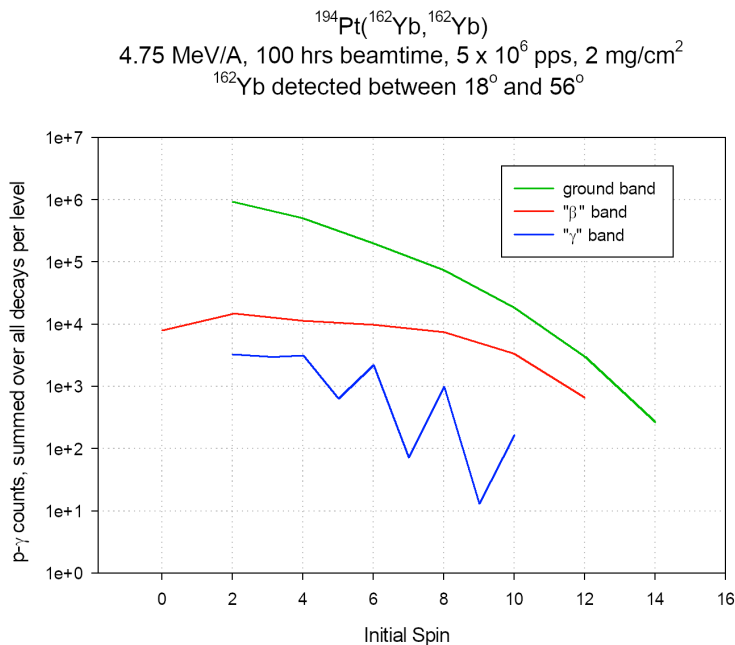

$^{194}Pt(^{162}Yb, ^{162}Yb)$
4.75 MeV/A, 100 hrs beamtime, 5×10^6 pps, 2 mg/cm^2
^{162}Yb detected between 18° and 56°

Figure. 3. Integrated p-γ coincidence counts of a safe Coulomb Excitation measurement for the levels of the ground, 0_2^+ and γ-bands of ^{162}Yb. The detected particle is ^{,162}Yb.

Table 1. Estimated γ-ray yields, assuming constant efficiency (7%) and 100 hrs of beam time, for transitions depopulating the β-band of ^{162}Yb. "Clean" transitions are highlighted.

Level	Transition	^{162}Yb Eγ (keV)	Experimental γ-branching	p-γ yield 2 mg/cm^2 ^{194}Pt 5×10^6 pps
$0_β$	$0_β \rightarrow 2_1$	839	100	7980
$2_β$	$2_β \rightarrow 0_1$	1130	100	6580
	$2_β \rightarrow 2_1$	963	74	2860
	$2_β \rightarrow 4_1$	643	50	3280
$4_β$	$4_β \rightarrow 2_1$	1176	100	10400
	$4_β \rightarrow 2_β$			
	$4_β \rightarrow 4_1$	854	8	832
$6_β$	$6_β \rightarrow 4_1$	1160	100	5760
	$6_β \rightarrow 4_β$	304	68	3920
	$6_β \rightarrow 6_1$			
$8_β$	$8_β \rightarrow 6_1$	1061	31	1060
	$8_β \rightarrow 6_β$	339	44	1520
	$8_β \rightarrow 8_1$	540	44	1520
	$8_β \rightarrow 6_γ$	412	100	3420

The effect of Doppler broadening on the lineshapes has been estimated by using the opening angle of the Miniball detector segments for the detector width, and adding an intrinsic resolution of 2.3 keV in quadrature. Furthermore, we note that according to GOSIA, more than 90% of the cross-section

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for populating states above spin 2 in the "β"-band resides at Yb scattering angles above 40°. We therefore calculate the resolution around a ring centered on θ=45°, with a Miniball detector at θ=45°. For a 1 MeV γ-ray, the FWHM ranges from 2.6 keV to 16 keV, with a weighted average of 11.5 keV.

With these values in hand, we have checked the decays from each level to see if any peaks would overlap. The cleanest lines for each level are those highlighted in yellow. The intensities of other transitions depopulating a level can then be obtained knowing the branching ratios. The only (small) concern is the proximity of the 1160 and 1176 keV lines, but the strength of the 1160 keV line can be derived from the branching ratio and the strength of the 304 keV line.

RDDS

RDDS was proposed in LOI226 using a ^{92}Mo target. With this target (of 1 mb/cm^2 thickness) the yields would be lower. Nevertheless we have assessed that it would be possible to measure the lifetime of the 0_β state and the 2_β state. But complications would occur for the 4_β state due to the close proximity of the 1060 line to the 1176 keV line, while for higher lying states, there would be insufficient statistics. We have therefore chosen to concentrate on a pure Coulomb Excitation measurement, in which case the statistics are enhanced using a heavier and thicker target.

β-decay

The γ-ray branching ratios for decays from the levels of the "β"-band are necessary to determine the in- band B(E2) values. As the 6$^+$ and 8$^+$ levels show evidence of interactions at the crossing with the γ-band (see Figs. 1 and 2), the 2$^+$ and 4$^+$ levels become important, as they sample a "pure" superdeformed triaxial wavefunction. However, two important in-band transitions of the "β"-band have not been reported so far. These are the 124 keV 2$^+$→ 0$^+$ and the 213 keV 4$^+$→ 2$^+$ transitions, (see Fig.4). This is undoubtedly due to the large (E$_\gamma$)^5 factors in the expression for the transition rate, which favour out-of-band transitions. For example, $(1130/124)^5 = 62847$. In fact, using the B(E2) values of [Ma19] one may calculate the branching ratios $P_\gamma(124)/\sum_i P_\gamma(i) = 5.3 \times 10^{-4}$ and $P_\gamma(213)/\sum_i P_\gamma(i) = 10^{-2}$, where $P_\gamma(i)$ is the transition probability of the ith γ-ray depopulating the 2$^+$ or 4$^+$ level. However, the B(E2) values of [Ma19] predict that the 963 keV transition be only 3% of the intensity of the 1130 keV transition, while the experimental [Mc04] ratio is 74%. Because of this large discrepancy between theory and experiment, it is not possible to predict the 124 keV intensity with any reliability. In the best case scenario it could have a similar intensity to the 213 keV transition.

Therefore we propose to measure at least the intensity of the 213 keV transition from the β-decay of ^{162}Lu, which has a ground state with an 82s half-life, and isomers with 1.5 and 1.9 m half-lives, using the ISOLDE Decay Station (IDS). Two methods are considered, a singles measurement, or a co-incidence measurement.

Singles

A clover singles spectrum of ^{162}Yb from the decay of ^{162}Lu is shown in Fig. 2(a) of [Mc04]. In this experiment, 1.4 x 10^{11} decays were presented to a clover array of 1.1% efficiency at 1.3 MeV. The relative intensities published by [Mc04], and singles spectrum allow a relation to be established between the intensities and the counts seen in the spectrum. Taken together with the above branching ratio, the 213 keV transition would be expected to have around 900 counts in this spectrum, which would be swamped by the uncertainty on the background which is around 300000 counts high. To set the condition to observe a line in singles to e.g., 20% accuracy, we demand that the number of counts in the peak

$$N_\gamma > 5\sqrt{N_b}, \qquad (1)$$

where N_b is the number of counts in the background. Assuming the IDS is equipped with 12 clovers, with an efficiency of 6% at 1.3 MeV, then this condition will be met if the overall decays presented to the detectors are increased by a factor of 6.2 for the 213 keV line, implying about 8×10^{11} decays would need to be presented to the IDS. Furthermore, to confirm that the 213 keV line belongs to ^{162}Yb, its lifetime should be measured, which would require an out-of-beam measuring period of 3 half-lives. Alternatively, coincidences could be used.
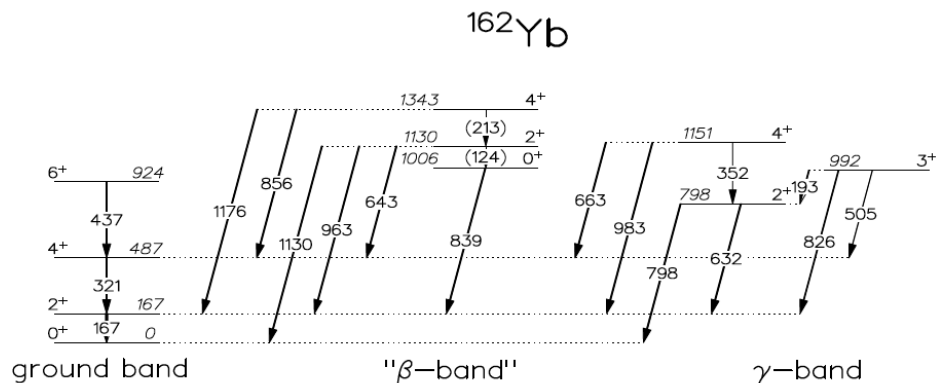

Figure. 4. *Close-up of the levels and related transitions of the ground, "β" and γ-bands of ^{162}Yb, as observed in β-decay [Mc04]. Transitions in parenthesis have not been observed.*

Coincidences

In Fig. 2(b) of [Mc04] a coincidence gate on the 167 keV transition is presented. The background is reduced by a factor of about 250 compared to the singles spectrum. The peaks near 1.3 MeV are reduced by a factor 0.01 in this spectrum, due to requirement to detect the second γ-ray, resulting in an improvement in the peak-to-background ratio. In the IDS, peaks near 1.3 MeV would be expected to have a smaller reduction in height as the assumed efficiency is 0.06. To observe the 214 keV transition, we would gate on 1130, 963 and 643 lines which could be summed. (The 167 gate will probably be associated with a higher background but can also be used). A similar analysis now finds a factor of 22 increase in decays is required, or 2.9×10^{12} decays.

The important point is that a shortened out-of-beam period is not required.

Beamtime requirements

The listed intensity [ISLu] of the ^{162}Lu beam, from a Ta target, is 1.8×10^7 pps/μC. Ultimately, the amount of beam that can be utilized in the IDS clover array is limited by the counting rate in a detector. If the beam is continuously implanted into the tape, eventually the decay rate will equal the implantation rate, when $t \gg \tau_{1/2}$. With 1.8×10^7 decays/second, and assuming each decay emits on average 2 γ-rays, which are detected with 6% efficiency over 12 clovers, 1.8×10^5 decays per detector are implied. However, in [Mc04], the 1.4×10^{11} decays only produced 3.1×10^8 singles events. Allowing for the 1% efficiency of the Yale setup, it implies that only as much as 22% of the β-decays emitted γ-rays. Presumably the rest decayed to the ground state. Applying this final 22% correction to the IDS brings the rate per detector down to 40kHz.

We propose to implant and count for 6 half-lives before moving the tape to limit the build-up of activity from the daughters. Under these conditions about 10^{12} decays should be presented to the array per day. Three days of beamtime would allow the intensity of the 213 keV transition to be measured to an accuracy of about 20%. The 124 keV transition may be detected.

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Summary of requested shifts:

In summary, 12 shifts are requested for the coulex of ^{162}Yb.

For the IDS measurement, we request 9 shifts of ^{162}Lu beam.

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Appendix

DESCRIPTION OF THE PROPOSED EXPERIMENT

The experimental setup comprises: *(name the fixed-ISOLDE installations, as well as flexible elements of the experiment)*

Part of the Choose an item.	Availability	Design and manufacturing
Beam Current Measurement after REX EBIS	☒ Existing	☒ To be used without any modification
Miniball + CD detector	☒ Existing	☒ To be used without any modification ☐ To be modified
	☐ New	☐ Standard equipment supplied by a manufacturer ☐ CERN/collaboration responsible for the design and/or manufacturing
IDS	X☐ Existing	X☐ To be used without any modification ☐ To be modified
	☐ New	☐ Standard equipment supplied by a manufacturer ☐ CERN/collaboration responsible for the design and/or manufacturing
[insert lines if needed]		

HAZARDS GENERATED BY THE EXPERIMENT

(if using fixed installation) Hazards named in the document relevant for the fixed [MINIBALL + only CD, MINIBALL + T-REX] installation.

Additional hazards:

Hazards	[Part 1 of the experiment/equipment]	[Part 2 of the experiment/equipment]	[Part 3 of the experiment/equipment]
Thermodynamic and fluidic			
Pressure			
Vacuum	High Vacuum 10^{-6} mbar	High Vacuum 10^{-6} mbar	
Temperature	LN_2 77 [K]	LN_2 77 [K]	
Heat transfer			
Thermal properties of materials			
Cryogenic fluid	LN_2, 1 Bar, 10l	LN_2, 1 Bar, 10l	
Electrical and electromagnetic			
Electricity	[voltage] [V], [current][A]		
Static electricity			
Magnetic field	[magnetic field] [T]		
Batteries	☐		
Capacitors	☐		
Ionizing radiation			
Target material	[material]		
Beam particle type (e, p, ions, etc)	^{162}Yb	^{162}Lu	
Beam intensity	> 2 x 10^6 pps	> 1.8 x10^7 pps	
Beam energy	4.7MeV/A		

Cooling liquids	[liquid]		
Gases	[gas]		
Calibration sources:	☒		
• Open source	☐		
• Sealed source	☒ [ISO standard]		
• Isotope	^{152}Eu, ^{133}Ba, ^{60}Co	^{152}Eu, ^{133}Ba, ^{60}Co	
• Activity	~ 10 kBq	~ 10 kBq	
Use of activated material:			
• Description	☐		
• Dose rate on contact and in 10 cm distance	[dose][mSV]		
• Isotope			
• Activity			

Non-ionizing radiation

Laser			
UV light			
Microwaves (300MHz-30 GHz)			
Radiofrequency (1-300MHz)			

Chemical

Toxic	[chemical agent], [quantity]		
Harmful	[chemical agent], [quantity]		
CMR (carcinogens, mutagens and substances toxic to reproduction)	[chemical agent], [quantity]		
Corrosive	[chemical agent], [quantity]		
Irritant	[chemical agent], [quantity]		
Flammable	[chemical agent], [quantity]		
Oxidizing	[chemical agent], [quantity]		
Explosiveness	[chemical agent], [quantity]		
Asphyxiant	[chemical agent], [quantity]		
Dangerous for the environment	[chemical agent], [quantity]		

Mechanical

Physical impact or mechanical energy (moving parts)	[location]		
Mechanical properties (Sharp, rough, slippery)	[location]		
Vibration	[location]		
Vehicles and Means of Transport	[location]		

Noise

Frequency	[frequency],[Hz]		
Intensity			

Physical

Confined spaces	[location]		
High workplaces	[location]		
Access to high workplaces	[location]		
Obstructions in passageways	[location]		
Manual handling	[location]		
Poor ergonomics	[location]		

0.1 Hazard identification

The longest lived activity from the ^{162}Lu decay chains has a half-life of approximately 1 day.

3.2 Average electrical power requirements (excluding fixed ISOLDE-installation mentioned above): *(make a rough estimate of the total power consumption of the additional equipment used in the experiment)*

None above fixed ISOLDE-installation for beam development. Plunger uses < 1kW.