Search for Highly-Ionizing Particles in pp Collisions During LHC Run-2 Using the Full MoEDAL Detector

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This search for Magnetic Monopoles (MMs) and High Electric Charge Objects (HECOs) with spins 0, 1/2 and 1, uses for the first time the full MoEDAL detector, exposed to 6.6 fb⁻¹ protonproton collisions at 13 TeV. The results are interpreted in terms of Drell-Yan and photon-fusion pair production. Mass limits on direct production of MMs of up to 10 Dirac magnetic charges and HECOs with electric charge in the range 5e to 350e, were achieved. The charge limits placed on MM and HECO production are currently the strongest in the world. MoEDAL is the only LHC experiment capable of being directly calibrated for highly-ionizing particles using heavy ions and with a detector system dedicated to definitively measuring magnetic charge.

The detection of a massive, stable or pseudo-stable, Highly-Ionizing Particle (HIP) with a significantly large electric charge $|q| \gg e$ (where e is the elementary charge) and/or a magnetic charge g_D , would provide compelling evidence for physics beyond the Standard Model. Many hypothetical particles capable of producing HIP signatures have been proposed, including Magnetic Monopoles (MMs) [\[1–](#page-4-4)[12\]](#page-4-5) and dyons [\[13\]](#page-5-0); Q-balls [\[14,](#page-5-1) [15\]](#page-5-2); micro black-hole remnants [\[16\]](#page-5-3); doubly charged massive particles [\[17\]](#page-5-4); scalars in neutrino-mass models [\[18\]](#page-5-5); and aggregates of ud- [\[19\]](#page-5-6) or s-quark matter [\[20\]](#page-5-7).

HIPs have been sought in matter [\[21\]](#page-5-8), cosmic rays [\[21,](#page-5-8)

[22\]](#page-5-9) and in accelerator-based experiments [\[9,](#page-4-6) [12,](#page-4-5) [23\]](#page-5-10), with recent searches conducted at the LHC [\[24–](#page-5-11)[40\]](#page-5-12).

According to the Dirac Quantization Condition [\[1\]](#page-4-4), magnetic charge would be quantized in units of $q_{\text{D}} =$ $e/2\alpha \approx 68.5e$, where α is the fine structure constant. Due to the exceptionally strong coupling between a MM and the photon, perturbative calculations cannot reliably predict cross-sections associated with MM production. The diagrams involved need to undergo appropriate resummation in order to account for potential non-perturbative quantum corrections [\[41](#page-5-13)? , [42\]](#page-5-14). Such techniques habe been investigated, especially for High Electric Charge Objects (HECOs) [\[44\]](#page-5-15). For simplicity and ease of comparison with other search results, here we use leadingorder Feynman diagrams for cross-section estimates.

FIG. 1. Tree-level Feynman diagrams for the following: (a) DY production of HIP–anti-HIP pairs; (b) spin-1/² HECO pairs; and, (c,d) PF production of HIP–anti-HIP pairs.

The Drell–Yan (DY) pair production mechanism provides a basic model for HIP creation. HIP pair production of spin-0, spin-1/2 and spin-1 are computed using the Feynman diagrams shown at the top of Fig. [1.](#page-1-0) Spin- $1/2$ HECO DY production can take place via virtual photon (γ) or γ/Z^0 exchange [\[45\]](#page-5-16). For DY production of spin- $1/2$ MMs, the coupling of the Z boson to magnetic charge is conventionally assumed to be absent. In some MM models, this can be proven explicitly [\[7,](#page-4-7) [46\]](#page-5-17).

FIG. 2. A GEANT4 Panoramix view of the full MoEDAL detector deployed at IP8 during LHC's Run-2.

Additionally, MoEDAL has pioneered the search for HIPs at the LHC using photon fusion (PF) [\[33,](#page-5-18) [47](#page-5-19)[–49\]](#page-5-20) described by the two Feynman diagrams shown at the bottom of Fig. [1.](#page-1-0) For the mass range considered here, PF production of HIPs has a considerable cross-sectional advantage compared to DY production [\[47\]](#page-5-19). Consequently, PF dominates when setting mass bounds. This picture is maintained even after resummation [\[41,](#page-5-13) [42,](#page-5-14) [44\]](#page-5-15).

The physics processes considered here were generated using MADGRAPH5 [\[50\]](#page-5-21) utilizing the Universal Feyn-Rules Output presented in Ref. [\[47\]](#page-5-19). The parton distribution functions (PDFs) NNPDF23 [\[51\]](#page-6-0) and LUXqed [\[52\]](#page-6-1) were used for the DY and PF production processes, respectively. The LUXqed PDF was created in a modelindependent way utilizing ep scattering data.

In this search we used, for the first time, the full Run-2 MoEDAL detector shown in Fig. [2.](#page-1-1) MoEDAL's detector technology differs radically from the general-purpose LHC experiments, ATLAS and CMS. The MoEDAL detector, positioned around LHCb's VErtex LOcator detector (VELO) at IP8, employs two unconventional passive detection methodologies dedicated to HIP detection. The first is a system of plastic Nuclear Track Detectors $(NTDs)$ — including the High-Charge Catcher (HCC) designed to register HIP ionization trails. The second detector system, the Magnetic Monopole Trapper (MMT), is designed to capture HIPs that stop within its sensitive volume, allowing for further study at the ETH Zurich SQUID magnetometer facility.

Both NTD and MMT detector systems require neither readout electronics nor a trigger since no Standard Model (SM) particles can produce the distinctive signatures of HIPs traversing the MoEDAL detector. Thus, only a few HIP messengers of new physics observed in MoEDAL data are needed to herald a discovery. Below we give a brief description of the MoEDAL detector. A more detailed description of the detectors and their calibration and analysis is given in the supplemental material [\[53\]](#page-6-2).

The NTD detector system is positioned around LHCb's VELO detector, as presented in Fig. [2.](#page-1-1) It consists of an array of standard NTD stacks and the HCC, both of which are comprised of Makrofol NTD plastic. The HCC array is designed to extend the search for HIPs to the highest charge possible. This is achieved by situating the HCC between LHCb's RICH1 detector and the first LHCb downstream tracking detector, TT1, minimizing the material in which the very highest ionizing particles may be absorbed. After exposure in the LHC's IP8 region, the MoEDAL NTD stacks are sent to INFN Bologna for etching and scanning.

The pertinent quantity for MoEDAL's plastic NTDs is the Restricted Energy Loss (REL) [\[54\]](#page-6-3). Heavy ion beams are used to determine the NTD response over a wide range of energy loss, as explained in Ref. [\[55\]](#page-6-4). The NTD response is calibrated directly using heavy-ion beams at the NASA Space Radiation Facility (NSRL) at the Brookhaven National Laboratory in the US and at the CERN SPS. The REL corresponding to the threshold of the Makrofol NTDs utilized is $\sim 2700 \text{ MeV g}^{-1} \text{cm}^2$.

A study of the HIP detection efficiency of NTDs in the presence of beam backgrounds was performed by using NTD calibration stacks exposed to a relativistic lead-ion beam. The stacks were comprised of Makrofol NTD foils, exposed to beam backgrounds as part on MoEDAL's NTD array at LHC's Run-2 during 2018, interleaved with previously unexposed Makrofol NTD sheets using plastic from the same production batch utilized in calibration and standard data taking. The NTDs sheets comprising the calibration stacks were then etched and scanned using the same techniques and procedures employed to examine all MoEDAL NTD stacks. As the relativistic lead-ion calibration beam particles penetrate the whole stack, the signal etch-pits seen in the LHC unexposed sheets can serve as a map of the passage of the heavyions. The identification efficiency of etch-pits in the LHCunexposed sheets is measured to be effectively 100% by making independent comparison scans of the other LHCunexposed sheets in the stack which have the identical etch-pit number and pattern.

During Run-2 the surface area of standard NTD stacks facing IP8 was 10.7 m^2 . The corresponding area of HCC foils was 3.24 m^2 . To avoid excessive damage from beaminduced backgrounds the standard stacks were replaced three times. The HCC foils were replaced more frequently, 7 times in all, as they were deployed nearer the beam line.

A pair of collinear incident and exiting etch-pits, found in the first layer of a 6-layer NTD stack, that are consistent with pointing to the IP, is defined as a "candidate". The discovery of such a candidate would trigger the analysis of all 5 downstream foils comprising an NTD stack. A HIP "candidate track" requires collinear etchpits pairs that point to the collision point in all six NTD sheets in the stack. No "candidate" or "candidate track" was found.

The MMT detector comprises 2400 aluminium bars with a mass of 800 kg deployed in three arrays transverse to and just forward of IP8. Aluminium was chosen as the trapping material because the aluminium nucleus has an anomalously large magnetic moment which engenders a monopole–nucleus binding energy of 0.5– 2.5 MeV [\[57\]](#page-6-5), which is consonant with the shell-model splittings. A MM will stop in the MMT if its speed falls below $\beta \leq 10^{-3}$. It will then bind to the nucleus due to the interaction between the MM and the nuclear magnetic moment [\[56–](#page-6-6)[60\]](#page-6-7). MMs bound in such a way would be trapped indefinitely [\[56,](#page-6-6) [57\]](#page-6-5).

After the MMT's aluminium volumes were exposed for roughly a year they were sent to the ETH Zurich Laboratory for Natural Magnetism. They were passed through a SQUID magnetometer to check for trapped magnetic charges. The SQUID magnetometer calibration was performed using a known magnetic dipole sample and checked using a simulated MM comprised of long thin solenoids providing the same response as a MM with a known magnetic charge.

The acceptance of the MoEDAL detector at Run-2 is defined to be the fraction of events in which at least one HIP of the produced pair was detected in MoEDAL in either the NTD detector or the MMT detector, giving two sets of acceptance curves, one for each production mechanism considered. The acceptance for HECOs and MMs depends on an interplay between the positions of MoEDAL detector modules; energy loss in the detectors; the mass and charge of the particles; and the spin-dependent kinematics of the interaction products. For HECOs, MoEDAL's NTD system provides the only means of detection. The spin-dependent acceptance for different spins are mostly due to the degree of coincidence of the azimuthal (ϕ) and polar (θ) distributions of the produced HIPs with that of the detector elements. Example acceptance curves are provided in the supplemental material [\[53\]](#page-6-2). The Run-2 geometric acceptance of MoEDAL's NTD and MMT detectors for MMs partly overlap. Thus, care must be taken not to double-count signals when calculating the acceptance of the overall detector. Only the NTDs can be utilized for the HECO analysis since we cannot register HECOs trapped in the MMT detectors.

This analysis is dominated by systematic errors due to insufficient knowledge of the exact amount of material arising from the VELO detector, between the interaction point and the MoEDAL detector modules. The elements of the VELO detector within LHCb's physics acceptance are naturally simulated with great precision in the LHCb geometry. However, the VELO elements outside of the LHCb's physics acceptance were not sufficiently detailed to allow us to provide a precise estimate of the material budget. Estimates indicate the intervening material lying between the VELO detector the MoEDAL detector elements is between 0.1 and 8.0 radiation lengths (X_0) in thickness and on average, around $1.4X_0$ [\[62\]](#page-6-8) in thickness. Two geometries provide upper and lower estimates of the uncertain amount of material described in the map. They are conservative estimates of uncertainties about material thicknesses and density, and they compare to the best assessment that is compatible both with direct measurements and existing drawings. The resulting relative uncertainty for singly charged MMs ($|q| = q_D$) is in the order of 10% [\[30\]](#page-5-22). The uncertainty increases with electric and magnetic charges. For doubly charged MMs $(|g| = 2g_D)$ the uncertainty is around 10–20% for masses around 1 TeV.

Another source of systematic error is due to a conservative estimate of approximately 1 cm uncertainty in the trapping detector location. Simulations indicate this error is in the range 1–17% [\[30\]](#page-5-22). Additionally, a systematic error arises from the energy-loss uncertainty as a function of β , resulting in a 1–10% relative uncertainty in the acceptance [\[30\]](#page-5-22). Lastly, the error on the reduced etch rate, p, [\[53\]](#page-6-2) leads to an error in the threshold value for the detection of plastic and an error in the variation of efficiency with angle. All the sources of (uncorrelated) systematic uncertainties on the overall efficiency of detection mentioned above were added in quadrature and included in the final limit calculation.

FIG. 3. 95% C.L. upper limits to the cross-section for the following production mechanisms: (Top Left) a DY model with virtual γ/Z^0 exchange for spin-1/2 production of HECOs with charge in the range 100e–225e; (Top Right) PF production of HECOs with charge q in the range $100e-225e$; (Bottom Left) a DY model with virtual photon spin-1/2 production of MMs with magnetic charge in the range $1g_D-Gg_D$; and (Bottom Right) PF production of MMs with magnetic charge in the range $1g_D-6g_D$. The solid lines denote the cross-section predictions for each case considered.

			Magnetic charge (g_D)														
	Spin Process		$1 \quad 2$			5	6				10						
		95% CL mass limits (GeV)															
0	DY	1450 1660 1730 1680 1590 1510 1380 1210 980									790						
1/2	DY	2070 2300 2370 2360 2300 2200 2030 1810 1470 1040															
	DY	2180 2410 2510 2520 2460 2370 2240 2090 1870 1550															
0	$\gamma\gamma$							2980 3210 3250 3200 3100 2950 2750 2500									
1/2	$\gamma\gamma$							3210 3430 3490 3430 3320 3200 3020 2700 2510									
	$\gamma\gamma$							3620 3850 3890 3820 3710 3570 3400 3180 2790									

TABLE I. 95% CL mass limits for the magnetic monopole search.

No MM or HECO candidates were found after exposure of the MoEDAL detector to 6.46 fb⁻¹ of pp collisions at a center-of-mass energy of 13 TeV during LHC's Run-2. Consequently, MoEDAL placed 95% confidence level (CL) lower mass limits on spin-1, spin-1/2 and spin-0 MM and HECO production. A complete set of limit curves for all HIP charge and mass points considered is included in the supplemental material [\[53\]](#page-6-2).

Examples of the limit curves obtained for spin- $\frac{1}{2}$ HECOs produced via γ/Z^0 exchange and photon-fusion, with charges ranging from $100e-225e$, are given in Fig. [3](#page-3-0) (top left) and (top right), respectively. In the MM case, the example limit curves for MMs produced via DY and

photon-fusion with charge from $1g_D$ to $6g_D$ are shown in Fig. [3](#page-3-0) (bottom left) and (bottom right), respectively.

The results of this MoEDAL search for MMs at the LHC reached a sensitivity to DY production cross-section in the range of approximately 1 fb to 5 pb. The mass limits as high as ∼ 2.5 TeV were placed on magnetic charges up to $10q_D$. The corresponding 95% CL mass limits were placed on MMs produced via photon-fusion for: i) crosssection in the range of approximately 1 fb to 5 pb; ii) magnetic charge reaching up to $9g_D$; and iii) MM mass as high as ∼ 3.4 TeV. MoEDAL's lower mass limits are summarized in Table [I.](#page-3-1) A sample of the curves obtained for MMs produced by DY and photon-fusion are given in

TABLE II. 95% CL mass limits for the HECO search.

			Electric charge (e)															
	Process/ exchange	5	-10	15	20	25	50	75	100	125	150	175	200	225	-250	275	300	325 350
			95% CL mass limits (GeV)															
	DY γ		80	220	400		580 1300 1390 1420 1430 1430 1410 1390 1370 1340 1290 1210 1070 900											
1/2	DY γ		290	620			920 1190 1850 1940 1980 2000 2000 1980 1940 1900 1830 1740 1610 1380											
1/2	$DY \gamma/Z^*$		320	620			930 1170 1840 1930 1970 1990 1980 1970 1940 1900 1840 1740 1620											
	DY γ	$\qquad \qquad -$	330	640			960 1240 2020 2120 2170 2180 2180 2170 2140 2100 2060 1980 1850 1620											
θ	$\gamma\gamma$	440					910 1450 1880 2180 2710 2760 2770 2750 2710 2650 2590 2510 2390 2210 2020											
1/2	$\gamma\gamma$						-1110 1750 2180 2480 2980 3030 3030 2990 2940 2880 2810 2710 2580 2430 2220											
	$\gamma\gamma$						-1600 2320 2730 3010 3360 3390 3380 3340 3300 3240 3160 3100 2980 2630											

Fig. [3](#page-3-0) (bottom left) and (bottom right), respectively.

Interpreting our results as a search for HECOs, we placed 95% CL lower mass limits on the following: i) HECO production via the DY mechanism for HECOs of spin-0, $\frac{1}{2}$ and 1; ii) cross-sections from around 1 fb to 10 pb; iii) electric charges in the range $10e \le |q| \le 350e$; and iv) mass limits ranging up to 2.2 TeV. For spin- $1/2$ HECOS, we also considered DY production via γ/Z^0 exchange. In this case, 95% CL mass limits were placed on HECO production with a cross-section in the range 1 fb to 2 pb; electric charges from 10e to 300e; and mass limits as high as 2.0 TeV. In the case of HECOs produced via photon-fusion, 95% CL lower mass limits were placed on HECOs, with the following properties: spin-1/2, 0 and 1; cross-section in the range 1 fb to 4 pb; electric charges in the range 5e to 350e. The corresponding mass limits, that range up to 3.4 TeV, are tabulated in Table [II.](#page-4-8)

At the LHC, ATLAS is the only other experiment to have published searches for MMs and HECOs [\[35\]](#page-5-23) based on DY production of MMs or HECOs and, much more recently, on PF and DY production [\[40\]](#page-5-12).

MoEDAL's direct limits on the MM and HECO charge are by far the strongest published to date. Importantly, MoEDAL is the sole collider experiment to utilize dedicated detectors able to measure definitively the magnetic charge of the MM and also to be able to calibrate experimentally its detectors for HIPs directly using heavy-ions.

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