

SPS-ME-84-12 (DI-MST)

Measurement of the coupling impedance of the SPS

T. Linnecar, W. Scandale

The head-tail Q-shift arising from the interaction of a dense proton bunch with the reactive part of the transverse impedance of the SPS, was evaluated in the ppbar workshop of 1980<sup>1)</sup>, using the standard broad-band model.

For the mode  $m = 0$ , the result of ref. 1 page 5, can be scaled by the following formula

$$\Delta Q_{HT} = 0.012 * \frac{2.1}{\tau_L} * \frac{270}{p} \frac{I_b}{10^{11}} * \frac{Z_{\perp}}{125}$$

where

$\tau_L$  is the total bunch duration in nS

$p$  is the momentum in GeV/c

$I_b$  is the n of protons in the bunch

$Z_{\perp}$  is the transverse impedance in  $M\Omega m^{-1}$ .

It is also usual to relate the longitudinal and the transverse impedance by the following formula

$$Z_{\perp} = \frac{2C}{b^2 \omega_{rev}} \frac{Z_{//}}{n}$$

where

$c = 3 \times 10^8 \text{ mS}^{-1}$  is the speed of light  
 $\omega_{\text{rev}} = 2\pi f_{\text{rev}}$  is the angular revolution frequency  
 $b$  is the vacuum pipe dimension  
(for the vertical plane  $b = 23 \text{ mm}$ ).

We succeeded in measuring the relative shift of the vertical tune between two bunches, one of which had previously been strongly reduced in intensity, during a storage at 315 GeV/c. The relevant parameters of the three bunches were the following

$p = 315 \text{ GeV/c}$   
 $i_A = 8.22 \cdot 10^{10}$   
 $i_B = 5.0 \cdot 10^9$   
 $i_C = 7.53 \cdot 10^{10}$   
 $\tau_A = \tau_B = \tau_C = 2.4 \text{ n S}$

The vertical tune of each bunch was measured using the Schottky noise detector. The Schottky signal of the less intense bunch B was relatively enhanced by a white noise vertical excitation, gated in time.

The result of the measurement is shown in photo 1. The bunch shapes are shown in photos 2 to 4.

The tune shift between the bunch B and bunch A is

$$\Delta Q_v = 2.65 \cdot 10^{-3}$$

As a consequence one can deduce the following values for the transverse and the longitudinal impedance of the SPS

$$Z_{\perp} = 47.7 \text{ M}\Omega \text{ m}^{-1}$$

$$Z_{\parallel}/n = 11.5 \Omega$$

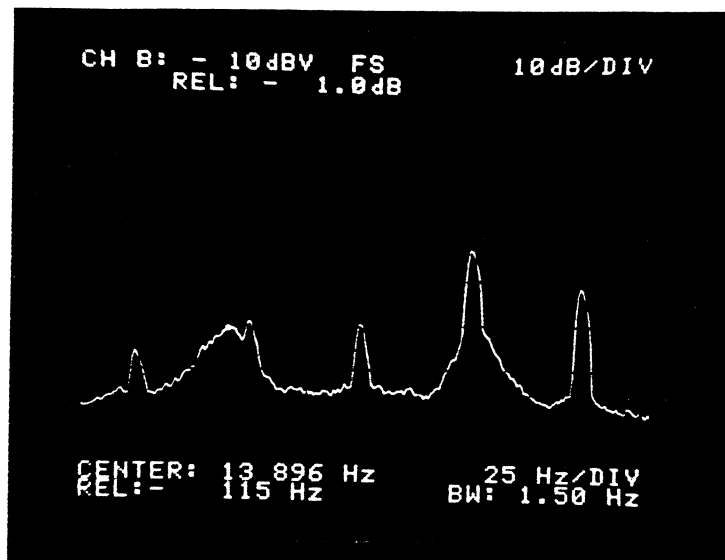


Photo 1

Schottky scan of the vertical tune  
Beam having bunch A of  $8.22 \cdot 10^{10}$  proton bunch B of  $5 \cdot 10^9$  protons

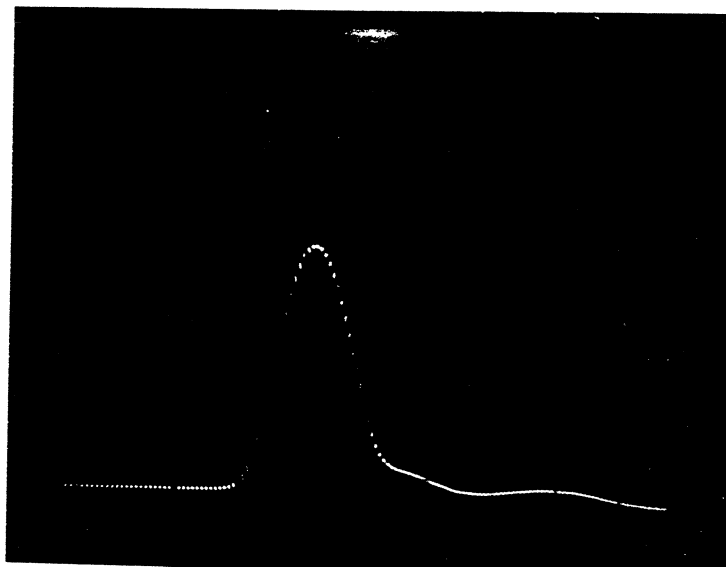


Photo 2

Shape of bunch A (1 nS/div)

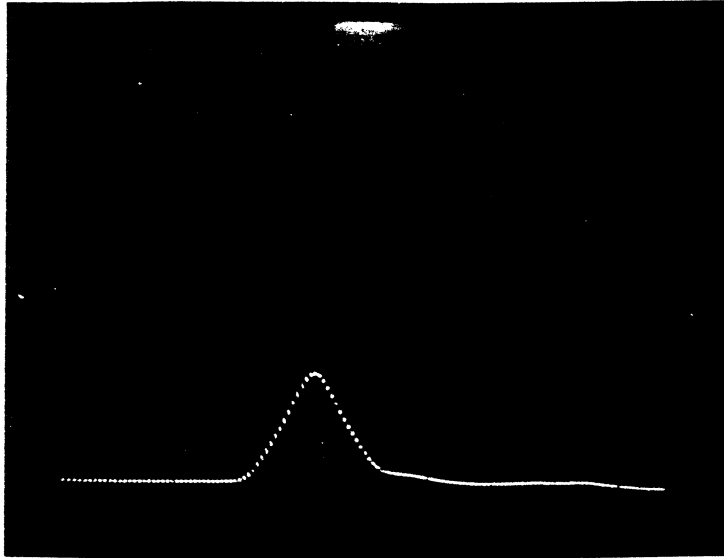


Photo 3

Shape of bunch B (1 nS/div)

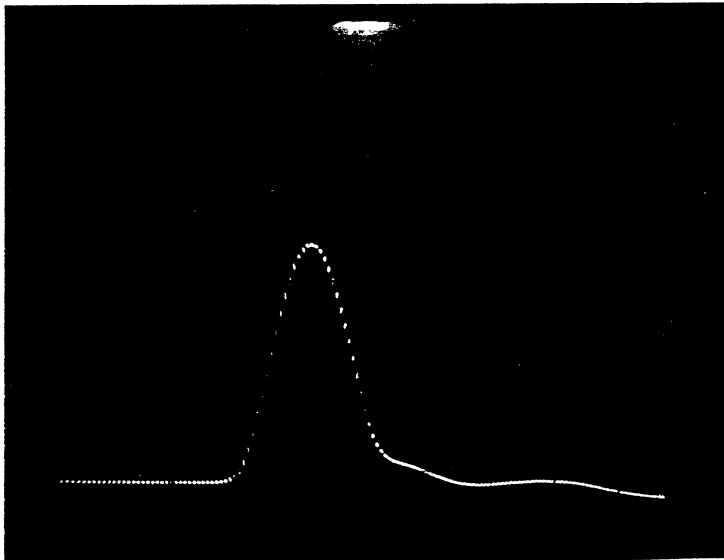


Photo 4

Shape of bunch C (1 nS/div)