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# Physics performance for Dark Matter searches at $\sqrt{s} = 3$ TeV at CLIC using mono-photons and polarised beams.

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## Abstract

At  $e^- e^+$  colliders, Weakly Interacting Massive Particles (WIMPs) are candidates for dark matter (DM) and can be searched for using as tag a photon from initial state radiation. The potential for detecting DM at the Compact Linear Collider (CLIC) is investigated at  $\sqrt{s} = 3$  TeV. The sensitivity of the search is estimated by computing the 95% confidence level upper limit cross section as a function of the dark matter mass. Left-handed (right-handed) polarised  $e^-$  beams increase (decrease) respectively the Standard Model backgrounds and are essential to characterize the WIMPs properties and control the systematic errors. Using right-handed polarised  $e^-$  beams is decreasing significantly the 95% confidence level cross section. Using the ratio of the energy distributions for left-handed and right-handed polarised  $e^-$  beams, systematic errors cancel out. Computing the 95% confidence level upper limit cross section using the ratio requires a model assumption to compute the expected number of signal events. Exclusion limits for dark matter are derived using dark matter Simplified Models for two values of the  $e$ - $e$ -mediator vertex coupling, a mediator width of 10 GeV and for a fixed value of the mediator-DM-DM coupling. For a mediator mass of 3.5 TeV, the measurement of the differential distribution of the significance as a function of the photon energy for the process  $e^- e^+ \rightarrow X X \gamma$  allows the discrimination between different dark matter mediators and the measurement of the WIMP mass to nearly half the centre-of-mass energy. For a 1 TeV WIMP, the mass is determined with a 1% accuracy.

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## 1 Introduction

The Compact Linear Collider (CLIC) is a mature option for a future TeV-scale  $e^- e^+$  collider. CLIC is proposed to run according to a staging scenario with different centre-of-mass energies,  $\sqrt{s}=380$  GeV, 1.5 TeV and 3 TeV. The baseline machine allows for up to  $\pm 80\%$  electron polarisation. The lowest energy stage will concentrate on Higgs and Top physics [1], [2] collecting data corresponding to an integrated luminosity of  $1 \text{ ab}^{-1}$  [3].

At all centre-of-mass energies, Beyond Standard Model (BSM) searches will also be performed, among which are searches for dark matter (DM). The existence of DM has been firmly established through observation of its gravitational effects, but its nature is not established. A widely accepted hypothesis on the form for dark matter is that it is composed of weakly interacting massive particles (WIMPs) that interact only through gravity and the weak force. There are alternative hypotheses that attempt to account for the observations without invoking additional matter. WIMP searches at  $e^- e^+$  colliders are complementary to the direct and indirect searches and to the hadron collider searches. As the WIMP escapes detection, in  $e^- e^+$  collisions the signature is a photon radiated off the initial-state leptons and missing energy. Searches for single and multiphoton final states with missing energy have been performed by LEP experiments [4], [5] [6], [7] and investigated at the International Linear Collider [8]. The main background processes are  $e^- e^+ \rightarrow \nu \bar{\nu} \gamma$  and  $e^- e^+ \rightarrow e^- e^+ \gamma$ . The neutrino background is irreducible, but can be enhanced or reduced by changing the  $e^-$  beam polarisation. Radiative Bhabha scattering has a large cross section and mimics the signal if both leptons are undetected. For the reduction of this background, excellent hermiticity in the forward region of the detector is required. To assess the CLIC physics potential, the 95% confidence level upper limit on the cross section is determined as a function of dark matter mass for different polarisation conditions. The 95% confidence level upper limit cross section as a function of dark matter mass is then used to derive exclusion limits in the framework of dark matter Simplified Models (DMSMs) [9], [10], [11]. Simplified models are designed to grab the basic details of collider phenomenology found in rigorously-derived theories of new physics, without the complexity of the full theory. They are used to compare hadron and lepton collider physics potential. These simplified models assume that DM is a Dirac fermion  $X$  and there is an additional heavy particle mediating the SM-DM interaction, the “mediator  $Y$ ”. In the most basic set of these models, the mediator is a vector, an axial-vector, a scalar or a pseudo-scalar boson. In this study, CLICdp focused on the subset of the models where the mediator is exchanged in the s-channel. In the presence of the signal, using the photon energy distribution, the distribution of the significance  $Z$  as a function of  $E_\gamma$ ,  $dZ/dE_\gamma$  is computed for pseudo-data and for different mediator templates coupling to dark matter. The  $\chi^2$  between the significance of pseudo-data and templates is computed. It is used to discriminate among different mediator hypotheses and to determine the dark matter mass.

## 2 Dark Matter exclusion limits at 3 TeV

### 2.1 Event simulation and selection at 3 TeV

Cross-section calculation and event generation are done using the WHIZARD 2 program [12]. The cross sections are calculated at 3 TeV without and with  $e^-$  beam polarisation. Beamstrahlung effects on the luminosity spectrum are included using results of the CLIC beam simulation for the 3 TeV accelerator parameters. There are three sources of the centre-of-mass energy spread: the momentum spread in the linac, the beamstrahlung which creates a long tail, and initial state radiation (ISR). The first two are collectively referred to as “luminosity spectrum”. The luminosity spectrum is obtained from the GuineaPig [13] beam simulation, it is interfaced to WHIZARD using circe2 [12]. The standard procedure to take ISR effects into account when generating events with WHIZARD is to use the built-in lepton ISR structure function which includes all orders of soft and soft-collinear photons as well as up to the third

order in high-energy collinear photons. However, this approach allows only for a proper modelling of the kinematics of the hard scattering, but is not suitable when we expect photons to be detected in the experiment. For proper description of the photon kinematics, hard non-collinear photon emission should be included in the generation of the background processes on the matrix element level. To obtain a realistic distribution of the photon polar angle, up to three photons are included in the matrix element. Events with ISR photons emitted in the same kinematic region as matrix element (ME) photons are rejected using a merging procedure [14]. Table 1 shows the integrated luminosity ( $L$ ) assumptions at  $\sqrt{s}=3$  TeV for different beam polarisation conditions. It shows also the cross sections of the two main Standard Model processes for different beam polarisation conditions requiring  $P_{t\gamma}/\sqrt{s} > 0.02$ ,  $10^\circ < \theta_\gamma < 170^\circ$  and without ISR/ME merging cut.  $\theta_\gamma$  and  $P_{t\gamma}$  are the polar angle and the transverse momentum of the photon respectively.  $P_{e^-}$  is the longitudinal degree of polarisation of the  $e^-$  beam,  $P_{e^-} > 0$  (right-handed polarisation) No additional selection cut is applied for the cross section calculation and event generation. The ISR/ME merging efficiency is 70% for  $\nu \bar{\nu} \gamma$  and 69% for  $e^- e^+ \gamma$ .

Table 1: Cross sections of main Standard Model background processes at  $\sqrt{s} = 3$  TeV

Polarisation	No	$P_{e^-}, P_{e^+}$ -80, 0	$P_{e^-}, P_{e^+}$ +80, 0
Integrated luminosity ( $L$ )	5 ab $^{-1}$	4 ab $^{-1}$	1 ab $^{-1}$
$\sigma(e^- e^+ \rightarrow \nu \bar{\nu} \gamma (\gamma))$ [fb]	$1.06 \times 10^3$	$1.88 \times 10^3$	$2.35 \times 10^2$
$\sigma(e^- e^+ \rightarrow e^- e^+ \gamma (\gamma))$ [fb]	$1.92 \times 10^3$	$1.96 \times 10^3$	$1.89 \times 10^3$

A fast simulation is used to compute the expected  $e^- e^+ \rightarrow \nu \bar{\nu} \gamma (\gamma)$  and  $e^- e^+ \rightarrow e^- e^+ \gamma (\gamma)$  backgrounds. To take into account the detector resolution, the momentum and energy of the particles are randomly modified using Gaussian resolution parameters according to the particle type. Table 2 shows the angular coverage of the different detectors used for the analysis, the simulation parameters and parameter values used for the fast simulation of electrons and photons.  $\theta$  is the polar angle of the particle, electron or photon. The parameter values are obtained from full simulation studies. Details about CLIC event simulation and detector performance can be found in [15], [16] and methods of the background simulation and electron reconstruction are described in [17] and [18].

Table 2: Detector regions, simulation parameters and efficiencies at  $\sqrt{s} = 3$  TeV

Detector	Angular region mrad	Particle	$E_{min}$ GeV	$\sigma(E)/E$ $E$ [GeV]	$\varepsilon_D$ %
BeamCal	$15 < \theta < 40$	e, $\gamma$	1000	0.1	$f(E, \theta)$
LumiCal	$40 < \theta < 100$	e, $\gamma$	500	$0.8/\sqrt{E}$	99
Ecal No tracking	$100 < \theta < 175$	e, $\gamma$	50	$0.2/\sqrt{E}$	99
Ecal and tracking	$\theta > 175$	e	20	F(1)	99.5
Ecal and tracking	$\theta > 175$	$\gamma$	20	$0.17/\sqrt{E}$	99

$E_{min}$  is the minimum energy required to compute the energy of the particle and apply a detection efficiency.  $\sigma(E)/E$  is the energy resolution, and  $\varepsilon_D$  is the detection efficiency. In the BeamCal,  $\sigma(E)/E = 0.1$  [GeV] and the detection efficiency is a function of the energy and of the angle of the particle. The efficiency  $f(E, \theta)$  is computed using the ElectronEfficiency library developed for the CLIC CDR [19]. In the LumiCal,  $\sigma(E)/E = 0.8/\sqrt{E}$  [GeV] and the detection efficiency is  $\varepsilon_D=99\%$ . In the Ecal region without tracking system,  $\sigma(E)/E = 0.2/\sqrt{E}$  [GeV] and the detection efficiency is  $\varepsilon_D=99\%$ . In the "signal region",  $10^\circ < \theta < 170^\circ$ , the energy resolution and the detection efficiency are different

for electrons and photons. For the electrons, the momentum resolution function is:

$$\frac{\sigma(P)}{P} \approx a \cdot P \oplus b \cdot \frac{1}{\sqrt{\sin \theta}} \oplus c \cdot \frac{\cos \theta}{\sin \theta}, \quad (1)$$

the parameter  $a$ ,  $b$  and  $c$  represents the contribution from the curvature measurement, from the multiple-scattering and from the angular resolution respectively. The values were obtained by fitting the  $P_T$  resolution of fully simulated charged particle data as a function of the  $P_T$  [15]. For  $\theta = 90^\circ$ ,  $a = 2.0 \times 10^{-5}$  [GeV $^{-1}$ ],  $b = 2.0 \times 10^{-3}$  and  $c = 2.0 \times 10^{-4}$ . For tracks measured in the tracker barrel  $\theta > 40^\circ$  and  $\theta < 140^\circ$  parameter  $a$  is independent of  $\theta$ . For tracks measured in the end cap disks the path length  $L$  depends on  $\theta$  and therefore  $a$  depends on  $\theta$ . The detection efficiency is  $\varepsilon_D=99.5\%$ . For the photons,  $\sigma(E)/E = 0.17/\sqrt{E}$  [GeV] and the detection efficiency is  $\varepsilon_D=99\%$ . With these parameters, listed in Table 2, the fake rate due to beam-induced backgrounds, is well below  $10^{-4}$  in all detector regions.

The mono-photon selection requires an isolated photon with an energy greater than 60 GeV in the signal region and little energy in the other parts of the detector. This selection includes:

- A photon isolation selection based on the observable  $E_i$  defined as:

$$E_i = |E_{Tr} - E_\gamma|/E_{Tr}. \quad (2)$$

$E_\gamma$  is the photon energy and  $E_{Tr}$  is the energy sum of the particles in a cone of width  $\Delta R=0.4$  around the photon direction with

$$\Delta R = \sqrt{\Delta\eta^2 + \Delta\phi^2}. \quad (3)$$

- A missing energy selection requiring little energy in addition to the photon energy

$$E_o = |E_{Tot} - E_\gamma|/E_{Tot}. \quad (4)$$

$E_{Tot}$  is the total energy of the event.

When there are several photons in the signal region the photons are sorted by energy. The energy of the most energetic photon is considered to be the energy  $E_\gamma$  of the signal photon and  $E_\gamma$  is randomly modified using the photon energy resolution of the signal region. The particles outside the signal region cannot be identified and are considered as electrons. To compute  $E_{Tr}$  and  $E_{Tot}$ , the energy of the remaining particles are considered if their energy is greater than  $E_{min}$ . For all these particles the energy is randomly modified using the energy resolution of the detector region where the particle is detected and the detection efficiency is taken into account when computing  $E_{Tr}$  and  $E_{Tot}$ . Figure 1(a) shows for the process  $e^- e^+ \rightarrow \nu \bar{\nu} \gamma (\gamma)$ , the distribution  $dN/dE_i$  of the observable  $E_i$  used for the photon isolation selection. The events with  $E_i > 0.01$  are events for which the energy of an additional photon is measured in the cone around the high energy signal photon. Figure 1(b) shows the distribution  $dN/dE_o$  of the observable  $E_o$  used for the missing energy selection. The events with  $E_o > 0.1$  are events for which the energy of an additional photon is measured, either in the signal region or outside the signal region. Figure 2(a) and Figure 2(b) show the same distributions  $dN/dE_i$  and  $dN/dE_o$  for the process  $e^- e^+ \rightarrow e^- e^+ \gamma (\gamma)$ . The events with  $E_o > 0.1$  are events for which the energy of an additional photon or electron is measured, either in the signal region or outside the signal region. Taking into account the high energy required for the signal photon,  $E_\gamma > 60$  GeV and the low beam-induced fake rate in all detection regions, potential energy deposits originating from beam-induced background are neglected when computing the mono-photon selection efficiency. Table 3 shows for the two main SM backgrounds  $e^- e^+ \rightarrow \nu \bar{\nu} \gamma (\gamma)$  and  $e^- e^+ \rightarrow e^- e^+ \gamma (\gamma)$ , the selection efficiencies of the photon isolation cut  $E_i$  and of the missing energy

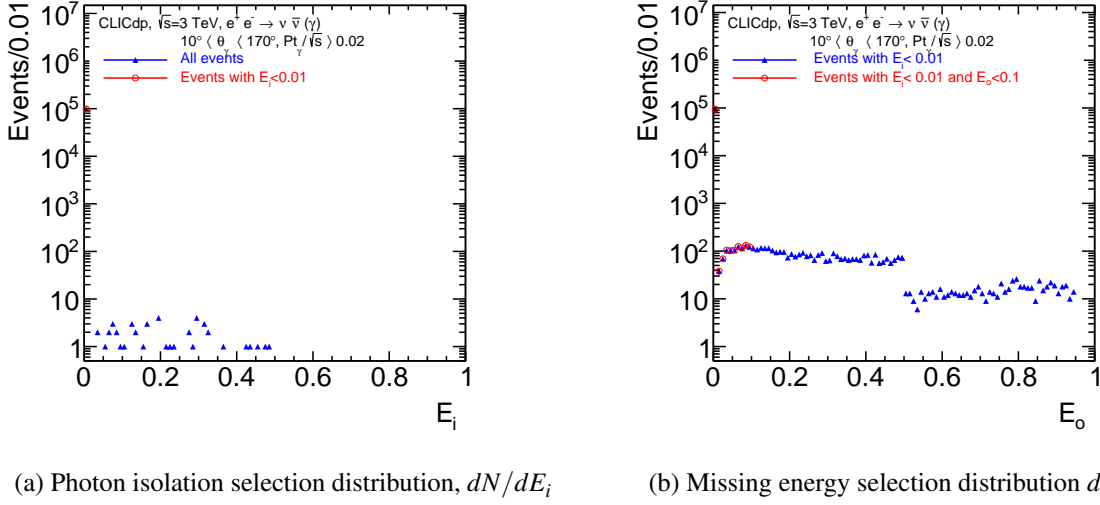


Figure 1: Mono-photon selection for the process  $e^- e^+ \rightarrow \nu \bar{\nu} \gamma (\gamma)$  (a) Photon isolation selection distribution  $dN/dE_i$  (b) Photon missing energy selection distribution  $dN/dE_o$

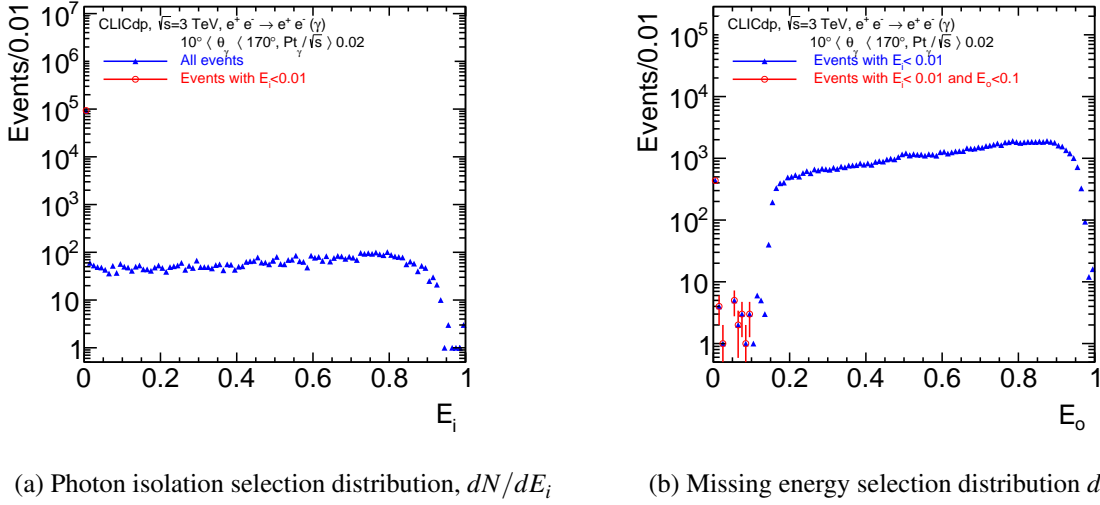


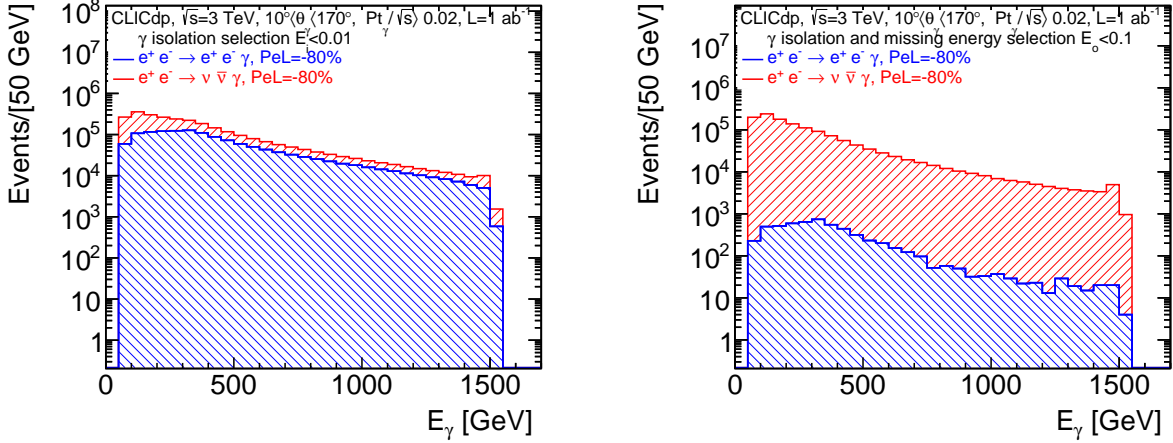
Figure 2: Mono-photon selection for the process  $e^- e^+ \rightarrow e^- e^+ \gamma (\gamma)$  (a) Photon isolation selection distribution  $dN/dE_i$  (b) Photon missing energy selection distribution  $dN/dE_o$

Table 3: Selection cuts and selection efficiencies of the two main SM backgrounds

Cut name	Cut value	Process	Process
		$e^- e^+ \rightarrow \nu \bar{\nu} \gamma (\gamma)$	$e^- e^+ \rightarrow e^- e^+ \gamma (\gamma)$
$E_i$	$E_i < 0.01$	Selection efficiency	Selection efficiency
		0.99	0.935
$E_i$ and $E_o$	$E_i < 0.01$ and $E_o < 0.1$	Selection efficiency	Selection efficiency
		0.95	$4.6 \times 10^{-3}$

selection cut  $E_o$ . The selection efficiencies for left-handed 80% polarised  $e^-$  beam and for right-handed 80% polarised  $e^-$  beam are the same.

Figure 3(a) shows for a left-handed 80% polarised  $e^-$  beam (PeL), the stacked histogram of the photon energy distribution of  $e^- e^+ \rightarrow \nu \bar{\nu} \gamma(\gamma)$  and  $e^- e^+ \rightarrow e^- e^+ \gamma(\gamma)$  events selected using the photon isolation selection  $E_i < 0.01$ . The number of events corresponds to an integrated luminosity of  $1 \text{ ab}^{-1}$ . Figure 3(b) shows the photon energy distribution for events selected using the photon isolation selection



(a)  $dN/dE_\gamma$  spectrum with photon isolation selection  $E_i < 0.01$

(b)  $dN/dE_\gamma$  spectrum with photon isolation selection  $E_i < 0.01$  and missing energy selection  $E_o < 0.1$

Figure 3: Left-handed 80% polarised electron beam  $e^- e^+ \rightarrow \nu \bar{\nu} \gamma(\gamma)$  and  $e^- e^+ \rightarrow e^- e^+ \gamma(\gamma)$  events with mono-photon selection (a) with photon isolation selection  $E_i < 0.01$  (b) with photon isolation selections  $E_i < 0.01$  and missing energy selection  $E_o < 0.1$

$E_i < 0.01$  and the missing energy selection  $E_o < 0.1$ .

Figure 4(a) shows for a right-handed 80% polarised  $e^-$  beam (PeR), the stacked histograms of the photon energy distribution of  $e^- e^+ \rightarrow \nu \bar{\nu} \gamma(\gamma)$  and  $e^- e^+ \rightarrow e^- e^+ \gamma(\gamma)$  events selected using the photon isolation selection  $E_i < 0.01$ . Figure 4(b) shows the photon energy distribution for events selected using the photon isolation selection  $E_i < 0.01$  and the missing energy selection  $E_o < 0.1$ .

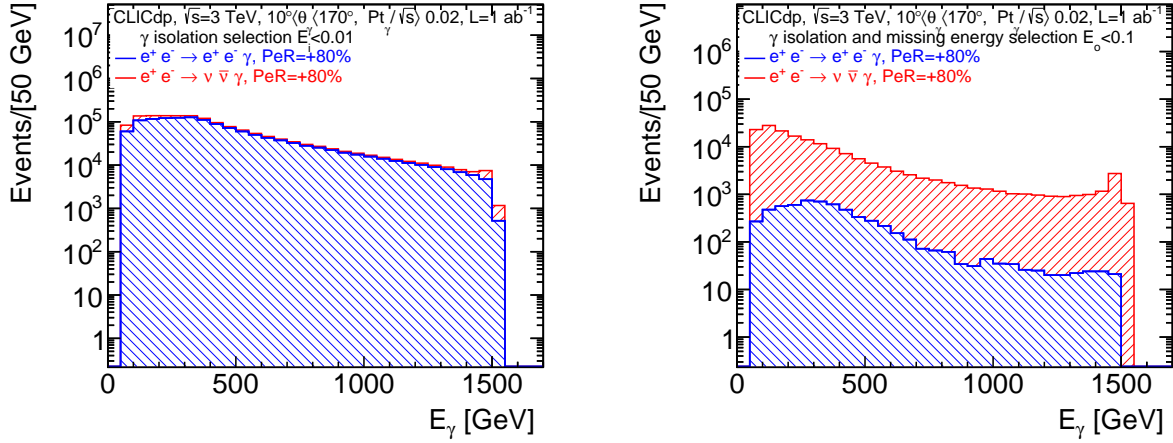
## 2.2 95% confidence level upper limit cross section calculation

The photon energy distributions, with photon isolation and missing energy selection, shown in Figure 3(b) and 4(b), together with the systematic uncertainties listed in Table 4 are input to the 95% confidence level upper limit cross section calculation for the DM signal observation. The 95% con-

Table 4: Main systematic uncertainties at  $\sqrt{s} = 3 \text{ TeV}$

Systematic error source	value
$\nu \bar{\nu}(\gamma)$ event selection	$2.0 \times 10^{-3}$
$e^+ e^-(\gamma)$ event selection	$5.0 \times 10^{-5}$
Luminosity measurement	$2.0 \times 10^{-3}$
Polarisation measurement	$2.0 \times 10^{-3}$

idence level upper limit cross sections are computed using the ratio of confidences in the signal plus background to background hypothesis, so called ‘‘CLS’’ method [20]. For a counting experiment with a



(a)  $dN/dE_\gamma$  spectrum with photon isolation selection  $E_i < 0.01$  (b)  $dN/dE_\gamma$  spectrum with photon isolation selections  $E_i < 0.01$  and missing energy selection  $E_o < 0.1$

Figure 4: Right-handed 80% polarised electron beam  $e^- e^+ \rightarrow \nu \bar{\nu} \gamma (\gamma)$  and  $e^- e^+ \rightarrow e^- e^+ \gamma (\gamma)$  events with mono-photon selection (a) with photon isolation selection  $E_i < 0.01$  (b) with photon isolation selections  $E_i < 0.01$  and missing energy selection  $E_o < 0.1$

single channel

$$CL_s = \frac{CL_{s+b}}{CL_b} = \frac{\sum_{n=0}^b \frac{e^{-(b+s)} (b+s)^n}{n!}}{\sum_{n=0}^b \frac{e^{-b} b^n}{n!}}, \quad (5)$$

where  $b$  is the number of background events and  $s$  is the number of signal events. For the process  $e^- e^+ \rightarrow X X \gamma$ , the angular distribution of the photon is independent of the process but the photon energy spectrum depends on the dark matter mass. To compute the 95% confidence level upper limit cross section as a function of the dark matter mass  $m_X$ , for each  $m_X$  value, the number of background events  $b$  is computed using

$$b = \int_{E_\gamma \min}^{E_\gamma \max} \frac{\partial N}{\partial E_\gamma} dE_\gamma, \quad \text{with } E_\gamma \min = 60 \text{ GeV and } E_\gamma \max = \sqrt{s}/2 - m_X^2/\sqrt{s}. \quad (6)$$

$CL_s(PeR)$ ,  $CL_s(PeL)$  and  $CL_s(PeNo)$  are computed for right-handed, left-handed 80% polarised beams and without polarisation ( $PeNo$ ). The number of signal events excluded at 95% CL,  $s_{exc}$ , is obtained for  $CL_s \geq 0.05$ . To derive the limits using the right-handed and left-handed polarised photon energy distributions, for each  $m_X$  value, the ratio  $R_b$  and the error  $\sigma(R_b)$  are computed,

$$R_b = \frac{b(PeL)}{b(PeR)}, \quad (7)$$

where  $b(PeL)$  and  $b(PeR)$  are the number of background events for left-handed and right-handed polarised beams, respectively. The ratio  $R_{b+s}$  is computed using

$$R_{b+s} = \frac{(b+s)(PeL)}{(b+s)(PeR)}. \quad (8)$$

The expressions  $(b+s)(PeL)$  and  $(b+s)(PeR)$  are the number of background plus signal events for left-handed and right-handed polarised beams respectively and assuming the polarisation dependence

of dark matter Simplified Models. The number of signal events excluded at 95% CL,  $s_{exc}$ , is obtained for  $R_b - R_{b+s} \geq 2 \times \sigma(R_b)$ . The 95% confidence level upper limit cross sections are  $\sigma(95\%) = s_{exc}/L$ , where  $L$  is the integrated luminosity corresponding to the polarisation condition. Figure 5 shows the 95% confidence level upper limit cross section as a function of the dark matter mass for different polarisation and luminosity conditions, left-handed 80% polarised  $e^-$  beam, right-handed 80% polarised  $e^-$  beam, using the ratios  $R_b$  and  $R_{b+s}$  for left-handed and right-handed 80% polarised  $e^-$  beams and without polarisation. The lowest 95% confidence level upper limit cross section is obtained using the ratios  $R_b$  and  $R_{b+s}$  for left and right-handed polarised  $e^-$  beams. The method using the ratios  $R_b$  and  $R_{b+s}$  is model dependant.

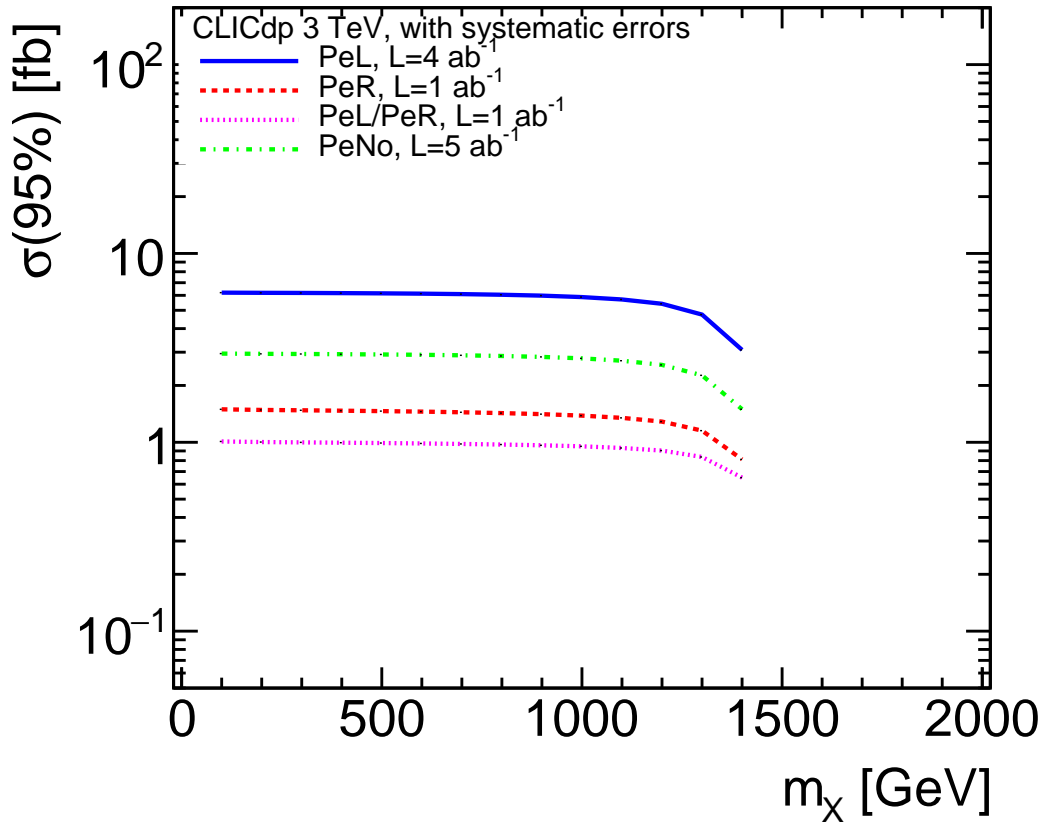


Figure 5: 95% confidence level upper limit cross section as a function of dark matter mass for different polarisation and luminosity conditions.

### 2.3 Exclusion limits in simplified dark matter models

In this study CLICdp focused on a subset of simplified dark matter models where the mediator is exchanged in the s-channel. The parameters of these models are the DM mediator  $Y$  type, vector (v) or axial-vector(a-v) or scalar(s), the mediator mass  $m_Y$ , the e-e-mediator vertex coupling  $geY$ , the DM mass  $m_X$ , and the mediator-DM-DM vertex coupling  $gYX$ . For the cross section calculation the mediator width is fixed to 10 GeV. Limits are derived in the  $(m_Y, m_X)$  plane using  $\sigma(95\%)$  computed with  $R_b - R_{b+s}$ . In the plane  $(m_Y, m_X)$ , in many points, the expected cross sections are computed. For each mediator mass  $m_Y$ , the limit in  $m_X$  is the point where the cross section  $\sigma(m_Y, m_X) \geq \sigma(95\%)$ . To compute the expected signal cross section, in each mass point, requires generating events and applying the same event



selection as for the radiative neutrino events. This is very time consuming, therefore a simplified method was considered. In the simplified method the signal cross section is calculated using the beam spectrum, the ISR function, one (ME) photon on which the generator cuts are applied, but no ISR merging cut is applied. For the same points the signal cross section is also computed using the same procedure as for the radiative neutrino events. Applying the simplified method leads to cross sections which are underestimated by 3% to 4% depending on the mass point. This leads to mass limits which are overestimated by 20 to 30 GeV. Figure 6(a) shows, in the mass plane ( $m_Y, m_X$ ), the exclusion limits computed for vector, axial-vector and scalar mediators with a coupling  $geY=1$  and using the simplified cross section calculation. For a light WIMP mass the exclusion range extends up to 9 TeV, and WIMP masses close to half the centre-of-mass energy can be measured for a large range of mediator masses.

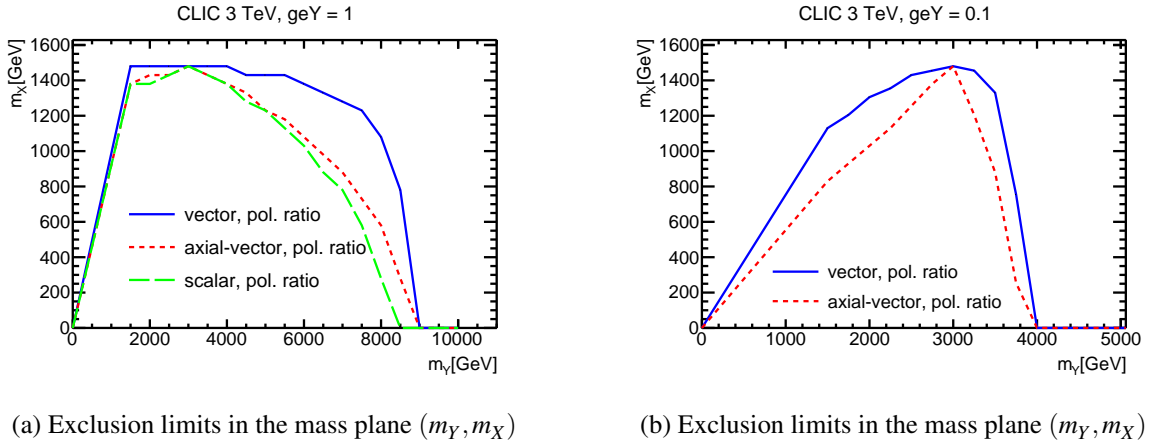


Figure 6: Exclusion limits in the mass plane ( $m_Y, m_X$ ) using the ratios  $R_b$  and  $R_{b+s}$  and an integrated luminosity of  $1 \text{ ab}^{-1}$  (a)  $geY=1$  (b)  $geY=0.1$

Figure 6(b) shows, in the mass plane ( $m_Y, m_X$ ), the exclusion limits computed for vector and axial-vector mediators with a coupling  $geY=0.1$ . For a light WIMP mass the exclusion range extends up to 4 TeV, and WIMP masses of 1 TeV can be measured for mediator masses up to 3.5 TeV.

### 3 Model discrimination and dark matter mass determination

The model discrimination study and dark matter mass determination is done using the simplified dark matter models with the following parameters:

- DM mediator, v or a-v with  $m_Y=3.5 \text{ TeV}$  and  $\Gamma_Y=10 \text{ GeV}$ ;
- Coupling  $geY=1$  or  $0.5$ ;
- DM mass  $m_X$  in the range between 200 GeV and 1.4 TeV;
- Coupling  $gYX=1$ .

As can be seen on Figure 6(b), a mediator mass  $m_Y=3.5 \text{ TeV}$  is close to the exclusion limit, it leads to a challenging benchmark point.

#### 3.1 Signal significance calculation

Figure 7(a) shows, for background events, the ratio  $dR_B/dE_\gamma$  of the photon energy distributions for left-handed polarised  $e^-$  beam over right-handed polarised  $e^-$  beam. It shows also, for pseudo data events

(background plus signal), the ratio  $dR_D/dE_\gamma$  of the photon energy distributions for left-handed polarised  $e^-$  beam over right polarised  $e^-$  beam. The signal events correspond to a vector mediator of mass  $m_\gamma=3.5$  TeV with a coupling  $geY=1$  and a dark matter mass of 1 TeV.

$$\frac{dR_B}{dE_\gamma} = \frac{[dN_B/dE_\gamma]_{PeL}}{[dN_B/dE_\gamma]_{PeR}}, \quad \frac{dR_D}{dE_\gamma} = \frac{[dN_D/dE_\gamma]_{PeL}}{[dN_B/dE_\gamma]_{PeR}}, \quad (9)$$

where  $dN_B/dE_\gamma$  is the photon energy distribution of background events, and  $dN_D/dE_\gamma$  is the photon energy distribution of pseudo-data events.

From these two distributions, the energy distribution of the signal events  $dN_S/dE_\gamma$  is

$$\frac{dN_S}{dE_\gamma} = \left[ \frac{dN_B}{dE_\gamma} \right]_{PeR} \left[ \frac{dR_B}{dE_\gamma} - \frac{dR_D}{dE_\gamma} \right] \left[ \frac{dR_D}{dE_\gamma} - 1 \right]. \quad (10)$$

For a discovery, the figure of merit is  $1 - CL_b$ . For a counting experiment with a single channel,  $CL_b$  is computed in each  $E_\gamma$  bin using

$$CL_b = \sum_{n=0}^{n_{obs}} \frac{e^{-(b)} (b)^n}{n!}, \quad (11)$$

where  $b$  is the number of background events,  $b = [dN_B/dE_\gamma]_{PeR}$ , and  $n_{obs}$  is the number of signal plus background events,  $s = dN_S/dE_\gamma$ . The significance  $Z$  is derived

$$Z = \sqrt{2} \cdot \text{Erf}^{-1} [1 - 2(1 - CL_b)]. \quad (12)$$

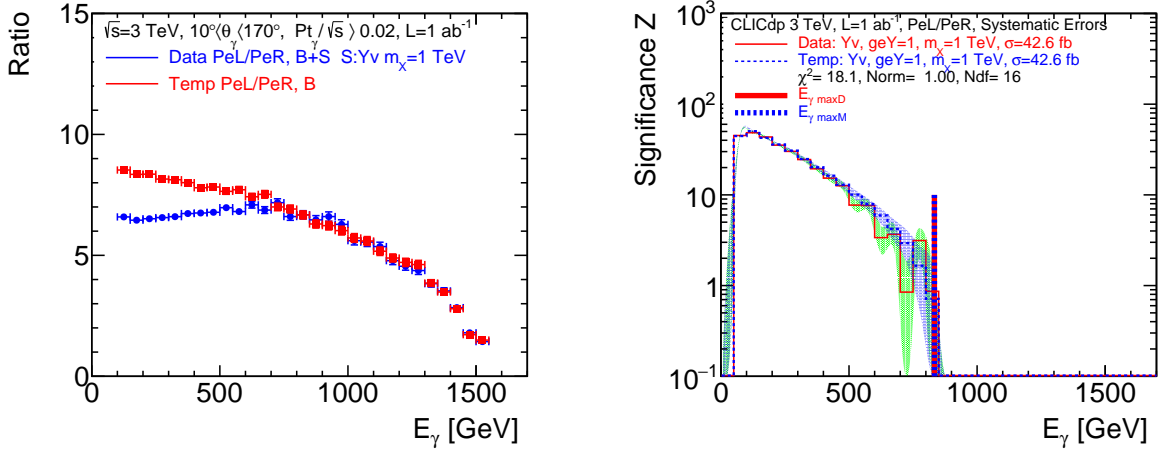
The uncertainty on the significance,  $\delta Z$ , is obtained using Toy Monte Carlo events to generate the distribution  $dN/dZ$ ; a fit of  $dN/dZ$  is performed to extract  $\delta Z$ . Using the same procedure,  $dZ/dE_\gamma$  is computed for different templates (vector, axial-vector) coupling to DM with different DM masses. Figure 7(b) shows the significance  $Z$  as a function of  $E_\gamma$  for a pseudo data sample and a template sample corresponding to a vector mediator of mass  $m_\gamma=3.5$  TeV with a coupling  $geY=1$  and a dark matter mass of 1 TeV; the green band corresponds to  $Z \pm 1\sigma$ . Figure 7(b) shows also the significance  $Z$  as a function of  $E_\gamma$  for a template sample corresponding to a vector mediator of dark matter mass 1 TeV and coupling  $geY=1$ . For the template energy distributions the statistics is  $10\times$  larger, to reduce fluctuations. Before computing the significance distribution of the templates, the energy distributions are weighted to the expected luminosity. To compare the significance of the pseudo-data (ZData) and templates (ZTemp), a  $\chi^2$  fit is performed with:

$$\chi^2 = \sum_{E_\gamma=60\text{GeV}}^{E_\gamma=1400\text{GeV}} \frac{[(ZData(E_\gamma) - ZTemp(E_\gamma))]^2}{[\delta ZTemp(E_\gamma)]^2}. \quad (13)$$

The  $\chi^2$  fit is performed with the normalisation free (shape comparison) or with a normalisation using the pseudo-data and the template cross sections (absolute comparison).

### 3.2 $\chi^2$ fit calculation check

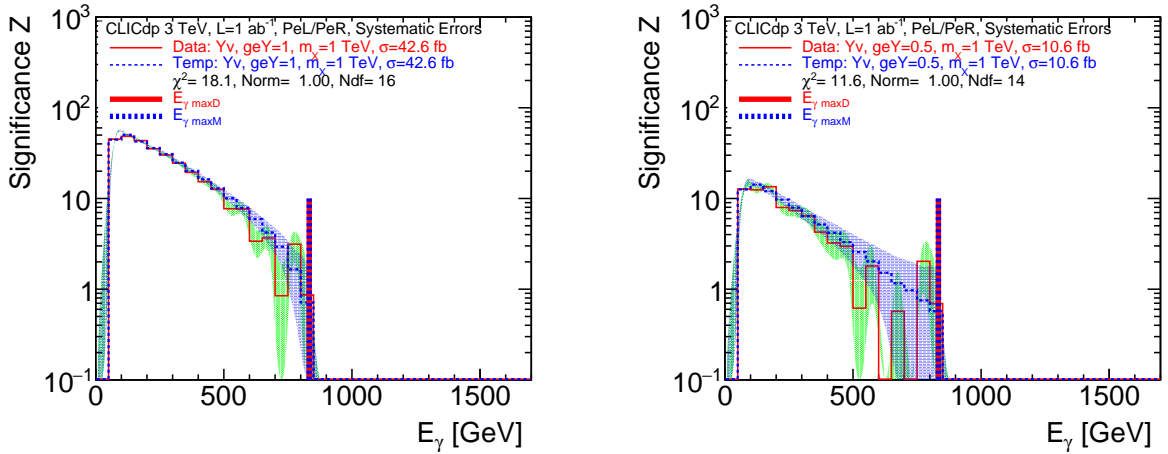
Figure 8(a) shows the significance  $Z$  as a function of  $E_\gamma$  for a pseudo-data sample and a template sample corresponding to a vector mediator coupling to a dark matter of mass 1 TeV. For both samples the coupling  $geY=1$ . The  $\chi^2/Ndf=1.13$ ,  $Ndf$  is the number of degrees of freedom. Figure 8(b) shows the same distributions for pseudo-data and template samples with a coupling  $geY=0.5$ . For a coupling  $geY=0.5$  the cross sections are 4 times lower, the  $\chi^2/Ndf=0.82$ . This check shows that the  $\chi^2/Ndf$  is stable with respect to cross section changes.



(a)  $dR_B/dE_\gamma$  background distribution and  $dR_D/dE_\gamma$  pseudo-data distribution for a vector mediator with  $m_Y=3.5$  TeV and  $m_X=1$  TeV

(b)  $dZ/dE_\gamma$  distributions: pseudo-data: vector mediator,  $m_Y=3.5$  TeV and  $m_X=1$  TeV; template: vector mediator,  $m_Y=3.5$  TeV and  $m_X=1$  TeV

Figure 7: (a) Ratio of, left-handed over right-handed, photon energy distribution for background and for pseudo-data. (b) Pseudo-data and template significance  $dZ/dE_\gamma$  distributions



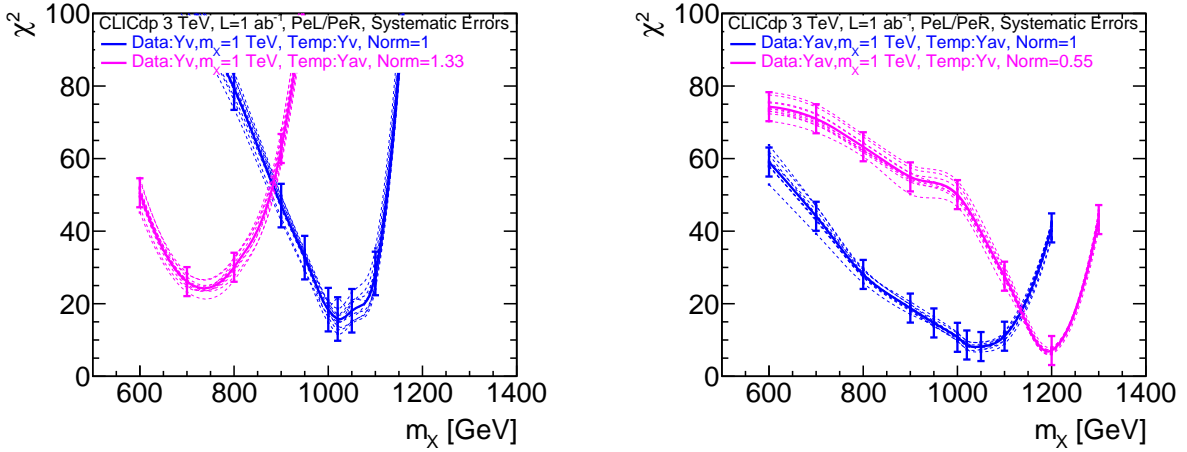
(a)  $dZ/dE_\gamma$  distributions for pseudo-data and template samples with  $geY=1$ .

(b)  $dZ/dE_\gamma$  distributions for pseudo-data and template samples with  $geY=0.5$ .

Figure 8: Pseudo-data and template significance  $dZ/dE_\gamma$  distributions for vector mediators with  $m_Y=3.5$  TeV and  $m_X=1$  TeV; (a)  $geY=1$  (b)  $geY=0.5$

### 3.3 $\chi^2$ fit and model discrimination

Figure 9(a) shows the  $\chi^2$  fit values as a function of the dark matter mass. The blue dotted lines correspond to  $\chi^2$  values computed for vector mediator pseudo-data samples coupling to a dark matter mass of 1 TeV and vector mediator templates coupling to dark matter masses ranging between 200 GeV and 1.4 TeV. Ten vector mediator pseudo-data samples are generated with the same conditions. The blue full line corresponds to an average of the  $\chi^2$  values of the ten samples. The error bars drawn for these points correspond to  $\sigma(\chi^2) = \sqrt{(2.Ndf)}$ . The minimum  $\chi^2$  value is 18 and the normalisation value is 1 for  $m_X$  around 1 TeV. The magenta dotted-lines correspond to  $\chi^2$  values computed for vector mediator pseudo-



(a)  $\chi^2$  fit values as a function of the dark matter mass, pseudo-data: vector mediator with  $m_X=1$  TeV, templates: vector and axial-vector mediator

(b)  $\chi^2$  fit values as a function of the dark matter mass, pseudo-data: axial-vector mediator with  $m_X=1$  TeV, templates: axial-vector and vector mediator

Figure 9:  $\chi^2$  fit values as a function of the dark matter mass,  $m_Y=3.5$  TeV, (a) Pseudo-data, vector mediator with  $m_X=1$  TeV, templates vector and axial-vector mediator (b) pseudo-data, axial-vector mediator with  $m_X=1$  TeV, templates axial-vector and vector mediator

data samples coupling to a dark matter mass of 1 TeV and axial-vector mediator templates coupling to dark matter masses ranging between 200 GeV and 1.4 TeV. Ten axial-vector mediators pseudo-data samples are generated with the same conditions. The magenta full line correspond to an average of the  $\chi^2$  values of the ten samples. The minimum  $\chi^2$  value is 25 and the normalisation value is 1.33 for  $m_X$  around 750 GeV. For the pseudo-data sample and the template samples the coupling is  $geY=1$ . The smallest  $\chi^2$  values corresponds to the right mediator type but the  $\chi^2$  separation is too small to discriminate the vector-vector hypothesis from the vector-axial-vector hypothesis. Taking into account the normalisation allows discarding the vector-axial-vector hypothesis. Different statistical tests are available to compare the shape of the two distributions. The Kolmogorov-Smirnov test was also performed on the same distributions, it leads to the same conclusion, the shape comparison does not allow discriminating between different models. Figure 9(b) shows the same distributions. The blue line and dotted lines correspond to  $\chi^2$  values computed for axial-vector mediator pseudo-data and template samples. The minimum  $\chi^2$  value is 8.6 and the normalisation value is 1 for  $m_X$  around 1 TeV. The magenta line and dotted-lines corresponds to a  $\chi^2$  computed for an axial-vector mediator pseudo-data sample and vector mediator templates. The minimum  $\chi^2$  value is 7.2 and the normalisation value is 0.55 for  $m_X$  around 1.2 TeV. The  $\chi^2$  values are too close to allow the discrimination between the axial-vector-vector hypothesis and the vector-vector hypothesis. Taking into account the normalisation allows discarding the vector-vector hypothesis.

### 3.4 $\chi^2$ fit and dark matter mass determination

Figure 10 shows the  $\chi^2$  fit values as a function of the dark matter mass. The blue dotted line corresponds to a  $\chi^2$  computed for vector mediator pseudo-data samples coupling to a dark matter mass of 1 TeV and vector mediator templates coupling to dark matter masses ranging between 200 GeV and 1.4 TeV. The ten vector mediators pseudo-data samples are all generated with the same conditions. The blue full line correspond to an average of the  $\chi^2$  values of the ten samples. The error bars drawn for these points correspond to  $\sigma(\chi^2) = \sqrt{(2.Ndf)}$ . The minimum  $\chi^2$  value is 15.6 and the normalisation value is 1 for  $m_X$  around 1 TeV. For the pseudo-data samples and the template samples the coupling is  $geY=1$ . The fit

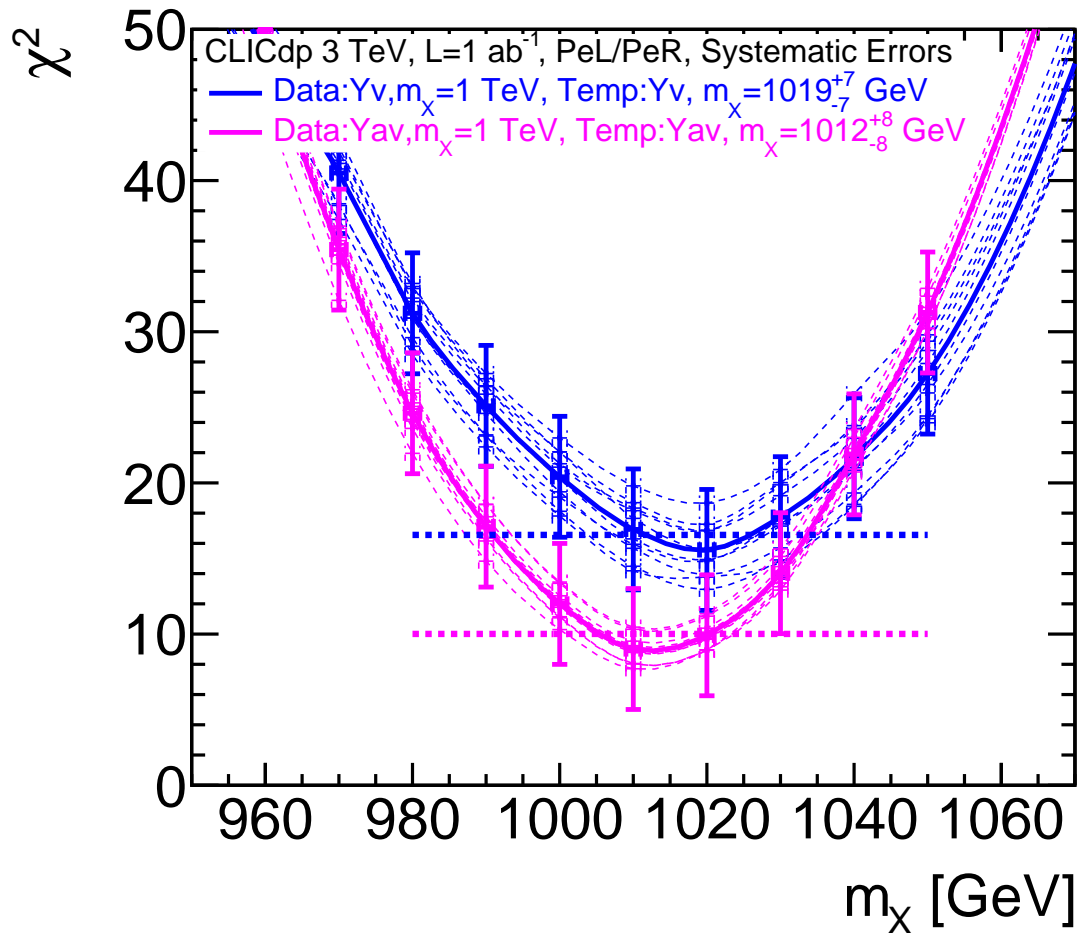


Figure 10:  $\chi^2$  fit values as a function of the dark matter mass for pseudo-data vector and axial-vector mediators with  $m_\gamma=3.5$  TeV and  $geY=1$  coupling to a dark matter mass of 1 TeV

takes into account the shape of the  $dZ/dE_\gamma$  distributions and the cross sections. The minimum value of the  $\chi^2$  gives the mass of the dark matter, the uncertainty on the mass,  $\delta M$ , corresponds to a  $\chi^2$  variation of 1. For the vector-vector hypothesis  $m_X = 1019^{+7}_{-7}$  GeV.

The magenta dotted lines corresponds  $\chi^2$  values computed for a axial-vector mediator pseudo-data samples coupling to a dark matter mass of 1 TeV and axial-vector mediator templates coupling to dark matter masses ranging between 200 GeV and 1.4 TeV. For the pseudo-data sample and the template samples the coupling is  $geY=1$ . Ten axial-vector mediator pseudo-data samples are generated with the same conditions. The magenta full line corresponds to an average of the  $\chi^2$  values of the ten samples. The minimum  $\chi^2$  value is 9.0 and the normalisation value is 1 for  $m_X$  around 1 TeV. For the axial-vector-axial-vector hypothesis  $m_X = 1012^{+8}_{-8}$  GeV.

## 4 Summary

To assess the CLIC physics potential for dark matter searches, the 95% confidence level upper limit on the cross section is computed as a function of the dark matter mass for different polarisation conditions. For simplified dark matter models, the lowest 95% confidence level upper limit cross section is obtained

using the ratios  $R_b$  and  $R_{b+s}$  for left-handed and right-handed polarised  $e^-$  beams. Using the 95% cross section as a function of the dark matter mass, exclusion limits are derived using dark matter Simplified Models. For a coupling  $geY=1$  and a light WIMP mass the exclusion range extends up to 9 TeV. WIMP masses close to half the centre-of-mass energy can be measured for a large range of mediator masses. For a coupling  $geY=0.1$  and a light WIMP mass the exclusion range extends up to 4 TeV, and WIMP masses of 1 TeV can be measured for mediator masses up to 3.5 TeV. To discriminate between different mediator hypotheses coupling to different DM masses,  $\chi^2$  fits of the differential distribution  $dZ/E_\gamma$  of pseudo-data and templates of different mediators coupling to DM with different DM masses are performed. The fit is using the shape of the differential distribution of the significance  $dZ/dE_\gamma$  and the cross sections. It allows also the determination of the dark matter mass and of the uncertainty on the mass. For a dark matter mass of 1 TeV the accuracy on the mass is 1%, without a statistically significant bias.

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