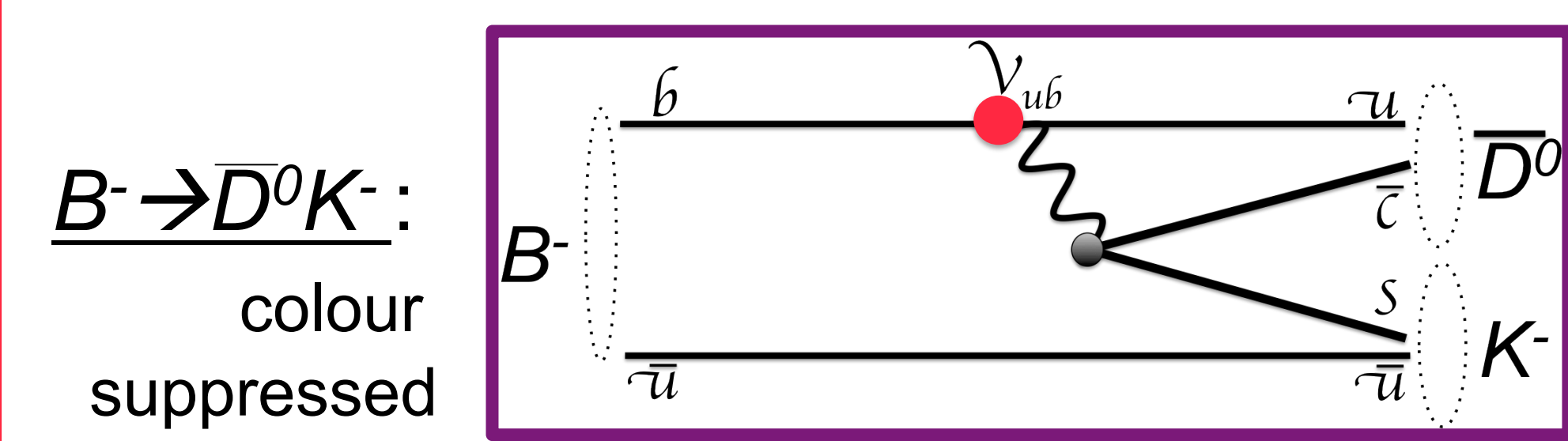
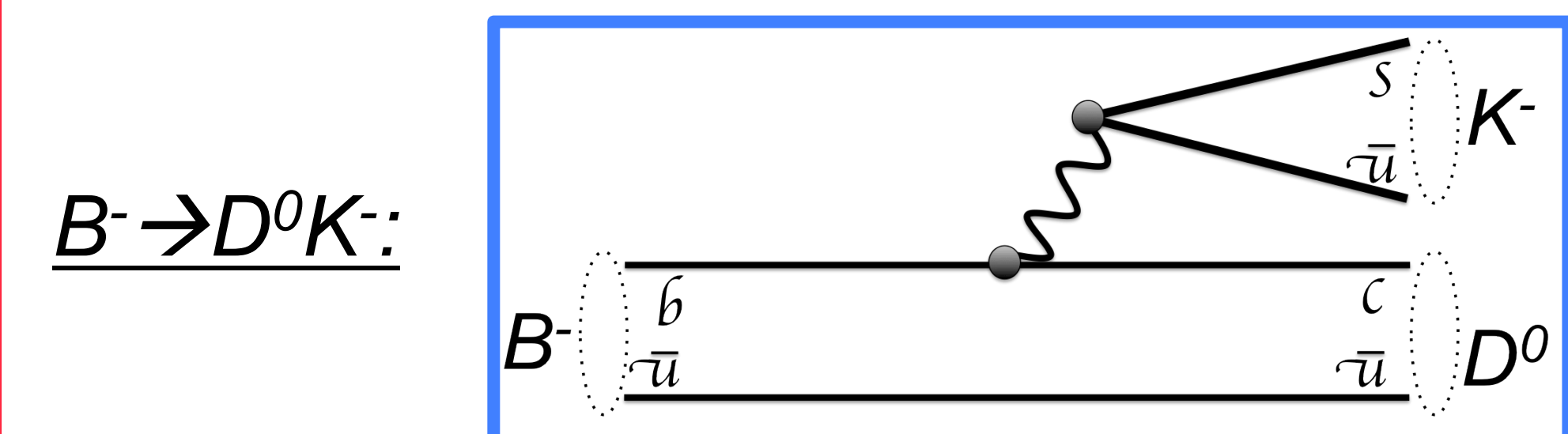
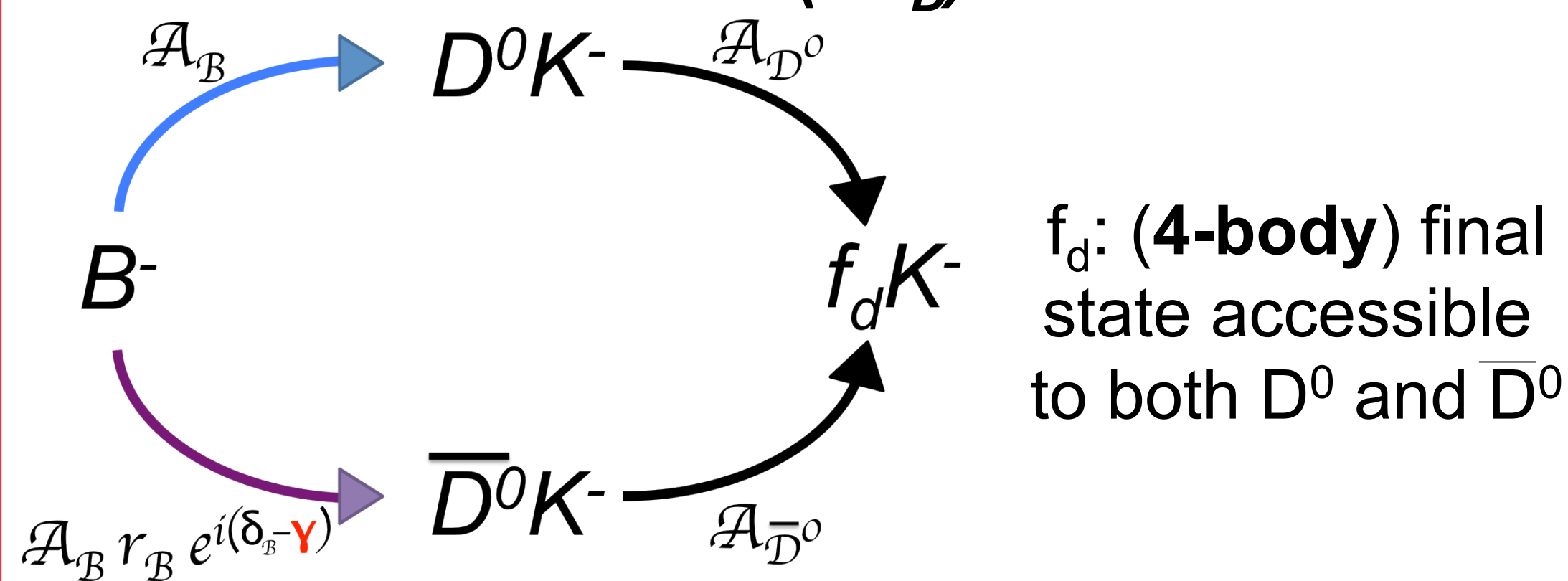


Measurement of CKM angle γ through interference in $B^\pm \rightarrow D(\rightarrow f_D)K^\pm$



Partial decay width

$$d\Gamma_{B^-}(\mathbf{x}) \propto A_{D^0}^2(\mathbf{x}) + r_B^2 A_{\bar{D}^0}^2(\mathbf{x}) + 2A_{D^0}(\mathbf{x})A_{\bar{D}^0}(\mathbf{x}) [x_- \cos(\Delta\delta(\mathbf{x})) + y_- \sin(\Delta\delta(\mathbf{x}))]$$

$$x_- = r_B \cos(\delta_B - \gamma) \quad y_- = r_B \sin(\delta_B - \gamma)$$

γ becomes an observable through interference

Binned phase-space for the D decay

$$A_{D^0}(\mathbf{x}) = A_{D^0}(\mathbf{x})e^{i\delta_{D^0}(\mathbf{x})} \quad \Delta\delta(\mathbf{x}) = \delta_{D^0}(\mathbf{x}) - \delta_{\bar{D}^0}(\mathbf{x})$$

$$d\Gamma_{B^-}(\mathbf{x}) \propto A_{D^0}^2(\mathbf{x}) + r_B^2 A_{\bar{D}^0}^2(\mathbf{x}) + 2A_{D^0}(\mathbf{x})A_{\bar{D}^0}(\mathbf{x}) [x_- \cos(\Delta\delta(\mathbf{x})) + y_- \sin(\Delta\delta(\mathbf{x}))]$$

easy to determine difficult to determine

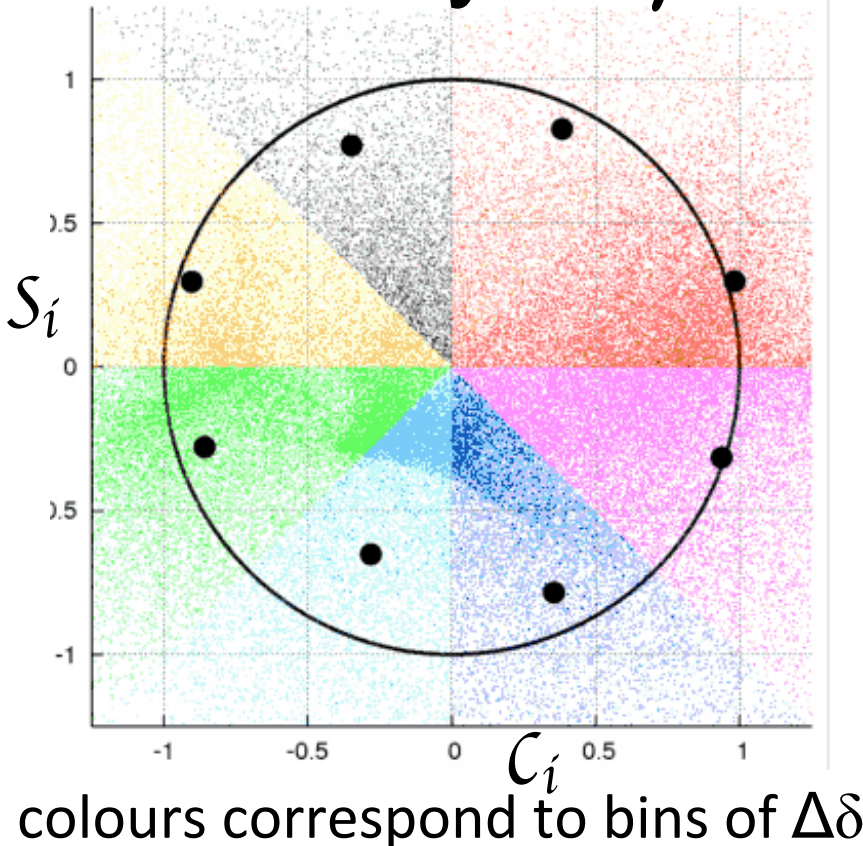
Binned five-dimensional phase-space:

$$N_i(B^- \rightarrow D^0 K^-) \propto h(K_i + r_B^2 K_{-i} + 2\sqrt{K_i K_{-i}} [x_- c_i + y_- s_i])$$

$$c_i = \frac{\int A_{D^0}(\mathbf{x})A_{\bar{D}^0}(\mathbf{x}) \cos(\Delta\delta(\mathbf{x}))d\mathbf{x}}{\sqrt{\int A_{D^0}^2(\mathbf{x})d\mathbf{x} \int A_{\bar{D}^0}^2(\mathbf{x})d\mathbf{x}}} \quad K_i = \int A_{D^0}^2(\mathbf{x})d\mathbf{x}$$

Model inspired binning:

bins with minimal variation of $\Delta\delta \rightarrow$ highest sensitivity to γ



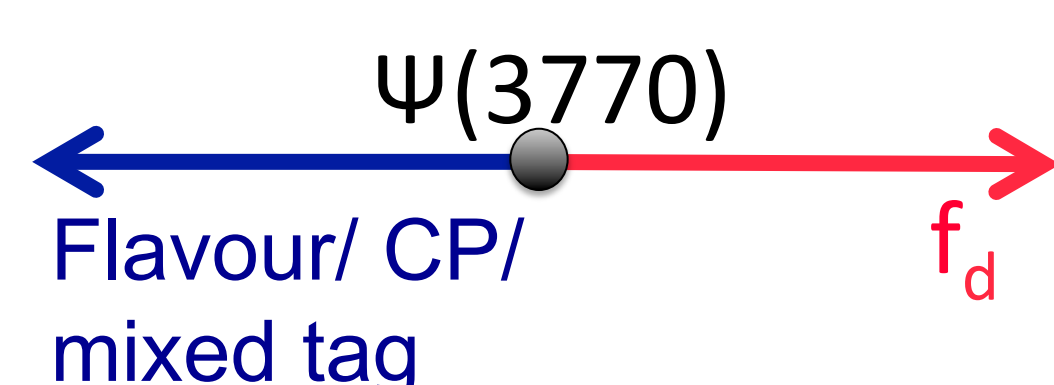
$$\langle c_i \rangle = 0.04$$

$$\langle s_i \rangle = -0.01$$

\rightarrow use amplitude model to find the binning

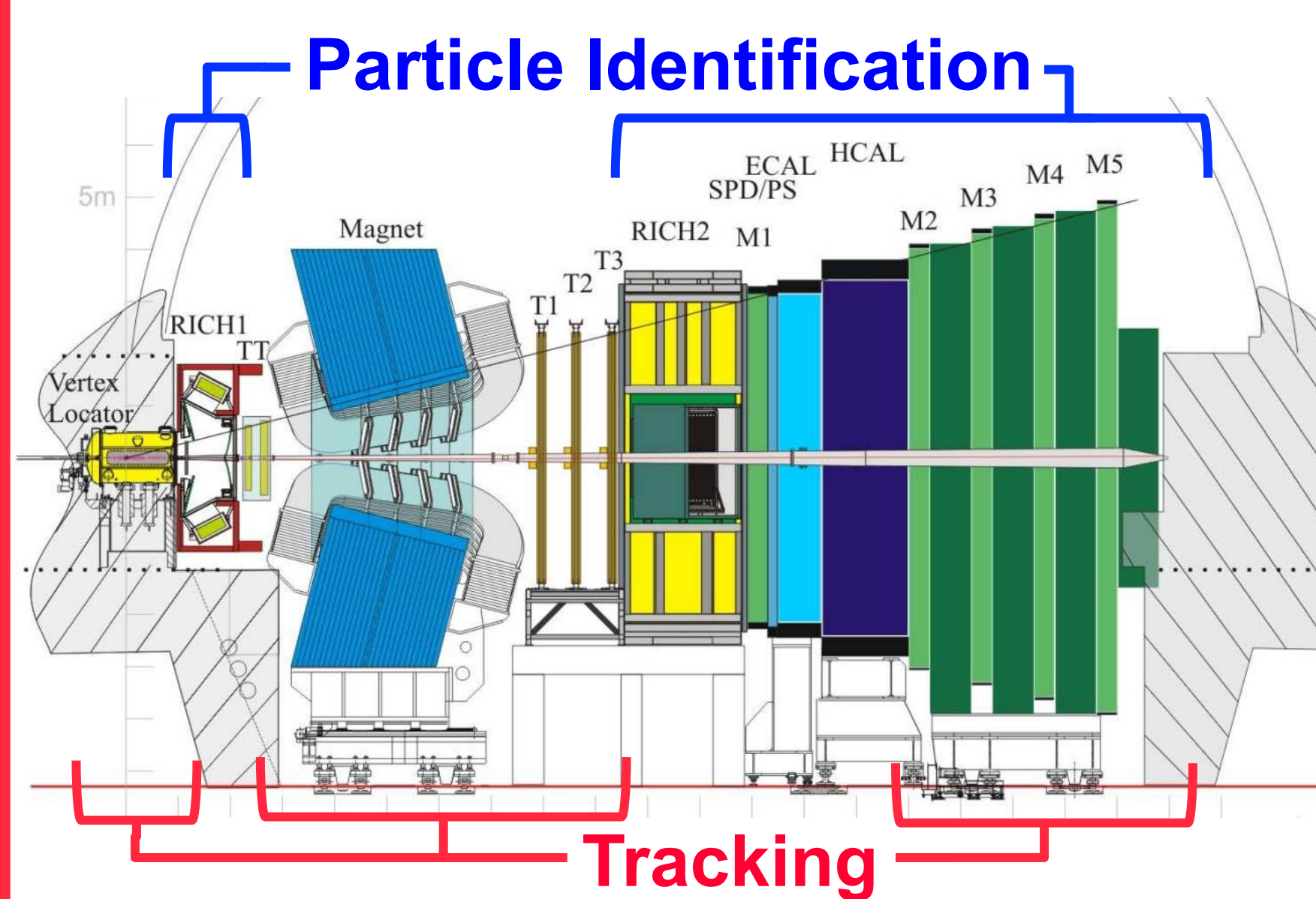
Model independent c_i and s_i :

- CLEO-c
- Correlated $D^0\text{-}\bar{D}^0$ decays



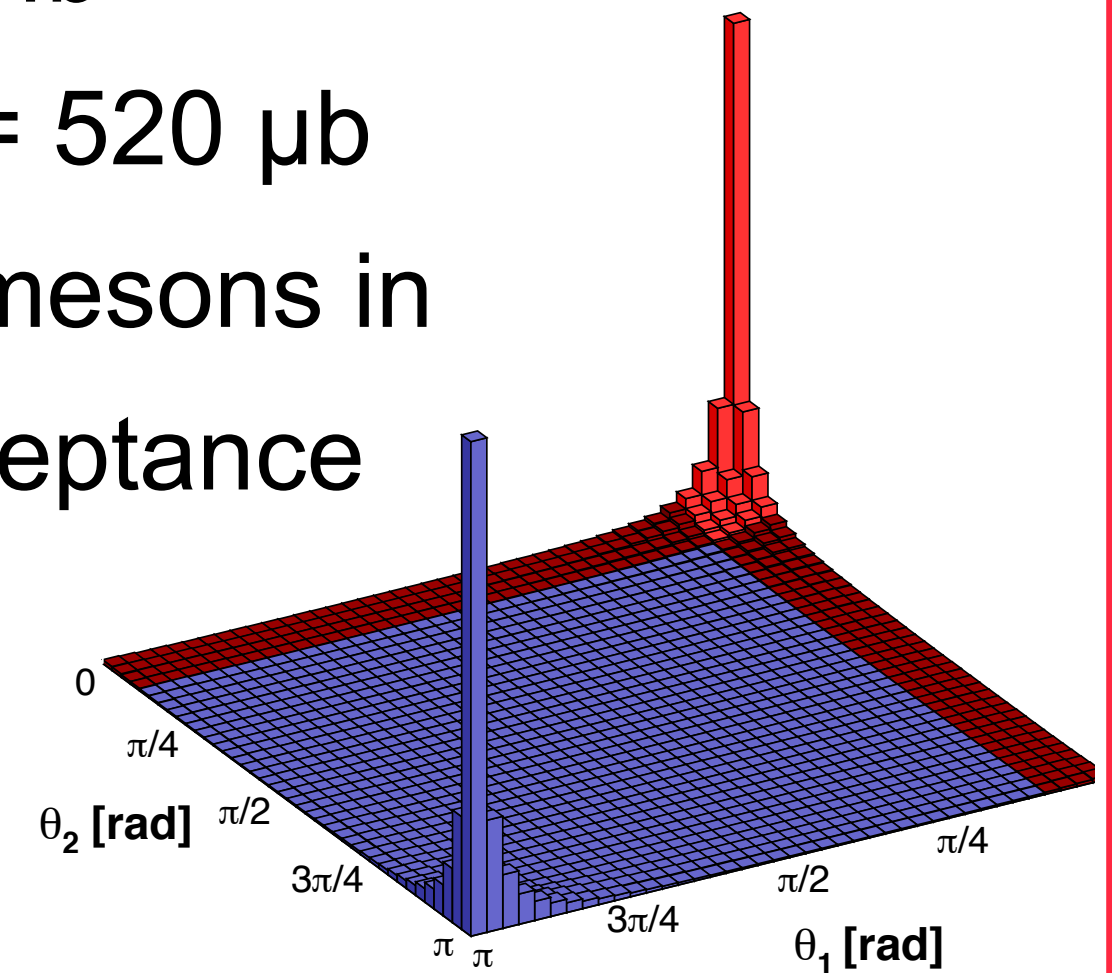
Binning influences the sensitivity not the value of γ !

The LHCb Experiment



Run II:

- $\mathcal{L}_{\text{int}} \sim 1.99 \text{ 1/fb}$
- $\sigma_{\text{bb}}(13\text{TeV}) = 520 \mu\text{b}$
- $2.3 \cdot 10^{11}$ B^\pm mesons in detector acceptance

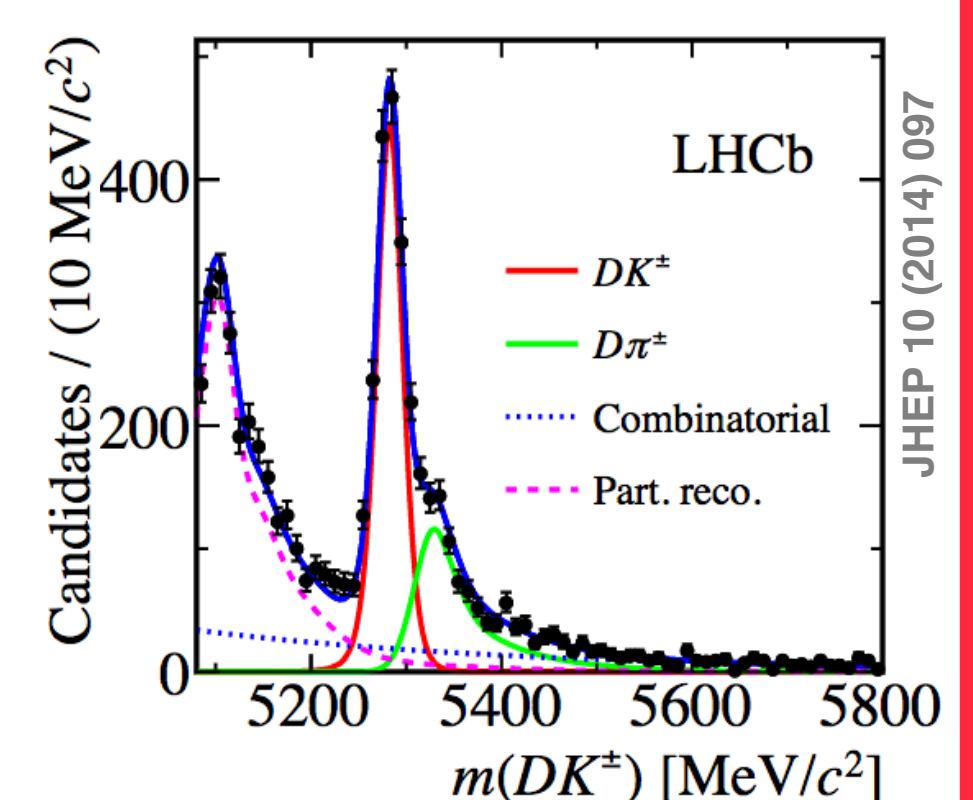
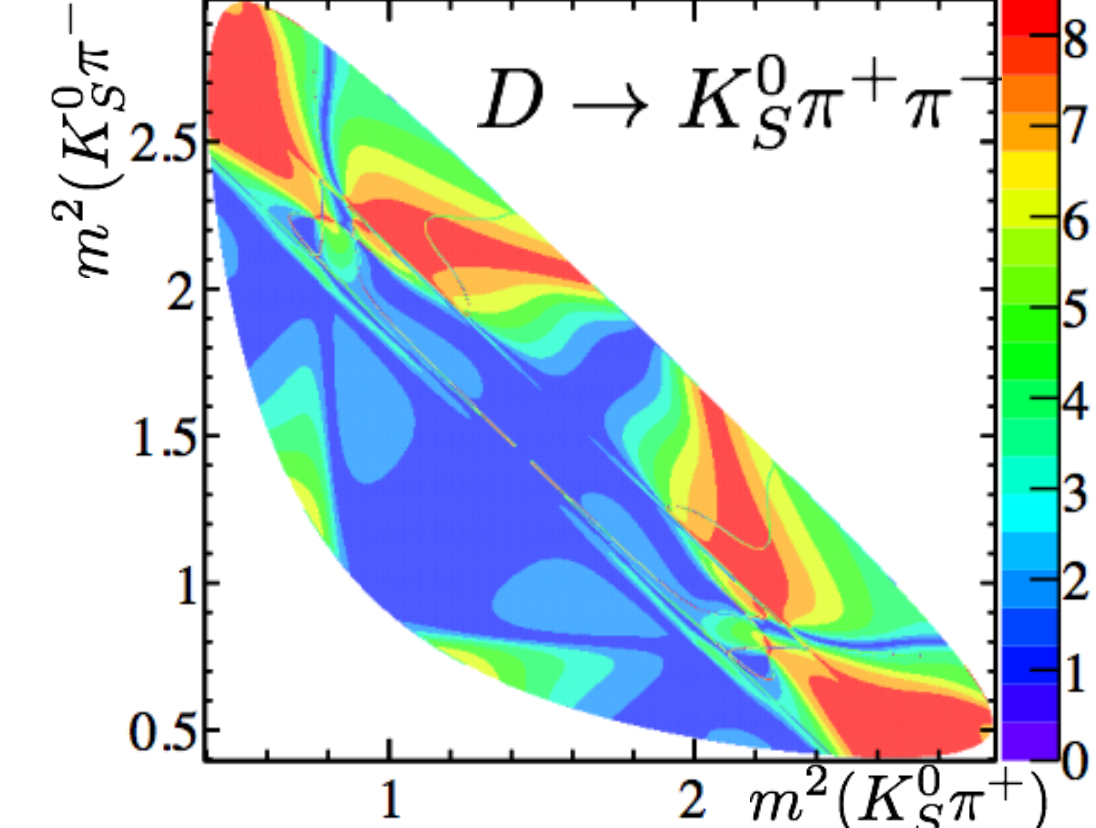


Current results

$D \rightarrow K_S \pi^+ \pi^-$:

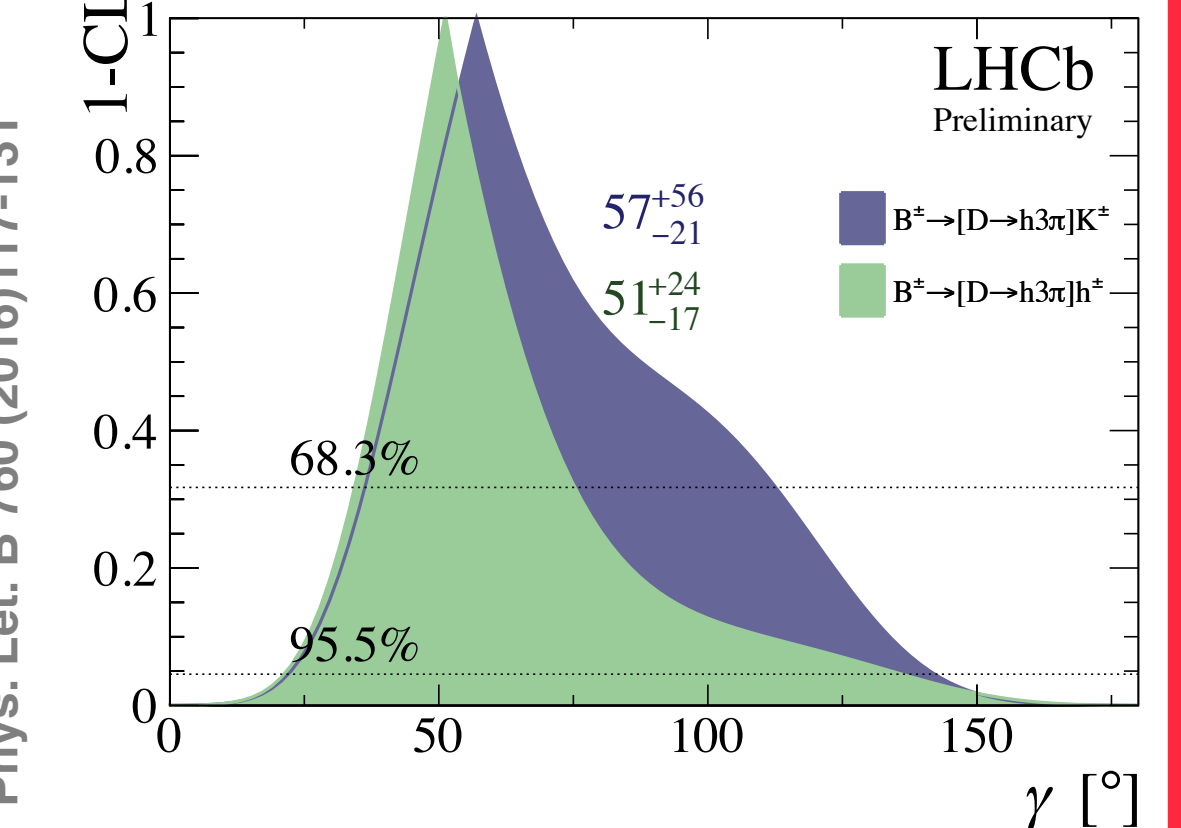
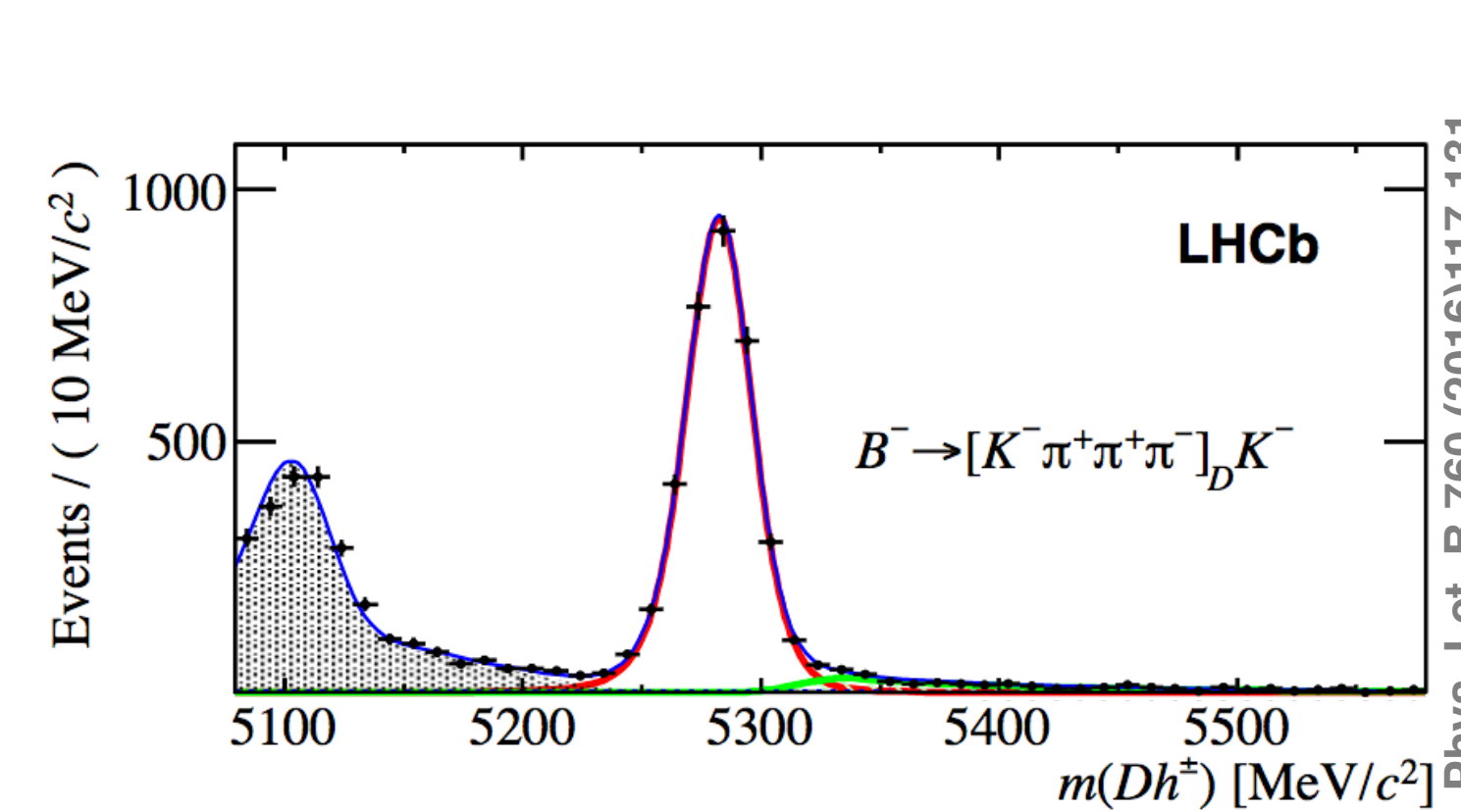
- Babar, Belle, LHCb Run I
- Binned
- Most precise measurement from single analysis
- LHCb: $\gamma = 62^{+15}_{-14}^\circ$

Binned Dalitz plot



$D \rightarrow h \pi^+ \pi^+ \pi^-$:

- LHCb Run I
- Phase-space integrated
- $\gamma = 57^{+56}_{-21}^\circ$

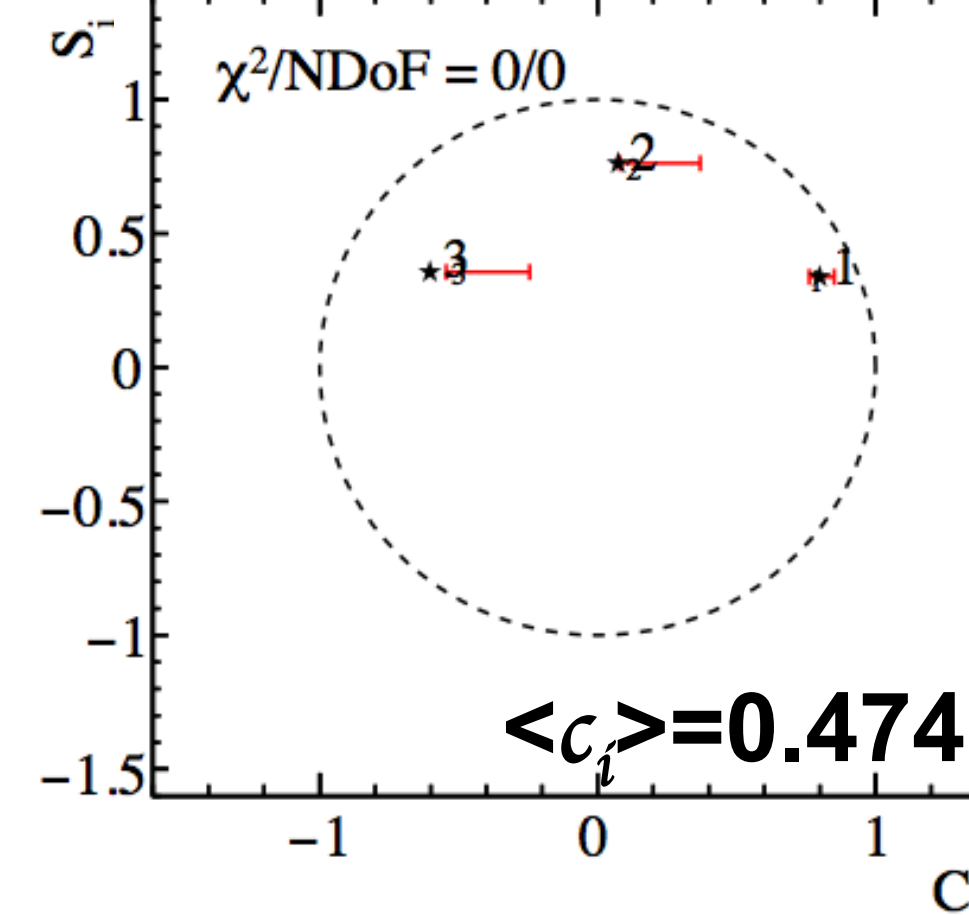


Future prospects

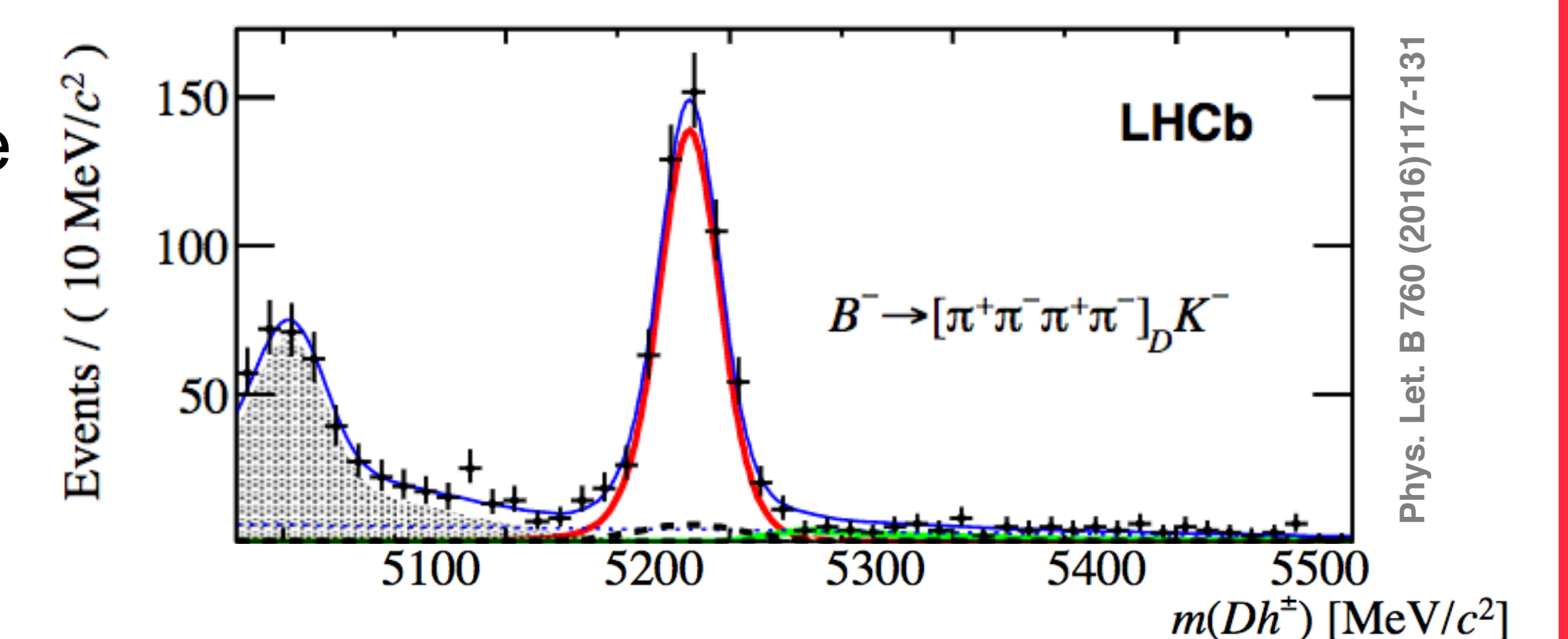
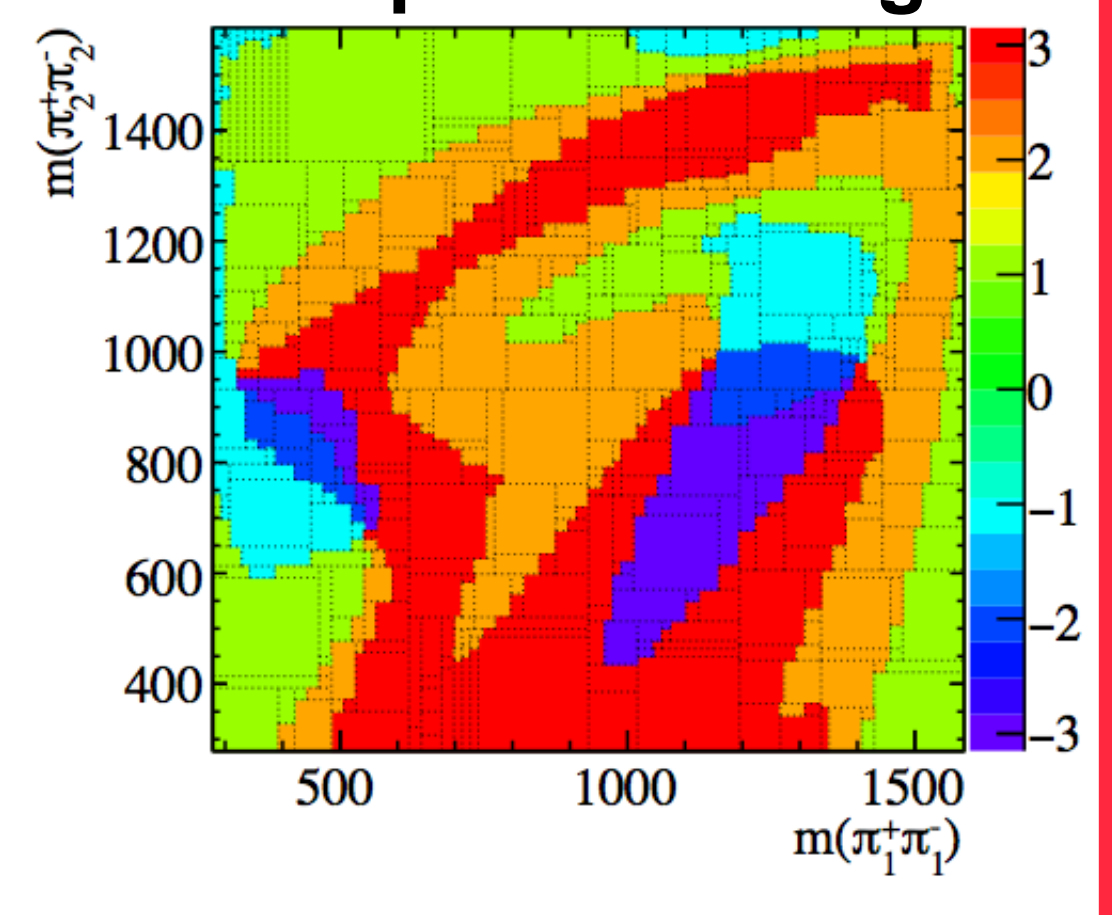
$D \rightarrow \pi^+ \pi^+ \pi^-$:

- Self-conj. state \rightarrow GGSZ
- Expect gain from binned analysis
- 5k $B^\pm \rightarrow D(\rightarrow 4\pi)K^\pm$ events** after reconstruction and selection 2015 + 2016
- 5-dimensional phase-space \rightarrow **adaptive binning**
- Similar sensitivity to γ as from $D \rightarrow K_S \pi^+ \pi^-$

Obvious gains



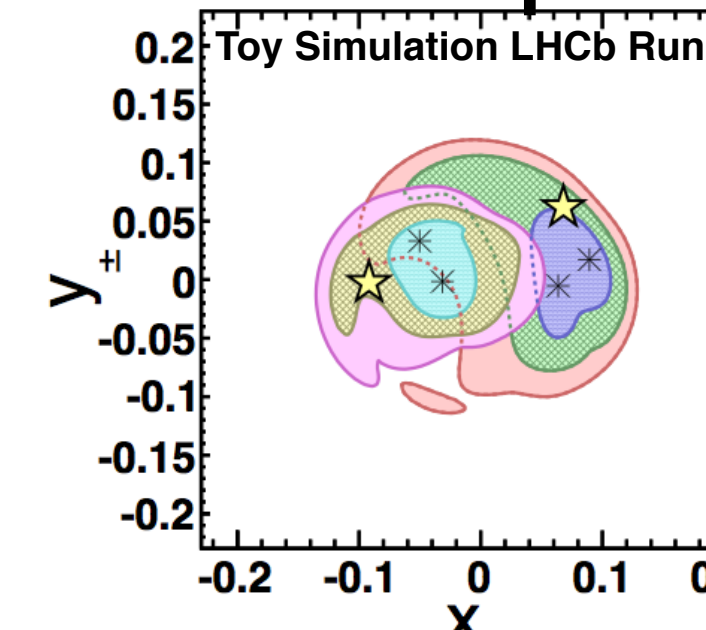
Adaptive Binning



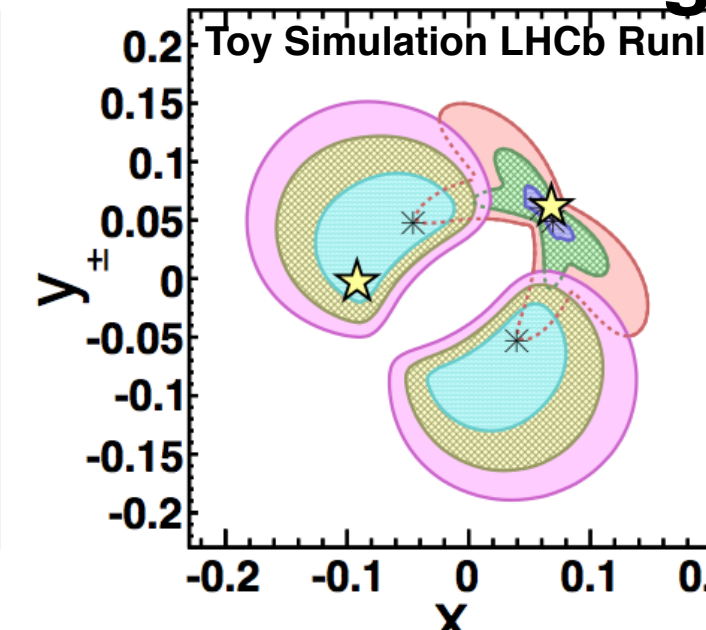
$D \rightarrow K^- \pi^+ \pi^+ \pi^-$:

- ADS mode
- 10x higher BR than $D \rightarrow \pi^+ \pi^+ \pi^-$
- Possible further input:
 - BESIII
 - LHCb $D^0\text{-}\bar{D}^0$ mixing

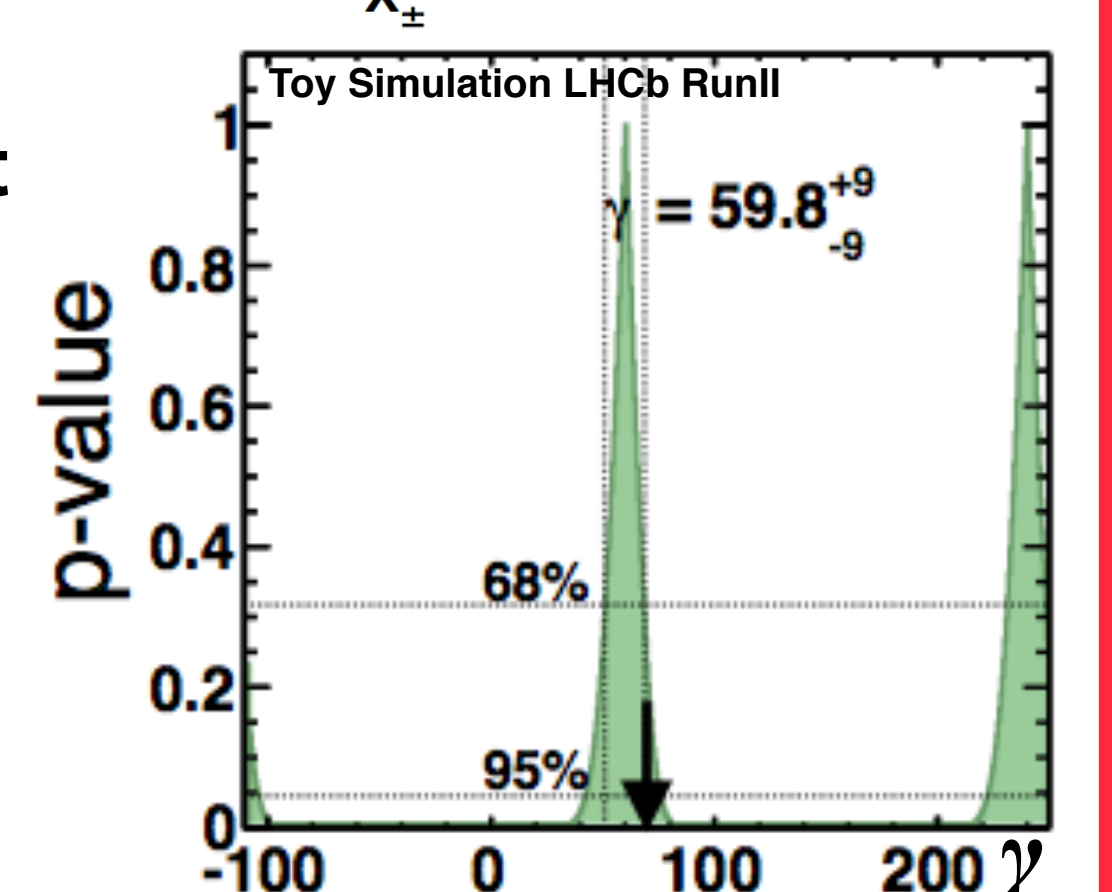
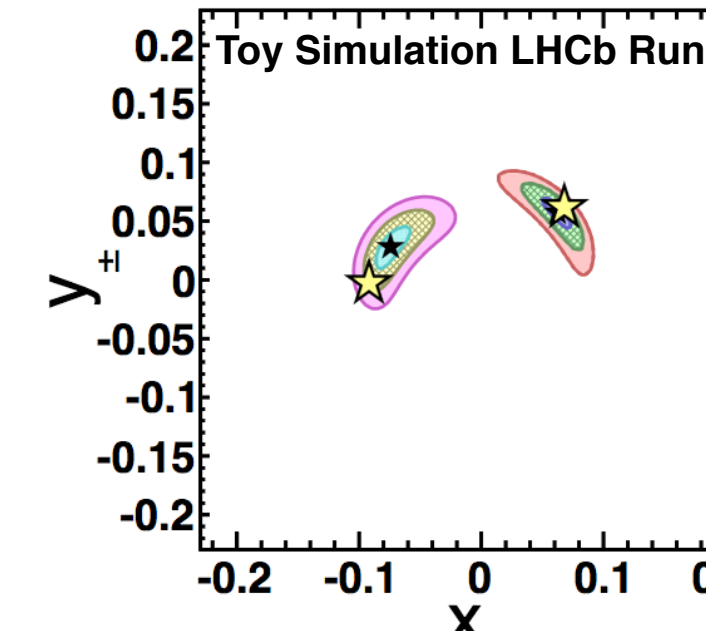
BESII Input



LHCb mixing Input



Combined Input



Toy simulation with expected LHCb statistics at the end of Run II : $\sigma(\gamma) \sim 9^\circ$