



# Boson Boson scattering analysis

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**Probe of EWSB**

**Properties of VBS**

**NoHiggs and Silh benchmark**

**Unitarized Models implementation**

**Comparison wit EVBA**

**Counting experiments with UM**

**Outlook at 7 TeV**

**Conclusions**

**In collaboration with: E.Maina, G. Bevilacqua, D.B. Franzosi, L.Oggero**



Despite the huge effort in the search for the Higgs, **EWSB mechanism remains unclear**

High energy vector boson scattering continues to play a central role,  
either as a test of the nature of the Higgs boson  
or as one of the main experimental grounds  
to the understanding of which alternative theory is at work

The relevance of high energy vector boson scattering :

**boson boson elastic scattering** violates perturbative unitarity without higgs contributions  
for L polarized vector bosons at about 1 TeV

If the higgs is not there, **some other mechanism must show up** to tame this violation

**$V_L V_L$  elastic scattering depends on it**

Many theories have been studied which provide alternative EWSB

Different interactions among vector bosons depend also on the scale  $\Lambda$  of EWSB



$\Lambda_{SB} \lesssim 1 \text{ TeV}$  below unitarity limit

**SB sector is weakly coupled** (small amplitudes)

Perturbative method work

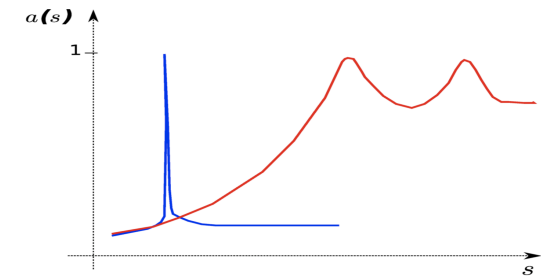
SM Higgs Boson, Susy

$\Lambda_{SB} \gtrsim 1 \text{ TeV}$

**SB sector is strongly coupled** (large amplitudes)

QCD like resonance spectrum

Dynamical Symmetri Breaking, Technicolor, Eztra Dimensions...



**Strong Vector Boson Scattering**

## SILH Strongly interacting light Higgs

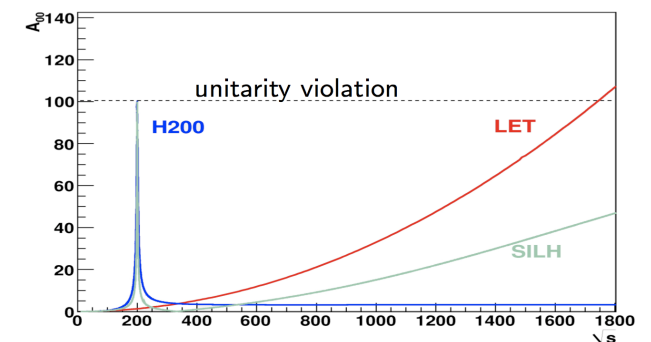
(Giudice Grojean Rattazzi...)

**Higgs a pseudo Goldstone Boson of a new strong sector**  
**Both a light higgs and Bosons strongly coupled**

Modified higgs coupling

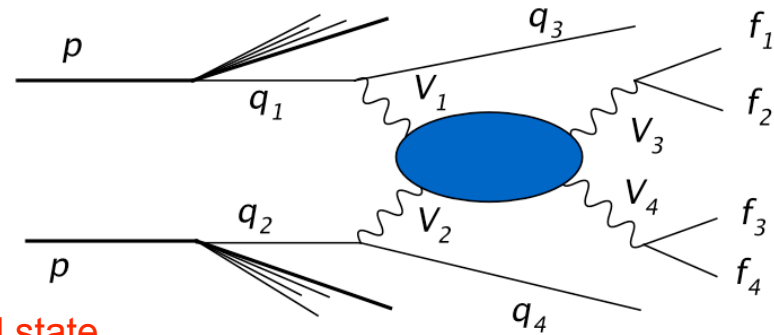
$$h \rightarrow h / \sqrt{1 + \xi c_H}, \quad \xi = v^2 / f^2$$

Little Higgs Holographic Higgs





What we observe at LHC:



Off Shell incoming and six fermion final state

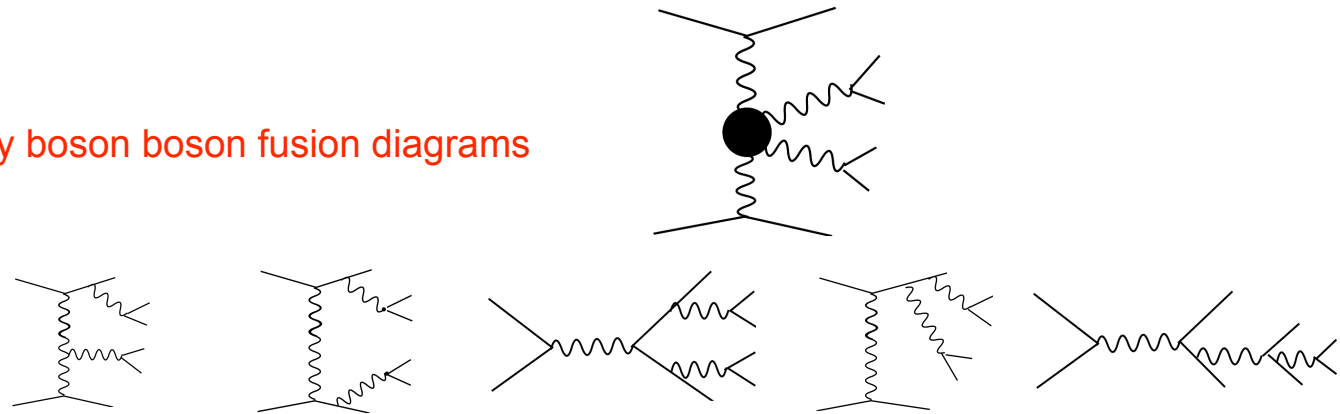
Equivalent Vector Boson Approximation connects it to elastic scattering

But in reality

Final state is produced by boson boson fusion diagrams

AND

all other topologies

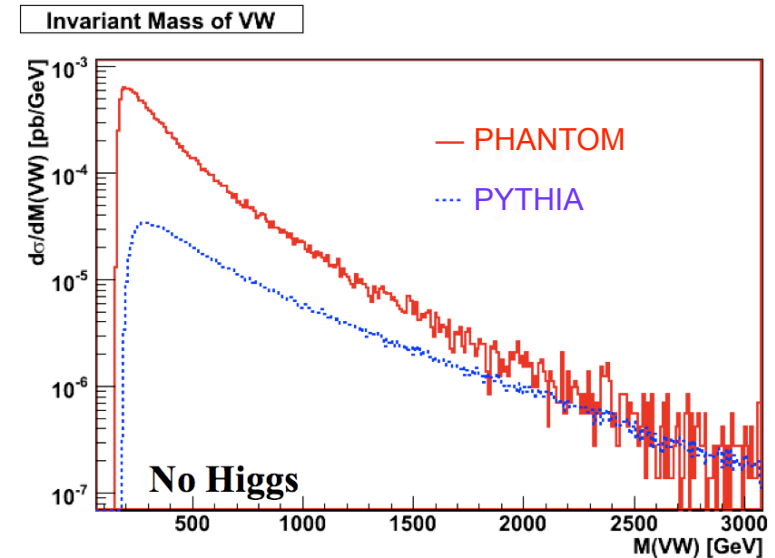
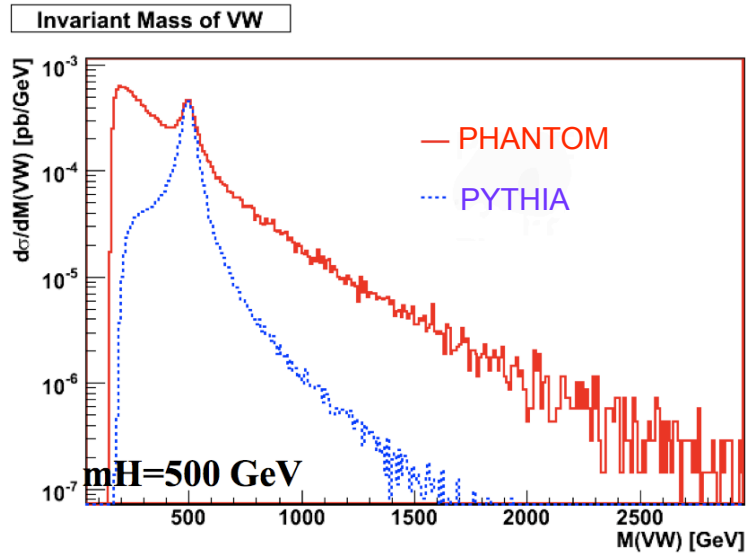


The two sets are not separately gauge invariant and there are huge interference cancellations



Lot of phenomenological studies have been made in EVBA

which nowadays seems inadequate



PYTHIA has only LL in EVBA approximation

After: Top veto, W mass cut

$p_T^W > 50$  GeV in WW CM

PHANTOM is a LO Monte Carlo and generator which can compute full contributions to any process with 6 parton in the final state for LHC, Tevatron, ILC at  $\mathcal{O}(\alpha_{em}^6) + \mathcal{O}(\alpha_{em}^4 \alpha_s^2)$

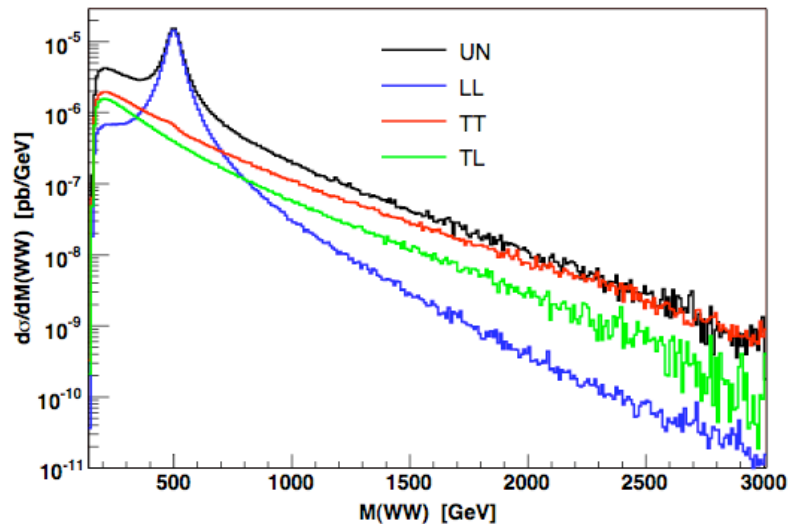
VBFNLO (Zeppenfeld Oleari ...) computes vector boson scattering at NLO in six fermion final states for fully leptonic boson decays.

General purpose ME MC may be used

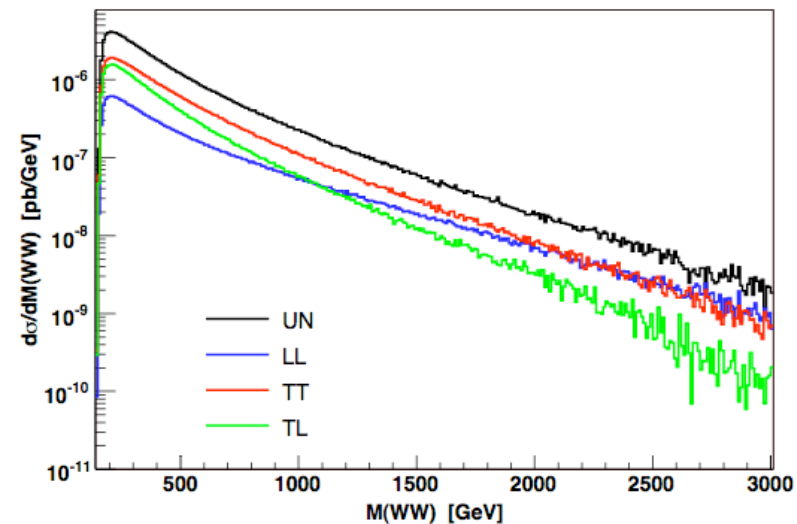


Contrary to what one expects LL do not dominate at high VV invariant mass

ud  $\rightarrow$  ud  $W^+W^- \rightarrow$  ud  $\mu \nu c s$



ud  $\rightarrow$  ud  $W^+W^- \rightarrow$  ud  $\mu \nu c s$



The decrease in the cross section at high invariant masses due to PDF suggests that careful analysis must be performed to evidence boson boson scattering effect

The invariant VV mass is the equivalent of the cm energy of the elastic VV scattering

Regions of the order of the TeV or higher in invariant mass must be examined for effects of alternative EWSB theories.



## The 7 channels:

### totally leptonic

$$PP \rightarrow jjl^+l^-l'\nu$$

$$PP \rightarrow jjl^+l^-l^+l^-$$

$$PP \rightarrow jjl^\pm l^\pm \nu\nu$$

$$PP \rightarrow jjW^+W^- \rightarrow jjl^+l^- \nu\nu$$

$$PP \rightarrow jjZZ \rightarrow jjl^+l^- \nu\nu$$

### semi-leptonic

$$PP \rightarrow jjjjl\nu$$

$$PP \rightarrow jjjjl^+l^-$$

$$l = \mu, e$$

For the last 3 (2ν) VV mass cannot be reconstructed

## Few analysis with complete calculations (not EVBA):

- CMS studies at hadron level with fast detector simulation  
CMS AN 2007/005 arXiv:1010.5848
- Studies on specific models  
eg. Zeppenfeld et al arXiv:0812.2564  
on warped higgsless models
- Our results on benchmark and Unitarized Models





To study **VBS** one would like to separate it from irreducible background due to all other diagrams contributions

**Huge interferences and non gauge invariance forbid to do so**

**One has to rely on appropriate cuts to evidentiate boson boson contributions**

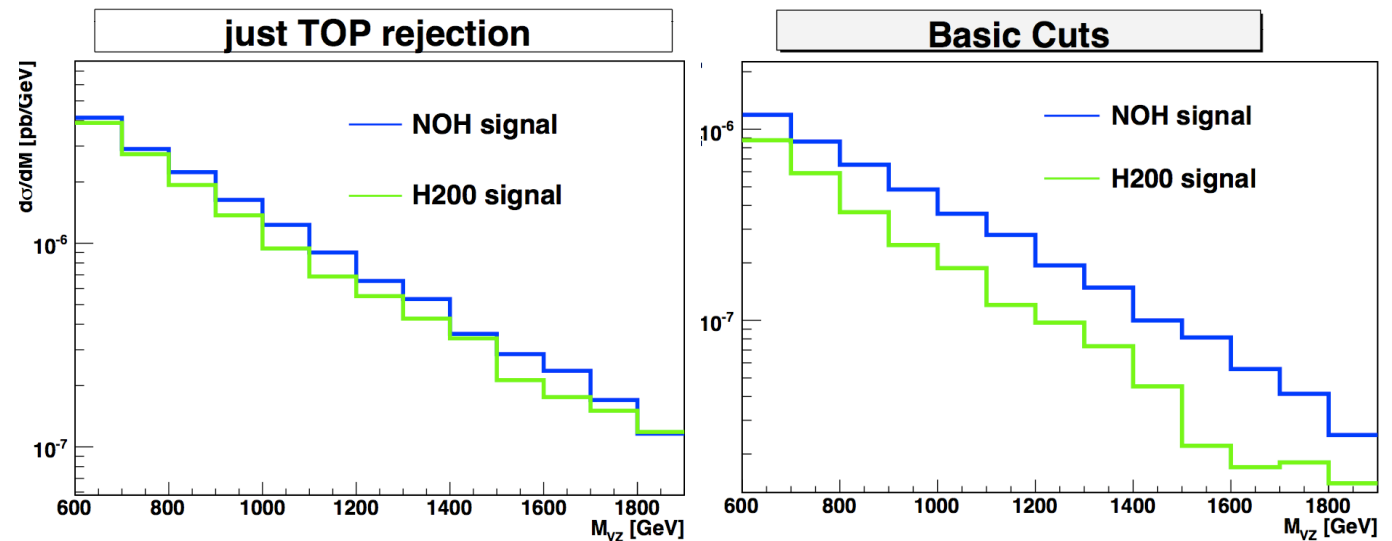
**Some cuts are obvious and well known :**

eg. large  $\Delta\eta$  separation between forward and backward jet

**A good strategy is that of looking for the cuts which increase the difference between light higgs (weak coupling) and no-higgs (strong coupling) distributions at high invariant VV masses**

PP  $\rightarrow$   $4j\mu\mu$

Generation Cuts	
$ \eta(\ell^\pm)  < 3.0$	$E(\ell^\pm) > 20$ GeV
$p_T(\ell^\pm) > 20$ GeV	$M(\ell^\pm\ell^\pm) > 20$ GeV
$ \eta(j)  < 6.5$	$E(j) > 20$ GeV
$p_T(j) > 30$ GeV	$M(jj) > 60$ GeV
Basic Selection Cuts	
$\Delta\eta(j_f j_b) > 4$	
$M(j_f j_b) > 100$ GeV	
$\eta(\mu\mu) < 2$	
$70\text{GeV} < M(j_c j_c) < 100\text{GeV}$	
$ M(jjj) - M_{TOP}  > 15$ GeV	





Benchmark studies performed on two scenarios: no-higgs and Silh

✓ no-higgs :

model independent representative at LHC of Strong Interacting Theories

- One expects predictions similar to those of SIT at LHC:  
 slightly higher than theories with no resonances below 2TeV  
 lower than those with lower mass resonant states
- Pdf strongly depress high VV invariant mass where its predictions are  
 higher than unitary theories
- No higgs prescription is gauge invariant: corresponds to  $m_H \rightarrow \infty$   
 It is however not a consistent theory .

✓ Silh:

We have chosen Silh with  $\xi c_H=1$  as representative of upper limit  
 of model independent lagrangian description of these theories

- The main effect for these processes is the variation of the higgs coupling that  
 correspond to a redefinition of higgs propagator.

$$\frac{1}{p^2 - m_H^2} \rightarrow \frac{1}{1 + \xi c_H} \frac{1}{p^2 - m_H^2}$$

- Cancellations do not occur exactly  
 and the model violates unitarity
- The onset of the violation is postponed to higher a higher scale than SM



All 7 channels analyzed at parton level at 14 TeV

Generated with Phantom all signals and irreducible backgrounds

Madevent used for Z /W +4jets at  $\mathcal{O}(\alpha_{EM}^2 \alpha_S^4)$  and tt+jets

Performed careful analysis of the best cuts for the regions of interest

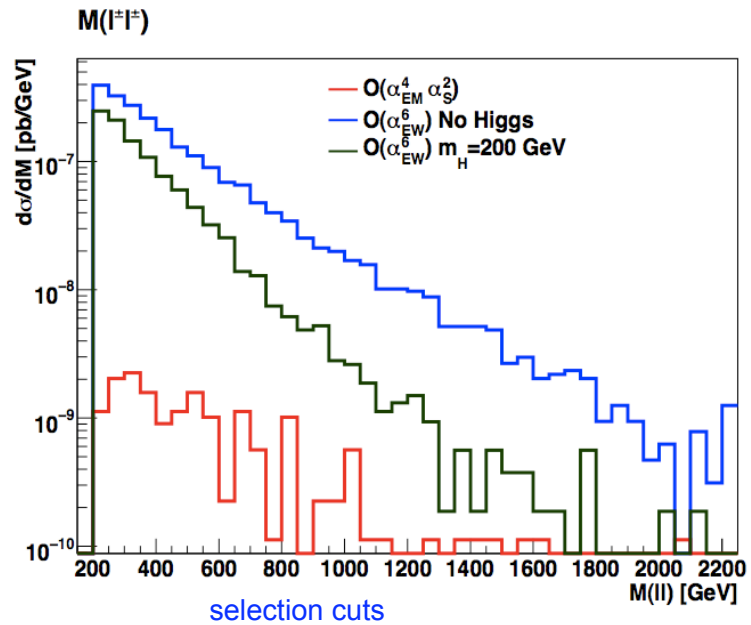
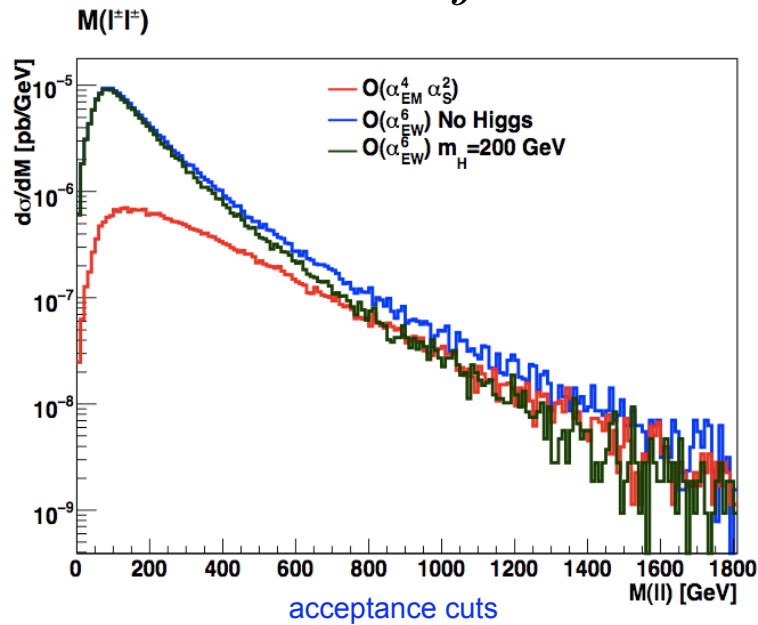
Typical basic and selection cuts used for the analysis

Basic Cuts
$p_T(\ell^\pm) > 20$ GeV
$ \eta(\ell^\pm)  < 3.0$
$M(\ell^+\ell^-) > 20$ GeV
$M(\ell^+\ell^-) > 250$ GeV ( $2jW^+W^-$ )
$76$ GeV $< M(\ell^+\ell^-) < 106$ GeV ( $2jZZ$ )
$p_T(j) > 30$ GeV
$ \eta(j)  < 6.5$
$M(jj) > 60$ GeV
$M(j_f j_b) < 70$ GeV; $M(j_f j_b) > 100$ GeV
$ \Delta\eta(jj)  > 3.0$ ( $2j2\ell2\nu$ )
$ \Delta\eta(j_f j_b)  > 4.0$ ( $2j4\ell, 4j\ell\nu, 4j\ell\ell$ )
$ M(jjj) - M_{top}  > 15$ GeV ( $4j\ell\nu, 4j\ell\ell$ )
$ M(j\ell\nu_{rec}) - M_{top}  > 15$ GeV ( $3\ell\nu + 2j, 4j\ell\nu$ )
$70$ GeV $< M(j_c j_c) < 100$ GeV ( $4j\ell\nu, 4j\ell\ell$ )
$\Delta R(jj) > 0.3$ ( $4j\ell\nu, 4j\ell\ell$ )

Cuts	Processes ( $W^+W^-$ )	$2j\ell^+\ell^-\nu\bar{\nu}$ ( $ZZ$ )	$2j\ell^\pm\nu\ell^\pm\nu$	$4j\ell\nu$	$4j\ell\ell$	$2j3\ell\nu$	$2j4\ell\nu$
$ \eta(\ell^\pm)  <$	2.0			2.0		2.0	
$M(j_f j_b) >$	1000	800		1000	1000	1000	800
$ \Delta\eta(j_f j_b)  >$	4.8	4.5	4.5	4.8	4.8	4.8	
$p_T(j_c) >$				70	60		
$p_T(j_c j_c) >$					200		
$p_T(\ell\nu) >$				200		200	
$p_{Tmiss} >$		120		100			
$p_T(\ell^+\ell^-) >$		120			200	200	100
$p_T(\ell) >$			50				
$minp_T(j) <$			120				
$E(j) >$	180						
$max \eta(j)  >$	2.5		2.5		2.8		
$ \eta(j)  >$	1.3	1.9				1.2	
$ \Delta\eta(Vj)  >$				0.6	1.1	1.5	
$\Delta\eta(\ell j) >$	0.8	1.3					
$\Delta R(\ell j) >$	1		1.5				
$\Delta R(Zj) >$							1
$M(\ell j) >$	180						
$M(Vj) >$					300		
$ \vec{p}_T(\ell_1) - \vec{p}_T(\ell_2)  >$	220		150				
$ \vec{p}_T(\ell^+\ell^-) - \vec{p}_T^{miss}  >$		290					
$\cos(\delta\phi_{\ell\ell}) <$	-0.6		-0.6				
$\cos(\delta\phi_{ZZ}) <$							-0.4
$\Delta R(\ell^+\ell^-) <$					1.0		



Result for one channel:  $2j\ell^\pm\ell'^\pm\nu\nu$

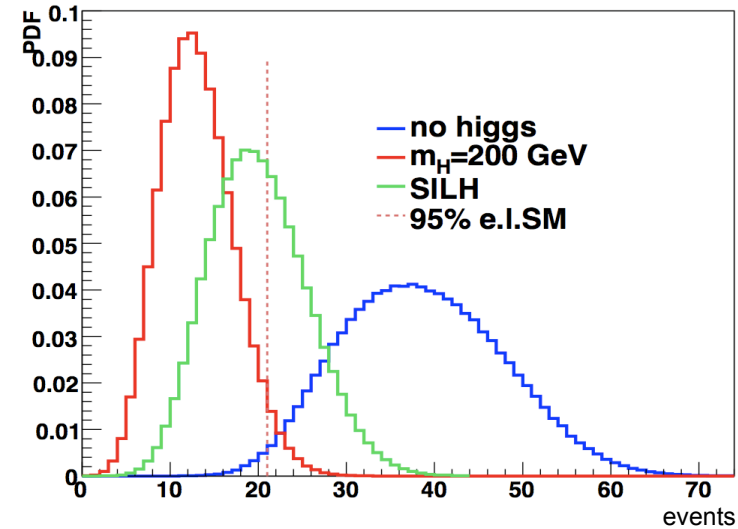


Cross sections

$M_{cut}$ (GeV)	no Higgs		SILH		$M_H = 200$ GeV
	$\sigma$ (fb)	PBSM	$\sigma$ (fb)	PBSM	$\sigma$ (fb)
200	.435(.431)	94.9%	.276 (.273)	39.1%	.206(.203)
300	.290(.288)	98.2%	.166 (.164)	42.3%	.114(.111)
400	.191(.189)	98.7%	.0977(.0958)	41.2%	.0629(.0609)
500	.129(.128)	98.7%	.0604(.0588)	34.4%	.0351(.0336)
600	.0886(.0876)	97.5%	.0385(.0375)	37.1%	.0194(.0183)
700	.0614(.0607)	96.6%	.0262(.0254)	42.3%	.0112(.0105)
800	.0438(.0432)	91.1%	.0184(.0178)	31.2%	.00701(.00640)

Full set of cuts . ( ) = EW only PBSM at 95% L=200 fb<sup>-1</sup>

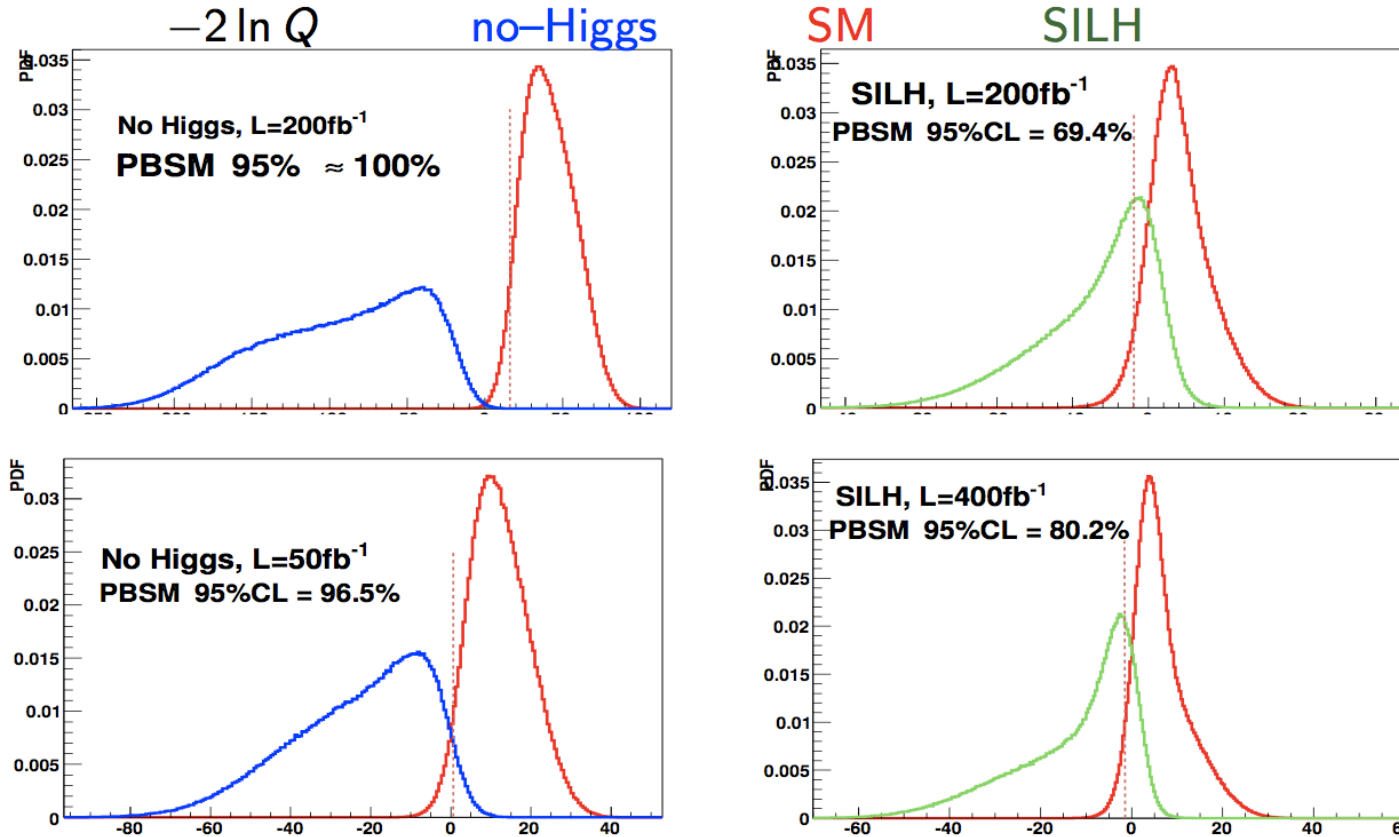
PDF. Statistical and th errors.



Th error assumed +- 30% Only stat for tt+2j and V+4j



Combining all 7 channels (likelihood ratio)



$$Q(\vec{k}; \vec{\lambda}_{BSM}, \vec{\lambda}_{SM}) = \frac{\mathcal{P}(\vec{k}; \vec{\lambda}_{BSM})}{\mathcal{P}(\vec{k}; \vec{\lambda}_{SM})}, \quad \sum_{\vec{k}} \mathcal{P}(\vec{k}; \vec{\lambda}_{SM}) \theta(\alpha - Q(\vec{k}; \vec{\lambda}_{BSM}, \vec{\lambda}_{SM})) = 95\%.$$

$$\text{PBSM@95\%CL} = \sum_{\vec{k}} \mathcal{P}(\vec{k}; \vec{\lambda}_{BSM}) \theta(Q(\vec{k}; \vec{\lambda}_{BSM}, \vec{\lambda}_{SM}) - \alpha).$$



## Unitarization Models

Low energy VBS amplitudes violate unitarity at  $\sqrt{s} \approx 1 - 2 \text{ TeV}$ . Unitarization models give a phenomenological description of these amplitudes much beyond these scales by forcing the divergent amplitudes to satisfy the unitarity condition.

- EWChL, describes the EW interaction at low energies through an expansion in  $E/\Lambda$ ,

$$\begin{aligned} \mathcal{L} = & \frac{v^2}{4} \text{Tr}[(D_\mu \Sigma)^\dagger D^\mu \Sigma] && \text{(W,Z masses, LET)} && \Sigma = \exp(i \frac{\sigma \cdot \omega(x)}{v^2}) \\ & + \alpha_4 [\text{Tr} V_\mu V_\nu]^2 + \alpha_5 [\text{Tr} V_\mu V^\mu]^2 && \text{(higher order operators)} && V_\mu = (D_\mu \Sigma) \Sigma^\dagger \\ & + \text{standard YM terms} \end{aligned}$$

We compute the leading part of longitudinal VBS at high energies, e.g:

$$A(W_L^+ W_L^- \rightarrow Z_L Z_L) = \frac{s}{v^2} + 4\alpha_4 \frac{t^2 + u^2}{v^4} + 8\alpha_5 \frac{s^2}{v^4} + \dots,$$

- To study unitarity issues, it is always convenient to expand  $V_L$  elastic scattering in terms of partial wave amplitudes of definite angular momenta,  $J$ , and isospin,  $I$  (associated with the custodial symmetry  $SU(2)_{L+R}$  group).

$$A_I(s, t) = 16\pi \sum_J (2J+1) a_{IJ}(s) P_J(\cos\theta), \quad a_{IJ}(s) = a_{IJ}^{(1)}(s) + a_{IJ}^{(2)}(s) + \dots$$

- Elastic unitarity condition,  $\text{Im} \hat{a}_{IJ}(s) = |\hat{a}_{IJ}(s)|^2$ .



Unitarized models modify the amplitudes in such a way that unitarity is satisfied keeping the same low energy behaviour

## Models implemented in PHANTOM

- K-matrix scheme:

$$a_{IJ}(s) \rightarrow \frac{1}{\text{Re}(1/a_{IJ}(s)) - i}$$

- Inverse Amplitude Method:

$$a_{IJ}(s) \rightarrow \frac{a_{IJ}^{(1)}(s)}{1 - a_{IJ}^{(2)}(s)/a_{IJ}^{(1)}(s)}$$

- N/D protocol:

$$a_{IJ}(s) \rightarrow \frac{N_{IJ}(s)}{1 + G(s)N_{IJ}(s)}$$

$$G(s) = \frac{1}{32\pi^2} \ln\left(-\frac{s}{M^2}\right)$$

$$N_{IJ}(s) = a_{IJ}^{(1)}(s) + a_{IJ}^{(2)}(s) + G(s)(a_{IJ}^{(1)}(s))^2;$$

In K-matrix scheme specific resonances (scalar vector or tensor) can be added to  $a_{IJ}(s)$ , while IAM and N/D prescriptions produce different resonances dependent on the specific value of  $\alpha_4$  and  $\alpha_5$ .

$\alpha_4$  and  $\alpha_5$  constrained in the range (Eboli et al hep-ph/0606118)

$$-7.7 \times 10^{-3} < \alpha_4 < 15 \times 10^{-3}$$

$$-12 \times 10^{-3} < \alpha_5 < 10 \times 10^{-3}$$



# Off-Shell Implementation

It has been proposed (Chanowitz, hep-ph/9512358) and implemented in the WHIZARD MC (Kilian et al, hep-ph/0806.4145) an off-shell realization of UM; however, only on-shell phenomenological studies have been performed so far, relying on EVBA and NWA. We have independently implemented complete 6 fermions final state UM in PHANTOM and studied their phenomenological implications.

- Notice that the SM without Higgs already contains the LET part. Subtract LET part from on-shell amplitudes  $\Delta A_{IJ}(s) = \hat{A}_{IJ}(s) - A_{IJ}^{LET}(s)$ ;

- Identify the process looking at the incoming and outgoing particles;

- Translate  $A_{IJ}$  into individual scattering amplitudes, e.g.:

$$\Delta A(W_L^+ W_L^- \rightarrow Z_L Z_L) = 4 \left[ \frac{v^4}{12s^2} (\Delta A_{00}(s) - \Delta A_{20}(s)) - \frac{5v^4}{6s^2} (\Delta A_{02}(s) - \Delta A_{22}(s)) \right] \frac{s^2}{v^4} + \left[ \frac{5v^4}{s^2} (\Delta A_{02}(s) - \Delta A_{22}(s)) \right] \frac{t^2 + u^2}{v^4}$$

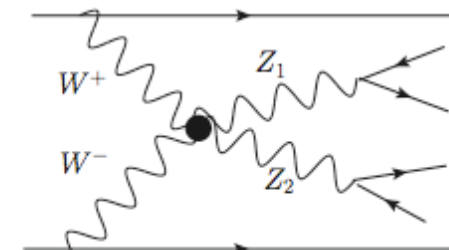
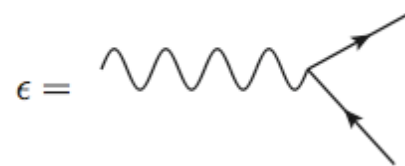
- Embed elastic amplitude as effective quartic coupling, identifying the factors  $s^2$ ,  $t^2$  and  $u^2$  with appropriate contraction of polarization vectors,

e.g. in  $W_L^+ W_L^- \rightarrow Z_L Z_L$

$$s^2 \rightarrow 4M_W^2 M_Z^2 \epsilon^+ \cdot \epsilon^- \epsilon^1 \cdot \epsilon^2$$

$$t^2 \rightarrow 4M_W^2 M_Z^2 \epsilon^+ \cdot \epsilon^1 \epsilon^- \cdot \epsilon^2$$

$$u^2 \rightarrow 4M_W^2 M_Z^2 \epsilon^+ \cdot \epsilon^2 \epsilon^- \cdot \epsilon^1$$

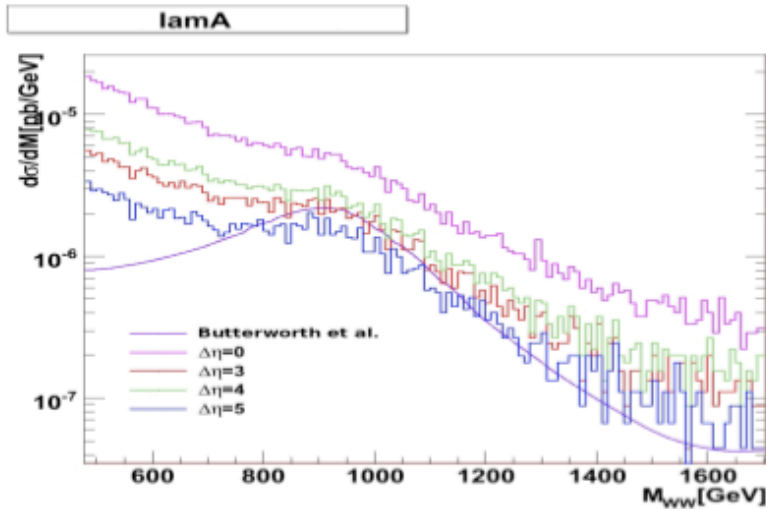






# Results for Unitarization Models

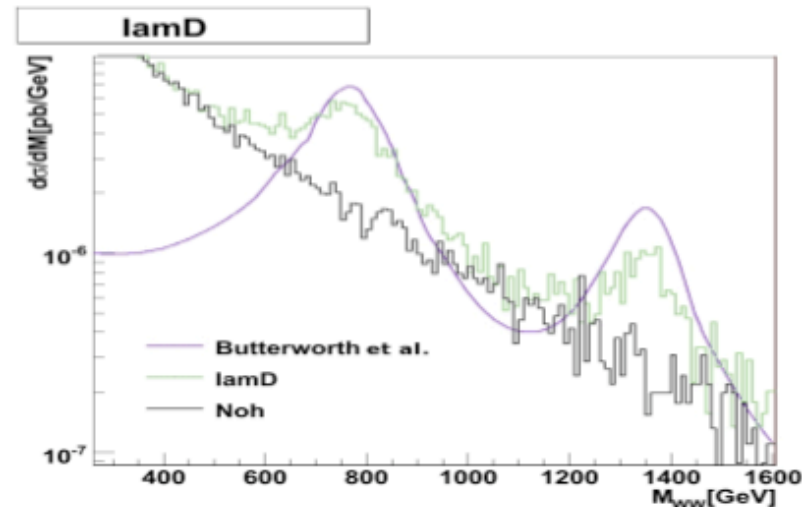
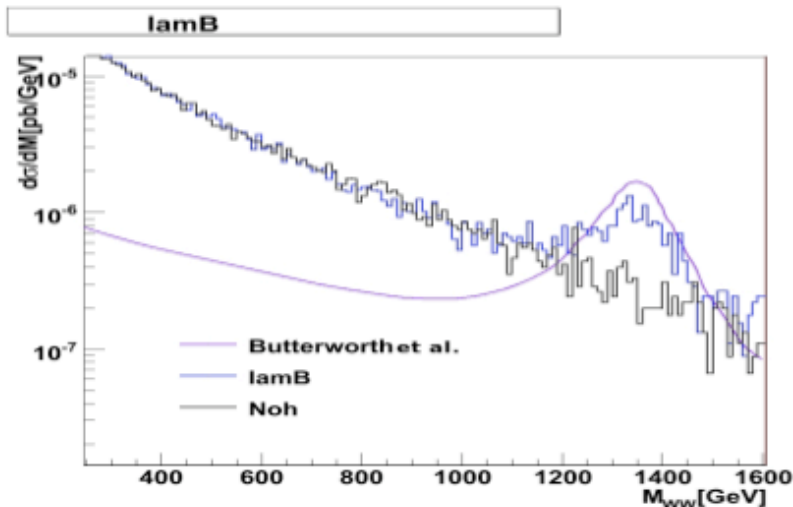
Comparison with previous study (Butterworth et al, hep-ph/0201098) based on on-shell amplitudes and EVBA.



$2j\mu^\pm e^\mp \nu\bar{\nu}$   
 $\Delta\eta(jj) > 4$   
 no top processes

scenario	$\alpha_4$	$\alpha_5$
IAM A	0.0	0.003
IAM B	0.002	-0.003
IAM D	0.008	0.0

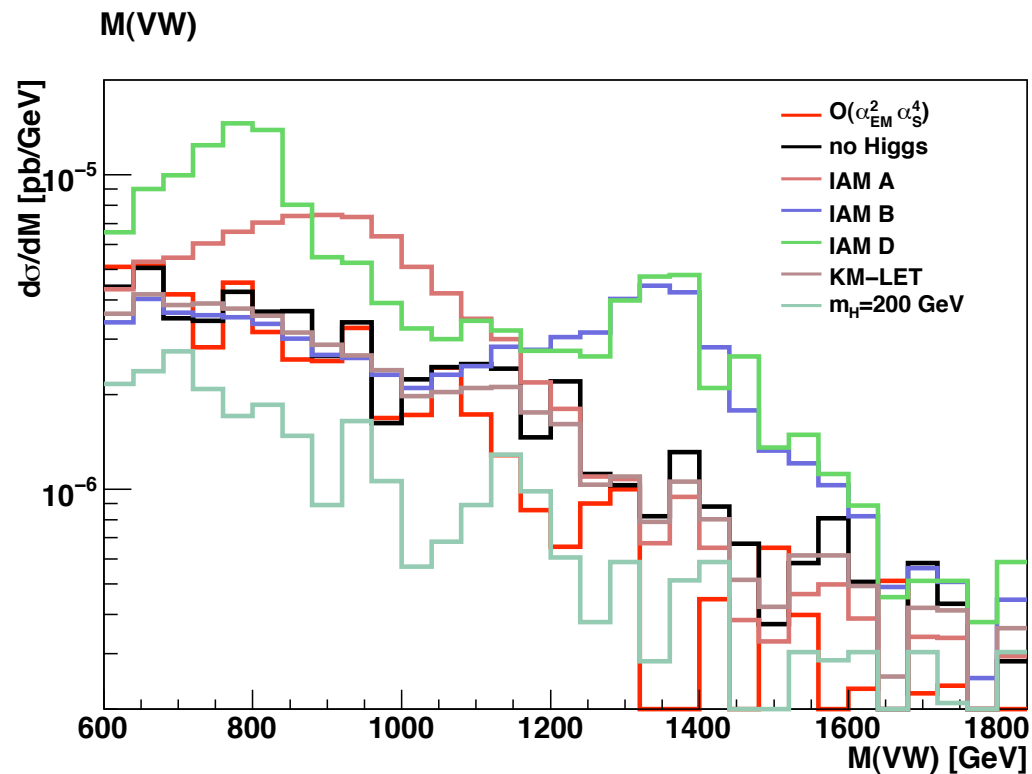
IAM determines resonances depending on chiral coeff:  
 IAMA 1 TeV scalar  
 IAMB 1.4 vector  
 IAMD 0.8 scal 1.4 vect





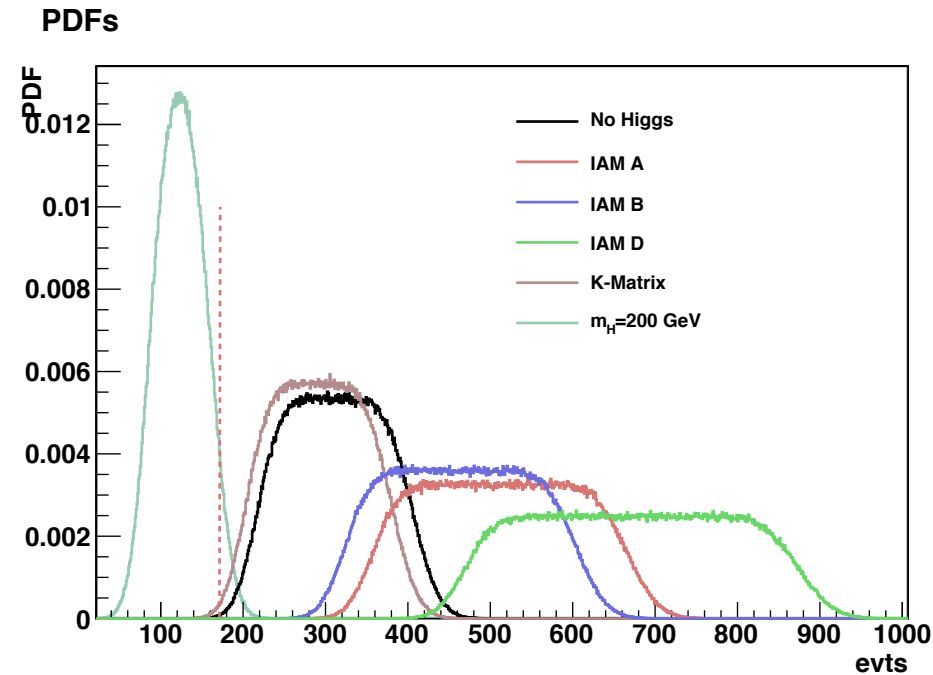
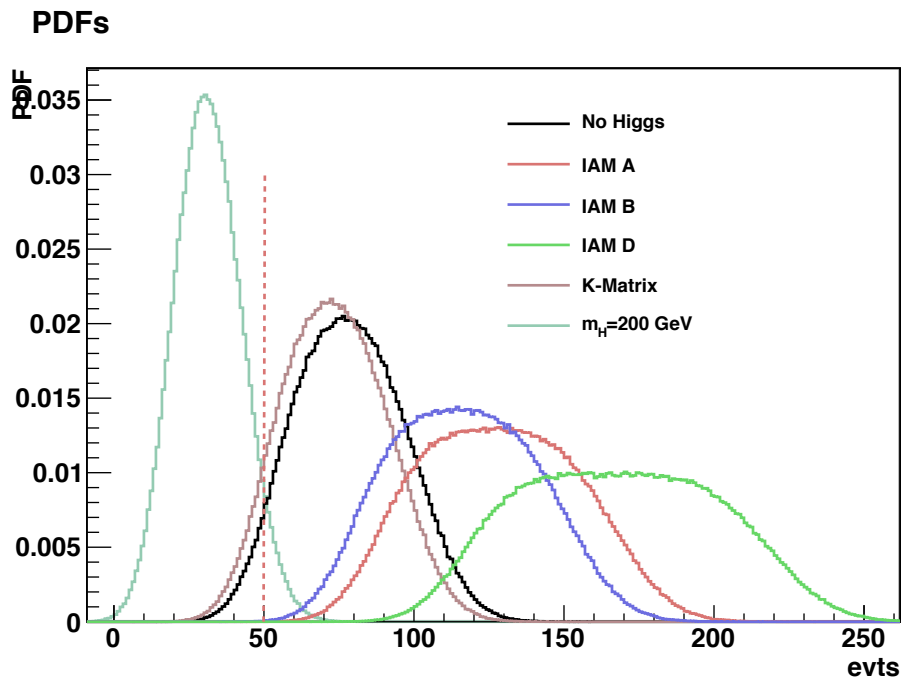
2 examples

4jlv



cross sections fb<sup>-1</sup>  
with all selection cuts

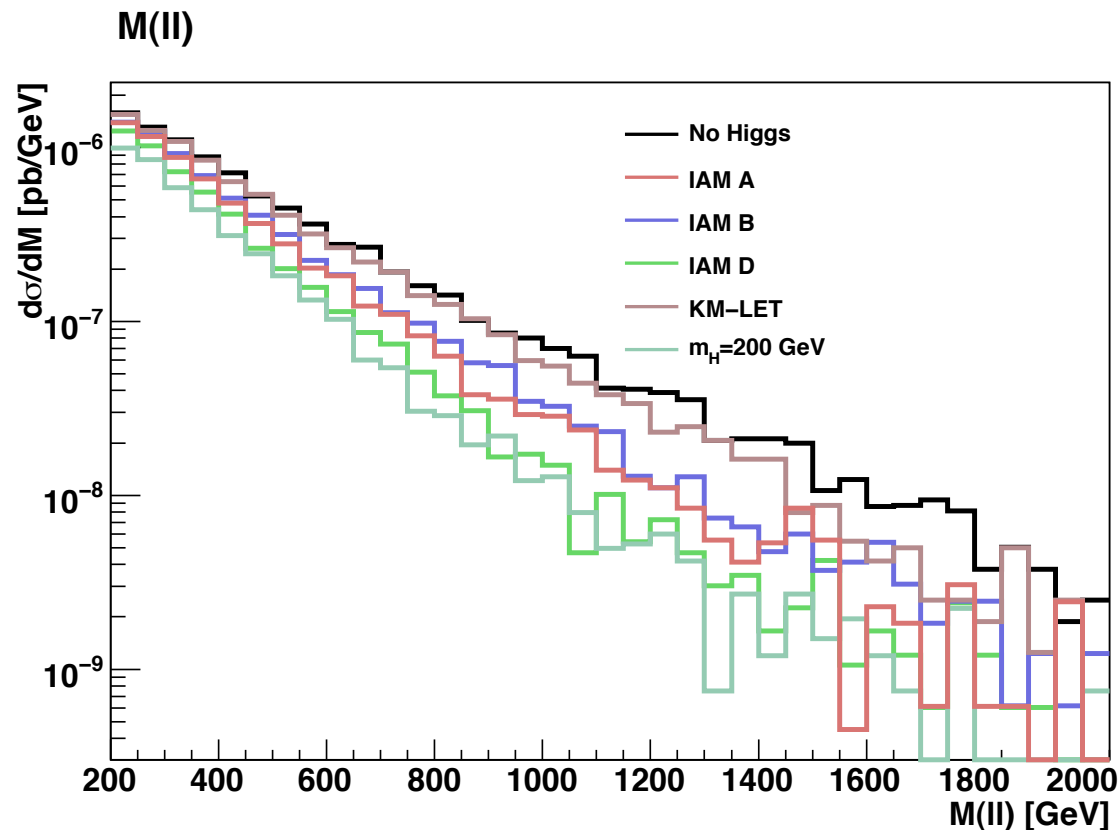
$M_{cut}$	no Higgs	KM-LET	IAM A	IAM B	IAM D	SM	$W + 4j$	$t\bar{t} + 2j$
600	2.36	2.23	3.66	3.04	5.46	1.048	2.03	.432
800	1.558	1.46	2.56	2.32	3.36	.618	1.15	.167
1000	.966	.877	1.13	1.76	1.90	.338	0.62	.0617
1200	.526	.478	.414	1.26	1.27	.188	0.30	.0264



	$L \text{ fb}^{-1}$	$M_{cut}$	no-Higgs	KM-LET	IAM A	IAM B	IAM D
PB SM@95Cl	50	800	94.51%	91.03%	99.99%	99.97%	100%
	200	800	99.93%	99.64%	100%	100%	100%

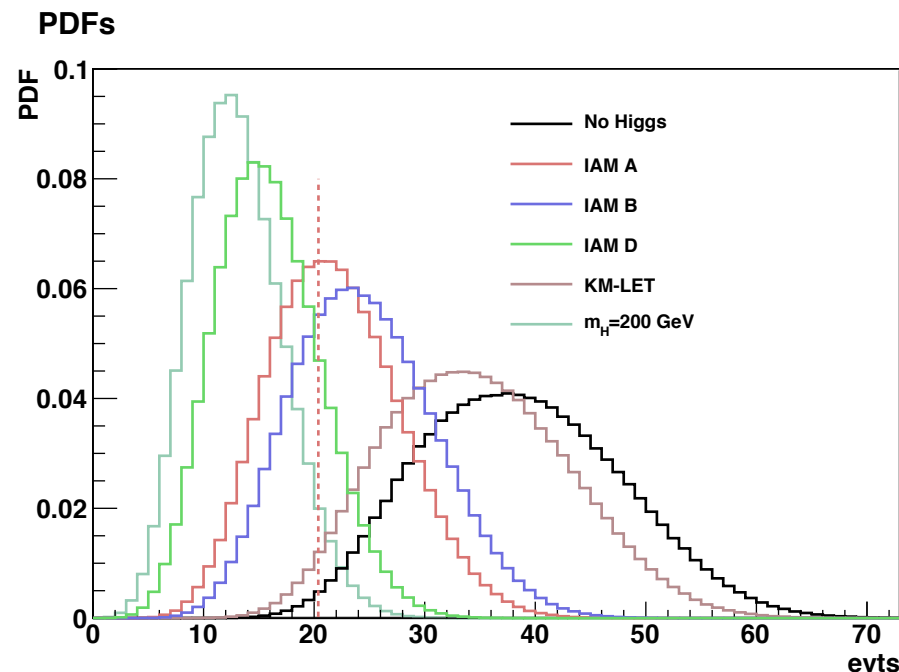
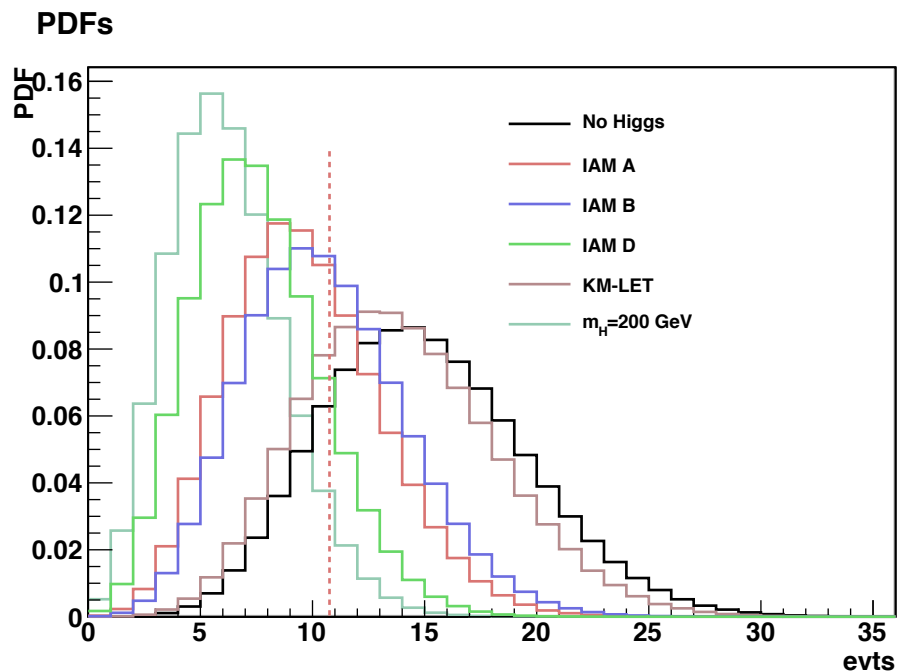


2jllvv samesign



cross sections fb<sup>-1</sup>  
with all selection cuts

$M_{cut}$	no Higgs	KM-LET	IAM A	IAM B	IAM D	SM
200	.435	.407	.310	.332	.254	.206
300	.290	.267	.183	.201	.141	.114
400	.191	.171	.107	.120	.0768	.0629
500	.129	.112	.0643	.0744	.0430	.0351
600	.0886	.0760	.0403	.0474	.0250	.0194
700	.0614	.0517	.0250	.0304	.0150	.0112



PBSM@95CI

$L \text{ fb}^{-1}$	$M_{cut}$	no-Higgs	KM-LET	IAM A	IAM B	IAM D
50	300	81.42%	74.36%	34.48%	44.36%	13.60%
200	400	98.96%	96.92%	57.72%	72.03%	17.21%



Is it possible to study Boson Boson scattering at 7 TeV?  
With what L?

Preliminary work

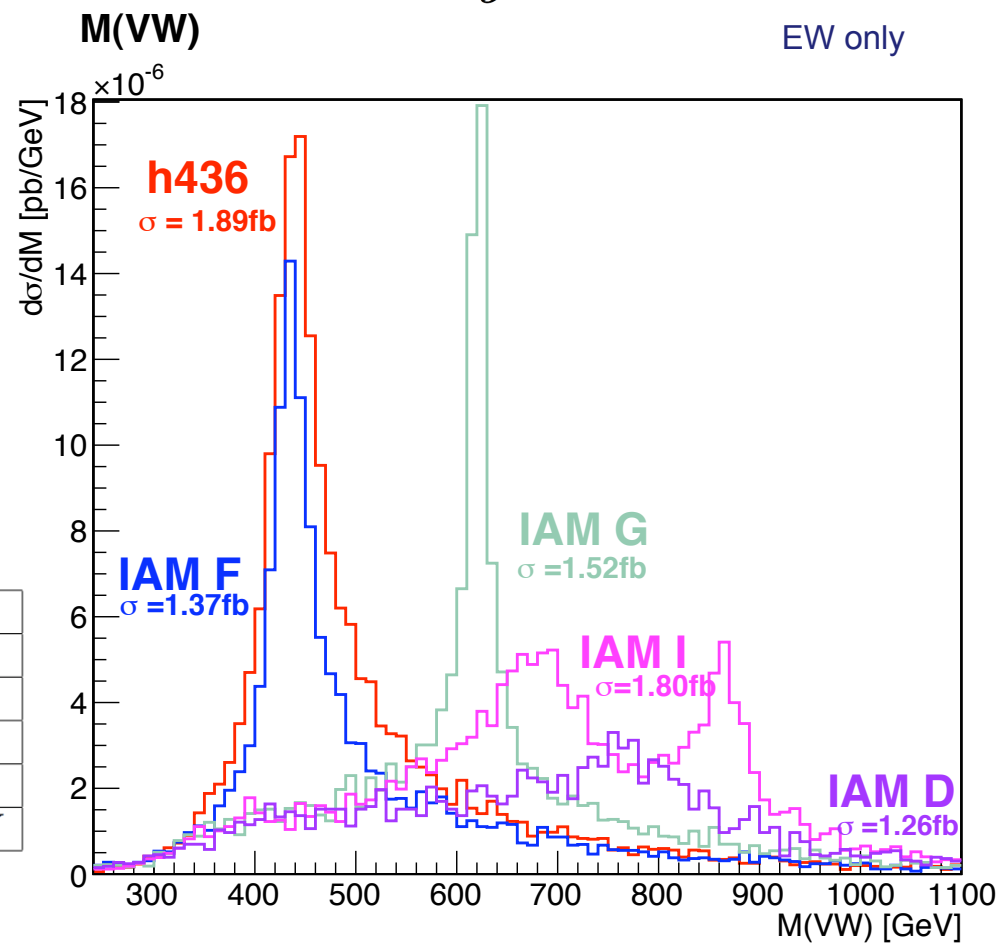
New light resonances scenarios

scenario	$\alpha_4 \times 10^3$	$\alpha_5 \times 10^3$	res	$\sim M_r (TeV)$
IAM A	0	3	s	1
IAM B	2	-3	v	1.4
IAM D	8	0	s+v	0.8 1.4
IAM F	15	10	s	0.44
IAM G	15	-12	v	0.62
IAM I	15	-2.5	s+v	0.7 0.87

$4j\ell\nu$

New reduced set of cuts

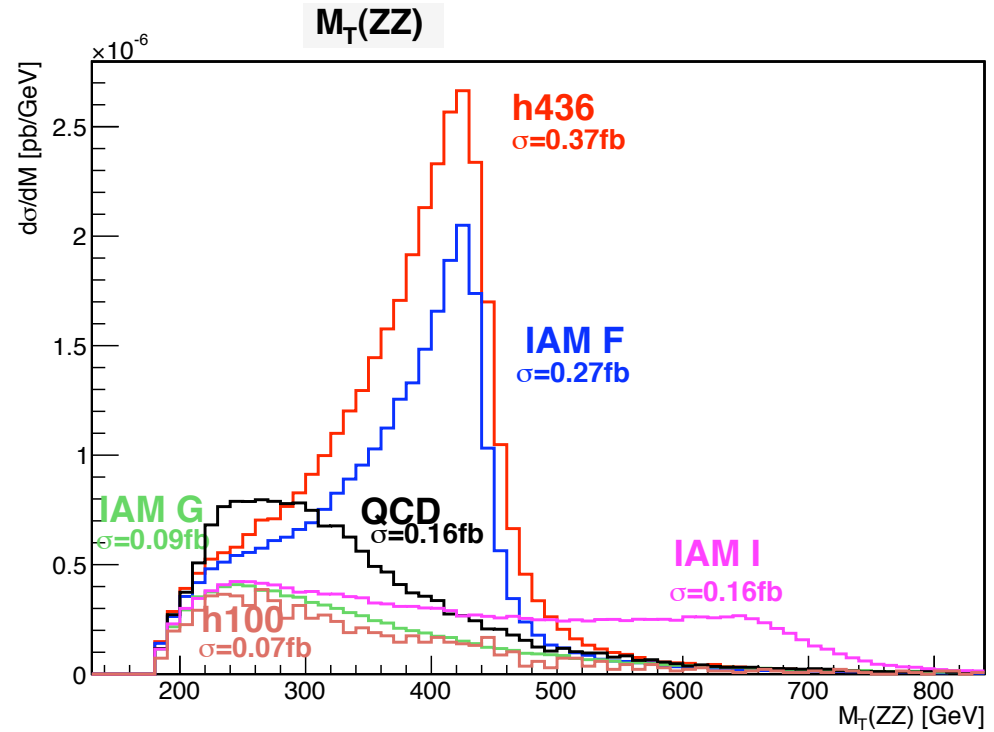
Cuts $4j\ell\nu$	
$\eta(\mu) < 2$	$M(j_f j_b) > 100 \text{ GeV}$
$p_T(\mu) > 20 \text{ GeV}$	$\Delta\eta(j_f j_b) > 3$
$\cancel{P}_T > 70 \text{ GeV}$	$p_T(j) > 30 \text{ GeV}$
$\Delta\eta(V j_{f,b}) > 0.3$	$p_T(j_c) > 70 \text{ GeV}$
$M(jV) - M_{TOP} > 15 \text{ GeV}$	$60 \text{ GeV} < M(j_c j_c) < 100 \text{ GeV}$



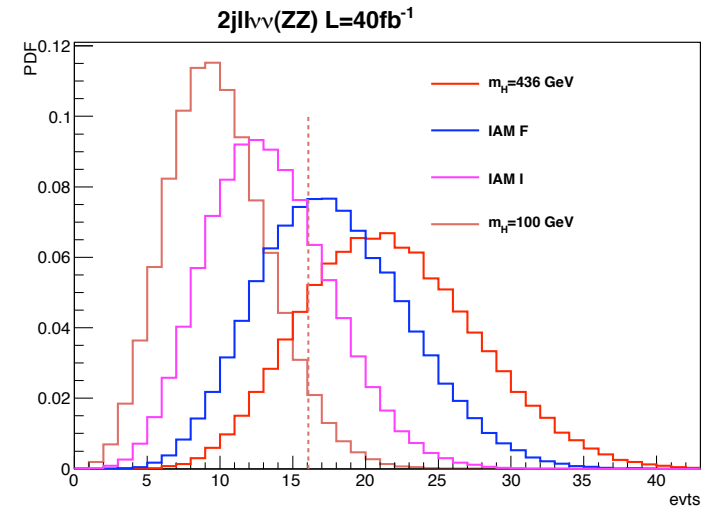


$$2jZZ \rightarrow 2j\ell^+\ell^-\nu\nu$$

Cuts $2jZZ \rightarrow 2j\ell^+\ell^-\nu\nu$	
$\eta(\mu) < 3$	$M(jj) > 100 \text{ GeV}$
$p_T(\mu) > 20 \text{ GeV}$	$\Delta\eta(jj) > 3$
$ M(\mu\mu) - M_Z  < 15 \text{ GeV}$	$p_T(j) > 30 \text{ GeV}$
$\cancel{P}_T > 120 \text{ GeV}$	



Cross Sections (fb) and PBSM@95%CL						
	IAM F	IAM G	IAM I	H436	H100	QCD
$\sigma$	.270	.090	.159	.368	.0744	.163
PBSM $L = 20 \text{ fb}^{-1}$	44.1714	n.c.	18.50	65.39	—	—
PBSM $L = 40 \text{ fb}^{-1}$	61.0219	n.c.	25.53	82.81	—	—

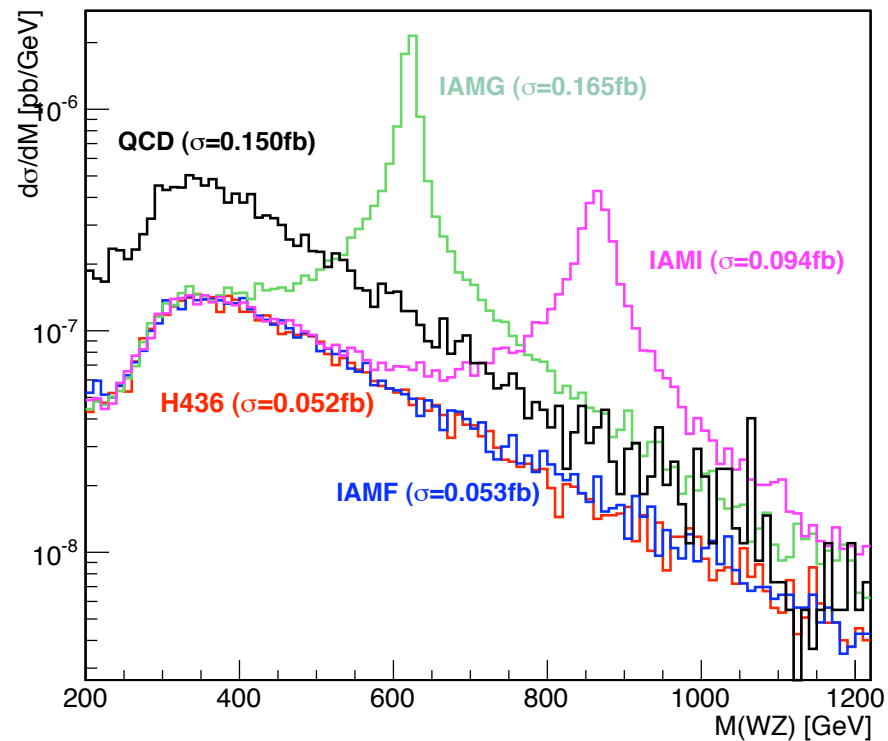




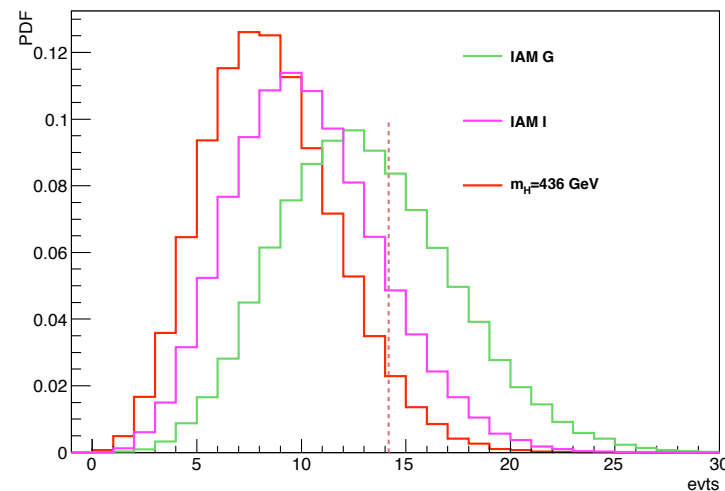
# 2j3lν

Cuts 2j3lν	
$\eta(\mu) < 3$	$M(jj) > 100 \text{ GeV}$
$p_T(\mu) > 20 \text{ GeV}$	$\Delta\eta(jj) > 3$
$p_T(Z) > 100 \text{ GeV}$	$p_T(j) > 30 \text{ GeV}$
$p_T(W) > 100 \text{ GeV}$	$\Delta\eta(Vj) > 0.6$
$P_T > 20 \text{ GeV}$	

## M(WZ)



2j3lv L=40fb<sup>-1</sup>



Cross Sections (fb) and PBSM@95%CL (%)					
	IAM F	IAM G	IAM I	H436	QCD
$\sigma$	.053	.165	.094	.052	.150
PBSM $L = 20 \text{ fb}^{-1}$	n.c.	26.50	11.00	—	—
PBSM $L = 40 \text{ fb}^{-1}$	n.c.	37.82	14.01	—	—





- ◆ Boson Boson scattering is the most important channel for EWSB
- ◆ strong experimental effort needed:
  - If higgs not found: to investigate it and try to discover fingerprints of new theories
  - If a higgs is found: VV scattering could still be strong and different from SM predictions
- ◆ Unitarized models can serve as a guide to the exploration of this region and to predict what one could expect from a phenomenological point of view
- ◆ 7 TeV run at foreseen luminosity can only start to examine this region and possible scenarios
- ◆ 14 TeV at full lumi will surely prove or exclude most of possible alternatives to SM EWSB