

ISR PERFORMANCE REPORTRun 600 - 20 May 1975Ring 1 - 26 GeV/cA simple and precise method for coupling measurementIntroduction

The simple and precise method for measuring the magnitude of the coupling coefficient of the difference resonance as proposed in Ref. 1 works well in practice. The method consists in observing simultaneously the following two quantities of the coherent coupled oscillations of beam excited by a horizontal kick:

- i) the period  $T$  of the amplitude modulation in the vertical plane;
- ii) the ratio  $R$  of the minimum to the maximum of the amplitude modulation envelope in the horizontal plane.

The  $T$  and  $R$  are related to the coupling coefficient  $\kappa$ <sup>2)</sup> of the difference resonance by the following expressions:

$$T = \frac{1}{f \sqrt{\Delta^2 + 4|\kappa|^2}} \quad (1)$$

$$R = \frac{|\Delta|}{\sqrt{\Delta^2 + 4|\kappa|^2}} \quad (2)$$

where  $\Delta$  denotes an unperturbed  $Q$ -separation  $\Delta = Q_h - Q_v$ , and  $f$  a revolution frequency of the beam. A simultaneous measurement of  $T$  and  $R$  enables us to get the  $|\kappa|$  and  $|\Delta|$  at once. The method differs from the previous ones<sup>3)</sup> in the point that the unperturbed  $Q$ -separation  $|\Delta|$  is measured at the same time with  $|\kappa|$ . Thus, neither calibrations of the  $\Delta$ -varying magnet nor any tedious data fitting procedures are necessary, which were previously required because of lack of the knowledge of  $\Delta$ . Since it is possible to

quickly know  $|\kappa|$  from a single measurement of T and R, the method may be operational in the ISR, and even an electronic measurement will be possible<sup>1)</sup>.

### Results

The T and R were measured by taking photographs of the filter output signals of the automatic Q-meter. Figure 1 shows an example of the photographs taken. In order to confirm that the proposed method works well in practice, the coupling coefficient is measured at different values of  $\Delta$  with the other conditions fixed. Figure 2 shows the obtained data in this series of the experiment. Here the abscissa denotes the percentage current of the TD1 which is used to vary  $\Delta$ . The obtained values of  $|\kappa|$  for different values of  $\Delta$  agree quite well with each other. From this we can conclude that we can accurately know  $|\kappa|$  by a single measurement provided that the  $\Delta$ -varying magnet is set at an arbitrary value within the region of  $|\Delta|/|\kappa| \lesssim 1.7$ , or  $R \lesssim 0.6$ . In the second series of the experiment, we have tried to seek an optimum setting of the correction skew quadrupole magnet. Figure 3 shows the obtained data of  $|\kappa|$  for different excitations of the skew quadrupole Q2 with the other conditions fixed (Ring 1, central orbit, Q1 = -2.06 %, TD1 = +3.00 %). From this figure it is found that the optimum setting of Q2 is -2.4 % for the conditions investigated, and the coupling coefficient  $|\kappa|$  is reduced to as small as  $0.3 \times 10^{-3}$ . The third series of the experiment, intended to survey  $|\kappa|$  at different radial positions of the Ring, could not be made due to PS failure.

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### References

- 1) K. Takikawa, A simple and precise method for measuring the coupling coefficient of difference resonance, to be published.
- 2) G. Guignard, Divisional Report CERN ISR-MA/75-23.
- 3) P.J. Bryant and G. Guignard, ISR Performance Report ISR-MA/PJB/GG/mm of 15 May 1975, Runs 575, 580 and 587.

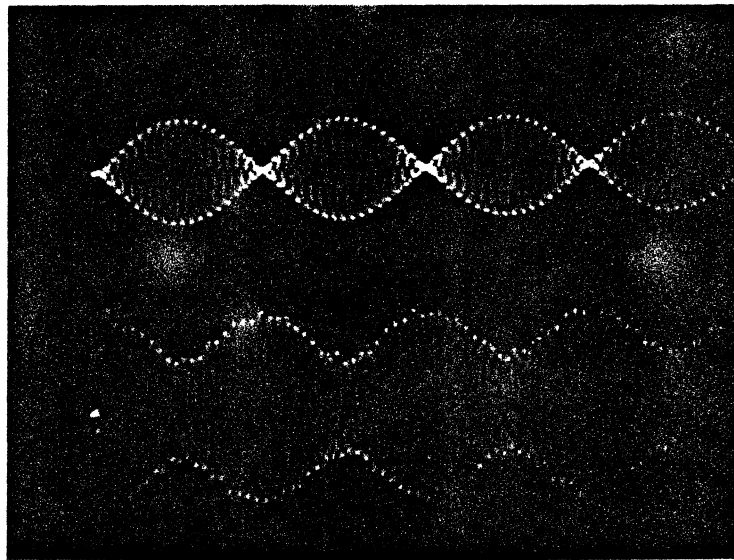


Fig. 1 An example of the photographs of the filter output signals of the automatic Q-meter. The upper trace shows the vertical coherent oscillation, and the lower trace the horizontal coherent oscillation, when the beam is kicked horizontally. The time base is  $0.2\text{ms/div}$ . From the upper trace we obtain the period  $T$ , and from the lower trace the ratio  $R$ .

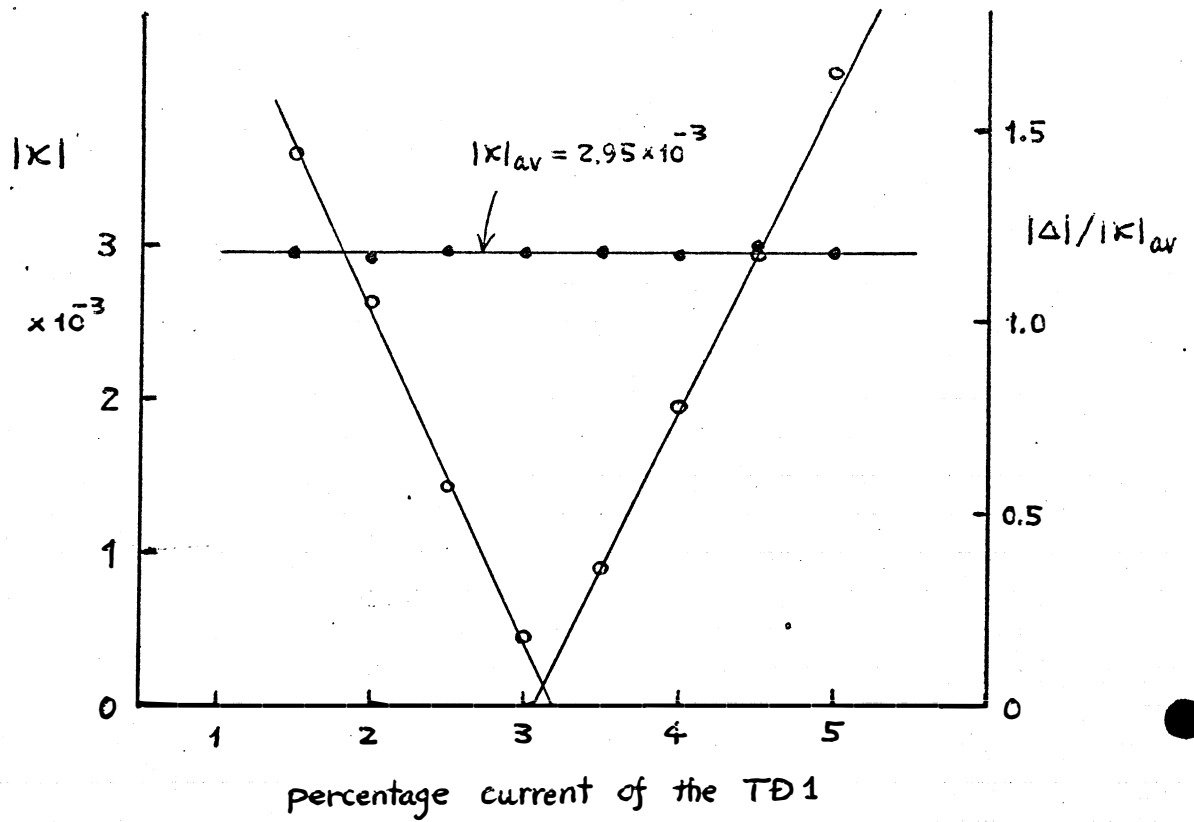


Fig. 2 The coupling coefficient  $|\kappa|$  and the unperturbed Q-separation  $|\Delta|/|\kappa|_{av}$  for different excitations of the TD1.

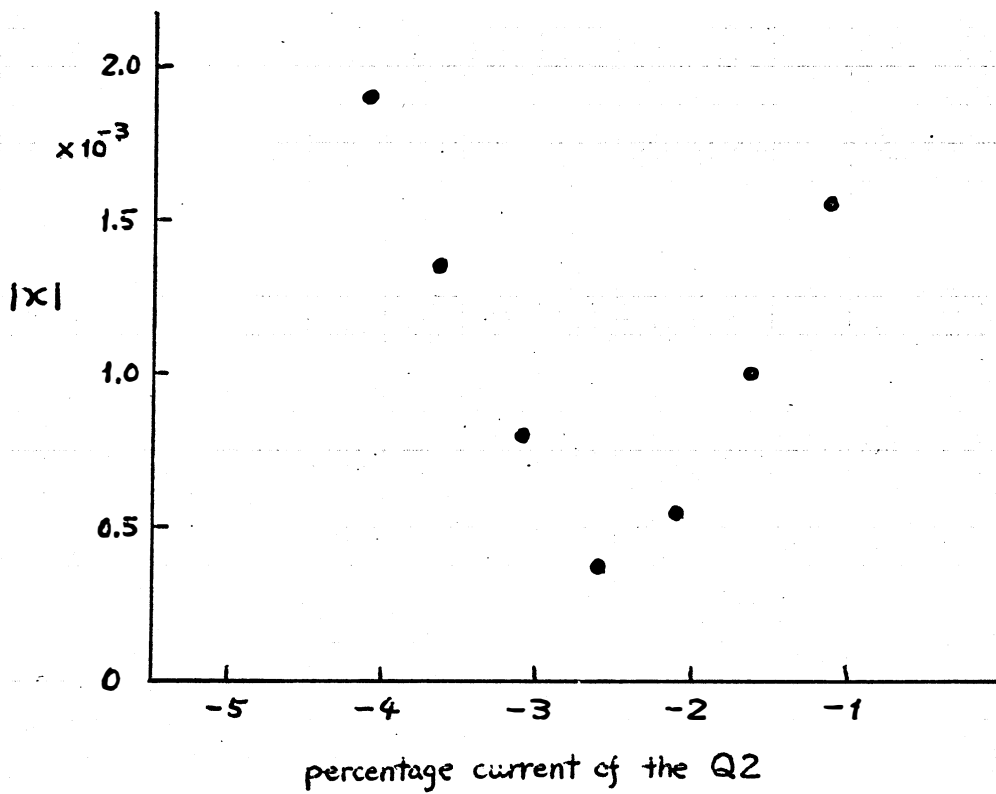


Fig. 3 An optimization of the correction skew-quadrupoles Q2