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AN ANALYSIS OF ANGULAR DISTRIBUTION OF RELATIVISTIC  
PARTICLES IN INELASTIC PION - NUCLEUS COLLISIONS AT 200 GEV/C

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IN INELASTIC PION-NUCLEUS COLLISIONS AT 200 GEV/C

Alma-Ata-Gatchina-Moscow-Tashkent Collaboration

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## ABSTRACT

General parameters characterizing single particle inclusive distributions of shower particles and their dependence on the multiplicity are discussed in  $\bar{p}$ A interactions at 200 Gev. The qualitative comparison of data presented with predictions of several popular models for hadron-nucleus collisions are performed.

Angular spectra of charged secondaries are one of the basic sources of information on the single particle distributions in hadron-nucleus interactions provoking the considerable interest last years in connection with the hope to clarify the mechanism of multiple production at high energies.

The present paper devoted to the study of angular distributions of shower particles in inelastic  $\pi^-$ -nucleus ( $\pi^-A$ ) interactions at  $p_0 = 200$  Gev/c and their dependence of various parameters characterizing incoherent events. Multiplicity distributions and two particle correlations in these collisions were discussed in other papers; some preliminary results on angular characteristics based on a part of the total statistics were published in the papers [1, 2].

The experimental material analyzed in this report consists of 4853 inelastic  $\pi^-A$  events and (for comparison purposes) 1333 events classified as interactions on the free and quasifree nucleons ( $\pi^-N$  events). These events were systematically selected for measurements without any omissions after the "along the track" scanning of emulsion plates exposed to 200 Gev/c  $\pi^-$  mesons at the FNAL accelerator (Batavia). The data for  $\pi^-A$  and  $\pi^-N$  collisions belong to the different lengths of scanned track. The abovementioned numbers of  $\pi^-A$  and  $\pi^-N$  events do not include coherent reactions on emulsion nuclei (those are analyzed in details in the paper [3] ); additionally we have statistically excluded interactions on the free emulsion hydrogen from  $\pi^-A$  events. So, the considered sample of  $\pi^-A$

events consists of incoherent interactions with C,N,O (~26%) and Ag, Br (~74%) nuclei. More detailed information is given in the references [1, 4].

As angular variable we are using the quantity  $\eta = -\ln \tan \frac{\theta}{2}$ , where  $\theta$  is the polar angle in the laboratory system. This is the so called pseudorapidity giving for secondary pions a good approximation of longitudinal rapidity  $y \approx (1/2) \ln [(E+p^z)/(E-p^z)]$ . In cosmic ray physics the quantity  $\lambda = \ln \tan \theta$  is used usually and it is easy to connect  $\eta$  and  $\lambda$  using the relations for the mean values and standards

$$\begin{aligned} \langle \lambda \rangle &\approx -0.43 (\langle \eta \rangle - 0.7), \\ \sigma(\lambda) &\approx 0.43 \sigma(\eta). \end{aligned} \quad (1)$$

The accuracy of these formulae at considered  $p_0$  is not worse than a few % for all analyzed groups of events; the first formula is true, with the same accuracy, also for the separate tracks at  $\eta \geq 1$ .

The existing theoretical approaches to hadron-nucleus interactions can be separated conventionally into two large groups: models with the repeated independent collisions, where hadron-nucleus interactions can be considered as some superposition of intranuclear collisions with the separate nucleons; the second class consists of models, where the effective target at high energies should be considered as structureless medium. In correspondence with the axiomatics of these models the parameter, conditioning structure of the "average" event is, in the

first class, the effective number of intranuclear collisions ( $\langle V \rangle$ ), and, in the second class, the thickness of nuclear matter interacting with a projectile nucleon. Both these quantities, strictly speaking, are not measurable experimentally, however it is widely assumed that their's measure (in average) is given by the number of slow (heavily ionizing or h-) particles emitted by the target nucleus. It has been pointed out in the number of papers (see, for instance [4]) that multiplicity and other characteristics of produced particles under go the most rapid variation with the change in the number of so called g-particles (consisting mainly from recoil protons). So, we can conclude, if the abovementioned circumstance is true, the best quantity characterizing  $\langle V \rangle$  or the mean mass of effective target is  $n_g$ . We are using  $n_g$  as the basic parameter characterizing hA interactions in this sense; due to proportionality (Fig.1) of  $n_g$  and  $n_h$  (h-particles include all the heavily ionizing secondaries having the velocity  $\beta \geq 0.7$ ) all the conclusions about  $n_g$ -dependence of considered characteristics are true also for  $n_h$ -dependencies (we have tested this directly too).

Fig.2 shows inclusive  $\eta$ -distributions of shower particles in A and N interactions at 200 Gev/c as well as in  $\bar{N}A$  interactions with the different  $n_g$ . In Fig.3 we have plotted the difference  $d_n = (1/\sigma_{in}^{NA}) (d\sigma^{NA}/d\eta) - (1/\sigma_{in}^{NN}) (d\sigma^{NN}/d\eta)$ , and the ratios  $r_n = \frac{\sigma_{in}^{NN}}{\sigma_{in}^{NA}} (d\sigma^{NA}/d\eta) / (d\sigma^{NN}/d\eta)$  for the quoted groups of  $\bar{N}A$  interactions. One can see, that:

1.  $\eta$  - distributions in  $\pi^- A$  interactions differ significantly from those in  $\pi^+ N$ ; in  $\pi^- A$  collisions they are enriched by particles with small  $\eta$  and simultaneously they have less number of the most fast (leading) particles. These qualitative features of  $\eta$ -spectra are well known for different projectiles in the wide energy interval. "Deformations" of angular distributions are the stronger, the larger  $n_g$  (and/or  $n_h$ ); this means obviously that the number of slow particles is, in some extent, the measure of the influence of target-nucleus to the production of particles.

2. The shapes of  $\eta$  -spectra in  $\pi^- A$  and  $\pi^+ N$  interactions are different too, they undergo very specific deformation with the growth of  $n_g$  (Fig.2). Distributions in the majority of  $\pi^- A$  groups are characterized by the bimodal structure and contribution of the "second" maximum, which is small at small  $n_g$ , becomes dominant at large  $n_g$ . It is important to notice here that bimodal structure in  $\eta$ -spectra can arise even at the absence of any structure in distributions of longitudinal rapidities due to merely kinematical effects [5], but, on the other hand, the bimodality does not display itself in proton-nucleus interactions at the same  $p_0 = 200 \text{ Gev/c}$  [2] although the influence of secondary protons at accelerator energies should be negligible. This indicates that bimodality is the property inherent to pion-nucleus interactions at high energies.



The noted here changes of  $\eta$ -spectra in  $\bar{N}A$  interactions comparatively with  $\bar{N}N$  collisions, dependence of  $\eta$ -spectra on  $n_g$  and the difference between spectra in  $pA$  and  $\bar{N}A$  interactions at the same  $p_0$ , seem to be hardly explained by the simple versions of "tube" model [6,7], where production in  $hA$  interactions is identical entirely to that in  $hN$  collisions at some higher energies in the Centre of mass system. It should be noted, that the composite nature of emulsion having two groups of nuclei ( $C, N, O$  and  $Ag, Br$ ) cannot be responsible to the observed deformation of  $\eta$ -spectra, since: 1) groups of  $hA$  interactions with  $n_g > 3$  consist of  $Ag, Br$  events solely, 2)  $pA$  interactions in emulsion do not show bimodality, and 3) the direct separation of  $\bar{N}A$  interactions into collisions with  $C, N, O$  and  $Ag, Br$  nuclei performed in accordance with method described in [4] gives the same results (Fig.5).

More detail comparison with predictions of coherent tube model is given below.

3. The differences  $d$  and ratios  $r$  of inclusive distributions on nuclear and nucleon targets shown in Figs.3,4 demonstrate the following characteristic property. The values of pseudo-rapidity  $\eta_0$ , at which  $\frac{1}{G_{in}^{NA}} \frac{dG^{NA}}{d\eta} = \frac{1}{G_{in}^{NN}} \frac{dG^{NN}}{d\eta}$  does not depend within experimental errors on the number of slow particles ( $\eta_0 \approx 5$ ), being consistent with the Gottfried's EFC model [8], which predicts that the value of  $(y_0^* = \eta_0 - \text{Arch } \gamma_c)$ , should depend on  $p_0$  only, being independent on  $A$ . In the multiperipheral model (MPM)[9] the value of  $y_0^*$  in contrast, should

depend on  $A$ , being independent on  $p_0$ . The data presented in Fig.3,4 do not display any  $A$  dependence of  $\eta_0$ , but we cannot state the inconsistency with the MPM due to the qualitative character of prediction. On the other hand, there is the doubtless  $A$  dependence of shape of the "surpluses"  $d$ : distribution demonstrate some structure and their centers displace towards small  $\eta$ . This circumstance contradicts the EFG model. Moreover, the width of distributions, presented in Fig.3 is larger considerably than in  $hN$  interactions at small energies (corresponding to amount of energy carried out by the slow Gottfried's hadrons); this contradiction of experimental data with the EFG model has been stated earlier in the paper [10].

It should be noted, however, that for the certainty the analysis of data in the wide energy interval is needed.

4.  $n_g$  - dependence of ratios of inclusive distributions  $r$  is conditioned by the value of  $\eta$ . The most clearly this can be seen from Fig.6. At  $\eta > \eta_0 \approx 5$   $r$  decreases with growing  $n_g$  in such a way that the larger  $\eta$ , the less  $r$  (the diminishing in the number of leading particles); this contradicts the models including the "passivity" of primary hadrons after the first intranuclear collision.

At  $n_g \leq 7$  the dependence  $r(n_g)$  can be fitted satisfactorily by linear dependences, at larger  $n_g$  there is the effect of "saturation"  $r$  present (Fig.6). These properties of ratio  $r$  agree qualitatively with expectations on the basis of parton picture for  $hA$  interaction [11].

Let us consider some other general characteristics of angular spectra in  $\bar{\pi}A$  collisions. Figs. 7, 8 show  $n_g$  and  $n_h$  dependences of centers  $\langle \eta \rangle$  and standard deviations  $\sigma(\eta)$  of  $\eta$ -distributions (Figure 7 exemplifies  $n_h$  dependences too). Fig. 8 shows additionally the mean values  $\langle \sigma(\eta) \rangle$  of standard deviations of  $\eta$ -spectra from individual  $\bar{\pi}A$  collisions. As seen from Fig. 7,  $\langle \eta \rangle$  decreases monotonically with increasing multiplicity of all types of particles (there is the characteristic "oscillations" between  $\langle \eta \rangle$  for the odd and even multiplicity events at small  $n_g$ , analogical to those observed in  $\bar{\pi}N$  collisions and caused by charge conservation in peripheral interactions). Let us assume, for the estimate of dependence of  $\langle \eta \rangle$  on the number of intranuclear collisions  $\nu$ , that  $\langle \nu \rangle \sim n_g^{1/2}$  (or  $n_h^{1/2}$ ). The justification of this assumption is given by the fact, that  $\langle \nu \rangle \sim A^{1/3}$  and  $n_g$  (or  $n_h$ )  $\sim A^{2/3}$  (see, e.g. [4]). The data presented in Figs. 7, 8 do not contradict the linear dependence of  $\langle \eta \rangle$  on  $\langle \nu \rangle$ , i.e. on  $A^{1/3}$ . This is inconsistent with predictions of the "tube" type models [6, 7] (see [12]).

The another interesting property of  $\eta$ -spectra in  $hA$  interactions is the independence of their widths  $\sigma(\eta)$  on the number of slow particles (Fig. 8). This is true also (except the region of very small  $n_g$ ,  $n_h$ , where the larger part of cross section is governed by peripheral interactions with the one intranuclear nucleon) for the standards of individual collisions. The analogical property has been demonstrated earlier in proton-nucleus interactions in the range 20-200 GeV/c [12].

This peculiarity of angular distributions can be crucial for several models of hA interactions. So, for instance, it contradicts the coherent tube model [7], which predicts that angular spectra in hA interactions are identical to those in hN collisions (with the displacement in the rapidity scale  $(1/6) \ln A$  at larger by  $\sqrt{v}$  energy in the center of mass system. According to this model, the standard of spectrum  $\sigma(\eta)$  must increase with increasing  $v$  (i.e.  $n_g, n_h$ ), since

$$\frac{[\sigma(y)]_{hA}}{[\sigma(y)]_{hN}} \Big|_{p_0 = \text{const}} = \frac{\ln(\sqrt{s})}{\ln s} = 1 + \text{const} \cdot \ln v_{(2)}$$

It should be noted, that application of  $\eta$  (instead of  $y$ ), the consideration of spectra for all shower particles (instead of produced pions) cannot affect the last conclusion since the logarithmic growth of dispersions of  $\eta$  - distributions for charged particles in hN interactions is the well established experimental fact. So, one can conclude, the independence of  $\sigma(\eta)$  on  $n_g$  (or  $n_h$ ) - is the result contradicting the basic assumption of the coherent tube model.

The general properties of angular spectra of relativistic particles in nuclear interactions considered here seem to give the sensitive test for theoretical approaches to the problem. We would like to stress once more that the absence of quantitative calculations according to concrete models makes it difficult to give more certain conclusions about the applicability of nuclear production models.

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FIGURE CAPTIONS

- Fig.1 -  $n_h$  and  $n_g$  as functions of  $n_g$  in  $\pi^-A$  interactions at 200 Gev/c.
- Fig.2 - Inclusive  $\eta$  -distributions for: (a)  $\pi^-A$  and  $\pi^-N$  ;  
(b) for  $\pi^-A$  interactions with different  $n_g$ .
- Fig.3 -  $d$  as function of  $\eta$  for different  $n_g$  groups of  $\pi^-A$  events.
- Fig.4 -  $r$  as function of  $\eta$  for different  $n_g$  groups of  $\pi^-A$  events.
- Fig.5 - Inclusive  $\eta$  -distributions in  $\pi^-N(1)$ ,  $\pi^-CNO(2)$  and  $\pi^-AgBr(3)$  collisions at 200 Gev/c.
- Fig.6 -  $n_g$  dependence of the ratio  $r(\eta) : 1 + 9$  - the data for  $\eta < 0$ ,  $0 < \eta < 1, \dots, 6 < \eta < 7$  and  $\eta > 7$ , respectively. The straight lines are fits at  $n_g \leq 7$ .
- Fig.7 - Dependence of  $\langle \eta \rangle$  on  $n_g$  (a),  $n_g$  (b),  $\sqrt{n_g}$  (c),  $n_h$  (d) and  $\sqrt{n_h}$  (e) in  $\pi^-A$  interactions at 200Gev/c.
- Fig.8 - Dependence of  $\sigma(\eta)$  (the open data circles) and  $\langle \sigma(\eta) \rangle$  (the black points) on  $n_g$  and  $n_g$ . The solid and dotted curves reproduce values of  $\sigma(\eta)$  and  $\langle \sigma(\eta) \rangle$  respectively, for  $\pi^-A$  interactions with  $n_g > 2$ . The triangles shows the data from  $\pi^-N$  interactions.

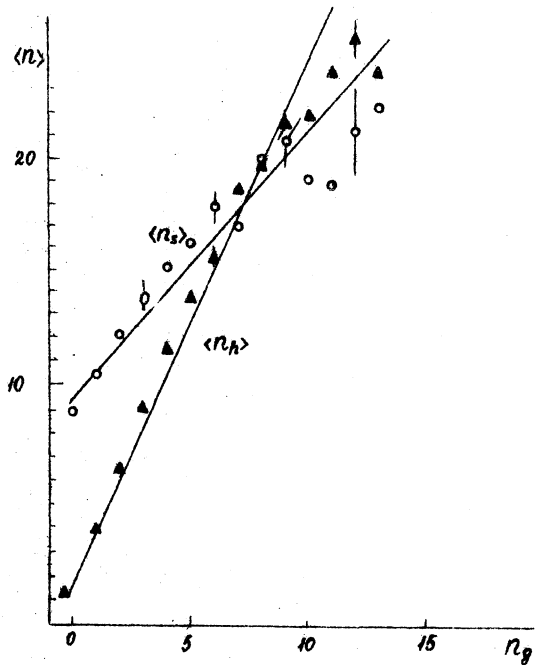


Fig. 1.



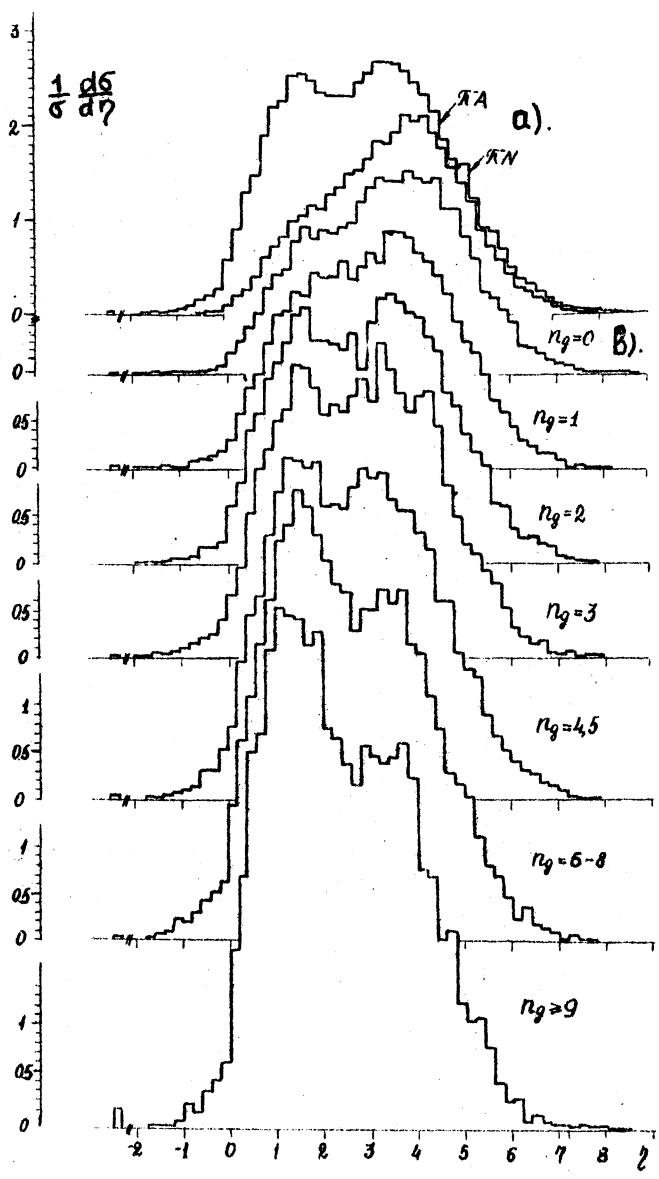
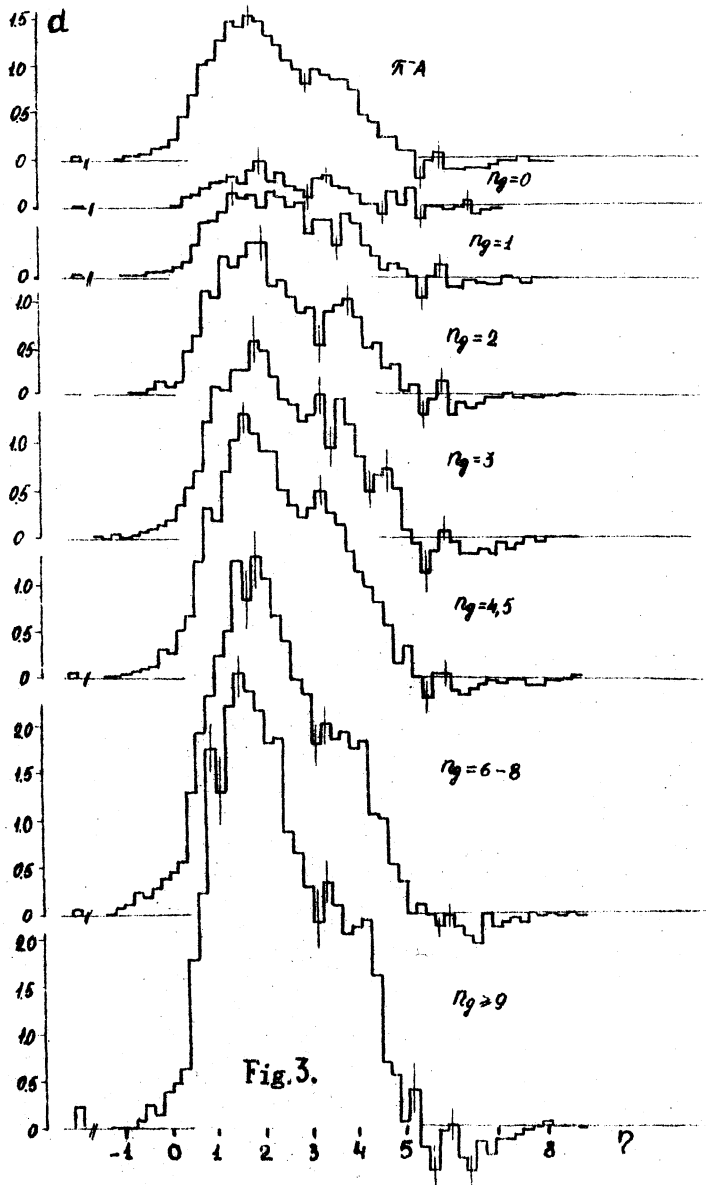


Fig.2.



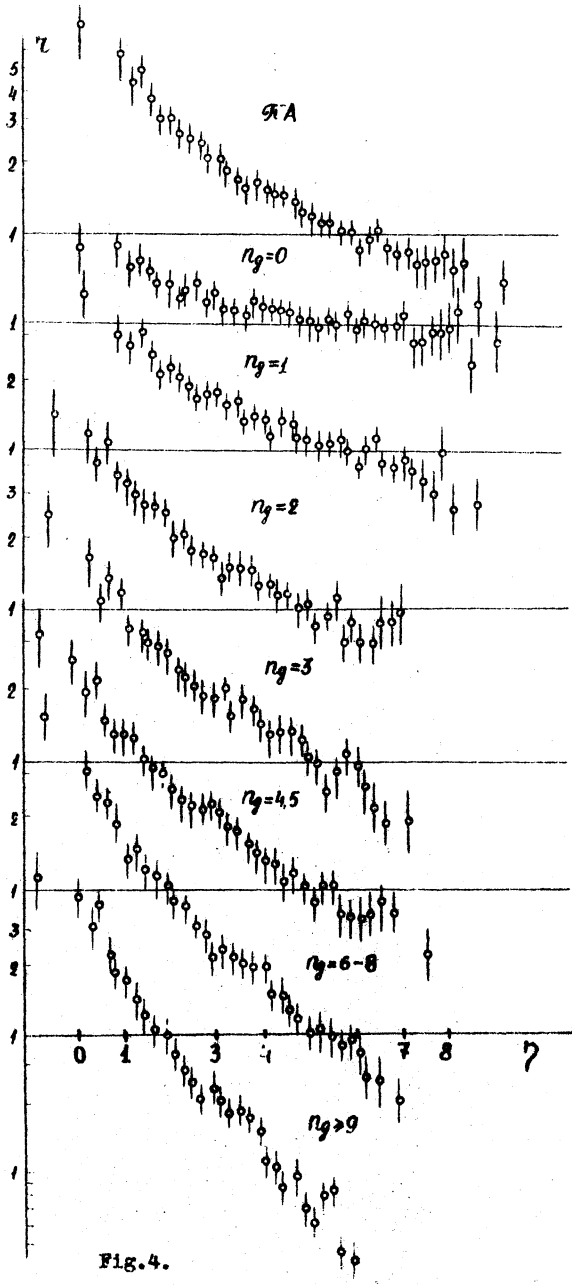


Fig. 4.

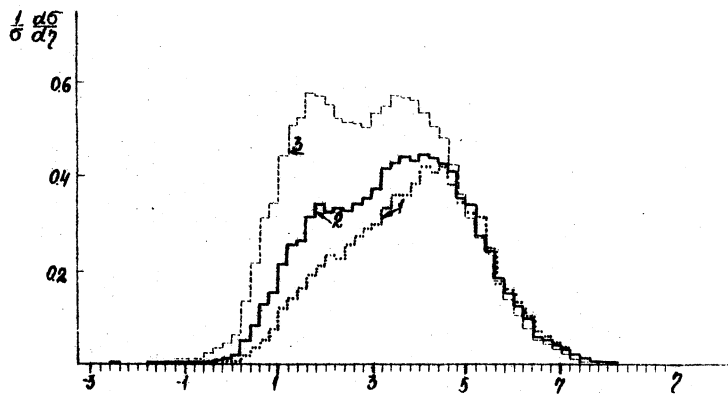


Fig.5.

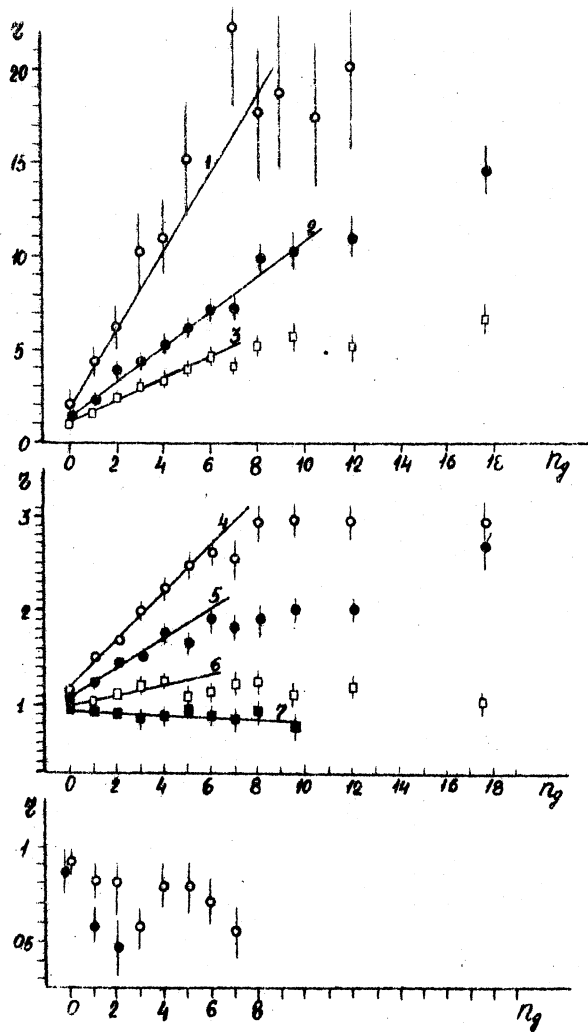


Fig.6.

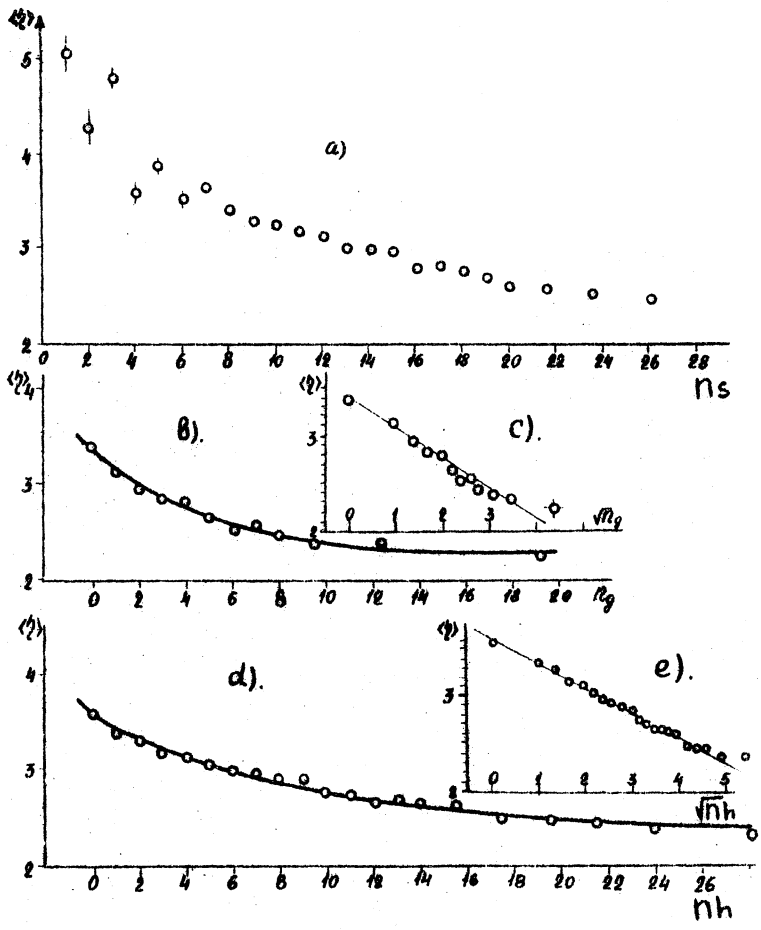


Fig.7.

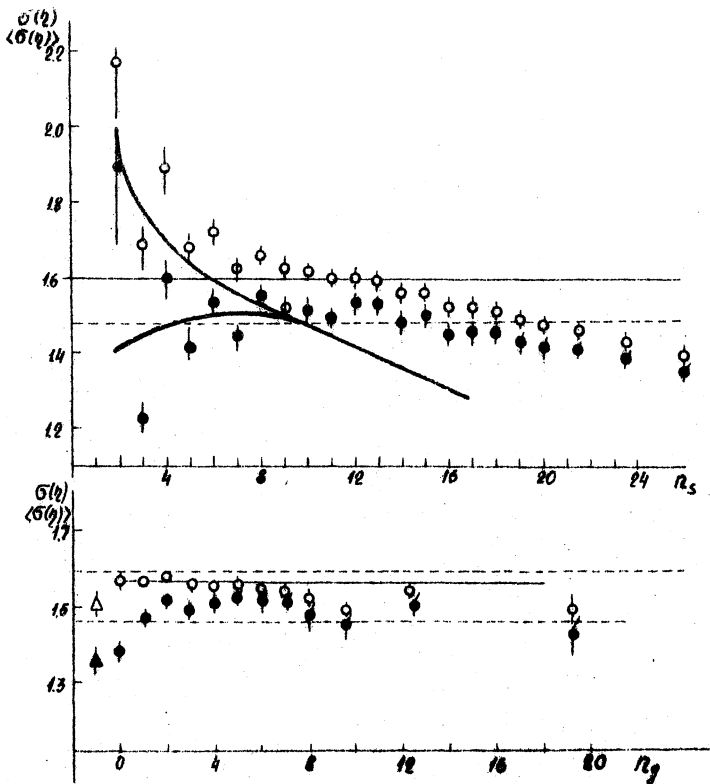


Fig.8.

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