



# Improving Foundation Models for Few-Shot Learning via Multitask Finetuning

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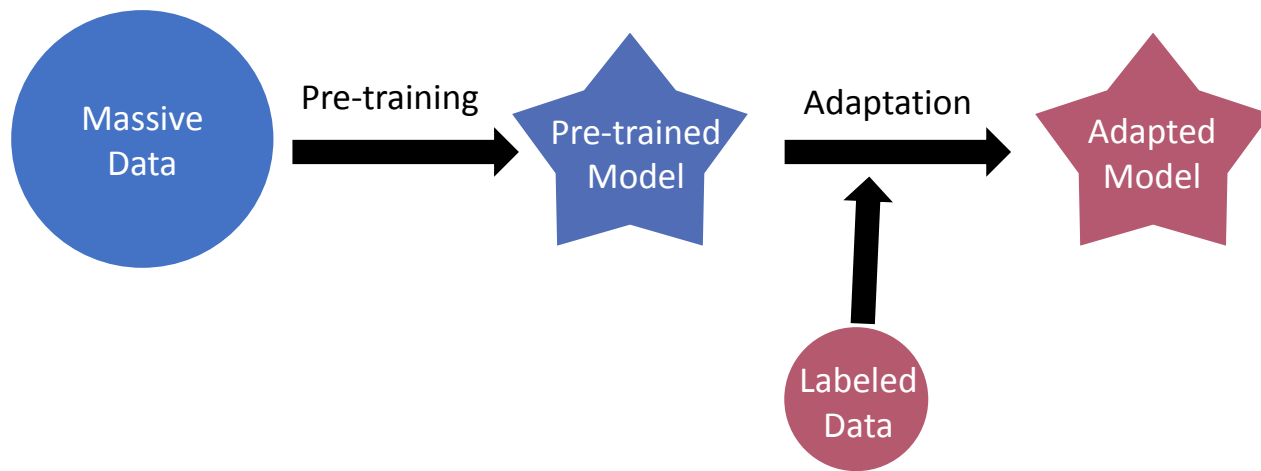
IFDS

# New Paradigm: Pretraining + Adaptation

Paradigm shift: supervised learning  $\implies$  pre-training + adaptation

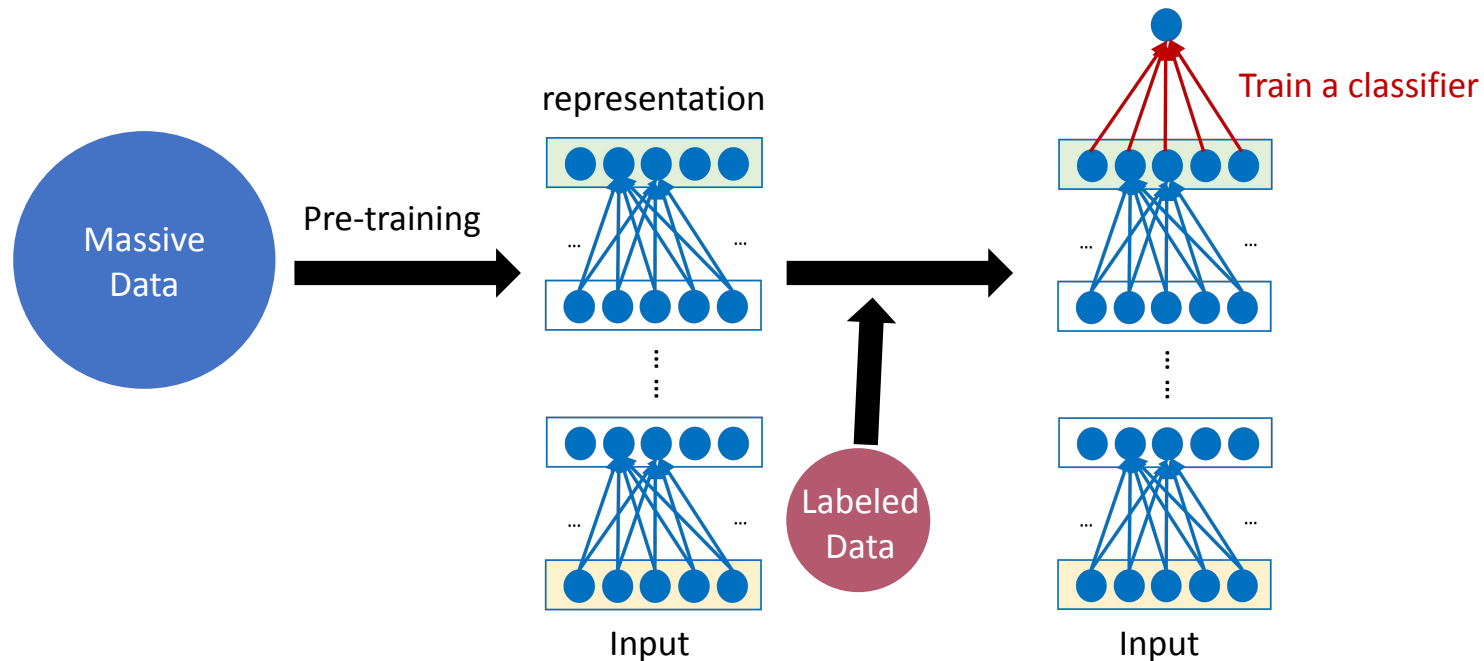
# New Paradigm: Pre-trained Representations

Paradigm shift: supervised learning  $\implies$  pre-training + adaptation



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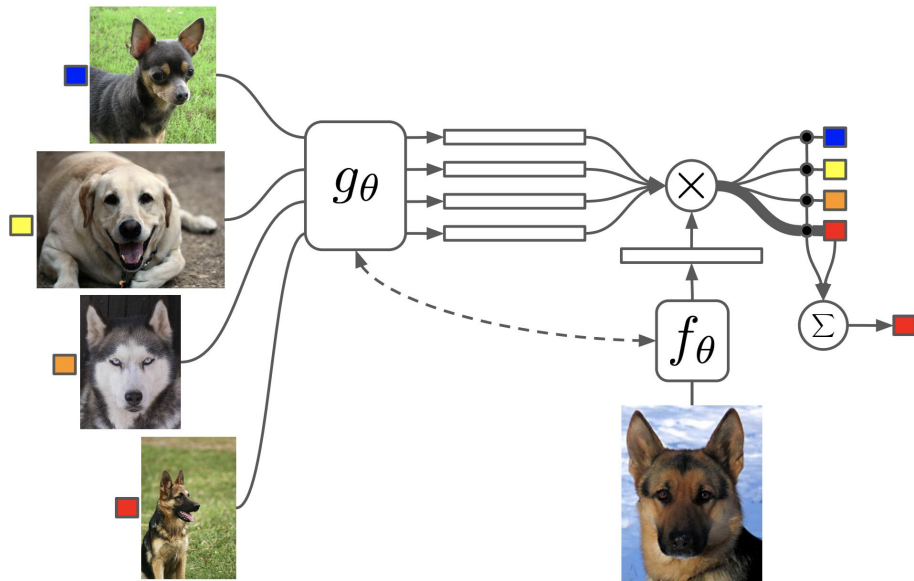


Figure 1: Matching Networks architecture

## Adaptation of a pre-trained image encoder

Figures from: *Matching Networks for One Shot Learning*, 2017.

# New Paradigm: Pre-trained Representations

Paradigm shift: supervised learning  $\implies$  pre-training + adaptation

Circulation revenue has increased by 5% in Finland. // Positive

Panostaja did not disclose the purchase price. // Neutral

Paying off the national debt will be extremely painful. // Negative

The company anticipated its operating profit to improve. // \_\_\_\_\_



Circulation revenue has increased by 5% in Finland. // Finance

They defeated ... in the NFC Championship Game. // Sports

Apple ... development of in-house chips. // Tech

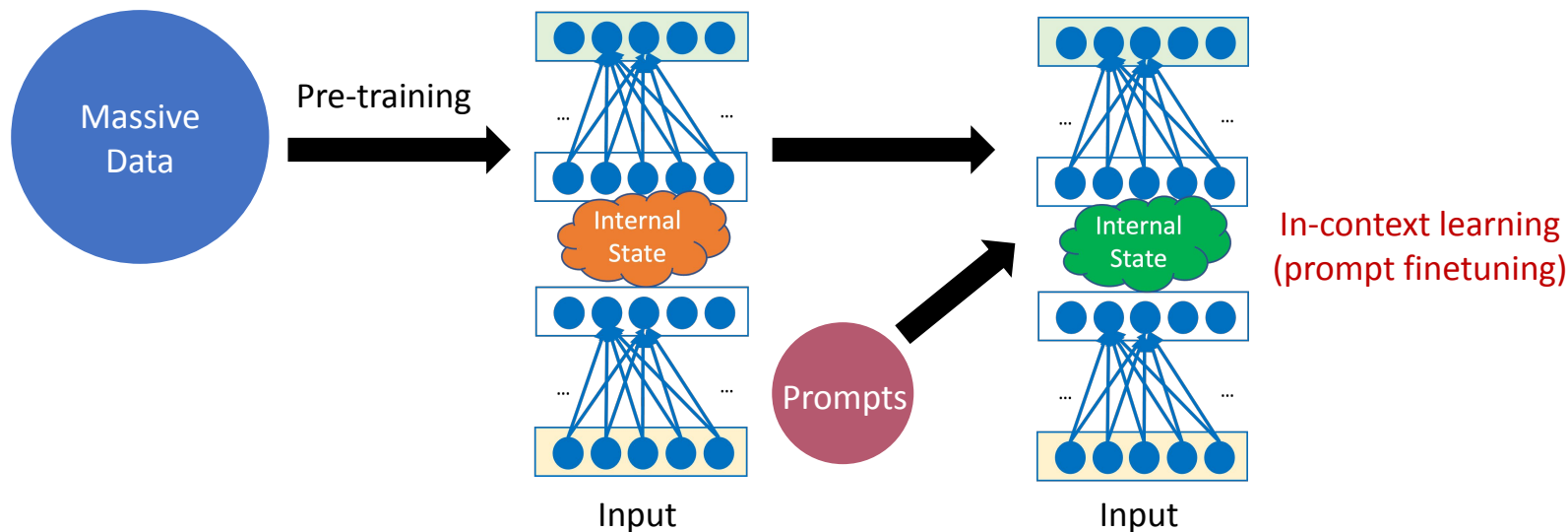
The company anticipated its operating profit to improve. // \_\_\_\_\_



Adaptation of a pre-trained language decoder

# New Paradigm: Pre-trained Representations

Paradigm shift: supervised learning  $\longrightarrow$  pre-training + adaptation

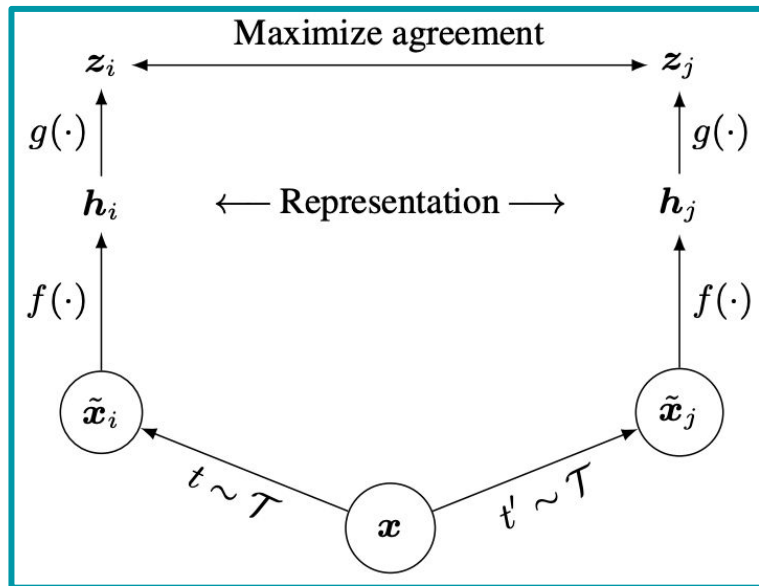


# What does pre-training look like?

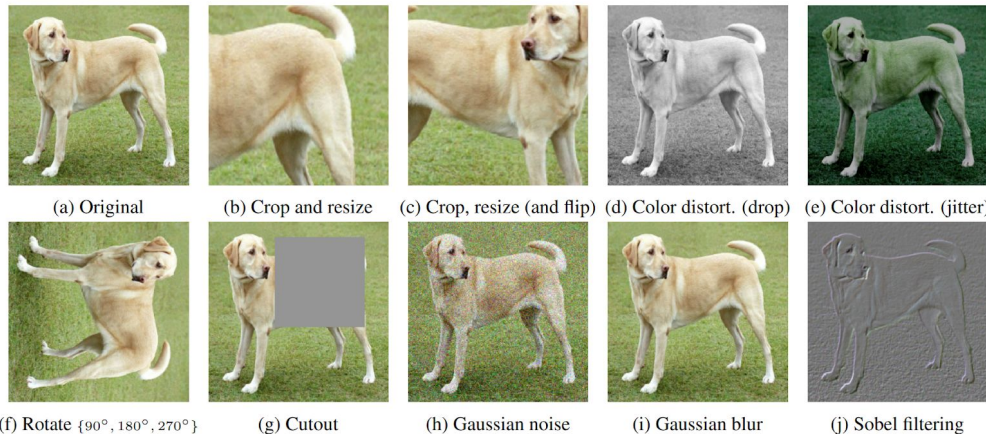
- Supervised learning
- Self-supervised learning:
  - Next sentence prediction (BERT)
  - Masked language prediction (BERT, RoBERTa)
  - Auto-regressive language modeling (GPT series)
  - Contrastive learning (SimCLR, SimCSE, CLIP)



# Intro - Contrastive Learning



$$\ell_{i,j} = -\log \frac{\exp(\text{sim}(z_i, z_j)/\tau)}{\sum_{k=1}^{2N} \mathbb{1}_{[k \neq i]} \exp(\text{sim}(z_i, z_k)/\tau)}$$

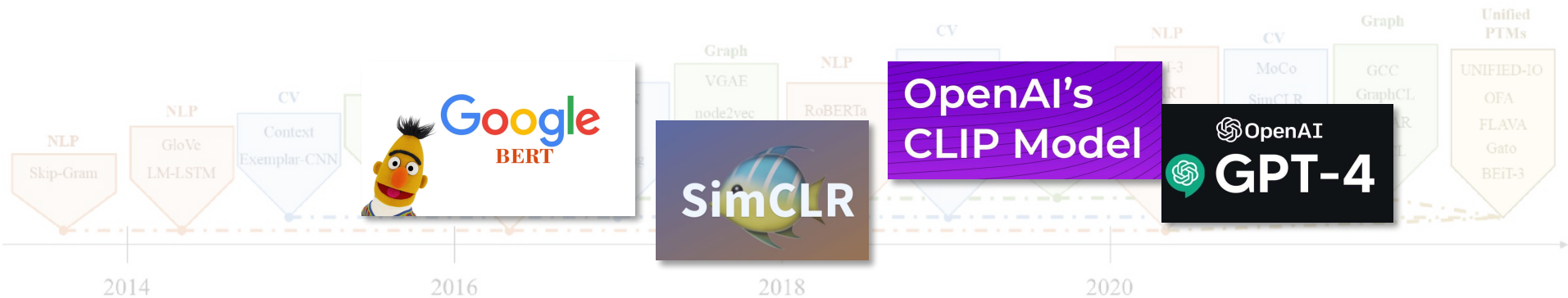


SimCLR - (Image, Image)  
No need labels

Image Data Augmentation

Figures from: *A Simple Framework for Contrastive Learning of Visual Representations, 2020*

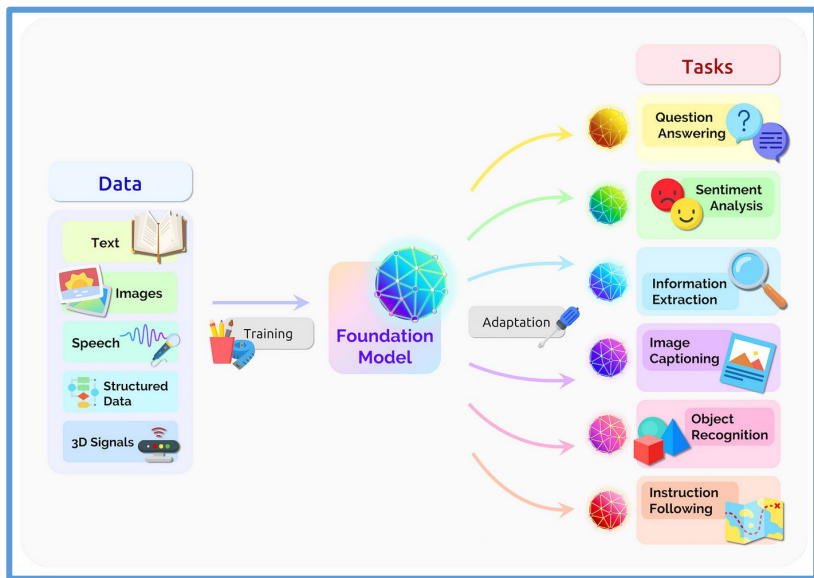
# Intro - Foundation Model



## The history and evolution of foundation models

Figures from: *A Comprehensive Survey on Pretrained Foundation Models: A History from BERT to ChatGPT, 2023.*

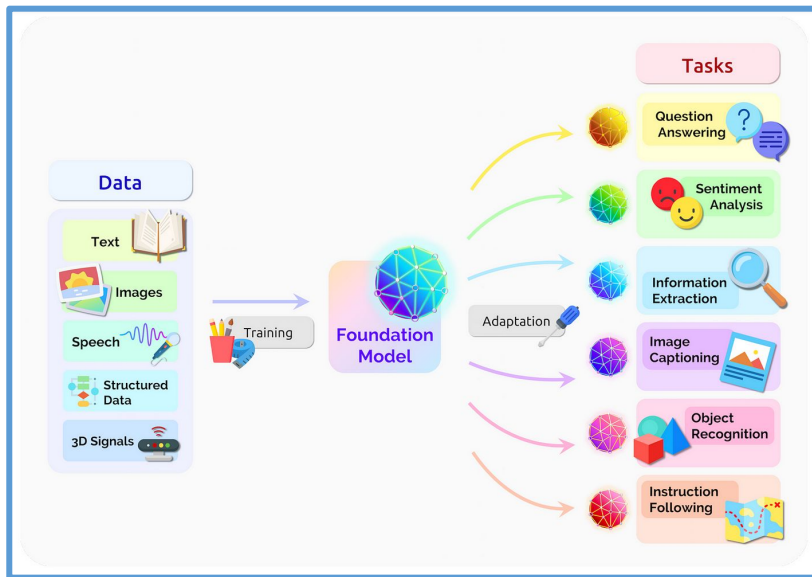
# Intro - Foundation Model



## Universality

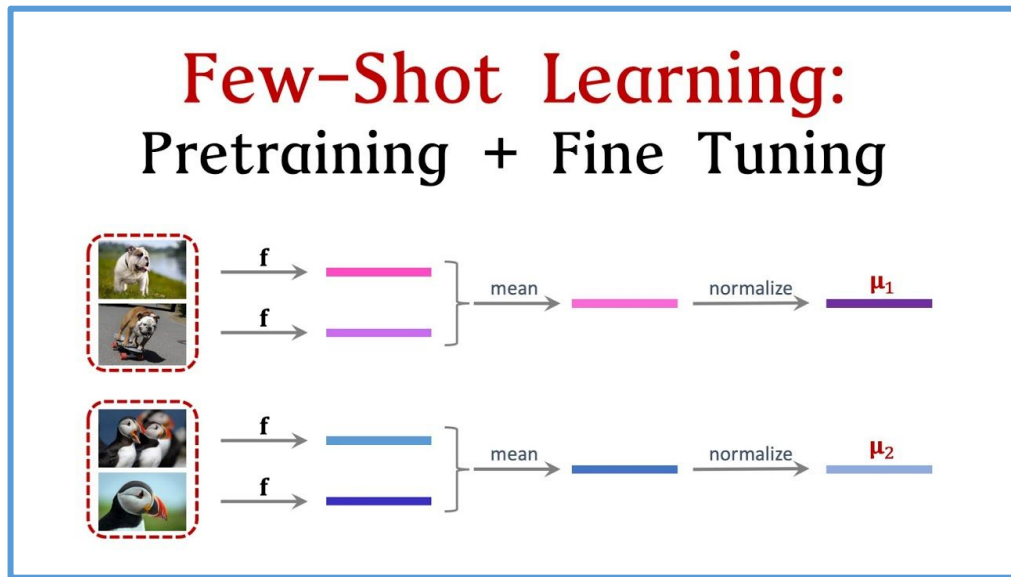
Figures from: *On the opportunities and risks of foundation models, 2021.*

# Intro - Foundation Model



## Universality

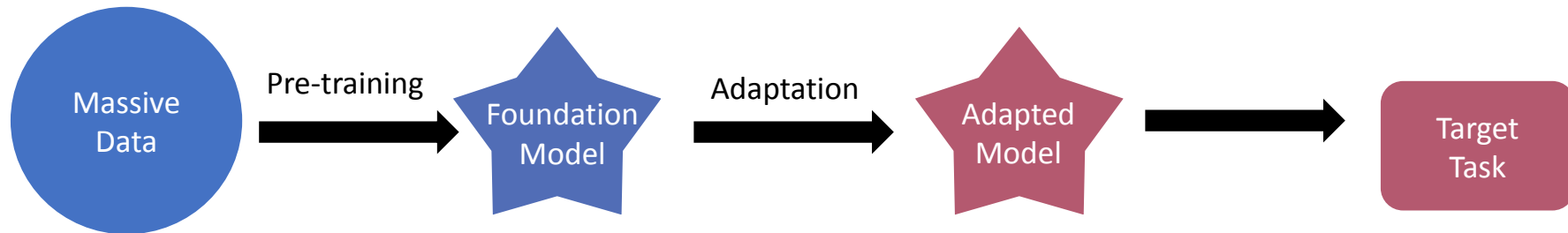
Figures from: *On the opportunities and risks of foundation models, 2021.*



## Label Efficiency

Figures from: [https://www.youtube.com/watch?v=U6uFOIURcD0&ab\\_channel=ShusenWang](https://www.youtube.com/watch?v=U6uFOIURcD0&ab_channel=ShusenWang), 2020

# Paradigm: Pre-training + Adaptation



Pre-training

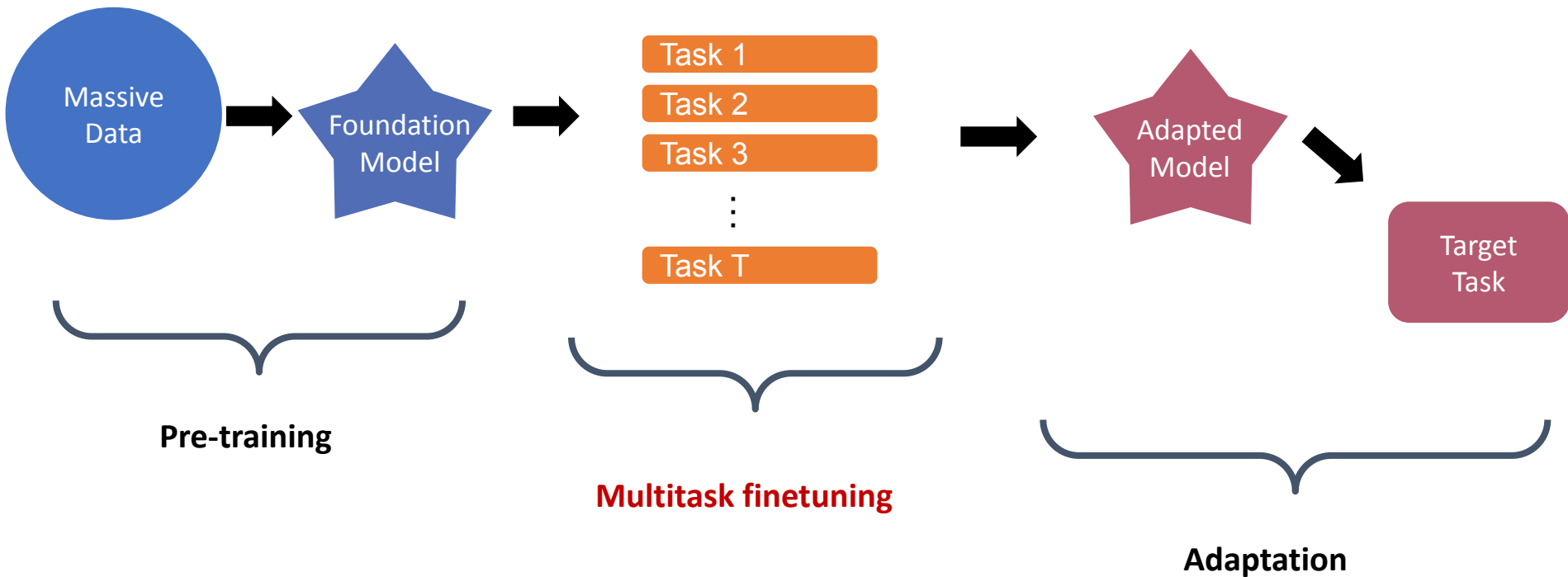


Adaptation



Q: Can we improve this?

# Pre-training + Finetuning + Adaptation



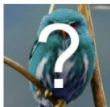
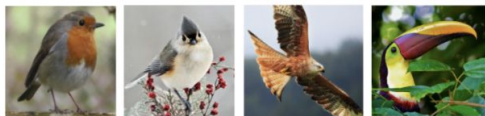
## Training

Train dataset #1: "cat-bird"

cats



birds



Train dataset #2: "flower-bike"

flowers



bikes



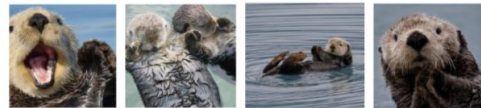
## Testing

Test dataset: "dog-otter"

dogs



otters

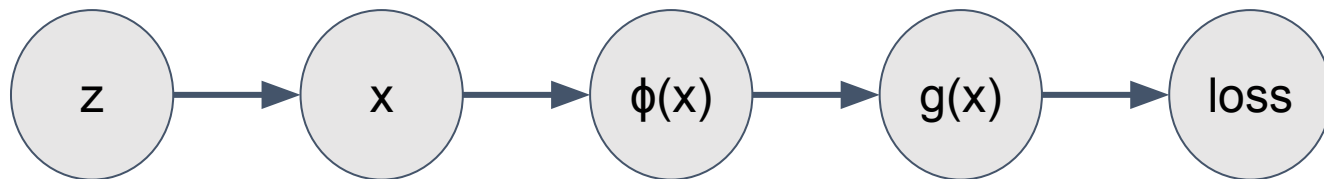


An example of 4-shot 2-class image classification

Figures from: [Meta-Learning: Learning to Learn Fast](#), 2018.

# Problem Setup - Hidden representation data model

- Latent class  $z \in \mathcal{C}$  over distribution  $z \sim \eta$
- Task  $\mathcal{T} = (z_1, \dots, z_{K+1}) \subseteq \mathcal{C}$ , instance  $x \sim \mathcal{D}(z)$
- $\phi \in \Phi$  hypothesis class of representation functions, e.g, ResNet, ViT
- $g(x) = W\phi(x)$  as prediction logits of latent class



**Dog**



$$\begin{bmatrix} \phi_1 \\ \phi_2 \\ \vdots \\ \phi_d \end{bmatrix}$$

$$\begin{bmatrix} g_1 \\ g_2 \\ \vdots \\ g_{K+1} \end{bmatrix}$$

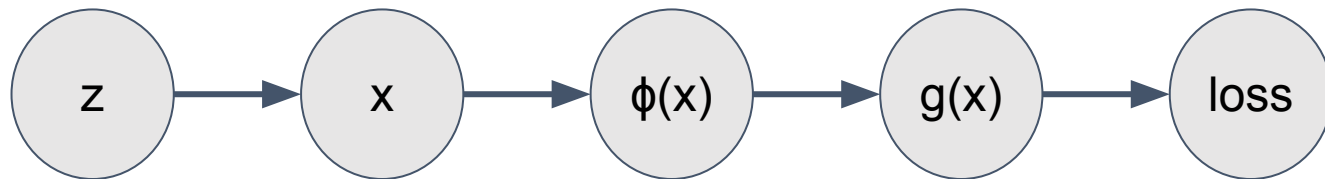
$$\ell(g(x), z) = -\log \left\{ \frac{\exp(g(\mathbf{x})_z)}{\sum_{k=1}^{K+1} \exp(g(\mathbf{x})_k)} \right\}$$



# Problem Setup - Objective for a downstream task?

- Latent class  $z \in \mathcal{C}$  over distribution  $z \sim \eta$
- Task  $\mathcal{T} = \{z_1, z_2\} \subseteq \mathcal{C}$ , instance  $x \sim \mathcal{D}(z)$
- $\phi \in \Phi$  hypothesis class of representation functions, e.g, ResNet, ViT
- $g(x) = W\phi(x)$  as prediction logits of latent class
- supervised loss w.r.t a task:

$$\mathcal{L}_{sup}(\mathcal{T}, \phi) := \min_W \mathbb{E}_{z \sim \mathcal{T}} \mathbb{E}_{x \sim \mathcal{D}(z)} [\ell(W\phi(x), z)]$$

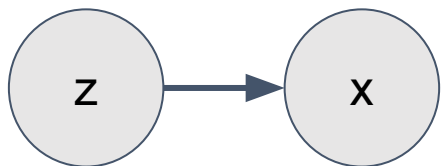


# Problem Setup - Contrastive pre-training

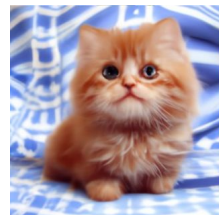
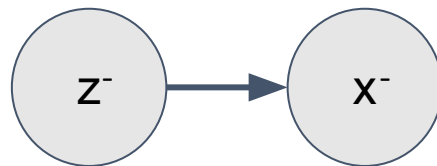
- $(z, z^-) \sim \eta^2$ ,  $x, x^+ \sim \mathcal{D}(z)$ ,  $x^- \sim \mathcal{D}(z^-)$ ,  $\tau := \Pr_{(z, z^-) \sim \eta^2} \{z = z^-\}$

- Contrastive loss:

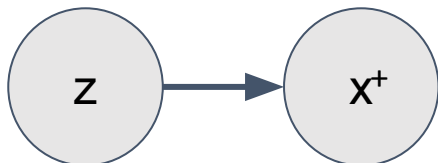
$$\mathbb{E} \left[ -\log \left( \frac{e^{\phi(x)^\top \phi(x^+)}}{e^{\phi(x)^\top \phi(x^+)} + e^{\phi(x)^\top \phi(x^-)}} \right) \right]$$



positive pair



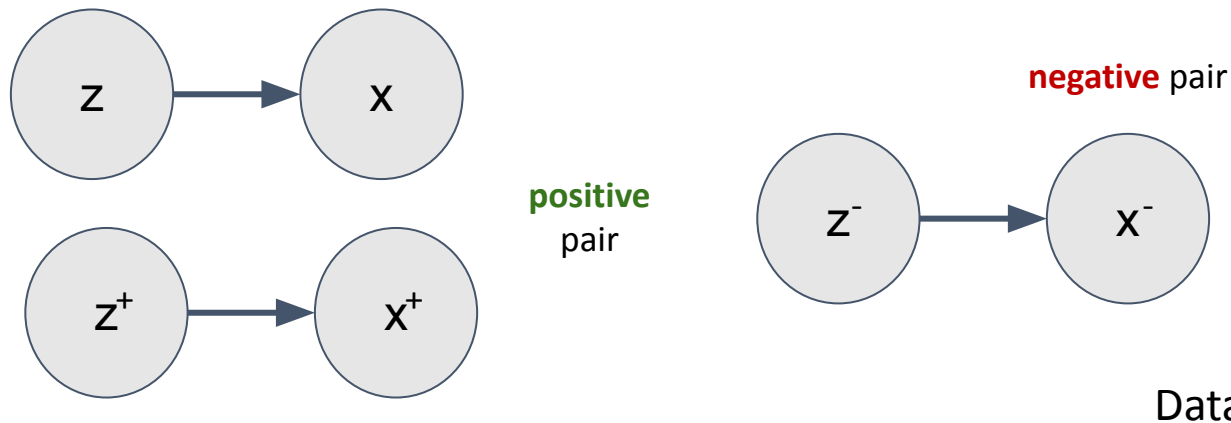
negative pair



Data Model

# Problem Setup - Contrastive pre-training

- $(z, z^-) \sim \eta^2$ ,  $x, x^+ \sim \mathcal{D}(z)$ ,  $x^- \sim \mathcal{D}(z^-)$
- Contrastive loss:  
$$\mathcal{L}_{un}(\phi) := \mathbb{E} [\ell_u (\phi(x)^\top (\phi(x^+) - \phi(x^-)))]$$
$$\widehat{\mathcal{L}}_{un}(\phi) := \frac{1}{N} \sum_{i=1}^N [\ell_u (\phi(x_i)^\top (\phi(x_i^+) - \phi(x_i^-)))]$$
- In particular:  $\ell_u(v) = \log(1 + \exp(-v))$  will recover the loss in previous slide



# Problem Setup - Multitask Finetuning

- Suppose in pre-training we have  $\hat{\mathcal{L}}_{un}(\hat{\phi}) \leq \epsilon_0$
- Suppose we construct  $M$  tasks, each with  $m$  sample
- We further multitask finetune to get a new  $\phi'$  by:

$$\min_{W_i \in \mathbb{R}^d, \phi \in \Phi} \frac{1}{M} \sum_{i=1}^M \frac{1}{m} \sum_{j=1}^m \ell(W_i \cdot \phi(x_j^i), z_j^i), \quad \text{s.t.} \quad \hat{\mathcal{L}}_{un}(\phi) \leq \epsilon_0$$

Intuition: Comparing to direct training, this reduce hypothesis space from  $\Phi$  to  $\Phi(\epsilon_0) = \left\{ \phi \in \Phi : \hat{\mathcal{L}}_{un}(\phi) \leq \epsilon_0 \right\}$

# Main Result

- Suppose target task is  $\mathcal{T}_0$
- Suppose there is  $\phi^*$  such that supervised loss are small across all tasks
- We want to bound  $\mathcal{L}_{sup}(\mathcal{T}_0, \phi) - \mathcal{L}_{sup}(\mathcal{T}_0, \phi^*)$

## Theorem 1 (Contrastive pre-training loss(baseline))

Suppose in pre-training we have  $\hat{\mathcal{L}}_{un}(\hat{\phi}) \leq \epsilon_0$ , then:

$$\mathcal{L}_{sup}(\mathcal{T}_0, \hat{\phi}) - \mathcal{L}_{sup}(\mathcal{T}_0, \phi^*) \leq \mathcal{O}((2\epsilon_0 - \tau) - \mathcal{L}_{sup}(\phi^*))$$

# Main Result

- Suppose target task is  $\mathcal{T}_0$
- We want to bound  $\mathcal{L}_{sup}(\mathcal{T}_0, \phi) - \mathcal{L}_{sup}(\mathcal{T}_0, \phi^*)$

## Theorem 2 (Multitask finetuning loss(Ours))

Suppose we solve multitask finetuning optimization with empirical loss smaller than  $\epsilon_1 = 2\alpha\epsilon_0$  and got  $\phi'$ . If:

$$M \geq \Omega\left(\frac{1}{\epsilon_1} \left[ \mathcal{R}_M(\Phi(\epsilon_0)) + \frac{1}{\epsilon_1} \log\left(\frac{1}{\delta}\right) \right]\right), \quad Mm \geq \Omega\left(\frac{1}{\epsilon_1} \left[ \mathcal{R}_{Mm}(\Phi(\epsilon_0)) + \frac{1}{\epsilon_1} \log\left(\frac{1}{\delta}\right) \right]\right)$$

Then with prob  $1 - \delta$ ,

$$\mathcal{L}_{sup}(\mathcal{T}_0, \phi') - \mathcal{L}_{sup}(\mathcal{T}_0, \phi^*) \leq \mathcal{O}(\alpha(2\epsilon_0 - \tau) - \mathcal{L}_{sup}(\phi^*))$$

# Remark

- Comparing to pre-training + adaptation(baseline), our multitask finetuning reduce error on target task by  $2(1 - \alpha)\epsilon_0$   
where finetuning sample complexity is  $\Theta\left(\frac{1}{\alpha\epsilon_0}\right)$
- Comparing to traditional supervised learning, self-supervised pre-training reduce error by  $O\left(\frac{1}{M_m} [\mathcal{R}_{M_m}(\Phi) - \mathcal{R}_{M_m}(\Phi(\epsilon_0))]\right)$

# Experiments: Few-shot Vision tasks

15-way accuracy (%) on *tiered-ImageNet*, 1 image per class in target task

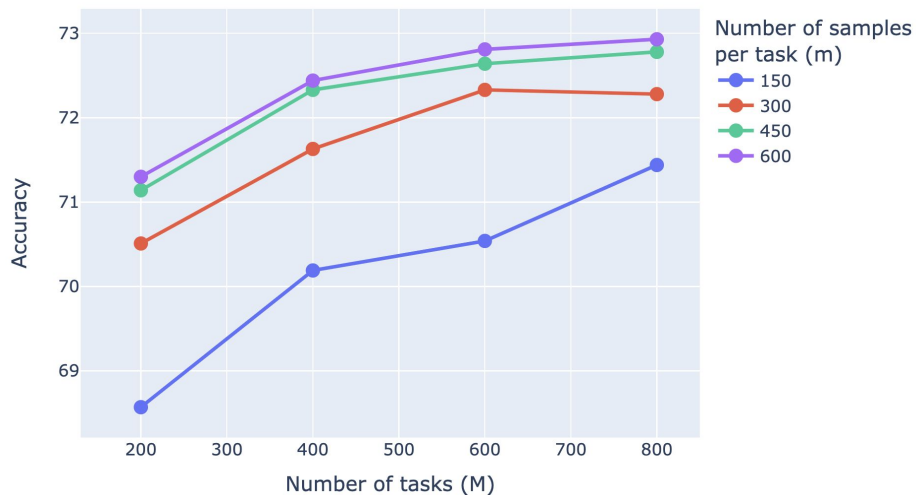
Backbone	Direct Adaptation	Finetuning
ViT-B32	59.55 $\pm$ 0.21	<b>68.57</b> $\pm$ 0.37
ResNet50	51.76 $\pm$ 0.36	<b>57.56</b> $\pm$ 0.36

Effects of multitask finetuning

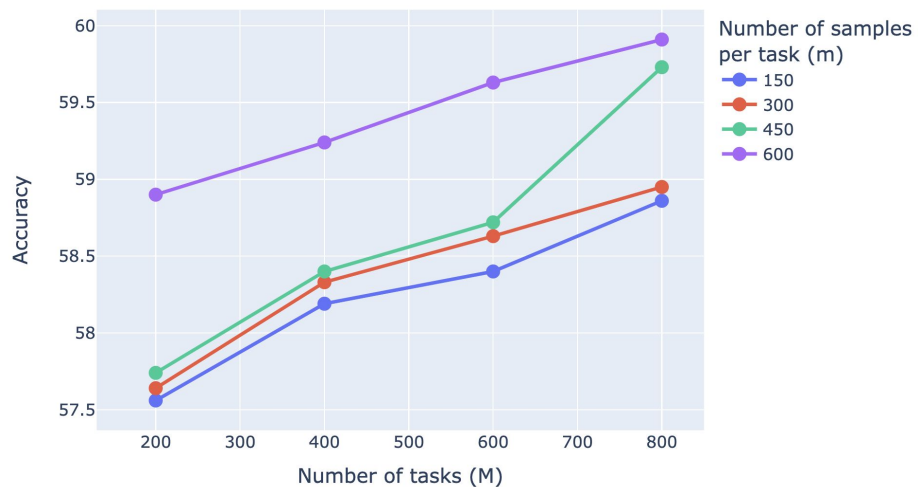


# Experiments: Few-shot Vision tasks

15-way accuracy (%) on *tiered-ImageNet*, 1 image per class in target task



ViT-B32



ResNet50

Accuracy with varying number of tasks and samples

# Experiments: Few-shot Language task

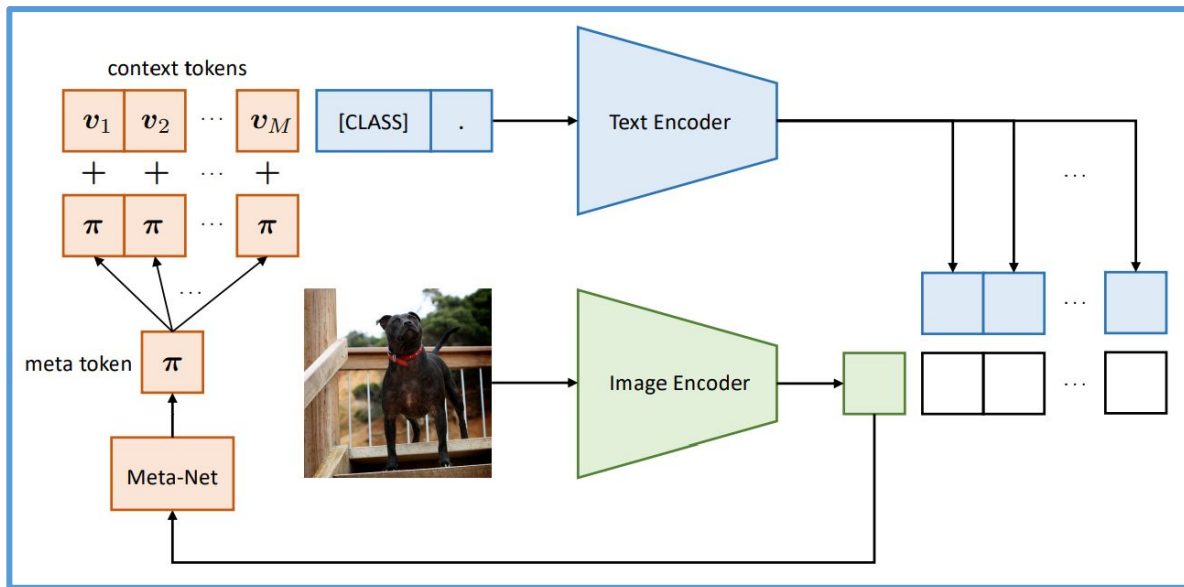
Text classification for different text dataset, with prompt-base finetuning

	<b>SST-2</b> (acc)	<b>SST-5</b> (acc)	<b>MR</b> (acc)	<b>CR</b> (acc)	<b>MPQA</b> (acc)	<b>Subj</b> (acc)	<b>TREC</b> (acc)	<b>CoLA</b> (Matt.)
Prompt-based zero-shot	83.6	35.0	80.8	79.5	67.6	51.4	32.0	2.0
Multitask FT zero-shot	<b>92.9</b>	37.2	86.5	88.8	73.9	55.3	36.8	-0.065
Prompt-based FT <sup>†</sup>	92.7 (0.9)	47.4 (2.5)	87.0 (1.2)	90.3 (1.0)	84.7 (2.2)	<b>91.2</b> (1.1)	84.8 (5.1)	<b>9.3</b> (7.3)
Multitask Prompt-based FT	92.0 (1.2)	<b>48.5</b> (1.2)	86.9 (2.2)	90.5 (1.3)	<b>86.0</b> (1.6)	89.9 (2.9)	83.6 (4.4)	5.1 (3.8)
+ task selection	92.6 (0.5)	47.1 (2.3)	<b>87.2</b> (1.6)	<b>91.6</b> (0.9)	85.2 (1.0)	90.7 (1.6)	<b>87.6</b> (3.5)	3.8 (3.2)
	<b>MNLI</b> (acc)	<b>MNLI-mm</b> (acc)	<b>SNLI</b> (acc)	<b>QNLI</b> (acc)	<b>RTE</b> (acc)	<b>MRPC</b> (F1)	<b>QQP</b> (F1)	
Prompt-based zero-shot	50.8	51.7	49.5	50.8	51.3	61.9	49.7	
Multitask FT zero-shot	63.2	65.7	61.8	65.8	74.0	81.6	63.4	
Prompt-based FT <sup>†</sup>	68.3 (2.3)	70.5 (1.9)	77.2 (3.7)	64.5 (4.2)	69.1 (3.6)	74.5 (5.3)	65.5 (5.3)	
Multitask Prompt-based FT	70.9 (1.5)	73.4 (1.4)	<b>78.7</b> (2.0)	71.7 (2.2)	<b>74.0</b> (2.5)	<b>79.5</b> (4.8)	67.9 (1.6)	
+ task selection	<b>73.5</b> (1.6)	<b>75.8</b> (1.5)	77.4 (1.6)	<b>72.0</b> (1.6)	70.0 (1.6)	76.0 (6.8)	<b>69.8</b> (1.7)	

Our main results using RoBERTa-large. †: Result in (GFC20);

# Experiments: zero-shot vision language task

## Conditional context optimization for CLIP model



CoCoOp

Figures from: *Conditional Prompt Learning for Vision-Language Models, 2022.*

# Experiments: zero-shot vision language task

160(all)-way zero-shot accuracy (%) on *tiered-ImageNet* test split

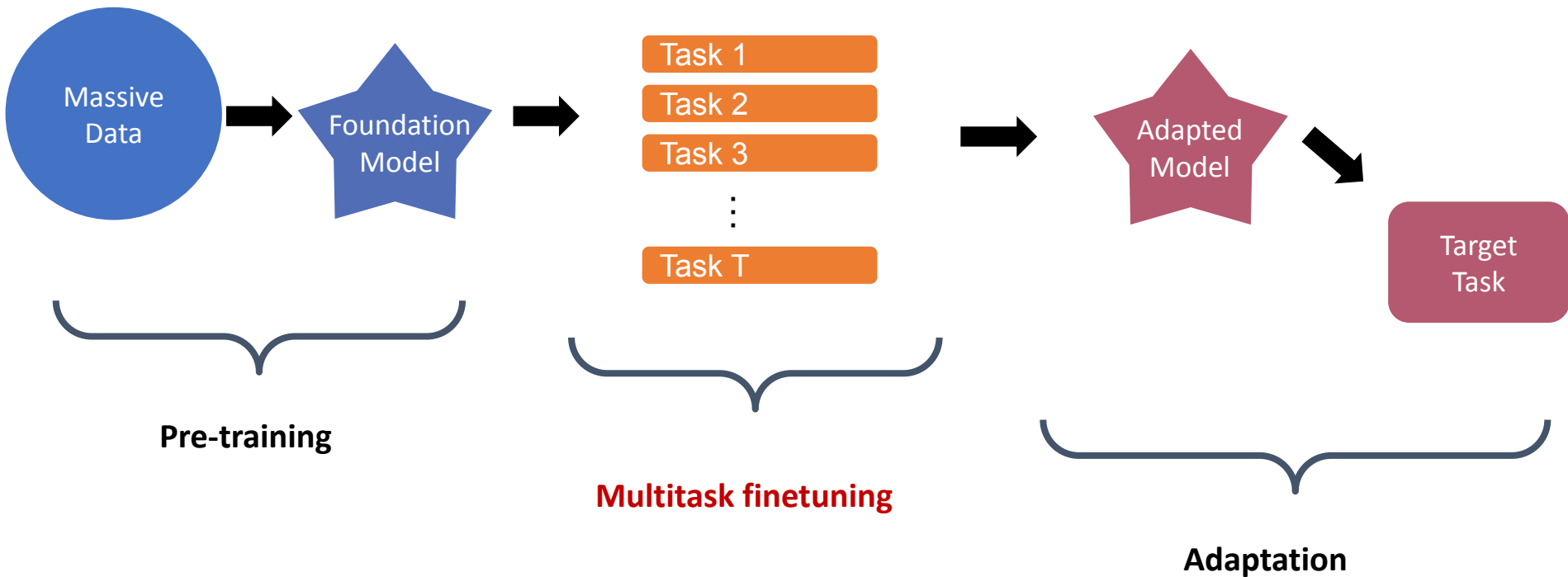
<b>Backbone</b>	<b>Zero-shot</b>	<b>Multitask finetune</b>
<b>ViT-B32</b>	69.9	71.4

Effects of multitask finetuning

# Future Work

- Theoretically: How would we quantify the relationship of data between multitask and target task? Concrete and well-motivated problem instances satisfying the task diversity assumptions for instantiating the error guarantee.
- Empirically: Does task diversity provide any insights on data selection in multitask finetuning? Can we design better strategies for constructing and choosing finetuning task?

# Take Home Message



**Thanks!**

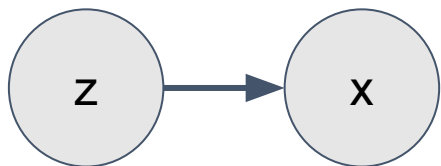
# Appendix

# Problem Setup - Contrastive pre-training

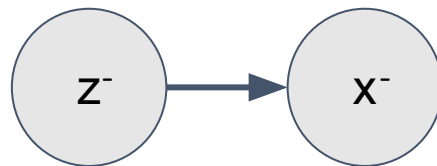
- $(z, z^-) \sim \eta^2, x, x^+ \sim \mathcal{D}(z), x^- \sim \mathcal{D}(z^-)$

- Contrastive loss:

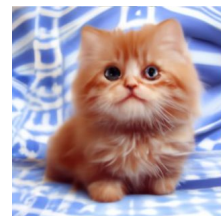
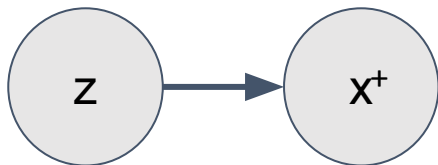
$$\mathbb{E} \left[ -\log \left( \frac{e^{\phi(x)^\top \phi(x^+)}}{e^{\phi(x)^\top \phi(x^+)} + e^{\phi(x)^\top \phi(x^-)}} \right) \right]$$



positive pair



negative pair



Data Model



# Main Result

- Suppose target task is  $\mathcal{T}_0$
- We want to bound  $\mathcal{L}_{sup}(\mathcal{T}_0, \phi)$
- let  $\zeta$  denote the conditional distribution of  $(z_1, z_2) \sim \eta^2$  conditioned on  $z_1 \neq z_2$

## Definition 1 (Averaged representation difference)

$$\bar{d}_\zeta(\phi, \tilde{\phi}) := \mathbb{E}_{\mathcal{T} \sim \zeta} \left[ \mathcal{L}_{sup}(\mathcal{T}, \phi) - \mathcal{L}_{sup}(\mathcal{T}, \tilde{\phi}) \right] = \mathcal{L}_{sup}(\phi) - \mathcal{L}_{sup}(\tilde{\phi})$$

## Definition 2 (worst-case representation difference)

$$d_{\mathcal{C}_0}(\phi, \tilde{\phi}) := \sup_{\mathcal{T}_0 \subseteq \mathcal{C}_0} \left[ \mathcal{L}_{sup}(\mathcal{T}_0, \phi) - \mathcal{L}_{sup}(\mathcal{T}_0, \tilde{\phi}) \right]$$

$(\nu, \epsilon)$ -diversity: For any  $\phi, \tilde{\phi} \in \Phi$ ,  $d_{\mathcal{C}_0}(\phi, \tilde{\phi}) \leq \bar{d}_\zeta(\phi, \tilde{\phi})/\nu + \epsilon$

# Main Result

- Suppose target task is  $\mathcal{T}_0$
- let  $\zeta$  denote the conditional distribution of  $(z_1, z_2) \sim \eta^2$  conditioned on  $z_1 \neq z_2$
- $(\nu, \epsilon)$ -diversity: For any  $\phi, \tilde{\phi} \in \Phi$ ,  $d_{\mathcal{C}_0}(\phi, \tilde{\phi}) \leq \bar{d}_{\zeta}(\phi, \tilde{\phi})/\nu + \epsilon$
- Suppose there is  $\phi^*$  such that supervised loss are small across all tasks

## Theorem 1 (Contrastive pre-training loss(baseline))

Suppose in pre-training we have  $\hat{\mathcal{L}}_{un}(\hat{\phi}) \leq \epsilon_0$ , then:

$$\mathcal{L}_{sup}(\mathcal{T}_0, \hat{\phi}) - \mathcal{L}_{sup}(\mathcal{T}_0, \phi^*) \leq \frac{1}{\nu} \left[ \frac{1}{1 - \tau} (2\epsilon_0 - \tau) - \mathcal{L}_{sup}(\phi^*) \right] + \epsilon.$$

# Main Result

- Suppose target task is  $\mathcal{T}_0$
- let  $\zeta$  denote the conditional distribution of  $(z_1, z_2) \sim \eta^2$  conditioned on  $z_1 \neq z_2$
- $(\nu, \epsilon)$ -diversity: For any  $\phi, \tilde{\phi} \in \Phi$ ,  $d_{\mathcal{L}_0}(\phi, \tilde{\phi}) \leq \bar{d}_{\zeta}(\phi, \tilde{\phi})/\nu + \epsilon$

## Theorem 2 (Multitask finetuning loss(Ours))

Suppose we solve multitask finetuning optimization with empirical loss smaller than  $\epsilon_1 = \frac{\alpha}{3} \frac{1}{1-\tau} (2\epsilon_0 - \tau)$  and got  $\phi'$ . If:

$$M \geq \Omega \left( \frac{1}{\epsilon_1} \left[ \mathcal{R}_M(\Phi(\epsilon_0)) + \frac{1}{\epsilon_1} \log \left( \frac{1}{\delta} \right) \right] \right), \quad Mm \geq \Omega \left( \frac{1}{\epsilon_1} \left[ \mathcal{R}_{Mm}(\Phi(\epsilon_0)) + \frac{1}{\epsilon_1} \log \left( \frac{1}{\delta} \right) \right] \right)$$

Then with prob  $1 - \delta$ ,

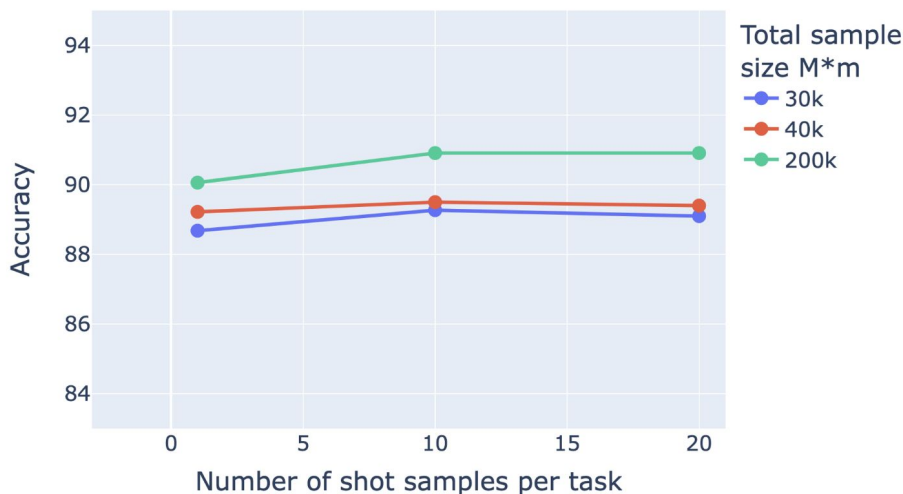
$$\mathcal{L}_{sup}(\mathcal{T}_0, \phi') - \mathcal{L}_{sup}(\mathcal{T}_0, \phi^*) \leq \frac{1}{\nu} \left[ \alpha \frac{1}{1-\tau} (2\epsilon_0 - \tau) - \mathcal{L}_{sup}(\phi^*) \right] + \epsilon$$

# Remark

- Comparing to pre-training + adaptation(baseline), our multitask finetuning reduce error on target task by  $\frac{1}{\nu} \left[ (1 - \alpha) \frac{1}{1 - \tau} (2\epsilon_0 - \tau) \right]$   
where finetuning sample complexity is  $\Theta \left( \frac{1}{\alpha\epsilon_0} \right)$
- Comparing to traditional supervised learning, self-supervised pre-training reduce error by  $O \left( \frac{1}{M_m} [\mathcal{R}_{M_m}(\Phi) - \mathcal{R}_{M_m}(\Phi(\epsilon_0))] \right)$

# Experiments: Few-shot Vision tasks

5-way accuracy (%) on *mini-ImageNet*, 1/10/20 image per class in target task



ViT-B32

Accuracy with varying number shot images