

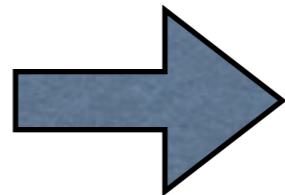
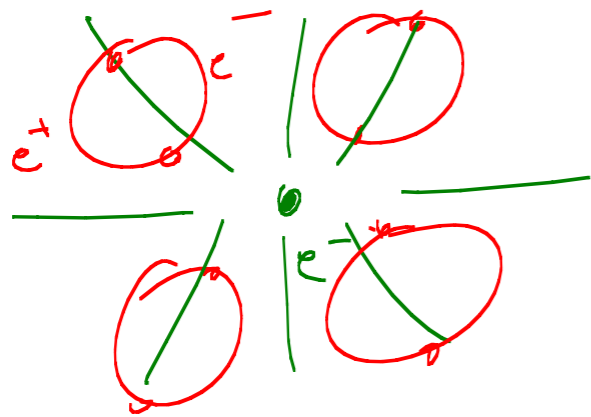
The background of the slide is a complex, light gray pattern of particle tracks and spirals, resembling a particle detector's output or a theoretical model of particle interactions. The tracks are composed of various line styles, including solid, dashed, and dotted lines, some of which form tight spirals or loops. The overall appearance is that of a technical or scientific illustration.

# BSM 3/3

Andreas Weiler  
CERN & DESY

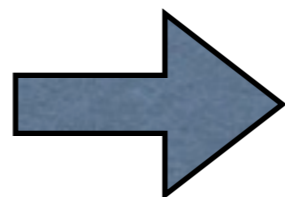
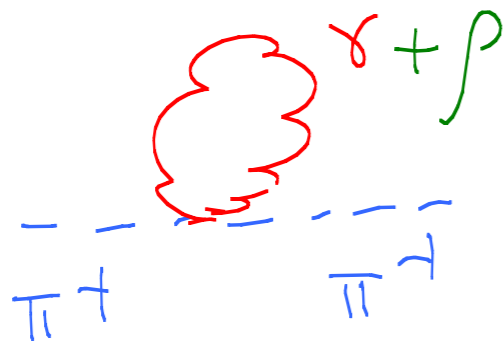
[andreas.weiler@cern.ch](mailto:andreas.weiler@cern.ch)

2



Supersymmetry  
(new space-time  
symmetry)

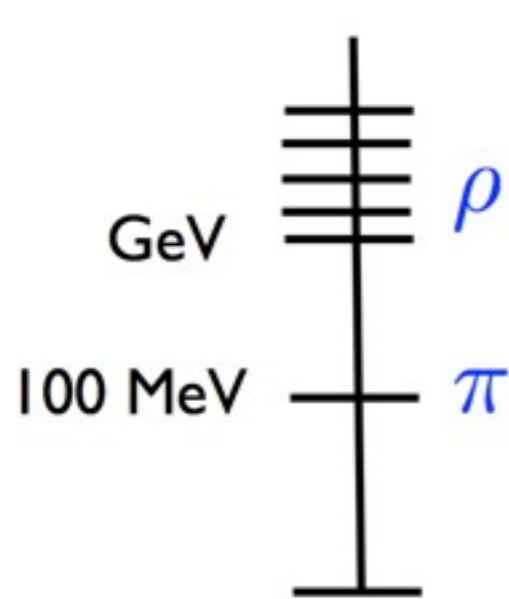
3



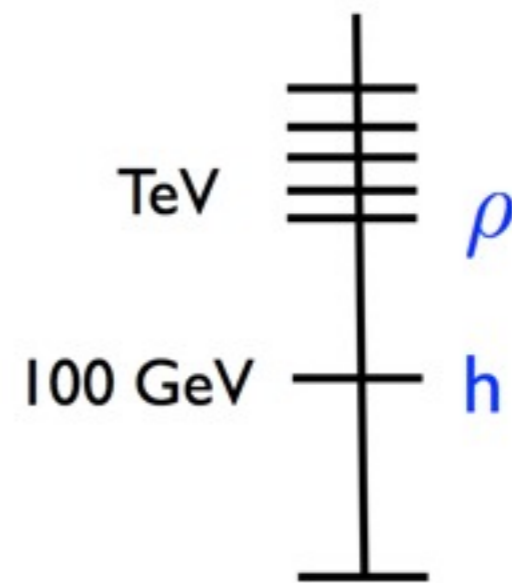
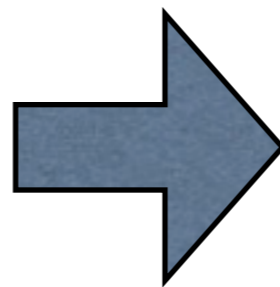
Composite Higgs



# Strong EWSB (Composite Higgs)



QCD



Higgs as a pGB

# Why is the Higgs light?

Kaplan; Agashe et. al

Inspired by QCD: (pseudo) scalar pion is the lightest state


Shift symmetry...

$$\pi \rightarrow \pi + c$$

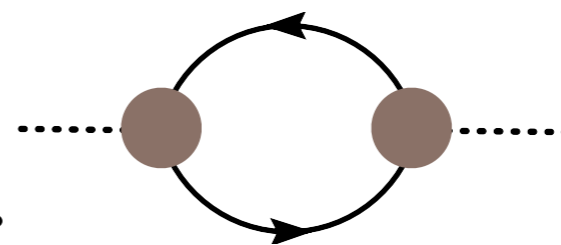
... protects its mass.

Interactions are perturbative for  $E \ll 4\pi f$

No pure composite effects due to Goldstone symmetry


$$= 0$$

Shift symmetry broken by elementary-composite couplings:



$$m_h^2 \sim \frac{\lambda^2}{16\pi^2} \Lambda_{comp}^2$$

$$\lambda \ll 4\pi$$

Supersymmetry is a **weakly coupled** solution to the hierarchy problem. We can extrapolate physics to the Planck scale, complete the MSSM in a GUT.

There is another way and it's already in use. Nature already employs a **strongly coupled** mechanism to explain why

$$\Lambda_{\text{QCD}} \ll M_{\text{Planck}}$$
$$\sim 1 \text{ GeV} \quad 10^{19} \text{ GeV}$$

# QCD



David J. Gross



H. David Politzer



Frank Wilczek

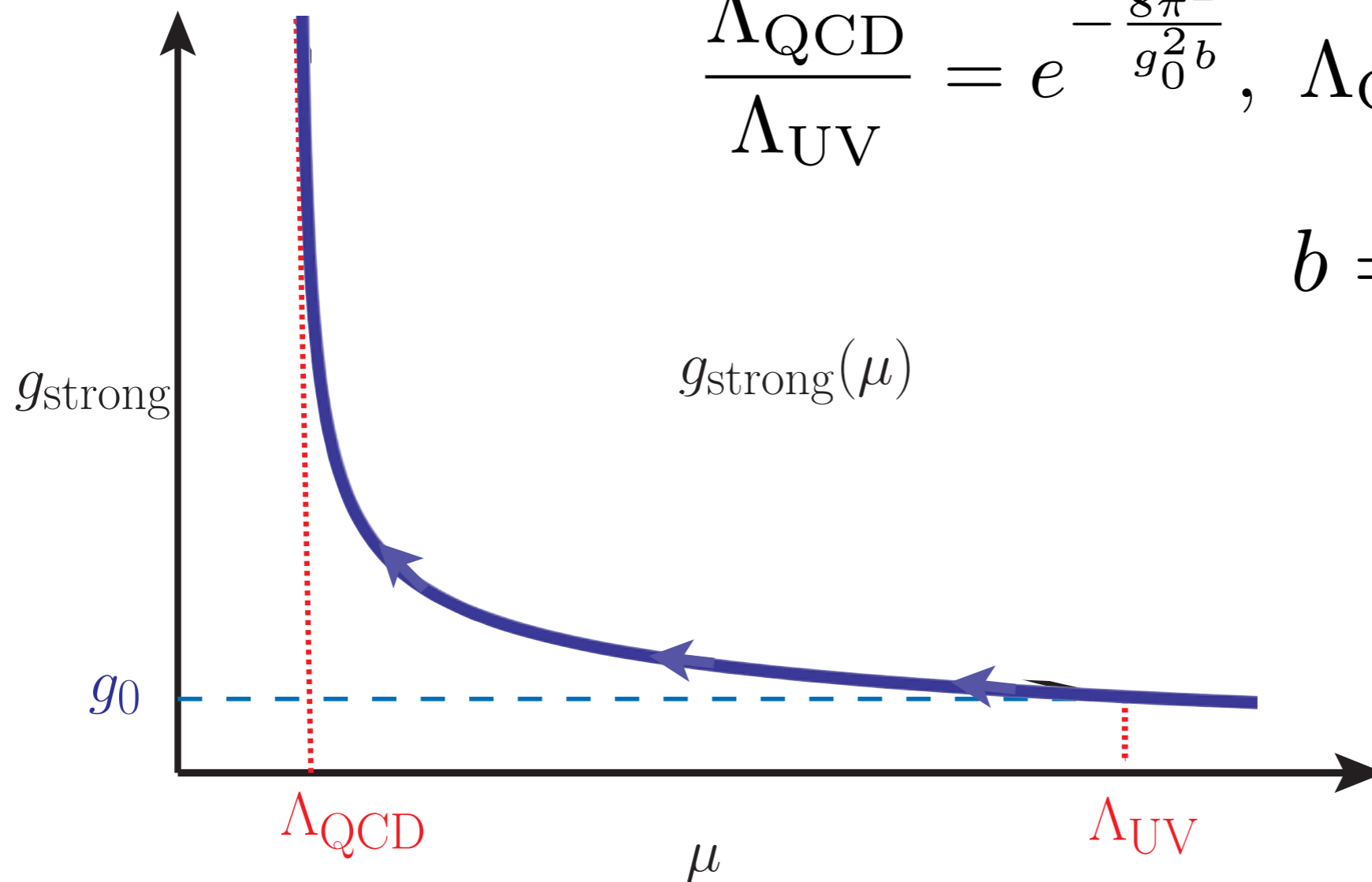
Fix QCD coupling at some high scale

→ exponential hierarchy generated dynamically



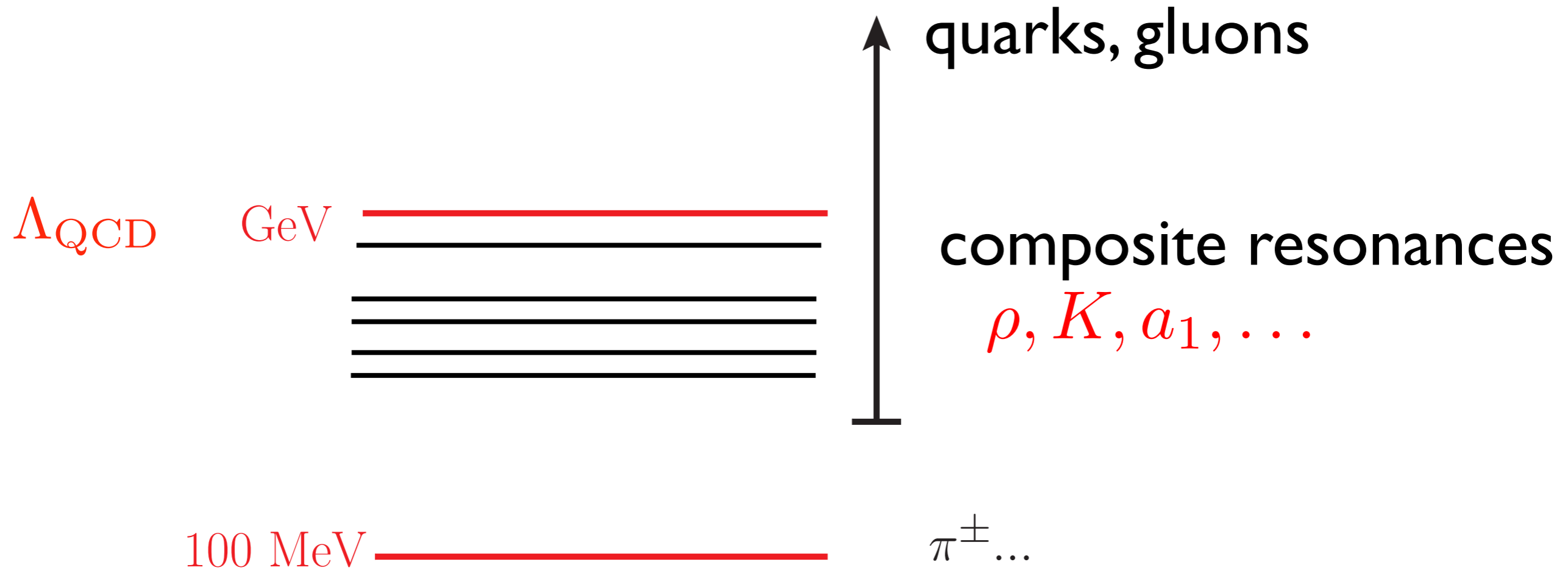
$$\frac{\Lambda_{\text{QCD}}}{\Lambda_{\text{UV}}} = e^{-\frac{8\pi^2}{g_0^2 b}}, \quad \Lambda_{\text{QCD}} \leq \text{GeV}$$

$$b = 7$$



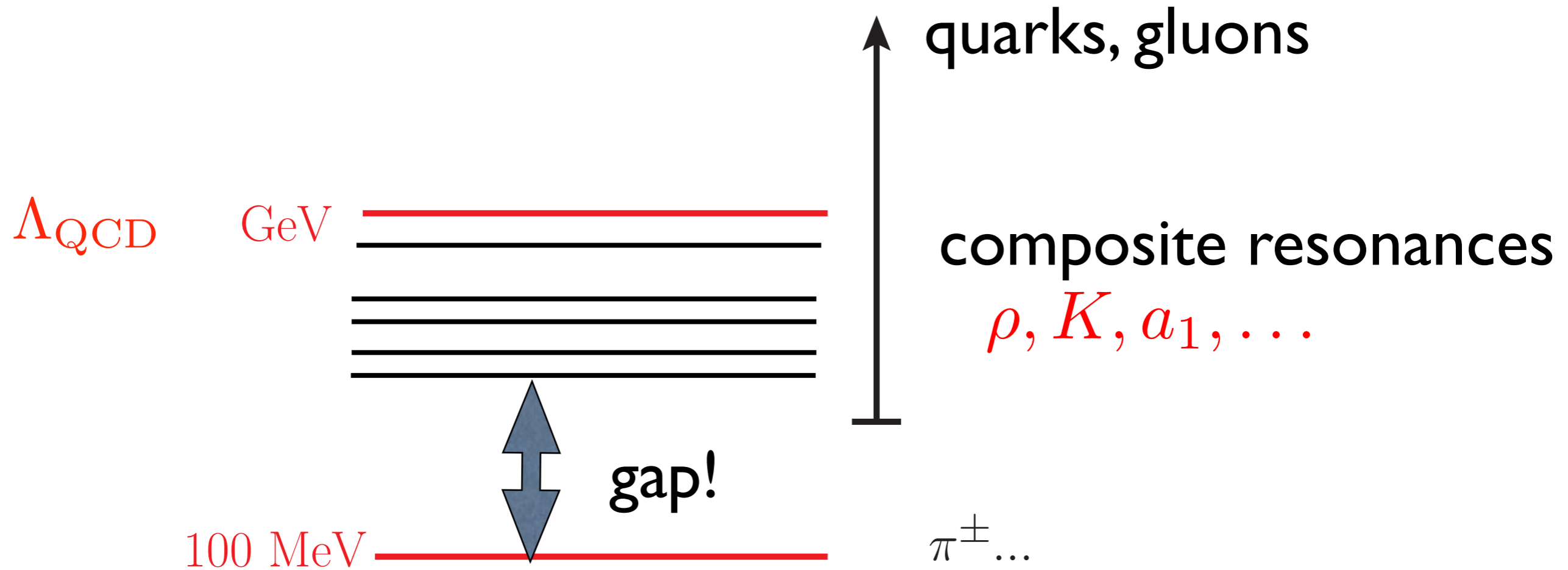
Asymptotic  
freedom

# QCD: composite bound states



At strong coupling, new resonances are generated

# QCD: composite bound states



At strong coupling, new resonances are generated

# QCD vs. EWSB

QCD dynamically breaks SM gauge symmetry

$$SU(2)_L \times SU(2)_R \rightarrow SU(2)_V$$

$$\langle \bar{q}_L q_R \rangle \simeq \Lambda_{\text{QCD}}^3 \sim (\text{GeV})^3$$

# QCD vs. EWSB

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$$\langle \bar{q}_L q_R \rangle \simeq \Lambda_{\text{QCD}}^3 \sim (\text{GeV})^3$$

The QCD masses of W/Z are small

$$m_{W,Z} \sim \frac{g}{4\pi} \Lambda_{\text{QCD}} \sim 100 \text{ MeV}$$

Longitudinal components of W & Z have tiny admixture of pions...



# Technicolor

Scaled up version of QCD mechanism

$$\langle \bar{q}'_L q'_R \rangle \sim \Lambda_{\text{TC}}^3, \quad \Lambda_{\text{TC}} \sim \text{TeV}$$

Technicolor, doesn't have a Higgs ...

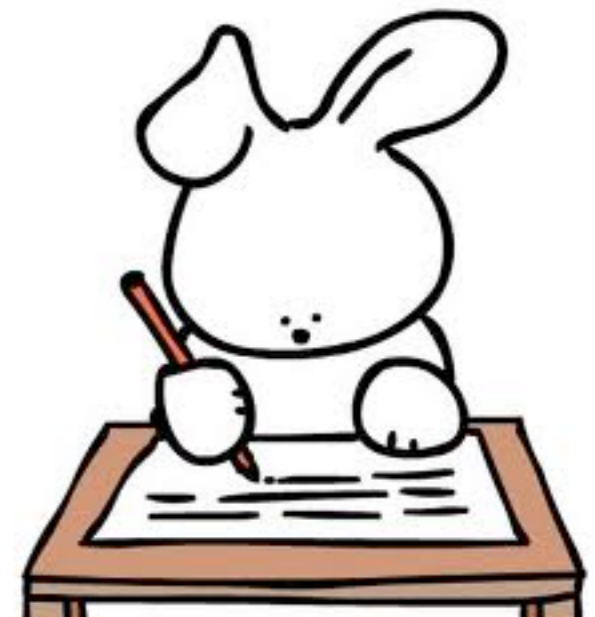


\* the Higgs as the dilaton  
as the last bastion ...

# Composite Higgs

- Want to copy QCD, but extend pion sector (QCD:  $\pi^0, \pi^\pm$ )
- Higgs as a (pseudo) Goldstone boson

Need to learn about  
goldstone bosons...



# Quantum Protection

Symmetries can soften quantum behaviour

$$\mathcal{L} = |\partial_\mu \phi|^2 + \mu^2 |\phi|^2 - \lambda |\phi|^4 + \dots$$

breaks susy  $\rightarrow$  corrections must be  
proportional to susy breaking

# Shift symmetry

Higgs mass term can be forbidden

$$\mathcal{L} = |\partial_\mu \phi|^2 + \mu^2 |\phi|^2 - \lambda |\phi|^4 + \dots$$

$$\phi \rightarrow e^{i\alpha} \phi$$

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$$\phi \rightarrow \phi + \alpha$$

works!

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$$\phi \rightarrow \phi + \alpha$$

works!

Can we make the Higgs transform this way?



# Spontaneous breaking of U(1)

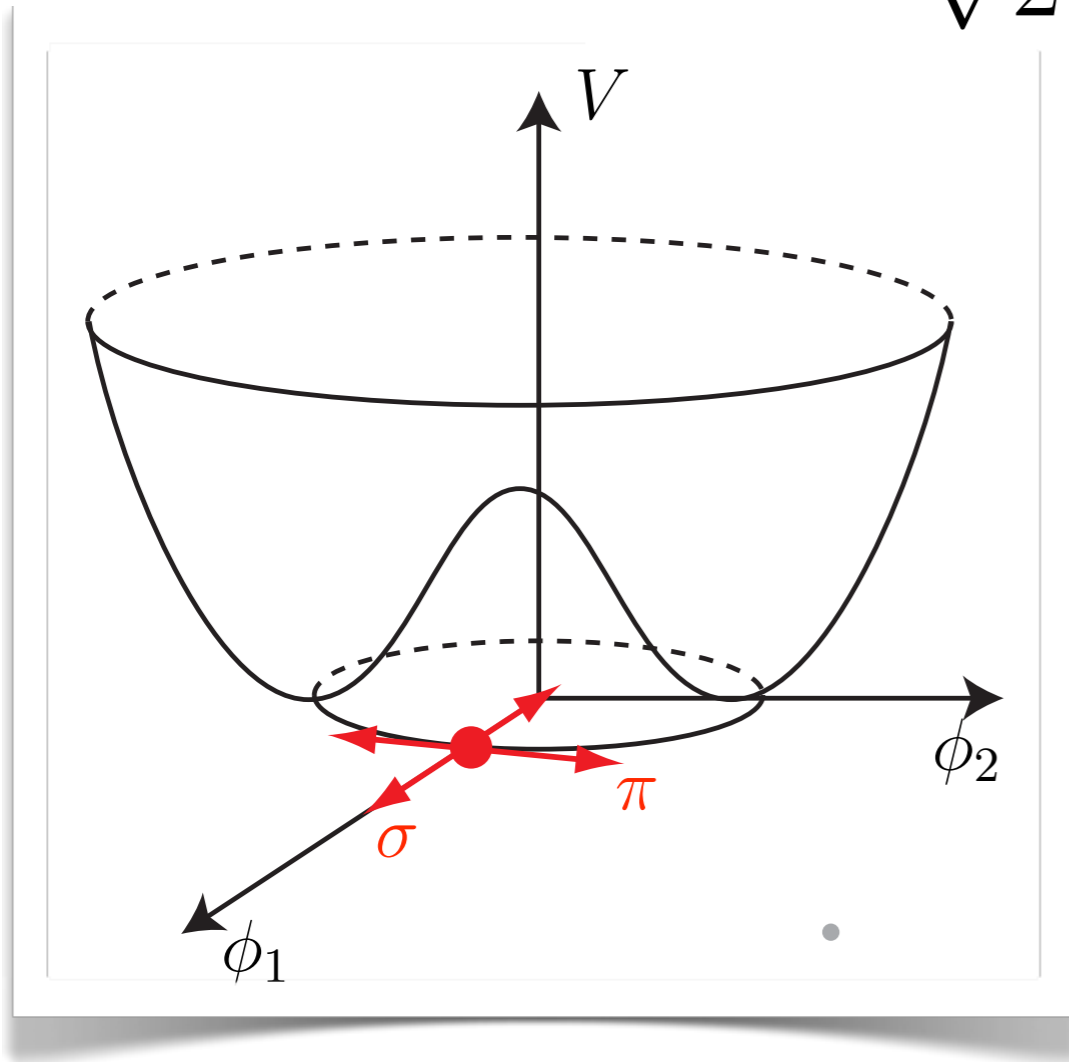
$$\langle \Phi \rangle = \frac{f}{\sqrt{2}}$$

Instead describing this with

$$\phi = \phi_1 + i\phi_2$$

redefine field to

$$\phi(x) = \frac{1}{2} e^{i\pi(x)/f} (f + \sigma(x))$$



$$\mathcal{L} = |\partial_\mu \phi|^2 + \mu^2 |\phi|^2 - \lambda |\phi|^4 + \dots$$

$$\mathcal{L} = |\partial_\mu \phi|^2 + \mu^2 |\phi|^2 - \lambda |\phi|^4 + \dots$$

**use**  $\phi(x) = \frac{1}{2} e^{i\pi(x)/f} (f + \sigma(x))$

$$\mathcal{L} = |\partial_\mu \phi|^2 + \mu^2 |\phi|^2 - \lambda |\phi|^4 + \dots$$

use  $\phi(x) = \frac{1}{2} e^{i\pi(x)/f} (f + \sigma(x))$

$$\partial^\mu \phi^\dagger \partial_\mu \phi = \frac{1}{2} \partial^\mu \sigma \partial_\mu \sigma + \frac{1}{2} (1 + \sigma/f)^2 \frac{1}{2} \partial^\mu \pi \partial_\mu \pi$$

$$\mathcal{L} = |\partial_\mu \phi|^2 + \mu^2 |\phi|^2 - \lambda |\phi|^4 + \dots \quad V(|\phi(x)|^2)$$

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$$V(|\phi(x)|^2) = V(\sigma(x))$$

no dependence on  $\pi(x)$

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$$V(|\phi(x)|^2) = V(\sigma(x)) \quad \text{no mass term}$$

no dependence on  $\pi(x)$

$$\frac{1}{2} (1 + \sigma(x)/f)^2 \frac{1}{2} \partial^\mu \pi \partial_\mu \pi + \frac{1}{2} \partial^\mu \sigma \partial_\mu \sigma - V(\sigma(x))$$

Using this parameterization there's a new symmetry:

$$\pi(x) \rightarrow \pi(x) + \alpha$$

because

$$\partial_\mu (\pi(x) + \alpha) = \partial_\mu \pi(x)$$

$$\frac{1}{2} (1 + \sigma(x)/f)^2 \frac{1}{2} \partial^\mu \pi \partial_\mu \pi + \frac{1}{2} \partial^\mu \sigma \partial_\mu \sigma - V(\sigma(x))$$

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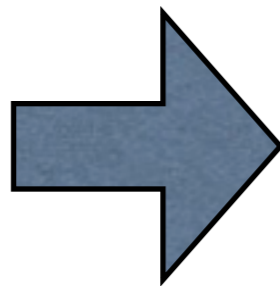
But what happened to the U(1) symmetry ?  
Fields are real...



But what happened to the U(1) symmetry ?

$$\phi \rightarrow e^{i\alpha} \phi$$

$$e^{i\pi(x)/f} (f + \sigma(x)) \rightarrow e^{i\alpha} e^{i\pi(x)/f} (f + \sigma(x))$$



$$\sigma(x) \rightarrow \sigma(x)$$

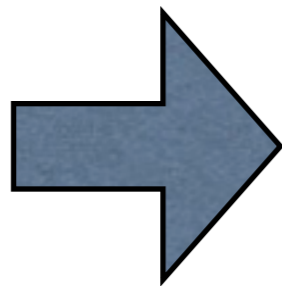
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Phase rotation becomes shift symmetry

But what happened to the U(1) symmetry ?

$$\phi \rightarrow e^{i\alpha} \phi$$

$$e^{i\pi(x)/f} (f + \sigma(x)) \rightarrow e^{i\alpha} e^{i\pi(x)/f} (f + \sigma(x))$$



$$\sigma(x) \rightarrow \sigma(x)$$

$$\pi(x) \rightarrow \pi(x) + \alpha$$

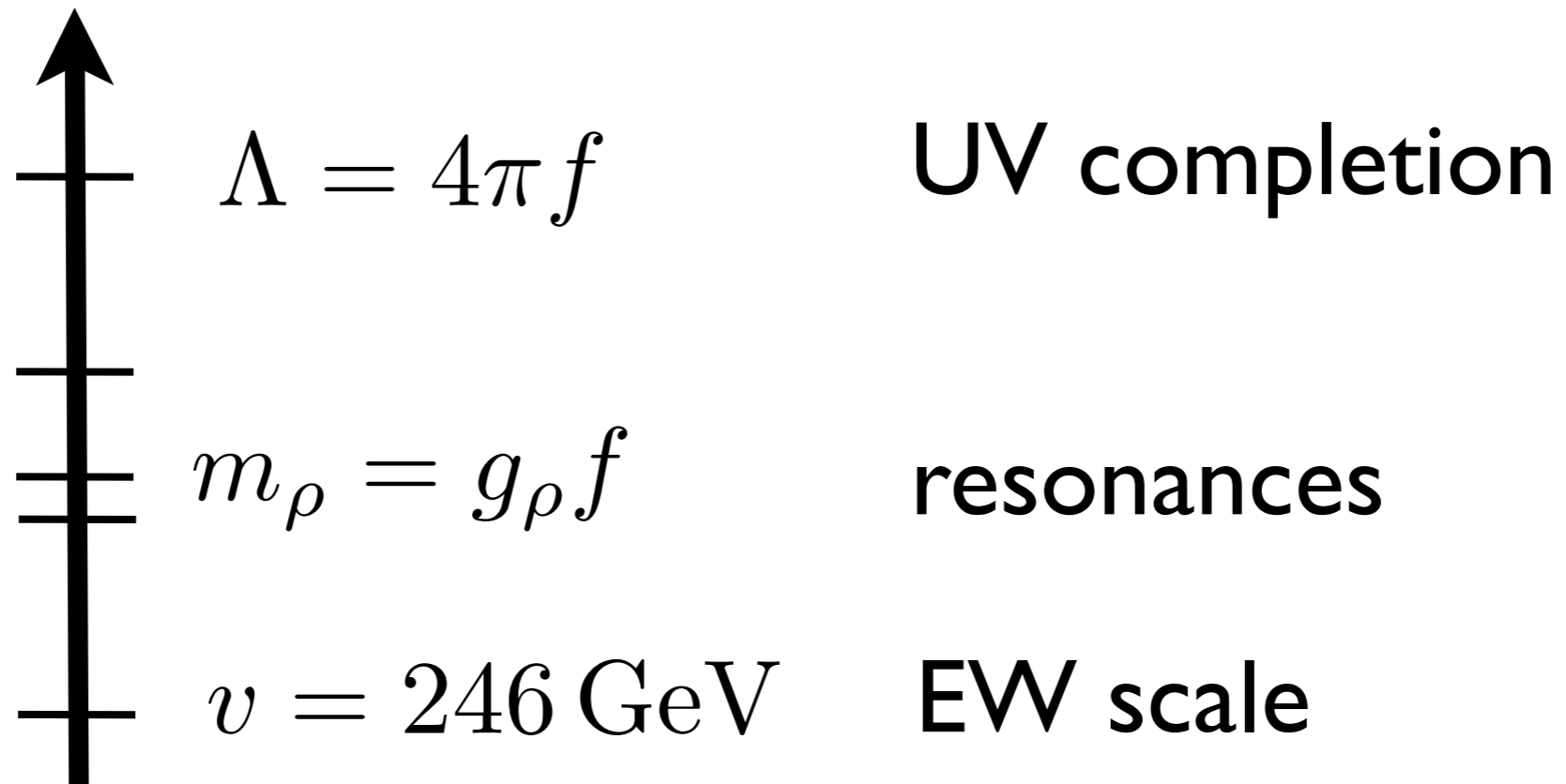
Phase rotation becomes shift symmetry

$\pi(x)$  is **massless** **but** also no

- gauge couplings
- potential
- yukawas

# Semi-realistic model





# pGB Higgs

$$SU(3) \rightarrow SU(2)$$

Break symmetry using

$$\langle \Phi \rangle = \begin{pmatrix} 0 \\ 0 \\ f \end{pmatrix}$$

# Goldstone bosons = # broken generators

$$\Phi = \frac{1}{\sqrt{2}} e^{i\Pi/f} \begin{pmatrix} 0 \\ 0 \\ f + \sigma \end{pmatrix} \quad \Pi = \frac{1}{\sqrt{2}} \begin{pmatrix} \eta/\sqrt{3} & 0 & H_1 \\ 0 & \eta/\sqrt{3} & H_2 \\ H_1^* & H_2^* & -2\eta/\sqrt{3} \end{pmatrix}$$

$$\Phi = \frac{1}{\sqrt{2}} e^{i\Pi/f} \begin{pmatrix} 0 \\ 0 \\ f + \sigma \end{pmatrix} \quad \Pi = \frac{1}{\sqrt{2}} \begin{pmatrix} \eta/\sqrt{3} & 0 & H_1 \\ 0 & \eta/\sqrt{3} & H_2 \\ H_1^* & H_2^* & -2\eta/\sqrt{3} \end{pmatrix}$$

**Expand**

$$\Phi(x) = \begin{pmatrix} H_1(x) \\ H_2(x) \\ -\frac{2}{\sqrt{2}}\eta(x) \end{pmatrix} + \dots$$

**Contains a Higgs:**  $H = \begin{pmatrix} H_1 \\ H_2 \end{pmatrix} = SU(2) \text{ doublet}$

$$SU(3) \rightarrow SU(2)$$

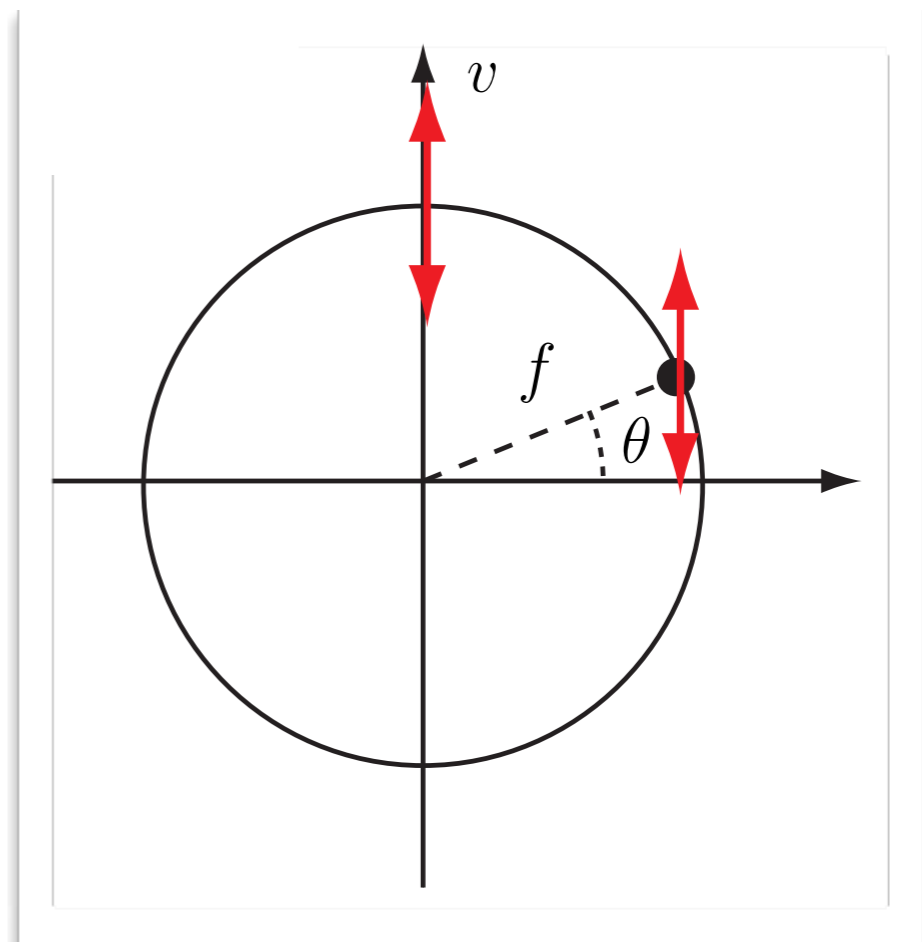
# pGB Higgs

Unbroken gauge symmetry in global  $SU(2)$ ,  
dynamics generates ‘**vacuum mis-alignment**’

$SU(2)_L$  vs.  $SU(2)$

$$\langle \Phi \rangle = \frac{f}{\sqrt{2}} \begin{pmatrix} 0 \\ \sin \theta \\ \cos \theta \end{pmatrix} \quad SU(2)_L$$

EW symmetry broken



# pGB Higgs

$$\langle \Phi \rangle = \frac{f}{\sqrt{2}} \begin{pmatrix} 0 \\ \sin \theta \\ \cos \theta \end{pmatrix} \text{SU}(2)_L$$

Electro-weak scale  $v = f \sin \theta$

$f \sim$  scale of new physics

$\sin \theta \ll 1 \Leftrightarrow f \gg v$  (SM limit)

$$\Rightarrow \langle H \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v \end{pmatrix}$$



# Collective Breaking

We now want to add a yukawa coupling to give mass to the top quark

$$\lambda_t \bar{Q}_i H_i^c t_R \quad i: \text{sum over SU}(2)$$

Fundamental field is a triplet

$$\phi = \exp \left\{ i \begin{pmatrix} h_1 \\ h_2 \\ h_1^* & h_2^* \end{pmatrix} \right\} \begin{pmatrix} \\ \\ f \end{pmatrix}$$

# Top yukawa: 1st try

$$\sum_i^2 \lambda_t \bar{\phi}_i H_i^c t_R \quad \text{works, gives mass to the top}$$

... but breaks **SU(3)** structure explicitly, does not respect Goldstone symmetry protecting the Higgs mass:

# Top yukawa: 1st try

<sup>2</sup>  
 $\sum_i \lambda_t \bar{\phi}_i H_i^c t_R$  works, gives mass to the top

... but breaks **SU(3)** structure explicitly, does not respect Goldstone symmetry protecting the Higgs mass:

$$\sim \frac{\lambda_t^2}{16\pi^2} \Lambda_{UV}^2$$

we've accomplished nothing...

# Collective breaking

Example:  $SU(3) \rightarrow SU(2)$  (ignore  $U(1)_Y$  again)

$$\langle \Phi_1 \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ 0 \\ f_1 \end{pmatrix} \quad \langle \Phi_2 \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ 0 \\ 2 \end{pmatrix}$$

Gauge full  $SU(3) \Rightarrow$  exact symmetry

$$\Psi_L = \begin{pmatrix} t_L \\ b_L \\ T_L \end{pmatrix} \quad t_{1R}, t_{2R}, b_R$$

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$$\mathcal{L}_{\text{Yukawa}} = y_1 \bar{\Psi}_L \Phi_1 t_{1R} + y_2 \bar{\Psi}_L \Phi_2 t_{2R}$$

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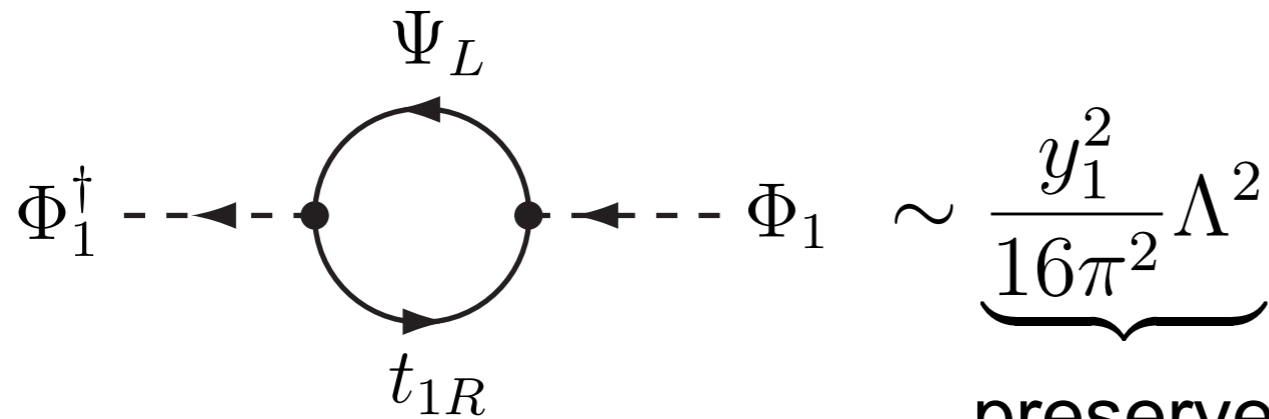
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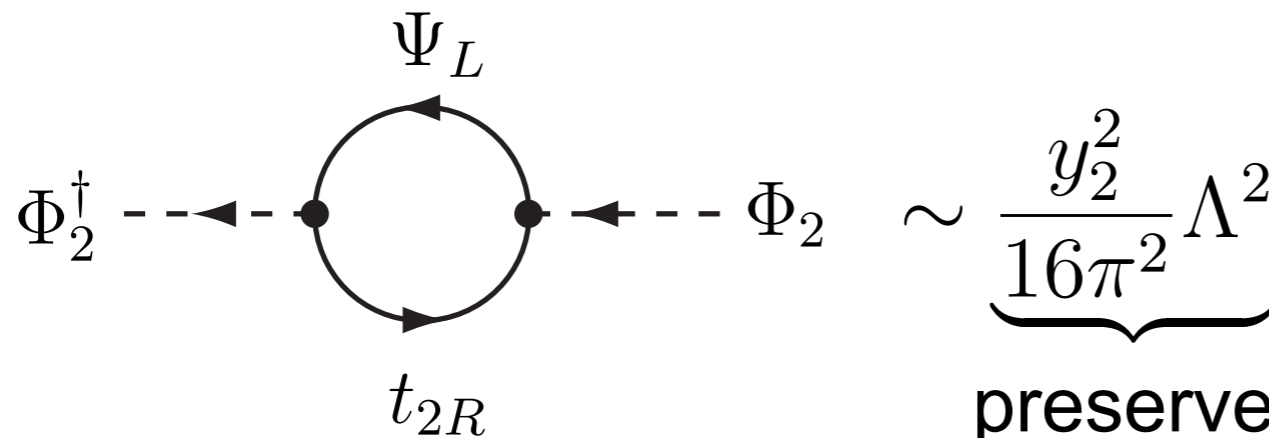
$y_1 \rightarrow 0 \Rightarrow$  exact  $SU(3)_2 \rightarrow SU(2)_2$  and vice versa

Both  $y_1, y_2 \neq 0$  required for non-derivative couplings  
of PNGB Higgs



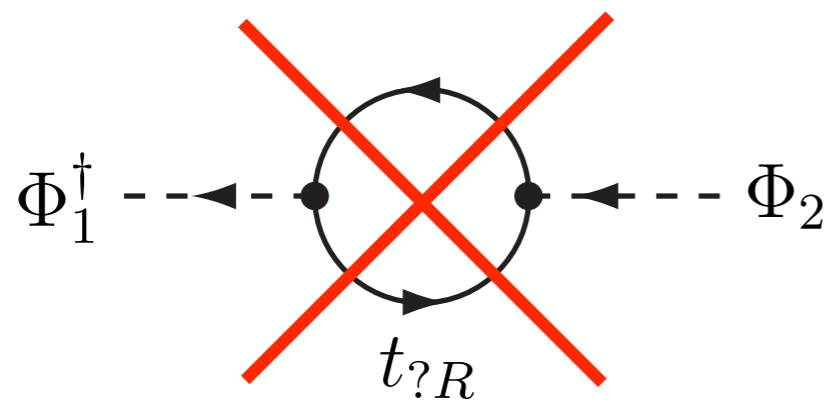
$$\sim \underbrace{\frac{y_1^2}{16\pi^2}} \Lambda^2$$

preserves  $SU(3)_2 \rightarrow SU(2)_2$   
 $\Rightarrow$  no PNGB Higgs mass



$$\sim \underbrace{\frac{y_2^2}{16\pi^2}} \Lambda^2$$

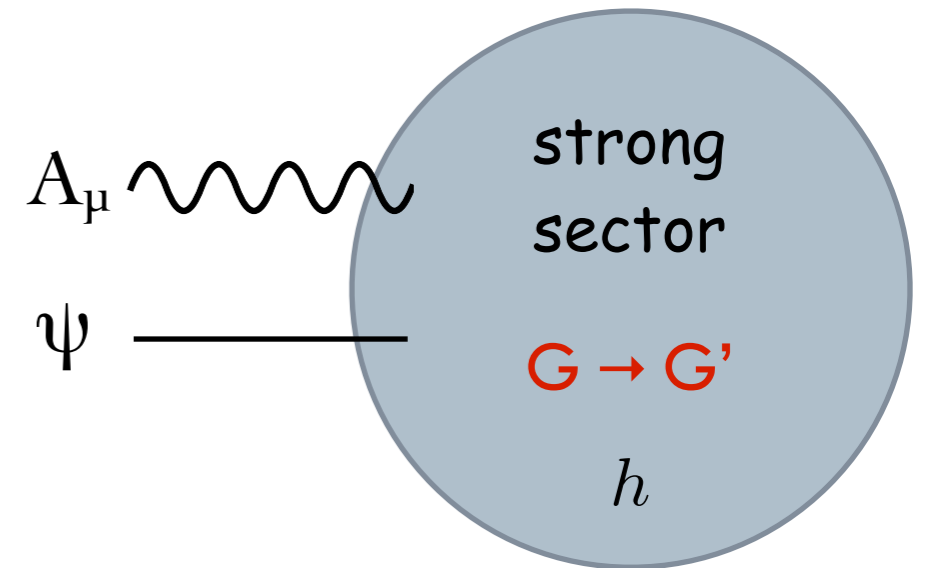
preserves  $SU(3)_1 \rightarrow SU(2)_1$   
 $\Rightarrow$  no PNGB Higgs mass



Not allowed

# Minimal composite Higgs

Agashe et. al

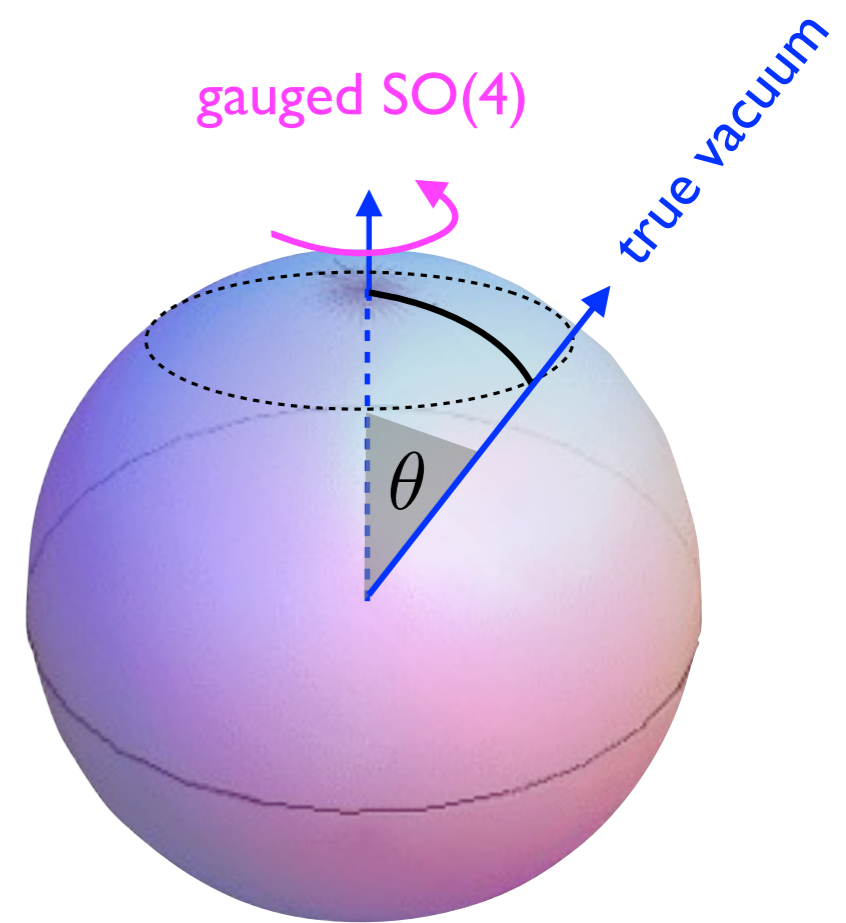


Minimal bottom up construction

$$SO(5) \rightarrow SO(4) \sim SU(2)_L \times SU(2)_R$$



# $SO(5)/SO(4)$



Tree level: gauge  $SO(4)$  aligned

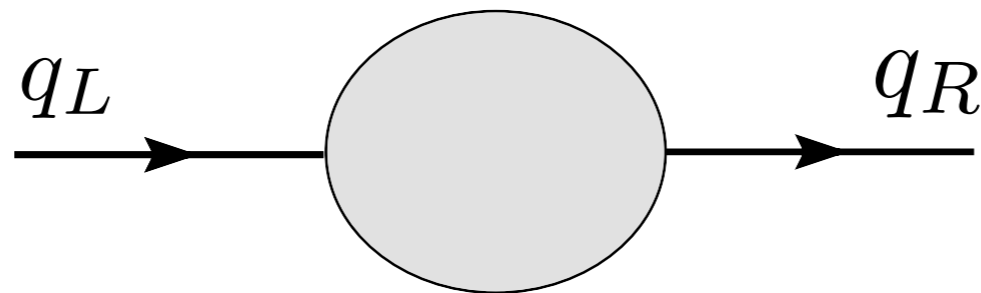
Higgs

$$\phi = e^{i\pi \hat{a} T^{\hat{a}} / f} \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 1 \end{pmatrix} = \begin{pmatrix} \sin(\pi/f) \times \begin{pmatrix} \hat{\pi}^1 \\ \hat{\pi}^2 \\ \hat{\pi}^3 \\ \hat{\pi}^4 \end{pmatrix} \\ \cos(\pi/f) \end{pmatrix} \stackrel{\text{I-loop } \langle \phi(x) \rangle = \theta \cdot f}{=} \begin{pmatrix} \sin(\theta + h(x)/f) e^{i\chi^i(x) A^i / v} \begin{pmatrix} 0 \\ 0 \\ 0 \\ 1 \end{pmatrix} \\ \cos(\theta + h(x)/f) \end{pmatrix}$$

eaten by  $W_L, Z_L$

# Linear couplings

$$\mathcal{L} = \lambda_L \bar{q}_L O_R + \lambda_R \bar{u}_R O_L + h.c.$$



$$m_q \sim \frac{\lambda_L(\mu)\lambda_R(\mu)}{g_*} v$$

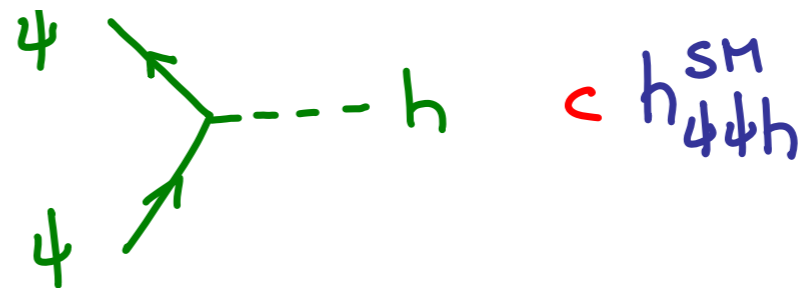
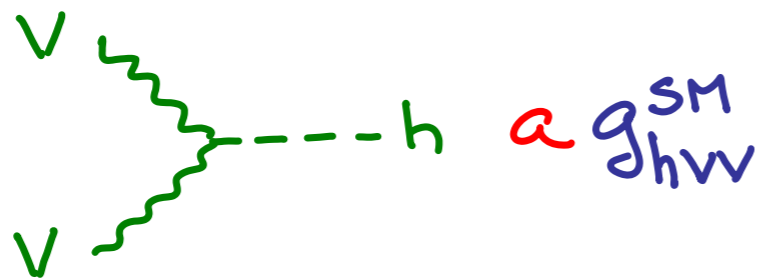
Interesting  
consequences  
for flavor..

# Deviations from SM Higgs

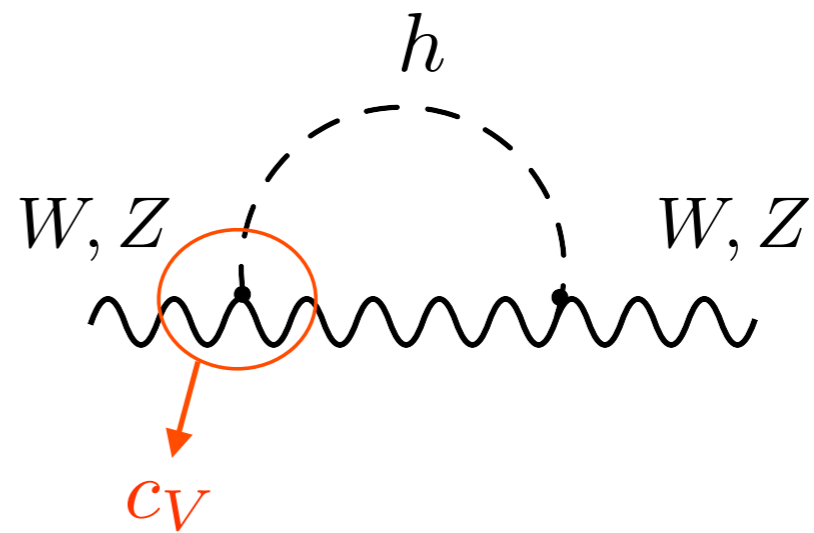
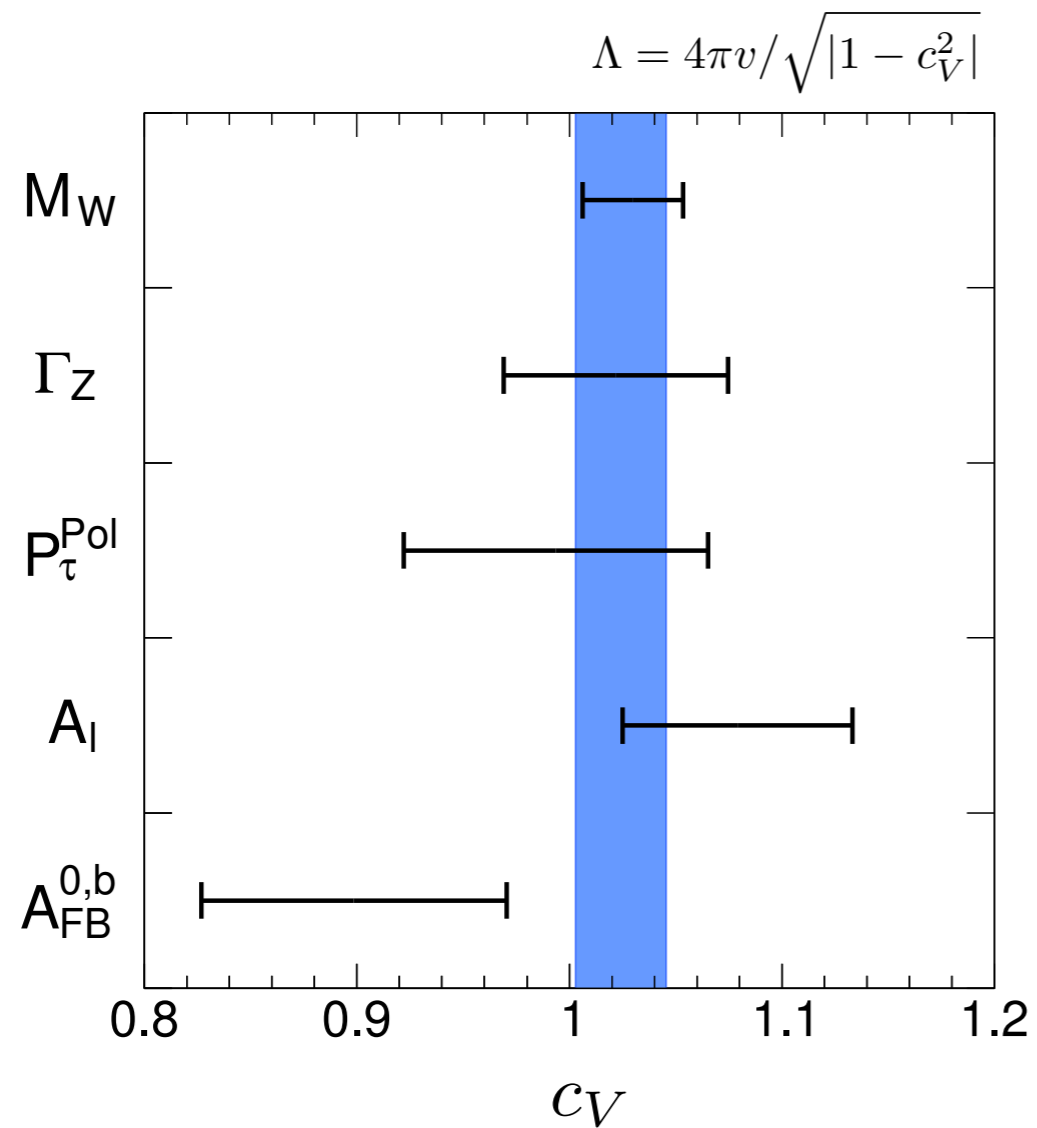
## Goldstone boson nature

$$f^2 \left| \partial_\mu e^{i\pi/f} \right|^2 = |D_\mu H|^2 + \frac{c_H}{2f^2} [\partial_\mu (H^\dagger H)]^2 + \frac{c'_H}{2f^4} (H^\dagger H) [\partial_\mu (H^\dagger H)]^2 + \dots$$

Giudice et al. JHEP 0706 (2007) 045

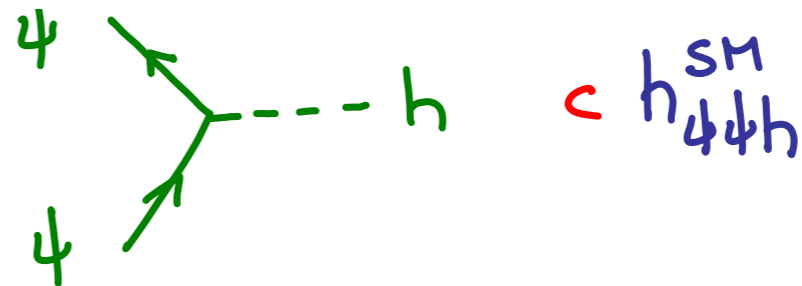
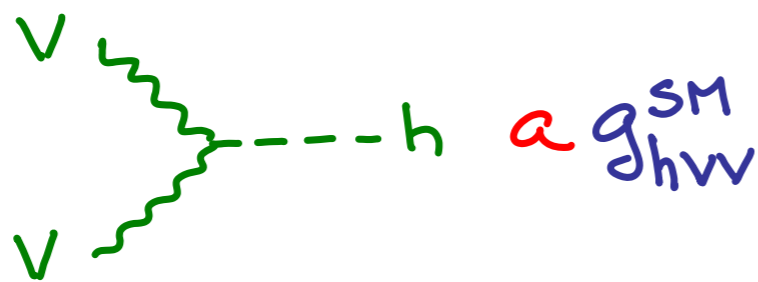


# EW precision tests



# Higgs couplings

Have been measured to 20-30% precision



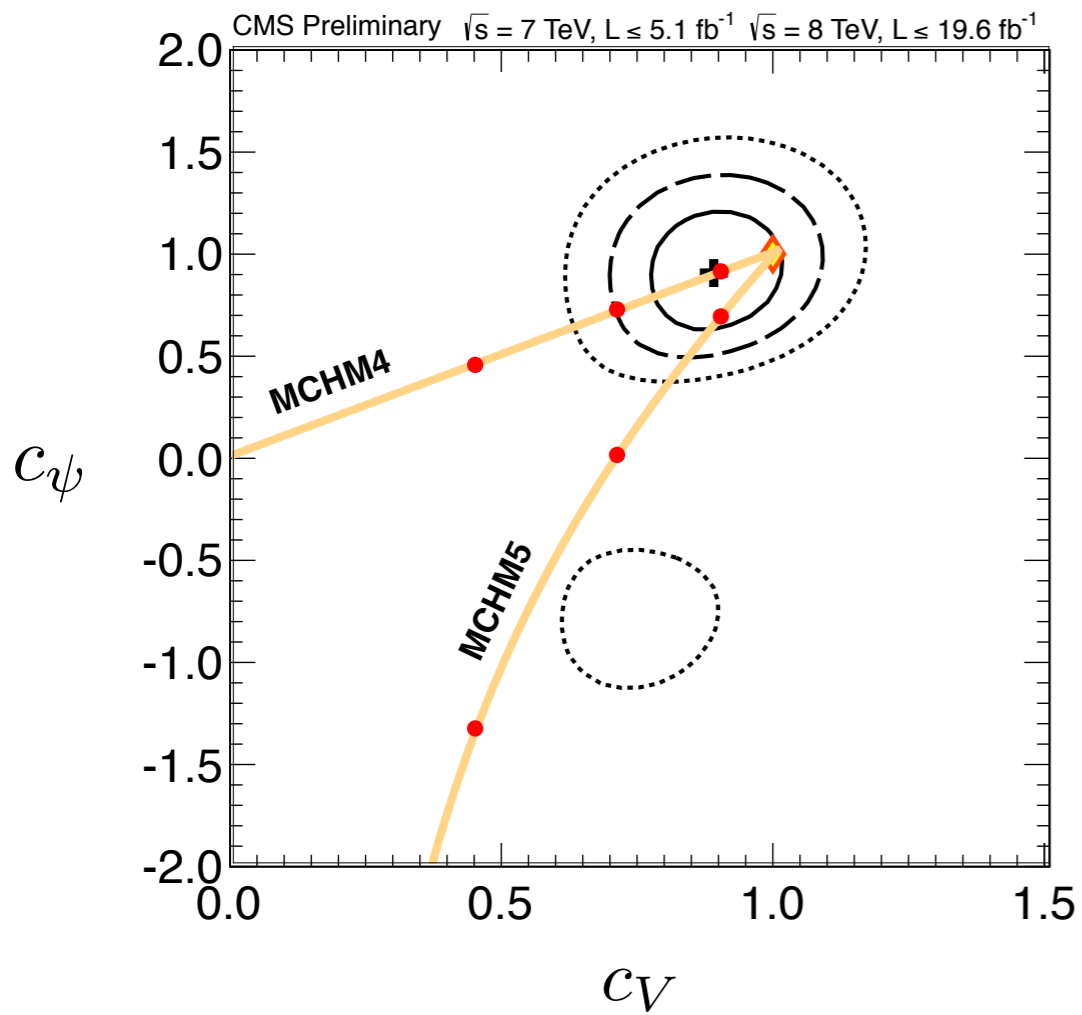
Expect deviations  $\sim (v/f)^2$

$$\xi \equiv \frac{v^2}{f^2}$$

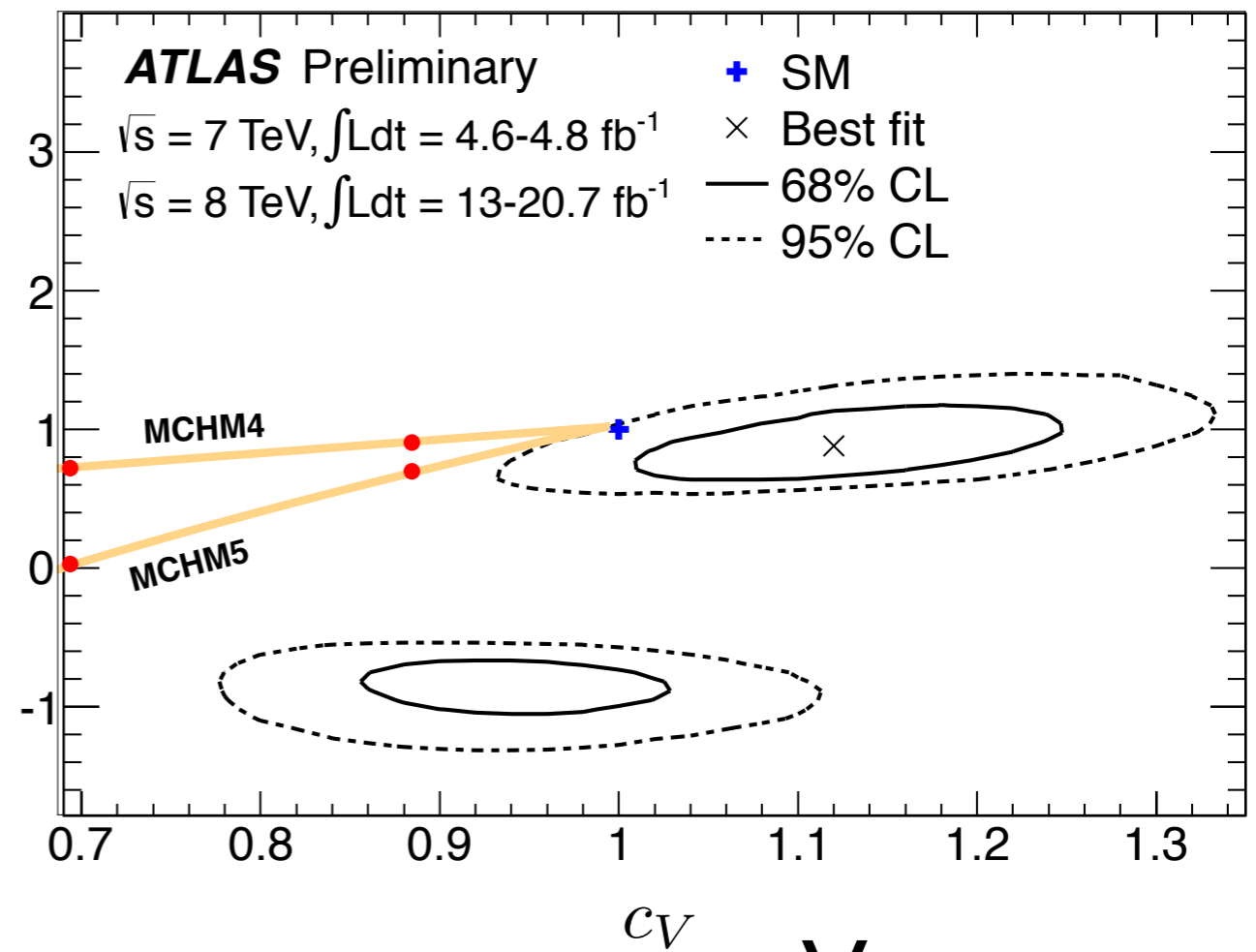
$$a = \sqrt{1 - \xi}$$

$$c_f = \frac{1 - (1 + n)\xi}{1 - \xi}$$

# Higgs couplings



Fermion



Red points at  $\xi \equiv (v/f)^2 = 0.2, 0.5, 0.8$

Vector

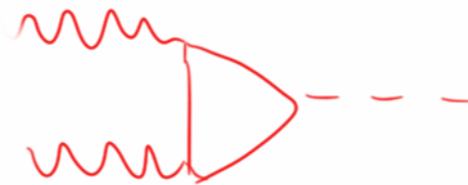
# Higgs couplings

$$\mathbf{SM} + \mathcal{L} = \frac{\alpha_s c_g}{12\pi} |H|^2 G_{\mu\nu}^a{}^2 + \frac{\alpha c_\gamma}{2\pi} |H|^2 F_{\mu\nu} + y_t c_t \bar{q}_L \tilde{H} t_R |H|^2$$

$$\frac{\sigma(gg \rightarrow h)}{\text{SM}} = (1 + (c_g - c_t)v^2)^2$$



Degeneracy 'short-distance' vs 'long-distance'



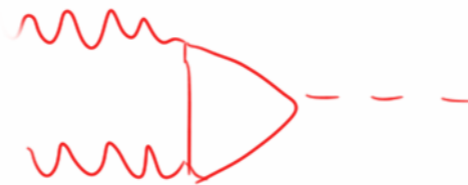
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$$\mathbf{SM} + \mathcal{L} = \frac{\alpha_s c_g}{12\pi} |H|^2 G_{\mu\nu}^a{}^2 + \frac{\alpha c_\gamma}{2\pi} |H|^2 F_{\mu\nu} + y_t c_t \bar{q}_L \tilde{H} t_R |H|^2$$

$$\frac{\sigma(gg \rightarrow h)}{\text{SM}} = (1 + (c_g - c_t)v^2)^2$$



Degeneracy ‘short-distance’ vs ‘long-distance’

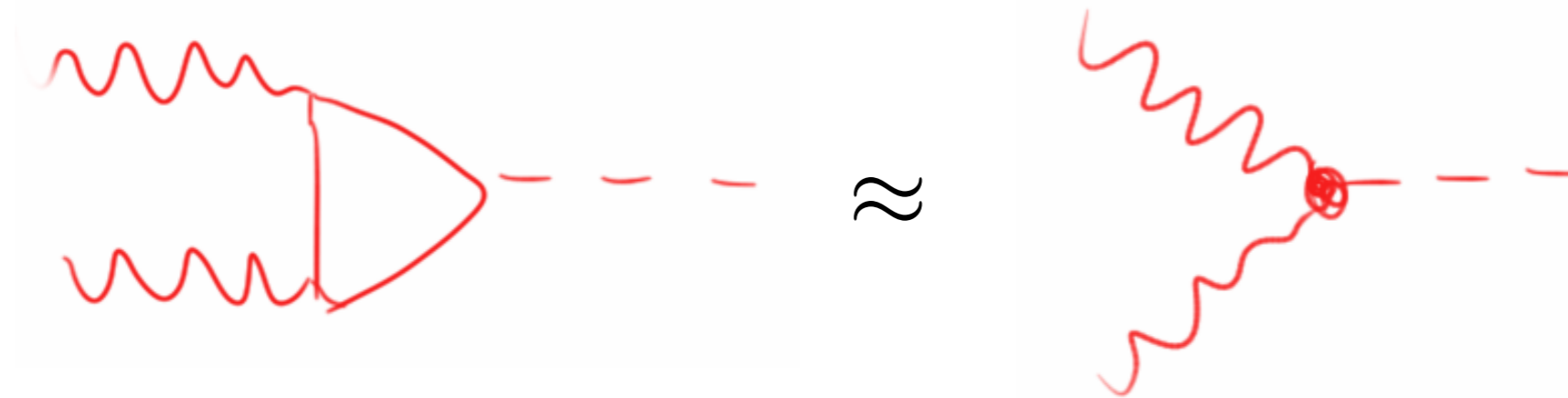


E.g. fermionic top partners MCHM:  $\Delta c_t = \Delta c_g$



$$\sigma(pp \rightarrow H + X)_{\text{inclusive}}$$

Does not resolve short-distance physics

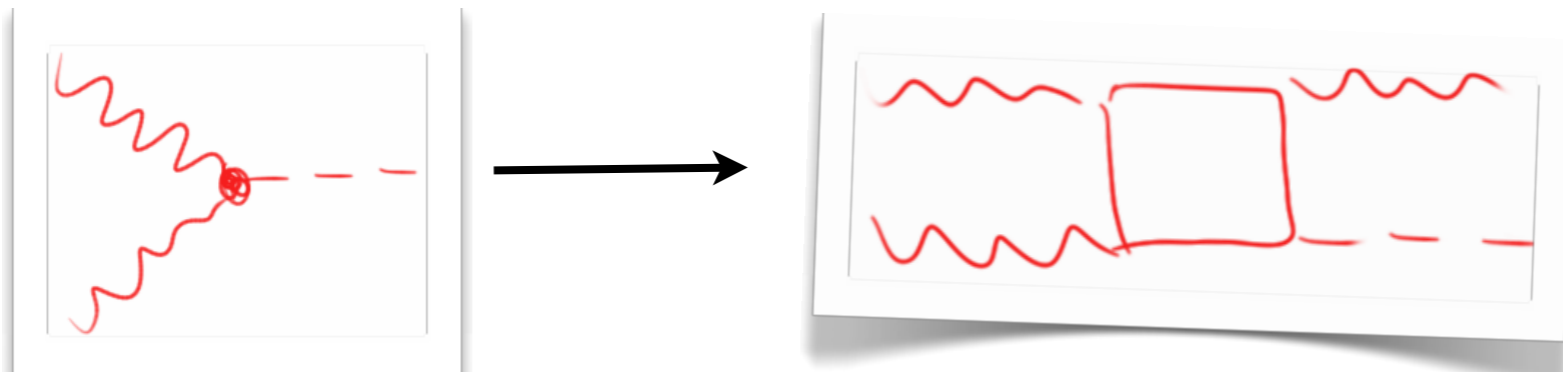


$m_H(\text{GeV})$	$\frac{\sigma_{NLO}(m_t)}{\sigma_{NLO}(m_t \rightarrow \infty)}$	$\frac{\sigma_{NLO}(m_t, m_b)}{\sigma_{NLO}(m_t \rightarrow \infty)}$
125	1.061	0.988
150	1.093	1.028
200	1.185	1.134

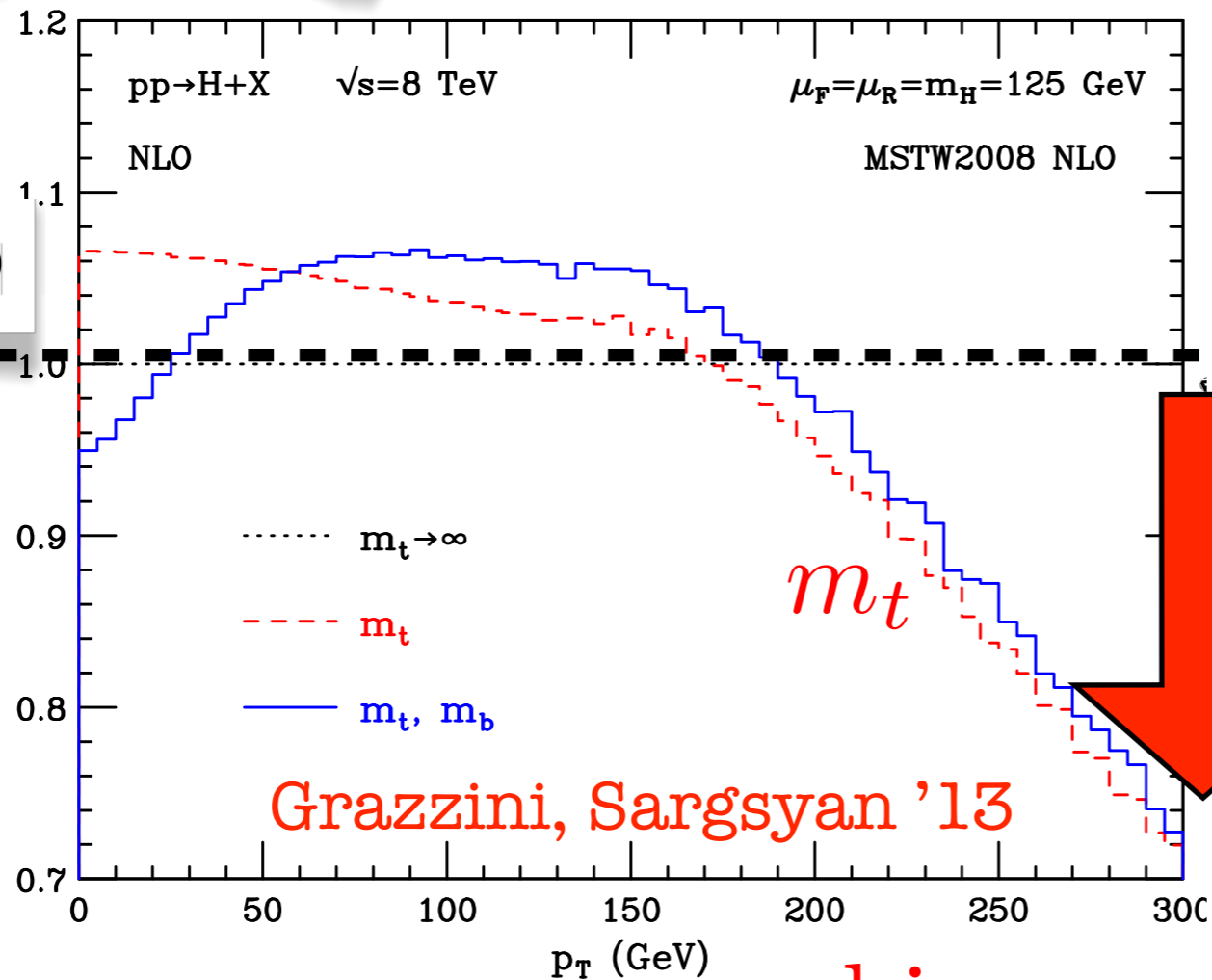
e.g. [1306.4581](#)

# Beyond current observables

Cut the loop open, recoil against hard jet



$$p_T \gg m_t$$



Baur, Glover '90,  
Langenegger et. al '06,  
1308.4771

high  $p_T$  tail resolves  
loop dynamics

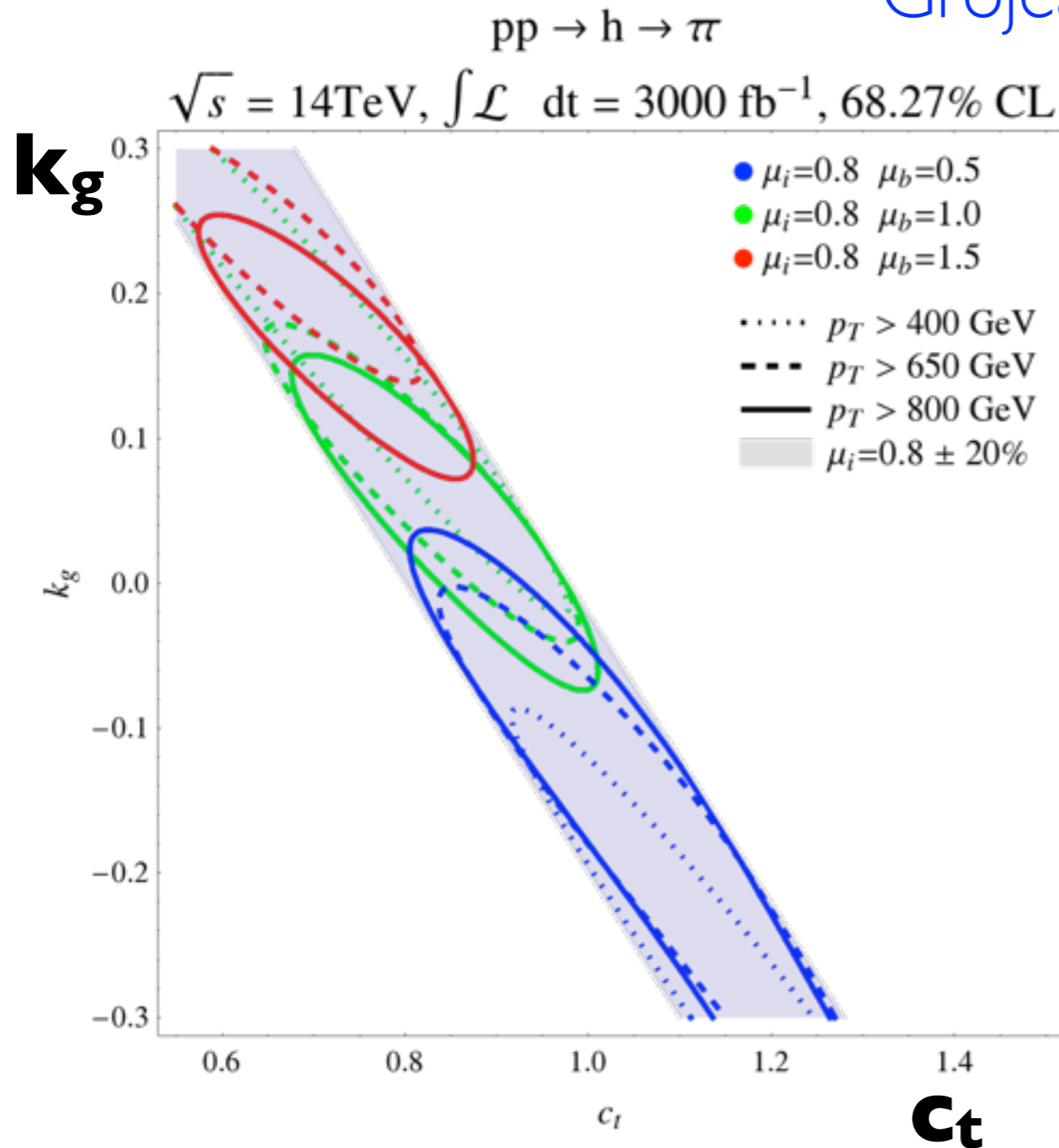
Grazzini, Sargsyan '13

higgs -  $p_T$

$$m_t \rightarrow \infty$$

# Complementary to $h\bar{t}t$

Grojean, Salvioni, Schlaffer, AW, in progress



Competitive/complement to notoriously difficult  $h\bar{t}t$  channel

Theory frontier:

NLO $_{m_t}$  not yet calculated,  
 $1/m_t$  known to  $\mathcal{O}(\alpha_S^4)$ :  
few % up to  $p_T \sim 150 \text{ GeV}$

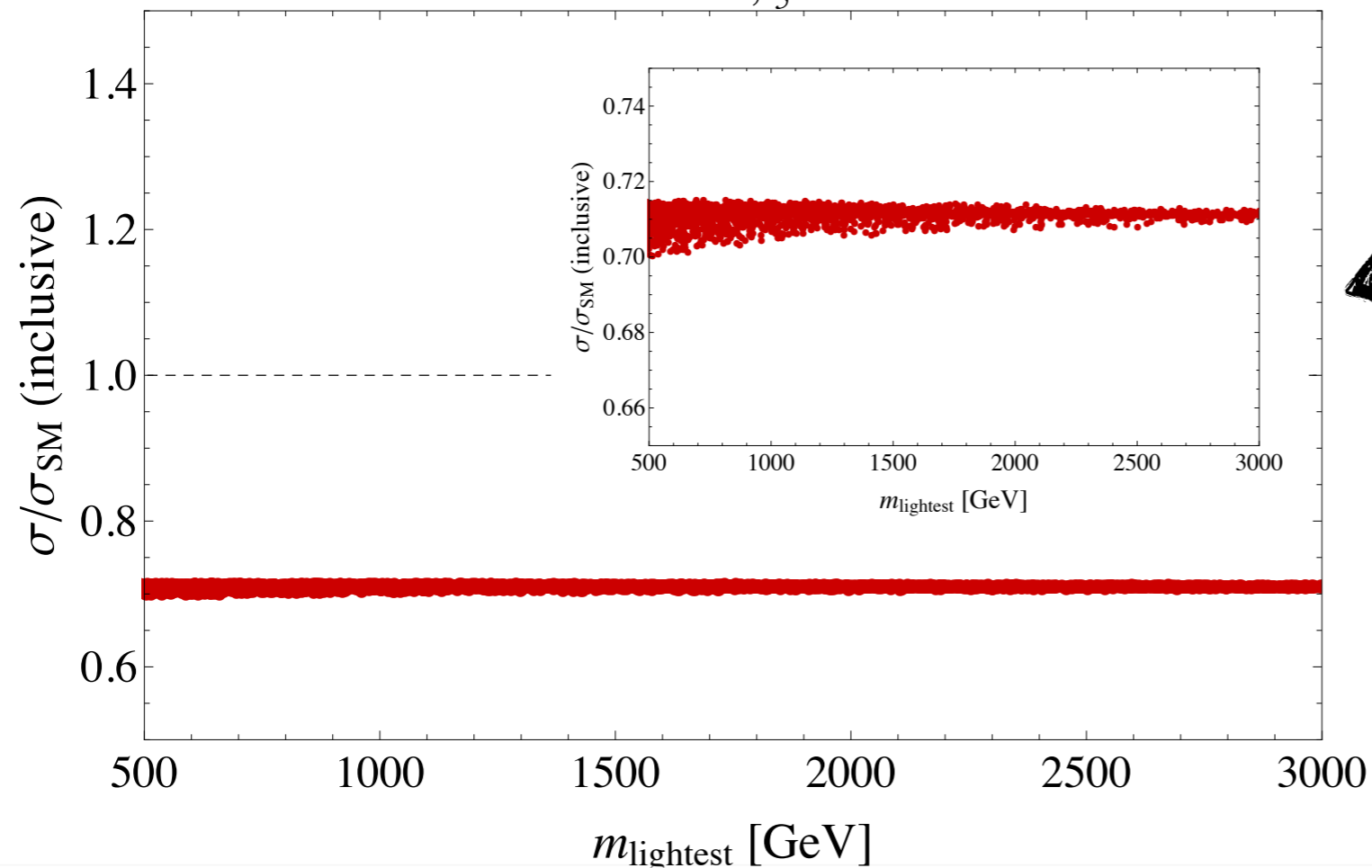
Harlander et al '12

# Top partner example

Grojean, Salvioni, Schlaffer, AW

**Inclusive**

MCHM 5,  $\xi = 0.1$

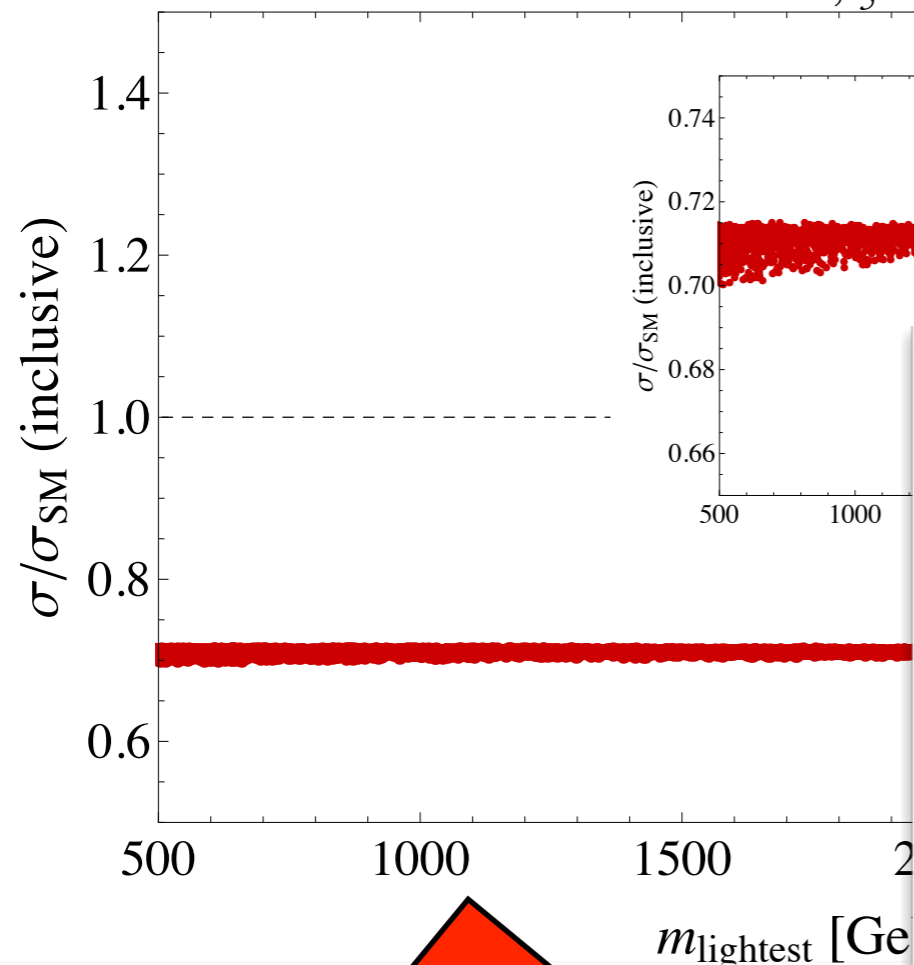


# Top partner example

Grojean, Salvioni, Schlaffer, AW

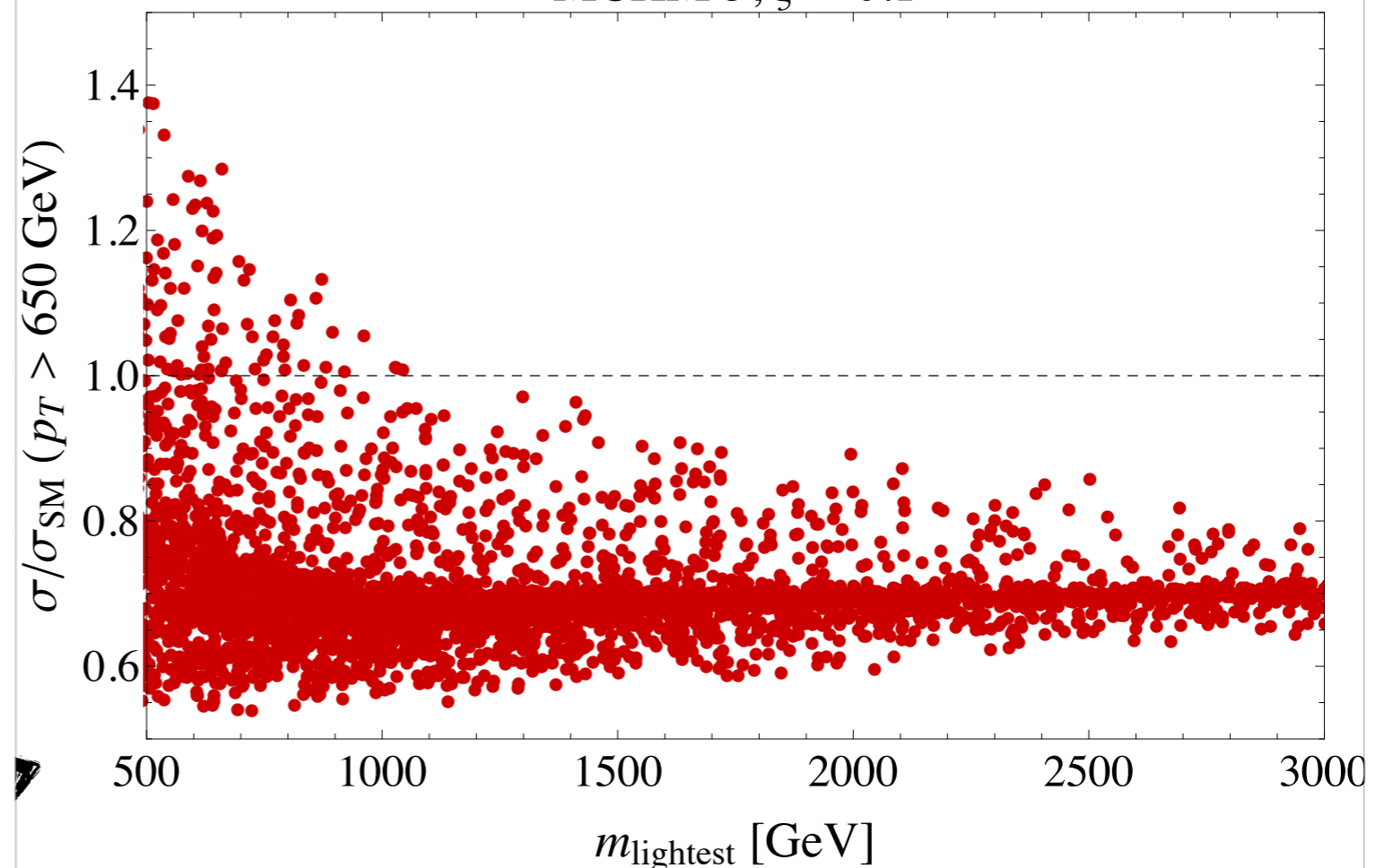
**Inclusive**

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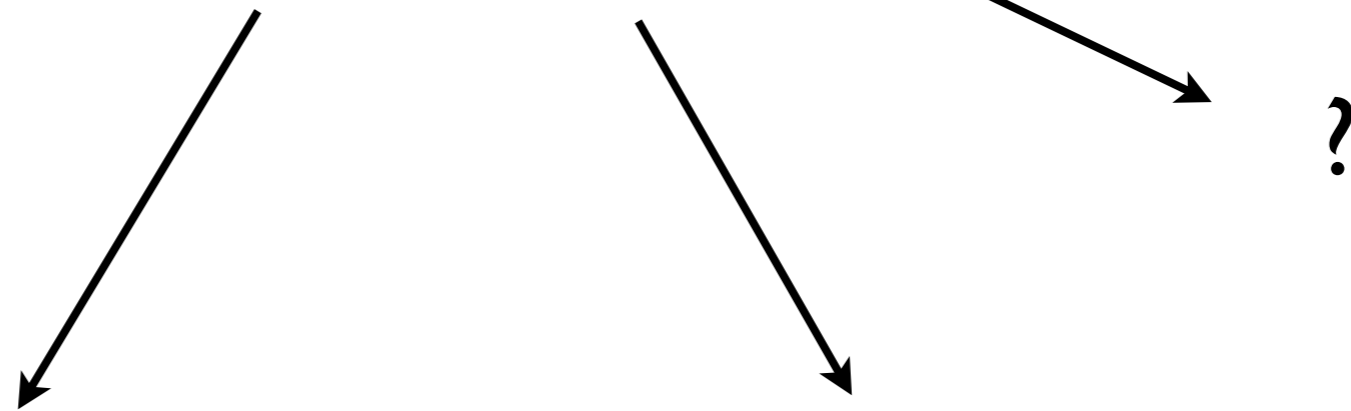
MCHM 5,  $\xi = 0.1$

**high  $p_T$**



# New physics & naturalness

## Light Higgs

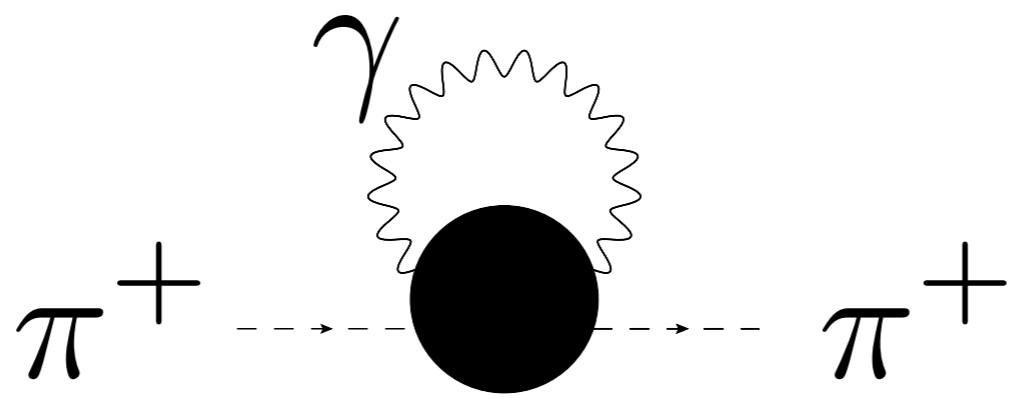


light stops<sub>1,2</sub>, sbottom<sub>L</sub>,  
higgsinos, gluinos, ...

supersymmetry

light top partners  
( $Q=5/3, 2/3, 1/3$ ),  
anything else ?

composite Higgs



Das et al '67

# Implications of $m_H = 125 \text{ GeV}$

Potential is fully radiatively generated

Agashe et. al

$$V_{gauge}(h) = \frac{9}{2} \int \frac{d^4 p}{(2\pi)^4} \log \left( \Pi_0(p) + \frac{s_h^2}{4} \Pi_1(p) \right) \quad s_h \equiv \sin h/f$$

$$\Pi_0(p) = \frac{p^2}{g^2} + \Pi_a(p) \quad , \quad \Pi_1(p) = 2[\Pi_{\hat{a}}(p) - \Pi_a(p)]$$



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$$\int d^4 p \Pi_1(p)/\Pi_0(p) < \infty$$

**Higgs dependent term  
UV finite**

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Higgs dependent term  
UV finite

→ 'Weinberg sum rules'

$$\lim_{p^2 \rightarrow \infty} \Pi_1(p) = 0 ,$$

$$\lim_{p^2 \rightarrow \infty} p^2 \Pi_1(p) = 0$$

UV finiteness requires at least two resonances

$$\Pi_1(p) = \frac{f^2 m_\rho^2 m_{a_1}^2}{(p^2 + m_\rho^2)(p^2 + m_{a_1}^2)} \quad \text{spin 1}$$

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Similarly for SO(5) fermionic contribution

Pomarol et al; Marzocca

$$m_h^2 \simeq \frac{N_c}{\pi^2} \left[ \frac{m_t^2}{f^2} \frac{m_{Q_4}^2 m_{Q_1}^2}{m_{Q_1}^2 - m_{Q_4}^2} \log \left( \frac{m_{Q_1}^2}{m_{Q_4}^2} \right) \right]$$

similar result in deconstruction:  
Matsedonskyi et al; Redi et al

5 = 4 + 1      with EM charges 5/3, 2/3, -1/3  
 $Q_4$     $Q_1$

→ solve for  $m_h = 125$  GeV

# Light Higgs implies light fermionic top partners

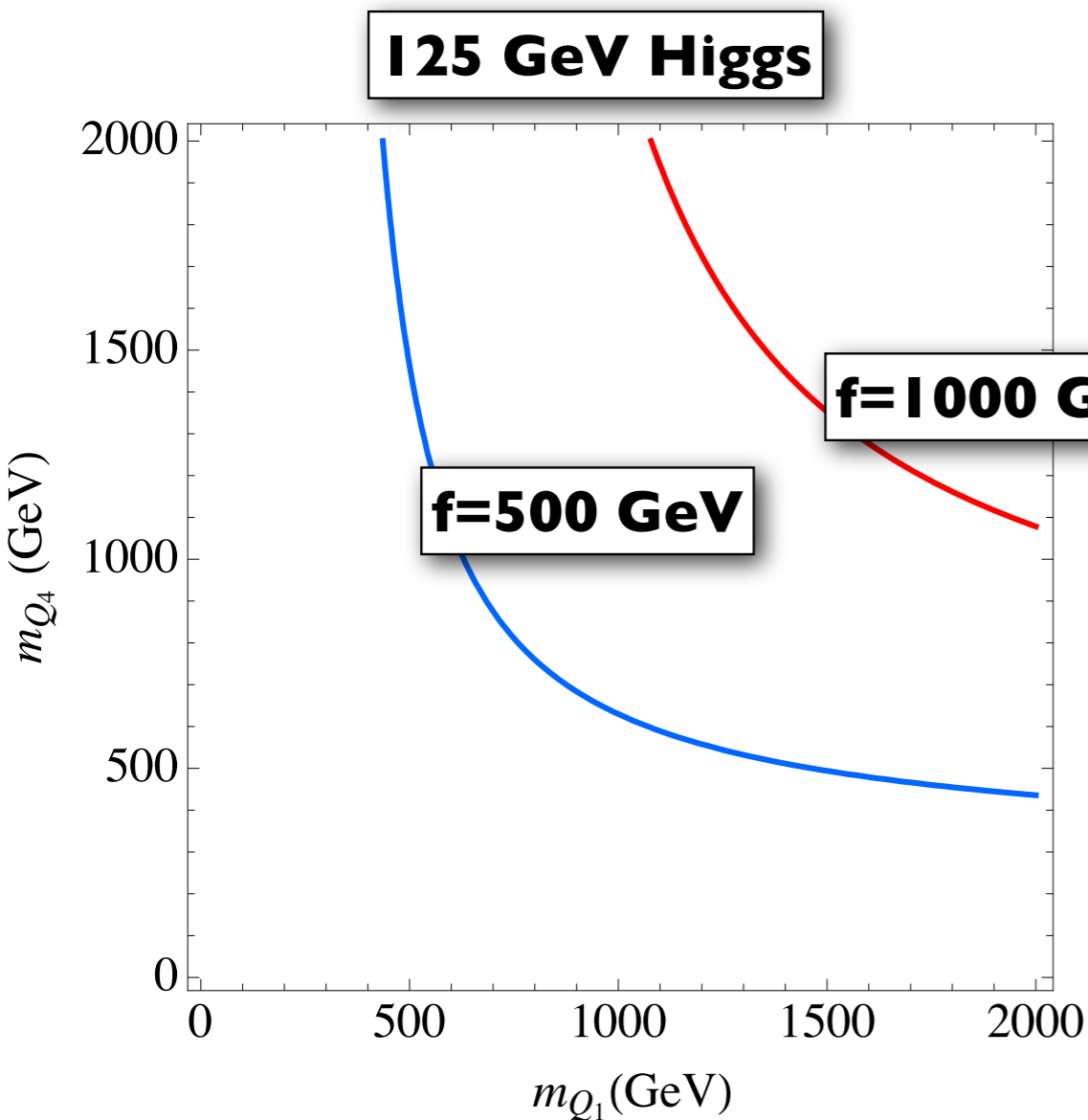
$$m_h^2 \simeq \frac{N_c}{\pi^2} \left[ \frac{m_t^2}{f^2} \frac{m_{Q_4}^2 m_{Q_1}^2}{m_{Q_1}^2 - m_{Q_4}^2} \log \left( \frac{m_{Q_1}^2}{m_{Q_4}^2} \right) \right]$$

Pomarol et al; Marzocca

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Pomarol et al; Marzocca



$$5 = 4 + 1$$

$Q_4 \quad Q_1$

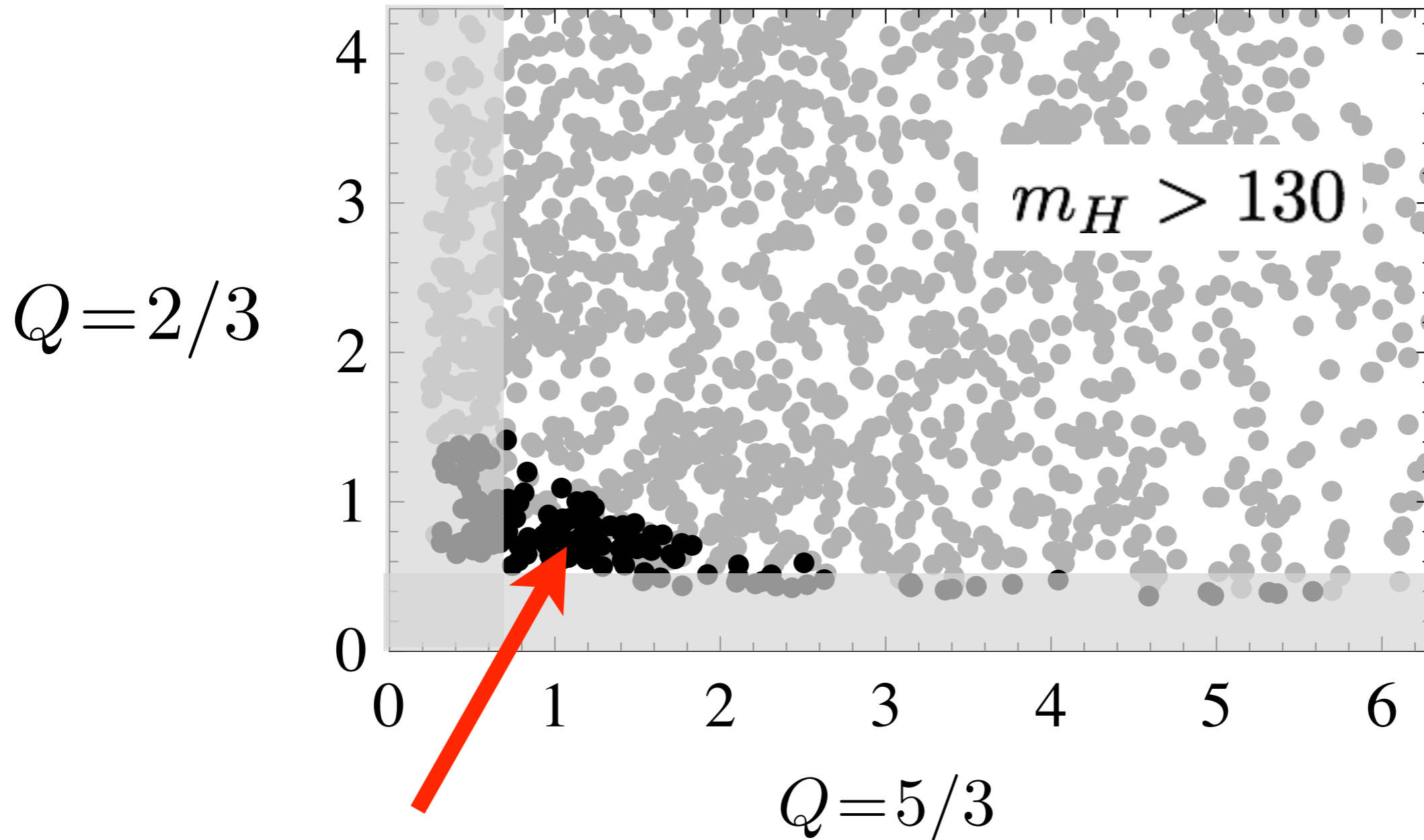
with EM charges  $5/3, 2/3, -1/3$

Contino et al; Pomarol, Riva;  
Matsedonskyi, Panico, Wulzer; Redi, Tesi;  
Marzocca, Serone, Shu;

# Scan over composite Higgs parameter space

$$\xi = 0.2$$

from 1204.6333

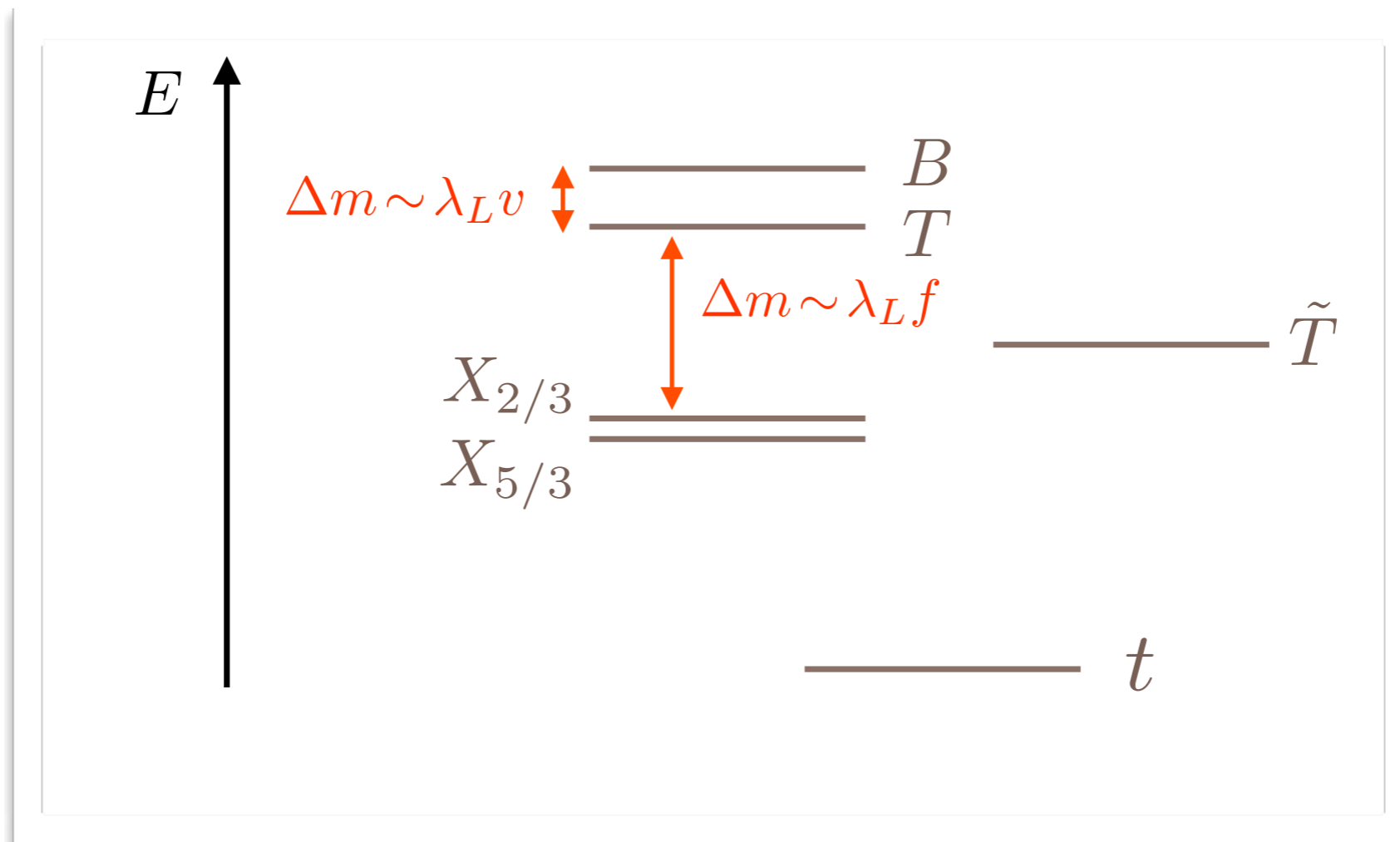


$$Q = 2/3$$

$$Q = 5/3$$

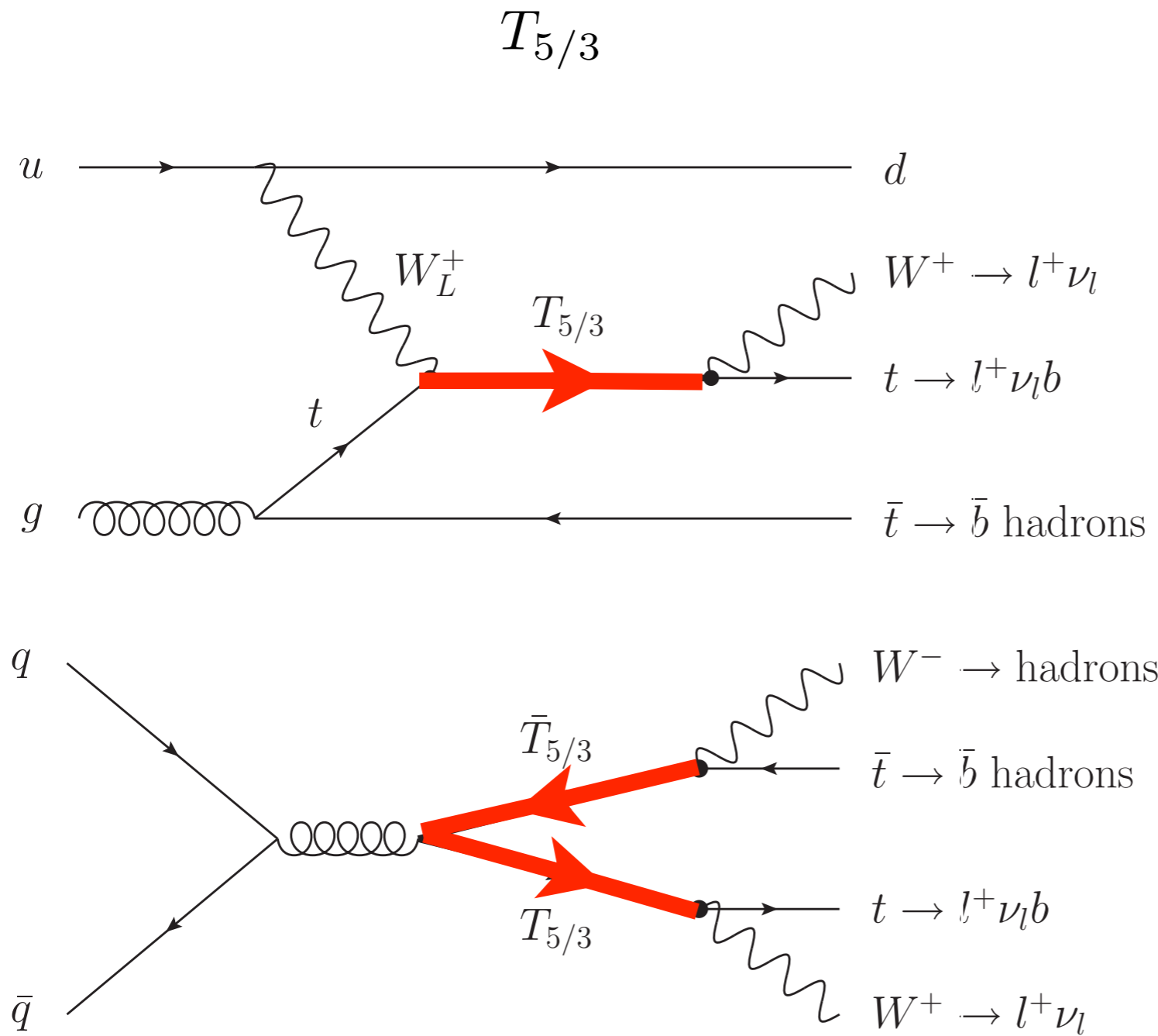
$$m_H = 115 \dots 130 \text{ GeV}$$

# Top partners





e.g. Perelstein, Pierce, Peskin  
 Contino, Servant; Mrazek, Wulzer;  
 De Simone, Matsedonkyi, Rattazzi, Wulzer



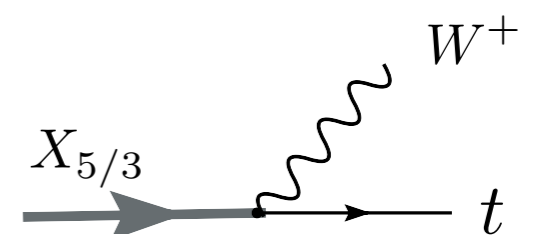
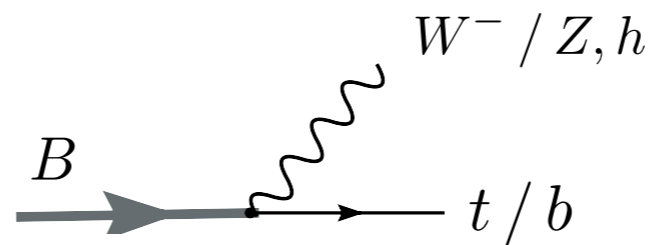
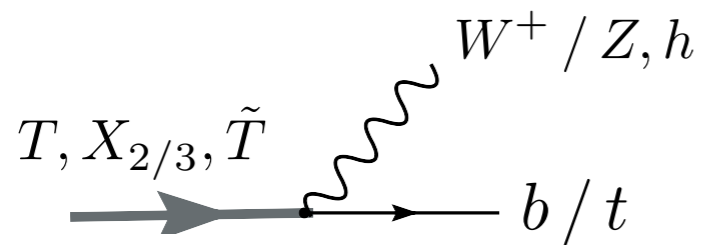
**Single**

**Spectrum:**  
 —  $B$   
 —  $T$

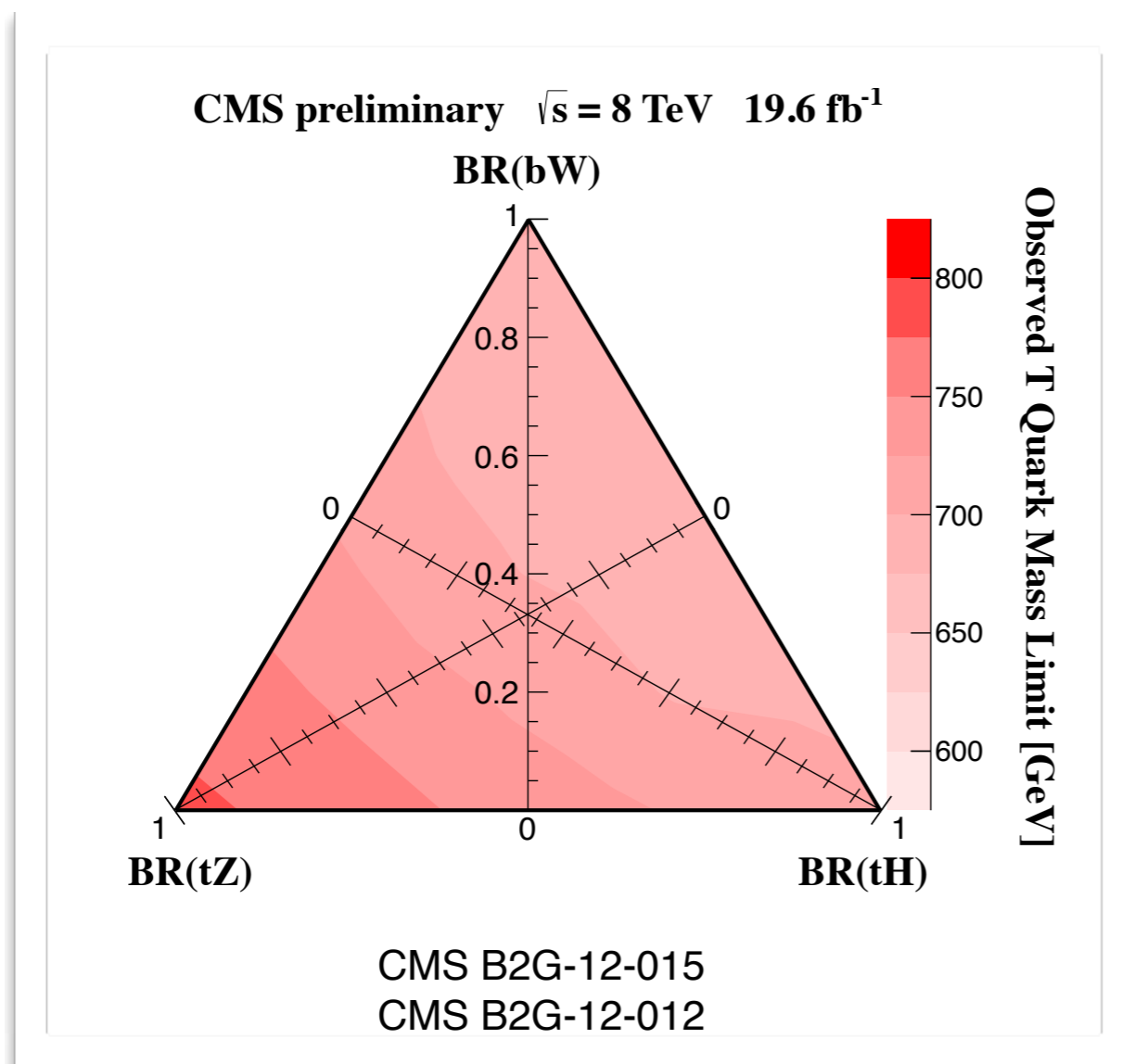
$X_{2/3}$   
 $X_{5/3}$

**Double**

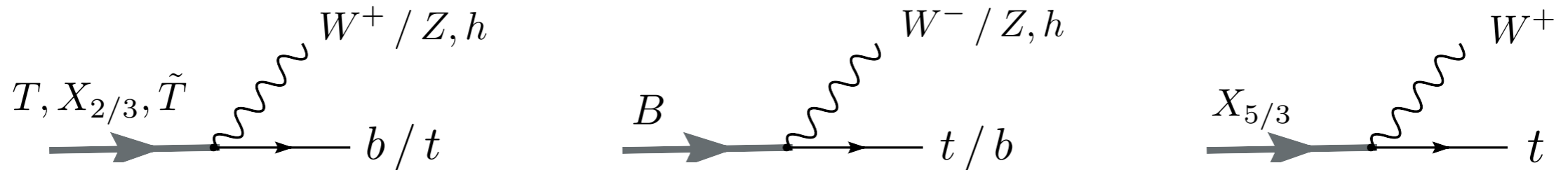
# Decay modes



Current limits  
 $> 700 - 800 \text{ GeV}$



# Decay modes



Current limits  
 $> 700 - 800 \text{ GeV}$

CMS preliminary  $\sqrt{s} = 8 \text{ TeV} \quad 19.6 \text{ fb}^{-1}$

BR(hW)

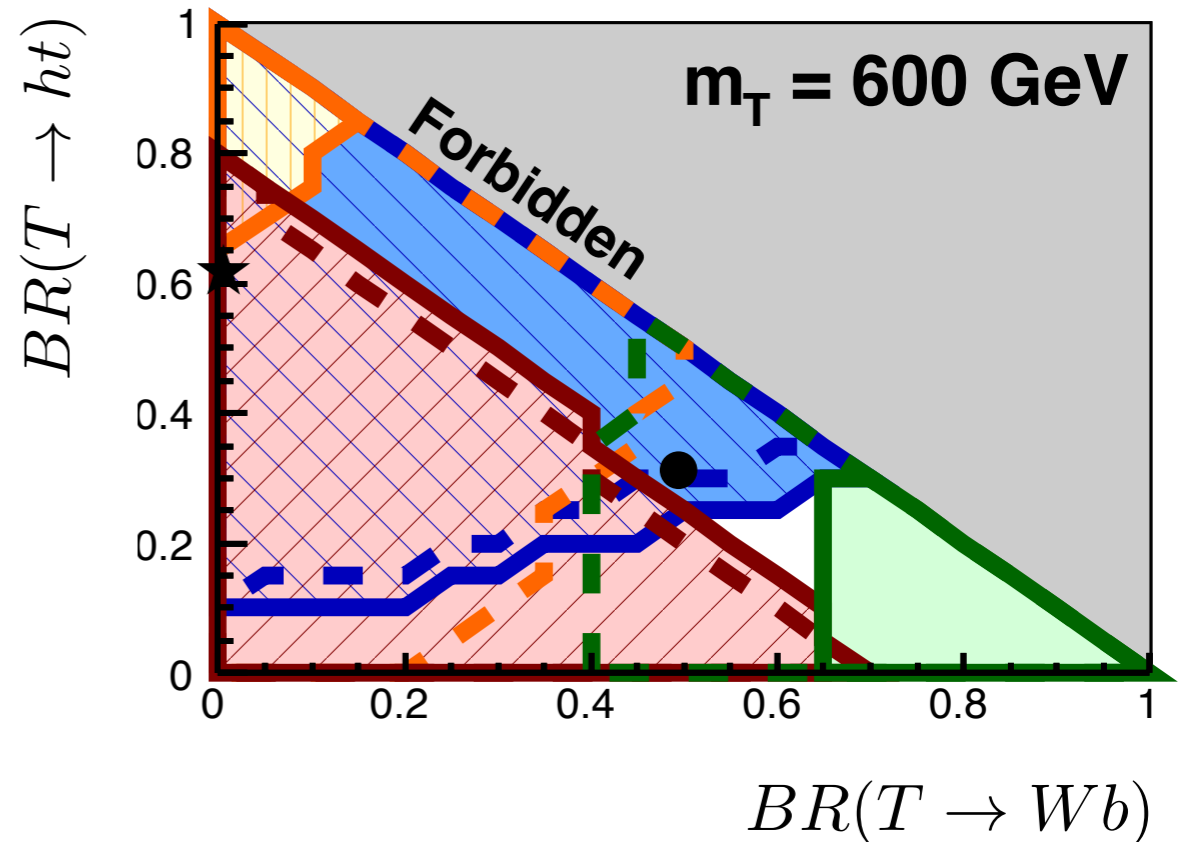
**ATLAS Preliminary**

Status: Lepton-Photon 2013

$\sqrt{s} = 8 \text{ TeV}, \quad \int L dt = 14.3 \text{ fb}^{-1}$

- 95% CL exp. excl.
  95% CL obs. excl.
- Ht+X [ATLAS-CONF-2013-018]
- Same-Sign [ATLAS-CONF-2013-051]
- Zb/t+X [ATLAS-CONF-2013-056]
- Wb+X [ATLAS-CONF-2013-060]
- ★ SU(2) (T,B) doub.
 ● SU(2) singlet

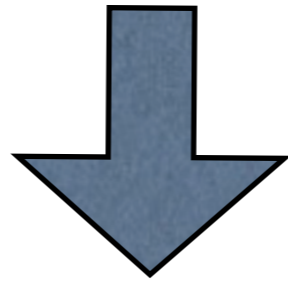
BR(t)



# Flavor used to be a show-stopper

## CPV in Kaon mixing

$$|\epsilon| = 2.3 \times 10^{-3} \implies \frac{M_{ETC}}{g_{ETC} \sqrt{\text{Im}(V_{sd}^2)}} \gtrsim 16,000 \text{ TeV}$$

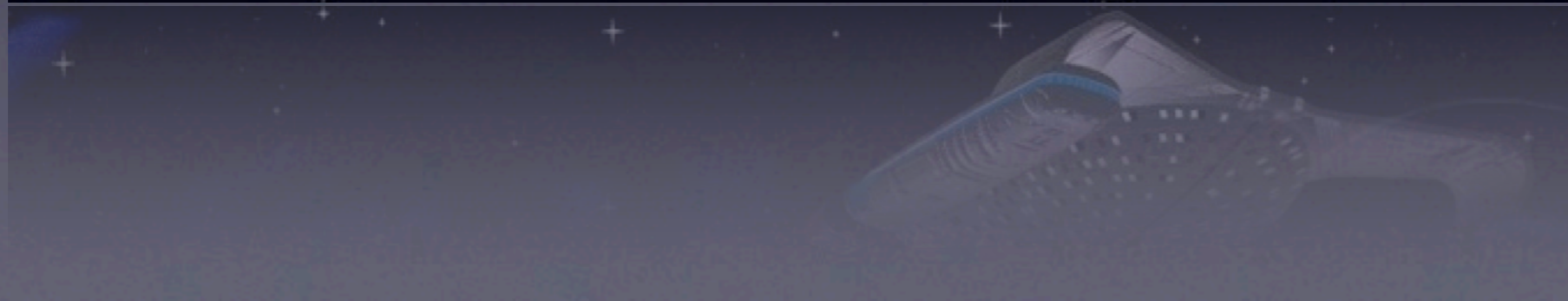


$$m_{q,\ell,T}(M_{ETC}) \simeq \frac{g_{ETC}^2}{2M_{ETC}^2} \langle \bar{T}T \rangle_{ETC} \lesssim \frac{0.1 \text{ MeV}}{|V_{sd}|^2 N^{3/2}} \quad \text{vs. } m_{\text{top}}$$

“Into the Extra-dimension  
and back”



Exciting journey...



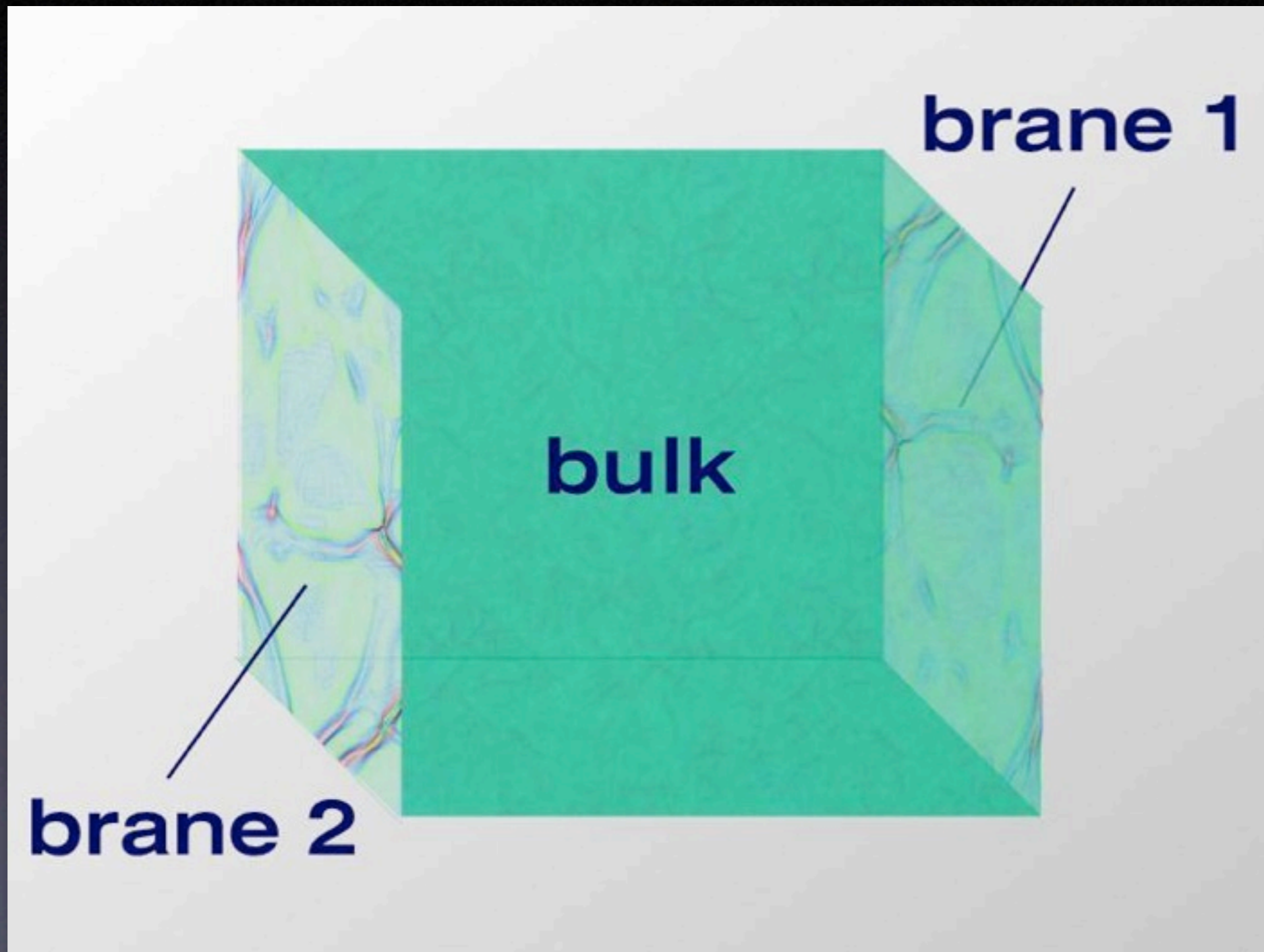


Depends on the perspective...



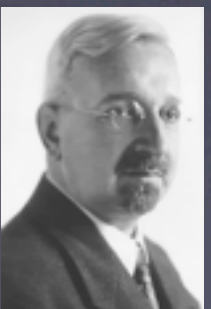


# Extra-dimensions



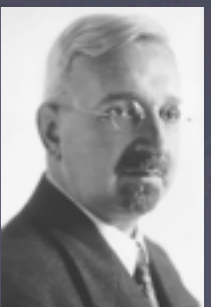
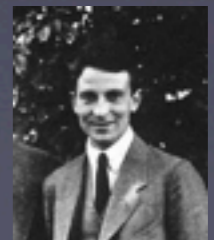


# General Properties of ED theories



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Compact Extra-dimension  $\Rightarrow$  momentum in ED direction is quantized:  $p_{ED} = n/(\text{size of ED})$



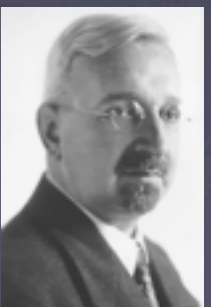


# General Properties of ED theories

Compact Extra-dimension => momentum in ED direction is quantized:  $p_{ED} = n/(\text{size of ED})$

$$p^2 = m^2 \quad \rightarrow \quad p_{5D}^2 = p^2 - (n/R)^2 = m^2$$

4D  5D





# General Properties of ED theories

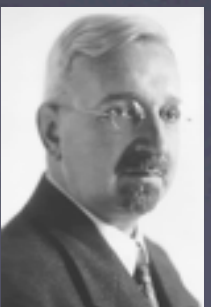
Compact Extra-dimension  $\Rightarrow$  momentum in ED direction is quantized:  $p_{ED} = n/(\text{size of ED})$

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4D  5D

Two pictures ( $n/R$  on LHS or RHS):

1) 5D field with quantized momentum and mass  $m^2$





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Compact Extra-dimension  $\Rightarrow$  momentum in ED direction is quantized:  $p_{ED} = n/(\text{size of ED})$

$$p^2 = m^2 \quad \xrightarrow{\quad} \quad p_{5D}^2 = p^2 - (n/R)^2 = m^2$$

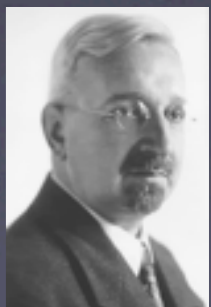
4D  5D

Two pictures ( $n/R$  on LHS or RHS):

- 1) 5D field with quantized momentum and mass  $m^2$
- 2) **infinite** tower of 4D fields labeled by 5 momentum  $n/R$  with masses

$$M_n^2 = m^2 + (n/R)^2$$

new particles: Kaluza Klein (KK) modes



# The SM flavor puzzle

$$Y_D \approx \text{diag} (2 \cdot 10^{-5} \quad 0.0005 \quad 0.02)$$

$$Y_U \approx \begin{pmatrix} 6 \cdot 10^{-6} & -0.001 & 0.008 + 0.004i \\ 1 \cdot 10^{-6} & 0.004 & -0.04 + 0.001i \\ 8 \cdot 10^{-9} + 2 \cdot 10^{-8}i & 0.0002 & 0.98 \end{pmatrix}$$

Why this structure?

Other dimensionless parameters of the SM:

$$g_s \sim 1, \quad g \sim 0.6, \quad g' \sim 0.3, \quad \lambda_{\text{Higgs}} \sim 1, \quad |\theta| < 10^{-9}$$



# Log(SM flavor puzzle)

$$-\log |Y_D| \approx \text{diag} (11 \quad 8 \quad 4)$$

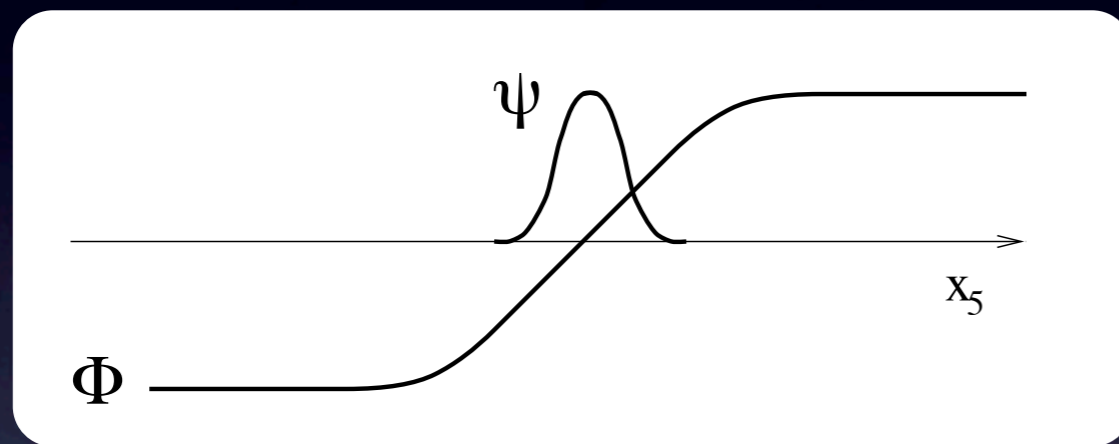
$$-\log |Y_U| \approx \begin{pmatrix} 12 & 7 & 5 \\ 14 & 6 & 3 \\ 18 & 9 & 0 \end{pmatrix}$$

If  $Y = e^{-\Delta}$ , then the  $\Delta$  don't look crazy.

# Hierarchies w/o Symmetries

Arkani-Hamed, Schmaltz

SM on thick brane & domain wall  $\Rightarrow$  chiral localization



$$\mathcal{S} = \int d^5x \sum_{i,j} \bar{\Psi}_i [i \not{\partial}_5 + \lambda \Phi(x_5) - m]_{ij} \Psi_j$$

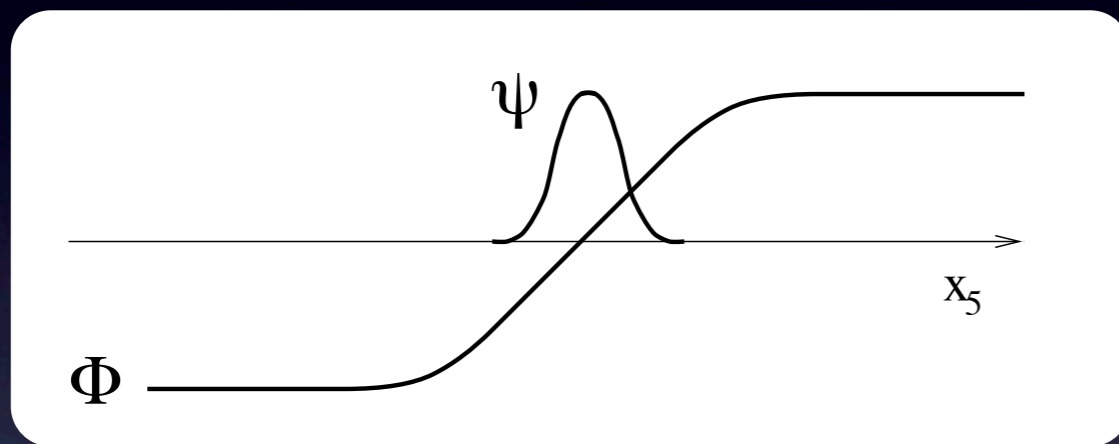
$$\Psi = \begin{pmatrix} \Psi_L \\ \Psi_R \end{pmatrix} = \begin{pmatrix} \psi_L^0 \\ 0 \end{pmatrix} + \text{KK modes}$$



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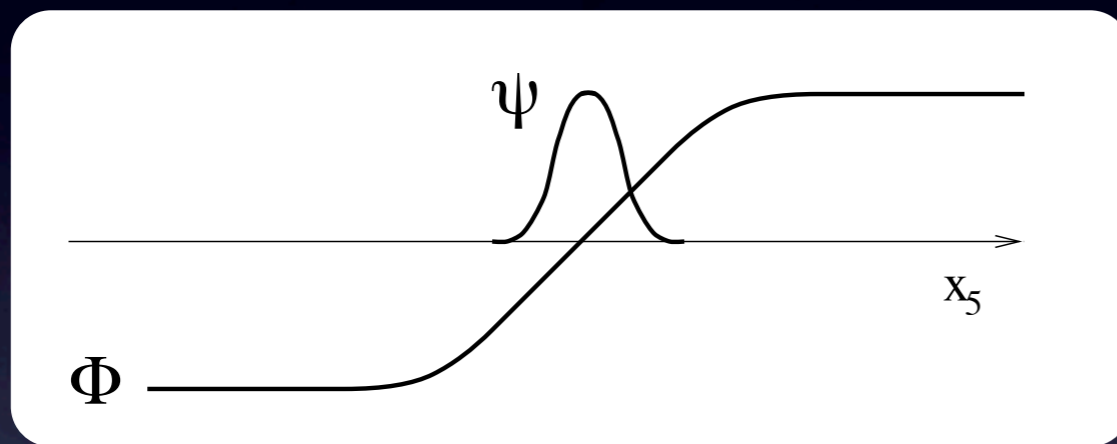
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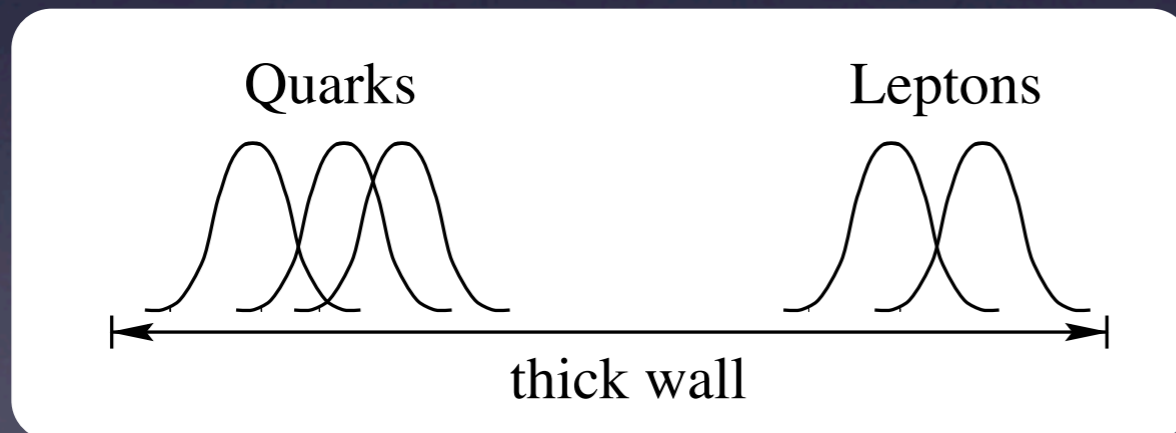
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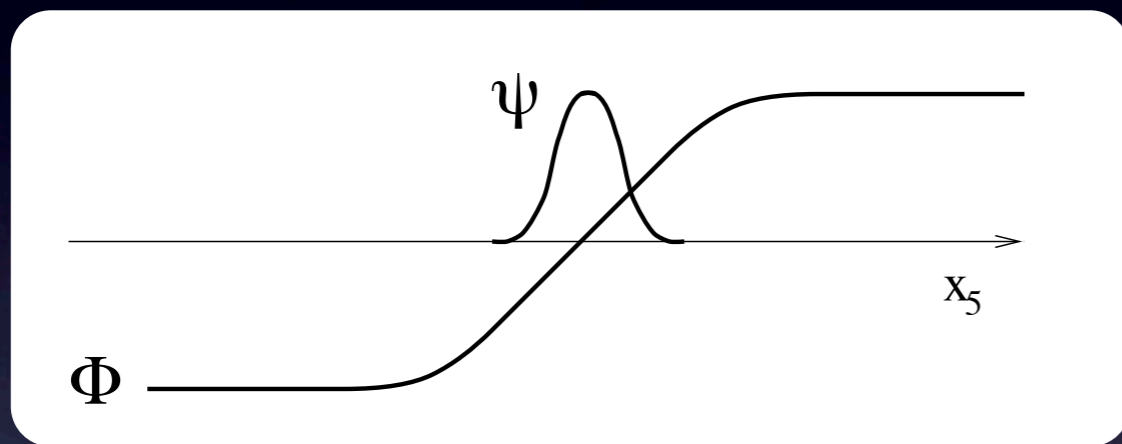
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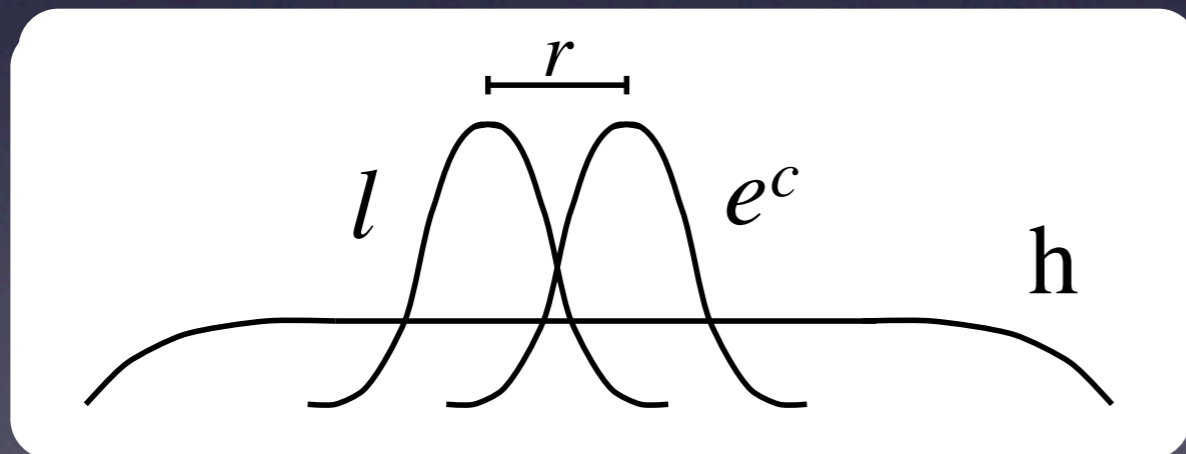
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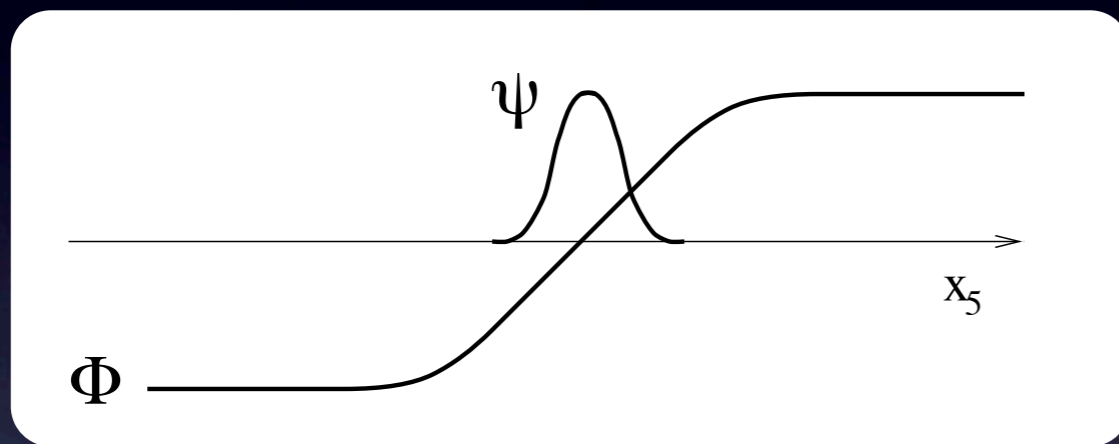
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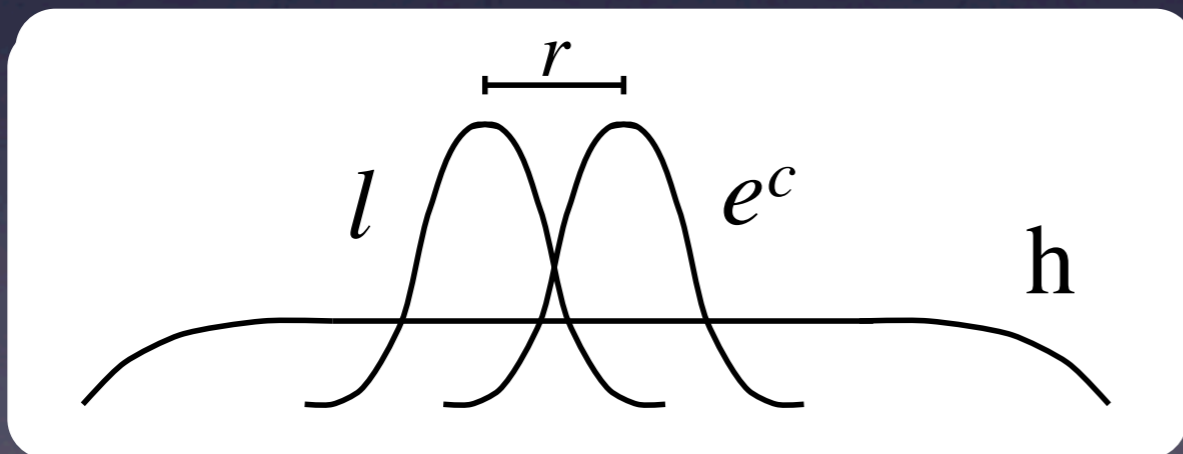
Arkani-Hamed, Schmaltz

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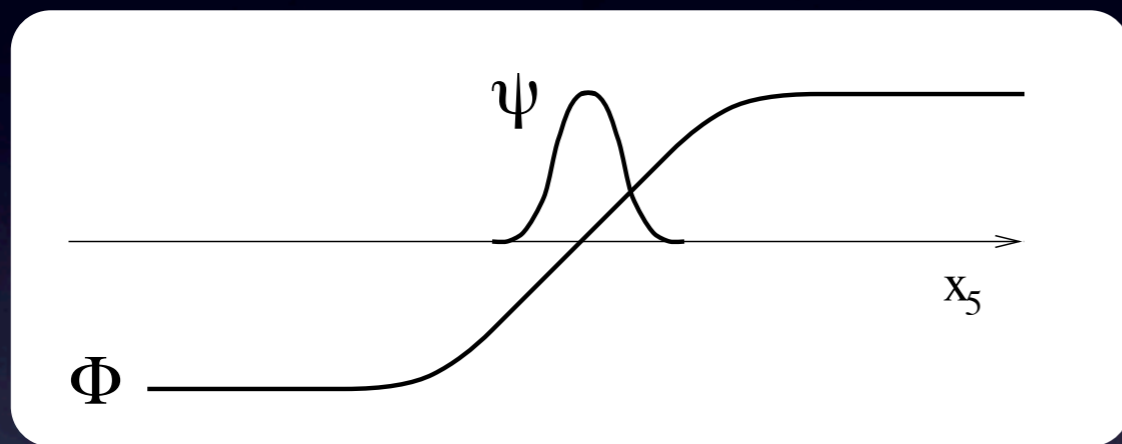
$$\int dx_5 \phi_l(x_5) \phi_{ec}(x_5) = \frac{\sqrt{2}\mu}{\sqrt{\pi}} \int dx_5 e^{-\mu^2 x_5^2} e^{-\mu^2 (x_5 - r)^2} = e^{-\mu^2 r^2 / 2}$$



# Hierarchies w/o Symmetries

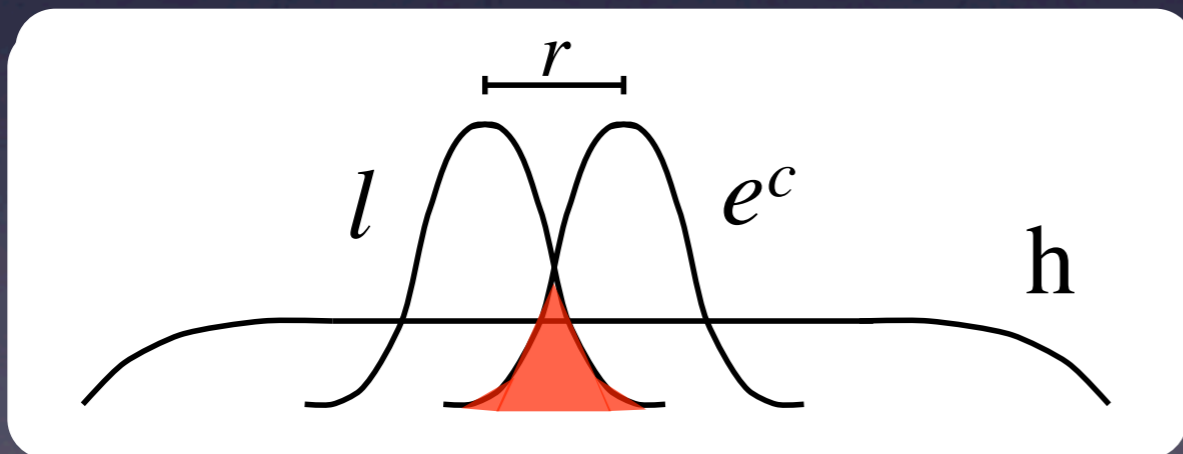
Arkani-Hamed, Schmaltz

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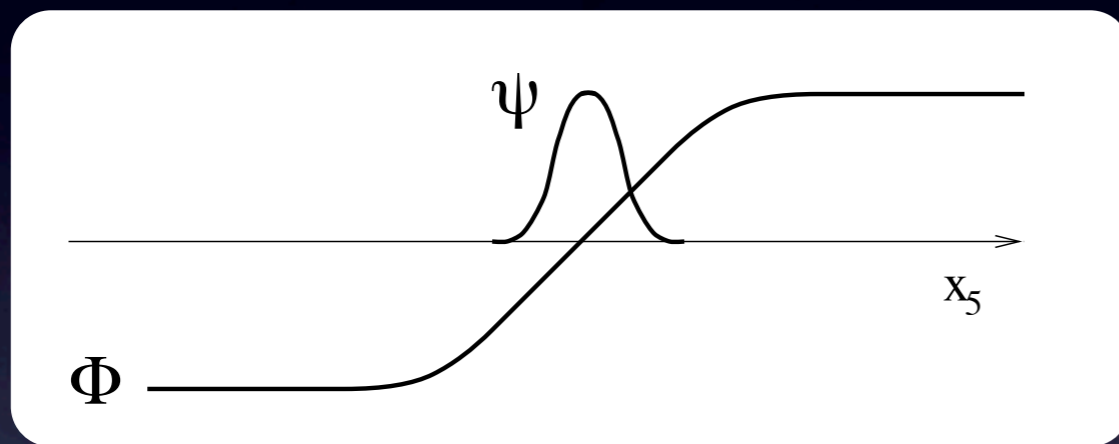


$$\int dx_5 \phi_l(x_5) \phi_{e^c}(x_5) = \frac{\sqrt{2}\mu}{\sqrt{\pi}} \int dx_5 e^{-\mu^2 x_5^2} e^{-\mu^2 (x_5 - r)^2} = \underline{e^{-\mu^2 r^2 / 2}}$$

# Hierarchies w/o Symmetries

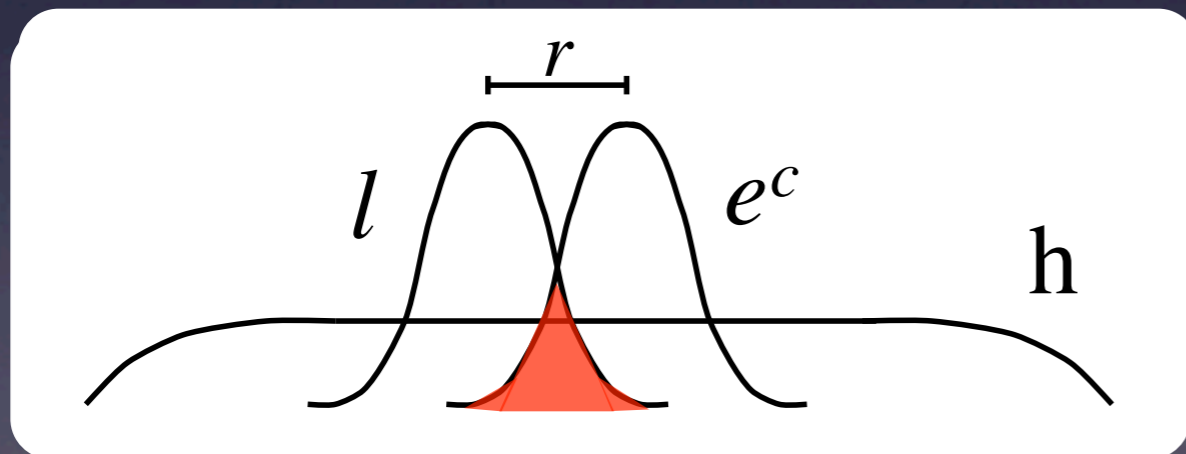
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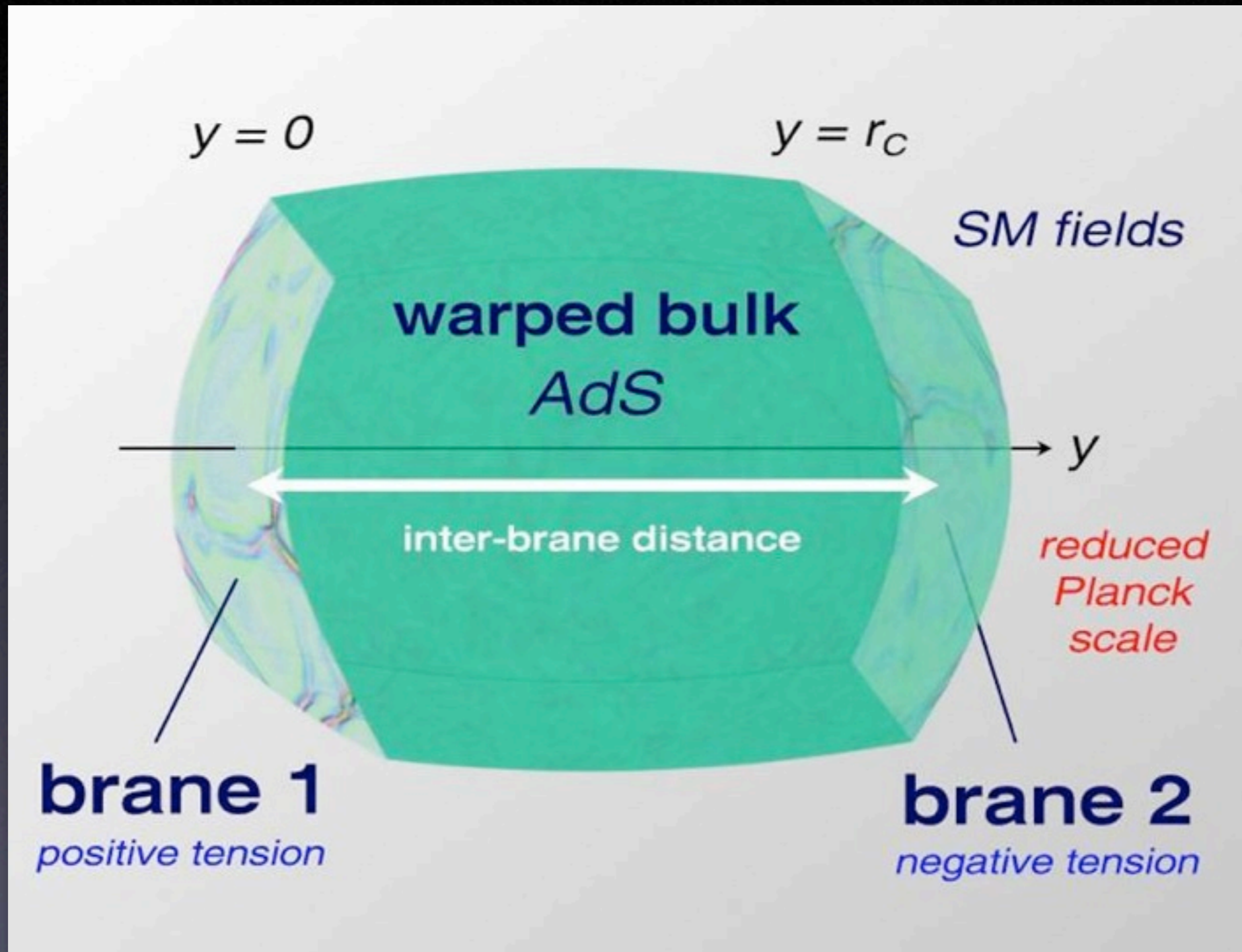
$$\Psi = \begin{pmatrix} \Psi_L \\ \Psi_R \end{pmatrix} = \begin{pmatrix} \psi_L^0 \\ 0 \end{pmatrix} + \text{KK modes}$$



Log(flavor hierarchy)!

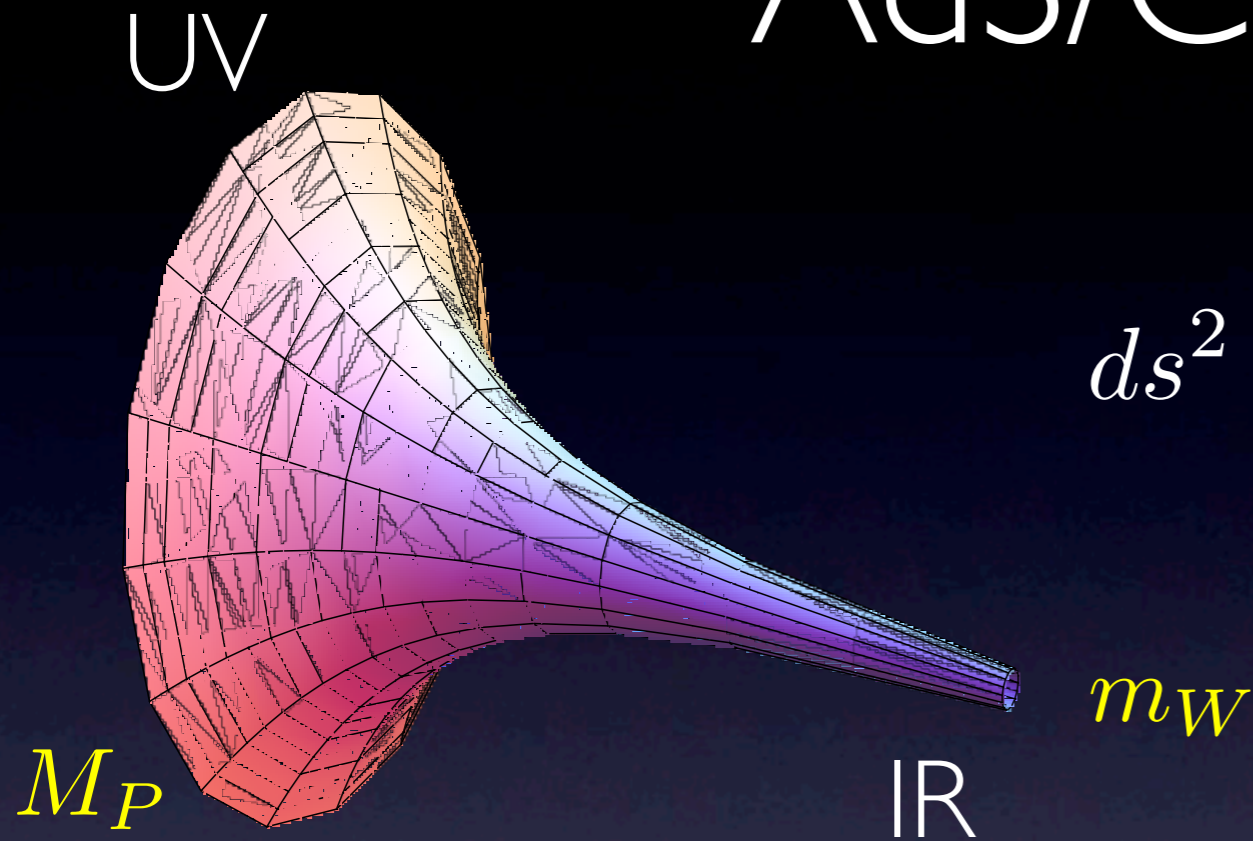
$$\int dx_5 \phi_l(x_5) \phi_{e^c}(x_5) = \frac{\sqrt{2}\mu}{\sqrt{\pi}} \int dx_5 e^{-\mu^2 x_5^2} e^{-\mu^2 (x_5 - r)^2} = \underline{e^{-\mu^2 r^2 / 2}}$$

# Warped Extra Dimensions





# AdS/CFT dictionary



$$ds^2 = \left(\frac{R}{z}\right)^2 (dx_\mu dx_\nu - dz^2)$$

Randall, Sundrum

Anti-de-Sitter (AdS)



Conformal (CFT)

Compactification



Mass gap

Red-shifting of scales



Dimensional trans-  
mutation

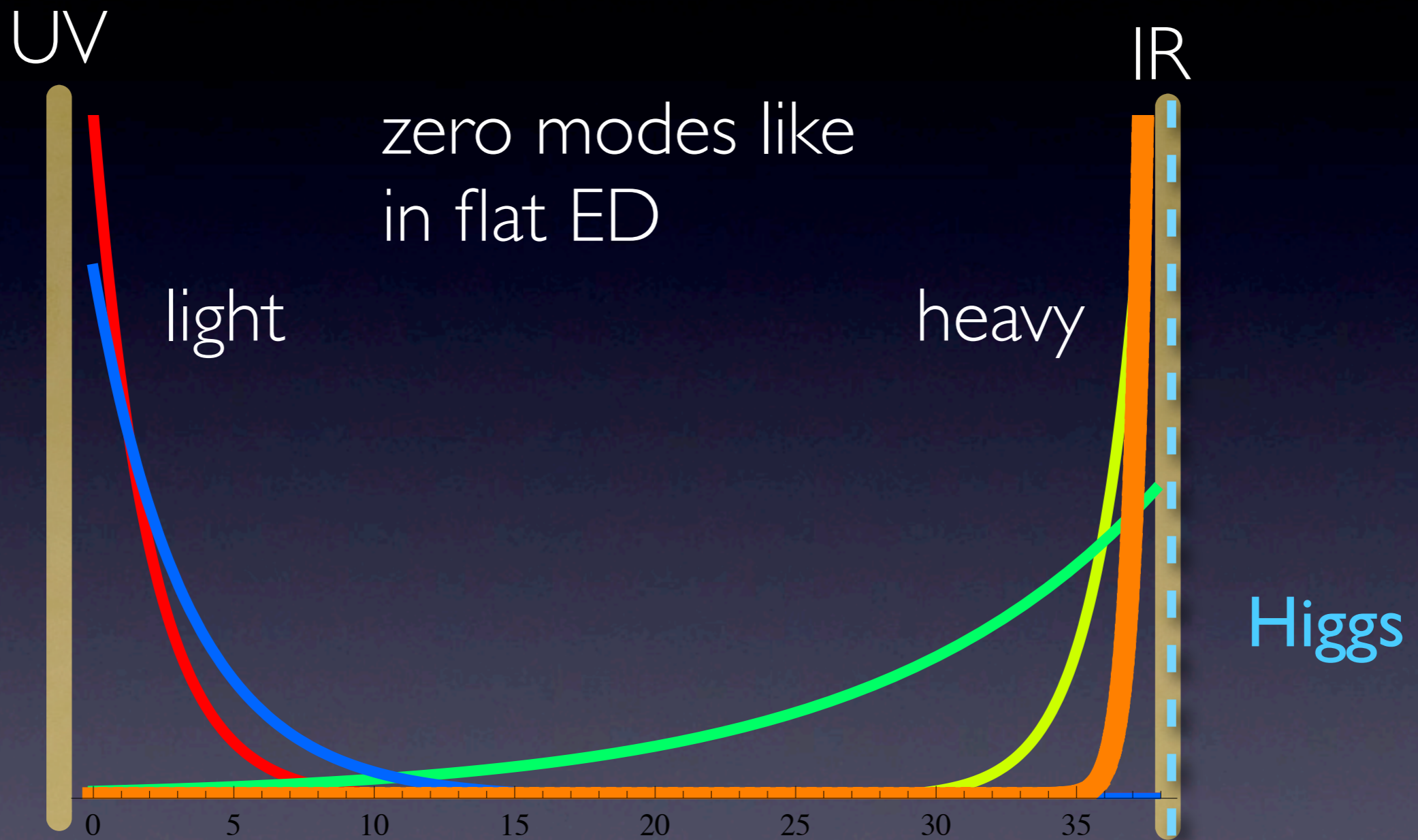
$$m_W = \sqrt{\frac{g(IR)}{g(UV)}} M_P \ll M_P$$

$$m_W \sim e^{-4\pi/\alpha} M_P$$



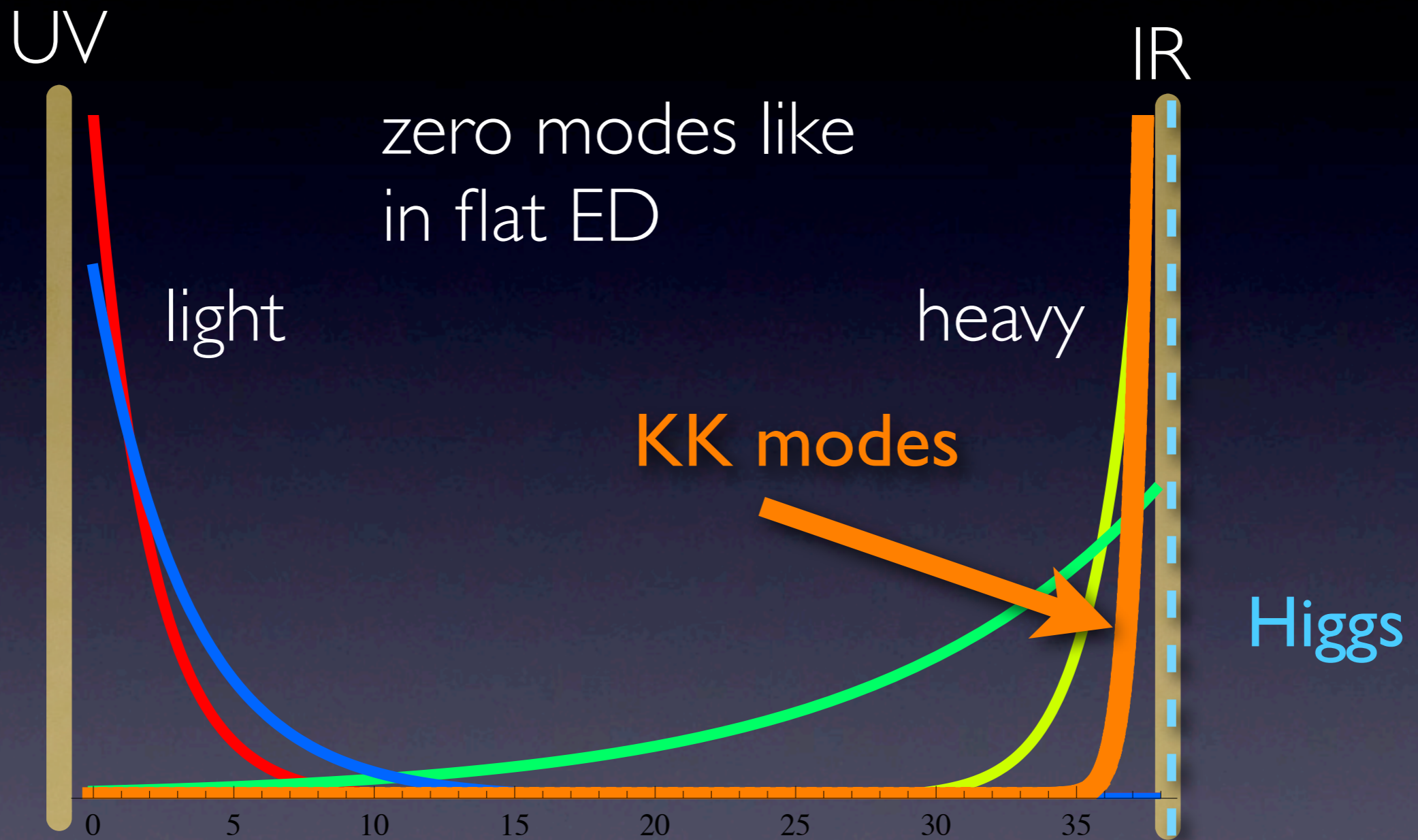
# Flavor in RS

Grossman, Neubert; Gherghetta, Pomarol; Huber;



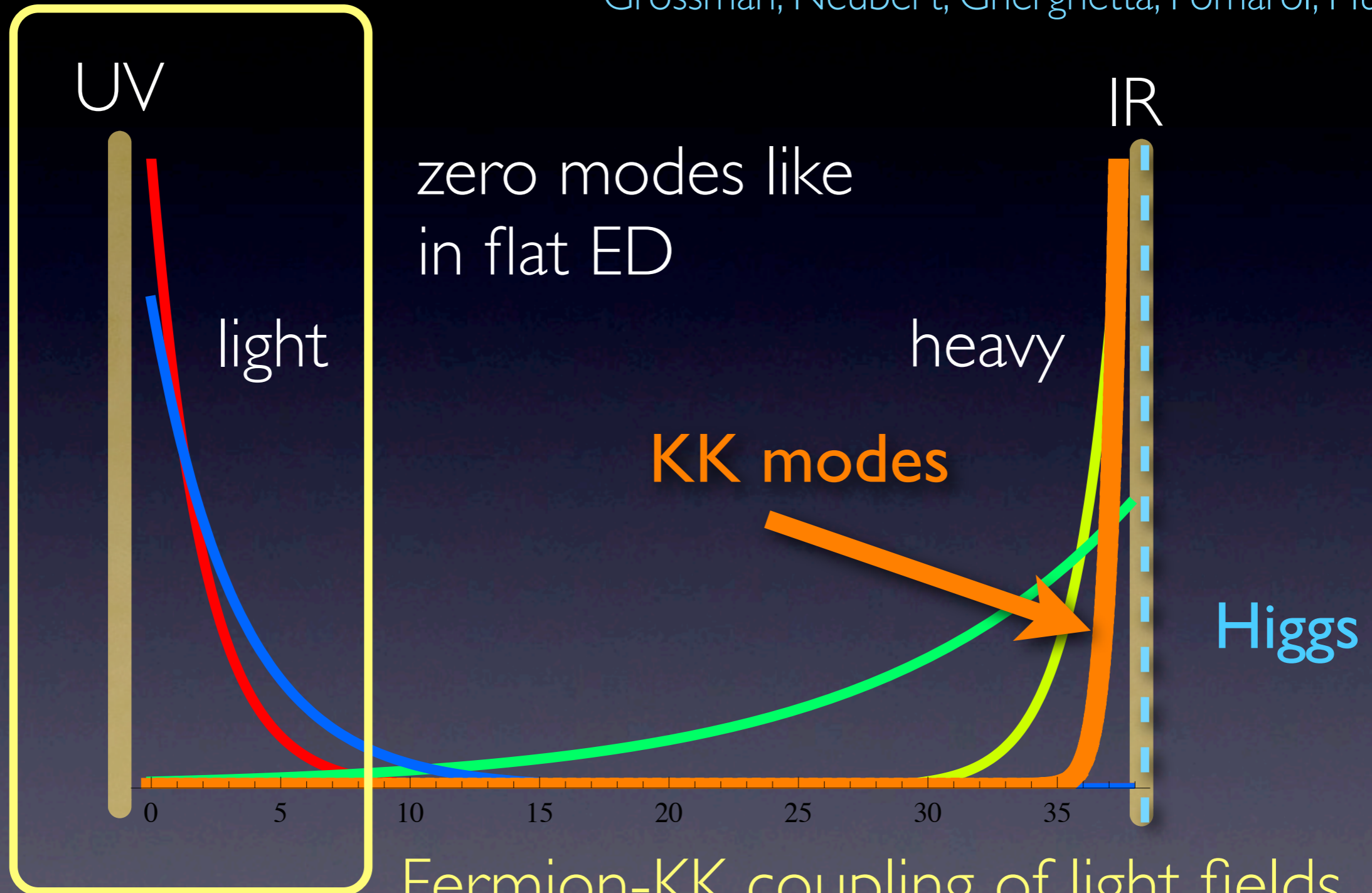
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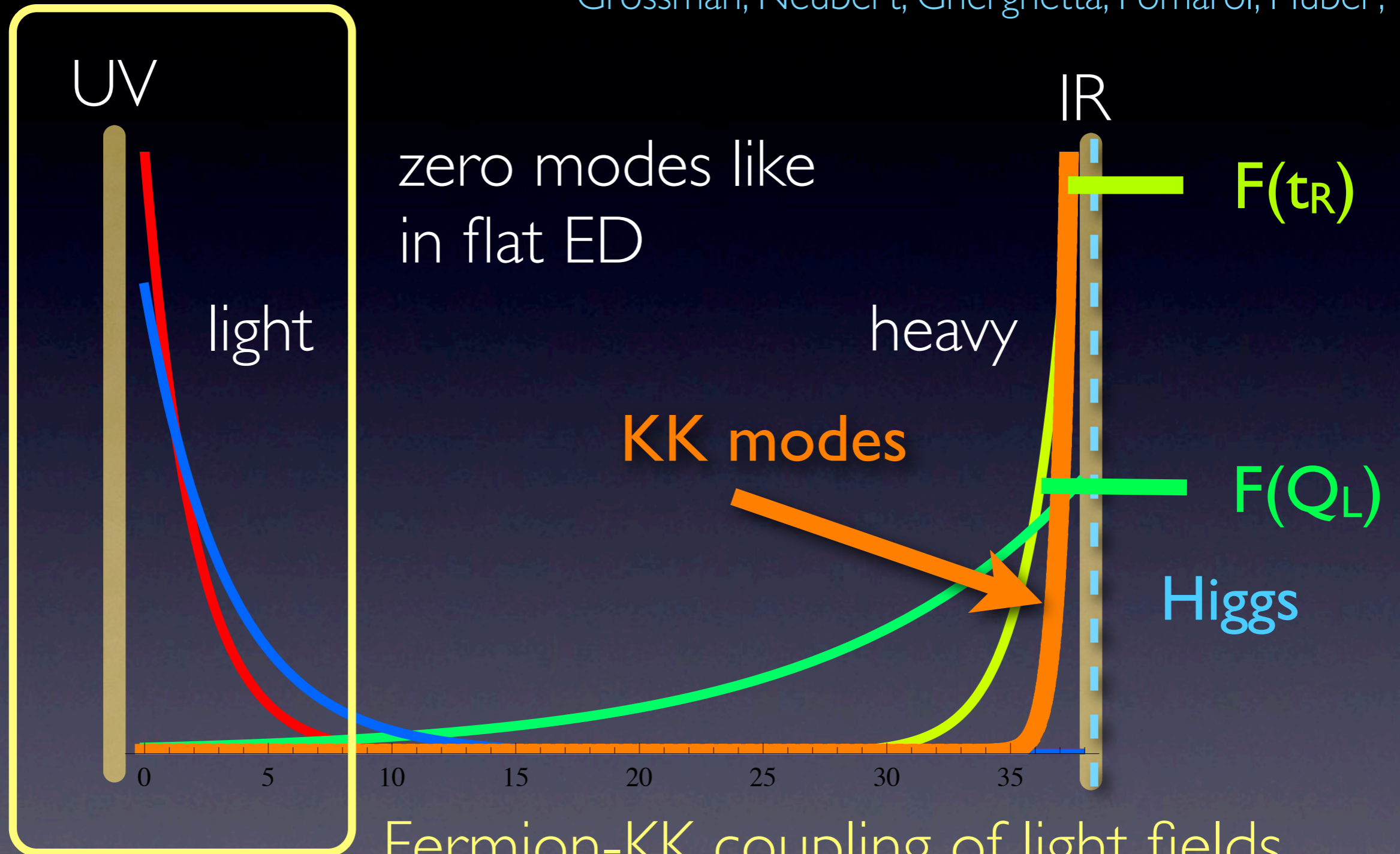


Fermion-KK coupling of light fields almost universal!



# Flavor in RS

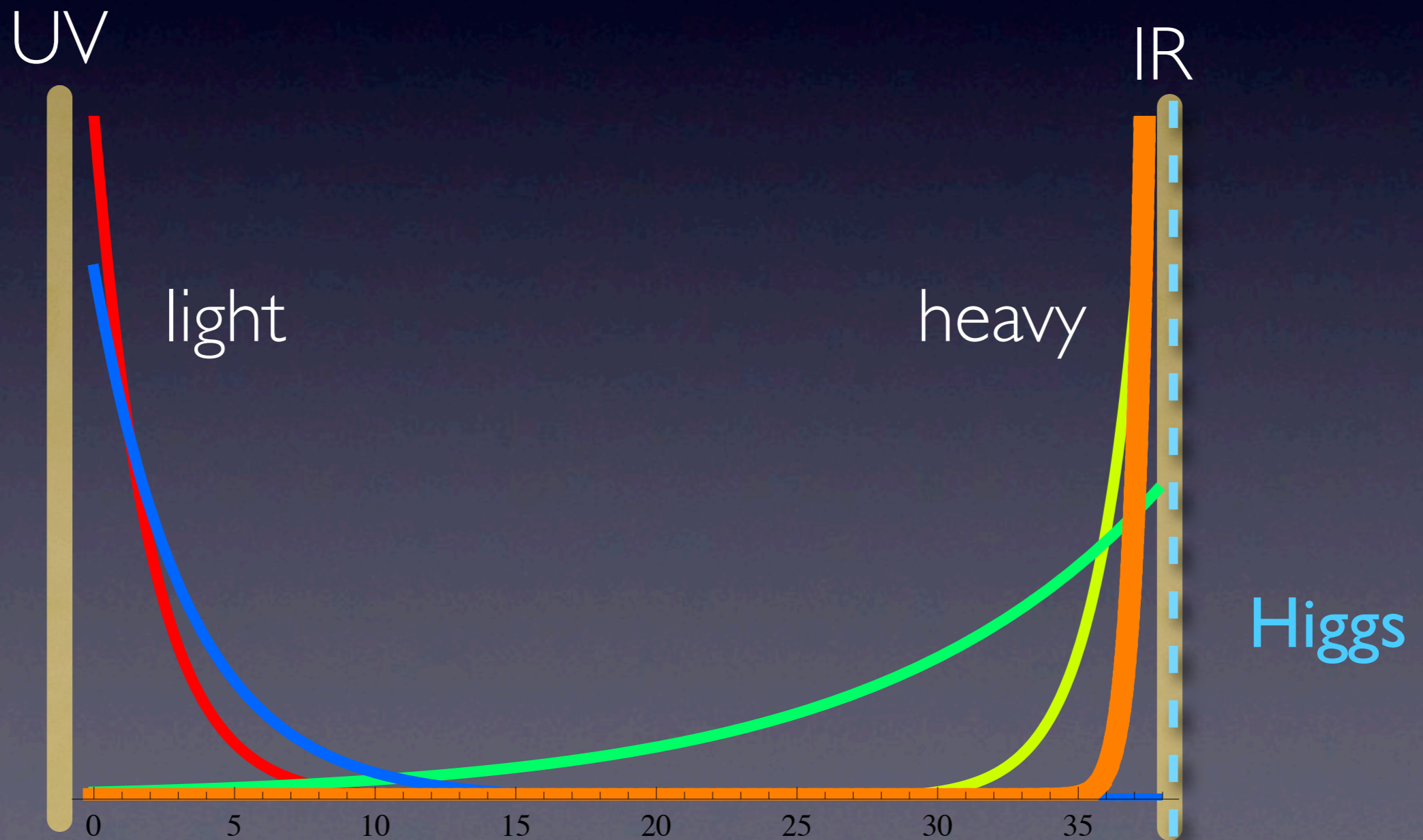
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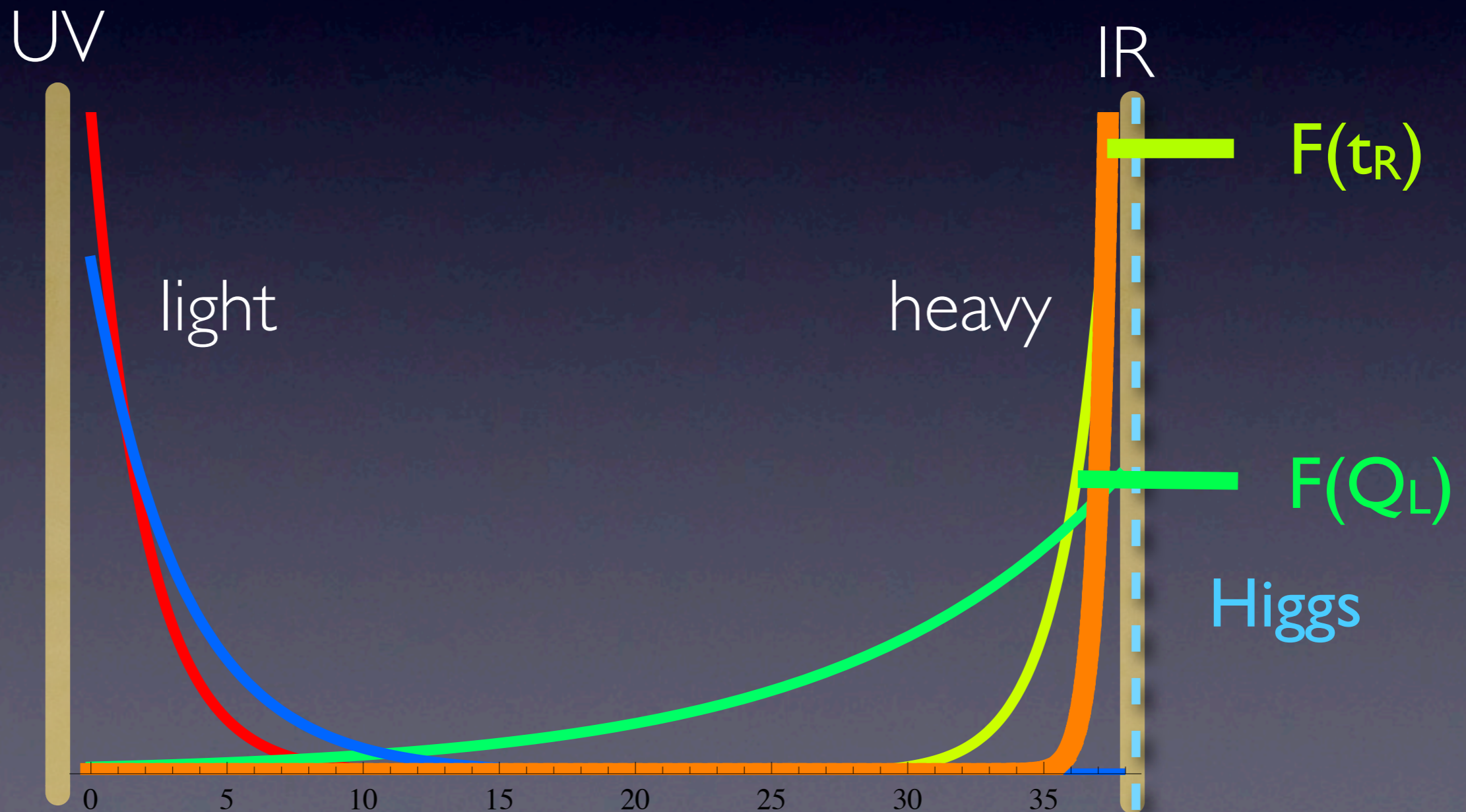
# Fermion zero mode on the IR brane

$$F(c) \sim \begin{cases} (\text{TeV/Planck})^{c-\frac{1}{2}} & c > 1/2 \\ \sqrt{1-2c} & c < 1/2 \end{cases}$$



# Fermion zero mode on the IR brane

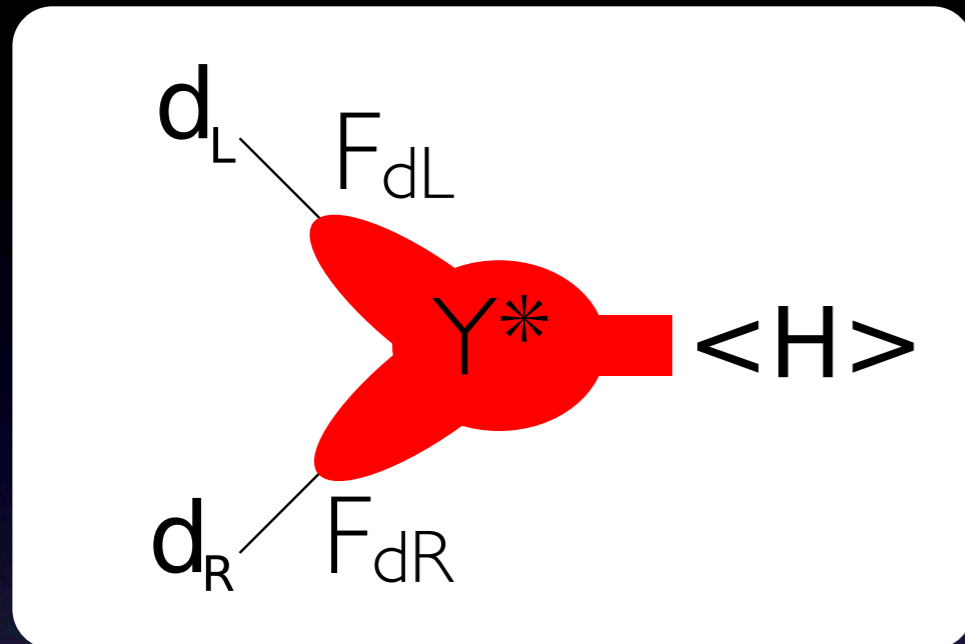
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# RS GIM - partial compositeness

Gherghetta, Pomarol; Huber; Agashe, Perez, Soni;

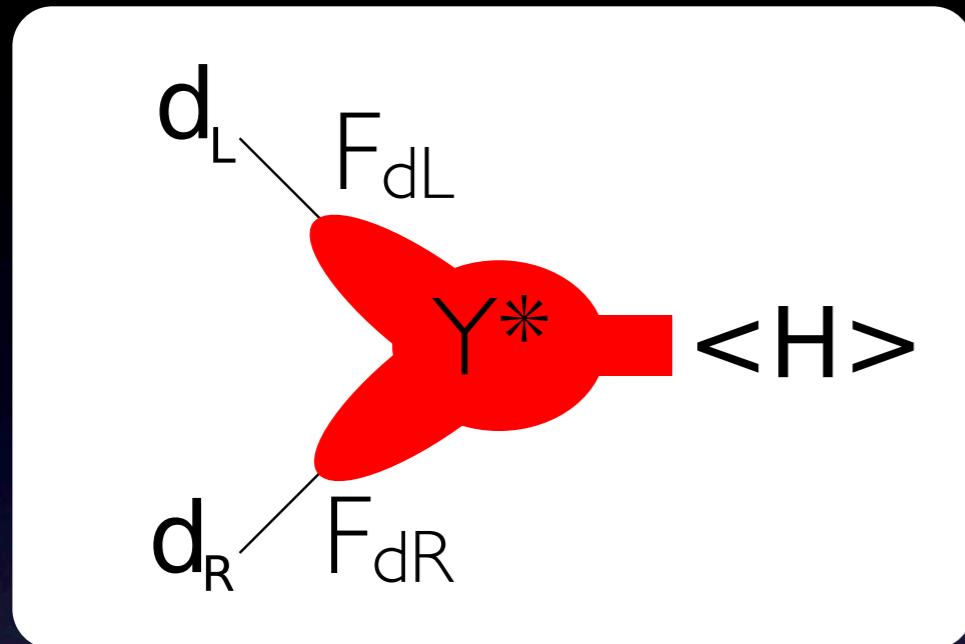


Flavor hierarchy from hierarchy in  $F_i$

$$m_d \sim v F_{d_L} Y^* F_{d_R}$$

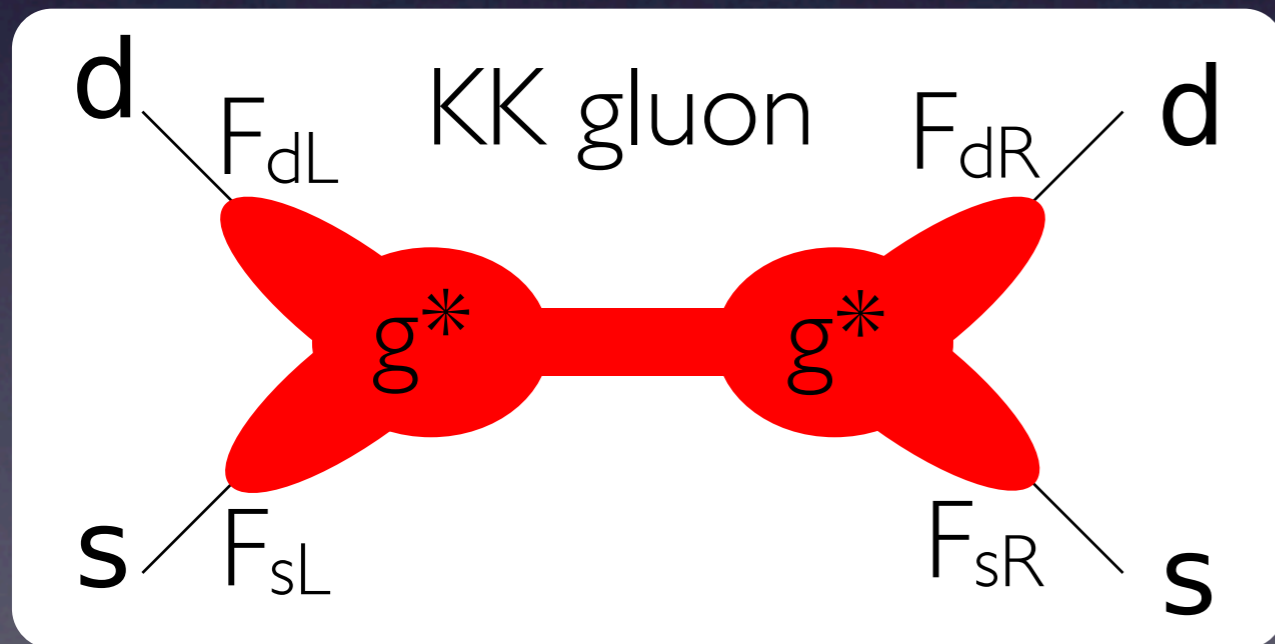
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Flavor hierarchy from hierarchy in  $F_i$

$$m_d \sim v F_{dL} Y^* F_{dR}$$



KK gluon FCNCs proportional to the same small  $F_i$ :

$$\sim \frac{(g^*)^2}{M_{KK}^2} F_{dL} F_{dR} F_{sL} F_{sR}$$

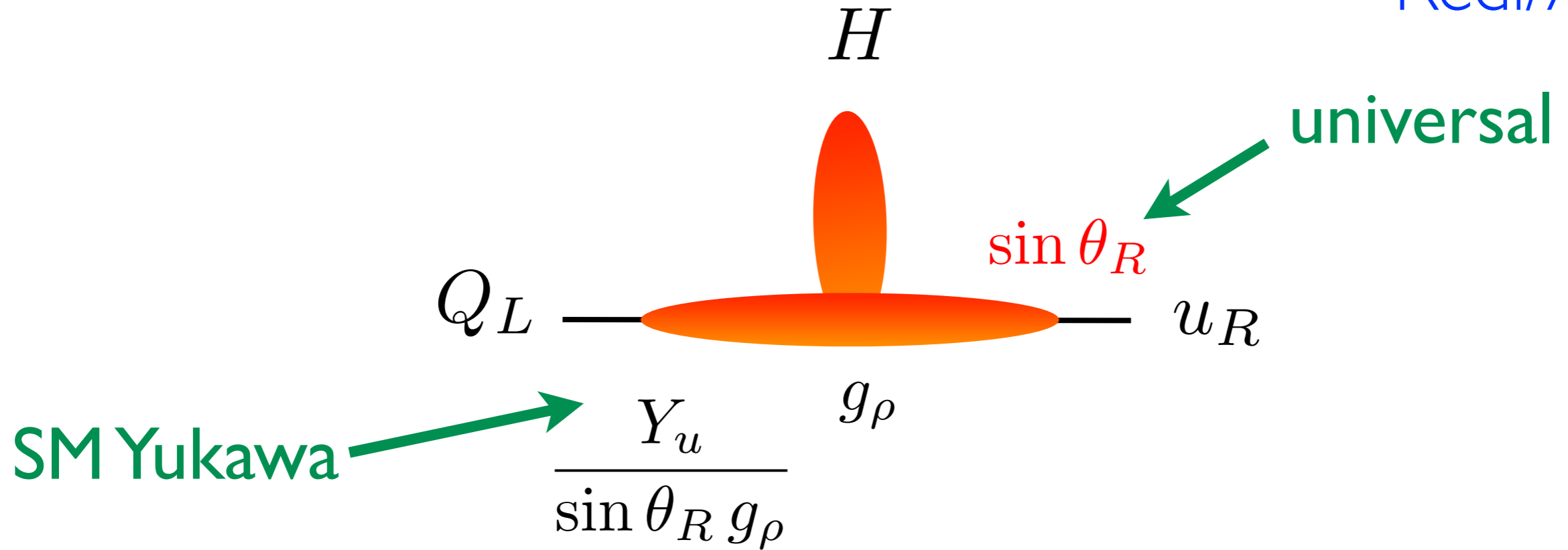
$$\sim \frac{(g^*)^2}{M_{KK}^2} \frac{m_d m_s}{(v Y^*)^2}$$



Back to 4D ...

# A Minimal Flavor Violating Composite Higgs

Redi/AW\*



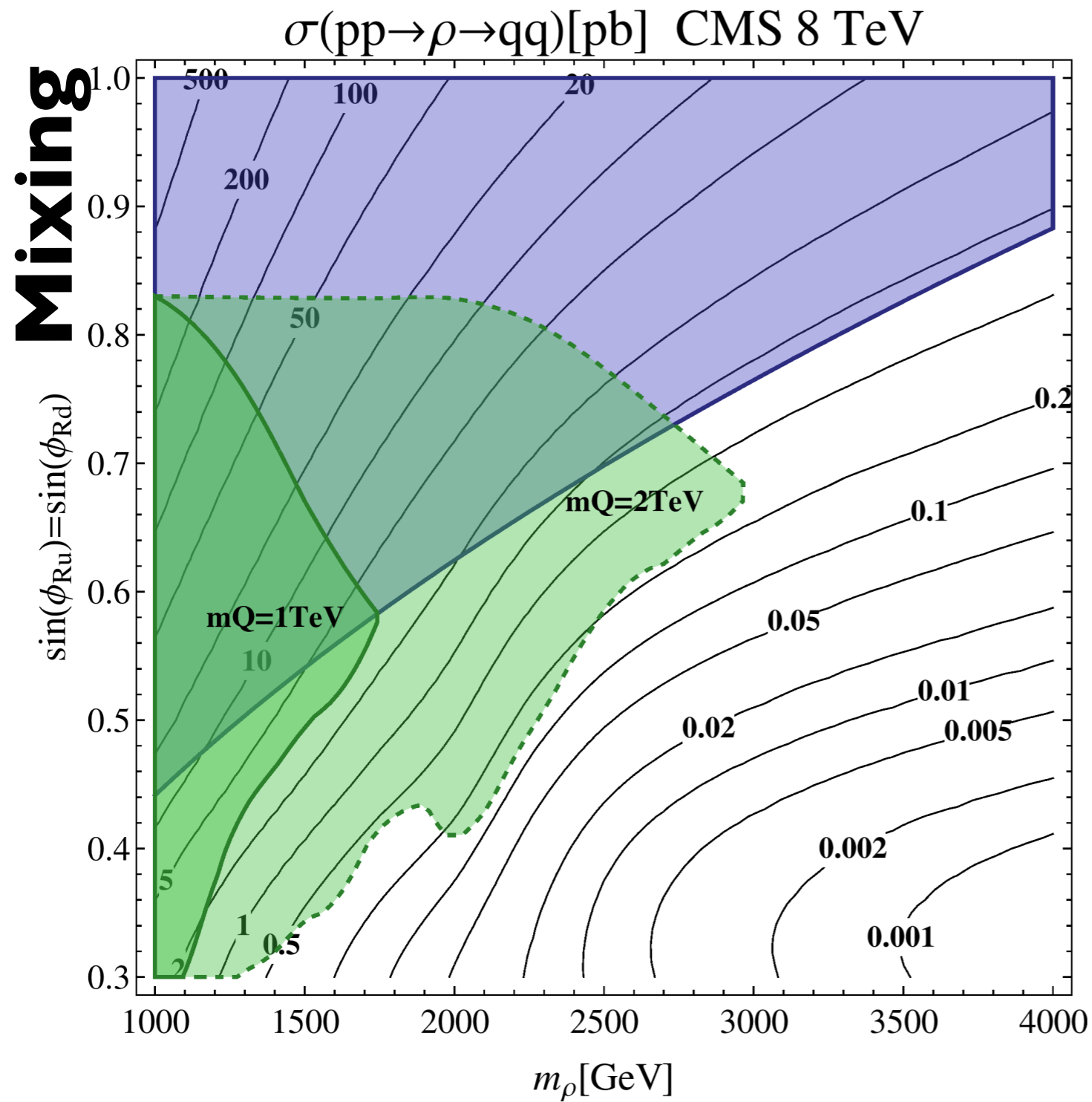
\*for RS realization: Csaki,AW et al; Delaunay et al; da Rold; see also Barbieri et al



# LHC8 limits

...similar plot using ATLAS results

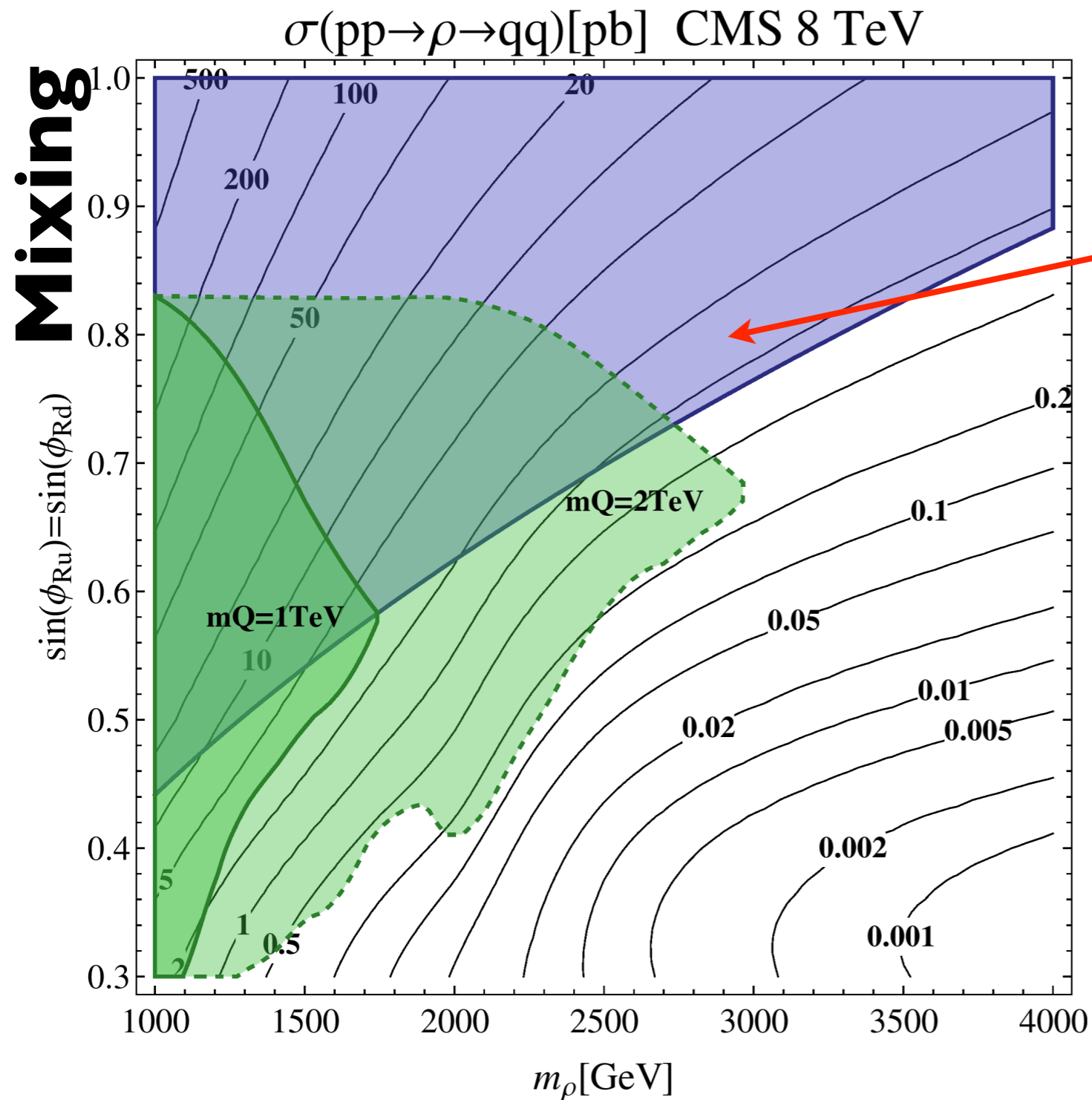
de Vries, Redi, Sanz, AW, 13



# LHC8 limits

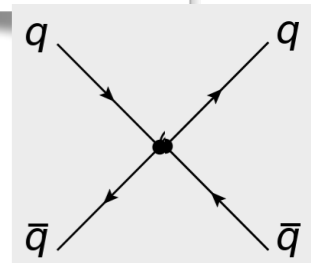
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de Vries, Redi, Sanz, AW, 13



CMS dijet angular searches

$$\mathcal{L} = \frac{2\pi}{\Lambda^2} (\bar{q}_{L,R} \gamma^\mu q_{L,R})^2$$

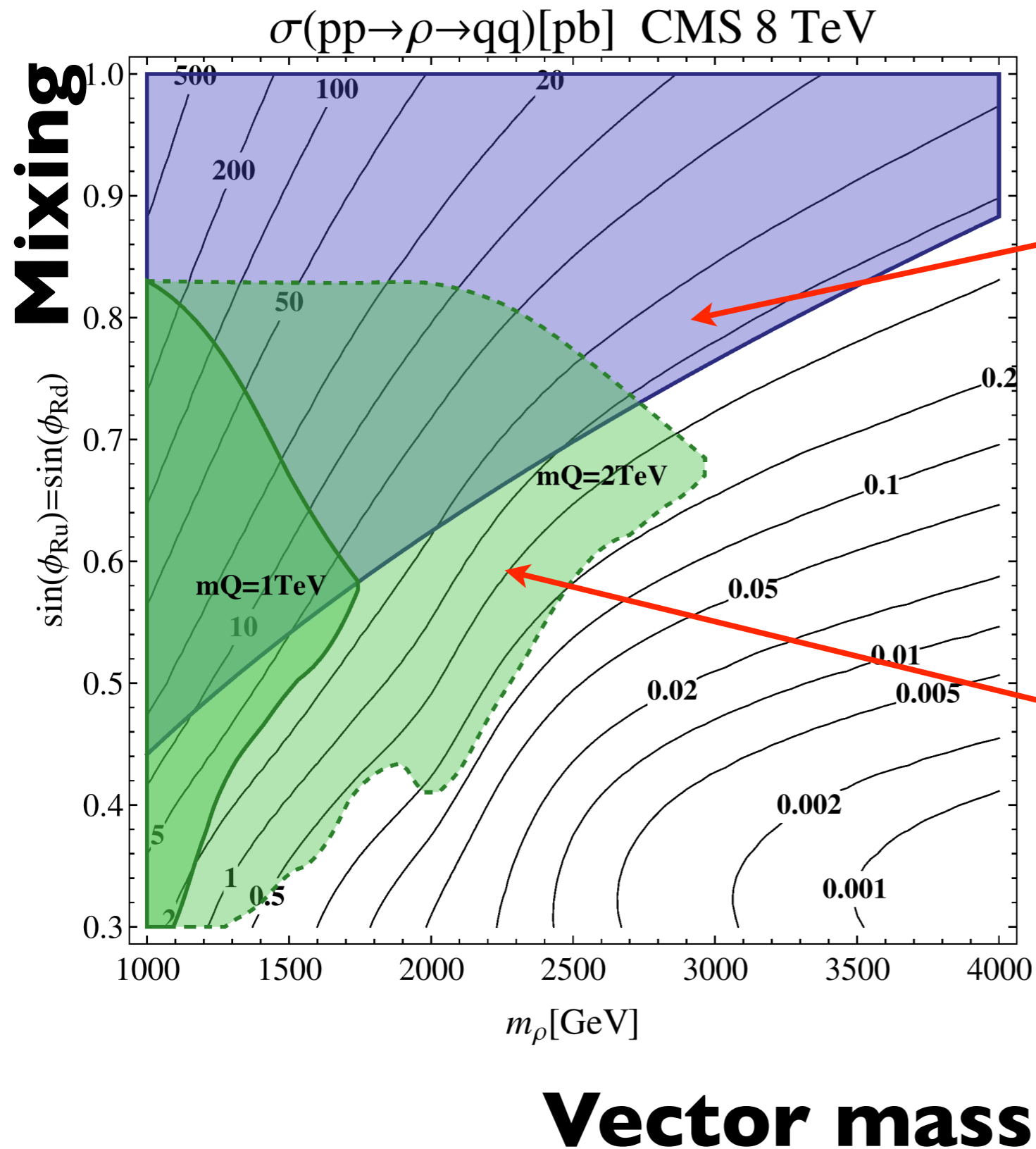


## Vector mass

# LHC8 limits

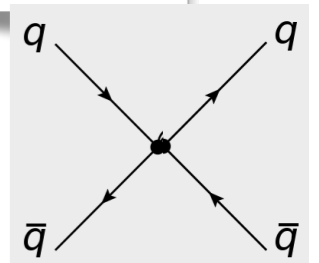
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de Vries, Redi, Sanz, AW, 13

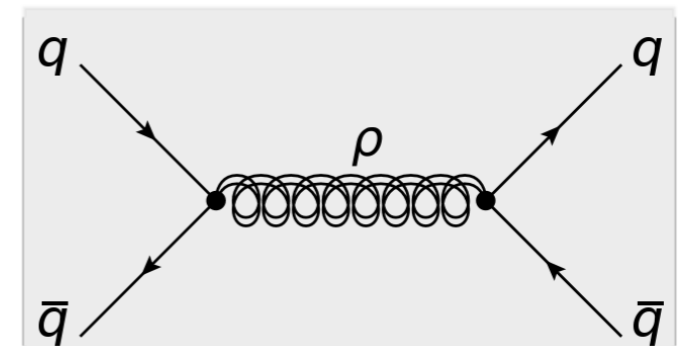


CMS dijet angular searches

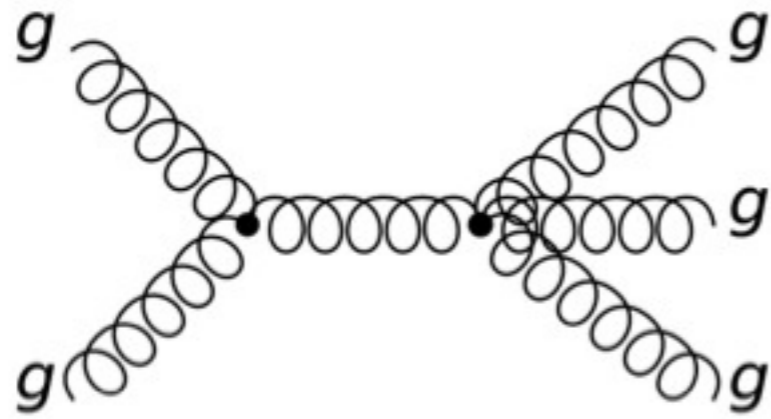
$$\mathcal{L} = \frac{2\pi}{\Lambda^2} (\bar{q}_{L,R} \gamma^\mu q_{L,R})^2$$



Dijet bump search  
CMS

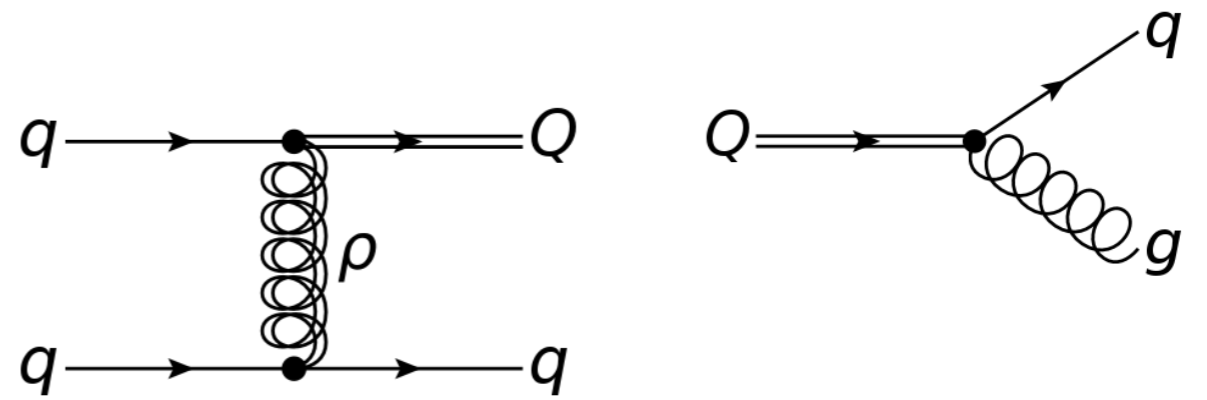






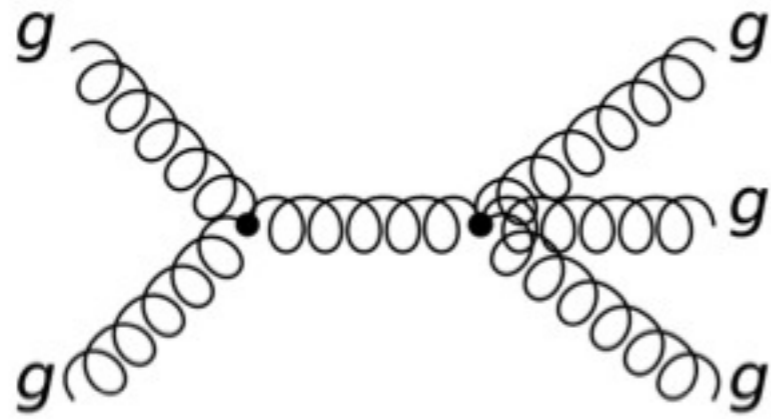
QCD

vs.



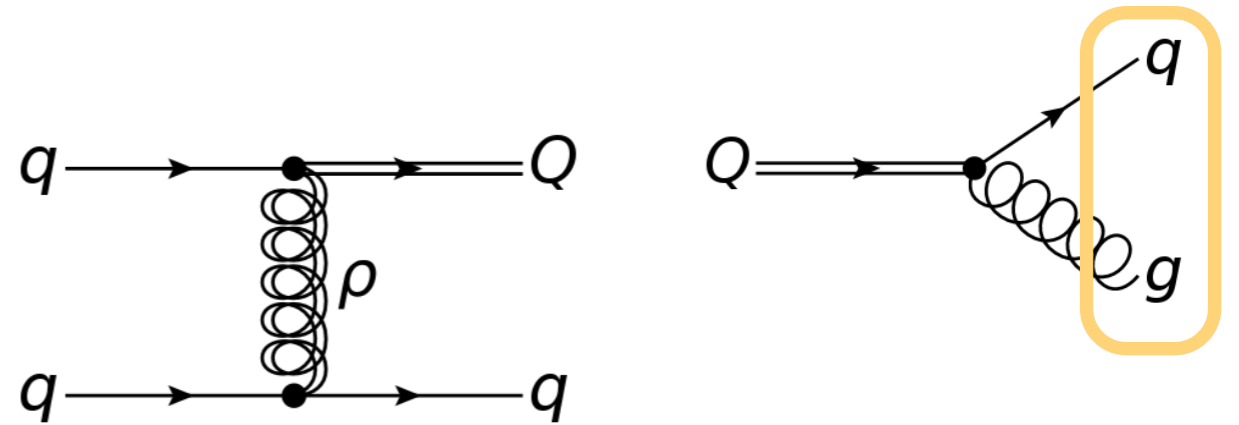
Composite Partners

bump in sub-leading jets



QCD

vs.



Composite Partners

# Dedicated search

deVries, Redi, Sanz, AW, '13

Cut-flow	$m_Q = 600 \text{ GeV}$		$m_Q = 1200 \text{ GeV}$	
	signal	QCD	signal	QCD
$p_T \text{ leading jet} > 450 \text{ GeV}$	0.51	0.0067	0.90	0.0067
$H_T > m_Q$	0.51	0.0067	0.80	0.0015
$ m_{jj} - m_Q  < (30, 50) \text{ GeV}$	0.15	0.00037	0.11	$2.5 \times 10^{-5}$
$\Delta\phi_{jj} > 1.5$	0.045	$9.9 \times 10^{-5}$	0.060	$2.1 \times 10^{-7}$

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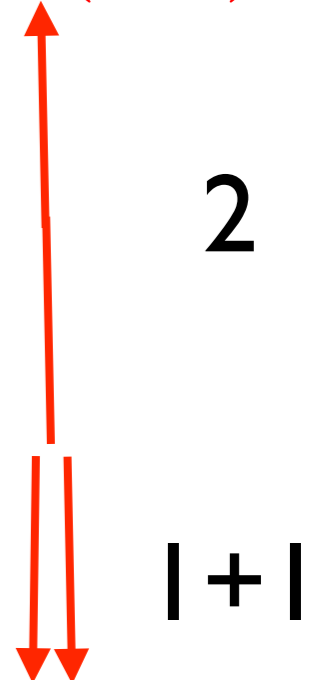
QCD prefers mercedes

$$M \sim 3(p_T)_{\min}$$



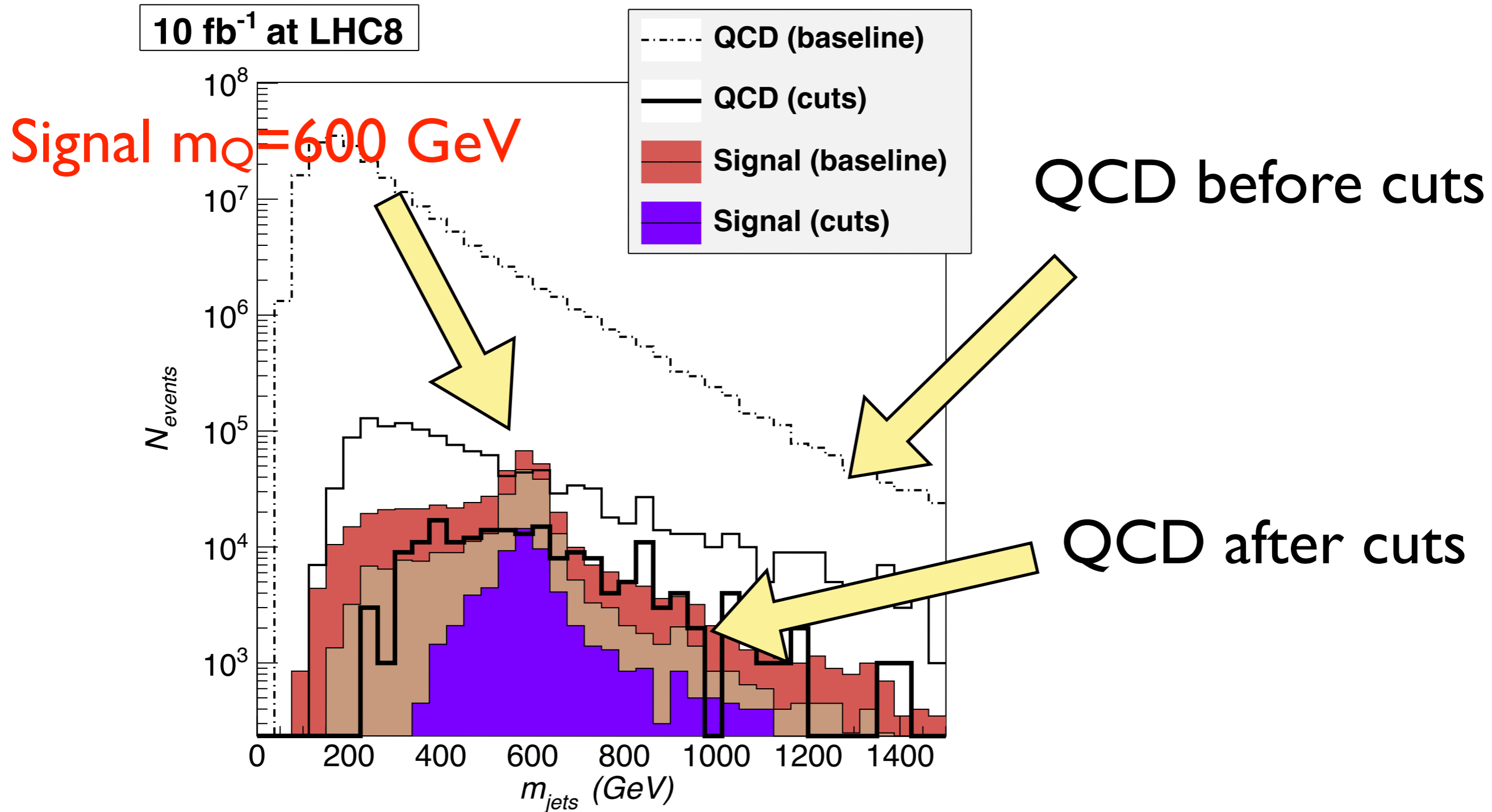
vs

$$M \sim 4(p_T)_{\min}$$



# Discovery potential of a dedicated search

deVries, Redi, Sanz, AW, '13

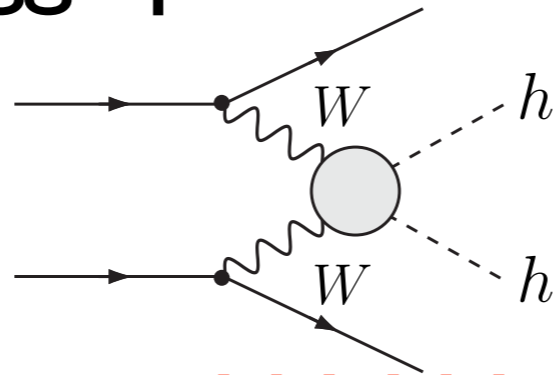


heavier signal easier, 3jet final state  
easier, no optimization



# Composite Higgs

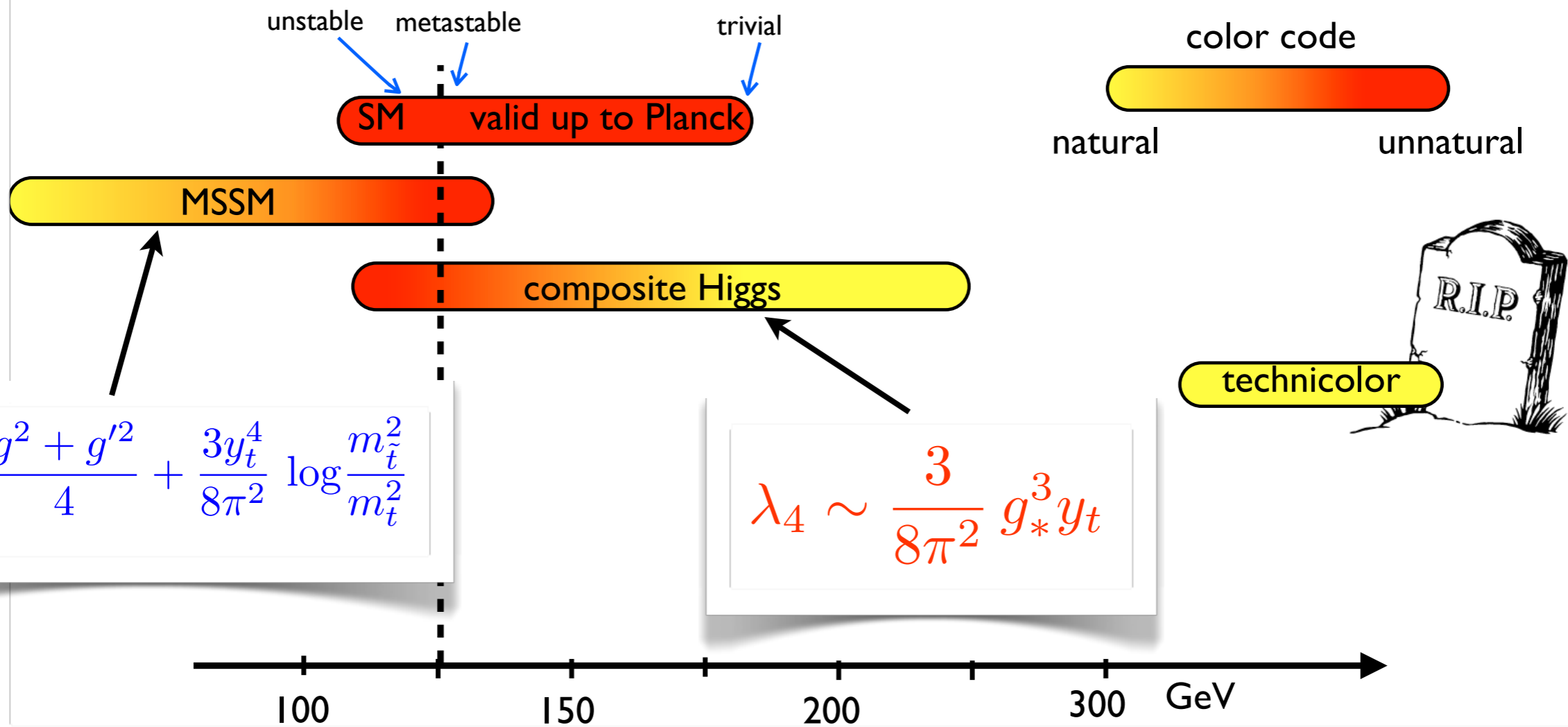
- ‘SM-like’ light Higgs
- Correlated deviations in Higgs couplings, e.g.  $g_{hVV} = g_{hVV}^{(\text{SM})} \cos \theta$  ( $V = W, Z$ )
- Double Higgs production smoking gun



- Keep an eye on  $W_L W_L \rightarrow W_L W_L$
- Top partners ( $Q = 5/3, 2/3, -1/3$ )

**Conclusion**

# WHAT IS THE MASS TELLING US?



# Conclusions

The battle for a natural resolution of the hierarchy problem goes on

Where is everybody?

LHC<sub>14</sub> will be decisive

