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## Measurements of $R_{\rm b}$ in e<sup>+</sup>e<sup>-</sup> Collisions at $182 - 209 \,\,{\rm GeV}$

The OPAL Collaboration

#### Abstract

Measurements of  $R_{\rm b}$ , the ratio of the bb cross-section to the q $\overline{\rm q}$  cross-section in e<sup>+</sup>e<sup>-</sup> collisions, are presented. The data were collected by the OPAL experiment at LEP at centre-of-mass energies between 182 GeV and 209 GeV. Lepton, lifetime and event-shape information is used to tag events containing b quarks with high efficiency. The data are compatible with the Standard Model expectation. The mean ratio of the eight measurements reported here to the Standard Model prediction is 1.055 ± 0.031 ± 0.037, where the first error is statistical and the second systematic.

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## 1 Introduction

The cross-section for bottom-quark pair production in  $e^+e^-$  annihilation relative to the hadronic cross-section,

$$R_{\rm b} \equiv \frac{\sigma({\rm e}^+{\rm e}^- \to \gamma/{\rm Z} \to {\rm b}\overline{\rm b})}{\sigma({\rm e}^+{\rm e}^- \to \gamma/{\rm Z} \to {\rm q}\overline{\rm q})},$$

is a sensitive probe of the Standard Model [1]. Measurements of  $R_{\rm b}$  have been made at the Z peak and at higher energies [2]. At the Z resonance, where fermion-pair production is dominated by Z decays, measurements of  $R_{\rm b}$  provide a precise determination of the ratio of the Z  $\rightarrow$  bb partial width to the hadronic width<sup>1</sup>  $R_{\rm b}^0 = \Gamma_{\rm bb}/\Gamma_{\rm had}$ . This quantity is of particular interest because of its unique sensitivity to electroweak radiative corrections; while sensitive to the top-quark mass, its dependence on other parameters, for example the Higgs boson mass and the strong coupling constant, is negligible [2]. Above the Z peak, the pure Z cross-section decreases and the contributions of photon exchange and  $\gamma$ -Z interference become important. Possible new physics at a high energy scale might manifest itself as a deviation from the Standard Model prediction.

In this paper, measurements of  $R_{\rm b}$  at energies above the Z resonance are presented. The data were taken by the OPAL detector at the LEP e<sup>+</sup>e<sup>-</sup> collider, at centre-of-mass energies,  $\sqrt{s}$ , ranging from 182 GeV to 209 GeV, during the LEP2 programme.

Above the Z peak a significant fraction of the observed fermion-pair events comes from radiative return to the Z through initial-state photon radiation. Only non-radiative events are considered here, according to the definition used by OPAL in the analysis of fermion-pair production at LEP2 [3]:

• An effective centre-of-mass energy  $\sqrt{s'} > 0.85\sqrt{s}$ , where s' is defined as the square of the mass of the  $\gamma/Z$  propagator.

 $<sup>{}^{1}</sup>R_{\rm b}^{0}$  is the partial width ratio for Z decays and not the cross-section ratio measured in this paper. It is smaller than the cross-section ratio at the peak of the Z resonance by 0.0002.

• The predicted contribution of interference between initial- and final-state photon radiation is removed.

At high energies, additional background sources also arise, mainly from  $W^+W^-$  and ZZ decaying to four-fermion final states.

Because of the limited statistics due to the low cross-section at LEP2, the double-tag technique as used at the Z resonance [4] is not optimal. Instead the measurement reported here relies on a single-tag method, and uses a sophisticated tagging algorithm based on lepton, lifetime and event-shape information to identify bb events. This algorithm is more efficient and has a higher purity than the one used in our previous measurement [5], where  $R_{\rm b}$  was measured up to 189 GeV. Hence the 183 GeV and 189 GeV results reported here supersede the previous values, while the measurements at higher energy are reported here by OPAL for the first time.

## 2 The OPAL detector, data sample and simulation

A detailed description of the OPAL detector can be found elsewhere [6]. For this analysis, the most relevant parts of the detector are the silicon micro-vertex detector, the tracking chambers, the electromagnetic and hadronic calorimeters, and the muon chambers. The micro-vertex detector is essential for the reconstruction of secondary vertices. The central detector provides precise measurements of the momenta of charged particles from the curvature of their trajectories in a magnetic field of 0.435 T. In addition, it allows the identification of charged particles through a combination of the measurement of the specific energy loss dE/dx and the momentum. The electromagnetic calorimeter consists of 11704 lead glass blocks, which completely cover the azimuthal<sup>2</sup> range up to polar angles of  $|\cos \theta| < 0.98$ . Almost the entire detector is surrounded with four layers of muon chambers, after approximately one metre of iron from the magnet return yoke, which is instrumented as a hadron calorimeter. Luminosity is determined using small-angle Bhabha scattering in the forward calorimeter [3].

## 2.1 Data sample

The data used in this analysis were collected by the OPAL detector at LEP during 1997-2000, at centre-of-mass energies between 182 GeV and 209 GeV. They are grouped into eight energy points. The centre-of-mass energies and integrated luminosities of the data samples are summarized in Table 1.

<sup>&</sup>lt;sup>2</sup>The OPAL coordinate system is defined as a right-handed Cartesian coordinate system, with the x axis pointing in the plane of the LEP collider toward the centre of the ring, the z axis in the direction of the electron beam, and  $\theta$  and  $\phi$  defined as the usual spherical polar coordinates.

Nominal Energy	Energy Range (GeV)	$\langle \sqrt{s} \rangle \; (\text{GeV})$	Integrated Luminosity $(pb^{-1})$
183	181.7 - 184.0	182.7	56
189	188.5 - 189.1	188.6	185
192	191.4 - 191.7	191.6	29
196	195.4 - 195.8	195.5	77
200	199.3 - 199.9	199.5	78
202	201.5 - 202.0	201.6	36
205	204.5 - 205.5	205.3	74
207	205.5 - 208.6	206.8	137

Table 1: The nominal energy, energy range, luminosity-weighted mean centre-of-mass energy and integrated luminosity of the data used in the analysis.

## 2.2 Simulation

Monte Carlo (MC) simulation is used to estimate the selection efficiency for  $b\overline{b}$  events and to evaluate backgrounds. MC samples are generated at the nominal centre-of-mass energies given in Table 1. The KK2F program [7] is used to simulate  $e^+e^- \rightarrow q\overline{q}(\gamma)$  events. Four-fermion background events are simulated with the grc4f generator [8] or with the KORALW [9] program with the grc4f matrix elements. The hadronization is performed by the PYTHIA 6.150 [10] string model, and heavy quark fragmentation is modelled according to the Peterson fragmentation scheme [11] with parameters tuned according to [12]. All the MC samples are passed through a detailed simulation of the OPAL detector [13].

The Standard Model cross-section predictions are calculated using ZFITTER 6.36 [14]. ZFITTER is used to calculate the Standard Model value of  $R_c$ , the ratio of the cross-section for charm-quark pair production to the hadronic cross-section, at which the resulting  $R_b$ is quoted, and to calculate  $R_b$  for comparison of the theoretical predictions with the measured values. ZFITTER is also used for estimating the effects of interference between initial- and final-state photon radiation, as described in Section 3.4.

## 3 Analysis procedure

The measurement of  $R_{\rm b}$  starts by selecting non-radiative hadronic events, applying fiducial cuts and rejecting four-fermion background events. The number of selected events,  $N_{\rm had}$ , is corrected for background and for the efficiency of the selection cuts to yield a corrected number of non-radiative hadronic events,  $N_{\rm q\bar{q}}$ . The background includes the residual four-fermion background and feedthrough of events with lower effective centre-of-mass energy,  $\sqrt{s'}$ . The contribution from interference between initial- and final-state radiation is also removed. A b-tagging algorithm is applied to the selected events, and the number of tagged events,  $N_{\rm tag}$ , is similarly corrected for the same background contributions and interference to obtain  $N_{\rm b\bar{b}}$ , which still contains contributions from cc and light-quark-pair

events.  $R_{\rm b}$  is then calculated using:

$$R_{\rm b} = \frac{N_{\rm b\overline{b}}/N_{\rm q\overline{q}} - \epsilon_{\rm c}R_{\rm c} - (1 - R_{\rm c})\epsilon_{\rm uds}}{\epsilon_{\rm b} - \epsilon_{\rm uds}},\tag{1}$$

where  $\epsilon_{b,c,uds}$  are the efficiencies for non-radiative  $b\overline{b}$ ,  $c\overline{c}$  and light-quark-pair events to pass the selection criteria and the b-tagging algorithm.

In the following sections, we describe the selection of high quality non-radiative hadronic events, the rejection of four fermion background (Section 3.1), and the tagging algorithm used to select events originating from  $e^+e^- \rightarrow b\bar{b}$  (Section 3.2). This is followed by the description of the residual background estimation (Section 3.3). The correction for interference is discussed in Section 3.4, and finally the calculation of  $R_b$  is presented (Section 3.5). The systematic uncertainties are described in Section 4, and the final results and conclusion are given in Section 5.

#### 3.1 Hadronic event selection

Hadronic events,  $e^+e^- \rightarrow \gamma/Z \rightarrow q\overline{q}$ , are selected based on the number of reconstructed charged particle tracks and the energy deposited in the calorimeters [15]. Further requirements follow, demanding at least seven tracks and that the polar angle of the thrust axis,  $\theta_{thr}$ , satisfy  $|\cos \theta_{thr}| < 0.9$ ; the thrust axis is calculated from all tracks and clusters and corrected for double-counting as in [16]. The effective centre-of-mass energy,  $\sqrt{s'}$ , of the  $e^+e^-$  collision is estimated as described in Ref. [3], and non-radiative hadronic events are selected if  $\sqrt{s'/s} > 0.85$ . For the centre-of-mass energies analysed in this paper, the production cross-section of W<sup>+</sup>W<sup>-</sup> events is comparable to that of non-radiative  $q\overline{q}$  events. The production cross-section of ZZ events is about an order of magnitude smaller. Using the same techniques as in [17], events are rejected if they are identified as W<sup>+</sup>W<sup>-</sup> events.

The number of events at each energy selected by the above cuts  $(N_{had})$  is given in Table 2. Typical efficiencies, including the  $\approx 90\%$  efficiency of the  $\cos \theta_{thr}$  cut, are 77% for bb and 80% for lighter (u, d, s and c) qq events. About 14% of the  $N_{had}$  sample are expected to be bb events. The selection of non-radiative events is less efficient for bb final states than for other flavours because of the generally larger missing energy due to the neutrinos in semileptonic b and c hadron decays. The remaining four-fermion background is estimated to be about 6% of the selected hadronic events.

## 3.2 b-tagging

In  $e^+e^- \rightarrow \gamma/Z \rightarrow b\overline{b}$  events, the quark and the anti-quark are typically boosted in opposite directions, and the subsequent hadronization is largely independent. In this analysis, each event is divided into two hemispheres defined by a plane that is orthogonal to the thrust direction.

We use a hemisphere-based b-tagger designed for LEP2 Higgs searches [18], where the tagging of  $b\overline{b}$  events is based on three nearly independent properties of the b-hadron and

its decay products: a lepton from a semileptonic b-hadron decay, the long lifetime, and kinematic differences between b-hadron decays and fragmentation in  $u\bar{u}$ ,  $d\bar{d}$ ,  $s\bar{s}$  events, due to the hard fragmentation of the b-hadron and the high multiplicity of its decay products.

For the lepton tag, semileptonic b-hadron decays are identified from their resultant electron or muon and the lepton momentum is used as the b-tag variable. Electrons are identified using an artificial neural network (ANN) [4] while muons are identified using information from the muon chambers in association with the tracking chambers, as in [19]. Electrons from photon conversions are rejected using an additional ANN described in [20].

For the lifetime tag, secondary vertices are reconstructed. Variables based on the vertex significance (the distance between the reconstructed primary and secondary vertices divided by the corresponding uncertainty) and the impact parameters of the tracks associated with the vertex are combined using an ANN scheme as in [18].

For the kinematic tag, three variables are combined using another ANN: the number of detected particles in the central part of the hemisphere, the angle between the hemisphere axis and its boosted sphericity axis, and the C parameter [21], the latter two being calculated in the rest frame of all the particles associated with the hemisphere.

In each hemisphere, the output of the lepton tag, the lifetime ANN and the kinematic ANN are combined with an unbinned likelihood calculation [22], and the likelihoods  $\mathcal{L}_{\text{hemi1}}^{\text{b}}, \mathcal{L}_{\text{hemi1}}^{\text{c}}, \mathcal{L}_{\text{hemi2}}^{\text{cd}}, \mathcal{L}_{\text{hemi2}}^{\text{cd}}, \mathcal{L}_{\text{hemi2}}^{\text{cd}}$  are obtained. The likelihood  $\mathcal{L}_{\text{hemi1}}^{\text{b}}$  is the probability for the first hemisphere to contain a b quark.  $\mathcal{L}_{\text{hemi2}}^{\text{b}}$  is the same probability for the second hemisphere, and  $\mathcal{L}_{\text{hemi1}(2)}^{\text{c(uds)}}$  are the corresponding probabilities for c-quark (light quarks). The two hemispheres' outputs are then combined into a single event b-tagging likelihood variable  $\mathcal{L}_{\text{event}}$ , using

$$\mathcal{L}_{\text{event}} = \frac{r_{\text{b}} \ \mathcal{L}_{\text{hemi1}}^{\text{b}} \mathcal{L}_{\text{hemi2}}^{\text{b}}}{r_{\text{b}} \ \mathcal{L}_{\text{hemi1}}^{\text{b}} \mathcal{L}_{\text{hemi2}}^{\text{b}} + r_{\text{c}} \ \mathcal{L}_{\text{hemi1}}^{\text{c}} \mathcal{L}_{\text{hemi2}}^{\text{c}} + r_{\text{uds}} \ \mathcal{L}_{\text{hemi1}}^{\text{uds}} \mathcal{L}_{\text{hemi2}}^{\text{uds}}}.$$

The normalization parameters are set to  $r_{\rm b} = 0.165$ ,  $r_{\rm c} = 0.253$  and  $r_{\rm uds} = 0.582$ , which are the ZFITTER theoretical predictions for  $R_{\rm b}$ ,  $R_{\rm c}$  and  $R_{\rm uds}$  at about 190 GeV. The same values are used for all data sets. The number of events,  $N_{\rm tag}$ , satisfying a b-tagging cut of  $\mathcal{L}_{\rm event} > 0.3$  is determined; this cut value minimizes the total uncertainty in the measurement of  $R_{\rm b}$ . Typical efficiencies for the b-tagger in the hadronic event sample are 65%, 6.3% and 1.5% for  $b\overline{b}, c\overline{c}$  and light-quark pair events respectively; for the residual four-fermion events the tagging efficiency is about 5%. On average, 77% of the tagged sample is expected to be  $b\overline{b}$  events. The distribution of  $\mathcal{L}_{\rm event}$  for the 182–209 GeV data is shown in Figure 1, together with the expectation from the Monte Carlo. Good agreement between the data and the Monte Carlo is observed.

#### **3.3** Background estimation

The residual four-fermion background is estimated from Monte Carlo simulation and subtracted from the number of selected hadronic  $(N_{had})$  and b-tagged  $(N_{tag})$  events. It is 6.5% for the hadronic event sample and 2.5% for the b-tagged sample. The dominant

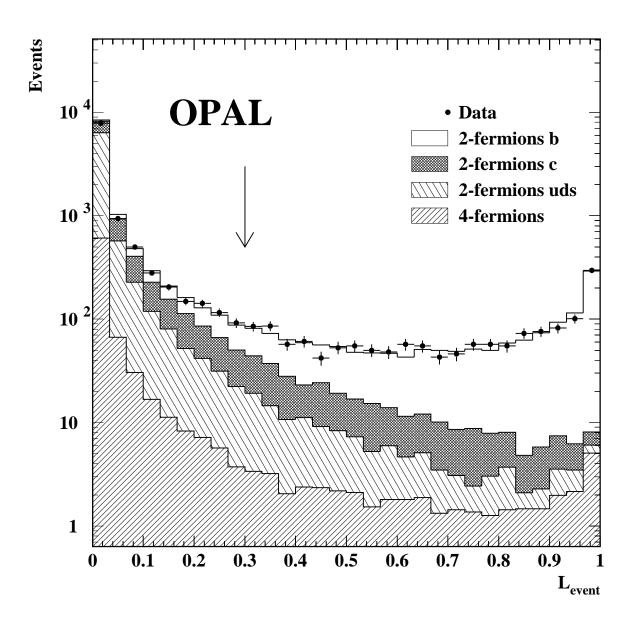


Figure 1:  $\mathcal{L}_{\text{event}}$  distributions for selected non-radiative hadronic events. The points represent the data (182–209 GeV) and the histogram represents the Monte Carlo prediction, normalized according to the integrated luminosity of the data, with the open area representing the expected  $b\overline{b}$  content and the hatched areas representing the contributions from  $c\overline{c}$  light-quark pair and four-fermion events. The arrow indicates the cut used.

contribution to the four-fermion background originates from  $W^+W^-$  and ZZ final states, with only 5% coming from non- $W^+W^-$  and non-ZZ events.

Backgrounds from two-photon collisions and  $e^+e^- \rightarrow \tau^+\tau^-$  events were found to be negligible. The selected event sample has a small contamination from radiative hadronic events where  $\sqrt{s'/s}$  was overestimated. This contamination is estimated using Monte Carlo simulation and subtracted from  $N_{had}$  and  $N_{tag}$  when calculating  $N_{q\bar{q}}$  and  $N_{b\bar{b}}$ . Since both the b-tagged and the hadronic samples include such contamination, the effect on the measured value of  $R_b$  is small. About 3% of the selected hadronic events and 4% of the b-tagged events have a true value of  $\sqrt{s'}$  smaller than  $0.85\sqrt{s}$ .

The contributions from non-radiative  $c\bar{c}$  and light-quark-pair events that are b-tagged are taken into account by the two negative terms in the numerator of equation 1. The secondary production of heavy quarks, commonly referred to as gluon splitting, can also lead to primary light-quark-pair events being selected by the b-tagging algorithm. This contribution is fully accounted for by the efficiencies in equation 1 if the rates of this production in the Monte Carlo are correct. These rates were measured at LEP1 [23–25]. We extrapolate the measured values to the higher energies using theoretical predictions given in [10,26,27]. We obtain production rates per hadronic event,  $g_{c\bar{c}} = 0.064\pm0.010$  and  $g_{b\bar{b}} = 0.0065\pm0.0015$  at  $\sqrt{s} = 200$  GeV where the uncertainties include the uncertainty on the measurements and the variation of the theoretical models used for the extrapolation to higher energy. The default Monte Carlo values are  $g_{c\bar{c}} = 0.032$  and  $g_{b\bar{b}} = 0.0053$ . We correct the value of  $g_{c\bar{c}}$  in the Monte Carlo according to the extrapolated value. Since the Monte Carlo value of  $g_{b\bar{b}}$  agrees with the data we do not correct the Monte Carlo for  $g_{b\bar{b}}$  but take the difference between the Monte Carlo value and the maximal extrapolated rate (0.0053 - 0.0080) as the corresponding systematic uncertainty.

# **3.4** Subtraction of interference between initial- and final-state photon radiation

The interference cross-section is defined as the difference between the cross-section including interference between initial- and final-state photon radiation and the cross-section excluding interference. It is calculated using ZFITTER with the Standard Model value of the forward backward asymmetry, for  $e^+e^- \rightarrow b\overline{b}$ ,  $e^+e^- \rightarrow c\overline{c}$  and  $e^+e^- \rightarrow u\overline{u}$ ,  $d\overline{d}$ ,  $s\overline{s}$ , in bins of  $\cos\theta$  where  $\theta$  is the angle between the fermion direction and the direction of the  $e^$ beam. The interference cross-section can be positive or negative, depending on the value of  $\theta$ . The thrust axis gives a good estimate of the fermion direction, so we assume that the interference correction estimated in bins of  $\cos\theta$  can be applied in bins of  $\cos\theta_{thr}$ . The fractions of b, c and uds events in the hadronic and b-tagged samples are estimated from Monte Carlo samples generated excluding interference. The interference cross-section for each flavour is then weighted according to the estimated flavour composition, and the resulting numbers of events are subtracted from the number of b-tagged events and from the number of  $q\overline{q}$  events to obtain  $N_{b\overline{b}}$  and  $N_{q\overline{q}}$ , which appear in equation 1. These corrections are typically 0.3% for the hadronic sample and -0.5% for the b-tagged sample. The uncertainty on the above procedure is discussed in Section 4.1.3 and given in Table 3.

Data set	$N_{\rm had}$	$N_{\rm tag}$	$N_{\mathbf{q}\overline{\mathbf{q}}}$	$N_{\rm b\overline{b}}$	$\epsilon_{ m b}$	$\epsilon_{ m c}$	$\epsilon_{ m uds}$	$R_{\rm c}^{\rm SM}$	$R_{\rm b} \pm {\rm stat}$
183	1172	185	1199.8	176.1	0.60	0.062	0.012	0.2532	$0.207\pm0.018$
189	3496	447	3561.1	422.7	0.58	0.059	0.012	0.2551	$0.165\pm0.010$
192	573	80	584.7	76.4	0.58	0.064	0.014	0.2560	$0.174 \pm 0.025$
196	1343	182	1370.6	172.7	0.56	0.060	0.014	0.2570	$0.181 \pm 0.017$
200	1312	166	1333.9	157.3	0.58	0.061	0.014	0.2581	$0.164 \pm 0.016$
202	591	72	604.6	68.3	0.56	0.062	0.014	0.2585	$0.154 \pm 0.024$
205	1124	136	1140.6	128.0	0.55	0.061	0.014	0.2592	$0.158 \pm 0.018$
207	2046	251	2078.5	237.5	0.54	0.057	0.014	0.2597	$0.169 \pm 0.014$

Table 2: Number of selected  $(N_{had}, N_{tag})$  and corrected  $(N_{q\bar{q}}, N_{b\bar{b}})$  events; average (over all  $|\cos \theta_{thr}| < 0.9$  bins) selection (including b-tagging) efficiencies; the Standard Model prediction for  $R_c$  and the resulting value of  $R_b$  (with statistical uncertainties only) for the eight energies. Note that  $R_b$  is calculated from the values obtained in bins of  $\cos \theta_{thr}$  and is not a direct calculation using the numbers in the table.

## 3.5 Calculation of $R_{\rm b}$

To avoid dependence on the Monte Carlo angular distribution, the analysis is performed in bins of  $|\cos \theta_{\text{thr}}|$ . In each  $|\cos \theta_{\text{thr}}|$  bin, the efficiencies and corrected numbers of  $q\overline{q}$ and  $b\overline{b}$  events are determined. The efficiencies,  $\epsilon_{\text{b,c,uds}}$ , are defined as the number of MC events of the specific flavour b-tagged in the  $|\cos \theta_{\text{thr}}|$  bin, divided by the number of events of that specific flavour that were generated in that bin.

 $R_{\rm b}$  is then calculated in each bin in the range  $|\cos \theta_{\rm thr}| < 0.9$ . Figure 2 shows the value of  $R_{\rm b}$  versus  $|\cos \theta_{\rm thr}|$  for the 189 GeV and 207 GeV samples. The final value of  $R_{\rm b}$  is determined by taking the average over all bins. The total numbers of selected hadronic and tagged events, the values of the variables in equation 1, as well as the resulting  $R_{\rm b}$  value with its statistical uncertainty, are summarized in Table 2.

The resulting  $R_{\rm b}$  values are quoted for the case where  $R_{\rm c}$  is set to its Standard Model value,  $R_{\rm c}^{\rm SM}$ , given in Table 2. The dependence of the result on the assumed value of  $R_{\rm c}$  can be parametrized as:

$$\Delta R_{\rm b} = b \left( R_{\rm c} - R_{\rm c}^{\rm SM} \right) \,.$$

The parameter b, derived from equation 1, is determined separately for each centre-of-mass energy and is given in Table 4.

## 4 Systematic uncertainties

The systematic uncertainties considered for these measurements are described in the following paragraphs. A breakdown of the systematic uncertainty at 207 GeV is given in Table 3, and the total systematic error is given for all energies in Table 4.

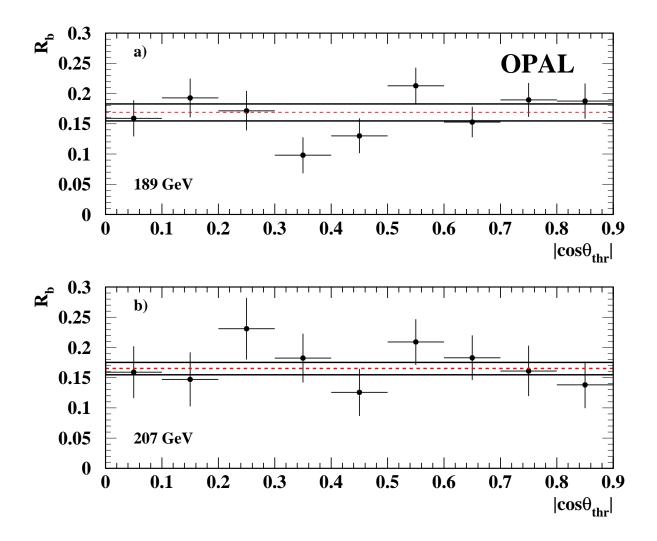


Figure 2: Measured values of  $R_{\rm b}$  for: a) the 189 GeV sample; b) the 207 GeV sample with statistical uncertainties only. The dashed line is the average value and the solid lines show the the band corresponding to the one standard deviation uncertainty.

Uncertainty source	$\Delta R_{ m b}/R_{ m b}~(\%)$
b fragmentation	0.6
b decay multiplicity	0.6
b hadron composition	0.3
b lifetime	0.1
c fragmentation	0.8
c decay multiplicity	0.1
c hadron composition	0.3
c lifetime	0.1
semileptonic branching ratio	0.1
semileptonic decay model	0.1
Total b,c physics modelling	1.3
$K^0$ , $\Lambda$ rate	0.2
Interference	0.3
Four-fermion background	0.1
$g_{b\overline{b}}$	0.1
gc <del>c</del>	0.1
Total physics modelling	1.3
Track reconstruction	3.2
Lepton ID	0.5
Non-radiative event selection	0.1
Monte Carlo statistics	0.6
Total detector effects	3.3
Total systematic uncertainty	3.5

Table 3: Systematic uncertainty breakdown at  $\sqrt{s} = 207$  GeV. The uncertainties at other centre-of-mass energies are similar.

## 4.1 Physics modelling

#### 4.1.1 Bottom and charm physics modelling

Uncertainties in bottom and charm fragmentation and decay properties are discussed below. The variation of parameters is realized by reweighting Monte Carlo events to the modified distribution.

• **b** fragmentation: Although the mean scaled energy  $2\langle E_b \rangle / \sqrt{s}$  of weakly decaying b hadrons is expected to change from LEP1 to LEP2 energies, the free parameter  $\epsilon_P^b$  of the Peterson fragmentation function [11] used in the default MC for heavy flavour events is assumed not to vary with energy. The value in bb events is varied in the range  $0.0030 < \epsilon_P^b < 0.0048$ , which corresponds to a variation of the mean scaled energy  $2\langle E_b \rangle / \sqrt{s}$  of weakly decaying b hadrons in Z decays in the range of  $2\langle E_b \rangle / \sqrt{s} = 0.702 \pm 0.008$  [12]. In addition, the heavy-quark fragmentation model is changed to that suggested by Collins and Spiller [28] and to that of Kartvelishvili [29]. The largest difference in all the above tests is from the Peterson parameter variation and is taken as the systematic uncertainty.

- **b** decay multiplicity: The multiplicity of the charged decay products of hadrons containing a b quark is varied in the Monte Carlo simulation according to [12].
- **b** hadron composition: The tagging efficiency differs for the various b hadron species. The fractions of b hadrons and their uncertainties have been taken from [30]. The fractions  $f(B_s^0)$  and  $f(b_{\text{baryon}})$  are varied independently within ranges of the experimental measurements, and their variation is compensated by the fraction of  $B^0$  and  $B^{\pm}$  mesons.
- **b hadron lifetimes:** The lifetimes of the different b hadrons are varied in the Monte Carlo by their uncertainties according to [30].
- c fragmentation: Simulated  $c\overline{c}$  events have their Peterson fragmentation parameter  $\epsilon_P^c$  varied in the range of  $0.022 < \epsilon_P^c < 0.039$ . This corresponds to a variation of the mean scaled energy  $2\langle E_c \rangle/\sqrt{s}$  of weakly decaying c hadrons in Z decays in the range of  $2\langle E_c \rangle/\sqrt{s} = 0.484 \pm 0.010$  [12].
- c decay multiplicity: The average charged particle multiplicities of D<sup>+</sup>, D<sup>0</sup> and D<sup>+</sup><sub>s</sub> decays are varied in the Monte Carlo within the ranges of the experimental measurements [31].
- c hadron composition: The D<sup>0</sup> fraction is written as  $f(D^0) = 1 f(D^+) f(D_s^+) f(c_{\text{baryon}})$ . The last three parameters are varied independently by their uncertainties according to [32] to evaluate the uncertainty on the charm efficiency.
- c hadron lifetimes: Charmed hadron lifetimes are varied within their experimental uncertainties according to [30].
- semileptonic decay modelling and branching ratios: The semileptonic branching ratios of bottom- and charm-hadrons are varied within their experimental uncertainties [12]. The uncertainty due to the semileptonic decay model used in the simulation is estimated as in [24].

## 4.1.2 Inclusive $K^0$ and $\Lambda$ production rate

The total production rates of  $K^0$  and  $\Lambda$  in the Monte Carlo are varied by 4% and 7% respectively according to [4]. This variation contributes an uncertainty of 0.18%.

## 4.1.3 Initial-final state interference

To asses the uncertainty on the correction for interference, we used the results of a study made in [3] by replacing the ZFITTER predictions with those of the KK2f program [7]. We assign the difference between the two predictions as a systematic uncertainty.

## 4.1.4 Four-fermion background

The uncertainties on the measured  $W^+W^-$  and ZZ cross-sections [2] and the uncertainty on the luminosity are found to have a negligible systematic effect on  $R_{\rm b}$ . The background from W- and Z-pairs has the highest probability to be accepted in the tagged sample when one or both bosons decay into a final state containing a charm- or bottom-quark. The systematic uncertainty on the W- and Z-pair tagging efficiency is estimated by varying the tagging efficiency by 5%. This variation introduces an uncertainty of 0.15%. The effect of the detector resolution is also taken into account, as described in Section 4.2.1.

#### 4.1.5 Secondary heavy-quark production

As discussed in Section 3.3, the difference between the Monte Carlo rate for secondary  $b\overline{b}$  production and the highest expected value is taken as an uncertainty. Typically, this process contributes a relative uncertainty of about 0.1%. The secondary  $c\overline{c}$  production rate is taken from [23,24] and weighted according to [26] as described in Section 3.3. The uncertainty on this estimation contributes a relative uncertainty of 0.13%.

### 4.1.6 Monte Carlo $b\overline{b}$ production

The transition  $N_{had} \rightarrow N_{q\bar{q}}$  has a small dependence on the Monte Carlo value of  $R_b$ . The default Monte Carlo value of  $R_b$  is varied within the measured uncertainty (Table 2). The effect on  $R_b$  is negligible.

## 4.2 Detector effects

#### 4.2.1 Track reconstruction

The detector performance in the Monte Carlo is varied as in [4,18]. The effect of the detector resolution on the track parameters is estimated by degrading the resolution of all tracks in the Monte Carlo simulation. This is done by applying a single multiplicative scale factor to the difference between the reconstructed and true track parameters. A 5% variation is applied independently to the  $r\phi$  and rz track parameters. These variations together contribute an uncertainty of 1.8%. In addition, the efficiency for assigning measurement points in the silicon microvertex detector to the tracks is varied by 1% in  $r\phi$  and 3% in rz. Each of these variations contributes an uncertainty of 1.3%. The track reconstruction efficiency is varied by 1%. This is done by randomly discarding 1% of the tracks, and contributes an uncertainty of 1.8%. The alignment of the silicon microvertex detector is changed in the Monte Carlo as in [4]. This variation gives an uncertainty of 0.4%. The systematic uncertainties resulting from the individual variations are summed in quadrature.

Since the largest part of this uncertainty is due to the effect on  $\epsilon_{uds}$ , we verify the validity of the 5% variation in the  $r\phi$  track parameters by using events that are rejected by the b-tagger. We look at the 182–209 GeV sample as well as at data collected in the same years at the Z peak for detector calibration. Events with a low value of  $\mathcal{L}_{hemi}$  in one hemisphere are selected, giving a sample dominated by light-quark pairs. The value of the vertex significance in the opposite hemisphere is then examined. Figure 3 shows

the fraction of events with vertex significance less than a negative cut value in the data and in the Monte Carlo with 5% variation in the  $r\phi$  track parameters, normalised to the fraction in Monte Carlo. This study suggests that the difference between the data and the Monte Carlo is smaller than the variation on the Monte Carlo and we conclude that the 5% variation is adequate.

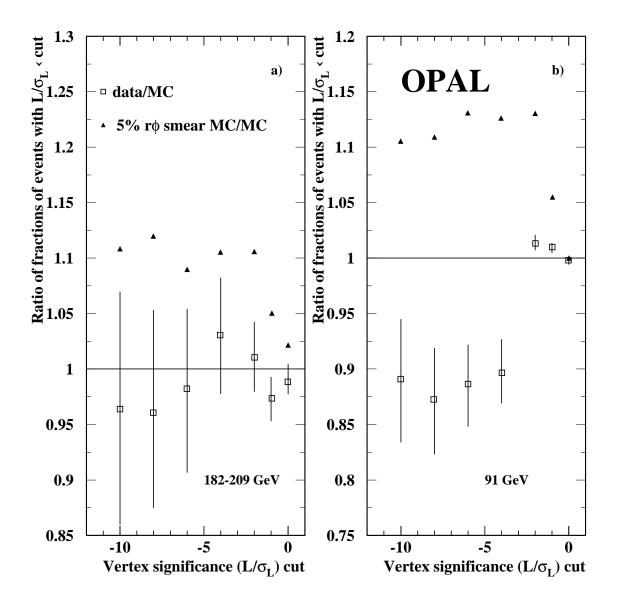


Figure 3: Ratios of fractions of hemispheres with vertex significance smaller than the cut value on the abscissa. The data (open squares) and the Monte Carlo with 5% deterioration of the tracking parameters resolution in  $r\phi$  (solid triangles) are normalised to the default Monte Carlo. The uncertainties are a combination of the data and Monte Carlo statistical uncertainties. Hemispheres are selected if the opposite hemisphere in the event has a low value of  $\mathcal{L}_{\text{hemi}}$ , giving a sample 75% pure in uds events. The 182–209 GeV sample is shown in a) and the 91 GeV sample in b).

#### 4.2.2 Lepton ID

The electron identification efficiency is varied by 15% and the electron fake rate by 30%. These values are 50% larger than those used in [5] following a later comparison of OPAL's data and Monte Carlo. The muon identification efficiency is varied by 2% and the fake rate by 14%. This source contributes typically an uncertainty of 0.45% on  $R_{\rm b}$  which is predominantly from the variation on the electron identification efficiency.

#### 4.2.3 Non-radiative event selection

We repeated the analysis using a different method for estimating s', described in [33]. The resulting  $R_{\rm b}$  was found to be different by less than 0.1%. This comparison is almost free of statistical uncertainties; thus we take this difference as an uncertainty.

#### 4.2.4 Monte Carlo statistics

The finite size of the Monte Carlo samples contributes between 0.6% and 0.8% uncertainty to the systematic error.

#### 4.3 Cross-checks

As a cross-check, the analysis is repeated on data collected in the same years at the Z peak for detector calibration. A value of  $R_{\rm b}(\sqrt{s} = m_{\rm Z}) = 0.210 \pm 0.001({\rm stat.}) \pm 0.006({\rm syst.})$  is obtained. The systematic uncertainty is determined as for the high-energy data samples. This result is consistent with the LEP1 average value of  $R_{\rm b}^0 = 0.21643 \pm 0.00073$  [2].

Another cross-check is made by comparing the likelihood of the hemisphere to contain a b-quark in Monte Carlo and data. This comparison is done for both the 182–209 GeV data and the calibration data at the Z peak. We select hemispheres where the b-tagger output in one hemisphere indicates a high probability for the event to be a bb event, and look at the opposite hemisphere. The samples are 60% and 88% pure in bb events for the high energy and the Z peak data respectively. We also look at hemispheres in events that are rejected by the b-tagger in the opposite hemisphere, giving samples with only 6% bb events. The results of this cross-check for the 182–209 GeV data and for the calibration data at the Z peak are shown in Figure 4. The small excess of data with respect to the Monte Carlo for  $\mathcal{L}_{\text{hemi}} > 0.85$  in the anti-b-tagged plot of the 182–209 GeV sample (Figure 4 (b)) is covered by the detector resolution uncertainty. It is consistent with the result of the study shown in Figure 3 (a). The difference between the Monte Carlo and the data in the b-tagged 91 GeV plot (Figure 4 (c)) is also covered by the detector resolution uncertainty.

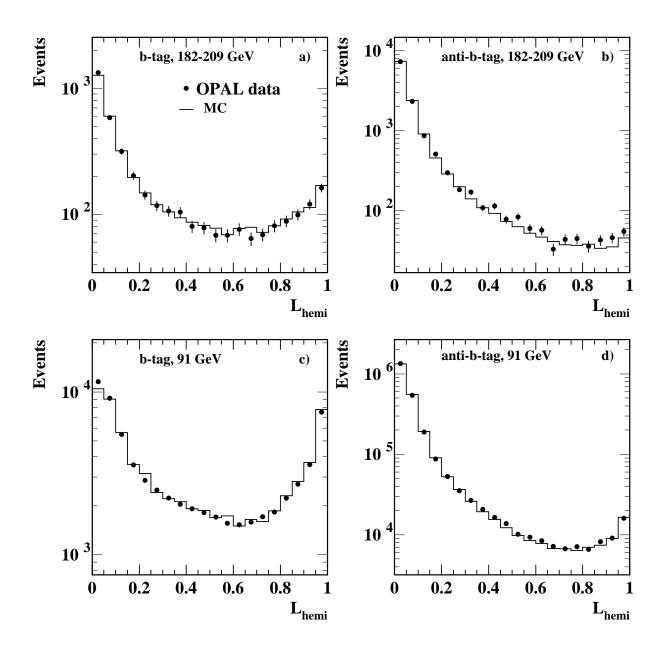


Figure 4: b-tagger output from one hemisphere for events selected by the opposite hemisphere. The top plots are for all data events in the range 182–209 GeV, and the bottom two are for the Z sample. a) and c) are for b-tagged opposite hemispheres and b) and d) are for anti-b-tagged opposite hemispheres.

## 5 Results and conclusion

The  $e^+e^- \rightarrow b\overline{b}$  production rate per non-radiative  $e^+e^- \rightarrow q\overline{q}$  event has been measured using data collected by the OPAL detector at LEP at centre-of-mass energies between 182 GeV and 209 GeV. The results are summarized in Table 4, together with earlier OPAL results from 130-172 GeV [5]. The measurements are shown in Figure 5, where they are compared with the predictions of the Standard Model, calculated using ZFITTER. Good agreement between the Standard Model and the measurements is observed. A comparison of the eight measurements reported here to the Standard Model prediction gives:  $\chi^2 = 5.0$ , or 76% probability of obtaining a larger difference than observed. Since the  $\chi^2$  test only uses the absolute difference between the prediction and measurement, we also made another test assuming that the ratio of the measurement to the prediction is constant. We perform a  $\chi^2$  fit for the ratio using only the statistical uncertainties and add the systematic uncertainties, which are assumed to be fully correlated, to the result. We obtain a ratio of  $1.055 \pm 0.031$  (stat.)  $\pm 0.037$  (sys.). Both tests suggest that these measurements are consistent with the Standard Model.

The measurement technique presented here has a larger selection efficiency and purity and thus yields a smaller statistical uncertainty and a smaller dependence on  $R_c$  than the one used previously. The 183 GeV and 189 GeV results are in agreement with [5] and supersede the previous measurements.

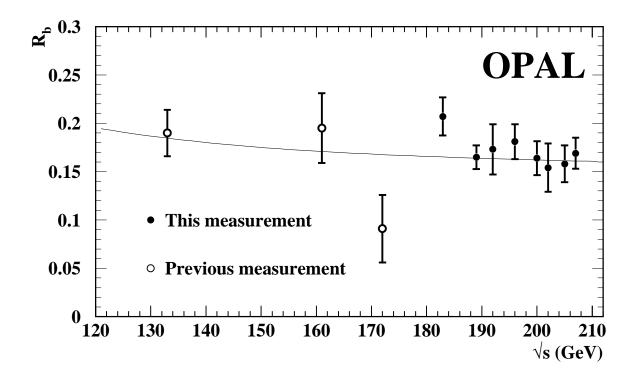


Figure 5: The measured  $R_{\rm b}$  values (points with error bars) and the Standard Model prediction (solid line).

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$\sqrt{s} \; (\text{GeV})$	$R_{\rm b} \pm {\rm stat} \pm {\rm sys}$	$b = \frac{\Delta R_{\rm b}}{(R_{\rm c} - R_{\rm c}^{\rm SM})}$
133.3 [5]	$0.190 \pm 0.023 \pm 0.007$	-0.12
161.3 [5]	$0.195 \pm 0.035 \pm 0.007$	-0.11
172.1 [5]	$0.091 \pm 0.034 \pm 0.005$	-0.11
182.7	$0.207 \pm 0.018 \pm 0.007$	-0.085
188.6	$0.165 \pm 0.010 \pm 0.006$	-0.082
191.6	$0.174 \pm 0.025 \pm 0.006$	-0.088
195.5	$0.181 \pm 0.017 \pm 0.006$	-0.092
199.5	$0.164 \pm 0.016 \pm 0.006$	-0.083
201.6	$0.154 \pm 0.024 \pm 0.005$	-0.088
205.3	$0.158 \pm 0.018 \pm 0.006$	-0.088
206.8	$0.169 \pm 0.014 \pm 0.006$	-0.082

Table 4:  $R_{\rm b}$  values with statistical (first) and systematic uncertainties. The last column gives the dependence of the  $R_{\rm b}$  value on  $R_{\rm c}$ . No variation of  $R_{\rm c}$  is included in the systematic uncertainty in the second column. The first three results are from the previous OPAL measurement [5].

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