

A Short Timescale Candidate Microlensing Event in the POINT-AGAPE Pixel Lensing Survey of M31

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ABSTRACT

We report the discovery of a short-duration microlensing candidate in the northern field of the POINT-AGAPE pixel lensing survey towards M31. The full-width half-maximum timescale is very short, $t_{1/2} = 1.8$ days. Almost certainly, the source star has been identified on *Hubble Space Telescope* archival images, allowing us to infer an Einstein crossing time of $t_E = 10.4$ days, a maximum magnification of $A_{\max} \sim 18$, and a lens-source proper motion $\mu_{\text{rel}} > 0.3 \mu\text{as/day}$. The event lies projected at $8'$ from the center of M31, which is beyond the bulk of the stellar lens population. The lens is likely to reside in one of three locations. It may be a star in the M31 disk, or a massive compact halo object (Macho) in either M31 or the Milky Way. The most probable mass is $0.06 M_{\odot}$ for an M31 Macho, $0.02 M_{\odot}$ for a Milky Way Macho and $0.2 M_{\odot}$ for an M31 stellar lens. Whilst the stellar interpretation is plausible, the Macho interpretation is the most probable for halo fractions above 20%.

Subject headings: Galaxy: halo – M31: halo – lensing – dark matter

1. Introduction

Following the suggestion of Paczyński (1986), several groups searched for dark matter in the form of massive compact halo objects (Machos), using gravitational microlensing of background stars in the Magellanic Clouds (see Alcock et al. 2000; Lasserre et al. 2000; and references therein). After monitoring about 10^7 stars for several years, the results are consistent with a Macho halo mass fraction of 20%, though with considerable uncertainty.

The possibility of detecting microlensing events in M31 was independently suggested by Crotts (1992) and Baillon et al. (1993). The advantage of targeting a large external galaxy is that the number of stars that can act as possible sources is enormous. Moreover, the high inclination of M31’s disk causes an asymmetry in the observed rate of microlensing by lenses in a spheroidal halo. Although this gives an unambiguous signature of the halo lenses (Crotts 1992), the difficulty is that the sources are resolved only while they are lensed (and then only if the magnification is substantial). Nonetheless, pilot campaigns by the Columbia-VATT group (Crotts & Tomaney 1997) and by the AGAPE collaboration (Ansari et al. 1997; Ansari et al. 1999) established the feasibility of such observations and identified some candidate microlensing events. In particular, the AGAPE collaboration (Ansari et al. 1999) reported a short duration candidate, AGAPE Z1, in the bulge of M31.

The POINT-AGAPE collaboration¹ employs the Wide Field Camera (WFC) on the 2.5 m Isaac Newton Telescope (INT) to carry out a pixel-lensing survey towards M31, monitoring two fields of 0.3 deg^2 each, located North and South of the M31 center. The survey has the potential to map the global distribution of the microlensing events in M31 and to determine any large-scale gradient. POINT-AGAPE is a long-term program, as at least three years of data will be required to make a convincing identification of a gradient

¹see <http://www.point-agape.org>

(Kerins et al. 2001). Also, it is usually necessary with pixel lensing to establish a long baseline to distinguish microlensing events from variable stars. In this *Letter*, we report on a particularly interesting and convincing early candidate, PA-99-N1, so named because it is the first event to be announced by POINT-AGAPE that peaks in the northern field in 1999.

2. Observations and Data Analysis

We restrict analysis to a ($11' \times 22'$) field centered $3'$ west and $12'$ north of the center of M31. The observations are spread over 36 epochs between August and December 1999. The exposures are in two bands: 36 epochs in Sloan r' and 26 epochs in Sloan g' . The exposure time is typically between 5 and 10 minutes per night. The sampling averages to one epoch every three nights, though the observations are strongly clustered because the WFC is not always mounted. The data reduction is described in detail elsewhere (Ansari et al. 1997; Strauman et al. 1998; Le Du 2000).

After bias subtraction and flat-fielding, each image is geometrically and photometrically aligned relative to a reference image (14 August 1999) which was chosen because it has a long exposure time, typical seeing ($1.''6$) and little contamination from the Moon. The lightcurves are computed by summing the flux in 7-pixel ($2.''3$) square “superpixels” and then removing the correlation with seeing variation. This size is set by the worst seeing $\sim 2.''1$.

We use a simple set of candidate selection criteria designed to isolate high signal-to-noise events. Detection of events is made in the r' band, which has better sampling and lower sky background variability. For an event to be detected, it must induce one and only one significant bump on the lightcurve. A bump is defined by at least 4 consecutive data points rising above the background by a minimum of 4σ . Its significance is quantified by the

probability P of obtaining data points, each of which has at least the signal to noise ratio of the measured points (evaluated assuming Gaussian errors). To pass as a microlensing candidate, we demand the lightcurve has only one bump with $-\ln P > 100$ and no other bump with $-\ln P > 20$. A similar selection procedure was used by the AGAPE Pic du Midi program (Ansari et al. 1997).

The background is the minimum of the running average of 7 consecutive data points. Flagged events are fitted to a high magnification degenerate microlensing curve (Gould 1996) simultaneously in the r' and g' bands, whose 6 parameters are $(t_{1/2}, t_0, F_{\text{base},r'}, F_{\text{base},g'}, \Delta F_{\text{peak},r'}, \Delta F_{\text{peak},g'})$. Here, $t_{1/2}$ is the full-width at half-maximum, t_0 is the time of the peak, F_{base} is the baseline flux and ΔF_{peak} is the flux difference between baseline and maximum. We require a χ^2 per degree of freedom be less than 3 for this fit. We also require at least minimal detection in g' , i.e. $\Delta F_{\text{peak},g'} > 1 \text{ ADU s}^{-1}$. To insure a high probability of detecting microlensing rather than other forms of stellar variability, given the clustered sampling and relatively short duration of the observations, we demand $t_{1/2} < 8$ days and a peak flux $\Delta F_{\text{peak},r'} > 10 \text{ ADU s}^{-1}$, corresponding to $R_{\text{peak}} < 21.5$. We find one candidate which has $t_{1/2} \sim 1.8$ day and $\Delta F_{\text{peak},r'} \sim 17 \text{ ADU s}^{-1}$.

3. The Microlensing Candidate

Figure 1 shows the lightcurves in r' and g' of this candidate together with the non-degenerate fit derived below. The g' data with comparatively large error bars were taken on nights with high Moon background. Using the Aladin Sky Atlas², we find that PA-99-N1 has J2000 position: $\alpha = 00^{\text{h}}42^{\text{m}}51^{\text{s}}.42$, $\delta = +41^{\circ}23'53''.7$. That is, it lies projected on the near disk, $7'52''$ from the center of M31.

²see <http://aladin.u-strasbg.fr/aladin.gml>

There are some straightforward tests to see if PA-99-N1 is compatible with microlensing. First, there are no comparable “bumps” in the remainder of the lightcurve shown in Figure 1 as might be expected for many classes of variable stars. (There is, however, a much smaller but somewhat disturbing bump in December, near day 130. We investigate this bump in § 4.1.) There also are no comparable bumps at this field position in our data taken in 1998 and 1999 with the 1.3m McGraw-Hill telescope at the MDM observatory. Second, microlensing events are achromatic, so the ratio of flux *change* in different bands should be constant in time (e.g., Ansari et al. 1997). This requires

$$\frac{\Delta F_{g'}(t)}{\Delta F_{r'}(t)} = \frac{F_{g'}(t) - F_{\text{base},g'}}{F_{r'}(t) - F_{\text{base},r'}} = \text{constant}, \quad (1)$$

which does indeed hold for PA-99-N1 (see Fig. 1c).

Using DAOPHOT (Stetson 1987) on the images taken nearest maximum magnification, we find $R = 20.80 \pm 0.13$ and $V = 22.00 \pm 0.17$, i.e., $V - R = 1.20 \pm 0.22$ and $M_V = -2.8 \pm 0.3$, assuming $(m - M)_{0,M31} = 24.43$ and estimated total extinction $A_V = 0.4 \pm 0.2$. The transformation from instrumental (r', g') to Johnson (V, R) is based on 31 standard stars that lie in the same field as PA-99-N1 (Magnier et al. 1992; Magnier et al. 1993; Haiman et al. 1994).

The PA-99-N1 position lies within a series of five *Hubble Space Telescope (HST)* WFPC2 archival images taken in July 1996, three with F814W ($\sim I$) and two with F606W ($\sim V$). We use the relations of Zheng et al. (2001) to transform from these filters to Johnson-Cousins V and I . Since the event is very red, $V - R \sim 1.2$, the source must lie either high up on the giant branch where essentially all stars are resolved by *HST*, or must be on the main-sequence and so magnified by $A_{\text{max}} \gtrsim 10^4$ (see Fig. 2). The latter possibility is extremely unlikely a priori. Hence, a firm prediction of the microlensing interpretation is that there should be a resolved star in the *HST* image with the same color and same position as the event.

To measure the spatial position of the event within the INT image we take the difference of the image at maximum and another image at baseline that has similar seeing. The difference image shows a well-defined and isolated difference star whose position we measure using IRAF IMEXAMIN. Variation of the IMEXAMIN parameters changes the result by ~ 0.2 pixels ($0''.07$), which we adopt as the error in the measurement. The spatial transformation between the INT and *HST* fields is derived by comparing the positions of the eight stars that are both resolved in the INT image and unsaturated in the *HST* image. The uncertainty in this transformation is much smaller than that of the INT position measurement. Figure 3 shows part of the *HST* field with the 1σ and 3σ positional error circle centered on the event. Close to this circle there is a resolved star for which we find $V = 24.51 \pm 0.12$ and $I = 22.41 \pm 0.10$, implying $V - I = 2.10 \pm 0.16$. There are no other resolved stars within the 3σ circle. For typical stellar populations this $V - I$ is compatible with the $V - R = 1.20 \pm 0.22$ measured for the event (Demarque et al. 1996; Yi, Demarque, & Oemler 1996). The prior probability to find such a star so close to the predicted position is only 3%. We conclude that the resolved HST object is almost certainly the source star of the event.

4. Lightcurve Interpretation

4.1. PA-99-N1 as a Variable Star

Before analyzing PA-99-N1 as a microlensing event, we need to ask whether it is consistent with an interpretation as a variable star? The color and magnitude are compatible with a M0 Mira at maximum. However, such Miras have periods greater than 200 days and their flux at maximum does not vary as rapidly as the event (Allen 1999). PA-99-N1 is unlikely to be a dwarf nova. It is too bright at maximum to be in M31. If it is a Galactic dwarf nova, it must be either unusually faint or improbably far from us

(> 10 kpc). It is also unlikely to be a nova. The brightness decrease of PA-99-N1 just after maximum is very rapid with a rate of decline of about 0.7 magnitudes/day. Capaccioli et al. (1989) studied the relation between the rate of decline and the magnitude at maximum for novae in M31 and found that the brighter the nova, the faster the decrease. The decline of PA-99-N1 would indicate a nova as bright as $V = 16$, which would imply $A_V = 6$, in stark contrast to the small extinction seen in Figure 2. To conclude, there is no type of stellar variability known to us that could generate the lightcurve of PA-99-N1.

However, if the December bump near day 130 in Figure 1 were due to the event source, one would nevertheless have to conclude that the source was probably a variable. We therefore investigate this bump closely. For each of the nine December images, we find a corresponding image at baseline with comparable seeing, and subtract the two. Summing these difference images, we find a very clear stellar profile located $1.''1 \pm 0.''1$ south of the source. Hence, this bump is due to genuine stellar variability, which was close enough to contaminate our $2.''3$ superpixels, but is clearly distinguishable from the event source. We eliminate these contaminated December points from the analysis.

4.2. PA-99-N1 as a Microlensing Event

Making use of the identification of the *HST* star as the source of the microlensing event, we fit the data to a full (non-degenerate) microlensing curve and so evaluate the Einstein crossing time, $t_E = 10.4$ days.

By permitting the measurement of t_E ,

$$t_E = \frac{\theta_E}{\mu_{\text{rel}}}, \quad \theta_E = \sqrt{\pi_{\text{rel}} \left(\frac{4GM/c^2}{\text{AU}} \right)}, \quad (2)$$

the identification of the source reduces but does not eliminate the degeneracy in the lens parameters. The mass M remains entangled with π_{rel} and μ_{rel} , the lens-source relative

parallax and proper motion. If the lens transits the source, one can measure μ_{rel} and so further break the parameter degeneracy (Gould 1994; Alcock et al. 1997). We are not able to measure μ_{rel} for PA-99-N1, but are able to strongly constrain it from the lack of finite source effects that would be induced by a transit.

Let $\rho_* = \theta_*/\theta_{\text{E}}$, where θ_* is the angular radius of the source. We find that if we fit the lightcurve with ρ_* fixed at any value $\rho_* \leq 0.1$, then the other parameters all assume the same values as in Table 1. However, as ρ_* is increased further, t_{E} declines, so that the parameter combination $\rho_* t_{\text{E}}$ saturates at 1.0 day, and then for $\rho_* \gtrsim 0.12$, χ^2 rises dramatically. From this we derive the constraint $\rho_* t_{\text{E}} \leq 1.0$ day, implying,

$$\mu_{\text{rel}} = \frac{\theta_{\text{E}}}{t_{\text{E}}} = \frac{\theta_*}{\rho_* t_{\text{E}}} \geq \frac{\theta_*}{1.0 \text{ day}}. \quad (3)$$

Using the empirical surface-brightness/color relation of van Belle (1999), the color-color transformation of Bessell & Brett (1988), and an estimated total extinction $A_V = 0.4 \pm 0.2$, we find $\theta_* = 0.30 \pm 0.04 \mu\text{as}$, where the uncertainty is dominated by the 11% intrinsic scatter about the van Belle (1999) relation. The constraint (3) then yields

$$v_{\text{rel}} = \mu_{\text{rel}} D_l > 400 \text{ km s}^{-1} \left(\frac{\rho_* t_{\text{E}}}{1.0 \text{ day}} \right)^{-1} \left(\frac{\theta_*}{0.3 \mu\text{as}} \right) \left(\frac{D_l}{770 \text{ kpc}} \right), \quad (4)$$

where v_{rel} is the transverse speed of the lens relative to the observer-source line of sight, and D_l is the distance to the lens. While the constraint (4) is unimportant for Galactic lenses (where $D_l \sim 10 - 30$ kpc), it strongly limits the allowed range of μ_{rel} for M31 lenses (since high values are exponentially suppressed). Hence μ_{rel} is crudely measured, which implies, via equation (2), a constrained relation between M and π_{rel} . Thus, when the proper-motion constraint (4) is incorporated into the Monte Carlo (see below) it indirectly constrains the mass to a much narrower range than would be allowed without it. Note that our finite source fits incorporate a linear limb-darkening parameter of 0.78 in R band, which is appropriate for a $V - I = 2.1$ (M0-M1, 3630 K) star (Manduca, Bell & Gustafsson 1977; Johnson 1966).

5. Discussion

The location of PA-99-N1, at nearly $8'$ from the center of M31, is interesting because the majority of stellar lenses are expected to reside within $5'$ of the M31 center (e.g., Kerins et al. 2001). The significance of the candidate is assessed by performing Monte Carlo simulations of events with the same source magnitude, Einstein timescale and projected position as PA-99-N1, as well as taking account of the lower limit on μ_{rel} in equation (4). We use the actual sampling and exposure times for the 1999 season. We model the halos of both galaxies with cored near-isothermal spheres, taking the mass of M31 as twice the mass of the Galaxy and assuming a core radius of 5 kpc for both galaxies. The M31 bulge follows Kent’s (1989) axisymmetric model while the disk has a sech-squared profile (see Kerins et al. 2001 for details). We model the disk stellar lens masses based on the Galactic disk mass function (MF) of Gould, Bahcall, & Flynn (1997) corrected for binaries and extended down to $0.01 M_{\odot}$, and the bulge stellar masses using the Zoccali et al. (2000) Galactic bulge MF, similarly corrected and extended.

The thick solid line in Figure 4 (a) shows the relative probability P that PA-99-N1 is due to a Macho of mass M , assuming full Macho halos. The curve is normalized with respect to the probability that the lens is a star, P_{\star} . The thick dashed (dotted) curve gives the contribution to $P(M)$ from M31 (Milky Way) Machos. In addition to this, we have plotted the M31 distribution before applying the proper motion cut of equation (4) (thin dashed line). The black horizontal line (‘d/b’) gives the fractional contribution of the disk lens and bulge source configuration to P_{\star} , whilst the gray line (‘b/b’) shows the contribution of bulge-bulge lensing. The width of these lines reflects the dispersion in the logarithm of the stellar lens mass.

Clearly, if the halos are full of Machos, the most probable interpretation is that the lens is a Macho with mass $\sim 0.03 M_{\odot}$. This is about five times more likely than PA-99-N1 being

due to a stellar lens. The lens is about equally likely to lie in the Milky Way or M31 halo, which is quite unexpected given that the line of sight passes only 2 kpc from the center of M31, but 8 kpc from the Galactic center. Normally this would cause the M31 probability to be much higher (as shown by thin dashed line). However, the μ_{rel} constraint (4) severely suppresses the M31 distribution at low masses, while leaving the Milky Way distribution virtually unaffected. This is because the average Milky Way Macho has a relative proper motion of $\sim 10 \mu\text{as/day}$, whilst for the typical M31 Macho it is $\sim 0.2 \mu\text{as/day}$. The constraint also has the effect of displacing the peak of the M31 distribution towards higher mass.

Assuming a logarithmic prior in the Macho mass gives $M = 6.4_{-4.9}^{+21} \times 10^{-2} M_{\odot}$ for an M31 Macho and $2.1_{-1.6}^{+7.0} \times 10^{-2} M_{\odot}$ for a Milky Way Macho. The M31 and Milky Way distributions are both quite broad. As they are about equal in amplitude and are displaced from one another by nearly a decade in mass, their combined distribution is even broader, with a FWHM extending from the planetary to the stellar mass range.

If the lens is a star, then the overall mass probability distribution is given by the thick solid line in Figure 4 (b). The thick dashed line (‘d/b’) shows the contribution from disk-bulge lensing whilst the thick dotted line (‘b/b’) shows the distribution for bulge-bulge lensing. The contribution of lensing involving disk sources is negligible. In the absence of the relative proper motion cut, the disk and bulge distributions would be given by the thin dashed and dotted lines respectively. Including these cuts results in a most probable mass around $0.2 M_{\odot}$, making a rather plausible hypothesis that the lens is a low mass star. Logarithmic averaging of the solid line gives $M = 0.27_{-0.12}^{+0.21} M_{\odot}$, i.e., only a factor 1.8 (1σ) uncertainty.

We see that, if the lens is an M31 star, it most likely lies in the disk. This is a direct consequence of the fact that the source lies at the edge of the bulge, while the line of sight

passes through the near side of the disk. Comparing Figures 4a and 4b, it is clear that the mass of the lens is much better constrained if it lies in the M31 disk than the M31 halo. This is because for M31 lenses, $M \propto (\mu_{\text{rel}} t_E D_{\text{ls}})^2$ where D_{ls} is the distance from the lens to the source (see eq. [2]). For both populations, the product $\mu_{\text{rel}} t_E$ is reasonably well constrained, but for halo lenses, D_{ls} can take on a very broad range of values, while for disk lenses, the geometry implies $D_{\text{ls}} = 4.0 \pm 1.8 \text{ kpc}$. Since t_E is measured and μ_{rel} is constrained by equation (4), M is also constrained. This means that we only detect events at the location and timescale of PA-99-N1 if the stellar mass $M > 0.1 M_{\odot} (4 \text{ kpc} / D_{\text{ls}})$.

The relative rate of Machos to stars is subject to a number of modeling uncertainties. First, we have assumed that the M31 halo is twice as massive as that of the Milky Way. The most recent mass estimates of the M31 halo derived from the kinematics of the satellite galaxies suggest that it may be only roughly as massive as the Milky Way (Evans et al. 2000). Second, it is sensitive to the choice of the core radius for M31’s halo, with larger core radii giving a reduced M31 Macho rate at the location of PA-99-N1. Third, we have assumed that the M31 bulge is axisymmetric, but the twisting of the optical isophotes (e.g., Waltherbos & Kennicutt 1987) is evidence for the presence of a bar. Inspection of their Figure 5 shows that the twisting is away from the location of PA-99-N1. We therefore expect a bar model with the same overall mass as our axisymmetric model to have a lower surface density at the position of the event and thus a lower stellar lensing rate there.

6. Conclusions

We have reported the discovery of PA-99-N1, a high signal-to-noise, short duration event which is consistent with the microlensing hypothesis. Almost certainly, the source star has been identified on archival *HST* frames, from which the Einstein crossing time of 10.4 days has been determined. We have argued – from the stability of the lightcurve, the

achromaticity of the flux excess, the excellence of the fit, and the consistency of the color of the event at maximum with the color of the *HST* source – that by far the most natural explanation of this event is microlensing. The lens is most likely to be a Macho if the halo fraction is above 20%. However, it is also plausible that the lens is a disk star with a mass of $\sim 0.2 M_{\odot}$.

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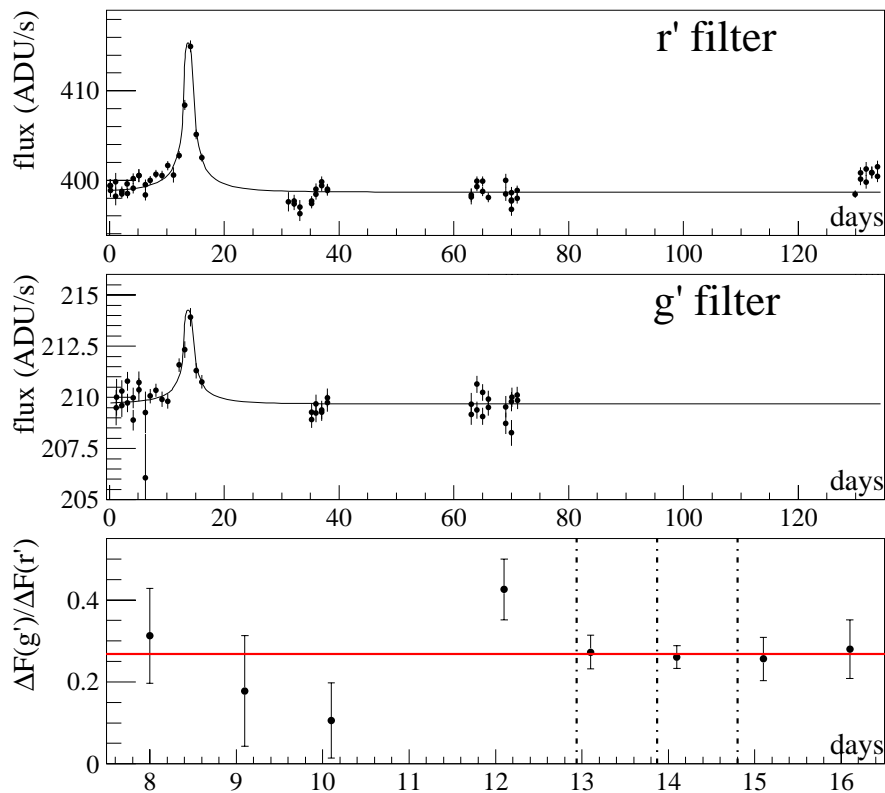


Fig. 1.— Panels (a) and (b) show the flux in r' and g' against time in days. Panel (c) is a zoom centred on the event that shows the variation of the ratio of the flux change in the two passbands $\Delta F_{g'}/\Delta F_{r'}$ with time. The vertical lines are centred on t_0 and are separated by 0.9 days, i.e., half the full width at half-maximum. The days correspond to $J - 2451392.5$ where J is the Julian date.

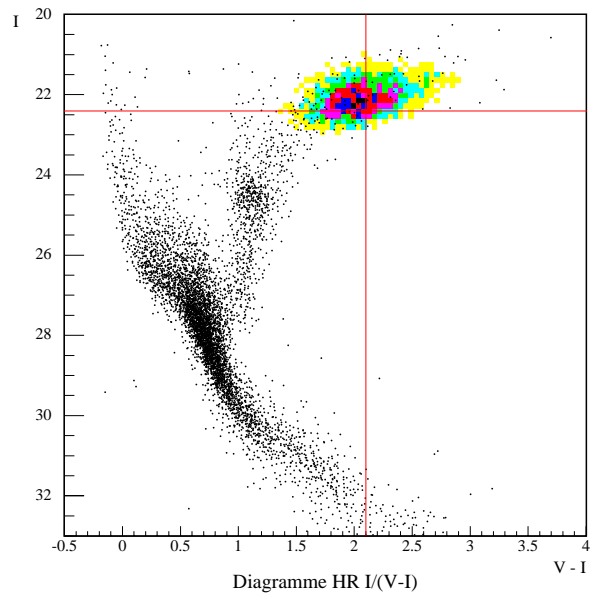


Fig. 2.— Superposition of the Hipparcos (points) and *HST* (shaded area) color-magnitude diagrams. The Hipparcos stars have been moved to the position of M31 [assuming $(m - M)_0 = 24.43$ and Galactic foreground extinction $A_V = 0.24$]. The intersection of the horizontal and vertical lines shows the position of the HST object.

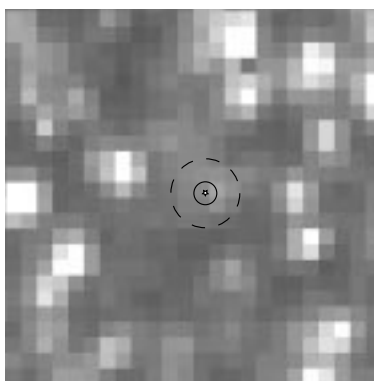


Fig. 3.— An image of the HST field showing the 1σ and 3σ error circles around the position of the event. There is a resolved source close to the 1σ circle.

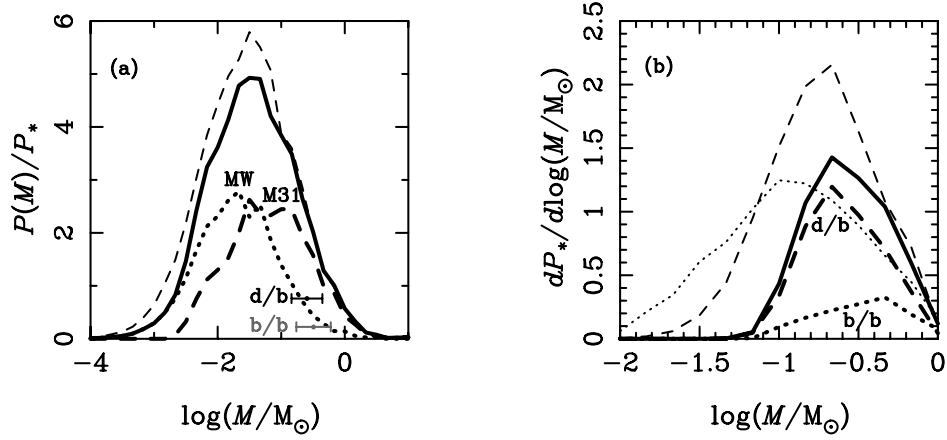


Fig. 4.— Panel (a) shows, for the case where PA-99-N1 is a Macho, the probability P that the lens has mass M (thick solid line), normalized to the probability P_* that PA-99-N1 is a stellar lens. The contribution to this curve from M31 (Milky Way) Machos is shown by the thick dashed (dotted) line. The thin dashed line shows $P(M)$ for M31 Machos before the relative proper motion cut (eq. 4). The horizontal bars show the contribution to P_* from bulge-bulge lensing ('b/b') and disk-bulge lensing ('d/b'), whilst their width indicates the logarithmic dispersion in the stellar lens mass. Panel (b) shows, for the case where PA-99-N1 is a stellar lens, the overall stellar probability density as a function of lens mass (solid line), including the contributions from bulge-bulge lensing (thick dotted line) and from disk-bulge lensing (thick dashed line). The thin dotted and dashed lines show the relative distributions of bulge and disk lenses before the proper motion cut.

Fit Parameters								
N	χ^2	t_0	u_0	t_E	$F_{s,r'}$	$F_{s,g'}$	$F_{b,r'}$	$F_{b,g'}$
		(days)		(days)	(ADU/s)	(ADU/s)	(ADU/s)	(ADU/s)
97	154	13.87	0.056	10.4	1.02	0.28	397.65	209.40
	\pm	0.04	0.009	1.5	0.17	0.05	0.18	0.10

Table 1: Fit parameters for PA-99-N1. N : number of points, t_0 : time of the peak, u_0 : impact parameter, t_E : Einstein timescale, F_s and F_b : source and background fluxes in two bands. The maximum magnification is $A_{\max} \sim u_0^{-1} \sim 18$.

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