

Measurement of the Mass and Width of the W Boson in e^+e^- Collisions at 189 GeV

The OPAL Collaboration

Abstract

The mass and width of the W boson are determined in e^+e^- collisions at LEP using 183 pb^{-1} of data recorded at a centre-of-mass energy $\sqrt{s} = 189 \text{ GeV}$ with the OPAL detector. The invariant mass distributions from 970 $W^+W^- \rightarrow \text{qqqq}$ and 1118 $W^+W^- \rightarrow \text{qq}\ell\nu_\ell$ candidate events are used to measure the mass of the W boson,

$$M_W = 80.451 \pm 0.076(\text{stat.}) \pm 0.049(\text{syst.}) \text{ GeV.}$$

A direct measurement of the width of the W boson gives $\Gamma_W = 2.09 \pm 0.18(\text{stat.}) \pm 0.09(\text{syst.}) \text{ GeV}$. The results are combined with previous OPAL results from 78 pb^{-1} of data recorded with \sqrt{s} from 161 to 183 GeV, to obtain:

$$\begin{aligned} M_W &= 80.432 \pm 0.066(\text{stat.}) \pm 0.045(\text{syst.}) \text{ GeV,} \\ \Gamma_W &= 2.04 \pm 0.16(\text{stat.}) \pm 0.09(\text{syst.}) \text{ GeV.} \end{aligned}$$

The consistency of the direct measurement of M_W with that inferred from other measurements of electroweak parameters provides an important test of the Standard Model of electroweak interactions.

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1 Introduction

The LEP e^+e^- collider at CERN provides an ideal environment for the study of the properties of the gauge bosons of the Standard Model (SM) of electroweak interactions [1]. In the first stage of its operation, LEP produced e^+e^- collisions at centre-of-mass energies, \sqrt{s} , within a few GeV of the Z^0 resonance, allowing precise measurements of the properties of the Z^0 boson including its mass and fermionic couplings [2, 3]. In the context of the SM these measurements place constraints on the mass of the Higgs boson and provide an indirect determination of the mass of the W boson, M_W . Since 1996, the LEP collider has operated above the threshold for W^+W^- production (LEP2), allowing measurements of the trilinear gauge boson couplings [4] and a direct measurement of M_W . When combined with the direct measurements of the top quark mass at the Tevatron [5], measurements of M_W enable further constraints to be set on the mass of the Higgs boson via electroweak radiative corrections [7, 6]. Comparison between the direct measurements of the mass of the W boson and the value determined indirectly from data recorded at $\sqrt{s} \approx M_Z$ provides an important test of the self-consistency of the Standard Model. The direct measurement of Γ_W further tests the consistency of the Standard Model.

The combination of direct measurements of M_W from LEP2 at $\sqrt{s} \sim 161 - 183$ GeV [8–13] and from hadron colliders [14] currently give $M_W = 80.419 \pm 0.056$ GeV [15]. This direct measurement is consistent with the indirect value obtained from lower energy data, primarily measurements at $\sqrt{s} \sim M_Z$, which give $M_W^{indirect} = 80.382 \pm 0.026$ GeV [3].

The published OPAL measurements of M_W are based on approximately 78 pb^{-1} of data. This paper describes a measurement of the mass of the W boson using a further 183 pb^{-1} of data recorded by OPAL during 1998 at $\sqrt{s} \sim 189$ GeV. This result is combined with previous OPAL measurements to give a direct measurement of the mass of the W boson with a total uncertainty of 79 MeV. It is expected that the ultimate LEP precision on M_W will be approximately 30 MeV when all data are included and the results of the four LEP experiments are combined [16].

2 Data and Monte Carlo Samples

A detailed description of the OPAL detector can be found in [17]. The data sample used for this analysis corresponds to an accepted integrated luminosity, evaluated using small angle Bhabha scattering events observed in the forward calorimeters [18], of $183.1 \pm 0.2(\text{stat.}) \pm 0.4(\text{syst.}) \text{ pb}^{-1}$. The luminosity weighted mean centre-of-mass energy for the data sample is $\sqrt{s} = 188.635 \pm 0.040$ GeV [19].

2.1 Monte Carlo samples

A number of Monte Carlo generators are used to simulate the physics processes relevant to the studies presented in this paper. All samples include a full simulation of the OPAL detector [20]. The main physics processes at LEP2 can be broken down into three main categories: four-fermion ($4f$) production, including $e^+e^- \rightarrow W^+W^- \rightarrow 4f$ and $e^+e^- \rightarrow Z^0Z^0 \rightarrow 4f$, but excluding contributions from multi-peripheral diagrams; two-fermion production; and multi-peripheral two-photon mediated processes. For the measurement of the W boson mass and width, only the four-fermion processes and the two-fermion background process $e^+e^- \rightarrow Z^0/\gamma \rightarrow q\bar{q}$ play an important role.

The KORALW program [21], which uses matrix elements calculated with grc4f [22], is used to

simulate the production of most four-fermion final states, $e^+e^- \rightarrow 4f$. The main Monte Carlo samples are generated at $\sqrt{s} = 188.634$ GeV with $M_W = 80.33$ GeV. The samples were generated using the running width scheme for the Breit-Wigner distribution. The four-fermion samples are divided into final states which have contributions from processes involving the W-boson propagator and those which do not. In the invariant mass region close to M_W , the four-fermion cross-section is dominated by doubly resonant W-pair production diagrams (CC03)¹. Additional KORALW four-fermion Monte Carlo samples are produced with different centre-of-mass energies and with different values of M_W . The four-fermion background from the process $e^+e^- \rightarrow e^+e^-q\bar{q}$ is simulated using the grc4f [22] generator. The most important two-fermion background process, $e^+e^- \rightarrow Z^0/\gamma \rightarrow q\bar{q}$, is simulated using PYTHIA [23], with HERWIG [24] used to assess possible systematic uncertainties.

3 W^+W^- Event Selection

The event selections are described in [25] and references therein. The selections are sensitive to the leptonic $W^+W^- \rightarrow \ell\nu_\ell\ell\nu_\ell$, semi-leptonic $W^+W^- \rightarrow qq\ell\nu_\ell$, and hadronic $W^+W^- \rightarrow qqqq$ final states. Due to the presence of two unobserved prompt neutrinos in the $W^+W^- \rightarrow \ell\nu_\ell\ell\nu_\ell$ final state there is little sensitivity to M_W and the leptonic final state is therefore not used here.

Semi-leptonic $W^+W^- \rightarrow qq\ell\nu_\ell$ decays comprise 44% of the total W^+W^- cross-section. The event selection employs three multivariate relative likelihood discriminants, one for each of the $W^+W^- \rightarrow qqe\nu_e$, $W^+W^- \rightarrow qq\mu\nu_\mu$, and $W^+W^- \rightarrow qq\tau\nu_\tau$ final states. The $W^+W^- \rightarrow qqe\nu_e$ and $W^+W^- \rightarrow qq\mu\nu_\mu$ channels are characterised by two well-separated hadronic jets, a high-momentum lepton and missing momentum due to the prompt neutrino from the leptonic W decay. The signature for the $W^+W^- \rightarrow qq\tau\nu_\tau$ channel is similar, with the exception that the τ lepton is identified as an isolated, low-multiplicity jet typically consisting of one or three tracks. $W^+W^- \rightarrow qq\ell\nu_\ell$ events are selected with an efficiency of 87% and a purity of 91%. The dominant backgrounds are $Z^0/\gamma \rightarrow q\bar{q}$ and four-fermion processes such as $e^+e^- \rightarrow We\nu_e$ and $e^+e^- \rightarrow (Z^0/\gamma)^*(Z^0/\gamma)^* \rightarrow q\bar{q}\ell^+\ell^-$.

Hadronic $W^+W^- \rightarrow qqqq$ decays comprise 46% of the total W^+W^- cross-section and are identified by requiring four energetic hadronic jets and little or no missing energy. A preselection removes approximately 98% of the dominant background process, $Z^0/\gamma \rightarrow q\bar{q}$. A multivariate relative likelihood discriminant is then employed to select the $W^+W^- \rightarrow qqqq$ candidates with an efficiency of 87% and a purity of 77%.

After the selections are applied, 1546 $W^+W^- \rightarrow qqqq$ and 1246 $W^+W^- \rightarrow qq\ell\nu_\ell$ candidate events remain, consistent with Standard Model expectations. Not all events are used in the measurements described here. As discussed in Section 4.1, additional cuts are applied to remove poorly reconstructed events and further reduce backgrounds.

4 Measurement of the Mass and Width of the W Boson

The measurement of the mass and width of the W boson proceeds in two stages. Firstly the invariant masses of the W decay products are reconstructed on an event-by-event basis. Kinematic fits are applied to each selected $W^+W^- \rightarrow qq\ell\nu_\ell$ and $W^+W^- \rightarrow qqqq$ event to improve the mass resolution. The reconstructed invariant mass spectra are then used to determine M_W and Γ_W .

¹In this paper, the doubly-resonant W pair production diagrams, *i.e.* t -channel ν_e exchange and s -channel Z^0/γ exchange, are referred to as ‘‘CC03’’, following the notation of [16].

Fits to the invariant mass spectra to obtain M_W are performed using three different techniques. The central results of this paper are obtained using a Monte Carlo reweighting technique [16] to fit the observed mass spectra to obtain M_W and Γ_W . The W mass is also determined using two alternative methods, which are used as cross-checks. In the first, an analytic fit to the measured mass spectrum uses an unbinned likelihood fit method to determine M_W . To describe the signal shape, the fit uses a parametrisation based on a Breit-Wigner function [9]. The second method uses a convolution technique [12, 16]. The three different fitting techniques have similar expected statistical sensitivities and similar estimated systematic uncertainties.

4.1 Invariant mass reconstruction

The three methods for extracting M_W use nearly identical procedures to reconstruct the invariant mass of the W candidates. The description here applies to the reweighting method. Small variations relevant for the alternative analyses are discussed in Section 4.3.

In previous OPAL measurements of M_W the tracks and clusters in selected $W^+W^- \rightarrow q\bar{q}q\bar{q}$ events were grouped into four jets using the Durham algorithm [26]. For the results presented here, $W^+W^- \rightarrow q\bar{q}q\bar{q}$ events are grouped into either four or five jet topologies depending on the value of $\ln(y_{45})$, where y_{45} is the value of the Durham jet resolution parameter at which the transition from 5 to 4 jets occurs. Events with $\ln(y_{45}) > -5.6$ are treated as five jets. This separation allows for the possibility of hard gluon radiation from one of the quarks and is found to improve the expected statistical sensitivity to M_W by approximately 5% compared with treating all events as four jets. The improvement in statistical sensitivity comes from events where, under the four jet hypothesis, a gluon jet from one W boson is combined with a quark jet from a different W boson. In the semi-leptonic decay channels, $W^+W^- \rightarrow q\bar{q}\ell\nu_\ell$, the lepton candidate is removed and the hadronic part of the event is reconstructed as two jets. The division of $W^+W^- \rightarrow q\bar{q}\ell\nu_\ell$ events into two and three jet would not improve the mass resolution. After the association of tracks and clusters into jets, corrections derived from the Monte Carlo simulation are applied to the measured jet momenta to account for double counting from particles which deposit energy in more than one sub-detector [27].

The invariant masses of the two W bosons can be determined directly from the reconstructed momenta of the observed decay products. However, the mass resolution is limited by the relatively large uncertainty on the measured energies of the jets, $\sigma_E/E \approx 20\%$, rather than by uncertainties on the measured jet directions. For this reason the use of a kinematic fit which imposes the four constraints of energy and momentum conservation [28] (4-C fit) significantly improves the invariant mass resolution. The improvements mainly arise from the energy in event being constrained to the well measured centre-of-mass energy. The output of the 4-C fit consists of two reconstructed masses per event, one for each W boson in the final state. The resolution of the kinematic fit can be improved by imposing a further constraint that the masses of the two reconstructed W boson candidates are equal (5-C fit), yielding a single reconstructed mass per event. For $W^+W^- \rightarrow q\bar{q}\ell\nu_\ell$ events the three unmeasured variables corresponding to the neutrino momentum means that the effective number of constraints in the semi-leptonic is two, giving a 2-C fit. For the results presented in this paper, the mass reconstruction is performed using the 5-C fit for $W^+W^- \rightarrow q\bar{q}q\bar{q}$ events and the 2-C fit for $W^+W^- \rightarrow q\bar{q}\ell\nu_\ell$ events.

A common kinematic fitting algorithm is used for $W^+W^- \rightarrow q\bar{q}e\nu_e$, $W^+W^- \rightarrow q\bar{q}\mu\nu_\mu$ and $W^+W^- \rightarrow q\bar{q}q\bar{q}$ events. The fitted mass is obtained using an iterative χ^2 -minimisation procedure where the constraints in the kinematic fit are implemented using Lagrange multipliers. The presence of initial state radiation (ISR) is neglected. The corrected jet momenta, their associated errors, and the measured jet masses are input to the kinematic fit. The errors on the measured jet momenta

are parameterised by expressions derived from Monte Carlo studies, which are functions of the visible energy and polar angle of the jet. The jet masses are fixed to their measured values. This is found to improve the mass resolution from the fit compared to treating jets as massless and also to reduce the bias in the fitted mass distribution.

The mass reconstruction for $W^+W^- \rightarrow qq\tau\nu_\tau$ events is different. In the $W^+W^- \rightarrow qq\tau\nu_\tau$ system, the absence of a measurement of the tau lepton energy means that the W mass information is determined entirely by the hadronic system. The absence of a measurement of the tau lepton energy reduces the effective number of constraints in the kinematic to one. Previously [10] the reconstructed mass in $W^+W^- \rightarrow qq\tau\nu_\tau$ events was obtained from the invariant mass of the jet-jet system, scaled by the ratio of the beam energy to the sum of the jet energies. For the results presented here an analytic formula which reproduces the results of the 1-C kinematic fit is used.

For $W^+W^- \rightarrow qqe\nu_e$ and $W^+W^- \rightarrow qq\mu\nu_\mu$ events the lepton direction is taken to coincide with the direction of the track associated with the electron or muon candidate. The energy is estimated from the associated electromagnetic calorimeter cluster for electrons and from the momentum of the track for muons. Unassociated electromagnetic clusters close to the lepton track, consistent with being from final state radiation (FSR), are included in the energy calculation. For each event a single mass is determined from a 2-C kinematic fit. In addition to the fitted mass, m_{rec} , the error on the fitted mass, σ_{rec} , and the χ^2 fit probability, P_{FIT} , are calculated. Events with $m_{\text{rec}} > 65$ GeV and $P_{\text{FIT}} > 0.001$ are retained. About half of the $W^+W^- \rightarrow qq\tau\nu_\tau$ events selected as either $W^+W^- \rightarrow qqe\nu_e$ or $W^+W^- \rightarrow qq\mu\nu_\mu$ fail these. The mass information is recovered by treating events with $m_{\text{rec}} < 65$ GeV or $P_{\text{FIT}} < 0.001$ as $W^+W^- \rightarrow qq\tau\nu_\tau$ events. In addition, about 4% of selected $W^+W^- \rightarrow qqe\nu_e$ and $W^+W^- \rightarrow qq\mu\nu_\mu$ events have the identified lepton beyond the effective tracking acceptance of the OPAL detector, within 20° of the beam axis, in which case the lepton energy is either poorly measured or not measured at all. These events are included in the $W^+W^- \rightarrow qq\tau\nu_\tau$ channel. The numbers of events used in each of the $W^+W^- \rightarrow qq\ell\nu_\ell$ channels are given in Table 1.

The situation for $W^+W^- \rightarrow qqqq$ events is complicated by the fact that there are three possible assignments of four jets to the two W bosons. For events reconstructed as five jets there are ten possible assignments of the jets to the W bosons. Incorrect combinations contain little or no information on the mass of the W boson. The incorrect jet-pairings result in a combinatorial background. For each $W^+W^- \rightarrow qqqq$ event, three (or ten) kinematic fits are performed, corresponding to the possible jet-pairings. To eliminate poorly reconstructed events and reduce backgrounds, only combinations which give a successful 5-C kinematic fit with a resulting χ^2 fit probability $P_{\text{FIT}} > 0.01$ and $m_{\text{rec}} > 65$ GeV are considered. A multivariate relative likelihood discriminant similar to that described in [10] is employed to pick out a single combination for each event and reduce combinatorial background. Different variables are used for the jet-pairing likelihoods for the four and five jet cases. For four jet events, the combination used in the fit is selected on the basis of two variables: the difference between the two fitted masses from the 4-C fit and the sum of the di-jet opening angles. In the five jet sample four variables are used: the 5-C fit mass, the difference between the two fitted masses from the 4-C fit, the minimum opening angle between the jets in the system assigned as $W^\pm \rightarrow q\bar{q}g$ and the cosine of the polar angle of the reconstructed $W^\pm \rightarrow q\bar{q}g$ system. For events reconstructed as four (five) jets, the combination corresponding to the largest jet-pairing likelihood is retained provided it has a likelihood output exceeding 0.40(0.42). Monte Carlo studies indicate that in 89% (70%) of the surviving signal events, the selected combination corresponds to the correct jet-pairing. The number of surviving events in the $W^+W^- \rightarrow qqqq$ channel is given in Table 1. Figure 1 shows the reconstructed mass distributions in both four and five jet channels before and after the jet-pairing likelihood cuts.

For events without ISR the average m_{rec} resolution (as defined in [10]) for the correct jet pairing in $W^+W^- \rightarrow qqqq$ events is 1.7 GeV. For $W^+W^- \rightarrow qq\ell\nu_\ell$ events the average m_{rec} resolution is

2.4 GeV, 2.8 GeV and 3.4 GeV in the $W^+W^- \rightarrow qqe\nu_e$, $W^+W^- \rightarrow qq\mu\nu_\mu$ and $W^+W^- \rightarrow qq\tau\nu_\tau$ channels respectively.

4.2 Extraction of the W mass and width

The Monte Carlo reweighting technique is used to provide the central results of this paper. The W boson mass and width are measured by directly comparing the reconstructed mass spectra in the data to Monte Carlo mass spectra corresponding to different values of M_W and Γ_W . A likelihood fit is then used to extract M_W and Γ_W by determining which Monte Carlo spectrum best describes the data. The Monte Carlo spectra for arbitrary (M_W, Γ_W) are obtained using the reweighting technique described in [9]. In previous OPAL publications, W^+W^- Monte Carlo samples generated using only CC03 diagrams were reweighted using the ratio of Breit-Wigner functions. For this analysis, KORALW $e^+e^- \rightarrow 4f$ reference samples generated with $(M_W = 80.33 \text{ GeV}, \Gamma_W = 2.093 \text{ GeV})$ are reweighted to (M'_W, Γ'_W) using the ratio of Breit-Wigner functions. The reference samples used for the reweighting include only final states which have contributions from diagrams involving the W propagator. This procedure is found to give a good approximation to the more exact treatment of using the full four-fermion matrix elements, introducing a bias of less than 5 MeV in the $W^+W^- \rightarrow qqe\nu_e$ channel and less than 2 MeV in the other channels. Using the ratio of Breit-Wigner functions rather than four-fermion matrix elements results in a much faster fit.

The mass spectra for background events are taken from Monte Carlo and are assumed to be independent of M_W and Γ_W . The main sources of background are $e^+e^- \rightarrow Z^0/\gamma \rightarrow q\bar{q}$ and four-fermion processes. The background mass distributions are normalised to the expected number of background events. The reweighted signal spectra are then normalised such that the total number of signal plus background events corresponds to the observed number of events. This is done separately for the $W^+W^- \rightarrow qq\bar{q}q$, $W^+W^- \rightarrow qqe\nu_e$, $W^+W^- \rightarrow qq\mu\nu_\mu$ and $W^+W^- \rightarrow qq\tau\nu_\tau$ channels, with the $W^+W^- \rightarrow qq\bar{q}q$ channel split into four and five jet topologies. In addition, the $W^+W^- \rightarrow qq\ell\nu_\ell$ channels are divided into four subsamples according to the error on the reconstructed invariant mass, σ_{rec} . This division gives a larger weight to events with reconstructed masses which are known with better precision (*i.e.* small σ_{rec}) and reduces the expected statistical uncertainty on the fitted W mass from the $W^+W^- \rightarrow qq\ell\nu_\ell$ channels by approximately 5%. In the $W^+W^- \rightarrow qq\bar{q}q$ channels, the width of the reconstructed mass distribution is dominated by the intrinsic width of the W. Consequently a similar subdivision into bins of σ_{rec} does not improve the M_W sensitivity. However, jet-pairings which give a large jet-pairing likelihood are more likely to be correct and have a better mass resolution as shown in Figure 2. For this reason, the $W^+W^- \rightarrow qq\bar{q}q$ events reconstructed as four jets are subdivided into four bins of jet-pairing likelihood, resulting in a 7% improvement in the statistical sensitivity to M_W . No subdivision is performed for the five jet events.

A binned log-likelihood fit to the m_{rec} distributions of the data is performed in the range $m_{\text{rec}} > 65 \text{ GeV}$. The log-likelihood function is identical to that used previously [10]. A log-likelihood curve is determined separately for each channel. For the $W^+W^- \rightarrow qq\ell\nu_\ell$ channels, the results are obtained by adding the log-likelihood curves separately determined from each channel in each bin of σ_{rec} . For the $W^+W^- \rightarrow qq\bar{q}q$ channel, the results are obtained by adding the likelihood curves obtained from the five jet events to the likelihood curves obtained from the four bins of jet-pairing likelihood for events reconstructed as four jets.

Two types of fit are performed. In the one parameter fit, Γ_W is constrained by the SM relation [16],

$$\Gamma_W = 3G_F M_W^3 (1 + 2\alpha_S/3\pi)/(2\sqrt{2}\pi), \quad (1)$$

and only M_W is determined. The results of this fit for each channel are given in Table 2 and displayed in Figure 3. The combined result is discussed in Section 6. In the two parameter fit, both M_W and Γ_W are determined simultaneously.

In the reweighting method the fitted parameters are expected to be unbiased since any offsets in the reconstructed mass introduced in the analysis are implicitly accounted for in the Monte Carlo reconstructed mass spectra used in the reweighting procedure. This is verified using several Monte Carlo samples generated at various M_W and Γ_W . In addition, tests using a large ensemble of Monte Carlo subsamples, each corresponding to 183 pb^{-1} and including background contributions, are used to verify for each channel separately and for all channels combined, that the measured fit errors accurately reflect the root-mean-squared spread of the residual distribution for both the M_W and Γ_W fits. Since M_W in the Monte Carlo corresponds to the running width definition, so does the fitted mass. The expected statistical error on the W mass from the combination of the $qq\ell\nu_\ell$ and $qqqq$ channels is $76 \pm 1 \text{ MeV}$, where the weights given to the two channels are determined by the both statistical and systematic error contributions. The quoted uncertainty on the expected statistical error is from Monte Carlo statistics.

4.3 Alternative fit methods

4.3.1 Breit-Wigner fit

The Breit-Wigner method is analogous to that described in [10]. It employs an unbinned maximum-likelihood fit to the reconstructed mass spectrum using an analytic Breit-Wigner function to describe the mass spectrum from $e^+e^- \rightarrow W^+W^-$. Due to initial-state radiation, the reconstructed mass spectrum is asymmetric. For the $W^+W^- \rightarrow qq\ell\nu_\ell$ channels a relativistic Breit-Wigner function, with different widths above and below the peak, gives a satisfactory description of the m_{rec} lineshape. The fitting function used is

$$S(m_{\text{rec}}) = A \frac{m_{\text{rec}}^2 \Gamma_{+(-)}^2}{(m_{\text{rec}}^2 - m_0^2)^2 + m_{\text{rec}}^2 \Gamma_{+(-)}^2}, \quad (2)$$

where $\Gamma_{+(-)}$ is the width assumed for all m_{rec} above (below) the peak centred at m_0 . This empirical choice of fitting function provides an adequate description for samples up to ten times the integrated luminosity of the data. The widths, $\Gamma_{+(-)}$, are fixed to values determined from fits to W^+W^- signal Monte Carlo samples. Different widths are obtained for each $W^+W^- \rightarrow qq\ell\nu_\ell$ decay channel. The shapes of the background distributions and the background fractions are determined from Monte Carlo. The background fractions are held constant in the fit. The fit is restricted to the range $70 < m_{\text{rec}} < 88 \text{ GeV}$.

In the $W^+W^- \rightarrow qqqq$ channel events are divided into four and five jet samples which are fitted separately. The division is made on the basis of the 5-C kinematic fit probability. Events are reconstructed as five jets if any of the ten possible jet-pairings in the five jet assignment gives a fit probability which is greater than twice that of highest probability of the three jet-pairings for the four jet hypothesis. For both four jet and five jet samples, the fitting function $S(m_{\text{rec}})$ is multiplied by $G(m_{\text{rec}}) = \exp[-(m_0 - m_{\text{rec}})^2/2\sigma^2]$. This empirical choice provides a good description of the reconstructed mass spectra in the fit range for $W^+W^- \rightarrow qqqq$ events. The value of σ is determined from Monte Carlo. For the four jet $W^+W^- \rightarrow qqqq$ sample either one or two jet-pairings are used following the procedure described in [9]. In the five jet sample, a jet-pairing likelihood is used. Here the variables used in the likelihood are those used for the reweighting fit described in Section 4.1, with the exception that the 5-C fit mass is not included.

In contrast to the procedure employed for the reweighting method, the $W^+W^- \rightarrow qq\ell\nu_\ell$ events are not divided into subsamples according to σ_{rec} nor are the $W^+W^- \rightarrow qqqq$ events divided into subsamples according to the jet-pairing likelihood. However, $W^+W^- \rightarrow qq\tau\nu_\tau$ events are sub-divided into fully-leptonic and semi-leptonic decays of the tau lepton.

The fitted mass, m_0 , must be corrected for offsets not accounted for in the fit, *e.g.* from initial-state radiation and event selection. The correction is determined using fully simulated Monte Carlo samples generated at different values of M_W with the expected background contributions included and is found to depend linearly on M_W . The results from the $W^+W^- \rightarrow qqqq$ and $W^+W^- \rightarrow qq\ell\nu_\ell$ channels, after correction, are given in Table 3. The expected statistical error on the combined W mass measurement is 78 ± 2 MeV.

4.3.2 Convolution fit

The convolution method [16, 12] attempts to exploit all available information by constructing a likelihood curve for each selected event. The likelihood is calculated using a functional form

$$\mathcal{L}(M_W, m_{\text{rec}}) = p_s \mathcal{P}_s(M_W, m_{\text{rec}}),$$

where p_s is the probability of a candidate event being a true signal event and \mathcal{P}_s is the probability function for M_W given the observed reconstructed mass, m_{rec} . The function $\mathcal{P}_s(M_W, m_{\text{rec}})$ is defined as

$$\mathcal{P}_s(M_W, m_{\text{rec}}) = \text{BW}(M_W, m, s') \otimes \text{ISR}(s, s') \otimes \text{R}(m, m_{\text{rec}}),$$

where $\text{BW}(M_W, m, s')$ is the relativistic Breit-Wigner function for producing off-shell W bosons with mass m for a W mass of M_W including the effects of phase space. Γ_W is fixed relative to M_W using Equation 1. The radiator function, $\text{ISR}(s, s')$, is used to account for the effects of ISR (on a statistical basis). The inclusion of this term accounts for the fact that in the kinematic fit the observed energy is constrained to \sqrt{s} , where in reality the effective centre-of-mass energy, $\sqrt{s'}$, depends on the amount of ISR. Finally, $\text{R}(m, m_{\text{rec}})$ is the probability density function relating the experimentally reconstructed mass, m_{rec} , to the average of the two true masses, m , of the off-shell W bosons in the event.

In the $W^+W^- \rightarrow qq\ell\nu_\ell$ channels, the full error information on the fitted mass of each event is used in an unbinned maximum likelihood fit. In a previous OPAL publication [10], the event probability function, $\text{R}(m, m_{\text{rec}})$, was assumed to be Gaussian with its central value and standard deviation taken from a 2-C kinematic fit. In this analysis, the 2-C fit is modified, replacing the equal W mass constraint by one in which the masses are individually constrained to a given W boson mass, m . The χ^2 distribution from this fit is converted into the event probability density function, $\text{R}(m, m_{\text{rec}})$, which is non-Gaussian.

In the $W^+W^- \rightarrow qqqq$ channel, all events are forced into a five jet topology. A relative likelihood, constructed from the difference between the reconstructed masses in a 4-C kinematic fit, is used to select on average about three jet-pairings per event thereby reducing significantly the combinatorial background. In the Monte Carlo 92% of selected events the correct jet-pairing combination is used in the fit. The convolution is performed in two dimensions, namely the reconstructed masses of the two W bosons, with joint probability density functions corresponding to each jet-pairing obtained from the 4-C kinematic fit. The probability density functions for the different combinations are added to form an event probability density function [12].

In both channels the log-likelihood curves from each selected event are summed to yield a single curve from which a fitted mass is determined. The fitted mass is corrected for offsets not accounted for

in the fit in the manner described for the Breit-Wigner fit. The results from the $W^+W^- \rightarrow q\bar{q}q\bar{q}$ and $W^+W^- \rightarrow q\bar{q}\ell\nu_\ell$ channels, after all corrections, are given in Table 3. The expected statistical error on the combined W mass measurement is 72 ± 2 MeV. The total combined expected error, statistical and systematic, from the convolution method is slightly smaller than that obtained from the reweighting fit. However, at present the reweighting fit is the only method in which a simultaneous fit for (M_W, Γ_W) is implemented. For this reason, and for consistency with previous OPAL publications, the reweighting method is retained for the results given in this publication.

5 Systematic Uncertainties

The systematic uncertainties for the measurement of M_W using the reweighting method are estimated as described below and summarised in Table 4. The contributions from each of the sources are added in quadrature to yield the total systematic uncertainty. All contributions were evaluated for both the M_W and Γ_W determinations. For the alternative analyses, the systematics are estimated similarly and yield comparable results. The determination of the individual systematic uncertainties is described below.

5.1 Beam energy

The average LEP beam energy is currently known with a precision of 20 MeV [19] which leads to a systematic uncertainty of 16 MeV on M_W and 2 MeV on Γ_W . The RMS spread in the LEP centre-of-mass energy of 237 ± 12 MeV [19] and the average difference between the electron and positron beam energies results in negligible impact on the measurement of M_W . The Monte Carlo does not include the intrinsic beam energy spread. This introduces a bias of +10 MeV to the value of Γ_W obtained from the reweighting fit. A -10 MeV correction is applied and the size of the correction taken as an additional systematic uncertainty on the measurement Γ_W .

5.2 Initial state radiation

The main KORALW Monte Carlo samples include an $\mathcal{O}(\alpha^3)$ treatment of initial state radiation (ISR). The systematic error associated with ISR is estimated by reweighting the generated KORALW events to correspond to an $\mathcal{O}(\alpha^2)$ or $\mathcal{O}(\alpha)$ treatment of ISR using the matrix elements calculated in KORALW. The resulting shifts from the comparison of $\mathcal{O}(\alpha^3)$ to $\mathcal{O}(\alpha)$ are less than 2 MeV and are neglected.

5.3 Full $\mathcal{O}(\alpha)$ corrections

In the process $e^+e^- \rightarrow 4f\gamma$ ISR diagrams dominate. The accuracy of the treatment of ISR in the KORALW generator is sufficient for this analysis. However the KORALW generator does not include all $\mathcal{O}(\alpha)$ effects. For example, interference between ISR and FSR graphs and photon radiation from the W bosons are not implemented. Recent calculations using the double-pole approximation indicate that possible mass biases of order 10 MeV could arise [29]. However, these estimates were based on generator level studies which compared mass distributions from the full $\mathcal{O}(\alpha)$ treatment with the corresponding Born level treatment which does not include any final state radiation. To obtain a proper estimate of the potential mass bias when applied to the experimental measurement it would

be necessary to use the full OPAL detector simulation and mass reconstruction procedure. Currently this is not possible since the necessary Monte Carlo programs are not yet available. For this paper possible systematic biases from the full $\mathcal{O}(\alpha)$ treatment of photon radiation are not included since the size of the effect is significantly smaller than the current statistical precision of the M_W measurement.

5.4 Hadronisation in $W^\pm \rightarrow q\bar{q}$ decays

The KORALW Monte Carlo samples taken as references in the extraction of M_W use the LUND string model as implemented in JETSET for the simulation of the hadronisation² of $W^\pm \rightarrow q\bar{q}$ decays. The JETSET model was tuned to OPAL hadronic data recorded at the Z^0 resonance [30]. The model was tuned to describe event shape variables and inclusive particle production rates. To assess a possible systematic error from the uncertainties in the tuning of the JETSET model, the JETSET parameters σ_q , b , Λ_{QCD} and Q_0 are each varied in turn by $\pm 1\sigma$ about their tuned values at the Z^0 [30]. The maximum resulting biases to the fitted values of M_W from these high statistics samples are 30 MeV and 20 MeV in the $qq\ell\nu_\ell$ and $qqqq$ channels respectively. In addition, an earlier OPAL tune of the JETSET model is used. This version was tuned to describe global event shape variables alone [31]. The resulting differences in the fitted value of M_W using the earlier OPAL tune are (-33 ± 14) MeV and (-30 ± 12) MeV in the $W^+W^- \rightarrow qqqq$ and $W^+W^- \rightarrow qq\ell\nu_\ell$ channels respectively.

As a further test of hadronisation uncertainties, the JETSET string model is replaced by the HERWIG cluster model. For this comparison, two samples were generated using the same W^+W^- final states and differing only in the hadronisation modelling. The resulting fitted mass values from the reweighting method from JETSET and HERWIG are compared. Differences (JETSET-HERWIG) of (-18 ± 14) MeV and (-11 ± 12) MeV are obtained for the $W^+W^- \rightarrow qq\ell\nu_\ell$ and $W^+W^- \rightarrow qqqq$ channels. A similar comparison is made using the ARIADNE colour dipole model [32]. Differences (JETSET-ARIADNE) of $(+15 \pm 14)$ MeV and $(+6 \pm 12)$ MeV are obtained for the $W^+W^- \rightarrow qq\ell\nu_\ell$ and $W^+W^- \rightarrow qqqq$ channels.

On the basis of these comparisons systematic uncertainties of 30 MeV are assigned to the W mass measurements from both $W^+W^- \rightarrow qq\ell\nu_\ell$ and $W^+W^- \rightarrow qqqq$. The hadronisation uncertainty is taken to be fully correlated between the two channels. For the measurement of Γ_W the corresponding systematic errors in the $W^+W^- \rightarrow qq\ell\nu_\ell$ and $W^+W^- \rightarrow qqqq$ channels are 25 MeV and 60 MeV respectively.

5.5 Detector calibration and simulation

The effects of detector mis-calibrations and deficiencies in the Monte Carlo are investigated by varying the jet and lepton energy scales over reasonable ranges. The ranges used for the systematic variations are dependent on polar angle and are determined from detailed comparisons of data and Monte Carlo utilising both data recorded at 189 GeV and 3.1 pb⁻¹ of data collected at $\sqrt{s} \approx M_Z$ during 1998. From $e^+e^- \rightarrow e^+e^-$ events the electro-magnetic calorimeter energy scale is known to 0.3%. Similarly from $e^+e^- \rightarrow Z^0 \rightarrow \mu^+\mu^-$ events, the uncertainty on momentum scale from the tracking detectors is determined to be 0.3%. These scale uncertainties dominate the detector related systematics in the $W^+W^- \rightarrow qqe\nu_e$ and $W^+W^- \rightarrow qq\mu\nu_\mu$ channels, and are 14 MeV and 16 MeV respectively. Uncertainties on energy (momentum) resolution and angular resolution are also evaluated but have much smaller impact. Uncertainties on the jet energy scale are determined from $e^+e^- \rightarrow Z^0 \rightarrow q\bar{q}$

²In this paper hadronisation refers to the process whereby the quarks produced in W decays produce the hadrons observed in the detector including the development of the parton shower.

events to be 0.2%–1.0% depending on the polar angle. The dominant effect of the jet energy scale uncertainty is a 6 MeV uncertainty in the $W^+W^- \rightarrow qq\tau\nu_\tau$ channel. In the $W^+W^- \rightarrow qqqq$ channel the sensitivity to the overall jet energy scale is greatly reduced due to the kinematic fit. Here the dominant effect is from the global uncertainty in the jet polar angle scale, *i.e.* the relative length-to-width scale of the detector, resulting in a 3 MeV uncertainty on the W mass. The linearity of the jet energy scale is checked using $e^+e^- \rightarrow Z^0 \rightarrow q\bar{q}$ events with a clear three-jet topology. For the measurement of Γ_W the main systematic error arises from uncertainties in the jet energy scale and resolution and is 47 MeV in both $W^+W^- \rightarrow qq\ell\nu_\ell$ and $W^+W^- \rightarrow qqqq$ channels.

5.6 Four-fermion modelling

Possible systematic effects associated with the modelling of the four-fermion final state, including interference between W^+W^- diagrams and other four-fermion processes, are investigated by comparing the `grc4f` and the `EXCALIBUR` [33] generators. The comparison is performed using the ratio of the `EXCALIBUR` to `grc4f` four-fermion matrix elements to reweight the `KORALW` Monte Carlo sample. This procedure avoids introducing an additional statistical error associated with generating additional Monte Carlo. The resulting shift in the reconstructed mass is 1 ± 1 MeV in the $W^+W^- \rightarrow qq\ell\nu_\ell$ channel and 0 ± 1 MeV in the $W^+W^- \rightarrow qqqq$ channel. Similar results are obtained when the `EXCALIBUR` Monte Carlo is reweighted using the ratio of the `grc4f` to `EXCALIBUR` four-fermion matrix elements. Consequently no additional systematic uncertainty is assigned. The corresponding systematic uncertainties on the measurement of Γ_W , of order 30 MeV, are determined by the statistical precision of the comparisons. In the $W^+W^- \rightarrow qqe\nu_e$ channel an additional 5 MeV uncertainty is assigned, associated with using the Breit-Wigner functions in the reweighting fit.

5.7 Background treatment

Uncertainties in the modelling of background processes mainly arise from the simulation of the $Z^0/\gamma \rightarrow q\bar{q}$ background in the $W^+W^- \rightarrow qq\tau\nu_\tau$ and $W^+W^- \rightarrow qqqq$ channels. A number of systematic checks of the normalisation and shape of the $Z^0/\gamma \rightarrow q\bar{q}$ background are performed. The background normalisation in the reweighting fit is varied by one standard deviation, using the uncertainties evaluated in [25]. The `HERWIG` cluster model is used as an alternative to the `LUND` string model used in `PYTHIA`. In addition, for the $W^+W^- \rightarrow qqqq$ channel, data taken at $\sqrt{s} \approx M_Z$, scaled by $(189 \text{ GeV}/M_Z)$, are also substituted for the $Z^0/\gamma \rightarrow q\bar{q}$ background. The sum in quadrature of the above systematic shifts leads to the assignment of a background systematic error of 6 MeV in the $W^+W^- \rightarrow qqqq$ channel and 8 MeV in the $W^+W^- \rightarrow qq\ell\nu_\ell$ channel. The systematic error on Γ_W due to uncertainties in background modelling is 25 MeV and 41 MeV in the $W^+W^- \rightarrow qq\ell\nu_\ell$ and $W^+W^- \rightarrow qqqq$ channels respectively arising from differences between `JETSET` and `HERWIG` and uncertainties on the accepted background cross section.

5.8 Monte Carlo statistics

The finite statistics of the Monte Carlo samples used in the reweighting procedure result in an additional uncertainty of 10 MeV on the W mass determined separately in the $W^+W^- \rightarrow qqqq$ and $W^+W^- \rightarrow qq\ell\nu_\ell$ channels. The corresponding systematic uncertainties for the W width measurement are 51 MeV.

5.9 Final state interactions (FSI)

A significant bias to the apparent W mass measured in the $W^+W^- \rightarrow q\bar{q}q\bar{q}$ channel could arise if the hadronisation of the two W bosons is not independent [16,34]. At LEP2 energies, the decay length for W bosons is about 0.1 fm, significantly less than the typical hadronisation scale, approximately 1 fm. The hadronisation of the two W bosons in the $W^+W^- \rightarrow q\bar{q}q\bar{q}$ channel may have space-time overlap allowing possible final state interactions between the decay products of different W bosons. Two possible sources of final state interactions, both leading to non-independent hadronisation, have been widely considered: Colour Reconnection (CR) and Bose-Einstein Correlations (BEC). Whether these effects play a significant role at LEP2 has yet to be experimentally determined. As a result, to assign a systematic error related to possible final state interactions it is necessary to rely on phenomenological models. The strategy adopted here is to consider only those models for CR and BEC which are consistent with both LEP1 and LEP2 data.

The CR systematic error refers to possible biases in the W mass measurement arising from QCD reconnection effects in the non-perturbative phase. Reconnection effects in the perturbative phase, *i.e.* multiple gluon exchange between quarks from different W bosons, have been shown to be small [35]. To investigate the systematic biases originating from non-perturbative CR effects, the models implemented in the PYTHIA and ARIADNE [32] Monte Carlo generators are studied. In both cases the results from the mass fit to a Monte Carlo sample including CR effects are compared to the results obtained from the corresponding sample without colour reconnection. The results are summarised in Table 5. The largest biases are seen in the ARIADNE 2 and ARIADNE 3 models³. However, these models have been strongly disfavoured by studies of three jet events in LEP1 Z^0 data [37]. For this reason the current ARIADNE implementation of CR is not used to assign a systematic uncertainty. Of the remaining models considered, the SK I model [35] produces the largest bias. The SK Monte Carlo samples use the JETSET tune of [30], where the parton shower cut-off, which directly influences the behaviour of the CR model [35], was set to 1.9 GeV. The strength parameter k_i (also called ρ) of the SK I model was set to 0.9, corresponding to 35% of events being reconnected. A systematic uncertainty of 66 MeV on M_W is assigned. The corresponding uncertainty on Γ_W is 68 MeV.

As is the case in Z^0 decays, BEC between like-sign charged pions are observed in W^\pm decays at LEP2 [38]. These correlations are not implemented in the standard Monte Carlo programs used in this analysis. Correlations between pions from the same W do not affect significantly the global jet properties and are unlikely to bias the M_W measurement. If BEC exist between pions from different W bosons in $W^+W^- \rightarrow q\bar{q}q\bar{q}$ events, significant biases to the reconstructed value of M_W may arise. To investigate possible systematic biases from BEC, a sample of $W^+W^- \rightarrow q\bar{q}q\bar{q}$ events is produced using the PYTHIA Monte Carlo generator which includes BEC as described in [39]. For the evaluation of the systematic error the BEC model BE_{32} of [39] with $\lambda = 1.0$ and $R = 0.42$ fm is used. The difference in the fitted W mass between a sample generated with BEC between different W bosons and a sample generated with BEC only between particles from the same W is $+67 \pm 14$ MeV (different-same). The resulting systematic uncertainties on M_W and Γ_W from BEC in the $W^+W^- \rightarrow q\bar{q}q\bar{q}$ channel are 67 MeV and 39 MeV respectively.

5.10 Fit procedure

A comparison of the results from the reweighting method with those from the Breit-Wigner and convolution fits, summarised in Table 3, is used to test for residual biases in the reweighting method. The

³Following the notation used in [36,37].

expected RMS of the differences of the results from the three methods are determined using an ensemble of Monte Carlo subsamples including background, each corresponding to an integrated luminosity of 183 pb^{-1} . For each subsample the difference in the fitted M_W determined using the reweighting method and that determined using each of the other methods is calculated for the $W^+W^- \rightarrow \text{qqqq}$ and $W^+W^- \rightarrow \text{qq}\ell\nu_\ell$ channels. These differences have mean values consistent with zero and RMS values of approximately 54 MeV and 41 MeV (62 MeV and 84 MeV) when comparing the reweighting fits to the Breit-Wigner (convolution) fits in the $W^+W^- \rightarrow \text{qq}\ell\nu_\ell$ and $W^+W^- \rightarrow \text{qqqq}$ samples, respectively. Since the alternative analyses yield results consistent with those obtained using the default reweighting analysis, no additional systematic error is assigned.

6 Results

For the reweighting method described in Section 4.2, the results of a simultaneous fit to M_W and Γ_W from the combined $W^+W^- \rightarrow \text{qqqq}$ and $W^+W^- \rightarrow \text{qq}\ell\nu_\ell$ event samples are

$$\begin{aligned} M_W &= 80.451 \pm 0.076(\text{stat.}) \pm 0.050(\text{syst.}) \text{ GeV}, \\ \Gamma_W &= 2.09 \pm 0.18(\text{stat.}) \pm 0.09(\text{syst.}) \text{ GeV}. \end{aligned}$$

The correlation coefficient between M_W and Γ_W is 0.04. For this fit, the central values are determined by adding the log-likelihood curves from the $W^+W^- \rightarrow \text{qqqq}$ and $W^+W^- \rightarrow \text{qq}\ell\nu_\ell$ channels including the effects of systematic uncertainties. The likelihood contours for this fit are displayed in Figure 4.

A one parameter fit for the mass is performed by constraining the width using Equation 1 to give $M_W = 80.402 \pm 0.104(\text{stat.}) \pm 0.101(\text{syst.}) \text{ GeV}$ in the $W^+W^- \rightarrow \text{qqqq}$ channel, and $M_W = 80.478 \pm 0.104(\text{stat.}) \pm 0.038(\text{syst.}) \text{ GeV}$ in the $W^+W^- \rightarrow \text{qq}\ell\nu_\ell$ channel. The combined result, taking into account the correlated systematics between the $W^+W^- \rightarrow \text{qqqq}$ and $W^+W^- \rightarrow \text{qq}\ell\nu_\ell$ channels, is

$$M_W = 80.451 \pm 0.076(\text{stat.}) \pm 0.049(\text{syst.}) \text{ GeV}.$$

Due to the larger systematic errors in the $W^+W^- \rightarrow \text{qqqq}$ channel, mainly from FSI, it carries a reduced weight of 0.36 in the combination. The combined $W^+W^- \rightarrow \text{qqqq}$ and $W^+W^- \rightarrow \text{qq}\ell\nu_\ell$ results from the alternative analyses, after all corrections, are for the Breit-Wigner fit, $M_W = 80.436 \pm 0.078(\text{stat.}) \pm 0.050(\text{syst.}) \text{ GeV}$, and for the convolution fit, $M_W = 80.378 \pm 0.073(\text{stat.}) \pm 0.051(\text{syst.}) \text{ GeV}$.

6.1 Combination with previous data

The results presented in this paper, based on 183 pb^{-1} of data, are combined with previous OPAL measurements of M_W from direct reconstruction at $\sqrt{s} \approx 172 \text{ GeV}$ [9] and at $\sqrt{s} \approx 183 \text{ GeV}$ [10]. The results in the $W^+W^- \rightarrow \text{qq}\ell\nu_\ell$ and $W^+W^- \rightarrow \text{qqqq}$ channels are combined independently taking into account systematic uncertainties which are correlated between data from the different centre-of-mass energies, giving:

$$\begin{aligned} M_W(W^+W^- \rightarrow \text{qq}\ell\nu_\ell) &= 80.441 \pm 0.086(\text{stat.}) \pm 0.034(\text{syst.}) \pm 0.017(\text{lep}) \text{ GeV}, \\ M_W(W^+W^- \rightarrow \text{qqqq}) &= 80.409 \pm 0.093(\text{stat.}) \pm 0.034(\text{syst.}) \pm 0.016(\text{lep}) \pm 0.094(\text{fsi}) \text{ GeV}. \end{aligned}$$

where the uncertainties from the LEP beam energy (lep) and from final state interactions (fsi) are quoted separately. In the combination the systematic uncertainties for the colour reconnection and Bose-Einstein correlations of the previous data were set to those presented in this paper.

The difference between the fitted M_W in the $W^+W^- \rightarrow qqqq$ and $W^+W^- \rightarrow qq\ell\nu_\ell$ channels is $\Delta M_W \equiv (M_W^{\text{qqqq}} - M_W^{\text{qq}\ell\nu_\ell}) = -0.032 \pm 0.127(\text{stat.}) \pm 0.047(\text{syst.})$ GeV. A significant non-zero value for ΔM_W could indicate that FSI effects are biasing the value of M_W determined from $W^+W^- \rightarrow qqqq$ events. The systematic error on the quoted value of ΔM_W does not include contributions from CR/BEC effects. For the ΔM_W measurement the hadronization systematic uncertainties in the $W^+W^- \rightarrow qqqq$ and $W^+W^- \rightarrow qq\ell\nu_\ell$ channels are taken to be uncorrelated; a conservative choice in the absence of a good estimate of the true correlation coefficient.

The M_W results from direct reconstruction in the $W^+W^- \rightarrow qq\ell\nu_\ell$ and $W^+W^- \rightarrow qqqq$ channels are combined with the OPAL measurement of M_W from the W^+W^- production cross-section at $\sqrt{s} \approx 161$ GeV [8]. The combination is made assuming that the mass measurements from direct reconstruction and from the threshold cross-section are uncorrelated, apart from the uncertainty associated with the LEP beam energy, which is taken to be fully correlated. The direct reconstruction measurements from the $W^+W^- \rightarrow qq\ell\nu_\ell$ and $W^+W^- \rightarrow qqqq$ channels from three different centre-of-mass energies are combined using the full covariance matrix. The combined result is

$$M_W = 80.432 \pm 0.066(\text{stat.}) \pm 0.032(\text{syst.}) \pm 0.028(\text{fsi}) \pm 0.017(\text{lep}) \text{ GeV.}$$

The measurement of Γ_W presented in this paper is combined with the previous OPAL measurements from direct reconstruction [9, 10] to give

$$\Gamma_W = 2.04 \pm 0.16(\text{stat.}) \pm 0.09(\text{syst.}) \text{ GeV.}$$

For the earlier data, with relatively low statistics, the measured statistical error is correlated with the measured width. Consequently, to avoid biasing the combination, the separate width measurements are weighted using the expected statistical error rather than the measured statistical error.

7 Summary

Using the 183 pb^{-1} of data recorded by the OPAL detector at a mean centre-of-mass energy of approximately 189 GeV, a total of 2088 $W^+W^- \rightarrow qqqq$ and $W^+W^- \rightarrow qq\ell\nu_\ell$ candidate events are used in a fit constraining Γ_W using Equation 1 to obtain a direct measurement of the W boson mass, $M_W = 80.451 \pm 0.076(\text{stat.}) \pm 0.049(\text{syst.})$ GeV, while a second fit is used to determine directly the width of the W boson, $\Gamma_W = 2.09 \pm 0.18(\text{stat.}) \pm 0.09(\text{syst.})$ GeV.

The results described in this paper are combined with the previous OPAL results from data recorded at $\sqrt{s} \approx 161 - 183$ GeV [8–10]. From this combined data sample the W boson mass is determined to be

$$M_W = 80.432 \pm 0.066(\text{stat.}) \pm 0.045(\text{syst.}) \text{ GeV.}$$

This result is consistent with both the other direct measurements and the indirect value inferred from fits to electroweak data [3]. It should be noted that the systematic error is dominated by the uncertainties arising from hadronisation and final state interactions. For future LEP combinations these uncertainties will need to be reduced to benefit from the ultimate LEP combined statistical uncertainty of about 25 MeV.

The result for the W boson width is combined with the previous OPAL result from data recorded at $\sqrt{s} \approx 172 - 183$ GeV to obtain

$$\Gamma_W = 2.04 \pm 0.16(\text{stat.}) \pm 0.09(\text{syst.}) \text{ GeV.}$$

This measurement of Γ_W is in good agreement with the Standard Model expectation and with other direct measurements at LEP [12, 13, 40] and at the Tevatron [41].

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References

- [1] S.L. Glashow, J. Iliopoulos, and L. Maiani, Phys. Rev. **D2** (1970) 1285;
S. Weinberg, Phys. Rev. Lett. **19** (1967) 1264;
A. Salam, *Elementary Particle Theory*, ed. N. Svartholm (Almquist and Wiksells, Stockholm, 1968), 367.
- [2] ALEPH Collaboration, R. Barate *et al.*, Eur. Phys. J. **C14** (2000) 1;
DELPHI Collaboration, “*Cross-Sections and Leptonic Forward-Backward Asymmetries from the Z^0 running of LEP*”, CERN-EP/2000-037, Accepted by Eur. Phys. J. C;
L3 Collaboration, M. Acciarri *et al.*, CERN-EP/2000-022, “*Measurements of Cross-Sections and Forward Backward Asymmetries at the Z^0 Resonance and Determination of Electroweak Parameters*” Accepted by Eur. Phys. J. C;
OPAL Collaboration, R. Akers *et al.*, Z. Phys. **C61** (1994) 19.
- [3] LEP Electroweak Working Group, CERN-EP/2000-016.
- [4] ALEPH Collaboration, R. Barate *et al.*, Phys. Lett. **B462** (1999) 389 ;
DELPHI Collaboration, P. Abreu *et al.*, Phys. Lett. **B459** (1999) 382 ;
L3 Collaboration, M. Acciarri *et al.*, Phys. Lett. **B467** (1999) 171 ;
OPAL Collaboration, G. Abbiendi *et al.*, Eur. Phys. J. **C8** (1999) 191.
- [5] CDF Collaboration, F. Abe *et al.*, Phys. Rev. Lett. **80** (1998) 2767;
CDF Collaboration, F. Abe *et al.*, Phys. Rev. Lett. **80** (1998) 2779;
D0 Collaboration, B. Abbott *et al.*, Phys. Rev. **D60** (1999) 052001;
D0 Collaboration, B. Abbott *et al.*, Phys. Rev. **D58** (1998) 052001.
- [6] G. Degrossi *et al.*, Phys. Lett. **B418** (1998) 209.
- [7] W.J. Marciano and A. Sirlin, Phys. Rev. **D29** (1984) 945.
- [8] OPAL Collaboration, K. Ackerstaff *et al.*, Phys. Lett. **B389** (1996) 416.
- [9] OPAL Collaboration, K. Ackerstaff *et al.*, Eur. Phys. J. **C1** (1998) 395.
- [10] OPAL Collaboration, G. Abbiendi *et al.*, Phys. Lett. **B453** (1999) 138.
- [11] ALEPH Collaboration, R. Barate *et al.*, Phys. Lett. **B453** (1999) 121.
- [12] DELPHI Collaboration, P. Abreu *et al.*, Phys. Lett. **B462** (1999) 410.
- [13] L3 Collaboration, M. Acciarri *et al.*, Phys. Lett. **B454** (1999) 386.
- [14] CDF Collaboration, F. Abe *et al.*, Phys. Rev. Lett. **65** (1990) 2243;
CDF Collaboration, F. Abe *et al.*, Phys. Rev. Lett. **75** (1995) 11;
D0 Collaboration, S. Abachi *et al.*, Phys. Rev. Lett. **84** (2000) 222;
UA1 Collaboration, C. Albajar *et al.*, Z. Phys. **C44** (1989) 15;
UA2 Collaboration, J. Alitti *et al.*, Phys. Lett. **B276** (1992) 354.
- [15] C. Caso *et al.*, Eur. Phys. J. **C15** (2000) 1.
- [16] Physics at LEP2, eds. G. Altarelli, T. Sjöstrand and F. Zwirner, CERN 96-01, (1996).
- [17] OPAL Collaboration, K. Ahmet *et al.*, Nucl. Instr. Meth. **A305** (1991) 275;
B.E. Anderson *et al.*, IEEE Transactions on Nuclear Science, **41** (1994) 845;
S. Anderson *et al.*, Nucl. Instr. Meth. **A403** (1998) 326.

- [18] OPAL Collaboration, G. Abbiendi *et al.*, Eur. Phys. J. **C13** (2000) 553.
- [19] LEP Energy Working Group, Report 99-01, “*Evaluation of the LEP centre-of-mass energy for data taken in 1998*”, private communication;
LEP Energy Working Group, A. Blondel *et al.*, Eur. Phys. J. **C11** (1999) 573.
- [20] J. Allison *et al.*, Nucl. Instr. Meth. **A317** (1992) 47.
- [21] S. Jadach, W. Placzek, M. Skrzypek, B.F.L. Ward and Z. Was, Comp. Phys. Comm. **119** (1999) 272.
- [22] J. Fujimoto *et al.*, Comp. Phys. Comm. **100** (1997) 128.
- [23] T. Sjöstrand, Comp. Phys. Comm. **82** (1994) 74. Pythia version 6.125 was used for the analysis presented in this paper.
- [24] G. Marchesini *et al.*, Comp. Phys. Comm. **67** (1992) 465.
- [25] OPAL Collaboration, G. Abbiendi *et al.*, “*W⁺W⁻ Production Cross Section and W Branching Fractions in e⁺e⁻ Collisions at 189 GeV*”, CERN-EP/2000-101, submitted to Phys. Lett. B.
- [26] N. Brown and W.J. Stirling, Phys. Lett. **B252** (1990) 657;
S. Catani *et al.*, Phys. Lett. **B269** (1991) 432;
S. Bethke, Z. Kunszt, D. Soper and W.J. Stirling, Nucl. Phys. **B370** (1992) 310;
N. Brown and W.J. Stirling, Z. Phys. **C53** (1992) 629.
- [27] OPAL Collaboration, K. Ackerstaff *et al.*, Eur. Phys. J. **C2** (1998) 213;
OPAL Collaboration, G. Abbiendi *et al.*, Eur. Phys. J. **C12** (2000) 567.
- [28] A. G. Frodesen, O. Skjeggstad, and H. Tofte, “*Probability and Statistics in Particle Physics*”, Universitetsforlaget (1979).
- [29] A. Denner, S. Dittmaier, M. Roth and D. Wackerth, Phys. Lett. **B475** (2000) 127.
- [30] OPAL Collaboration, G. Alexander *et al.*, Z. Phys. **C69** (1996) 543.
- [31] OPAL Collaboration, P.D. Acton *et al.*, Z. Phys. **C58** (1993) 387.
- [32] L. Lönnblad, Z. Phys. **C70** (1996) 107.
- [33] F.A. Berends, R. Pittau and R. Kleiss, Comp. Phys. Comm. **85** (1995) 437.
- [34] A. Ballestrero *et al.*, J. Phys. **G24** (1998) 365.
- [35] T. Sjöstrand and V.A. Khoze, Phys. Rev. Lett. **72** (1994) 28.
- [36] OPAL Collaboration, G. Abbiendi *et al.*, Phys. Lett. **B543** (1999) 153.
- [37] OPAL Collaboration, G. Abbiendi *et al.*, Eur. Phys. J. **C11** (1999) 217.
- [38] ALEPH Collaboration, R. Barate *et al.*, Phys. Lett. **B478** (2000) 50;
OPAL Collaboration, G. Abbiendi *et al.*, Eur. Phys. J. **C8** (1999) 559.
- [39] L. Lönnblad and T. Sjöstrand, Eur. Phys. J. **C2** (1998) 165.
- [40] ALEPH Collaboration, R. Barate *et al.*, CERN-EP/2000-045, “*Measurement of the W Mass and Width in e⁺e⁻ Collisions at 189 GeV*”, Submitted to Eur. Phys. J. C.
- [41] CDF Collaboration, T. Affolder *et al.*, FERMILAB-PUB-00-085-E, April 2000, “*Direct Measurement of the W Boson Width in p \bar{p} Collisions at $\sqrt{s} = 1.8$ TeV*”, Submitted to Phys. Rev. Lett.

Channel	Observed	Expected	Purity
$W^+W^- \rightarrow qq\bar{q}q$ (4-jet)	701	694	83%
$W^+W^- \rightarrow qq\bar{q}q$ (5-jet)	269	277	91%
$W^+W^- \rightarrow q\bar{q}e\nu_e$	350	376	98%
$W^+W^- \rightarrow q\bar{q}\mu\nu_\mu$	365	373	99%
$W^+W^- \rightarrow q\bar{q}\tau\nu_\tau$	403	403	89%
Combined	2088	2123	91%

Table 1: Numbers of events used in the W mass and width determination for each channel and all channels combined. Only events surviving the cuts described in Section 4.1 are included. The $W^+W^- \rightarrow q\bar{q}\tau\nu_\tau$ numbers include some events initially selected as either $W^+W^- \rightarrow qqe\nu_e$ or $W^+W^- \rightarrow qq\mu\nu_\mu$.

Channel	Measured M_W/GeV	Expected error/GeV
$W^+W^- \rightarrow qqe\nu_e$	80.375 ± 0.175	0.164
$W^+W^- \rightarrow qq\mu\nu_\mu$	80.513 ± 0.163	0.168
$W^+W^- \rightarrow qq\tau\nu_\tau$	80.594 ± 0.227	0.220
$W^+W^- \rightarrow qq\bar{q}q(4\text{-jet})$	80.424 ± 0.114	0.112
$W^+W^- \rightarrow qq\bar{q}q(5\text{-jet})$	80.290 ± 0.257	0.230
$W^+W^- \rightarrow qq\ell\nu_\ell$	80.478 ± 0.104	0.104
$W^+W^- \rightarrow qq\bar{q}q$	80.402 ± 0.104	0.100

Table 2: Results using the reweighting method for the fit from 183 pb^{-1} of data taken at $\sqrt{s} \approx 189 \text{ GeV}$ for each of the channels separately and for the combined $W^+W^- \rightarrow qq\ell\nu_\ell$ channel. Equation 1 is used to constrain Γ_W to M_W . The expected errors are estimated using an ensemble of Monte Carlo subsamples. The errors obtained in the data are consistent with the RMS spread of the errors obtained from the Monte Carlo subsamples.

Channel	Reweighting	Breit-Wigner fit	Convolution fit
	Measured M_W/GeV	Measured M_W/GeV	Measured M_W/GeV
$W^+W^- \rightarrow qq\ell\nu_\ell$	$80.48 \pm 0.10 \pm 0.04$	$80.47 \pm 0.11 \pm 0.04$	$80.38 \pm 0.11 \pm 0.04$
$W^+W^- \rightarrow qq\bar{q}q$	$80.40 \pm 0.10 \pm 0.10$	$80.38 \pm 0.11 \pm 0.10$	$80.37 \pm 0.09 \pm 0.09$

Table 3: Comparison of M_W fit results obtained using the three different fitting techniques for the $W^+W^- \rightarrow qq\ell\nu_\ell$ and $W^+W^- \rightarrow qq\bar{q}q$ channels separately. In each case the first uncertainty is statistical and the second systematic. The observed differences are compatible with the expected RMS differences between the results from the different fits.

Systematic errors (MeV)	M_W		Γ_W	
	qqqq	qq $\ell\nu_\ell$	qqqq	qq $\ell\nu_\ell$
Beam Energy	16	16	10	10
Hadronisation	30	30	60	25
Jet energy/Resolution	4	5	47	47
Lepton energy/Resolution	–	9	–	9
Four Fermion	–	–	33	29
Background	6	8	41	25
MC statistics	10	10	51	51
Sub-total	36	38	106	84
Colour Reconnection	66	–	68	–
Bose-Einstein Correlations	67	–	39	–
Total systematic error	101	38	132	84

Table 4: Summary of the systematic uncertainties for the fit results. For the fits to determine M_W , Γ_W is constrained to its Standard Model relation. The uncertainties are given separately for fits to the $W^+W^- \rightarrow qqqq$ and $W^+W^- \rightarrow qq\ell\nu_\ell$ samples. Uncertainties from ISR give negligible contributions to both M_W and Γ_W . The uncertainty related to the Monte Carlo models of the four-fermion process give is negligible for the measurement of M_W .

CR Model	Mass shift (MeV)	Width shift (MeV)
SK I	$+66 \pm 8$	$+68 \pm 22$
SK II	$+3 \pm 8$	$+20 \pm 22$
SK II'	$+10 \pm 8$	$+53 \pm 21$
AR 2	$+85 \pm 8$	$+128 \pm 22$
AR 3	$+140 \pm 10$	$+309 \pm 21$

Table 5: The predicted shifts in the fitted mass and width from the $W^+W^- \rightarrow qqqq$ channel for various colour-reconnection (CR) models. The numbers correspond to the fitted mass (width) using the reweighting method in the reconnected sample minus the fitted mass (width) for the corresponding sample without CR. The errors are statistical only.

OPAL $\sqrt{s}=189$ GeV

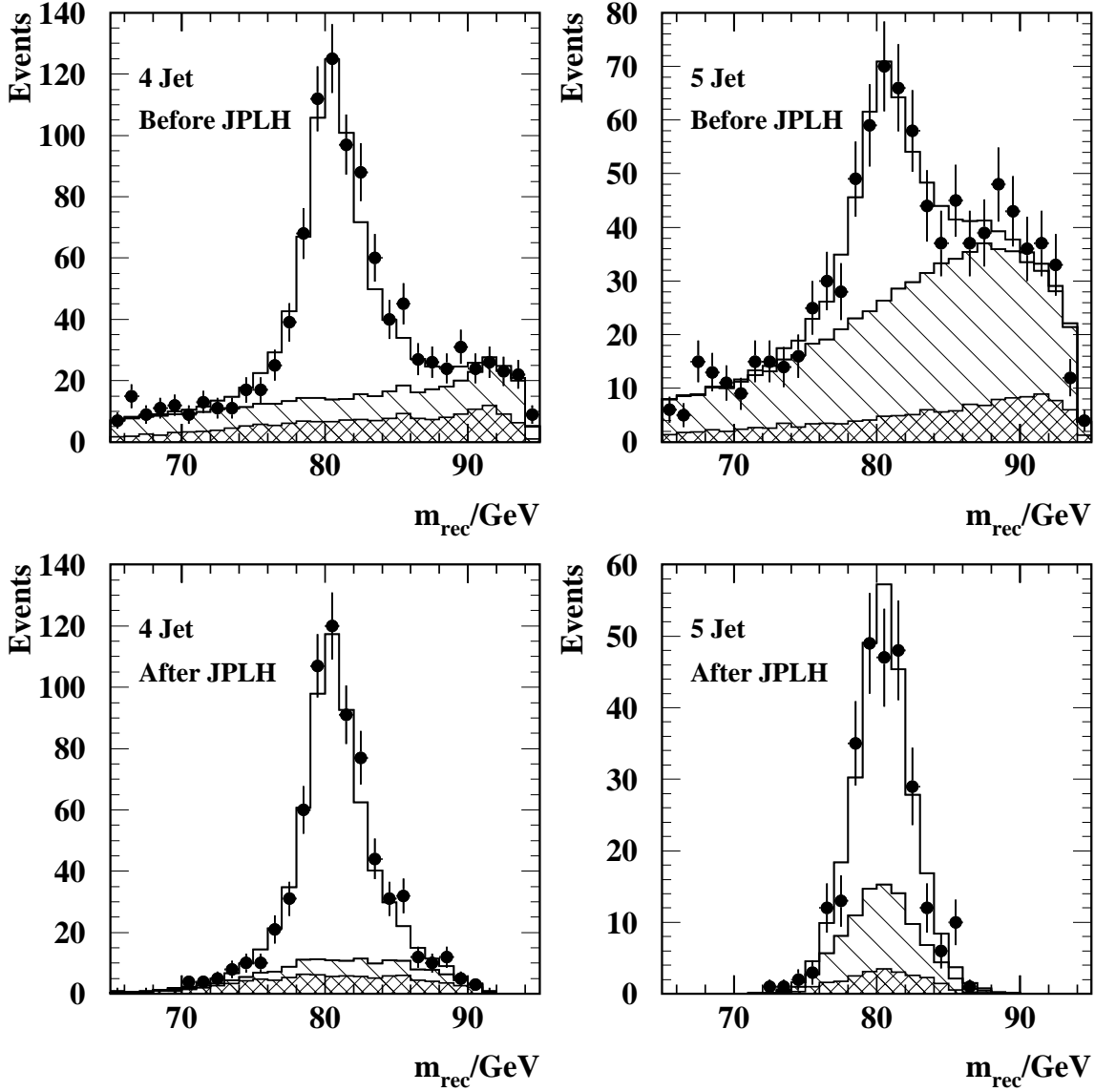


Figure 1: The reconstructed mass, m_{rec} , distributions for $W^+W^- \rightarrow qqqq$ events divided into four and five jet samples. The top two plots show the distributions before the jet-pairing likelihood (JPLH) cut. The lower two plots show the mass distributions which are used to determine M_W , *i.e.* after the cut on JPLH. The points correspond to the OPAL data and the histograms to the Monte Carlo predictions. The contribution from the non-WW background is shown as the cross-hatched histogram and the combinatorial background is indicated by the singly-hatched histogram.

OPAL $\sqrt{s}=189$ GeV

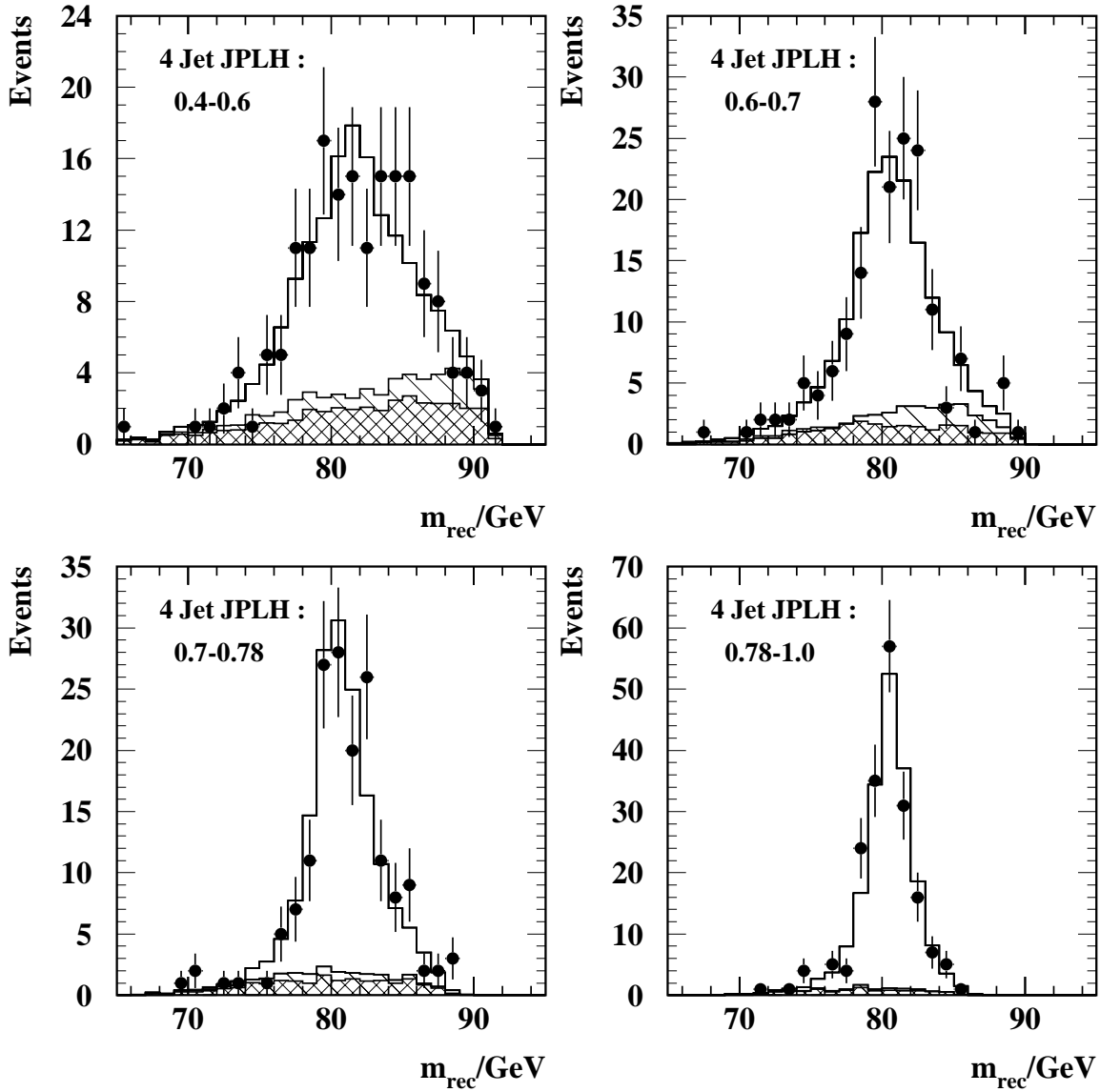


Figure 2: The reconstructed mass distributions for the four jet $W^+W^- \rightarrow qq\bar{q}\bar{q}$ sample divided into four bins of the output of the jet-pairing likelihood (JPLH) discriminant. The points correspond to the OPAL data and the histograms to the Monte Carlo predictions. The contribution from the non-WW background is shown as the cross-hatched histogram and the combinatorial background is indicated by the singly-hatched histogram.

OPAL $\sqrt{s}=189$ GeV

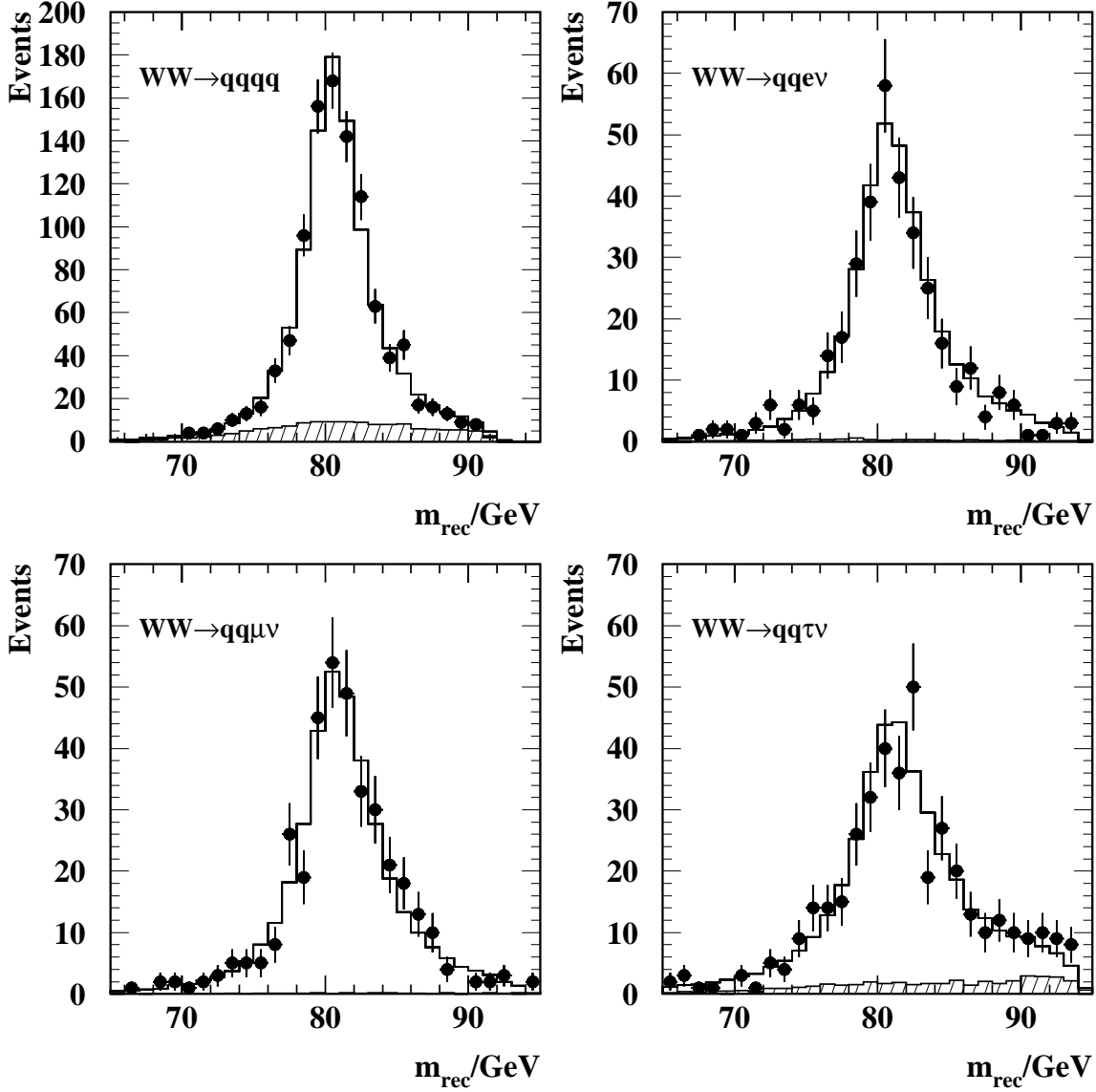


Figure 3: The reconstructed invariant mass distribution for the $W^+W^- \rightarrow qq qq$, $W^+W^- \rightarrow qq e \nu$, $W^+W^- \rightarrow qq \mu \nu$ and $W^+W^- \rightarrow qq \tau \nu$ samples. The points correspond to the OPAL data and the histograms to the reweighted Monte Carlo spectra corresponding to the fitted masses. The non-WW background contribution is indicated by the hatched histogram.

OPAL $\sqrt{s}=189$ GeV

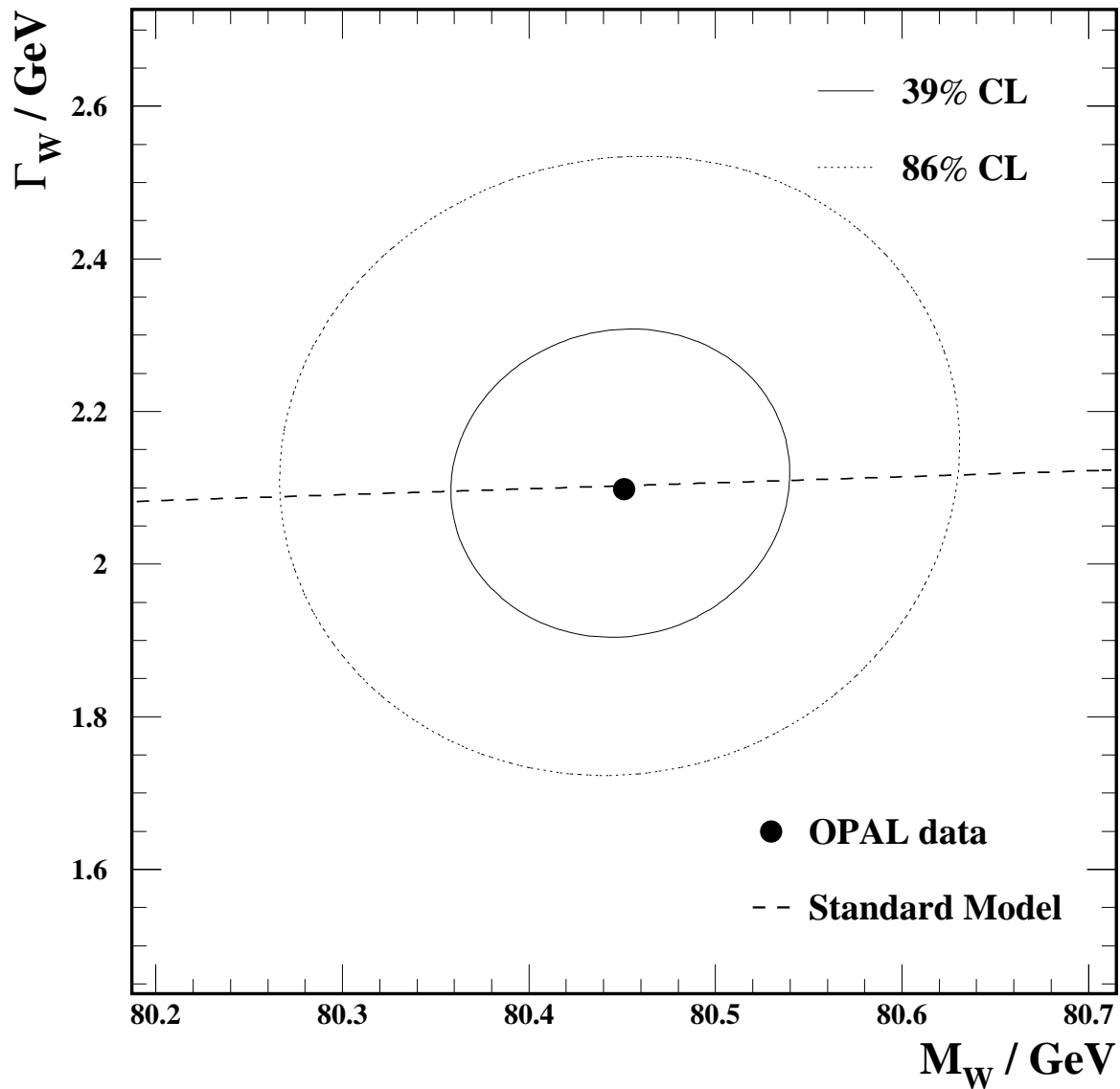


Figure 4: The 39% and 86% contour levels of the two parameter fit using the reweighting method including systematic contributions. The Standard Model relation between M_W and Γ_W , given in Equation 1, is shown by the dashed line.