# $pp$ -annimilation into  $\omega\pi$ ,  $\omega\eta$  and  $\omega\eta$  at ove, 1200 and 1940  $\text{MeV}\!/\text{c}$

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Abstract. The annihilation channels  $pp \rightarrow \omega \pi^*$ ,  $\omega \eta$ ,  $\omega \eta$ were studied with the CRYSTAL BARREL detector at LEAR at  $\bar{p}$ -momenta of 600, 1200, and 1940 MeV/c. In most cases angular distributions were measured which ahowed a complete  $J^{\pm}$  -analysis using the helicity formal-  $\hskip10mm$  it ism. The contribution of all relevant initial states could be determined. The maximal contributing angular momenta are dependent on the p-momentum and range up to  $J=5$ .

# Introduction

This paper reports on the measurement of selected two body  $\bar{p}p$ -annihilation channels performed with the CRYSthe Barrel CB-, which is a positive the position of the contract of the contract of the contract of the contract of 600, 1200 and 1940 MeV/c. The aims of the measurements were  $\mathbf{M}$  . The angular momenta mom in the  $\bar{p}p$ -system, which contribute to the annihilation process with increasing  $\bar{p}$ -momenta. This information is vital for the analysis of 3-or more body annihilation pro-

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cesses in flight, which contain mesonic or exotic resomances with masses up to  $\Delta$  . GeVc  $\Box$  ( $\Delta$ ) Assess whether such data from CB are analyzeable at all This is not straightforward because the angular distributions are forward peaked in the Lab-system, where the detector, optimized for at rest annihilations, becomes inefficient for  $\gamma$ -detection. The channels  $\omega \Lambda(\Lambda = \pi^* , \eta, \eta^*) (\Lambda \to \gamma \gamma)$  $\omega \rightarrow \pi$   $\gamma$ ) have been chosen, because they provide three independent observables, the production angle  $\Theta$  of the  $\omega$ , the decay angle  $\vartheta$  of the  $\omega$  and the angle  $\varphi$  between the  $\omega$ -direction and the  $\omega$ -decay plane (Treiman-Yangangle-, a complete particle and a complete particle wave  $\sim$ analysis using the helicity formalism and thus provides direct information on the contributing initial pp-states.

#### 2 Experimental set-up

The experimental set-up for  $\bar{p}p$ -experiments at rest with the CB-detector is described in  $[1]$ . The set-up used in flight is very similar, but behind the liquid hydrogen target an additional scintillation counter was installed It consisted of a 3 mm thick disk of 4 cm diameter, mounted at the end of a cylindrical tube of 15 cm diameter and 2 m length, both of which vetoed antiprotons which did not react in the target or were scattered at small angles According to calculations about  $1\%$  of all antiprotons

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entering the target were not vetoed and thus were can didates for annihilation events inside the target

The detector is optimized for pp-annihilations at rest, for which the two 12 degree holes along the beam line direction have only a small effect. The situation is different at higher antiproton beam momenta due to the Lorentz-boost along the  $\bar{p}$ -axis, so that the fraction of undetected particles increases. However, as we will show, this was not a severe limitation in the  $\bar{p}$ -momentum range up to  $1.94 \text{ GeV}/c$  (maximum LEAR momentum) and allowed the measurement of angular distributions over a sufficiently large range.

#### Data sample

Table 1 shows the data samples taken during the various beam periods. In most cases a "0-prong"-trigger was used, rejecting all events with charged particle hits in the cylindrical proportional chambers. In one case (August  $\overline{a}$  and  $\overline{a}$  and  $\overline{a}$  and  $\overline{a}$ events The last column refers to the number of truly 0-prong events in the offline analysis.

## 4 Event reconstruction

The event reconstruction was done in a similar way to that for annihilations at rest, and is described in  $[2]$ . I he  $\gamma$  s originating from  $\pi$ ,  $\eta$ ,  $\eta$  and  $\omega$ -decays hit one eve of the CsI-crystals of the electromagnetic spectrometer and give rise to electromagnetic showers extending over about 10 crystals in average. A PED (Particle Energy deposit-deposite is deposited as an area consistent crystal as an area consistent crystal and adjacent crystal tals with energy deposits higher than a minimum value and containing only one maximum. It is normally attributed to the hit of a single  $\gamma$ , but can also be due to a statistical uctuation split of the split of the shower A split of the shower  $\mathcal{L}_\mathbf{X}$ CLUSTER can contain several PEDS

In contrast to annihilations at rest, the energy of neutral pions can be so high that both decay  $\gamma$ 's merge into one PED, because their opening angle in the lab system can be as small as a few degrees In order to rec ognize such events, the invariant shower-mass of a PED was determined. It is defined as

$$
\mu_{Shower} = \sqrt{\left(\sum_i E_i\right)^2 - \left(\sum_i \overrightarrow{p_i}\right)^2}
$$

where i denotes the crystal number,  $E_i$  is the  $\gamma$ -energy deposit in crystal  $i$  and  $p_i$  is the  $\gamma-$ momentum, mea-li sured from the annihilation vertex to the crystal  $i$ . It has been successfully used in annihilations at rest to distin guish between a shower originating from a single  $\gamma$  and a shower produced by two overlapping  $\gamma$ 's [3]. Monte Carlo studies show that the shower masses of single (unmerged)  $\gamma$ 's are zero at low momentum rising slowly with energy. The shower masses of merging  $\gamma$ 's originating from high

energy neutral pions have generally higher values, start- $\max$  from 140 MeV/c for low energy pions. Both distributions are rather distinct allowing a good separation of events (Fig.  $1$ ).



Fig. Fig. (1994) of the invariant shower mass of two showers of two contracts of two contracts of two contracts  $m$ erged  $\gamma$  s from a  $\pi$  - as function of  $\pi$  - kinetic energy. The inner  $line corresponds to the center of gravity of the distribution, the$ outer lines indicate the cut against single  $\gamma$ 's.

where the compact  $\mathcal{L}$  is the rest in actions discussed here,  $\eta$  and  $\eta$  -cannot produce **I-PED**events, since their decay  $\gamma$ 's can always be spatially resolved

In some cases,  $\pi$  is and  $\eta$  s heading towards the forward opening of the detector will escape entirely un detected. In principle, such events could be identified by their missing total energy and momentum, and the remainder of the event could be used to reconstruct the complete event, e.g. by kinematic fitting. As will be apparent from the following and as was confirmed by MCsimulations, these events play only a minor role in the data discussed here Therefore only complete events ful filling energy and momentum conservation were used in this analysis

 - tries to separate single PEDS from split os This Table 2 shows the steps in the data reconstruction and the applied cuts to reduce the instrumental background eg electronic noise-physical physical background background the physical background of the physical bac ground (e.g. shower fluctuations or punchthroughs of high multiplicity channels-in joint multiplicity of the number of the number of  $\mathcal{A}$ ber of neutral events at the three  $\bar{p}$ -momenta investigated. "Neutral" means, that there was no hit in either of the two cylindrical proportional wire chambers nor in the inner three layers of the jet-drift-chamber . Step  $1$ lists the number of events after a cut on the number of PEDS The minimum value - corresponds to one PED  $\pi^+$  +3  $\gamma^-$  as it never occurs that both  $\pi^+$  s of an event form a single PED the maximum value of the maxim responds to  $5 \gamma$  PEDS + 5 split-offs. The next cut (step is done using the neural network "Brain"  $[4]$ , which was extensively checked with MC-data. In the next cut (step



**Table 1.** Data sample.

 $\mathfrak{so}_L$ , events are restricted to those with maximally two  $\pi^*$  s sev or one  $\pi$  and one  $\eta$ .

The events with one I PED  $\pi$  + three  $\gamma$  s and those with five  $\gamma$ 's were kinematically fitted to the hypothesis  $\vartheta$   $\gamma$  or  $\pi$   $\gamma\gamma\gamma$  (step 4), and then to the hy-  $\rightarrow$ pothesis  $\pi$   $\Lambda$   $\gamma$  ( $\Lambda$   $\equiv$   $\pi$  ,  $\eta$ ,  $\eta$ ) (step 5) and  $\omega$   $\gamma$  $\gamma$  (step 6). Figs. 2a/c show the  $\pi$   $\gamma$ -and  $\pi$   $\pi$  -invariant masses for  $\cdots$ the  $\pi$   $\omega$ -channel after step 5. It is obvious, that back-  $\sim$ ground, e.g. from  $\pi^+ f_2^-(f_2 \to \pi^+ \pi^-)$  one  $\gamma$  missing),  $\delta \pi^+$ (one  $\gamma$  missing) and  $2\pi$  (+ one spliton) is still present. In order to reduce this background a cut on the vertex distribution was applied. In the absence of charged annihilation products, the vertex could be determined only crudely by a kinematic fit to the events. This cut removed events originating from the veto counter behind the target (step  $7$ ).

Further cuts were channel specific. As an example, the  $\pi \omega$ -channel is discussed in more details. As no direct in to the channel  $\pi^*\omega$  was done due to the width of the  $\omega$  and in order to keep control on background a consistency check between the hypotheses of step and 6 was made. Only those events were kept for which either of the two  $\gamma$ 's of the  $\omega \gamma \gamma$ -hypothesis did not coincide with the  $\gamma$  of the  $\pi^+\pi^-\gamma$ -hypothesis (step 8a). This gave a nuge reduction of the background in the  $\pi$   $\gamma$ - and  $\pi^+ \pi^-$  invariant mass spectra (Figs. 20/0). Furthermore  $\tau^$ the assignment of  $\pi$ ,  $\eta$  and  $\eta$  particles to two  $\gamma$  s was checked by comparing the identification methods used in step was the step in the step which are step which are step in the step  $\omega$ independent. Consistency between the two methods was required (step  $8b$ ).

Comparing the backgrounds in the data with MC predictions we found it to be too large for some subsam ples of the data This was particularly true for events where split-offs had been recognized by "Brain", so that these events were finally removed (step  $\&c$ ).

A similar procedure was applied for the selection of the the channels external cuts and the steps are two functions of the cuts of the cuts of the cuts of the c were applied. A comparison between data (after step  $9c$ ) and MC-predictions showed too large a background for  $\mu$  is 1-r  $\mu$ D- $\pi$  -events. Consequently these events were by skipped step d- Furthermore the inspection of the  $\omega$ -decay angular distribution showed an accumulation of  $\Lambda$ it originated from falsely identified  $\pi^*\omega$ -events and so spin

event with a cost of contrast in the cost of the c and the cut of the cut

The  $\eta$   $\omega$ -channel was treated similarly, but no cut on cost and for 600 MeV $c$  p-momentum as the background at higher  $\bar{p}$ -momenta was too big. This is due to the fact that  $\eta'$ was analysed in its  $2\gamma$  decay mode only, which has a low branching ratio -

The resulting angular distributions for the three two body channels and the three momenta under inves tigation are shown in Fig.  $3$  and Fig.  $4$ .

## 5 Background Estimate

 $M_{\rm U}$  – data for the channels  $\pi^*\omega$ ,  $\eta\omega$ ,  $\eta\omega$ ,  $\pi^*\pi^*$ ,  $\pi^*\eta$ ,  $\pi^*\eta$ ,  $\eta\eta$ ,  $3\pi$ ,  $2\pi$   $\eta$  and  $3\eta$  were produced at the p-momenta under investigation. For the 2-body channels the angular distributions found here and from  $[5]$  were used and corrected for acceptance. For the simulation of 3-body channels at 600 and 1940 MeV $\ell$  no intermediate resonances were taken into account. However, it was found in MC-studies that the inclusion of intermediate states as found in  $[6]$  even reduces the feed through into the  $\omega X$ -channels. The background contributions could be determined by processing these data through the analysis chain discussed above. For the  $\pi$   $\omega$ -channel they varied between the contract of the con contribution from  $\sigma \pi$  ), for the  $\eta \omega$ -channel between  $4\gamma_0$ and  $14\%$  (main contribution from  $\pi \omega$ ,  $3\pi$  and  $2\pi \eta$ ), while for the  $\eta \omega$ -channel (600 wie  $\eta c$ ) the background is as migh as 21 %, mainly from  $\pi \omega$ ,  $\eta \omega$ ,  $3\pi$  and  $2\pi \eta$ .

#### Partial wave analysis

quantization at the third component of  $\alpha$  is really component of  $\alpha$  is really in  $\alpha$ For the partial wave analysis it is assumed that the initial states are well defined  $\bar{p}p$ -states with quantum numbers  $J^{\sim}$ . The direction of the incoming p is chosen as the stricted to  $M = 0, \pm 1$ . The  $0$   $\omega$ -system is characterized by the quantum numbers L angular momentum- total spin S - total helicity in S - total helicity in the decay of the angles  $\sigma$  and  $\varPsi$  of the  $\omega$ -direction. The  $\omega \rightarrow \pi$   $\gamma$ -system is characterized by the angular momentum  $\mathbf{f}$  total momentum  $\mathbf{f}$  total momentum  $\mathbf{f}$ spin s (  $\sim$  ), the total measure, i. ( ) measure, ( ) where the  $\sim$ 

	beam momentum [MeV/c]	600	1200	1940				
	$#$ of neutral events	2 266 054	10 923 847	8 558 977				
	cuts on multiplicities							
	1. PED-multiplicity $(4 \leq \text{\#}_P E$ <sub>PEDs</sub> $\leq 10)$	1 608 966	8 431 557	6 044 919				
	2. Removal of split offs	1 603 230	8 315 659	5 916 326				
general selection	3. Max. # of $\pi^0$ and $\eta$	250 224	1 222 317	839 153				
	kinematic fit							
	4. final state $(5\gamma \text{ or } \pi^0 \gamma \gamma \gamma)$	75 121	381 910	181 858				
	5. $\pi^0 X \gamma$ (X = $\pi^0$ , $\eta$ or $\eta'$ )	59 146	327 784	160 049				
	6. $\omega \gamma \gamma$	33 515	170 466	73 710				
	7. vertex	31 920	163 245	63 790				
	8. pp $\longrightarrow \pi^0 \omega$							
specific selection	a. consistency of $\pi^0 \pi^0 \gamma$ and $\omega \gamma \gamma$	12 486	64 716	28 48 5				
	b. consistency with meson recognition	12 462	64 340	27 989				
	c. no shower fluctuation (5 PEDs at most)	8 1 8 3	41 663	17 320				
	9. $\bar{p}p \longrightarrow \eta \omega$							
	a. consistency of $\pi^0 \eta \gamma$ and $\omega \gamma \gamma$	5 4 2 1	20 029	7 0 5 1				
	b. consistency of meson recognition	4 875	17 667	6 10 2				
channel	c. no shower fluctuation (5 PEDs at most)	3 2 6 9	11 283	3 6 6 0				
	d. no merged $\pi^0$ ("1-PED- $\pi^0$ ")	3 2 6 9	11 222	3 4 3 4				
	e. cut on $\omega$ decay angle	2 8 8 0	9 7 3 2	3 0 3 2				
	10. $\bar{p}p \rightarrow \eta' \omega$							
	a. consistency of $\pi^0 \eta' \gamma$ and $\omega \gamma \gamma$	1 9 6 4		too low statistics				
	b. consistency with meson recognition	670		with too large				
	c. no shower fluctuation (5 PEDs at most)	393		background				
	d. no merged $\pi^0$ ("1-PED- $\pi^0$ ")	393						
	survey of selected statistics							
	$\bar{p}p \longrightarrow \pi^0 \omega$ (4 & 5 PEDs)	8 1 8 3	41 663	17 320				
	5 PEDs	8 1 8 1	40 898	14 263				
	4 PEDs	$\overline{2}$	765	3 0 5 7				
	$\bar{p}p \longrightarrow \eta \omega \, (5 \, \overline{\mathrm{PEDs}})$	2 8 8 0	9 7 3 2	3 0 3 2				
$\bar{p}p -$	$\rightarrow \overline{\eta' \omega}$ (5 PEDs)	393		too low statistics				

**Table 4.** Steps of data selection for the  $\sigma \omega$  channels. Detailed explanations are qiven in the text.

 $\alpha$  and subsequently and such that spins  $\mu$  and spins  $\mu$  are the spins  $\alpha$  spins  $\alpha$  and spins  $\alpha$ and helicities of the  $\omega$  and  $\gamma$ , respectively.

The quantities which the analysis aims to deter mine are the frequencies with which the initial states of different  $J$  and  $M$ -values contribute to the measured angular distributions Taking into account the conservation of parity P-1 particles and conjugation co mentum Joy ment as sit to a semplement Jets yf an a meant out, that only specific  $J^{\ast}$  and M-values are allowed for the state process  $\bar{p}p \rightarrow 0^- \omega$ .  $J = 0$  states are excluded. For  $J =$ even-states only  $J^{-}$  with  $M = \pm 1$  is allowed, for J = odd-states only  $J^{--}$  with  $M = 0, \pm 1$  and  $J^{+-}$  with  $M = 0$  contribute.

The amplitudes are derived from the formulae given in [7]. Quantities needing coherent summation are written as subscripts and quantities needing incoherent summation are written as superscripts on the ampli tudes. Then the amplitude reads:

$$
A_{J\lambda_{\omega}}^{M\lambda_{\gamma}}(\overline{p}p \to 0^{-}\omega \to 0^{-}\pi^{\circ}\gamma) =
$$
  
\n
$$
A_{J\lambda_{\omega}}^{M}(\overline{p}p \to 0^{-}\omega) \times A_{\lambda_{\omega}}^{\lambda_{\gamma}}(\omega \to \pi^{\circ}\gamma) =
$$
  
\n
$$
\sum_{LS} \alpha_{LS}^{JM}(\overline{p}p) (L \times I | J \Lambda) (s_{\omega} \lambda_{\omega} 0 \times I | S \Lambda) \times
$$
  
\n
$$
D_{M\Lambda}^{J}{}^{*}(\Phi, \Theta, 0) \times
$$
 (1)

$$
\sum_{\ell\sigma} \alpha_{\ell s}^{JM}(\omega) (\ell \ 0 \ s \ \lambda \mid s_{\omega} \ \lambda) (s_{\gamma} \ \lambda_{\gamma} \ 0 \ 0 \mid \sigma \ \lambda) \times
$$
  

$$
D_{\lambda_{\omega} \lambda}^*(\varphi, \theta, 0)
$$

The  $\alpha_{LS}$  denote the complex spin orbit coupling amplitudes which are free parameters of the fit. With S  $s_{\omega} = s_{\omega} = 1$ ,  $s = s_{\gamma} = 1$  and  $\ell = 1$  (follows from parity conservation- and setting-

$$
\sqrt{3}\alpha_{L_1}^{JM}(\overline{p}p)\alpha_{L_1}^{JM}(\omega) = \alpha_{L}^{JM} = |\alpha_{L}^{JM}|e^{i\varphi_{L}^{JM}} ,
$$

$$
one\ obtains
$$

$$
A_{J\lambda_{\omega}}^{M\lambda_{\gamma}}(\overline{p}p \to 0^{-}\omega \to 0^{-}\pi^{\circ}\gamma) =
$$
  

$$
-\sqrt{\pi} \lambda_{\gamma} e^{i\lambda_{\omega}\varphi} d_{M\lambda_{\omega}}^{J} (cos\theta) d_{\lambda_{\omega}\lambda_{\gamma}} (cos\theta) \times
$$
  

$$
\sum_{L} |\alpha_{L}^{JM}| (L 0 1 \lambda_{\omega} | J \lambda_{\omega}) e^{i\varphi_{L}^{JM}},
$$
 (2)

of  $\alpha_L^{JM}$  were the free parameters to be fitted to the data. With  $\alpha_L^{JM}$  being equal for  $M = +1$  and  $M = -1$ ,  $\Gamma$  me minimization was done using a maximum likelihood The observed intensity is given as the modulus of  $(2)$ with coherent summation over J and  $\lambda_{\omega}$  and incoherent summation over the M and the Secondary over M and the Secondary Secondary was an ansatz was an ansatz was an a used to describe the matrix of magnitudes and phases and phases and three arbitrary phases remained, which were set to zero. method. For every iteration the fit results were treated as the weights to a MC-simulation, assuming an isotropic



 $\mathbf{r}$  ig.  $\mathbf{z}$ , control spectra for the  $\pi$   $\omega$  selection at 1940 MeV/c. Figs.  $z a, o$  show the invariant mass spectra of  $\pi$   $\gamma$  ( $z$  entries per event), rus. zc,a snow the invariant mass spectra of  $\pi^+\pi^-$  (1 entry per event). Fugs. za,c qive the spectra after the  $\pi^-\pi^-\gamma$  fit (step ə). Fugs. zo,a refer to the spectra after step  $8a$ .

distribution of the events in the CM-system, thus allowing a detailed fit-data comparison for every step. Figs.  $3$ and 4 show the results for the best final fits compared for the determination of the maximal contributing anguto the data. The agreement between fits and data is tudes and phases of  $\alpha_L^{JM}$ , as obtained from the fit with els of  $J_{max} = J_{max}$  (see next section). The errors are purely and diamstatistical

In order to obtain the maximal contributing angular mo menta  $J_{\max}$ , several fits with successively increasing curv maximal angular momentum  $J_{\text{max}}$  were performed for each beam momentum. For each of these fits every allowed transition with an angular momentum  $J \leq J_{\text{max}}$ was taken into account. Partial intensities were defined in order to visualize the result of every step These are intensities calculated for a given angular momentum  $J \leq J_{\text{max}}$  and one value of M. Figs. 5 and 6 show the development of these partial intensities for the three chan nels and the three  $\bar{p}$ -momenta under study. For even  $J$ values two M values - are possible for odd J values a singlet M and a triplet state M and a trip cur. The partial intensities are displayed as boxes whose size is proportional to their magnitudes Also shown is

the variation of the log likelihood  $\Delta\mathcal{L}$  with  $J_{\text{max}}$ (black squares, behaviour of L is taken as the criterion of the criterion of  $\mathcal{L}$ for the determination of the maximal contributing angular momentum  $J_{\text{max}}^{contr}$ . It is observed that after reaching a certain value of Jmax the change in the likelihood level els off and comes close to the values displayed by open diamonds in Figs. 5 and 6. They correspond to changes in  $\mathcal L$  expected for the case that a maximum is found and additional degrees of freedom do not give a refined description of the data  $\mathcal L$  is then only diminished due to the higher number of degrees of freedom A dimini nation in  $\Delta\mathcal{L}$  of 0.5 was assumed per degree of freedom.  $J_{\rm max}^{\rm max}$  is then defined as the value of  $J_{\rm max}$ , for which both curves begin to have the same shape It is emphasized in the figures by vertical lines. According to this definition the maximum contributing angular momenta are

- $J_{\text{max}}$  = 3 for pp  $\longrightarrow \pi \omega$  at 1940 MeV/c
- $\overline{J}^{\text{max}}_{\text{max}} = 5 \text{ for } \overline{p}p \longrightarrow \eta\omega$
- $\begin{aligned}\n&- \int_{\text{max}}^{\text{max}} &= 4 \text{ for } \bar{p}p \longrightarrow \pi^{\circ} \omega \text{ at } 1200 \text{ MeV/c} \\
&- \int_{\text{max}}^{\text{cont}} &= 3 \text{ for } \bar{p}p \longrightarrow \eta \omega \text{ at } 1200 \text{ MeV/c} \\
&- \int_{\text{max}}^{\text{cont}} &= 3 \text{ for } \bar{p}p \longrightarrow \pi^{\circ} \omega \text{ at } 600 \text{ MeV/c} \\
&- \int_{\text{max}}^{\text{cont}} &= 3 \text{ for } \bar{p}p \longrightarrow \eta \omega \text{ at } 600$
- 
- 
- 
- $\sigma = J_{\text{max}}^{\text{max}}$  compatible with 5 for pp  $\rightarrow$   $\eta \omega$  at 000 MeV/c

These values are in agreement with estimates of  $J_{\text{max}}$  as obtained by model calculations (see e.g. [0]). Some characteristics of the results are



 ${\bf r}$  ig. S. Distributions of the  $\omega$  production angle  $\varphi$  (not corrected for acceptance). The points with the error bars correspond to the data, the fit results are given as shaded areas.



 ${\bf r}$  ig. 4. Distributions of the  $\omega$  accay angle  $v$  and the Ireiman Yang angle  $\varphi$  (not corrected for acceptance). The points with the error  $bars$  correspond to the data, the fit results are given as shaded areas.

channel	$J^{PC}$	М	L	$\overline{\alpha_{I}^{JM}}$	$\varphi^{JM}_{L}$	
$\pi^0\omega$	$1^{--}$	$\mathbf{0}$				
			1	$0.41 \pm 0.19$	$0.$ (fixed)	
$600 \text{ MeV/c}$		±1	$\mathbf{1}$	$0.40 \pm 0.17$	$0.$ (fixed)	
	$1+$	$\overline{0}$	$\overline{0}$	$0.17 \pm 0.07$	$0.$ (fixed)	
			$\overline{2}$	$0.26 \pm 0.13$	$0.70 \pm 0.27$	
	$2^{--}$	$\pm 1$	1	$0.25 \pm 0.12$	$2.49 \pm 0.23$	
			3	$0.31 \pm 0.11$	$5.66 \pm 0.25$	
	$3^{--}$	$\overline{0}$	3	$0.53 \pm 0.21$	$-1.05 \pm 0.18$	
		±1	3	$0.36 \pm 0.16$	$2.06 \pm 0.26$	
	$3^{+-}$	$\theta$	$\overline{2}$	$0.77 \pm 0.27$	$-1.32 \pm 0.15$	
			$\overline{4}$	$0.57 \pm 0.22$	$-0.20 \pm 0.17$	
$\eta\omega$	$1 -$	$\mathbf{0}$	1	$0.66 \pm 0.34$	$0.$ (fixed)	
$600 \text{ MeV/c}$		±1	$\mathbf{1}$	$0.45 \pm 0.31$	$0.$ (fixed)	
	$1+$	$\theta$	$\bf{0}$	$0.23 \pm 0.22$	$0.$ (fixed)	
			$\overline{2}$	$0.37 \pm 0.25$	$-5.60 \pm 1.57$	
	$2^{--}$	$\pm 1$	1	$0.11 \pm 0.13$	$-0.73 \pm 0.66$	
			3	$0.24 \pm 0.19$	$-4.17 \pm 0.59$	
	$3^{--}$	$\overline{0}$	3	$0.45 \pm 0.24$	$3.14 \pm 2.47$	
		±1	3	$0.52 \pm 0.28$	$-4.81 \pm 0.38$	
	$3^{+-}$	$\theta$	$\overline{2}$	$0.32 \pm 0.27$	$-4.70 \pm 0.49$	
			$\overline{4}$	$0.23 \pm 0.21$	$-5.75 \pm 0.79$	
$\eta' \omega$	$1 - -$	$\theta$	1	$0.61 \pm 0.48$	$0.$ (fixed)	
$600 \text{ MeV/c}$		±1	$\mathbf{1}$	$0.36 \pm 0.35$	$0.$ (fixed)	
	$1+-$	$\overline{0}$	$\overline{0}$	$0.23 \pm 0.21$	$0.$ (fixed)	
			$\overline{2}$	$0.37 \pm 0.33$	$0.49 \pm 0.66$	
	$2^{-}$	$\pm 1$	$\mathbf{1}$	$0.17 \pm 0.20$	$-0.99 \pm 0.99$	
			3	$0.19 \pm 0.25$	$-0.78 \pm 1.08$	
	$3 - -$	$\theta$	3	$0.22 \pm 0.41$	$-3.14 \pm 2.77$	
		±1	3	$0.42 \pm 0.41$	$2.27 \pm 0.67$	
	$3^{+-}$	$\overline{0}$	$\overline{2}$	$0.65 \pm 0.50$	$1.33 \pm 0.46$	
			$\overline{4}$	$0.40 \pm 0.35$	$0.55 \pm 0.71$	

**Table 3.** Magnitudes and phases of  $\alpha_L^+$ , describing the best fit to the angular assistantially for the case  $J_{max} = J_{max}$ . The beam momentum is not all the contracts of the c

channel	$J^{PC}$	М	L	$\alpha_{r}^{J\overline{M}}$	$\varphi_{I}^{JM}$	
$\pi^0\omega$	$1 - -$	$\bf{0}$	1	$0.52 \pm 0.04$	$0.$ (fixed)	
$1200 \text{ MeV/c}$		$\pm$ 1	1	$0.02 \pm 0.06$	$0.$ (fixed)	
	$1+-$	0	$\mathbf{0}$	$0.22 \pm 0.04$	$0.$ (fixed)	
			$\overline{2}$	$0.32 \pm 0.09$	$0.12 \pm 0.12$	
	$2 - -$	±1	1	$0.11 \pm 0.03$	$1.24 \pm 0.33$	
			3	$0.17 \pm 0.05$	$0.81 \pm 0.29$	
	$3 - -$	$\mathbf{0}$	3	$0.53 \pm 0.10$	$-3.15 \pm 6.28$	
		$\pm$ 1	3	$0.59 \pm 0.10$	$-1.82 \pm 0.21$	
	$3^{+-}$	$\mathbf{0}$	$\overline{2}$	$0.78 \pm 0.15$	$-4.24 \pm 0.10$	
			4	$0.06 \pm 0.05$	$1.72 \pm 1.25$	It
	$4^{--}$	$\pm$ 1	3	$0.51 \pm 0.10$	$-1.90 \pm 0.21$	
			5	$0.58 \pm 0.11$	$4.57 \pm 0.21$	m.
$\eta\omega$	$1 - -$	$\mathbf{0}$	1	$0.46 \pm 0.09$	$0.$ (fixed)	m.
$1200 \text{ MeV/c}$		±1	1	$0.27 \pm 0.08$	$0.$ (fixed)	di:
	$1 + 1$	$\mathbf{0}$	$\mathbf{0}$	$0.39 \pm 0.08$	$0.$ (fixed)	[5]
			$\overline{2}$	$0.33 \pm 0.08$	$5.62 \pm 0.31$	ar
	$2^{--}$	±1	1	$0.10 \pm 0.18$	$0.45 \pm 0.29$	$\sigma$
			3	$0.19 \pm 0.10$	$3.42 \pm 0.34$	$J_{\scriptscriptstyle{\rm m}}^c$
	$3^{--}$	$\mathbf{0}$	3	$0.32 \pm 0.08$	$0.00 \pm 1.57$	$\pi^\circ$
		$\pm$ 1	3	$0.77 \pm 0.15$	$0.69 \pm 0.37$	
	$3^{+-}$	$\mathbf{0}$	$\overline{2}$	$0.22 \pm 0.23$	$4.93 \pm 0.54$	$\bar{p}p$
			$\overline{4}$	$0.26 \pm 0.22$	$4.44 \pm 0.18$	$_{\rm de}$

**Table 4.** Magnitudes and phases of  $\alpha_L^{\tau}$ , aescribing the best fit to the angular assimutions for the case  $J_{max} = J_{max}$ . The beam  $\frac{1}{N}$  the  $\frac{1}{N}$  $\mathcal{M}$ 

channel	$J^{PC}$	$\mathbf M$	L	$\alpha_I^{JM}$	$\varphi_L^{J\,M}$	
$\pi^0\omega$	$1 - -$	$\bf{0}$	$\mathbf{1}$	$0.14 \pm 0.08$	$0.$ (fixed)	
1940 MeV/c		±1	$\overline{1}$	$0.27 \pm 0.04$	$0.$ (fixed)	
	$1+$	$\mathbf{0}$	$\bf{0}$	$0.26 \pm 0.02$	$0.$ (fixed)	
			$\overline{2}$	$0.09 \pm 0.04$	$-1.17 \pm 0.29$	
	$2^{--}$	$\pm 1$	1	$0.01 \pm 0.02$	$5.60 \pm 3.00$	
			3	$0.05 \pm 0.04$	$-0.06 \pm 0.62$	
	$3^{--}$	$\overline{0}$	3	$0.03 \pm 0.06$	$0.00 \pm 6.28$	
		±1	3	$0.42 \pm 0.07$	$2.38 \pm 0.08$	
	$3^{+-}$	$\overline{0}$	$\overline{2}$	$0.59 \pm 0.04$	$1.19 \pm 0.08$	
			4	$0.47 \pm 0.06$	$-4.35 \pm 0.09$	
	$4^{-1}$	$\pm 1$	3	$0.04 \pm 0.06$	$0.88 \pm 1.36$	
			5	$0.05 \pm 0.06$	$2.76 \pm 1.00$	
	$5 - -$	$\overline{0}$	$\overline{5}$	$0.76 \pm 0.07$	$-3.14 \pm 4.58$	
		±1	5	$0.69 \pm 0.04$	$0.58 \pm 0.07$	
	$5^{+-}$	$\bf{0}$	$\overline{4}$	$0.54 \pm 0.04$	$4.36 \pm 0.10$	
			6	$0.89 \pm 0.05$	$3.89 \pm 0.07$	
$\eta\omega$	$1 - -$	$\overline{0}$	1	$0.74 \pm 0.03$	$0.$ (fixed)	
1940 MeV/c		±1	$\mathbf{1}$	$0.18 \pm 0.02$	$0.$ (fixed)	
	$1 + -$	$\bf{0}$	$\mathbf{0}$	$0.18 \pm 0.01$	$0.$ (fixed)	
			$\overline{2}$	$0.08 \pm 0.04$	$-3.96 \pm 0.39$	
	$2^{--}$	$\pm 1$	$\overline{1}$	$0.04 \pm 0.01$	$0.25 \pm 0.68$	
			3	$0.17 \pm 0.02$	$1.74 \pm 0.12$	
	$3^{--}$	$\overline{0}$	3	$0.54 \pm 0.03$	$5.43 \pm 0.08$	
		±1	3	$0.48 \pm 0.04$	$5.18 \pm 0.07$	
	$3+-$	$\overline{0}$	$\overline{2}$	$0.60 \pm 0.02$	$0.84 \pm 0.04$	
			$\overline{4}$	$0.03 \pm 0.02$	$-0.04 \pm 1.10$	
	$4 - -$	$\pm 1$	3	$0.04 \pm 0.03$	$-0.52 \pm 0.74$	
			5	$0.32 \pm 0.04$	$-1.12 \pm 0.08$	
	$5^{--}$	$\overline{0}$	5	$0.00 \pm 0.26$	$3.05 \pm 0.00$	
		±1	5	$0.45 \pm 0.02$	$1.88 \pm 0.09$	
	$5^{+-}$	$\bf{0}$	4	$0.31 \pm 0.02$	$3.16 \pm 0.09$	
			6	$0.58 \pm 0.04$	$-4.11 \pm 0.04$	

**Table 5.** Magnitudes and phases of  $\alpha_L^{T}$ , describing the best fit to the angular distributions for the case  $J_{max} = J_{max}^{cont}$ . The beam momentum is well as a series of the contract o

- even angular momenta are suppressed for all channels at all momenta
- $f = \text{for } pp \longrightarrow \pi^* \omega$  (all momenta). The dominant contributions originate from  $J = J_{\text{max}}$
- for positive and all momenta-dominant contributions of the dominant contribution of the dominant contribution o butions originate from  $J < J<sub>max</sub><sup>contr</sup>$
- $M = 0$  singlet states are preferred for pp  $\longrightarrow \pi^{\cdot} \omega$
- M triplet states are preferred for pp exception 

 MeV"c-

 dency because J is not allowed for ! nal states It is interesting to consider the dependence of the maxi mal contributing angular momenta on the produced mass. Table 6 shows the values of  $J_{\rm max}^{\rm max}$  for the reactions discussed here. In addition values for two  $0\,$   $\,$   $\,$  reactions  $\,$ [5] and for  $\omega\omega$ -annihilation [9] are given. The columns are arranged from left to right according to the masses of the particles produced. There is a slight tendency for  $J_{\rm max}$  -values to decrease with increasing masses (e.g.  $\pi \omega/\eta \omega$  at 1200 MeV(c). The value  $J_{\text{max}}^{\text{max}}$  = 2 for  $pp \longrightarrow \pi^+ \pi^-$  at our mev/c does not contradict this ten-

The data and analyses presented here form the ba sis for future work on  $\bar{p}p$ -annihilations in flight measured with the CB-detector. They demonstrate that the CBdetector in spite of its geometry is able to reasonably measure forward peaked angular distributions In the

decay channel		$\pi^{0}\pi^{0}$	$\pi^{\vee}$	$\pi^0\omega$	ηη	$n\omega$	$\omega\omega$	$\eta\omega$
mass	$\sqrt{\mathrm{MeV/c^2}}$	269.95	682.43	916.92	1094.90	1329.39	1563.88	1739.71
	$600~\mathrm{MeV/c}$	റ		.,				
nomentum	$1200 \text{ MeV/c}$					3		
	$1940 \text{ MeV/c}$	6		5		h.		

**Lable 6.** Contributing maximal angular momenta for  $\sigma \omega$ ,  $\sigma \sigma$  for and  $\omega \omega$  [9]

meantime, similar data have been taken at further  $\bar{p}$ momenta and are presently being evaluated. Together with the data presented here, they will form a set of data allowing a mass scan of specific partial waves up to 2.4 GeVC

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Fig- - Upper gures Change of Log-likelihood values <sup>L</sup> black squares as <sup>a</sup> function of Jmax as tted to the data The open diamonds describe the expected change of the increase of the increase of the increase of the increase of the n . A form and the form of the form and a function of Jmax From bottom to top singlet M - Journal M - Journal M and triplet  $M = -1, +1$  for J even. The value  $J_{\rm max}$  is emphasized by vertical lines.



 $\bf r$  ig.  $\bf o.$  Change of Log-ukeunood values  $\Delta\cal L$  and the Partial intensities for 1200 and 1940 MeV/c. For explanation of symbols see Fig. 5.

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