

Measurement of the muon flux at SND@LHC

S. Ilieva Ilieva¹,

Abstract

The Scattering and Neutrino Detector at the LHC (SND@LHC) is a compact standalone experiment, which started taking data at the beginning of Run 3 of the LHC. The experiment is designed to perform measurements with high-energy neutrinos in range 100 GeV–1 TeV produced at the LHC in a previously unexplored pseudo-rapidity range of $7.2 < \eta < 8.4$. The detector, located 480 m downstream of the ATLAS interaction point in the TI-18 tunnel, comprises a hybrid system based on an 800 kg target mass of tungsten plates, interleaved with emulsion and electronic trackers, followed downstream by a calorimeter and a muon system. The first electronic detector measurement of the muon flux in the TI-18 tunnel, using the SciFi tracker and downstream muon detector, is reported here. The geometrical acceptance of the downstream muon detector exceeds and fully covers the SciFi one. The measured muon flux through a 31×31 cm² central SciFi area is

$$2.06 \pm 0.01(\text{stat}) \pm 0.11(\text{sys}) \times 10^4 \text{ fb/cm}^2,$$

while for the downstream muon system the flux is

$$2.35 \pm 0.01(\text{stat}) \pm 0.08(\text{sys}) \times 10^4 \text{ fb/cm}^2$$

for a 52×52 cm² central detector area. The total relative uncertainty of the results is 5 % for the SciFi and 3 % for the DS measurement. The Monte Carlo simulation prediction of these fluxes is 20-25 % lower than the measured values.

¹ *Università di Napoli “Federico II”, Napoli, Italy*

VERSION	DATE	COMMENTS
01	02.10.2022	First version

Contents

1	Motivation	1
2	Detector description	1
2.1	Apparatus	1
2.2	Detector location and coordinate system	2
3	Data	4
4	Simulations	5
5	Detector spatial and time alignment	7
6	Tracking	11
6.1	Tracking environment	13
6.2	Tracking methods	16
6.2.1	Simple tracking	16
6.2.2	Hough transform	20
6.2.3	A final remark on tracking methods	21
6.3	MC tracking efficiency	23
6.4	Tracking efficiency with data	23
6.4.1	SciFi tracking efficiency using data	26
6.4.2	DS tracking efficiency using data	27
7	Angular distribution	35
8	Muon flux	38
9	Data/MC simulation comparison	43
10	Conclusions	46

1 Motivation

2 The majority of recorded events in the SND@LHC detector consist of long-range
 3 muons produced in proton-proton collisions at the ATLAS interaction point, hence-
 4 forth referred to as IP1 following the LHC convention. Besides detector response
 5 studies and calibration, muons penetrating the full detector possess two analysis
 6 purposes. First, it is the measurement of the muon flux at the SND@LHC loca-
 7 tion, i.e. in a very forward rapidity range. Second, the muon flux measurement is
 8 also important since muons reaching the detector location are the main source of
 9 background for the neutrino search. Muons can either enter the detector without
 10 being vetoed and generate showers via bremsstrahlung or deep inelastic scattering,
 11 or interact in the surrounding material and produce neutral hadrons entering the ap-
 12 paratus and possibly mimicking neutrino interactions. The muon flux measurement
 13 is the subject of the current note.

2 Detector description

2.1 Apparatus

16 The SND@LHC detector [1] is designed to perform measurements with high energy
 17 neutrinos (100 GeV–1 TeV) produced at the LHC in the forward pseudo-rapidity
 18 region $7.2 < \eta < 8.4$. It allows the identification of all three flavours of neutrino
 19 interactions with high efficiency.

20 SND@LHC is a compact hybrid apparatus, shown in Figure 1.

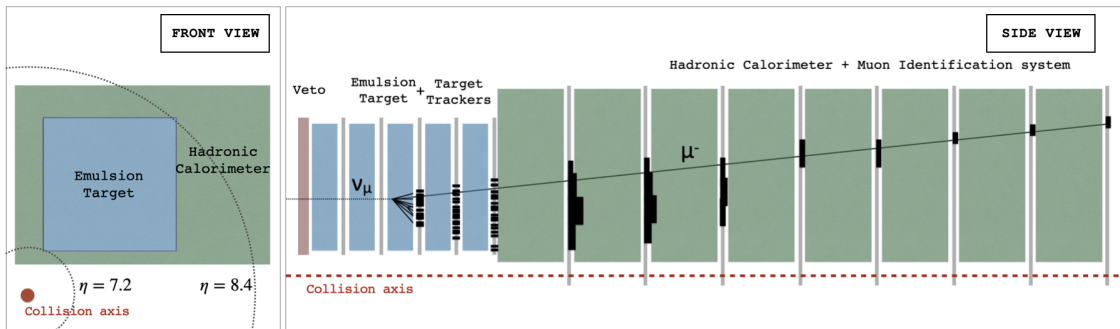


Figure 1: Layout of the SND@LHC detector.

21 It consists of three parts: veto, target and muon systems. The veto detec-
 22 tor (Veto) is situated in front of the target region. It is made of two planes, with
 23 a relative shift vertically with respect to one another, of seven vertically stacked
 24 $42 \times 6 \times 1 \text{ cm}^3$ scintillating bars. The Veto tags the passage of charged particles,
 25 which are mostly muons from IP1. The target section contains five walls. Each
 26 wall consists of four units of emulsion cloud chambers (ECC) and it is followed by a
 27 Scintillating Fibre tracker (SciFi) station. The muon system is placed downstream
 28 of the target. The electronic detectors, Veto, SciFi and muon systems, provide the

time stamp of the neutrino interaction, preselect the interaction region, measure the energy of electromagnetic and hadronic showers, and identify muons.

The sub-micrometric precision of nuclear emulsions allows the detection of short-lived particles like tau leptons. Each ECC module is a sequence of 60 emulsion films, $19.2 \times 19.2 \text{ cm}^2$, interleaved with 59 tungsten plates, 1 mm thick. Its weight is approximately 41.5 kg, adding up to 830 kg for the total target mass. The tungsten plates in one brick amount to about 17 radiation lengths, X_0 , or about 85 X_0 for the whole target. Each SciFi station consists of two $39 \times 39 \text{ cm}^2$ x - y planes of staggered scintillating fibres with a diameter of $250 \mu\text{m}$. The fibres are arranged in six densely-packed staggered layers, forming fibre mats of 1.35 mm thickness. Each mat is 13 cm wide and 39 cm long. Three fiber mats are integrated into a fibre plane, with less than $500 \mu\text{m}$ dead zones. The spatial resolution of single hits, about $150 \mu\text{m}$, is sufficient to link hits with an interaction in an ECC. The data from the ECC is not used for the analysis described in this note.

The muon system consists of two parts: upstream (US), the first five stations, and downstream (DS), the last three stations. In combination with SciFi, it acts as a coarse sampling calorimeter ($\sim 9.5 \lambda_{\text{int}}$), providing the energy measurement of hadronic jets. Each US station consists of 10 vertically stacked scintillator bars of $82.5 \times 6 \times 1 \text{ cm}^3$, similar to the upstream veto detector. Each DS station consists of two layers of thin bars, one horizontally and one vertically arranged, allowing for a spatial resolution less than 1 cm and acting as Muon Identification system. The most downstream DS station has an additional plane of horizontally stacked bars. The DS stations are interleaved with 20 cm thick iron blocks. Each of the latter is equivalent to 11 X_0 , or 33 X_0 in total for the whole DS system.

The readout electronics for the SciFi are arrays of silicon photomultipliers (SiPMs) which are glued to the fiber mats. The Veto and the muon system bars are also read out using SiPMs technology. For Veto and US bars, 8 SiPMs are reading the signal on each side of their horizontal bars. The signal in DS vertical bars is collected by a single SiPM on the top, while horizontal bars are readout by one SiPM on each side.

In many instances throughout the current note the short acronym denoting each system (Veto, SciFi, US, DS) is combined with a number indicating the Veto, SciFi, or the downstream muon system plane. For example, Veto 1, Veto 2, SciFi 1, ..., SciFi 5, US 1, ..., US 5, DS 1, ..., DS 4. The convention is the numbering of each system's planes and stations starts from the front of the detector, i.e. left to right on Figure 1. Additionally, the position of the electronic readout for a given detector element is indicated using L for left- and R for right-hand side readout position with the line-of-sight direction being from Veto to DS.

2.2 Detector location and coordinate system

The SND@LHC detector is placed in the TI-18 service tunnel that was initially constructed for injection of positrons from the SPS to the LEP accelerator. The schematic in Figure 2 describes the detector location in the accelerator area. The position is between the ATLAS interaction point (IP1), which is 480 m away, and the ALICE

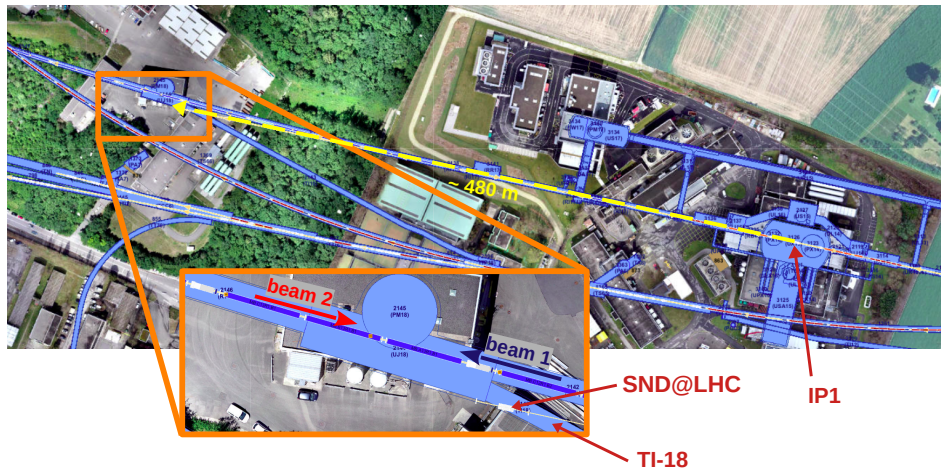


Figure 2: The location of the SND@LHC detector in the LHC complex area. The apparatus is located in the TI-18 tunnel, 480 m away from IP1. The directions of the two circulating beams, Beam 1 (blue) and Beam 2 (red) are shown in the zoomed panel. Beam directions and colors follow the convention used in Reference [2].

72 IP (IP2), which is more than 2 km away from the detector. Given the closer prox-
 73 imity and the much higher luminosity compared to IP2, beam crossings at IP1 are
 74 by far the dominant source of particles reaching the detector.

75 For every LHC fill a well-defined bunch structure, also noted as LHC filling
 76 scheme, is available at the LHC Programme Coordination web page [3]. The fill-
 77 ing scheme specifies which bunches cross at different interaction points and which
 78 bunches of Beam 1 and Beam 2 are circulating in the LHC without collision. It
 79 is a common convention that the clock-wise circulating beam is denoted Beam 1,
 80 while the counter clock-wise circulating one is Beam 2 [2]. Only after the bunches
 81 have been accelerated to the target energy and the LHC enters the "Stable beams"
 82 operation stage [4], bunches are brought to collision.

83 The information regarding the LHC bunch structure is synchronized with the
 84 SND@LHC event timestamp. The phase adjustments for both beams are done
 85 by finding the phase shift with maximum overlap with SND@LHC event rates.
 86 For Beam 1, it means matching the highest event rates to IP1 collisions. The
 87 synchronized bunch structure provides input on whether an event is associated with
 88 IP1 collisions. However, circulating beam particles can eventually interact with the
 89 machine elements, independent of whether the particle is in a colliding bunch or not.
 90 The filling scheme allows unambiguously to identify events originating from Beam 1
 91 which was not colliding in IP1, and Beam 2 which was not colliding in IP2.

92 The coordinate system adopted by the SND@LHC collaboration is presented in
 93 Figure 3. Its origin, the DCUM.480, is on the IP1 beam collision axis, 480 m away
 94 from IP1. The Z axis is aligned with the beam collision axis, the LHC machine axis
 95 at IP1, and points from IP1 towards the TI-18 tunnel. The Y axis is perpendicular

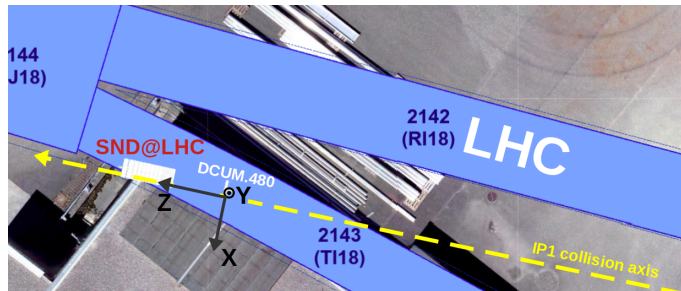


Figure 3: The SND@LHC coordinate system. The origin is noted DCUM.480 and is 480 m away from IP1. The Z axis is aligned with the IP1 beam collision axis for null crossing angle. The Y axis is perpendicular to the LHC machine plane and points upwards. The X axis is perpendicular to Y and Z and points away from the LHC center.

96 to the LHC machine plane and points upwards. The X axis is perpendicular to
 97 Y and Z and points away from the LHC center, as to have a right-handed coordinate
 98 system. In this coordinate system the $y - z$ plane contains local gravity and is the
 99 vertical plane, while the perpendicular $x - z$ plane is the horizontal one.

100 3 Data

101 The LHC Run 3 commissioning proton-proton collisions at 450 GeV served to
 102 confirm that the detector is operating as expected and traversing muons, other than
 103 cosmic-ray muons, can be successfully reconstructed. The detectors were running
 104 for the first LHC Run 3 proton-proton collisions at 13.6 TeV on July 5, 2022, and
 105 were taking data until the end of 2022. Detector operation has mostly been smooth
 106 and issues identified and sorted out promptly.

107 During the complete LHC proton run at 13.6 TeV, the recorded integrated lumi-
 108 nosity for SND@LHC 2022 run is $36.8 fb^{-1}$. It comprises 95% of the total $38.7 fb^{-1}$
 109 delivered luminosity at IP1 reported by the ATLAS collaboration [5, 6]. After the
 110 end of the proton-proton run on November 28, 2022, the last batch of emulsions was
 111 extracted. Still, the electronic detectors kept recording events during the following
 112 LHC ion run and continue operation as of now.

113 For this analysis, data collected during proton-proton collisions at 13.6 TeV
 114 energy, and "Stable beams" mode of the LHC accelerator are used. Two SND@LHC
 115 runs are selected. Information about them is outlined in Table 1. It includes the
 116 LHC fill number, integrated luminosity, mean number of inelastic pp collisions per
 117 bunch crossing, run number, number of recorded events, the date and duration for
 118 each run.

119 The run selection is based on event counts and the LHC filling scheme. The
 120 latter is important since it allows to identify muons from different origins which
 121 enter the detector depending on the passing beam direction and presence of proton-
 122 proton collisions. Muons penetrating the detector originate in IP1 collisions, as well
 123 as Beam 1 and Beam 2 interacting with the LHC machine elements or residual gas.

LHC fill number	L_{int} [fb^{-1}]	mean $N_{interactions}$ per bunch crossing	SND@LHC run number	N_{events} [10^6]	date, year 2022	duration [h]
8088	0.337	35.2	4705	71	3 Aug	12.5
8297	0.529	45.4	5086	101	20 Oct	19.8

Table 1: List of selected SND@LHC 2022 data runs. The runs are chosen to have large event counts, high delivered luminosity, isolated LHC bunches of Beam 2 passing without collisions, and different LHC filling schemes.

124 The filling scheme for LHC fill 8297 is a mixed one with alternated 25-ns bunch
 125 trains and 8 bunches and 4 empty slots (8b4e) trains. It suppresses the formation of
 126 electron cloud in LHC arcs and reduces beam-gas interactions [7]. The goal of the
 127 current analysis is the measurement of the muon flux at the SND@LHC detector
 128 that is associated with proton-proton collisions at IP1 and at LHC’s top energy of
 129 6.8 TeV per beam. The contributions of Beam 1 and Beam 2 interacting with the
 130 LHC machine elements or residual gas have to be subtracted from the total number
 131 of recorded muons. This is done using the filling scheme to identify Beam 1 passing
 132 with no IP1 collisions, and Beam 2 passing with no IP1 collisions. The selected runs,
 133 see Table 1, correspond to LHC fills with comparatively large isolated non-colliding
 134 Beam 2, and also non-colliding Beam 1, bunches, to facilitate extraction of their
 135 contribution.

136 The muon flux at the SND@LHC detector is estimated using emulsion data
 137 too. Emulsion runs are divided into groups following emulsion walls installation
 138 and extraction dates. A separate note treats the first emulsion data muon flux
 139 measurement [8].

140 4 Simulations

141 Apart from the data-driven tracking efficiency evaluation, simulations are used
 142 to estimate the Monte Carlo track reconstruction efficiency. Generally, the Monte
 143 Carlo simulation consists of two stages. The first step combines the generation of
 144 proton-proton collisions at the IP1 and the propagation of collision debris in the
 145 accelerator tunnel to a virtual scoring plane in the rock tens of meters upstream
 146 of the SND@LHC apparatus. The second stage includes particle transport through
 147 the rock and the detector.

148 The first step is carried out by CERN’s SY-STI team using FLUKA [9, 10]. The
 149 DPMJET event generator [11, 12] is used to simulate pp collisions at 13.6 TeV. The
 150 proton beams crossing angle is accounted for in the simulation. The proton beams
 151 cross in IP1 with a half-angle of about 150 microradians, either upwards(positive
 152 angle) or downwards(negative angle) in the vertical plane. In the year 2022 LHC
 153 run, that angle was $-160 \mu\text{rad}$. In the upward/downward configuration, the beam
 154 axis as seen in TI-18 gets vertically displaced up to 8 cm above/below the ATLAS
 155 detector axis [1].

156 Particle transport in the LHC is done using the LHC FLUKA model [13, 14].
 157 It has a detailed tunnel description and is being constantly improved. The simu-
 158 lations for the SND@LHC experiment do not feature the ATLAS solenoid magnet,
 159 i.e. particles produced in IP1 collisions go through the ATLAS cavern that does
 160 not include the detector, but only the vacuum chamber and the forward shield-
 161 ing. On the other hand, the model of the LHC magnetic fields is essential for the
 162 SND@LHC Monte Carlo simulation muon rate studies. Muons and anti-muons can
 163 be deflected towards or away from the detector acceptance. Recently, the SY-STI
 164 team has extended the description of the LHC magnetic field including the magnetic
 165 field map in the yoke of the recombination dipole (D2) and the matching section
 166 quadrupoles (Q4 to Q7). This implementation, together with the inclusion of the
 167 tight setting of the TCL6 physics debris collimator (1 mm half-gap) adopted in
 168 the 2022 run, has brought the MC simulation prediction and the SND@LHC elec-
 169 tronic detector muon flux measurement to a much better agreement than previously
 170 observed: a factor of 2 reduction of the predicted flux is obtained following the mag-
 171 netic field map expansion and the TCL6 collimator tightening. For this reason when
 172 making data/simulation comparisons in Section 9, two MC simulation sets are being
 173 considered, one before and one after adjusting the simulations to the actual experi-
 174 mental conditions as far as beam crossing angle, collimator settings, and magnetic
 175 field range are concerned. The differences between these two MC simulation samples
 176 are outlined in Table 2. These are the number of generated proton-proton collisions,
 177 scoring plane size, the beam crossing angle, the TCL6 gap, and the magnetic field
 178 map coverage. In both cases the scoring plane is centered on the ATLAS detector
 179 axis. Regardless of the larger surface of the first plane, they both cover the spatial
 area which contributes the most to the muon rate at the location of the detector.

date produced	number of pp collisions [10^6]	scoring plane size [m^2]	beam crossing angle [μrad]	TCL6 half-gap [mm]	magn. field map coverage
March 2022	10	2.5×2.5	-150	2	-
March 2023	200	1.8×1.8	-160	1	extended

Table 2: Overview of the two FLUKA samples of muons from IP1 proton-proton collisions that are used for the data/MC simulation comparison in Section 9. The number of generated pp collisions, the scoring plane size, the beam crossing angle, the TCL6 collimator settings, and the magnetic field coverage differ. The March 2023 set is preceded by a smaller 50-million pp collisions set that indicates the better agreement between data and MC simulation. Afterwards the larger-statistics simulation sample has been generated by the CERN SY-STI and provided to the SND@LHC collaboration.

180

181 The FLUKA particle transport is stopped at a virtual scoring plane where po-
 182 sitions and momenta of muons are recorded together with their statistical weight,
 183 which is different from 1 because of the use of convenient biasing techniques, and
 184 information on the muon history. For the latest FLUKA sample, the plane has di-
 185 mensions $1.8 \times 1.8 m^2$. It is located 60 m upstream of the TI-18 tunnel in order to

186 decouple muon interactions in rock and concrete upstream of the detector from the
 187 primary flux of muons produced at the IP and within LHC machine elements.

188 The second stage of the simulation chain is carried out by the SND@LHC team.
 189 The FLUKA simulation output serves as input for a GEANT4 [15] particle transport
 190 to and through the detector. Not all primary muons, i.e., muons recorded at the
 191 scoring plane, enter the detector. Also, primary muons can interact along the way
 192 and initiate new particle production. All generated particles are propagated through
 193 the rock upstream of the detector, then the TI-18 tunnel and the detector volume.
 194 It is found that particles produced by a primary muon more than 10 m upstream of
 195 the apparatus do not reach it.

196 After the simulation event sample is produced, the particle's energy loss in the
 197 SND@LHC sensitive detectors, SciFi fibers and veto and muon system bars, is dig-
 198 itized. The light propagation and attenuation inside the scintillators are taken into
 199 account. If several particles have passed through a sensitive volume in the same
 200 event, the sum of their energy deposit and the timing of the earliest entering par-
 201 ticle are assigned to the digitized hit charge and time. Additionally, each hit's
 202 timing information is smeared using the detector time resolution of a few hundred
 203 of picoseconds [16]. For SciFi, the known conversion of energy to number of pho-
 204 toelectrons, and a signal threshold check are applied. Per detector element with
 205 non-zero deposited energy, there is one digitized hit assigned to the corresponding
 206 readout channel. If the readout of the element is realized on more than one SiPM
 207 channels, the signal is equally divided between SiPMs. This is the case for the hor-
 208 izontal bars in the muon system. It is important to note that track finding is based
 209 on the coordinates of the fired detector elements. Besides the hit's signal threshold
 210 and unless otherwise imposed, tracking is independent of the charge and arrival time
 211 hit attributes.

212 5 Detector spatial and time alignment

213 The SciFi spatial alignment is made by minimizing the residuals of the muon trajec-
 214 tory with respect to the measurements used. The event selection for this procedure
 215 requires at least 10 measurements and a converged track fit using at least 8 mea-
 216 surements. The residual is calculated using the distance of closest approach between
 217 a SciFi track and a fired detector element. The SciFi detector consists of 5 stations
 218 and each of them is made of a horizontal and a vertical plane, with 3 mats of fibres
 219 in each plane. The alignment parameters used are the relative mat positions in the
 220 measurement plane and the rotation angles for the whole plane, see Figure 4. The
 221 procedure is not sensitive to the Z position. The initial positions are taken from
 222 the survey [17], which have a precision of about 1 mm. For each projection, in two
 223 of the planes the position of one mat is fixed, since the procedure cannot determine
 224 the global alignment of the SciFi detector within the TI-18 tunnel. The rotation
 225 of one plane is fixed. The alignment is done after each emulsion replacement. The
 226 procedure uses an iterative approach by running the SIMPLEX algorithm of Minuit
 227 by minimizing the residuals of the fitted track and its measurements. The final
 228 residuals have a spread of typically 150 - 200 μm , larger than expected from the

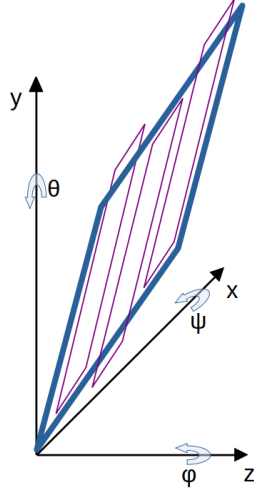


Figure 4: A schematic of a SciFi plane (blue titled square) comprising 3 mats (violet tilted rectangles). The SciFi spatial alignment procedure determines the relative positions of the mats in the plane and the rotation of the whole plane.

229 pure detector resolution [16] due to the material between stations and large mul-
 230 tiple scattering. Figure 5 presents the residuals per mat before and after spatial
 231 alignment.

232 The SciFi time alignment is done using the timing of measurements used for
 233 a SciFi track fit. The time is corrected for the signal speed knowing the particle
 234 impact point from the particle trajectory. A velocity of 15 cm/ns is assumed [16].
 235 In the first step, each station is time aligned internally. The channels within a SciFi
 236 mat are already well aligned. For each station, there are 2×3 time constants (two
 237 planes, each plane made of 3 mats) to be determined and 9 available time difference
 238 measurements for each combination of mats, see Figure 6a. The time constant
 239 for mat 0 of the horizontal plane is set to zero. Minuit is used to find the best
 240 solution for the other 5 constants. In the second step, the time alignment between
 241 the stations is determined by correcting for the time of flight of the particle. The
 242 average internal aligned time of a X and Y track measurement in a plane is used.
 243 There are 5 time constants to be determined and 10 time differences between stations
 244 available from the data, see Figure 6b. The time constant of the first station is set to
 245 zero, and Minuit is again used to get the best solution from the 10 mean differences
 246 between stations. Figure 7 shows an example of the timing residuals between SciFi
 247 stations 1 and 2, noted Δt on the plots, before and after time alignment. The data
 248 on each plot is fitted with a Gaussian and its width corresponds to about 250 ps
 249 time resolution per station.

250 The DS spatial alignment is done minimizing the residuals of DS hit positions
 251 with respect to extrapolated SciFi tracks. Since SciFi stations are moved for emul-
 252 sion extractions, even though the DS stations are stationary during all runs, the
 253 DS spatial alignment is re-done. Figure 8 is an example plot of DS X residuals
 254 before and after the alignment. In the presented case, the reference plane, where
 255 SciFi tracks are extrapolated to and their positions are compared to DS hits, is the

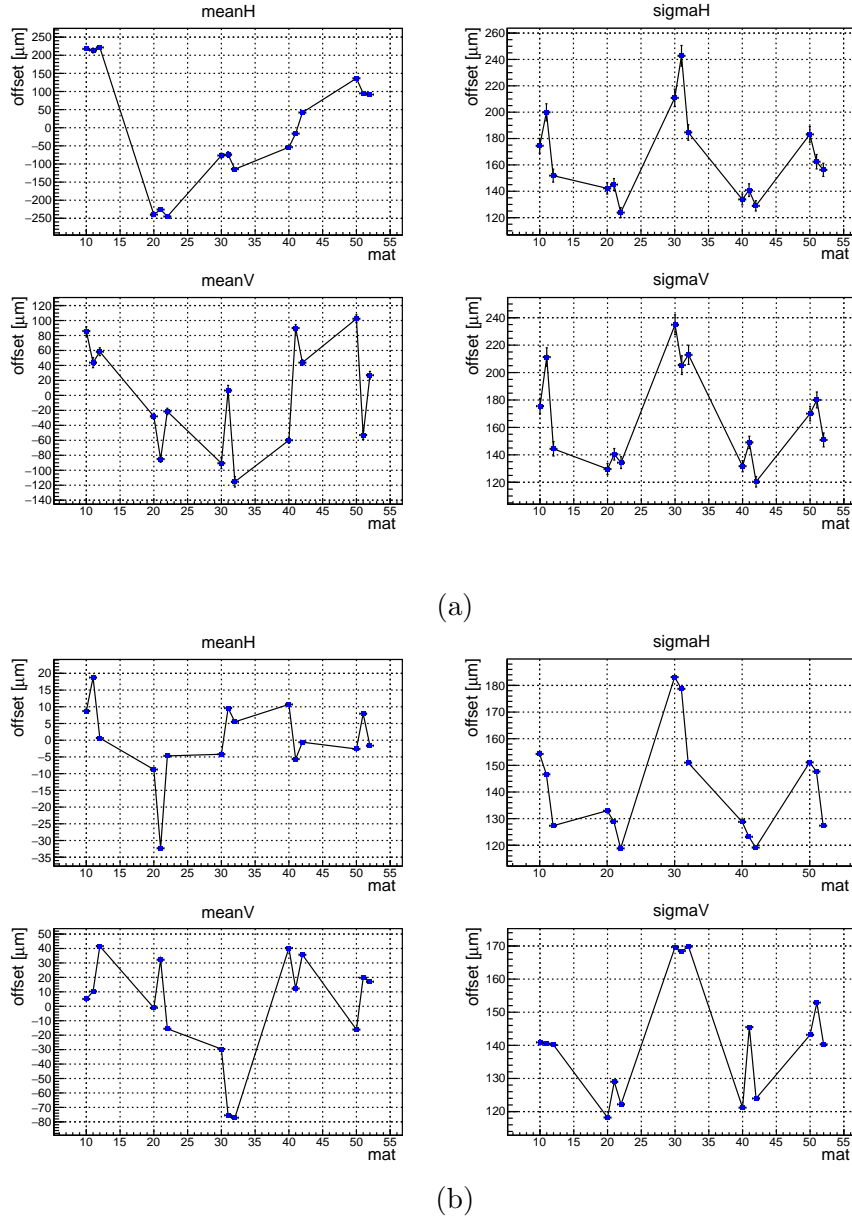


Figure 5: SciFi residuals before (a) and after (b) spatial alignment. Per horizontal (H) and vertical (V) projection there are the mean and widths of residual distributions per mat. For each plot, the abscissa label denotes the station by the tens of the number and the mat by the units. The top-panel plot is obtained using 1M events, while the bottom-panel one is for the full run. After the alignment residuals between tracks and measurements are significantly reduced. The vast majority of them have less than a 150-micrometer spread. Data from SND@LHC run 4705.

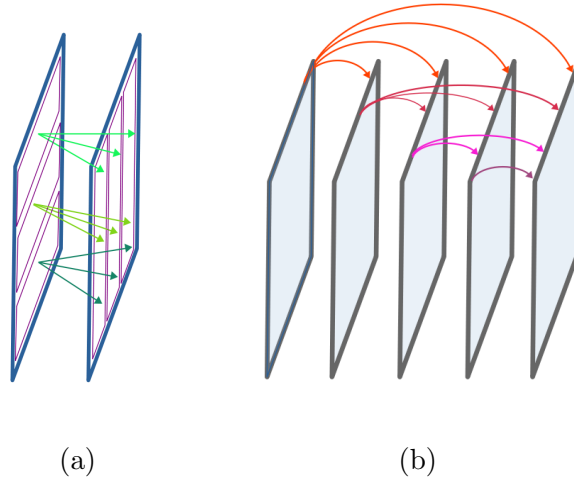


Figure 6: A diagram showing all mat combinations used for the internal time alignment of a SciFi station (a) and the station combinations used for the time alignment of the full SciFi detector (b). The arrows on each plot indicate the time difference measurements which are used in the alignment procedure. On plot (a), SciFi mats are depicted as violet tilted rectangles, while the two planes of horizontally and vertically staggered mats building up a station are presented as blue tilted squares. On plot (b), the 5 SciFi stations are depicted as tilted grey squares.

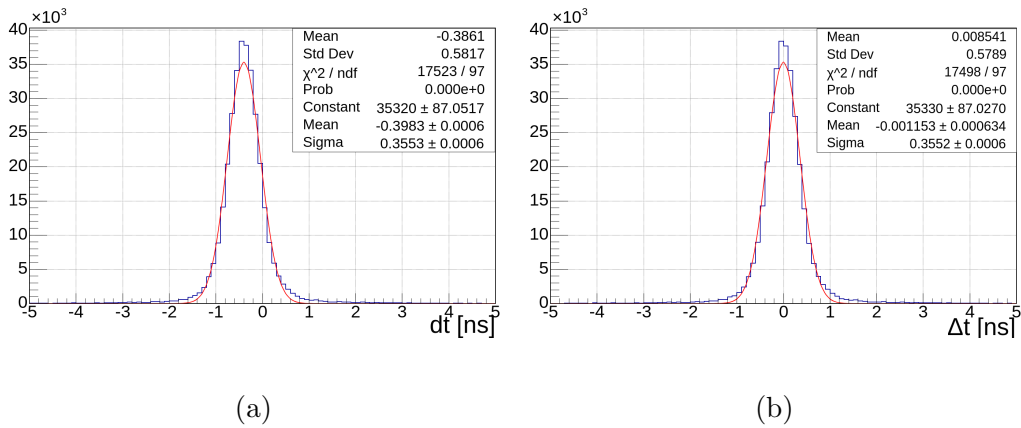


Figure 7: SciFi timing residuals between measurements in station 1 and 2 before (a) and after (b) time alignment. After the alignment, the residuals are symmetrically centered around 0. Each distribution is fitted with a Gaussian function. Its width corresponds to a 250 ps time resolution per station. Data from run 4705.

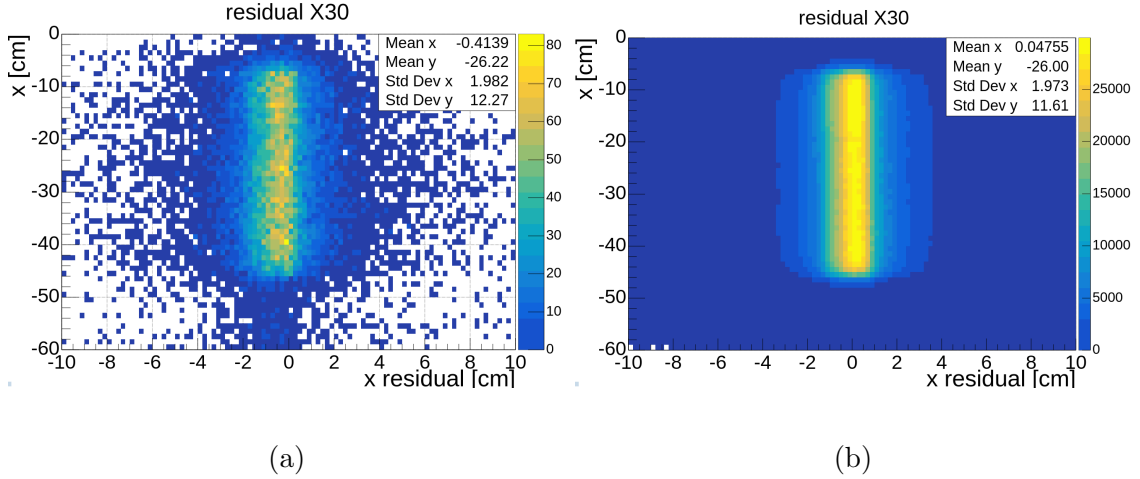


Figure 8: DS X residuals at the vertical DS 1 plane vs X position before (a) and after (b) spatial alignment. The left-panel plot is obtained using 1M events, while the right-panel one is for the full run. After the alignment, X residuals are reduced by a centimeter and symmetrically centered around 0. Data from run 4705.

256 vertical DS 1 plane.

257 The DS time alignment is done with respect to SciFi tracks. The latter are
 258 extrapolated to each DS plane. The timing residuals between a matched DS plane
 259 hit and the extrapolated track prediction are minimized. The timing residual, Δt ,
 260 is defined as

$$\Delta t = t_{DS \text{ hit}} - t_{sc. \text{ light}} - L/c - t_{SciFi \text{ ref}}. \quad (1)$$

261 The time of the recorded DS hit is $t_{DS \text{ hit}}$. The time of flight, L/c , between SciFi
 262 track's reference start position and the DS plane, assuming the particle's velocity
 263 $v = c$, is subtracted. The muon making the SciFi track crossed the reference start
 264 position at a time denoted $t_{SciFi \text{ ref}}$. The reference start position is SciFi 1. The
 265 time for scintillation light propagation inside a fired bar, $t_{sc. \text{ light}}$, is also accounted
 266 for. The light propagation speed along a DS bar is 15 cm/ns [16]. It is found that the
 267 DS time alignment is possible by applying a linear correction with a single slope and
 268 custom offsets per half-plane and readout side. Then, the time correction is applied
 269 per readout channel. The timing residuals after DS time alignment are shown on
 270 Figure 9.

271 6 Tracking

272 Tracking in the SND@LHC electronic detectors is performed independently in two
 273 detector sub-systems, the SciFi and the DS of the muon system. The Upstream
 274 Stations of the muon system are not considered for track building because of their
 275 large transverse dimension of $6 \times 1 \text{ cm}^2$. One argument for treating SciFi and DS as
 276 separate trackers is the much different granularity of their sensitive elements. While
 277 the DS transverse bar dimensions are $1 \times 1 \text{ cm}^2$, the width of the SiPM channels
 278 reading the SciFi fiber mats is only $250 \mu\text{m}$. Another reason is that by construction

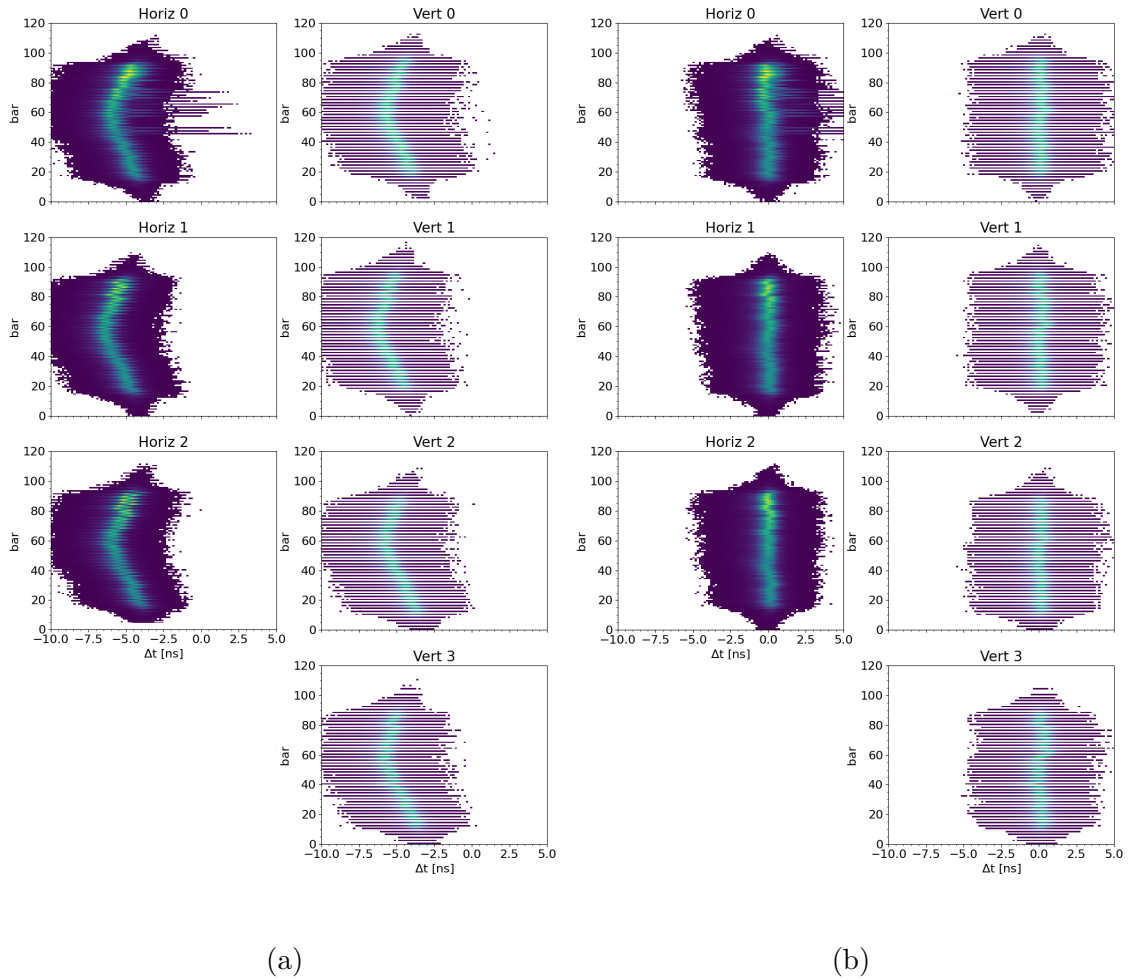


Figure 9: The timing residuals before (a) and after (b) DS time alignment. The timing residuals are defined in Equation 1. For horizontal DS planes, readout channels on the left detector side are noted using odd numbers, while even ones are reserved for right-side SiPMs. Vertical DS planes are readout only on the top, which is designated using odd numbers. Before time alignment, specific curved structures are clearly observable for each plane. They originate from differences in the routing of bar readout signals. All distributions are centered at $\Delta t = 0$ ns after the alignment. Data from run 4705.

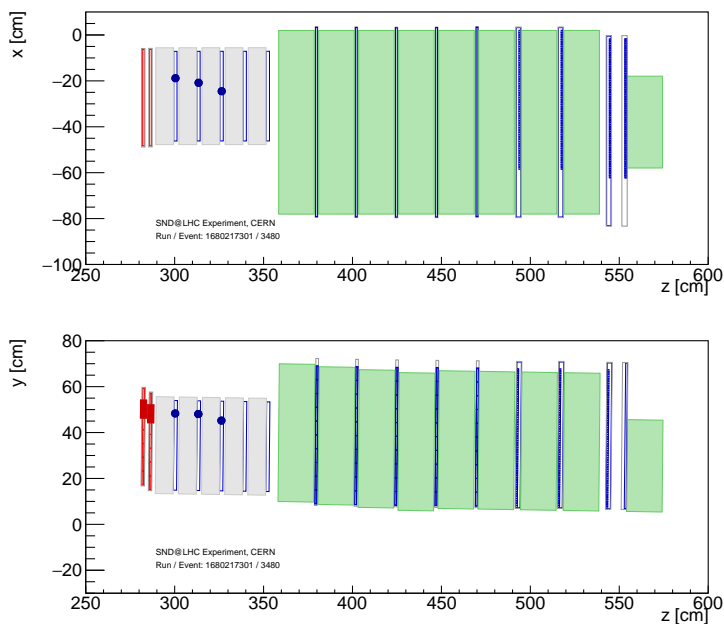


Figure 10: SND@LHC 2D event display of a simulated event where a 0.6 GeV muon is absorbed in the target region of the detector. The top panel shows the horizontal XZ plane, while the bottom one shows the vertical YZ plane.

279 the DS acceptance is 2.4 times larger than the SciFi one, with the DS fully covering
 280 the SciFi acceptance.

281 Most long-range muons traveling from IP1 towards the detector leave straight
 282 tracks in the latter owing to a lack of magnetic field in the apparatus vicinity. How-
 283 ever, multiple scattering in the heavy material of the detector can cause deviations
 284 of the muon trajectory. Its effect on the track angle and particle energy loss is
 285 discussed next in Section 6.1. Two complementary tracking methods used in the
 286 SND@LHC experiment are discussed in Section 6.2.

287 6.1 Tracking environment

288 Interactions in the heavy material between the electronic detectors planes are a
 289 challenge for particle tracking in the SND@LHC detector. These can be destructive
 290 processes that lead to muon absorption somewhere inside the detector and conse-
 291 quently inability to find a track. In other cases, processes like muon bremsstrahlung,
 292 delta-ray emission, and pair production generate additional activity in the detector
 293 and give rise to detector hits. Depending on the muon energy loss in these pro-
 294 cesses the number and energy of produced particles can be significant. However,
 295 this muon-induced radiation is typically colinear with the muon path and the corre-
 296 sponding hits are close to the muon ones. Further, there is also multiple scattering
 297 in the tungsten and iron. For low-energy muons, it can strongly deviate the muon
 298 trajectory, making it too bent to be fit. This is depicted in Figure 10, where the
 299 low-energy muon is in the end absorbed in the detector.

300 To demonstrate the effect of heavy material along the path of a high-energy
 301 particle, in Figure 11 the number of detector measurements per event are presented
 302 for data run 4705 and the passing-through-muons Monte Carlo simulation set dated
 303 March 2023. Detector measurements are either hits or clusters. The latter is a
 304 collection of fired adjacent detector elements. The time of a cluster is given by the
 305 earliest timestamp of any hit contributing to it. The data and simulation hit and
 306 cluster multiplicities do exceed the number of detector planes. For example, there
 307 are a total of 10 SciFi planes, 5 horizontal and 5 vertical, but the number of SciFi
 308 hits per event can be much larger than 10 for both data and passing-through-muons
 309 MC simulation. In each plot of Figure 11, the peak corresponds to a detector signal
 310 triggered by a passing-through muon. In Figure 11c, the larger value of the mean
 311 for data is explained by a displacement between the DS 1 horizontal bars and their
 312 readout SiPMs that appeared with time during the 2022 data-taking, see Figure 11e.
 313 Due to that shift, when a muon went through one bar, photons produced in that
 314 bar were collected by two SiPMs. Consequently, two digitized detector hits were
 315 created instead of a single one. The bar-readout shift appeared because the DS bars
 316 are manufactured with slightly different sizes and over time, gravity pulled them
 317 down with respect to SiPMs. To address this issue, special separators were installed
 318 between DS bars during the technical stop in the beginning of 2023. In general,
 319 data and MC simulation do show good agreement considering the number of hits
 320 and clusters per event.

321 The impact of heavy material along the muon trajectory in the detector can
 322 also be quantified in terms of energy loss, scattering angle, and displacement angles.
 323 The scattering angle, θ_{scatt} , is defined by the dot product of muon momenta entering
 324 (p_{in}) and going out (p_{out}) of a given volume:

$$\theta_{\text{scatt}} = \frac{(\vec{p}_{\text{in}} \cdot \vec{p}_{\text{out}})}{P_{\text{in}} P_{\text{out}}}. \quad (2)$$

The displacement angle is defined per projection, ($\theta_{\text{displ}_{xz}}$) and ($\theta_{\text{displ}_{yz}}$), as the ra-
 tio of the differences between X (or Y) and Z coordinates of a particle entering
 ($x_{\text{in}}, y_{\text{in}}, z_{\text{in}}$) and escaping ($x_{\text{out}}, y_{\text{out}}, z_{\text{out}}$) a given volume, i.e.

$$\theta_{\text{displ}_{xz}} = \text{atan} \left(\frac{\Delta x}{\Delta z} \right) = \text{atan} \left(\frac{x_{\text{out}} - x_{\text{in}}}{z_{\text{out}} - z_{\text{in}}} \right) \quad (3.1)$$

and

$$\theta_{\text{displ}_{yz}} = \text{atan} \left(\frac{\Delta y}{\Delta z} \right) = \text{atan} \left(\frac{y_{\text{out}} - y_{\text{in}}}{z_{\text{out}} - z_{\text{in}}} \right). \quad (3.2)$$

325
 326 The energy loss, scattering, and displacement angles and their dependence on
 327 energy are plotted on Figures 12-14. GEANT4 particle hit information in the detec-
 328 tor is used. The four different regions under consideration are shown in Figure 12c.
 329 As shown in Figure 12a, muons at the scoring plane 60 m upstream of the detector
 330 that have energy less than a few tens of GeV, do not reach the detector. The median
 331 of energy losses in both the target and the DS region is about 1 GeV. The energy

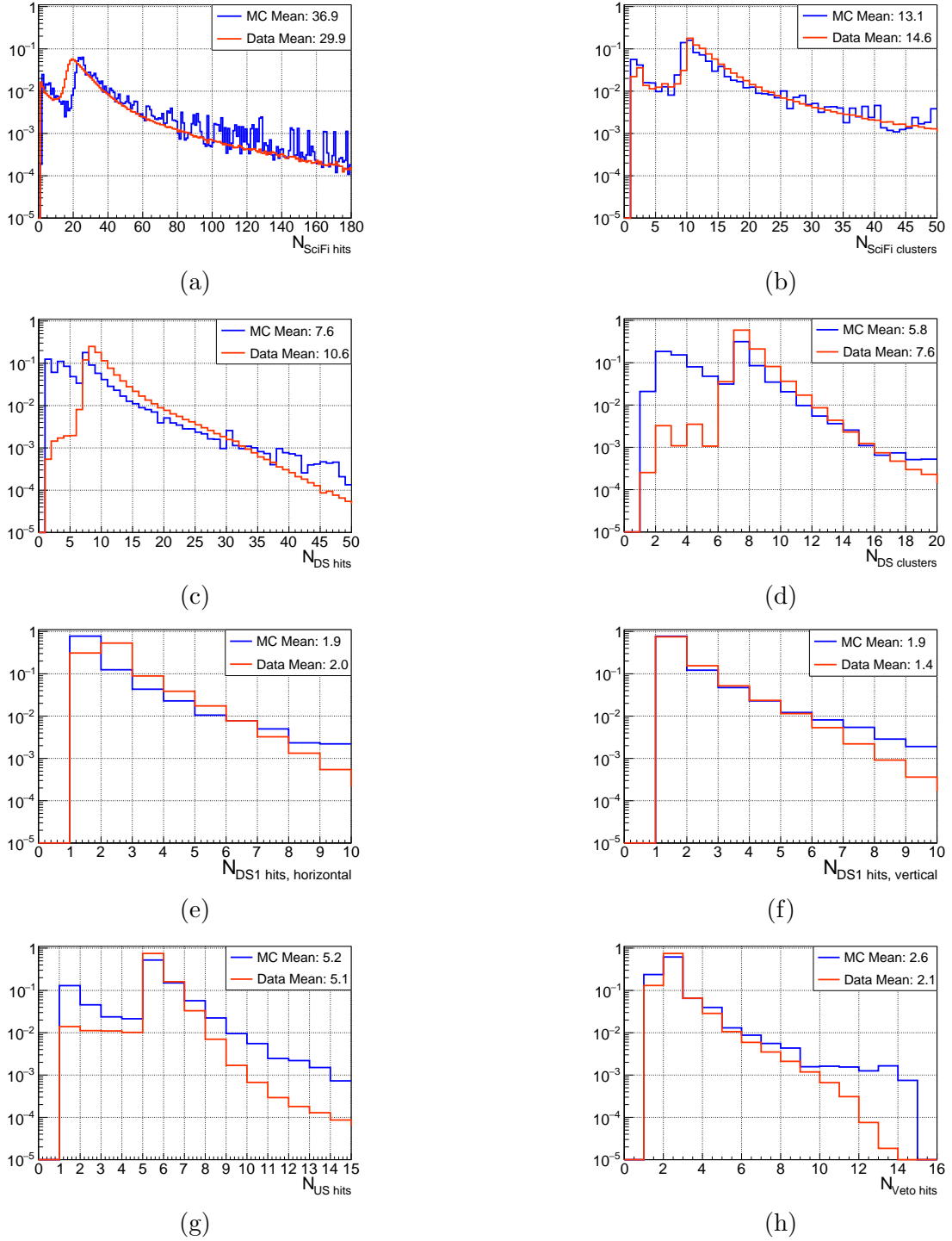


Figure 11: Detector measurement multiplicity per event for data (red) and Monte Carlo simulation (blue): SciFi hits (a) and clusters (b), DS hits (c) and clusters (d), DS1 hits in horizontal (e) and in vertical (f) bars, US hits (g), and Veto hits (h). They are all normalized to unit integral. The mean of each distribution is reported in the legend.

332 loss in the DS system for some muons is much lower than that. It is confirmed that
 333 these are muons passing through the very upper parts of the DS stations, which are
 334 not covered by the slightly shorter iron blocks. Thus energy loss for these particles
 335 is much lower.

336 The muon energy loss and scattering angle as functions of the initial muon energy
 337 before entering the target or the DS regions are shown in Figure 13. There is a wide
 338 spread in the energy losses for muons of energies above 200 GeV. Most muons,
 339 however, have lower energies and the respective losses are around 1 GeV, reported
 340 also in Figure 12a. As for the angles, low-energy muons can undergo large-angle
 341 scattering, while for muons above 30 GeV energy, the scattering is restricted to a
 342 10 mrad angle in both the target and the DS regions.

343 Another angular parameter is the displacement angle, see Equation 3. The
 344 distribution vs energy of the XZ and the YZ displacement angles in the target and
 345 the DS are plotted on Figure 14. A secondary angular direction, in the horizontal
 346 plane, is visible in Figures 14a and 14c. It does not correspond to a specific muon
 347 source, but rather to muon production via particle decay or interactions in various
 348 machine elements on the path from IP1. The muons angular distribution at the
 349 SND@LHC detector is discussed in more detail in Section 7.

350 6.2 Tracking methods

351 Two tracking methods were developed in the SND@LHC analysis framework. They
 352 differ in the way to find track candidates. One of the tracking methods makes use
 353 of a custom track finding solution. It is dubbed simple tracking(ST). The other
 354 tracking approach employs the Hough transform [18, 19] pattern recognition method
 355 and is referred to as Hough Transform(HT). In both cases, the track fitting is done
 356 using the Kalman Filter [20, 21] method in the GENFIT package [22, 23]. Each
 357 system's resolution for a single plane measurement, see Section 2.1, is used to set
 358 the covariance matrix elements used by the Kalman Filter.

359 Since all SciFi planes and vertical DS planes are read out on one side, their hits
 360 have two well defined spatial coordinates. Then, tracking in these syb-systems is
 361 done separately in the horizontal $x - z$ and vertical $y - z$ plane. The final 3D track
 362 is built combining the two 2D tracks. Events with multiple track candidates per
 363 projection can be reconstructed, but it creates degeneracy as to which two projec-
 364 tions belong to the same 3D particle trajectory. These multi-track cases are treated
 365 differently by the two tracking algorithms.

366 6.2.1 Simple tracking

367 The simple tracking is used for the detector alignment and online monitoring during
 368 data-taking. The specific properties of the ST are

- 369 • track building blocks are clusters of detector hits,
- 370 • tracking is only performed if at least 3 horizontal and also 3 vertical detector
 371 planes have no more than 5 clusters,

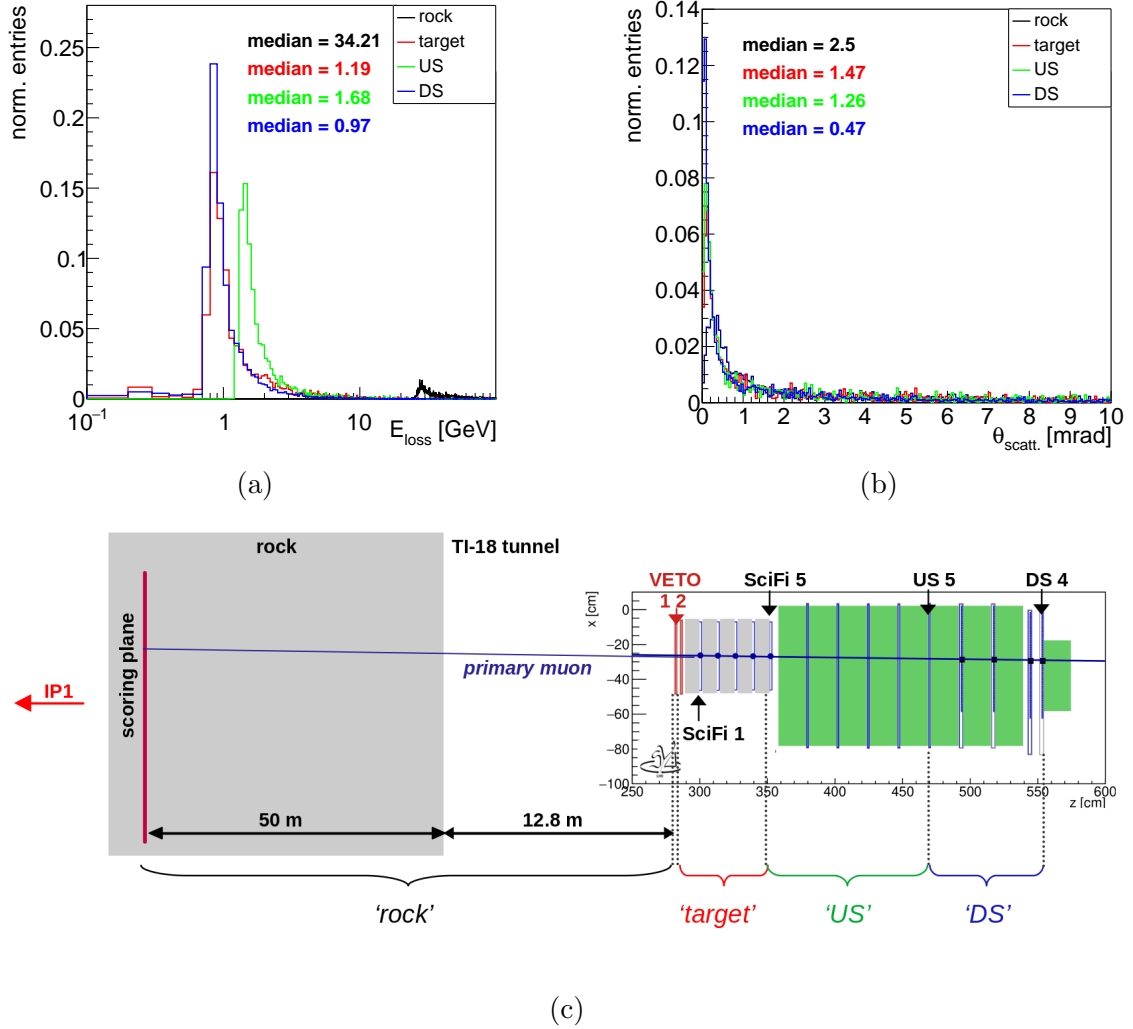


Figure 12: Energy loss (a) and scattering angle (b) for muons passing through different volumes (c) between the scoring plane and the detector. The distributions are normalized to unit integral. The distance between the scoring plane and the detector is not to scale. There are 50 meters of rock and 12.8 meters of air between the scoring plane and the SND@LHC apparatus. The region between the scoring plane and the very first detector element, Veto 1, is denoted as 'rock'. The label 'target' is for the neutrino target, i.e. the tungsten plates. However, the target here includes all materials between Veto 2 and SciFi 5. The US region starts at SciFi 5 and ends at the last US 5 station. The DS region spans from US 5 to the last DS 4 station.

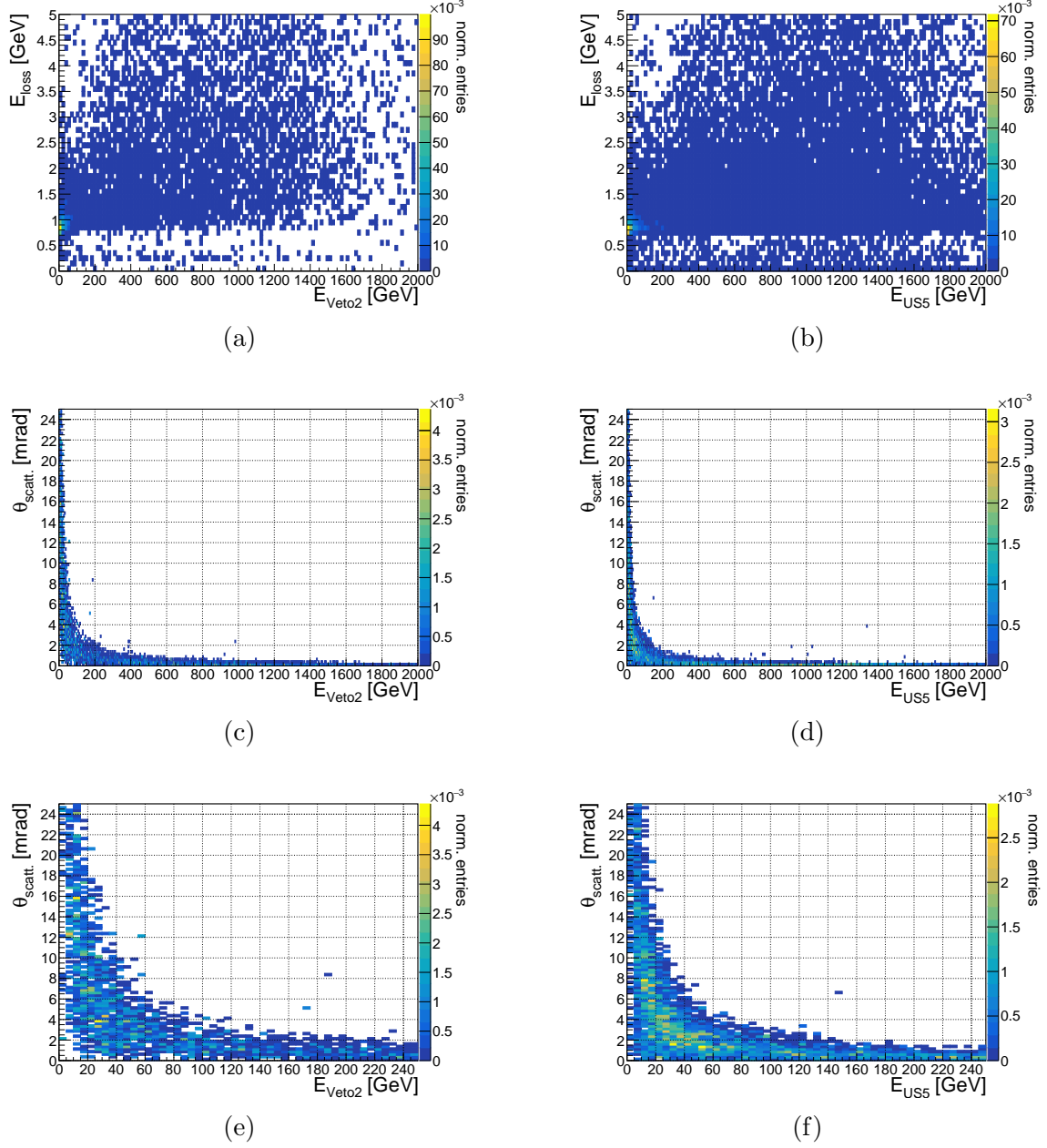


Figure 13: Energy loss vs E (a, b) and scattering angle vs E (c, d), also magnified in (e, f), for muons passing through the target(left side) and the DS regions(right side). The schematic drawing in Figure 12c depicts the target and the DS areas. The in-going energy of the muon entering each region is plotted on the abscissa.

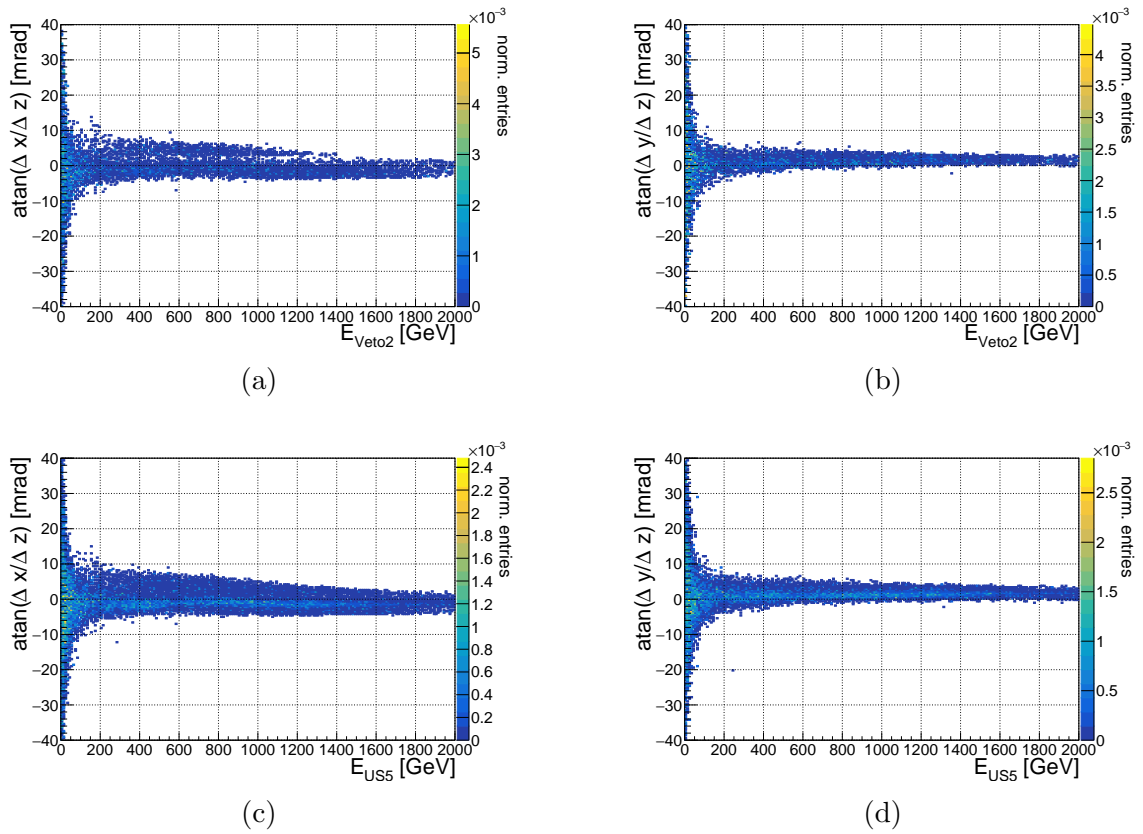


Figure 14: Displacement angles in the target (a, b) and the DS (c, d) in XZ(left panels) and YZ(right panels) projections. The schematic drawing in Figure 12c depicts the target and the DS areas. The in-going energy of the muon entering each region is plotted on the abscissa.

- 372 • to attempt DS tracking:
 - 373 – at least one plane has to have a single cluster, denoted a *seed cluster*
 - 374 – two planes together cannot have more than 6 clusters
- 375 • for SciFi tracking:
 - 376 – the SciFi planes with the highest occupancy are not used in the tracking
 - 377 (to avoid spurious associations) as long as there are at least 3 planes to
 - 378 allow a track fit
- 379 • the track fit is a straight line fit.

380 The SciFi track finding algorithm makes a straight-line fit in each projection
 381 and provides a list of clusters to the track fitter. While this track finding procedure
 382 is best suited to having one cluster per plane and projection, it also performs well
 383 with additional noise measurements. For the latter case, a coarse rejection of outlier
 384 clusters is made. Measurements having a cluster-to-fit residual larger than 7.5 mm
 385 are removed. The cut value is determined by scanning event displays. For reference,
 386 typical SciFi residuals are below 200 μm , as shown in Figure 5.

387 The DS track finding is based on minimization of the track residual. To start,
 388 lines are built for each combination of the seed cluster with clusters in the other
 389 planes that have the second lowest cluster occupancy, the plane of the seed cluster
 390 being the least occupied. Then, each line prediction is extrapolated to the remaining
 391 planes and the distance to clusters is calculated. The cluster combination with the
 392 smallest residual is chosen.

393 It is possible to reconstruct multiple SciFi tracks in an event using simple track-
 394 ing. The successful track candidates must have spatially well separated clusters, on
 395 the level of a few centimeters, in different tracking stations. This capability allows
 396 to study multi-trajectory events. However, it is not used to assess the muon rate in
 397 the detector.

398 6.2.2 Hough transform

399 The other tracking alternative, the Hough transform, has been developed to allow
 400 tracking in busy environments. Initially, the procedure was tuned to find muons
 401 produced in muon neutrino charged-current(CC) interactions. In the muon neutrino
 402 CC events, alongside the outgoing muon, a hadronic shower develops and generates
 403 numerous hits in the detector elements. Events with high hit occupancy may also
 404 originate from the passage of muons from the IP. Muons can interact in the detector
 405 material and produce multiple particles, mainly delta electrons and gamma rays. If
 406 the energy of these products is large enough, they initiate electromagnetic showers,
 407 which may span over one or more tracking stations. In both penetrating muons and
 408 neutrino CC interaction events, disentangling the muon from the accompanying
 409 shower is made possible using the powerful Hough transform method. Its role is
 410 to detect a line in the complicated picture of numerous fired detectors per tracking
 411 plane.

412 For the HT, when there are more than one track candidates per projection, it
 413 is checked whether the found candidates have a compact sample of slopes, i.e. that
 414 the predicted slopes are contained in a range comparable to the detector angular
 415 resolution. If that is the case, then the candidate having the slope closest to the
 416 sample's median is selected. In all other cases, the track fit is dropped. This strategy
 417 is well suited for the passing-through muon case. However, the HT procedure is also
 418 capable of finding multiple tracks per event.

419 After a track candidate has been found, it is verified to have passed through fired
 420 detector elements within a tolerance level. Much like the ST case, the requirement
 421 is that the HT line crosses within the tolerance at least 3 horizontal and 3 verti-
 422 cal planes. After that, the coordinates of these hit detector elements are used by
 423 GENFIT's Kalman Filter for a final 3D track fit. In more numerical details, the
 424 specific points for the Hough transform tracking are

- 425 • track building blocks are detector hits,
- 426 • tracking is only performed if at least 3 horizontal and 3 vertical detector
 427 planes (SciFi) or stations (DS) have hits,
- 428 • events with multiple 2D track projection candidates are treated as follows: if
 429 predicted slopes are contained in a range comparable to the detector angular
 430 resolution, the track with the slope closest to the sample's median is chosen.
 431 Otherwise, the event is dropped.
- 432 • at least 3 horizontal and 3 vertical tracking planes have hit detector elements
 433 that are crossed by the predicted track. It is checked that the line passes
 434 through fired detector elements within a tolerance level. The tolerance is
 435 0.1 cm for SciFi and 1 cm for DS tracking case. The SciFi tolerance value
 436 is equivalent to the distance between 4 SciFi SiPM channels. For the DS
 437 tracking, the tolerance level is equal to the DS bar transverse size.
- 438 • in low-hit-occupancy events, namely when detector planes have less than 4 hits
 439 each, the tolerance levels are increased to 0.5 cm for SciFi and 3 cm for DS.
 440 The aim is to maximize tracking efficiency while keeping the risk of building
 441 ghost tracks low.
- 442 • for SciFi tracking, when detector planes have less than 3 hits each, the user-
 443 defined precision of the Hough transform method is scaled down. It allows
 444 to find a track candidate using fewer measurements, which sometimes do not
 445 lie on a perfectly straight line due to multiple scattering. This tune is im-
 446 plemented to improve the tracking efficiency for low-energy muons, see Sec-
 447 tion 6.3.

448 6.2.3 A final remark on tracking methods

449 A notable difference between simple tracking and the Hough transform is that the
 450 first one uses detector clusters, while the second uses detector hits. Both measure-
 451 ment objects have their advantages. In SciFi for example, one SiPM channel can

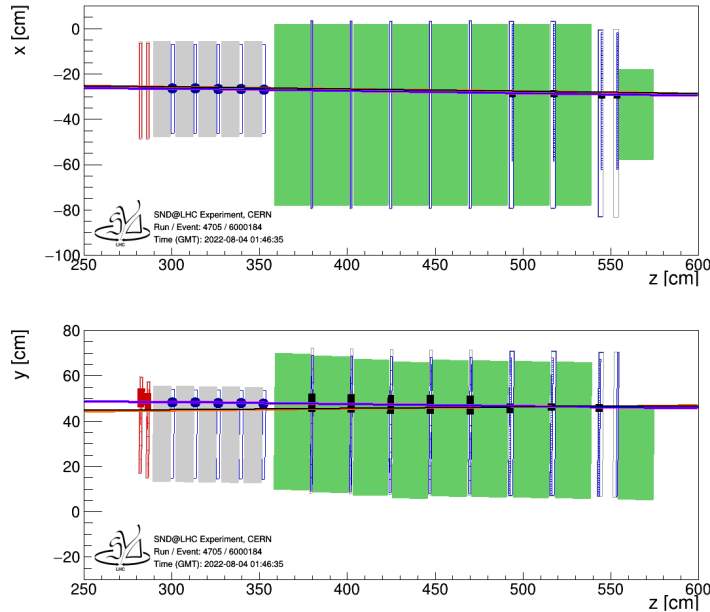


Figure 15: A SND@LHC 2D event display of a data event where SciFi and DS tracks using ST and HT are successfully built. SciFi tracks are drawn as blue and magenta lines for ST and HT, respectively. DS tracks are colored in black for ST and in orange for HT. The top panel shows the horizontal XZ plane, while the bottom one shows the vertical YZ plane. ST and HT SciFi tracks are well aligned on top of one another. Similarly, the ST and HT DS tracks are practically indistinguishable on the display. Due to the larger DS track angle resolution, the DS track extrapolation over large distances can lead to few-centimeter mismatches, e.g. between SciFi and DS tracks at same Z planes in SciFi. Detector hits in the Veto, the SciFi, and the hadronic calorimeter are shown as red bars, blue markers and black bars, respectively.

452 collect photons from multiple fibers. Hence, clustering SciFi hits seems imposed by
 453 detector construction. On the other hand, as there is substantial material budget
 454 between tracking planes, it is likely that various particles, electrons, gamma rays,
 455 etc., induce signals in neighbouring SiPM channels. Clustering would then combine
 456 all these together, compromising the origin of the measurement. Taking these two
 457 points into account, the Hough transform, which has the power to distinguish be-
 458 tween separate SiPM channels, uses detector hits. Alternatively, the performance
 459 of the simple tracking is boosted by reducing the number of track building points
 460 using clusters.

461 We close the tracking overview with an event display in Figure 15 of a clean
 462 SND@LHC event, where SciFi and DS tracks using ST and HT are successfully
 463 built.

464 6.3 MC tracking efficiency

465 The MC tracking efficiency of the ST and the HT procedures are assessed using
 466 the passing-through muons simulations described in Section 4. The MC tracking
 467 efficiency is defined as

$$\epsilon^{MC} = \frac{\text{Number of events with a reconstructed muon track}}{\text{Number of simulated events with a reconstructible muon track}}. \quad (4)$$

468 In the denominator, a reconstructible track is the track of a particle leaving at least
 469 3 MC points in horizontal and 3 MC points in vertical detector elements. The latter
 470 takes into account that three measurements per projection are required to attempt
 471 any of the two tracking methods.

472 The MC tracking efficiencies per SciFi and DS systems using the two tracking
 473 procedures are reported in Table 3. To better understand the differences in the
 474 observed values, in Figures 16-17 the MC tracking efficiency is plotted as a function
 475 of two parameters - number of detector measurements, and muon energy at its
 476 entry point into the detector. For SciFi simple tracking, the tracking efficiency is
 477 stable for events where the cluster multiplicity is not too large, i.e. below 20.
 478 Then, the efficiency falls when increasing the number of clusters per event. The
 479 reason is that events with high detector activity fail the criterion on number of
 480 clusters per plane and track fits are not attempted. The same rationale explains the
 481 efficiency's gradual decrease with increasing muon energy. For high-energy muons,
 482 particle production via bremsstrahlung, delta rays, or pair production is enhanced
 483 and cluster multiplicity per plane increases, lowering down track fit trials. To a
 484 much lesser extend the same trends are exhibited for DS simple tracking. However,
 485 the MC tracking efficiency for the DS ST is high in any bin.

486 Much like the DS simple tracking case, the DS Hough transform tracking ef-
 487 ficiency is about 98 % and stable in the whole muon energy and hit multiplicity
 488 range. On the other hand, the SciFi Hough tracking efficiency is lower for less hit-
 489 busy events compared to those having large hits counts. In terms of muon energy,
 490 there is a pronounced dip in efficiency for low-energy muons, when their energy
 491 is below 20 GeV. These two observations combined mean that about 20% of low-
 492 energy muons that penetrate through at least 3 detector planes undergo large-angle
 493 multiple scattering inside the target region. In such cases, the straight-line Hough
 494 transform prediction fails to go through sufficient number of planes to pass the
 495 tracking criteria. Inspection of such events further shows that sometimes these low-
 496 energy muons are absorbed in the tungsten plates between SciFi tracking stations.
 497 For more information on multiple scattering in the detector, refer to Section 6.1.

498 6.4 Tracking efficiency with data

499 Another way to assess the tracking efficiency is to use the independent track builds
 500 from SciFi and DS systems. The strategy is to use SciFi tracks as a tag to estimate
 501 DS tracking efficiency and vice versa. The main benefit of this approach is the
 502 large available data statistics well covering the full detector acceptance. Even so,
 503 due to the smaller size of the SciFi detector compared to the DS system and the

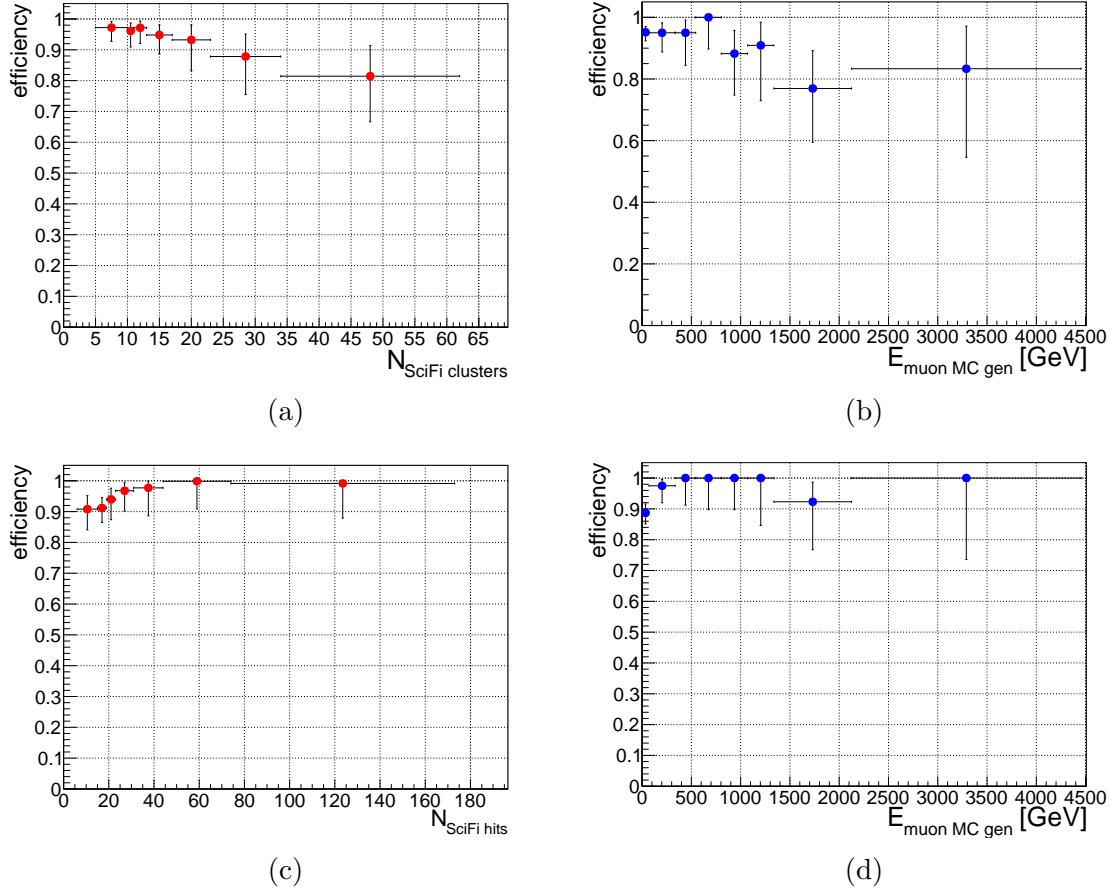


Figure 16: SciFi Monte Carlo tracking efficiency vs number of measurements (a and c) and vs generated muon energy (b and d) for tracks built using simple(top) and Hough transform(bottom) tracking procedures. The efficiency definition is given in Equation 4. The Clopper-Pearson statistics option and a 90 % confidence level are used to compute the confidence intervals.

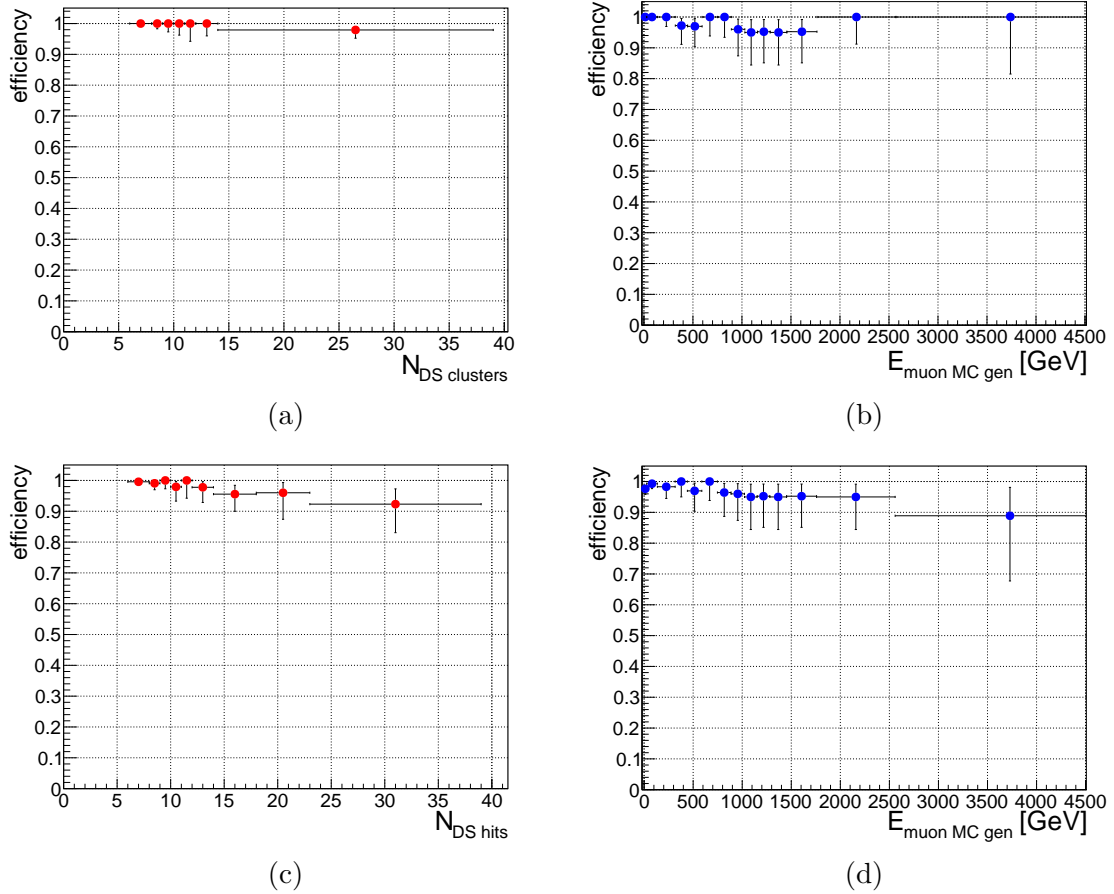


Figure 17: DS Monte Carlo tracking efficiency vs number of measurements (a and c) and vs generated muon energy (b and d) for tracks built using simple(top) and Hough transform(bottom) tracking procedures. The efficiency definition is given in Equation 4. The Clopper-Pearson statistics option and a 90 % confidence level are used to compute the confidence intervals.

system	tracking algorithm	MC tracking efficiency
SciFi	simple tracking	0.93 ± 0.03
	Hough transform	0.94 ± 0.03
DS	simple tracking	0.98 ± 0.02
	Hough transform	0.98 ± 0.02

Table 3: Monte Carlo tracking efficiency using the SciFi and DS detectors and applying simple and Hough transform tracking procedures. The efficiency definition is given in Equation 4. Statistical uncertainties are reported.

504 positions of the main muon sources with respect to the detector, only a part of the
 505 DS acceptance can be probed with this method. Nonetheless, it is assumed the
 506 obtained DS tracking efficiency can be applied to the full detector fiducial volume.
 507 Reasons for it are given in Section 6.4.2.

508 Another benefit of the data-based tracking efficiency is that the intrinsic spatial
 509 and energy distributions of muons at the detector are used. Since the energy loss and
 510 number of hits produced in the apparatus vary with muon energy, see Section 6.1, the
 511 data provides the best conditions to test the tracking methods. Additionally, using
 512 data to define tracking efficiency means there is no need to rely on external detector
 513 area description, as is the case for simulations. Materials and their positions along
 514 the particle’s path, with the exception that the detector has to be spatially aligned,
 515 are identical for all data measurements. Lastly, any particle registration inefficiency,
 516 due to dead zones inside tracking planes or detector readout inefficiency (dead time,
 517 saturation, or else) are by construction included in the data-based tracking efficiency.

518 6.4.1 SciFi tracking efficiency using data

519 The data SciFi tracking efficiency procedure is

- 520 • For each event, take a good DS track
 - 521 – converged fit, slopes in both projections below 80 mrad, $\chi^2/ndf < 5$.
- 522 • Check if the extrapolated DS track at the Veto planes is within 3 cm of a fired
 523 Veto bar. The tolerance value used here should not be too large, otherwise DS
 524 tracks outside of the Veto acceptance, and so of the SciFi one, will be selected.
- 525 • Extrapolate the DS track to a reference plane at $z = 490$ cm and fill a
 526 2D XY histogram with DS track intersection coordinates. The reference plane
 527 is located at the position of the first DS station. It is done to minimize ex-
 528 trapolation of DS tracks since they have worse angular resolution compared
 529 to SciFi tracks.
- 530 • take a good SciFi track in the same event,
 - 531 – converged fit, $\chi^2/ndf < 20$.
- 532 • Extrapolate the SciFi track to the same reference plane,

- 533 • If SciFi track's and DS track's projections on the reference plane are within
534 3 cm distance, fill a 2D XY histogram with DS track intersection,
- 535 • The ratio of the two histograms is an estimate of the SciFi tracking efficiency
536 using data.

537 The choice of selection parameters is motivated in Figures 18 and 19, where
538 data and Monte Carlo simulation distributions of χ^2/ndf and the distances between
539 extrapolated tracks and detector elements are shown. The selection cut for DS
540 tracks at Veto planes is determined by the half size of the Veto bar, since it is the
541 bar center that is used in the calculation.

542 The 2D XY histogram of the SciFi tracking efficiency using data is presented
543 in Figure 20 for simple tracking and in Figure 21 for Hough transform tracks. Only
544 the central region of the detector, where the efficiency is relatively uniform in $x - y$
545 space, is used to obtain the data tracking efficiency. The selected fiducial volume
546 is $-42 \text{ cm} \leq x \leq -11 \text{ cm}$ and $18 \text{ cm} \leq y \leq 49 \text{ cm}$. It corresponds to a $31 \times 31 \text{ cm}^2$
547 detector area. The mean of all efficiency values in $x - y$ bins, their distributions pre-
548 sented in Figures 20b and 21b, is assigned as the final data tracking efficiency. The
549 mean and standard deviation for both SciFi tracking alternatives are summarized
550 in Table 4.

551 6.4.2 DS tracking efficiency using data

552 The outline of the data DS tracking efficiency method is

- 553 • For each event, take a good SciFi track
 - 554 – converged fit, slopes in both projections below 80 mrad, $\chi^2/ndf < 20$.
- 555 • Check if the extrapolated SciFi track at US 5 plane is within 3 cm of a fired
556 US 5 bar,
- 557 • Check if the extrapolated SciFi track at DS 3 plane is inside its geometrical
558 acceptance within a 3-cm tolerance,
- 559 • Extrapolate SciFi track to a reference plane at $z = 490 \text{ cm}$ and fill a 2D XY his-
560 togram with SciFi track intersection coordinates. The reference plane is lo-
561 cated at the position of the first DS station.
- 562 • Take a DS track in the same event
 - 563 – converged fit, $\chi^2/ndf < 5$.
- 564 • Extrapolate it to the same reference plane,
- 565 • If DS track's and SciFi track's projections on the reference plane are within
566 3 cm distance, fill a 2D XY histogram with SciFi track intersection,
- 567 • The ratio of the two histograms is an estimate of the DS tracking efficiency
568 using data.

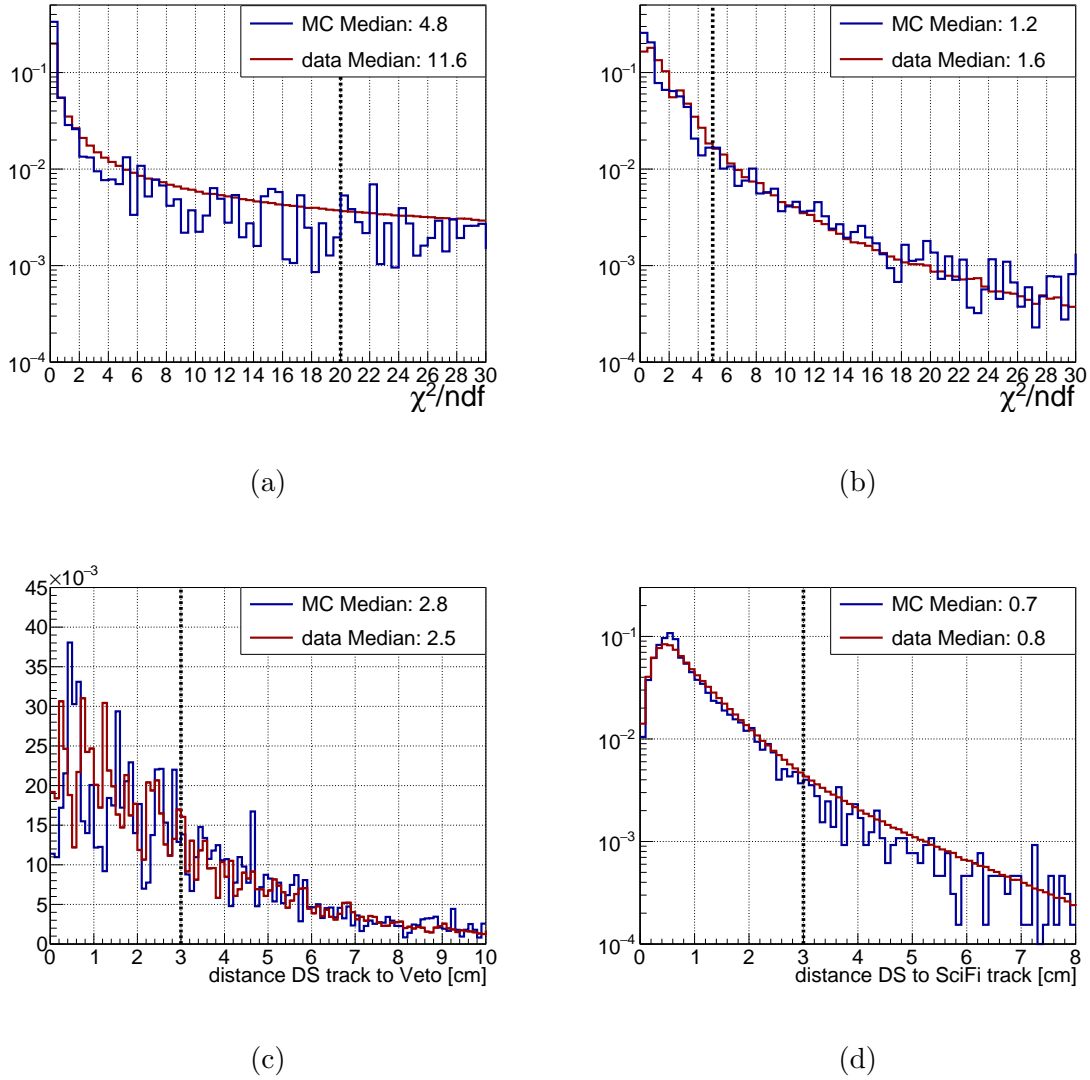


Figure 18: χ^2/ndf for SciFi (a) and DS (b) tracks built using the simple tracking, distance between ST DS track and a fired Veto bar (c), and distance between a ST SciFi track and a ST DS track extrapolated position to a reference plane at $z = 490$ cm (d). The cut values used in the SciFi tracking data-based efficiency estimation are noted with a dotted black line. They correspond to 2-3 times the median, i.e., 0.5 quantile, of the data distributions.

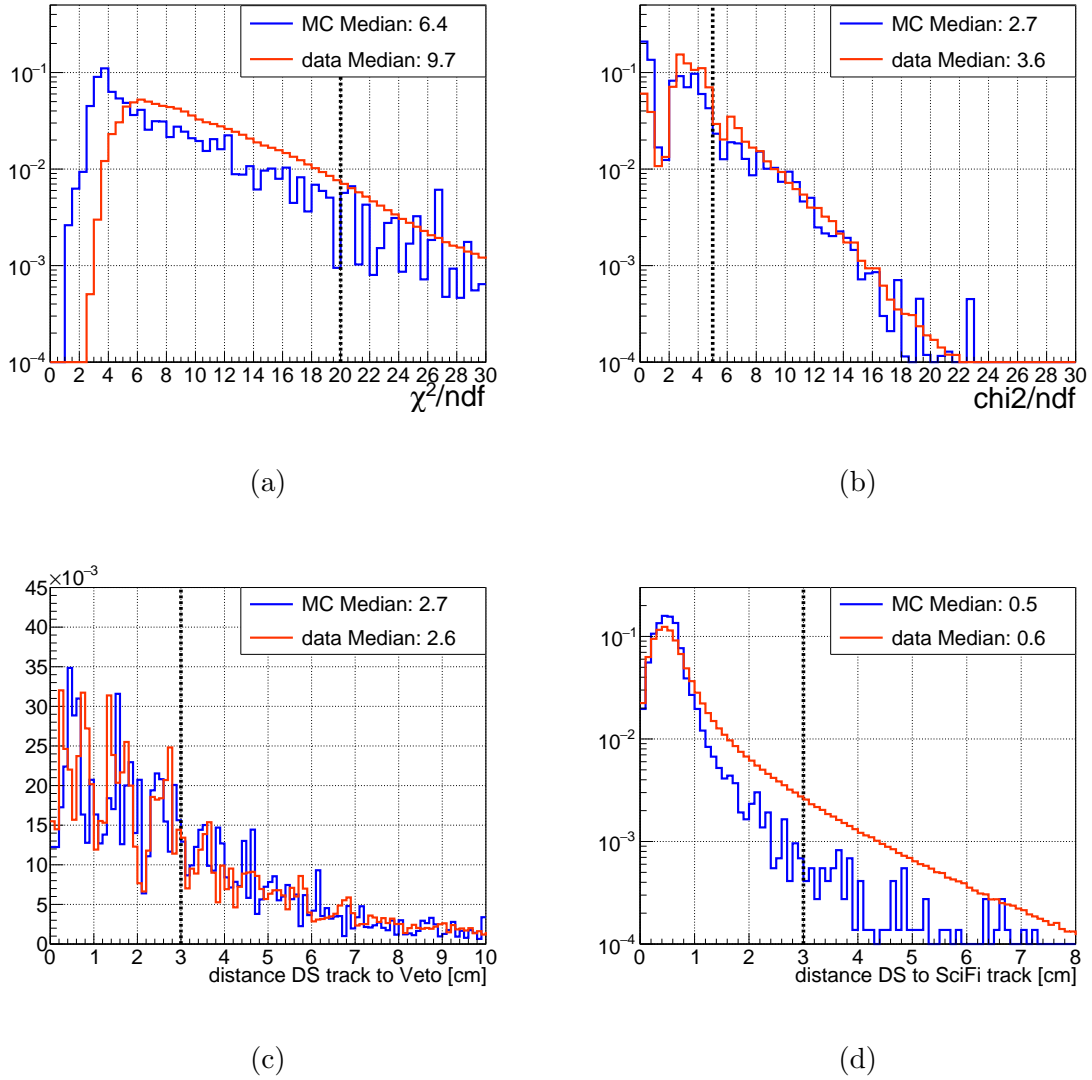


Figure 19: χ^2/ndf for SciFi (a) and DS (b) tracks build using the Hough transform, distance between HT DS track and a fired Veto bar (c), and distance between a HT SciFi track and a HT DS track extrapolated position to a reference plane at $z = 490$ cm (d). The cut values used in the SciFi tracking data-based efficiency estimation are noted with a dotted black line. They correspond to 2-3 times the median, i.e., 0.5 quantile, of the data distributions.

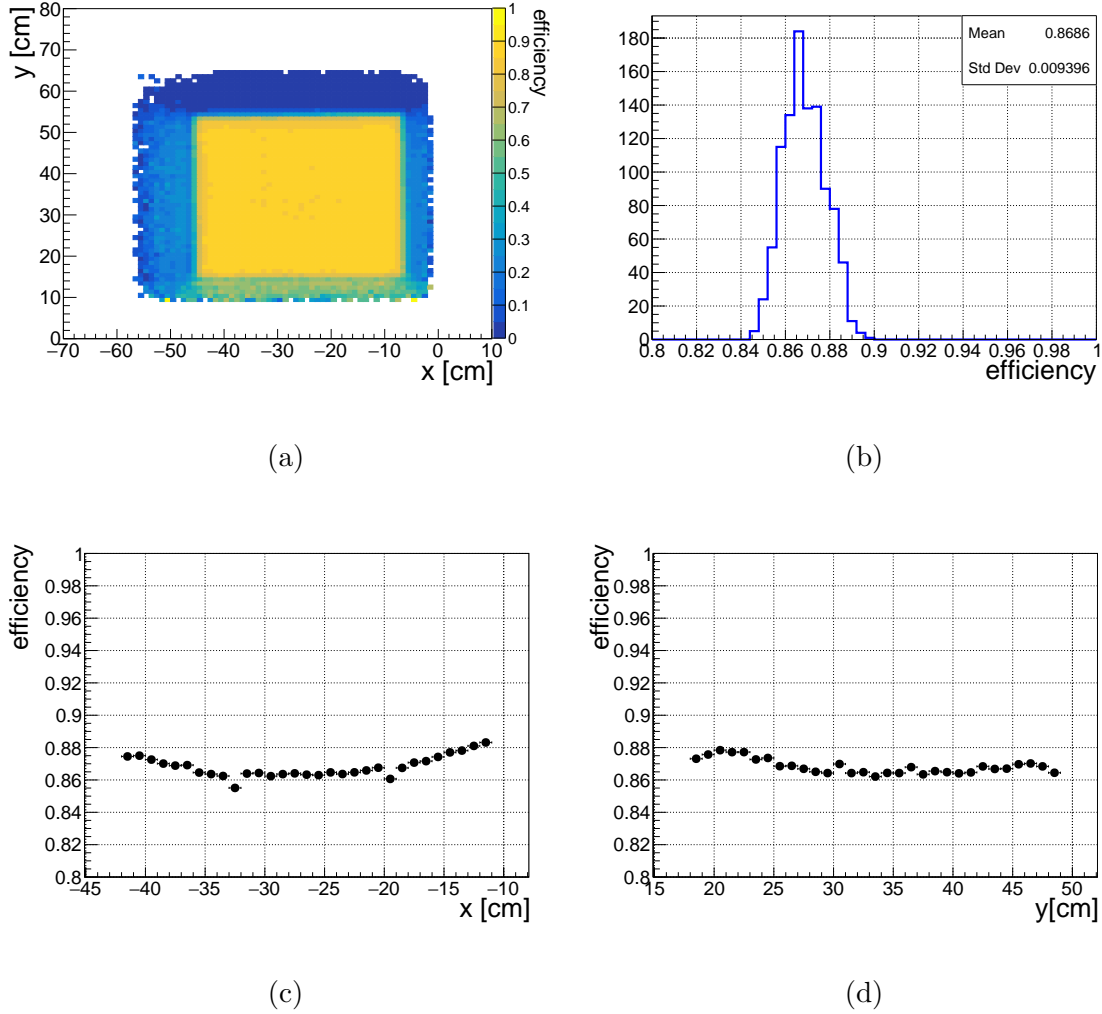


Figure 20: SciFi simple tracking efficiency obtained using the data. ST DS tracks are used as tags. The efficiency in $x - y$ bins (a) is used to determine a central region of relatively uniform efficiency. The fiducial volume selected is $-42 \text{ cm} \leq x \leq -11 \text{ cm}$ and $18 \text{ cm} \leq y \leq 49 \text{ cm}$. In that range the efficiency vs x (c) and y (d) position fluctuates by a few percent. The Clopper-Pearson statistics option and a 90 % confidence level are used to compute the confidence intervals for the efficiency in x (c) and y (d) bins. The final efficiency value is the mean over $x - y$ bins in the selected fiducial volume, shown on plot (b).

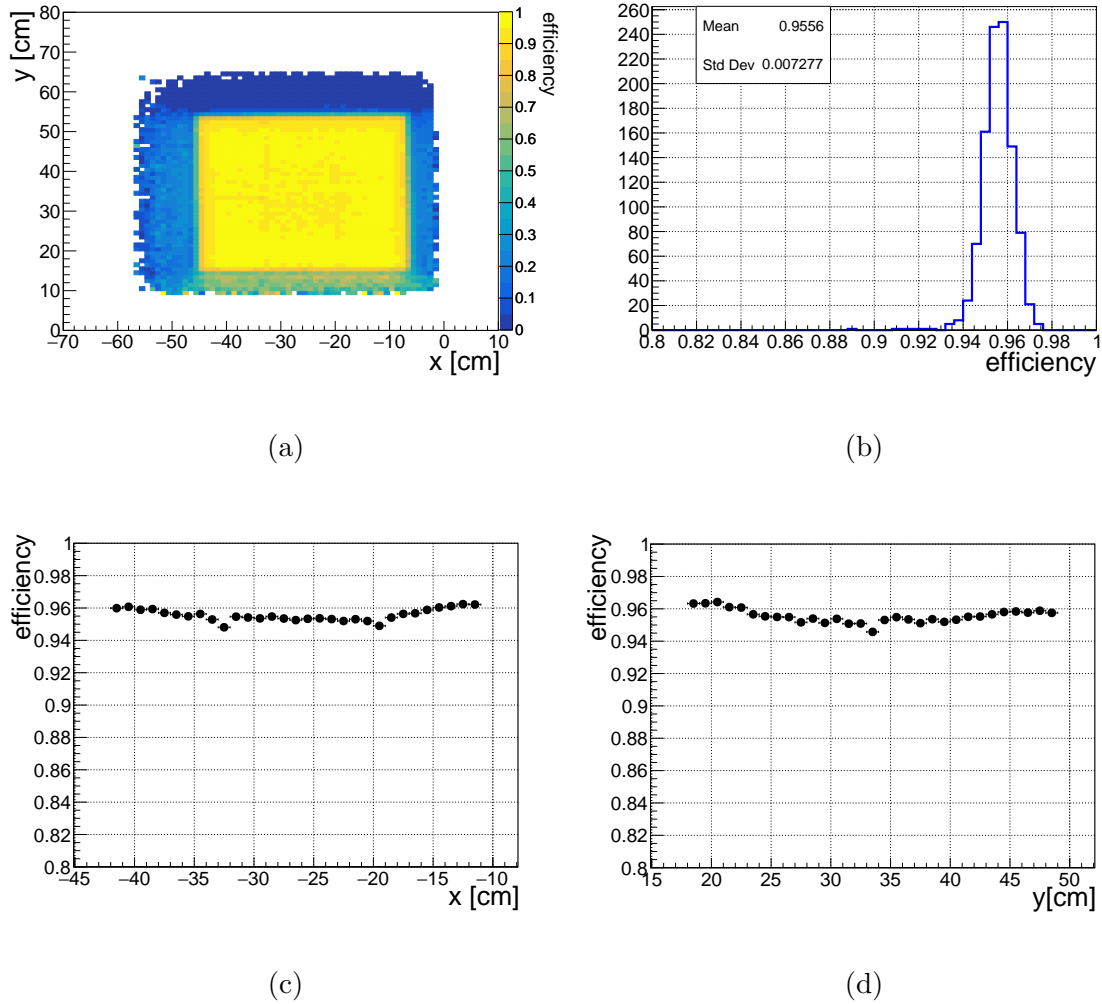


Figure 21: SciFi Hough transform tracking efficiency obtained using the data. HT DS tracks are used as tags. The efficiency in $x - y$ bins (a) is used to determine a central region of relatively uniform efficiency. The selected fiducial volume is $-42 \text{ cm} \leq x \leq -11 \text{ cm}$ and $18 \text{ cm} \leq y \leq 49 \text{ cm}$. In that range, the efficiency vs x (c) and y (d) position fluctuates by a few percent. The Clopper-Pearson statistics option and a 90 % confidence level are used to compute the confidence intervals for the efficiency in x (c) and y (d) bins. The final efficiency value is the mean over $x - y$ bins in the selected fiducial volume, shown on plot (b).

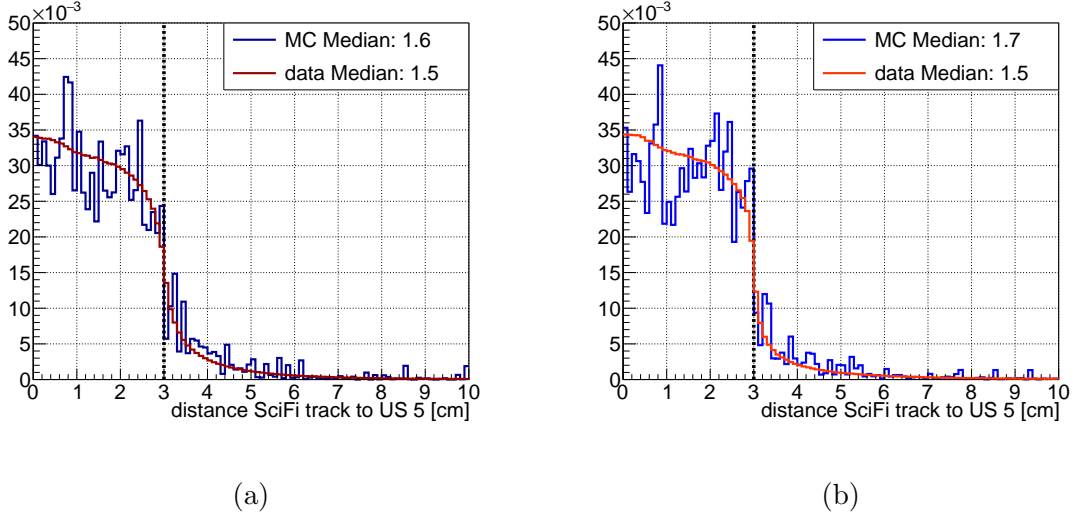


Figure 22: The distance between a ST SciFi track and a fired US 5 bar (a), and distance between a HT SciFi track and a fired US 5 bar (b). The cut value at 3 cm that is used in the DS tracking data-based efficiency estimation is noted with a dotted black line.

569 The selection cut for SciFi tracks at US 5 planes is determined by the half size
 570 of a US bar, since it is the bar center that is used in the respective calculation.
 571 The data and Monte Carlo simulation distributions of the distance between a SciFi
 572 extrapolated track and fired US 5 bars are shown in Figure 22 for the simple and
 573 the Hough transform tracking cases.

574 The 2D XY histogram of data DS tracking efficiency is presented in Figure 23 for
 575 simple tracking and in Figure 24 for Hough transform tracks. Due to the difference
 576 in the SciFi and the DS dimensions, the DS acceptance is partially covered by ex-
 577 trapolated SciFi tracks. Consequently, the DS detector region of uniform efficiency,
 578 which is used to obtain the data tracking efficiency, is identical to the one reported
 579 in Section 6.4.1 for the SciFi tracking efficiency. Again, the selected fiducial volume
 580 is $-42 \text{ cm} \leq x \leq -11 \text{ cm}$ and $18 \text{ cm} \leq y \leq 49 \text{ cm}$. The mean of all efficiency values
 581 in $x - y$ bins, the latter presented in Figures 23b and 24b, is assigned as the final
 582 data DS tracking efficiency. The mean and standard deviation of the efficiency for
 583 all detectors and tracking methods are summarized in Table 4. They will be used
 584 to asses the systematic uncertainty of the muon flux in the detector.

585 The DS tracking efficiency in the selected spatial region fluctuates by a few
 586 percent with vertical position change, see Figures 23d and 24d. Looking at DS hit
 587 distributions per station and bar, it is confirmed the observed fluctuations originate
 588 from bar inefficiencies. There are 3 horizontal DS stations and all of them must
 589 have at least one hit to attempt a track fit. As there is no plane redundancy for the
 590 DS track fits in the vertical projection, the tracking efficiency is slightly lower in the
 591 areas of those inefficient bars. Since the observed non-uniform behaviour of the DS
 592 tracking efficiency obtained using the data is understood, it is considered that the
 593 efficiency estimate can be safely applied to the full acceptance of the DS system.

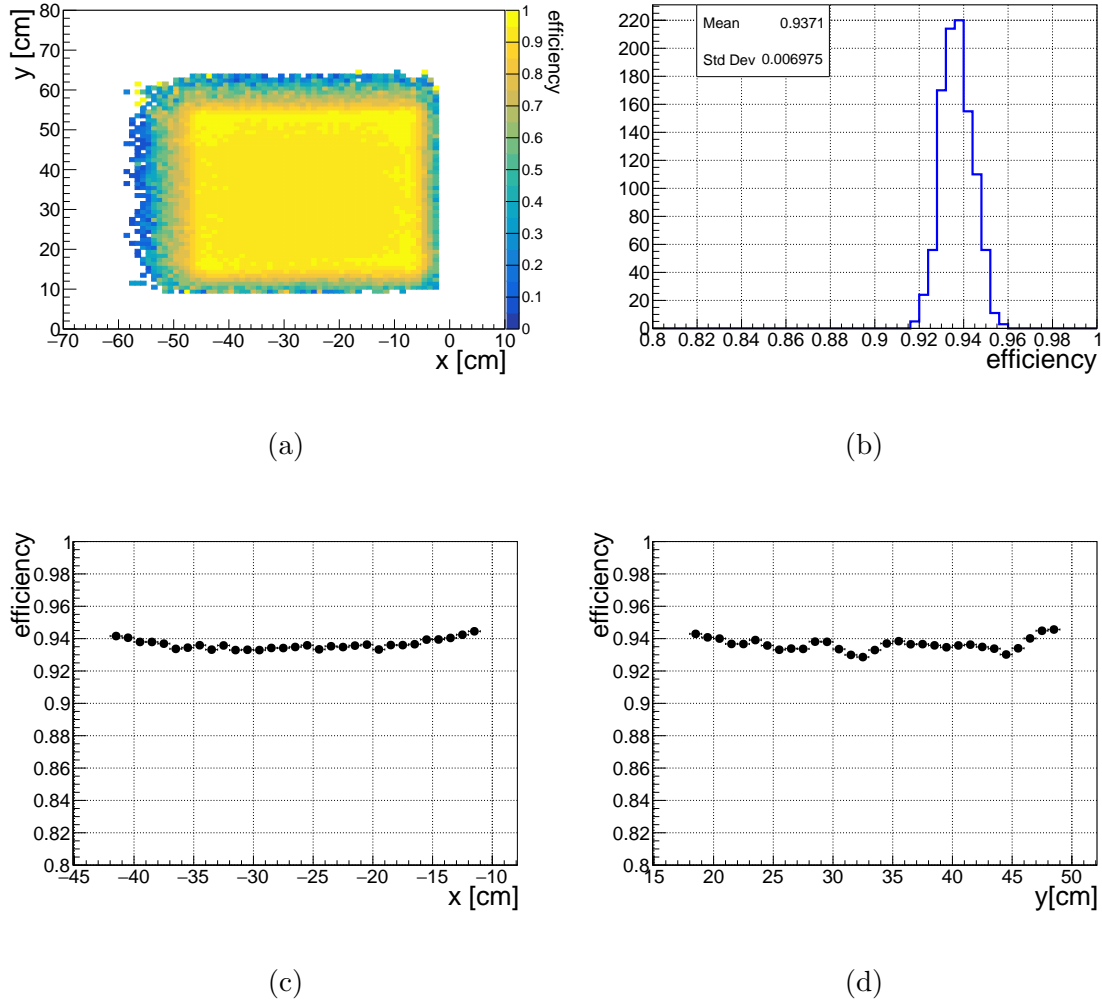


Figure 23: DS simple tracking efficiency obtained using the data. ST SciFi tracks are used as tags. The efficiency in $x - y$ bins (a) is used to determine a central region of relatively uniform efficiency. The fiducial volume selected is $-42 \text{ cm} \leq x \leq -11 \text{ cm}$ and $18 \text{ cm} \leq y \leq 49 \text{ cm}$. In that range, the efficiency vs x (c) and y (d) position fluctuates by a few percent. The Clopper-Pearson statistics option and a 90 % confidence level are used to compute the confidence intervals for the efficiency in x (c) and y (d) bins. The final efficiency value is the mean over $x - y$ bins in the selected fiducial volume, shown in plot (b).

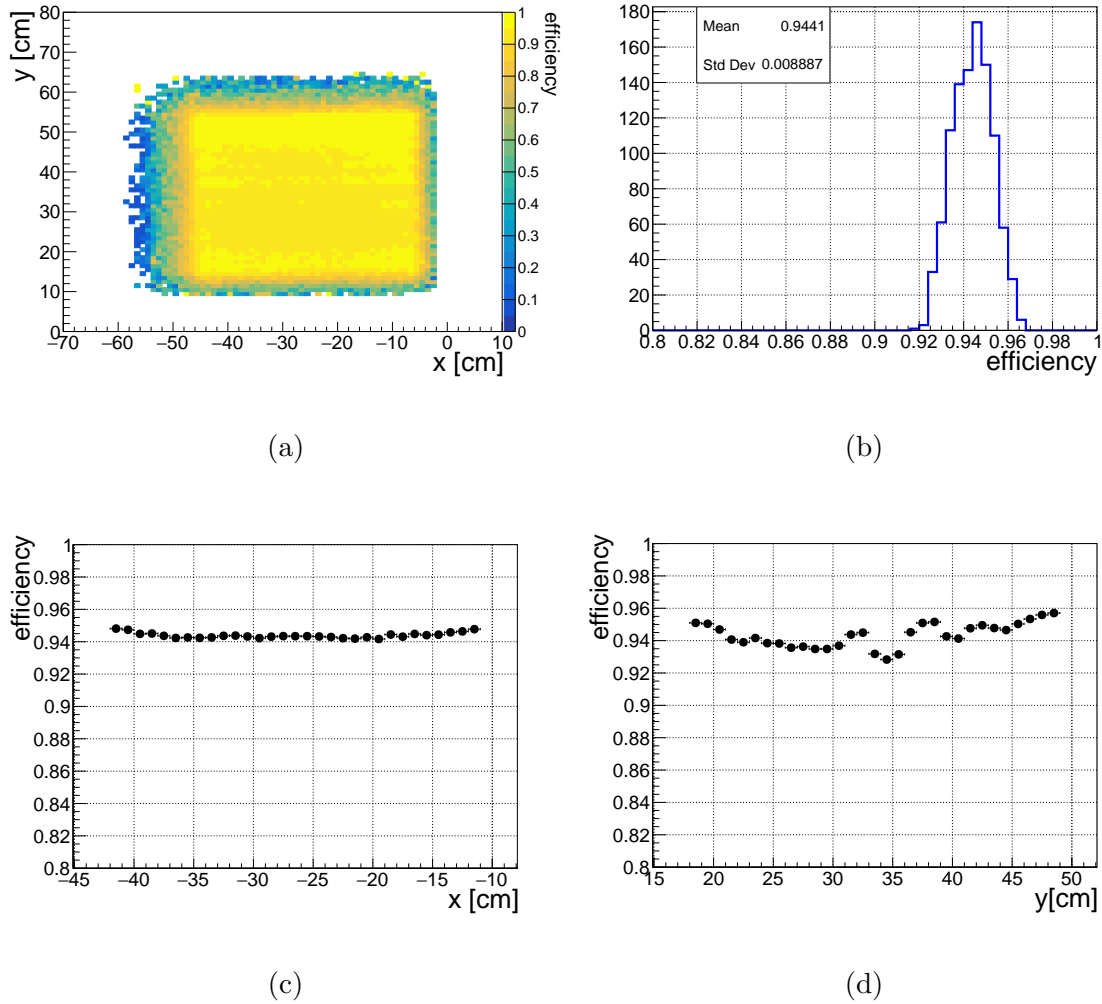


Figure 24: DS Hough transform tracking efficiency obtained using the data. HT SciFi tracks are used as tags. The efficiency in $x - y$ bins (a) is used to determine a central region of relatively uniform efficiency. The selected fiducial volume is $-42 \text{ cm} \leq x \leq -11 \text{ cm}$ and $18 \text{ cm} \leq y \leq 49 \text{ cm}$. In that range, the efficiency vs x (c) and y (d) position fluctuates by a few percent. The Clopper-Pearson statistics option and a 90 % confidence level are used to compute the confidence intervals for the efficiency in x (c) and y (d) bins. The final efficiency value is the mean over $x - y$ bins in the selected fiducial volume, shown in plot (b).

system	tracking algorithm	Data tracking efficiency
SciFi	simple tracking	0.868 ± 0.009
	Hough transform	0.956 ± 0.007
DS	simple tracking	0.937 ± 0.007
	Hough transform	0.944 ± 0.009

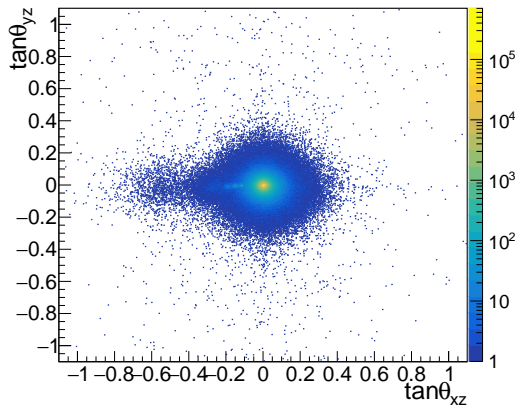
Table 4: Tracking efficiency using the data. Reported results are for SciFi and DS detectors, applying simple and Hough transform tracking procedures. The quoted values are mean and standard deviation over binned efficiencies in $x - y$ coordinates.

594 7 Angular distribution

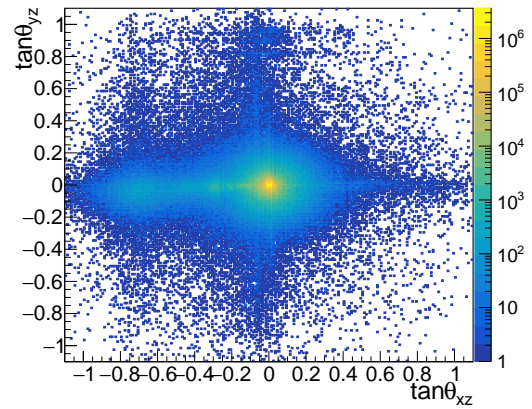
595 Due to the position of the SND@LHC detector 480 m away from IP1 and at a
 596 small off-axis angle, one expects that surviving long-range muons leave traces in
 597 the detector that are at small angles with respect to the SND@LHC's Z axis. This
 598 is exactly the case shown in Figure 25. The central peak corresponds to a distant
 599 source at IP1. This peak has large tails due to multiple scattering along the 480-m
 600 path from IP1 to the TI-18 tunnel.

601 In the logarithmic scale of track slopes in the $x - z$ plane, see Figures 25c and 25d,
 602 a few structures at negative slopes become visible. The origin of particles passing
 603 through the detector at such angles is beam-gas interactions in the beamline. As
 604 shown in Figure 26, after selecting events in sync with LHC bunches corresponding
 605 to non-colliding Beam 2 - no Beam 1 (B2noB1), the vast majority of reconstructed
 606 tracks have negative XZ slopes. Moreover, track direction studies based on detector
 607 hit timing show that tracks in Beam 2 events enter the detector from the back, see
 608 Figure 27. Then, the origin of these particles is downstream of the DS stations.
 609 The reconstructed angles point to elements in the LHC half-cells 12-17, with angles
 610 approaching 0 for more distant sources. For reference, a schematic view of the rel-
 611 evant part of the LHC complex, taken from the CERN GIS portal [24] is given on
 612 Figure 28.

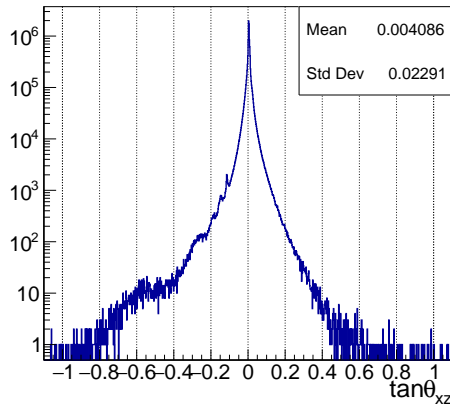
613 A closer look at the central region of the main peak in Figure 29 shows two
 614 slightly shifted sub-peaks. The angular distance in the $x - z$ plane between these
 615 sub-maxima is about 5 mrad. An identical two-peak structure is observed in the
 616 emulsion data too. As reported in Reference [8], the difference in slope between the
 617 two peaks in the emulsion data is also 5 mrad and matches the electronic detectors
 618 measurement. Similarly to the main-peak case, muons contributing to the smaller
 619 central sub-peak originate from interactions and particle (pion and kaon) decays
 620 at various locations. Among the more interesting cases, a contribution comes from
 621 interactions in the area where the clock-wise circulating LHC proton beam starts to
 622 be bent in the LHC circular orbit. That is approximately the quadrupole magnet
 623 of half-cell 9 and is 345 m away from IP1. For clarity, this is shown on the map in
 624 Figure 30. Another case are interactions in the area where the nominal IP1 collision
 625 axis intersects the ground outside the curved LHC tunnel in the direction of the
 626 TI-18 tunnel. This information is deduced thanks to FLUKA simulations, whose
 627 output purposefully provides the production history of muons reaching the scoring



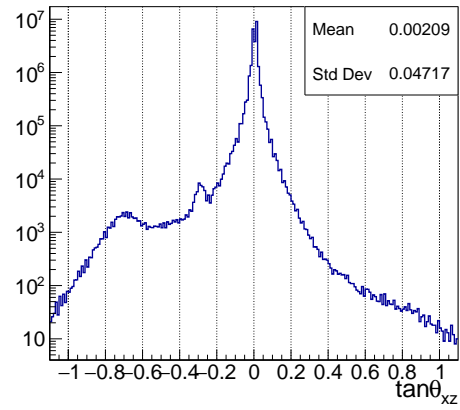
(a)



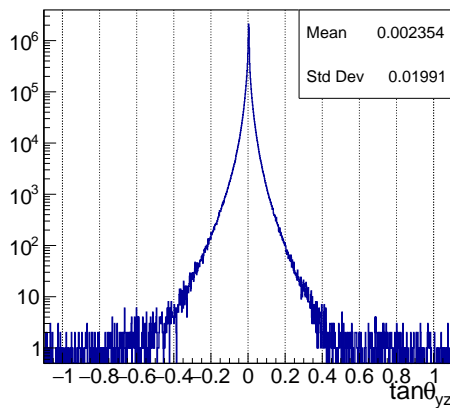
(b)



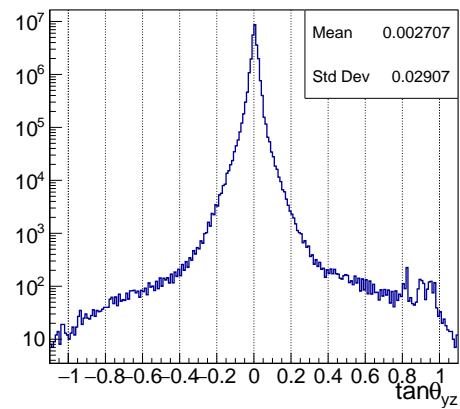
(c)



(d)



(e)



(f)

Figure 25: SciFi (a, c, e) and DS (b, d, f) track slopes in data. Tracks are built using the Hough transform method.

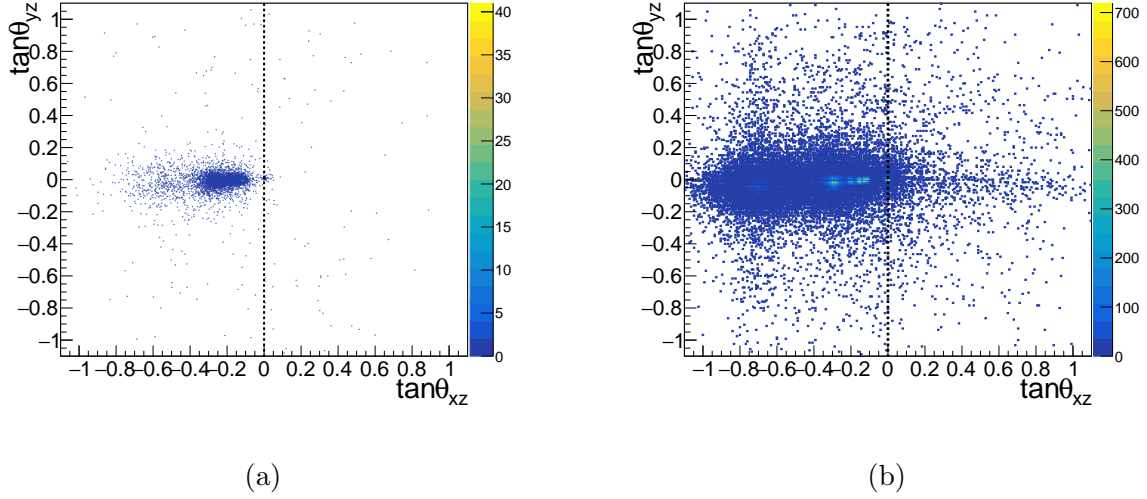


Figure 26: SciFi (a) and DS (b) track slopes for data events in sync with B2noB1 LHC bunches. Tracks are built using the Hough transform.

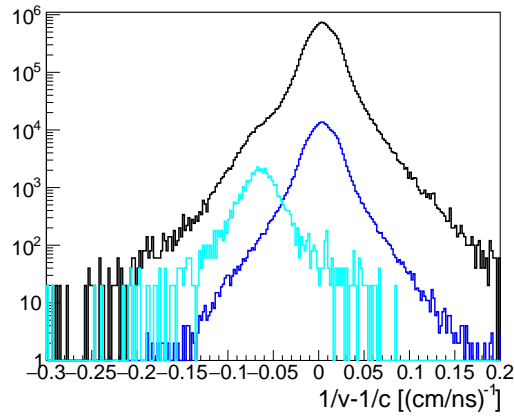


Figure 27: Track separation by particle propagation direction using simple tracking SciFi tracks. The black curve shows tracks reconstructed in all events. The blue distribution is for tracks in events of B1noB2 bunches and the cyan one - for events in B2noB1 bunches. Tracks of particles moving from the DS side towards the SciFi, dubbed backward-going, must have $1/v - 1/c$ values around $-2/c$ or $-0.067 \text{ (cm/ns)}^{-1}$.

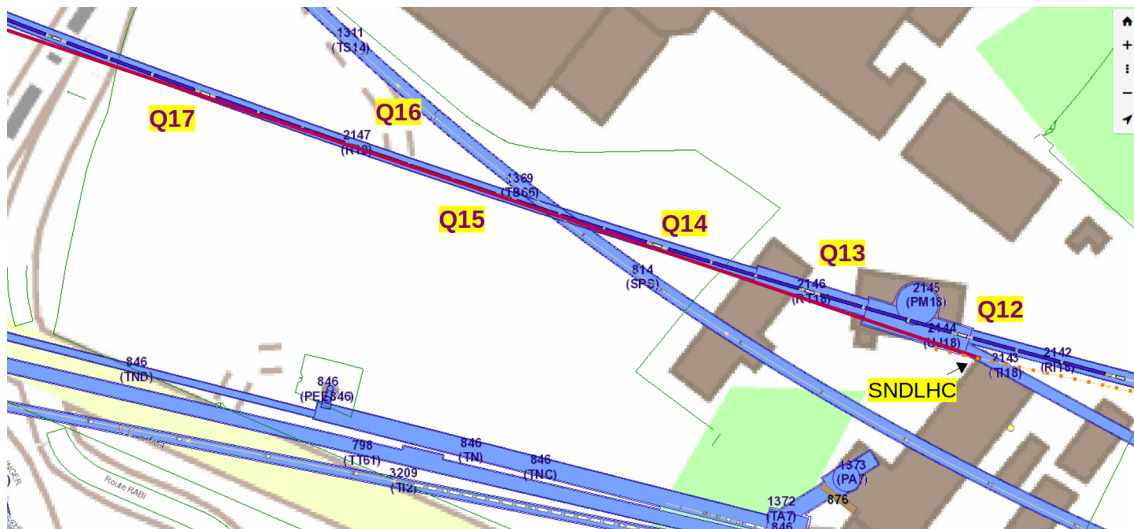


Figure 28: Map of the LHC area around the SND@LHC location. The abbreviations of the quadrupole magnets downstream of the detector are highlighted in yellow. The quadrupoles numbers correspond to the LHC half-cells of the same number. The original image is from the CERN GIS portal [24].

628 plane.

629 8 Muon flux

630 The flux of reconstructed muon tracks in the detector is estimated for two selected
 631 LHC fills, as discussed in Section 3. The muon flux is determined as the number
 632 of reconstructed tracks in a given SND@LHC run per corresponding IP1 integrated
 633 luminosity and unit detector area. Selected events are during "Stable beams" operation
 634 of the LHC and IP1 colliding bunches. IP1 collisions might coincide in time
 635 with other activity in the accelerator. The LHC bunch structure with respect to
 636 the SND@LHC detector is shown in Figure 31 for the two selected runs. Most
 637 bunch protons survive the IP beam crossings. At the SND@LHC location, IP1 collisions
 638 and the circulation of the remaining protons of the same IP1 colliding Beam 1
 639 bunch are always synchronous. Independent of the presence of a bunch crossing and
 640 while moving towards the SND@LHC detector, if Beam 1 interacts in the beamline
 641 outside the IP1 collision area, the outgoing produced particles might leave a recon-
 642 structible trace in the apparatus. Further, IP1 colliding bunches sometimes coincide
 643 with other non-colliding bunches of Beam 2 circulating in the ring. In this cases,
 644 Beam 2 can interact with the beamline elements, producing particles that impinge
 645 on the detector. Lastly, IP1 colliding bunches are often in sync with the crossing
 646 of a different bunch pair at IP2. Figure 31a shows little difference in event rates
 647 between circulation of non-colliding Beam 2 bunches and IP2 collisions. Therefore,
 648 the particle contribution from IP2 collisions in the detector is considered negligible.

649 The number of muons associated with non-IP1 sources is determined in two cases:
 650 non-colliding Beam 1 bunches and Beam 2 no Beam 1 LHC bunches, noted B2noB1

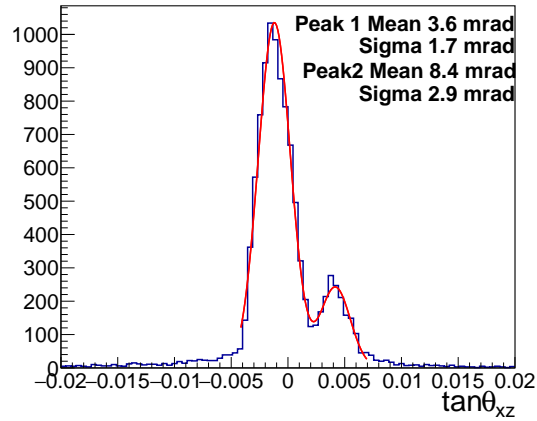


Figure 29: Data SciFi track slopes in the horizontal plane. The region around a few milliradian is selected to show the two central sub-peaks of the main peak. A double Gaussian is used to fit the peaks. The mean and sigma values of the global fit are reported.



Figure 30: Map of the LHC area where Beam 1, the clock-wise circulating beam moving from right to left in this figure, is bent in the LHC arc at half-cell 9. The light yellow line shows the ATLAS detector axis. Abbreviations denote the quadrupole magnets of the corresponding half-cells. The marked distances are with respect to IP1. The latter lies further on the left, outside of the map. The original image is from the CERN GIS portal [24].

651 for shortness. The latter accounts for particles entering the detector, but produced
 652 in Beam 2 interactions with the residual gas and the LHC machine elements. Once
 653 the number of muons per bunch in non-IP1 bunches is obtained, the contributions
 654 of Beam 1 and Beam 2 on the SND@LHC muon rate is subtracted from the number
 655 of reconstructed muons in IP1 colliding bunches. The following formula is used

$$N_{\mu IP1Only} = N_{\mu IP1} - \frac{N_{\mu B1Only}}{N_{B1Only}} \times N_{IP1\&B1} - \frac{N_{\mu B2noB1}}{N_{B2noB1}} \times N_{IP1\&B2}, \quad (5)$$

656 where N_{μ} is the number of reconstructed muon tracks and N is the number of
 657 bunches having the designated structure. Equation 5 implies an equal number of
 658 protons, equal beam current and dimensions per bunch.

659 The signal and background levels for the muon flux measurement are reported
 660 in Table 5 for the two selected fills. The filling scheme for fill 8297 is known to
 661 reduce beam-gas interactions, see Section 3. In terms of muons at the SND@LHC
 662 detector location, the observed reduction in the background levels associated with
 663 non-colliding Beam 1 and B2noB1 bunches is between 25 to 50 % depending on the
 detector system and the bunch type.

system	IP1 all [%]	IP1 collisions [%]	B1Only [%]	B2noB1 [%]
run 4705, LHC fill 8088				
SciFi	100	98.6	1.2	0.2
DS	100	98.5	1.1	0.4
run 5086, LHC fill 8297				
SciFi	100	99.2	0.7	0.1
DS	100	99.1	0.6	0.3

Table 5: Fractions of events associated with IP1 collisions, non-colliding Beam 1 and B2noB1 bunches for the two selected LHC fills. The filling scheme in fill 8297 suppresses the formation of electron cloud and reduces beam-gas interactions [7].

664
 665 After corrections for Beam 1 and Beam 2 contributions, the data-based tracking
 666 efficiency correction, reported in Table 4, is applied. The correction is defined as
 667 the inverse of the efficiency. This is done for both selected runs, for SciFi and DS
 668 tracks built using both SND@LHC tracking approaches. The corresponding muon
 669 flux values are reported in Table 6. As expected, the DS muon flux is larger than
 670 the SciFi one, given the non-uniform flux in the vertical direction and the difference
 671 in the system's geometrical acceptance. Then, there are a few percent variations in
 672 the results per detector when comparing estimates for different tracking methods.
 673 Using simulations, it is demonstrated in Figures 16-17 that as a consequence of the
 674 presence of heavy material between tracking stations, the tracking performance of
 675 the two algorithms is not identical in different energy spectrum intervals. Since the
 676 muon flux results for the two tracking algorithms vary more than multiple times
 677 the statistical uncertainty, the dependence of the tracking performance on the muon
 678 energy is considered a muon flux systematic uncertainty source.

679 The central value of the final muon flux result per detector is the average of
 680 the calculated fluxes for the two SND@LHC runs when using the Hough transform

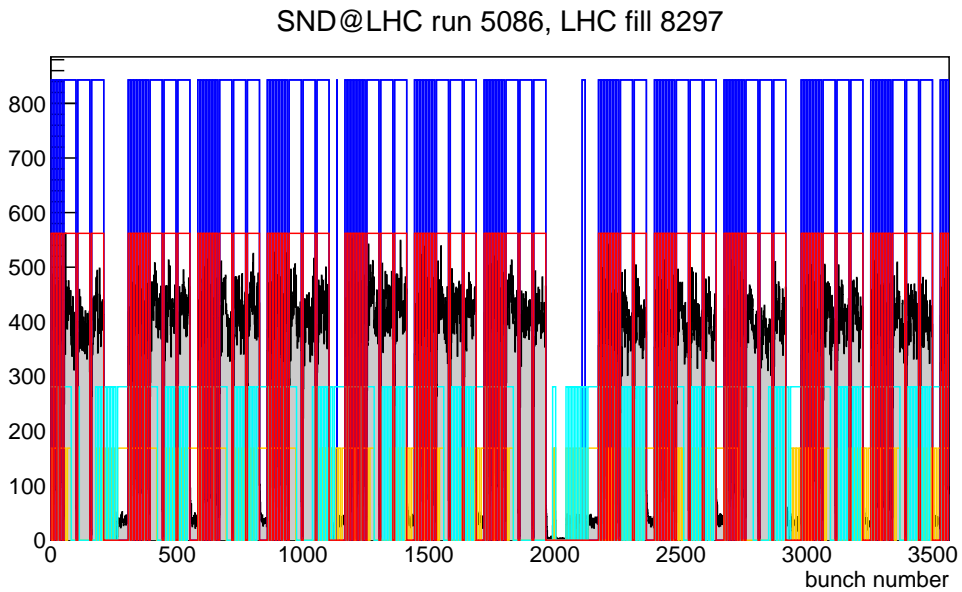
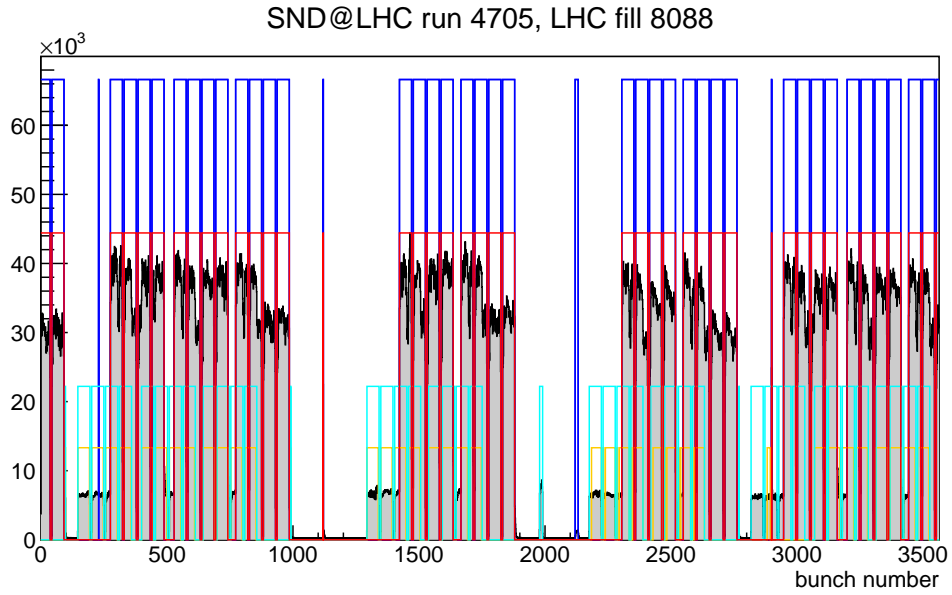


Figure 31: Bunch structure for LHC fill 8088, SND@LHC run 4705 (a) and LHC fill 8297, SND@LHC run 5086 (b). The black distribution on each plot is the SND@LHC event rate. The red boxes show bunches associated with Beam 1, the cyan ones - with Beam 2, the blue ones - IP1(ATLAS) collisions, the dark yellow ones - IP2(ALICE) collisions. The difference between the phase adjustments with respect to the SND@LHC clock of Beam 1 and of Beam 2 is 129 bunch numbers and corresponds to twice the distance from the detector to IP1.

681 tracking. The reason HT is selected is to maximize the tracking efficiency, thus min-
 682 imize the correction. The integrated luminosity for a LHC fill is used to normalize
 683 the muon flux and the uncertainty of the former is propagated to the flux result.
 684 The ATLAS collaboration reports a 2.2% uncertainty in the integrated luminosity
 685 for data recorded in 2022 [25]. Additionally, since the tracking efficiency directly
 686 enters the muon flux estimate as a correction factor, a systematic uncertainty is
 687 attributed to its assessment. The uncertainty of the efficiency evaluation is taken
 688 as triple the standard deviation of tracking efficiency values over $1 \times 1 \text{ cm}^2$ $x - y$
 689 detector coordinate bins, see Table 4. For each systematic uncertainty source, sep-
 690 arate flux estimates are calculated using one varied parameter at a time: tracking
 691 efficiency value, integrated luminosity or using the simple tracking. The deviations
 692 of those flux estimates from the central one are added in quadrature to form the
 693 total systematic uncertainty.

694 The muon flux is estimated in the selected SciFi inner fiducial volume between
 695 $-42 \text{ cm} \leq x \leq -11 \text{ cm}$ and $18 \text{ cm} \leq y \leq 49 \text{ cm}$. It defines a $31 \times 31 \text{ cm}^2$ central de-
 696 tector area, rejecting regions of non-uniform detector efficiency, see Section 6.4.1.
 697 For the DS, the selected area is $52 \times 52 \text{ cm}^2$, ranging between $-54 \text{ cm} \leq x \leq -2 \text{ cm}$
 698 and $12 \text{ cm} \leq y \leq 64 \text{ cm}$. The SciFi and the DS muon flux estimates in the so-defined
 699 areas with statistical and systematic uncertainties are reported in Table 7. The total
 700 relative uncertainty of the flux results is 5 % for the SciFi measurement and 3 % for
 the DS one.

system	tracking algorithm	muon flux [10^4 fb/cm^2]
run 4705, LHC fill 8088		
SciFi	simple tracking	2.20 ± 0.01
	Hough transform	2.05 ± 0.01
DS	simple tracking	2.43 ± 0.01
	Hough transform	2.38 ± 0.01
run 5086, LHC fill 8297		
SciFi	simple tracking	2.20 ± 0.01
	Hough transform	2.06 ± 0.01
DS	simple tracking	2.41 ± 0.01
	Hough transform	2.34 ± 0.01

Table 6: Muon flux in two selected SND@LHC runs and LHC fills. Estimates with SciFi and DS data tracks built using simple tracking and the Hough transform are reported separately. The statistical uncertainty for each case is quoted. The considered detector fiducial volumes are defined in the text.

701

702 The SciFi and the DS muon flux measurements are compared restricting the
 703 DS fiducial volume to the one used for the SciFi measurement. The muon flux for
 704 both detectors in an area between $-42 \text{ cm} \leq x \leq -11 \text{ cm}$ and $18 \text{ cm} \leq y \leq 49 \text{ cm}$ is
 705 reported in Table 8. The relative difference between the two detector measurements

system	muon flux [10^4 fb/cm 2]
SciFi	$2.06 \pm 0.01 \pm 0.11$
DS	$2.35 \pm 0.01 \pm 0.08$

Table 7: Muon flux in the SciFi and the DS detectors of the SND@LHC experiment. Statistical and systematic uncertainties are reported. The considered systematic uncertainty sources are the uncertainty of the luminosity measurement, the slight fluctuations in tracking efficiency in different $x - y$ detector regions, and the dependence of the tracking performance on the muon energy. The considered detector fiducial volumes are defined in the text.

706 is 2%. It is smaller than the total relative uncertainty of each detector measurement,
 707 which is 5 % for the SciFi and 3 % for the DS measurement. The difference in the
 708 DS flux results in Tables 7 and 8 for the two different transverse $x - y$ detector
 709 regions is due to a flux gradient with the vertical y position and is discussed in the
 following Section 9.

system	muon flux [10^4 fb/cm 2] <i>same fiducial area</i>
SciFi	$2.06 \pm 0.01 \pm 0.11$
DS	$2.02 \pm 0.01 \pm 0.06$

Table 8: Muon flux in the SciFi and the DS detectors of the SND@LHC experiment considering identical detector fiducial area in range $-42 \text{ cm} \leq x \leq -11 \text{ cm}$ and $18 \text{ cm} \leq y \leq 49 \text{ cm}$. Statistical and systematic uncertainties are reported. The considered systematic uncertainty sources are the uncertainty of the luminosity measurement, the slight fluctuations of tracking efficiency in different $x - y$ detector regions, and the dependence of the tracking performance on the muon energy.

710

711 9 Data/MC simulation comparison

712 Having a muon flux data estimate, one can compare it with the value predicted by
 713 simulations. This comparison is done for the two available sets of FLUKA simulations
 714 discussed in Section 4 and outlined in Table 2. It is not only the flux as a number
 715 that is to be compared. Important features such as the vertical flux gradient and
 716 the two neighboring peaks forming the main IP1 muon peak are to be sought in the
 717 Monte Carlo simulation as well.

718 In terms of muon flux, the two MC simulation sets provide expectations with a
 719 factor of 2 difference. The reason is the improved description of the experimental
 720 conditions, i.e., magnetic field extension, crossing angle, and TCL6 collimator set-
 721 tings, used to generate the March 2023 set. In Table 9 the MC simulation muon
 722 fluxes are reported for both sets and in two scenarios. One is the primary muon
 723 reaches the detector, and the other - the muon leaves a reconstructible trace in the

724 detector. The difference between these two cases is due to the absorption of soft
 725 muons in the heavy material between tracking planes, the potential failure of track
 726 reconstruction if a shower evolves, or muon deep inelastic scattering. Particles going
 727 close to the detector edge or entering the volumes at large angles contribute to a
 728 lesser extent. The reasons are that the selected fiducial volume is in the inner part
 729 of the detector, and most muons from IP1 that reach the detector have milliradian
 730 angles. Overall, the difference in the expected muon fluxes for the two scenarios is
 below 2% for both systems.

system	number of MC points	muon flux [10^4 fb/cm ²]
March 2022 MC simulation set		
SciFi	1	4.29 ± 0.38
	3H +3V	4.28 ± 0.38
DS	1	4.41 ± 0.22
	3H +3V	4.36 ± 0.22
March 2023 MC simulation set		
SciFi	1	1.61 ± 0.05
	3H +3V	1.60 ± 0.05
DS	1	1.82 ± 0.03
	3H +3V	1.79 ± 0.03

Table 9: Generator muon fluxes in the SciFi and the DS selected fiducial ranges, $-42 \text{ cm} \leq x \leq -11 \text{ cm}$ and $18 \text{ cm} \leq y \leq 49 \text{ cm}$ for SciFi, and $-54 \text{ cm} \leq x \leq -2 \text{ cm}$ and $12 \text{ cm} \leq y \leq 64 \text{ cm}$ for DS. The fluxes are estimated for two scenarios. One case is the generated primary muon makes at least 1 MC point in a detector. The other, the muon leaves points in at least 3 horizontal(H) and 3 vertical(V) detector planes, i.e. it leaves a reconstructible trace. The statistical uncertainty for each case is quoted. As expected, it decreases with increased MC simulation statistics.

731

732

733

734

735

736

737

738

739

740

741

742

743

744

745

The simulation that better reflects the beam crossing angle for the year 2022 LHC run and features an extended magnetic field map and the correct TCL6 aperture setting, the March 2023 one, provides a prediction that is closer to the data observation. In Table 10 data flux estimations and results for that simulation sample are compared in two cases. In the first one, the data muon flux with data-based tracking efficiency correction is examined across an estimate of the muon flux for generated reconstructible muons. In the second case, the data muon flux without tracking efficiency correction is compared to the MC simulation muon flux estimated using reconstructed MC tracks. For the latter, the Hough transform tracking is used. In all cases, the muon flux estimates for data and simulations differ between 20-25 %.

The assessed systematic uncertainty of the MC simulation flux prediction is reported in Table 10. The considered sources relate to the GEANT4 particle propagation simulation stage. Assessment of the FLUKA sample uncertainty is not included. The evaluated systematic uncertainty factors are the composition of the

746 rock between the scoring plane and the TI-18 tunnel and the precision of the rela-
 747 tive alignment between the scoring plane and the SND@LHC apparatus. Originally,
 748 the standard FLUKA rock model is used in the GEANT4 particle propagation stage.
 749 The density of the material is 2.0 g/cm^3 . As an alternative rock composition de-
 750 scription, the FLUKA definition of Molasse rock with a density of 2.4 g/cm^3 has been
 751 employed since a recent study shows it represents well the actual rock surrounding
 752 the LHC envelope [26]. To address the uncertainty due to the scoring plane’s rela-
 753 tive alignment to the detector, the whole plane has been moved along the Z axis by
 754 $\pm 10 \text{ cm}$ with respect to its nominal position. For each varied parameter, rock model,
 755 Z position of the scoring plane, a new simulation set has been generated and the
 756 MC analysis has been repeated. The total systematic uncertainty is the quadrature
 757 sum of the deviations of the new flux estimates with respect to the central one. Its
 magnitude is about 10% of the predicted flux value.

system	sample	muon flux [10^4 fb/cm^2]	$1 - \frac{\text{simulation}}{\text{data}}$ [%]
on the level of eff. corrected data and generator MC flux			
SciFi	data	$2.06 \pm 0.01 \pm 0.11$	22 ± 10
	simulation	$1.60 \pm 0.05 \pm 0.19$	
DS	data	$2.35 \pm 0.01 \pm 0.08$	24 ± 7
	simulation	$1.79 \pm 0.03 \pm 0.15$	
on the level of reconstructed tracks, no eff. corrections			
SciFi	data	$1.97 \pm 0.01 \pm 0.05$	23 ± 9
	simulation	$1.52 \pm 0.05 \pm 0.17$	
DS	data	$2.22 \pm 0.01 \pm 0.05$	21 ± 8
	simulation	$1.75 \pm 0.03 \pm 0.16$	

Table 10: Data/Monte Carlo simulation muon flux comparisons for SciFi and DS selected fiducial ranges. First, data muon flux with data-based tracking efficiency correction and the muon flux for generated reconstructible muons are reported. Second, the data muon flux without tracking efficiency correction and the MC simulation muon flux obtained using Hough transform MC reconstructed tracks are compared. The statistical and systematic uncertainties for each case are quoted. The agreement level between data and simulations and its total uncertainty are given in the last column.

758

759

760

761

762

763

764

765

766

The muon flux gradient with vertical position is evident in the SciFi and the DS data, which is shown in Figures 32a-b. However, the number of muons reaching the detector in as many as 200M simulated proton-proton interactions is insufficient to reproduce the vertical flux gradient in 2 dimensional(2D) $x - y$ bins, but the trend is clearly visible when one integrates over the x dimension. This is demonstrated in Figures 32c-f for the 2D case, where the March 2023 MC simulation is the single one that partially reflects the DS muon flux increase going to higher y positions. On the other hand, the SciFi and the DS 1D track distributions in y coordinate bins,

767 presented in Figure 33 for the March 2023 set, do show an increased flux for larger
768 y values.

769 It is reported in Section 7 that the electronic detectors data reveal a two-headed
770 central peak in the horizontal muon track slopes distribution. For the March 2023
771 simulation sample, the distribution of the same parameter is shown in Figure 34.
772 The two sub-peaks are present in the MC simulation as well, the distance between
773 them being 5.5 mrad. This value is well compatible with the emulsion and electronic
774 detectors data measurement of 5 mrad. The microradian shift of the absolute values
775 of the peaks in MC simulation with respect to the data is to be further investigated.
776 A possible reason can be the difference between actual geometry and the MC sim-
777 ulation geometry description induced by survey measurements' finite precision.

778

779 10 Conclusions

780 The muon flux at the SND@LHC detector location in the TI-18 tunnel has been
781 assessed using the first data collected by the experiment during the LHC Run 3
782 operation in 2022. Results using the information provided by the two independent
783 electronic detector systems, the fine-granulated SciFi and the DS, are reported. The
784 measured muon flux using the SciFi is $2.06 \pm 0.01(\text{stat}) \pm 0.11(\text{sys}) \times 10^4 \text{ fb/cm}^2$,
785 while for the DS it is $2.35 \pm 0.01(\text{stat}) \pm 0.08(\text{sys}) \times 10^4 \text{ fb/cm}^2$. The total relative
786 uncertainty of the results is 5 % for the SciFi and 3 % for the DS measurement.
787 The statistical uncertainties are rather low given the large analysis data sample. In
788 a single LHC fill, tens of millions of muons go through the detector. The reported
789 systematic uncertainty takes into account the dependence of the tracking perfor-
790 mance on the muon energy, respectively the tracking method used, the uncertainty
791 of the luminosity measurement, and the slight fluctuations in tracking efficiency in
792 different $x - y$ detector regions. Data/Monte Carlo simulation comparisons are also
793 reported. The predicted MC simulation muon flux in each detector is 20-25 % lower
794 than the measured one. The simulation prediction is assigned about 10 % relative
795 systematic uncertainty, not including the one of the FLUKA muon flux at the scor-
796 ing plane. The assessed systematic uncertainty of the MC simulation prediction is
797 associated with the GEANT4 particle propagation simulation stage and accounts for
798 rock modeling and alignment between the scoring plane and the detector.

799 Detector calibration, track reconstruction and tuning, and a thorough study of
800 the LHC filling scheme have been successfully performed and assist all analyses.
801 Furthermore, essential inputs for the flux measurement are the LHC accelerator sta-
802 tus and luminosity information. Consistent results for the origins of tracks entering
803 the detector from different sides, e.g. IP1, the back or sides of the detector, are
804 provided using the angular track distribution in the horizontal plane, the detector
805 hit timing, and the LHC bunch structure information. The vast majority of muons
806 originate in IP1 collisions. A small fraction of tracks, synchronous to Beam 2 pres-
807 ence in the area, impinge on the SciFi and the DS from the back or the sides. Their
808 contribution to the muon flux has been assessed and subtracted from the selected
809 data sample.

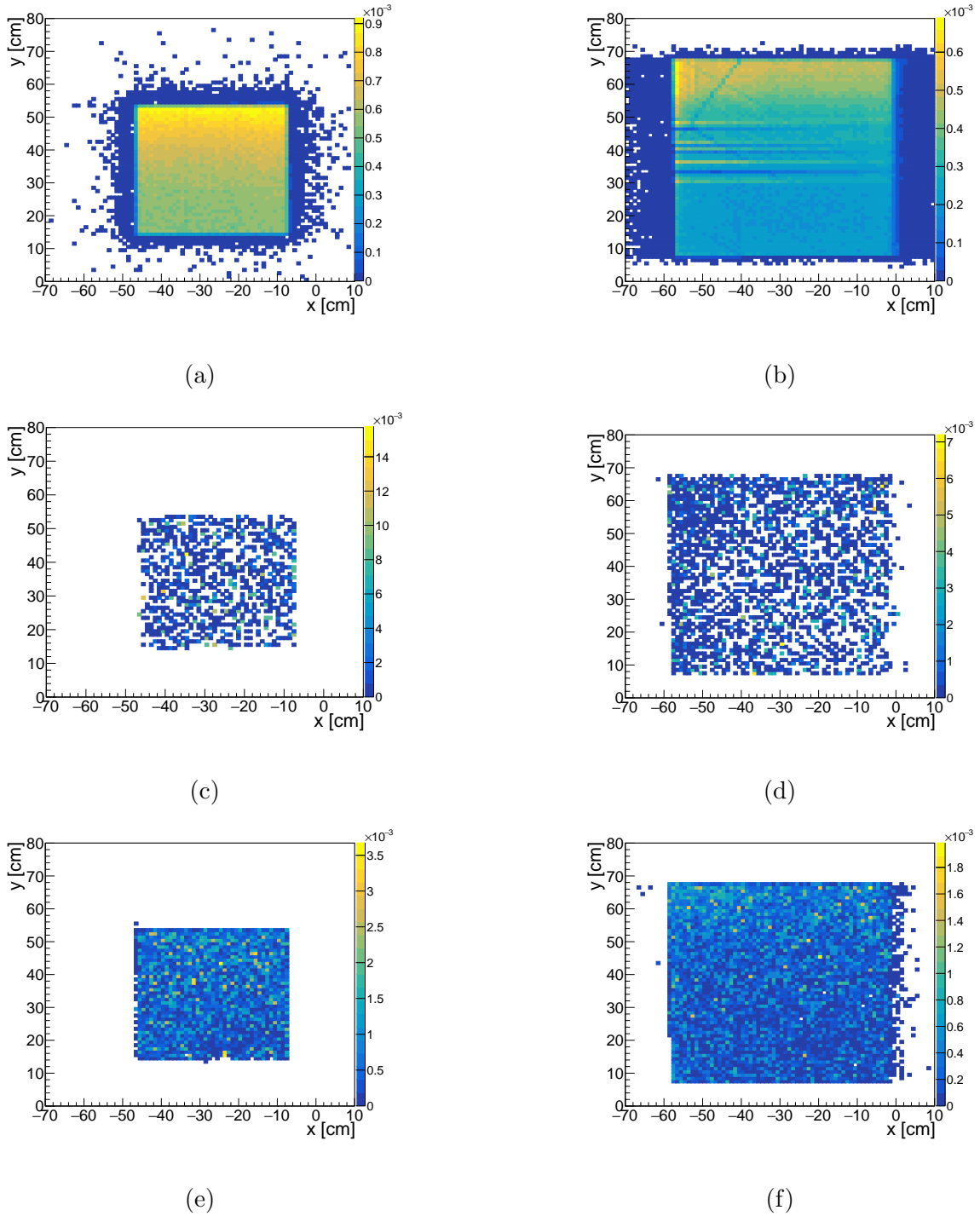


Figure 32: Reconstructed tracks $x - y$ profile at the upstream detector face for SciFi and DS tracks for data and simulations. Tracks are built using the Hough transform tracking. The data $x - y$ profiles in SciFi (a) and in DS (b) show an increase in the muon flux with vertical y position. It is not observed in the March 2022 MC simulation sample (c) - (d). For the March 2023 sample, the SciFi profile (e) is rather uniform, while there is a slight vertical gradient for the DS (f). Each distribution is normalized to unit integral.

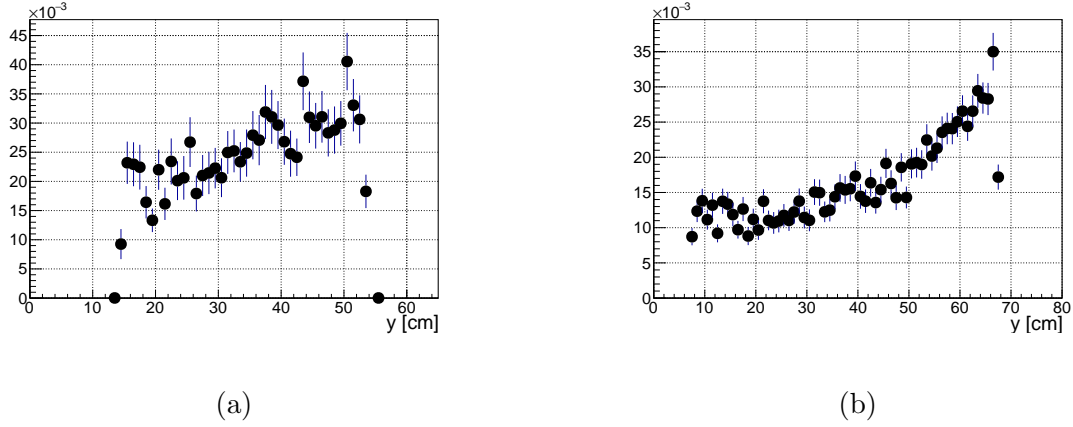


Figure 33: Normalized numbers of reconstructed tracks in vertical y position bins at the upstream detector face for SciFi (a) and DS (b) tracks using the March 2023 MC simulation set. Tracks are built using the Hough transform tracking. For each system, the muon flux increases towards the top of the detector. The two distributions are normalized to unit integral.

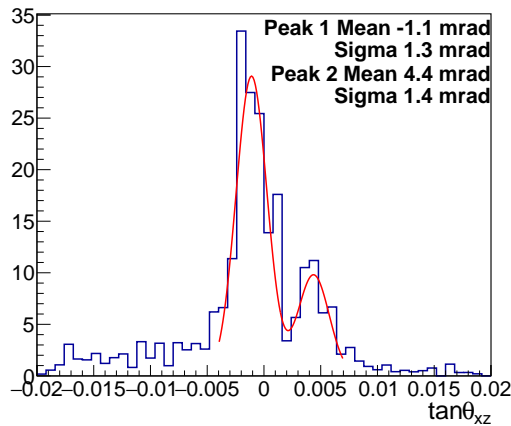


Figure 34: MC muon track slopes in the horizontal plane. The region around a few milliradians is magnified to show the two central sub-peaks of the main peak. A double Gaussian is used to fit the peaks. The means and sigmas of the global fit are reported.

810 A number of effects have been studied, verified between electronic detectors and
811 emulsion data, and cross-examined with simulations. A closer look at the horizon-
812 tal angular peak for muons penetrating the SciFi tracker reveals a two sub-peak
813 structure. The two peaks are also present in emulsion data and in MC simula-
814 tion. The distance between them in all cases is about 5 mrad. A point source
815 cannot be assigned to the muons forming the secondary peak. They are produced
816 in the follow-up of IP1 proton-proton collisions along the path from the IP to the
817 SND@LHC apparatus.

818 In the data, there is a well-pronounced gradient of the muon flux with the vertical
819 position for both SciFi and DS. The available simulation statistics are sufficient to
820 reproduce this effect when integrating over the horizontal x positions. Additionally,
821 preliminary emulsion data results show the same vertical structure in the emulsion
822 tracks density.

823 The current note provides a detailed overview of the first measurement of the
824 muon flux with the SND@LHC electronic detectors. The measured muon flux is
825 used to constrain the muon-induced background in neutrino searches.

References

- 826
- 827 [1] **SND@LHC** Collaboration, C. Ahdida et al., “SND@LHC - Scattering and
828 Neutrino Detector at the LHC.” <https://cds.cern.ch/record/2750060>,
829 2021.
- 830 [2] O. S. Brüning, P. Collier, P. Lebrun, S. Myers, R. Ostojic, J. Poole, and
831 P. Proudlock, *LHC Design Report*. CERN Yellow Reports: Monographs.
832 CERN, Geneva, 2004.
- 833 [3] “LHC Programme Coordination.” <https://lpc.web.cern.ch/>. Accessed
834 April 2023.
- 835 [4] R. Lauckner, *LHC Operational Modes, LHC-OP-ES-0004* (2004).
- 836 [5] **ATLAS** Collaboration, M. Aaboud et al., *Luminosity determination in pp*
837 *collisions at $\sqrt{s} = 8$ TeV using the ATLAS detector at the LHC*, *Eur. Phys.*
838 *J. C* **76** (2016), no. 12 653, [[arXiv:1608.03953](https://arxiv.org/abs/1608.03953)].
- 839 [6] **ATLAS** Collaboration, *Luminosity determination in pp collisions at $\sqrt{s} = 13$*
840 *TeV using the ATLAS detector at the LHC*, [[arXiv:2212.09379](https://arxiv.org/abs/2212.09379)].
- 841 [7] G. Iadarola, H. Bartosik, E. Belli, L. R. Carver, P. Dijkstal, K. S. B. Li,
842 L. Mether, A. Romano, and G. Rumolo, *MD421: Electron cloud studies on*
843 *25 ns beam variants (BCMS, 8b+4e)*, 2017.
844 <https://cds.cern.ch/record/2260998>.
- 845 [8] A. Iuliano, *Measurement of the muon flux with the emulsion target at*
846 *SND@LHC*, 2023. in preparation.
- 847 [9] G. Battistoni et al., *Overview of the FLUKA code*, *Annals Nucl. Energy* **82**
848 (2015) 10–18.
- 849 [10] C. Ahdida et al., *New Capabilities of the FLUKA Multi-Purpose Code*, *Front.*
850 *in Phys.* **9** (2022) 788253.
- 851 [11] S. Roesler, R. Engel, and J. Ranft, *The Monte Carlo event generator*
852 *DPMJET-III*, in *International Conference on Advanced Monte Carlo for*
853 *Radiation Physics, Particle Transport Simulation and Applications (MC*
854 *2000)*, pp. 1033–1038, 12, 2000. [[hep-ph/0012252](https://arxiv.org/abs/hep-ph/0012252)].
- 855 [12] A. Fedynitch, *Cascade equations and hadronic interactions at very high*
856 *energies*. PhD thesis, KIT, Karlsruhe, Dept. Phys., 11, 2015.
- 857 [13] A. Lechner et al., *Validation of energy deposition simulations for proton and*
858 *heavy ion losses in the CERN Large Hadron Collider*, *Phys. Rev. Accel.*
859 *Beams* **22** (2019), no. 7 071003.

- 860 [14] D. Prelicpean, K. Bilko, F. Cerutti, A. Ciccotelli, D. Di Francesca,
861 R. García Alía, B. Humann, G. Lerner, D. Ricci, and M. Sabaté-Gilarte,
862 *Comparison Between Run 2 TID Measurements and FLUKA Simulations in*
863 *the CERN LHC Tunnel of the Atlas Insertion Region, JACoW IPAC 2022*
864 (2022) 732–735. <http://cds.cern.ch/record/2839993>.
- 865 [15] **GEANT4** Collaboration, S. Agostinelli et al., *GEANT4—a simulation toolkit,*
866 *Nucl. Instrum. Meth. A* **506** (2003) 250–303.
- 867 [16] **SND@LHC** Collaboration, G. Acampora et al., *SND@LHC: The Scattering*
868 *and Neutrino Detector at the LHC*, [[arXiv:2210.02784](https://arxiv.org/abs/2210.02784)].
869 <https://cds.cern.ch/record/2838901>.
- 870 [17] “SND@LHC survey measurements.”
871 <https://edms.cern.ch/document/2882720/1/>.
- 872 [18] P. V. Hough, *Method and means for recognizing complex patterns, U.S. Patent*
873 *30696541962* (1962).
- 874 [19] V. F. Leavers, *Computer Vision: Shape Detection*, pp. 1–18. Springer London,
875 London, 1992.
- 876 [20] R. E. Kalman, *A New Approach to Linear Filtering and Prediction Problems,*
877 *Journal of Basic Engineering* **82** (03, 1960) 35–45.
- 878 [21] R. Fruhwirth, *Application of Kalman filtering to track and vertex fitting, Nucl.*
879 *Instrum. Meth. A* **262** (1987) 444–450.
- 880 [22] J. Rauch and T. Schlüter, *GENFIT — a Generic Track-Fitting Toolkit, J.*
881 *Phys. Conf. Ser.* **608** (2015), no. 1 012042, [[arXiv:1410.3698](https://arxiv.org/abs/1410.3698)].
- 882 [23] C. Höppner, S. Neubert, B. Ketzer, and S. Paul, *A novel generic framework*
883 *for track fitting in complex detector systems, Nuclear Instruments and*
884 *Methods in Physics Research Section A: Accelerators, Spectrometers,*
885 *Detectors and Associated Equipment* **620** (2010), no. 2 518–525.
- 886 [24] “CERN GIS Portal.” <https://gis.cern.ch>. Accessed April 2023.
- 887 [25] **ATLAS** Collaboration, *Preliminary analysis of the luminosity calibration of*
888 *the ATLAS 13.6 TeV data recorded in 2022*, tech. rep., CERN, Geneva, 2023.
889 All figures including auxiliary figures are available at
890 [https://atlas.web.cern.ch/Atlas/GROUPS/PHYSICS/PUBNOTES/ATL-](https://atlas.web.cern.ch/Atlas/GROUPS/PHYSICS/PUBNOTES/ATL-DAPR-PUB-2023-001)
891 [DAPR-PUB-2023-001](https://atlas.web.cern.ch/Atlas/GROUPS/PHYSICS/PUBNOTES/ATL-DAPR-PUB-2023-001).
- 892 [26] M. Tisi, A. Infantino, and P. Dyrzcz, “HL-LHC cores drilling: summary of
893 HSE-RP studies and recommendations.”
894 <https://edms.cern.ch/document/2861462/2/approvalAndComments>.
895 Presentation given to the HL-LHC WP15 Integration Meeting held on
896 March 24, 2023.