

Multi-lepton probes of new physics and lepton-universality in top-quark interactions

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We explore the sensitivity to new physics (NP) in the associated production of top-quarks with leptons $pp \rightarrow t\bar{t}\ell^+\ell^-$, which leads to the multi-leptons signals $pp \rightarrow n\ell + \text{jets} + \cancel{E}_T$, where $n = 2, 3, 4$. The NP is parameterized via 4-Fermi effective $t\bar{t}\ell^+\ell^-$ contact interactions of various types, which are generated by multi-TeV heavy scalar, vector or tensor exchanges in $t\bar{t} \rightarrow \ell^+\ell^-$; we focus on the case of $\ell = e, \mu$. We match the 4-Fermi $t\bar{t}\ell\ell$ terms to the SMEFT operators and also give examples of specific underlying heavy physics that can generate such terms. Analysis of the SM signals and corresponding backgrounds shows that the di-lepton and tri-lepton channels are much better probes of the effective $t\bar{t}\ell^+\ell^-$ 4-Fermi terms than the four-lepton one at the 13 TeV LHC. Therefore, the best sensitivity is obtained in the di- and tri-lepton channels, for which the dominant background $pp \rightarrow t\bar{t}$ and $pp \rightarrow WZ$, respectively, can be essentially eliminated after applying the 2ℓ and 3ℓ selections and a sufficiently high invariant mass selection for the opposite sign same flavor (OSSF) lepton-pair. We explore two cases: lepton flavor universal (LFU) NP where the $t\bar{t}ee$ and $t\bar{t}\mu\mu$ contact interactions are of same size and LFU violating (LFUV) NP, where the scale of the $t\bar{t}\mu\mu$ terms is assumed to be much lower. We show that in both cases it is possible to obtain new 95% CL bounds on the scale of the $t\bar{t}\ell\ell$ contact interactions at the level $\Lambda \gtrsim 2 - 3$ TeV, which are considerably tighter than the current bounds on these 4-Fermi terms.

CONTENTS

I. Introduction	1
II. Theoretical Framework	2
III. Matching: SMEFT and the underlying new physics	3
IV. Current Bounds on $t\bar{t}\ell\ell$ 4-Fermi operators	5
V. Signal and background analysis	5
A. Calculation setup and numerical session	5
B. Simulated Event Samples	6
C. Event selection and background	6
D. Domain of validity of the EFT setup	7
VI. Results	8
A. Cut-and-Count Study	8
B. Ratio observables and LFUV	9
VII. Summary	12
Acknowledgments	12
References	13
A. Cut-flow tables	18

I. INTRODUCTION

Third generation fermions are a promising window to potential new physics (NP) that underlies the Standard Model (SM). This is best manifested for the 3rd generation quark doublet and, in particular the top-quark, which is significantly heavier than all other quarks and is, therefore, expected to be the most sensitive to NP of a higher scale, such as new flavor physics [1–18] and CP-violation beyond the SM [19]. For this reason, model independent studies in the Effective Field Theory (EFT) approach have been widely applied to top physics in the past two decades [20–52]. Global and comprehensive EFT studies of various types of higher dimensional operators involving the top-quark field(s) can be found in [21–23, 26–30, 52–54]. The effects of (2-quarks)(2-leptons) 4-Fermi operators (which are of interest in this study) had been recently studied also in [21, 51, 52, 55–64]; the $t\bar{t}\ell\ell$ class of operators is, however, poorly bounded as will be further discussed below.

Furthermore, persistent hints for NP involving the 3rd generation quark-doublet and lepton flavor universality violation (LFUV) have been emerging in the past decade in B-decays [65–67]. Some of the notable ones are the ratios $\Gamma(B \rightarrow K^{(*)}\mu\mu)/\Gamma(B \rightarrow K^{(*)}ee)$ ($= R_{K^{(*)}}$) and to some degree the decay $B_s^0 \rightarrow \mu^+\mu^-$, all associated with $b \rightarrow s\mu^+\mu^-$ transitions, as well as the ratio $R_{D^{(*)}}$ which occurs in the SM via tree-level $b \rightarrow c\ell^-\nu_\ell$ (see also [68–89]). These LFUV signals may also imply that lepton flavor violation (LFV) effects can be sizable, i.e., much larger than expected in the SM [90]. In addition, the recently confirmed [91] muon $g-2$ anomaly and also recent interesting measurements (although with less statistical

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significance) that have been reported by ATLAS [92, 93] and CMS [94] in unequal production of di-muons versus di-electrons, provide further hints for possible NP involved in high- p_T lepton production, and may also indicate that LFUV NP may be mediated by new TeV-scale states of the underlying heavy theory; potentially in interactions between the 3rd generation quarks and the electrons and muons.

Indeed, in previous recent papers [55–58] we have explored the NP effects of higher-dimensional 4-Fermi interactions involving 3rd generation quarks and a pair of electrons and/or muons, on scattering processes at the LHC which lead to multi-leptons final states in associations with the 3rd generation quarks. In particular, the flavor changing $bs\ell\ell$ leading to $pp \rightarrow \ell^+\ell^- + j_b$ ($j_b = b$ -jet) [55], the SU(2) related $t\ell\ell$ (and also $t\mu\ell$) leading to e.g., $pp \rightarrow \ell^+\ell^- + t$ [58] as well as the flavor diagonal $b\ell\ell$ leading to e.g., $pp \rightarrow \ell^+\ell^- + j_b$ or $pp \rightarrow \ell^+\ell^- + 2j_b$ [56, 57].

In this paper we expand these studies and consider the effects of the (poorly constrained - see below) $tt\ell\ell$ 4-Fermi contact terms on multi-lepton production in association with a top-quark pair (or a single-top) at the LHC. We note (as further discussed below) that one-loop effects of higher-dimensional 4-Fermi operators involving the top-quark, in particular the $tt\ell\ell$ ones, can also address the $g-2$ [95, 96] and possibly the B-physics anomaly

[97–100] when the NP scale is $O(\text{TeV})$, potentially open to direct observation. In contrast, tree-level contributions from effective operators (e.g., operators generating a $b \rightarrow s\ell\ell$ vertex) require a NP scale in the 20 – 40 TeV range. Indeed, we find that the multi-lepton signals which we study in this paper are sensitive to the $tt\ell\ell$ contact interactions if their scale is $\Lambda \sim \text{few TeV}$.

Finally, we emphasize that while we are, to some degree, motivated by the above mentioned few σ deviations seen in B-physics lepton universality tests and also in muon ($g-2$) anomaly as hints of NP, our collider based search for beyond the SM (BSM) physics in multi-lepton final states is cast in more general terms. In particular, this search is designed for both lepton flavor diagonal as well as off-diagonal final states, but restricted in this study to comparing muons with electrons only. In fact such comparisons have been of interest for a very long time (see e.g. [101]).

II. THEORETICAL FRAMEWORK

We adopt the parameterization used in [58, 102] and [103, 104] for the effective Lagrangian of the flavor changing (FC) $t\bar{u}\ell^+\ell^-$ and flavor diagonal $t\bar{t}\ell^+\ell^-$ contact terms, respectively:

$$\mathcal{L}_{tt\ell\ell} = \frac{1}{\Lambda_\ell^2} \sum_{i,j=L,R} \left[V_{ij}^\ell (\bar{\ell}\gamma_\mu P_i \ell) (\bar{t}\gamma^\mu P_j t) + S_{ij}^\ell (\bar{\ell} P_i \ell) (\bar{t} P_j t) + T_{ij}^\ell (\bar{\ell}\sigma_{\mu\nu} P_i \ell) (\bar{t}\sigma_{\mu\nu} P_j t) \right], \quad (1)$$

where $P_{L,R} = (1 \mp \gamma_5)/2$ and V_{ij}^ℓ , S_{ij}^ℓ , T_{ij}^ℓ are the dimensionless couplings of the vector, scalar and tensor 4-Fermi interactions, respectively. As mentioned before throughout this work we will focus only on the NP involving electrons and muons, i.e., the $tt\mu\mu$ and $ttee$ terms, and assume that the scale of the corresponding LFV, off-diagonal in flavor, 4-Fermi interactions, $tt\mu e$, is much higher so that the effects of such LFV 4-Fermi operators can be neglected.

The scale of the underlying NP involving electrons and muons may be different; a lower scale for the NP involving muons provides a very reasonable interpretation of the above mentioned anomalies in B-decays and the muon $g-2$. Thus, in what follows, we will explore two cases: LFU NP where $\Lambda_e = \Lambda_\mu$ and LFUV muon-filic NP where $\Lambda_\mu \ll \Lambda_e$, for which case the leading effect of the tree-level exchanges of the heavy states is manifest in the $tt\mu\mu$ contact terms.

We will consider below the effects of these new $tt\ell\ell$ contact interactions ($\ell = \mu, e$) in top-quark pair production in association with a pair of opposite-sign (OS) leptons (see Figs. 1 and 2 for representative SM and NP diagrams

for these processes, respectively):¹

$$\begin{aligned} pp &\rightarrow t\bar{t}\ell^+\ell^-, \\ pp &\rightarrow t(\bar{t})\ell^+\ell^- + j_b + j, \end{aligned} \quad (2)$$

leading to the following di-lepton, tri-lepton or four-leptons signals ($j = \text{light-jet}$ and $j_b = b\text{-jet}$):

$$\begin{aligned} (tt\ell\ell)_{2\ell} &\equiv pp \rightarrow \ell^+\ell^- + 2 \cdot j_b + 4 \cdot j, \\ (tt\ell\ell)_{3\ell} &\equiv pp \rightarrow \ell'^{\pm}\ell^{\mp}\ell^+\ell^- + 2 \cdot j_b + 2 \cdot j + \cancel{E}_T, \\ (tt\ell\ell)_{4\ell} &\equiv pp \rightarrow \ell'^{\pm}\ell''^{\mp}\ell^+\ell^- + 2 \cdot j_b + \cancel{E}_T, \\ (t\ell\ell)_{2\ell} &\equiv pp \rightarrow \ell^+\ell^- + 2 \cdot j_b + 3 \cdot j, \\ (t\ell\ell)_{3\ell} &\equiv pp \rightarrow \ell'^{\pm}\ell^{\mp}\ell^+\ell^- + 2 \cdot j_b + j + \cancel{E}_T, \end{aligned} \quad (3)$$

depending on the top-quarks decay channels: $(tt\ell\ell)_{2\ell}$ when the $t\bar{t}$ pair decay hadronically via $t\bar{t} \rightarrow$

¹ The single-top production channel in association with di-leptons: $pp \rightarrow t\ell^+\ell^- + j_b + j$ (and the charged conjugate channel) via the underlying Wb scattering process $Wb \rightarrow t \rightarrow t\ell^+\ell^-$, is also generated by the new $tt\ell\ell$ interactions in Eq. 1 and are included in our analysis, although their relative contribution to the di- and tri-leptons signals considered here is considerably smaller.

$b\bar{b}W^+W^- \rightarrow 2j_b + 4j$, $(t\bar{t}l\ell)_{3\ell}$ when one top decays leptonically via $t \rightarrow bW \rightarrow j_b + \ell' + \cancel{E}_T$ and $(t\bar{t}l\ell)_{4\ell}$ when both tops decay leptonically $t\bar{t} \rightarrow b\bar{b}W^+W^- \rightarrow 2j_b + \ell'^{\pm}\ell''^{\mp} + \cancel{E}_T$. Similarly, in the single-top channels: $(t\bar{t}l\ell)_{2\ell}$ when the top (or anti-top) decays hadronically and $(t\bar{t}l\ell)_{3\ell}$ when it decays leptonically. For example, in the LFUV muon-filic NP case we have $2\ell = \mu^+\mu^-$, $3\ell = \mu^{\pm}\mu^+\mu^-$, $e^{\pm}\mu^+\mu^-$ and $4\ell = \mu^+\mu^-\mu^+\mu^-$, $e^+e^-\mu^+\mu^-$, $e^{\pm}\mu^{\mp}\mu^+\mu^-$. We note that the di-lepton channel was extensively studied in the past few years as a potential probe of high- p_T NP and LFUV effects at the LHC, both experimentally [92–94] and theoretically [55–58, 63, 67, 105–110]. Furthermore, the tri- and four-leptons channels were recently analyzed in searches for the classic $t\bar{t}Z$, $t\bar{t}W$ [111, 112] and $t\bar{t}H$ [113, 114] top signals, as well as the interesting 4-tops ($pp \rightarrow t\bar{t}t\bar{t}$) signal [115, 116]. They are also useful for generic NP searches [117, 118] and, although they are flavor-blind, they can also be very effectively used to search for FCNC physics in the top sector [50, 58].

We find that (at least at the 13 TeV LHC) the four-leptons channel, $(t\bar{t}l\ell)_{4\ell}$, is significantly less sensitive to the NP effect generated by the $t\bar{t}l\ell$ 4-Fermi interactions than the di- and tri-lepton channels, $(t\bar{t}l\ell)_{2\ell}$ and $(t\bar{t}l\ell)_{3\ell}$, respectively. Indeed, as will be shown below, the new 4-Fermi $t\bar{t}l\ell$ interactions can be very efficiently isolated from the SM background as well as from other potential sources of NP in the di- and tri-leptons channels $(t\bar{t}l\ell)_{2\ell}$ and $(t\bar{t}l\ell)_{3\ell}$ in Eq. 3, by selecting exactly 2 ℓ and 3 ℓ charged leptons in the final state and looking at the off-Z peak behavior of the OSSF di-leptons in $pp \rightarrow t\bar{t}l^+l^-$ along with extra selections on the accompanied high- p_T b -tagged and light-jets.

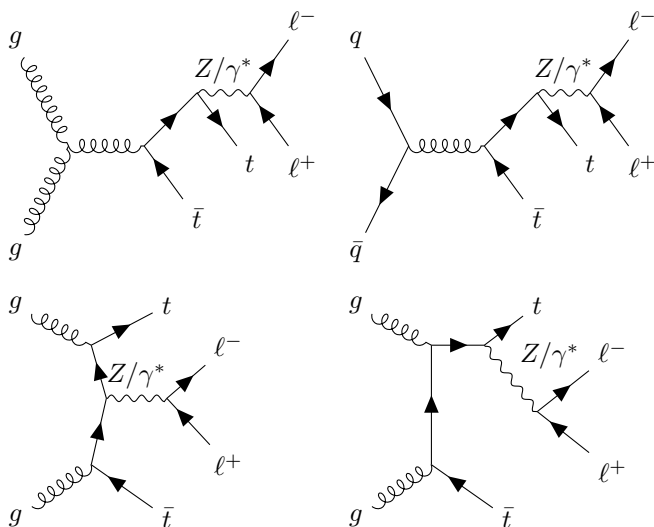


FIG. 1: Representative lowest-order SM Feynman diagrams for top-quark pair + di-lepton production, $pp \rightarrow t\bar{t}l^+l^-$.

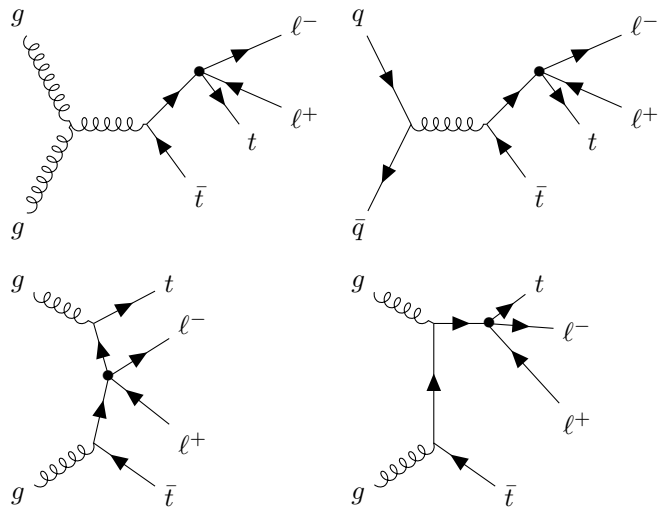


FIG. 2: Representative Feynman diagrams of $\mathcal{O}(1/\Lambda^2)$ for top-quark pair + di-lepton production $pp \rightarrow t\bar{t}l^+l^-$. The dimension six 4-Fermi interaction is marked by a heavy dot.

III. MATCHING: SMEFT AND THE UNDERLYING NEW PHYSICS

The dimension six 4-Fermi operators in Eq. 1 can be matched to the so-called SM Effective Field Theory (SMEFT) framework [119–123], where the higher dimensional effective operators are constructed using the SM fields and their coefficients are suppressed by inverse powers of the NP scale Λ :

$$\mathcal{L} = \mathcal{L}_{SM} + \sum_{n=5}^{\infty} \frac{1}{\Lambda^{n-4}} \sum_i \alpha_i \mathcal{O}_i^{(n)}, \quad (4)$$

so that n is the mass dimension of the operators $\mathcal{O}_i^{(n)}$, which equals the canonical dimension for a decoupling and weakly-coupled heavy NP and α_i are the (Wilson) coefficients which depend on the details of the underlying heavy theory (we give below an example of matching of the EFT setup to a specific underlying heavy NP scenario). The relevant SMEFT operators, which are related to our $t\bar{t}l\ell$ 4-Fermi operators in Eq. 1, are (p, r, s, t are flavor indices):

$$\begin{aligned} \mathcal{O}_{lq}^{(1)}(prst) &= (\bar{l}_p \gamma_\mu l_r) (\bar{q}_s \gamma^\mu q_t), \\ \mathcal{O}_{lq}^{(3)}(prst) &= (\bar{l}_p \gamma_\mu \tau^I l_r) (\bar{q}_s \gamma^\mu \tau^I q_t), \\ \mathcal{O}_{eu}(prst) &= (\bar{e}_p \gamma_\mu e_r) (\bar{u}_s \gamma^\mu u_t), \\ \mathcal{O}_{lu}(prst) &= (\bar{l}_p \gamma_\mu l_r) (\bar{u}_s \gamma^\mu u_t), \\ \mathcal{O}_{qe}(prst) &= (\bar{e}_p \gamma^\mu e_r) (\bar{q}_s \gamma_\mu q_t), \\ \mathcal{O}_{lequ}^{(1)}(prst) &= (\bar{l}_p^j e_r) \epsilon_{jk} (\bar{q}_s^k u_t), \\ \mathcal{O}_{lequ}^{(3)}(prst) &= (\bar{l}_p^j \sigma_{\mu\nu} e_r) \epsilon_{jk} (\bar{q}_s^k \sigma^{\mu\nu} u_t). \end{aligned} \quad (5)$$

The correspondence to this parameterization to that

in Eq. 1 is given by:²

$$\begin{aligned} V_{LL} &= \alpha_{\ell q}^{(1)} - \alpha_{\ell q}^{(3)}, \quad V_{LR} = \alpha_{\ell u}, \quad V_{RR} = \alpha_{e u}, \quad V_{RL} = \alpha_{q e}, \\ S_{RR} &= -\alpha_{\ell e q u}^{(1)}, \quad S_{LL} = S_{LR} = S_{RL} = 0, \\ T_{RR} &= -\alpha_{\ell e q u}^{(3)}, \quad T_{LL} = T_{LR} = T_{RL} = 0. \end{aligned} \quad (6)$$

The heavy physics processes that can generate the above dimension six effective operators at tree-level consists of exchanges of heavy vectors and scalars or their Fierz transforms. Interesting examples are the scalar S_1 , S_3 , R_2 and vector U_1 leptoquarks,³ which transform, respectively, as $(\bar{3}, 1, 1/3)$, $(\bar{3}, 3, 1/3)$, $(3, 2, 7/6)$ and $(3, 1, 2/3)$ under the $SU(3) \times SU(2) \times U(1)$ SM gauge group. These leptoquarks are particularly interesting, as they can address the persistent $R_{K^{(*)}}$, $R_{D^{(*)}}$ anomalies as well as the muon $g - 2$ anomaly: both $R_{K^{(*)}}$ and $R_{D^{(*)}}$ can be explained by a single U_1 vector leptoquark [124–134], or by the scalar leptoquark pairs S_1, S_3 and S_3, R_2 [135–141], which can also address the muon $g - 2$ discrepancy [95, 96], see also [142–151]. These leptoquarks have the following couplings to a quark-lepton pair [152]:⁴

$$\begin{aligned} \mathcal{L}_Y^{S_1} &= w_L \bar{q}^{i,C} \ell^j \epsilon_{ij} S_1 + w_R \bar{u}^C e S_1 + \text{h.c.}, \\ \mathcal{L}_Y^{S_3} &= z \bar{q}^{i,C} \ell^j (\epsilon \tau^I)_{ij} S_3^I + \text{h.c.}, \\ \mathcal{L}_Y^{R_2} &= y_q \bar{q}^i e R_2^i + y_u \bar{u} \ell^j \epsilon_{ij} R_2^i + \text{h.c.}, \\ \mathcal{L}_Y^{U_1} &\supset x \bar{q} \gamma_\mu U_1^\mu \ell + \text{h.c.}, \end{aligned} \quad (7)$$

where i, j are $SU(2)$ indices and flavor indices are not specified.

Tree-level exchanges of S_1 , S_3 , R_2 and U_1 among the lepton-quark pairs induce (after a Fierz transformation) some of the dimension six 4-Fermi operators in Eq. 5 and, therefore, the scalar, vector and tensor operators of Eq. 1 (see Eq. 6). In Table I we give the expressions of the operator coefficients in terms of those in Eq. 7.⁵ We note the following:

- Tree-level exchanges of the leptoquarks S_1 and R_2 (if they couple to a top-lepton pair) can generate both the scalar and tensor $tt\ell\ell$ operators, i.e., those with S_{RR} and T_{RR} couplings. In addition, S_1 can also generate the V_{LL} and V_{RR} vector operators, and R_2 the V_{RL} and V_{LR} ones.

- A vector leptoquark U_1 does not generate any of the scalar, vector and tensor 4-Fermi $tt\ell\ell$ operators in Eq. 1, even though it contributes to the operators $\mathcal{O}_{\ell q}^{(1,3)}$. The reason is that $V_{LL} = \alpha_{\ell q}^{(1)} - \alpha_{\ell q}^{(3)}$ (see Eq. 6) and $\alpha_{\ell q}^{(1)} = \alpha_{\ell q}^{(3)}$ if $\mathcal{O}_{\ell q}^{(1,3)}$ are generated by U_1 . Note, though, that it will generate the V_{LL} terms for the corresponding down-quark operators, e.g., $(\bar{\ell} \gamma_\mu P_i \ell) (\bar{b} \gamma^\mu P_j b)$ and/or the flavor changing $(\bar{\ell} \gamma_\mu P_i \ell) (\bar{b} \gamma^\mu P_j s)$, for which $V_{LL} = \alpha_{\ell q}^{(1)} + \alpha_{\ell q}^{(3)}$, see e.g., [67].
- The scalar leptoquark S_1 has the same quantum numbers as the right-handed sbottom and its couplings to a quark-lepton pair are, therefore, the same as in the R-parity violating (RPV) superpotential. Indeed, the RPV setup involving the 3rd generation quarks (the so called RPV3 of [153]) is a natural and well motivated RPV setup (see also [154, 155]) which is also an interesting candidate for addressing the B-physics and muon $g - 2$ anomalies [142, 153, 156, 157]. Note, though, that in this RPV3 framework the favored resolution to the muon $g - 2$ anomaly arises from 1-loop sneutrino exchanges [157]; the sneutrino does not, however, couple to up-quarks and therefore cannot generate our $tt\ell\ell$ 4-Fermi operators.

It is interesting to note that the tensor 4-Fermi operator $T_{RR} (\bar{\mu} \sigma_{\mu\nu} P_R \mu) (\bar{t} \sigma_{\mu\nu} P_R t)$ is the *only* $tt\mu\mu$ operator which can explain the muon $g - 2$ anomaly if $\Lambda \sim \mathcal{O}(\text{few TeV})$, its contribution is [95, 96]:

$$\Delta a_\mu \sim \mathcal{C} \cdot T_{RR} \cdot \frac{3}{\pi^2} \frac{m_\mu m_t}{\Lambda^2} \log \left(\frac{m_t^2}{\Lambda^2} \right) \quad (8)$$

where $\mathcal{C} \sim \mathcal{O}(0.1)$ if the tensor operator is generated from a tree-level exchange of the scalar leptoquark S_1 (see Table I).

Finally, some of the vector $tt\mu\mu$ operators, i.e., $\mathcal{O}_{\ell u}$ and $\mathcal{O}_{e u}$, involving right-handed top-quarks and corresponding to our $V_{LR} (\bar{\mu} \gamma_\mu P_L \ell) (\bar{t} \gamma^\mu P_R t)$ and $V_{RR} (\bar{\mu} \gamma_\mu P_R \ell) (\bar{t} \gamma^\mu P_R t)$ operators, respectively, can contribute at 1-loop to the $b \rightarrow s\ell\ell$ transitions and through RGE effects in the SMEFT framework [99, 100]. This result is of particular interest because it requires the NP scale to be $\Lambda \sim \mathcal{O}(\text{TeV})$ for natural couplings $V_{LR}, V_{RR} \sim \mathcal{O}(1)$ in order to address the anomalies measured in the $R_{K^{(*)}}$ observables [99, 100]. This suggests that the scale of these vector $tt\mu\mu$ 4-Fermi operators may be within the reach of the current LHC energies, in contrast to the case where the NP effect in $b \rightarrow s\ell\ell$ is generated at tree-level by 4-Fermi $bs\ell\ell$ operators where the NP scale required to address the B-anomalies is $\Lambda \sim 40 \text{ TeV}$.

Taking in earnest the above arguments in favor of the existence of TeV-scale scalar, tensor and vector $tt\ell\ell$ 4-Fermi interactions involving right-handed top-quarks, we will focus in the rest of this work on the S_{RR}, T_{RR} and V_{RR} $tt\ell\ell$ operators of Eq. 1. We note that the V_{RR} operator, i.e., constructed from the $SU(2)$ singlet fields, is the

² Note that no LL tensor or LL, LR and RL scalar terms are generated at dimension 6; they can, however, be generated by dimension 8 operators and thus have coefficients suppressed by $\sim (v^2/\Lambda^4)$, where $v = 246 \text{ GeV}$ is the Higgs vacuum expectation value.

³ Note that R_2 is the only scalar leptoquark that does not induce proton decay.

⁴ The vector leptoquark U_1 can have additional $d_R \gamma_\mu e_R$ and $u_R \gamma_\mu \nu_R$ couplings, which are not relevant for our $tt\ell\ell$ operators.

⁵ A compilation of the various additional types of NP that can induce the dimension six 4-Fermi interactions in Eq. 5 can be found in [63].

TABLE I: Matching leptoquarks exchanges to the 4-Fermi operators of $\mathcal{L}_{t\ell\ell}(V, S, T)$ in Eq. 1 and to the SMEFT operators in Eq. 5. See also text and Eq. 7.

$t\ell\ell$ coupling	S_1	S_3	R_2	U_1
$\alpha_{\ell q}^{(1)}$	$ w_L ^2/4M^2$	$3 z ^2/4M^2$	/	$- x ^2/2M^2$
$\alpha_{\ell q}^{(3)}$	$- w_L ^2/4M^2$	$ z ^2/4M^2$	/	$- x ^2/2M^2$
$V_{LL} = \alpha_{\ell q}^{(1)} - \alpha_{\ell q}^{(3)}$	$ w_L ^2/2M^2$	$ z ^2/2M^2$	/	/
$V_{LR} = \alpha_{\ell u}$	/	/	$- y_u ^2/2M^2$	/
$V_{RL} = \alpha_{qe}$	/	/	$- y_q ^2/2M^2$	/
$V_{RR} = \alpha_{eu}$	$ w_R ^2/2M^2$	/	/	/
$S_{RR} = -\alpha_{\ell e q u}^{(1)}$	$-w_R w_L^*/2M^2$	/	$-y_q y_u^*/2M^2$	/
$T_{RR} = -\alpha_{\ell e q u}^{(3)}$	$w_R w_L^*/8M^2$	/	$-y_q y_u^*/8M^2$	/

only vector 4-Fermi which does not directly contribute to b/B-physics, see [58] and discussion below.

IV. CURRENT BOUNDS ON $t\ell\ell$ 4-FERMI OPERATORS

As mentioned earlier, the $t\ell\ell$ 4-Fermi operators of Eq. 1 are in general poorly bounded, primarily since they are not accessible to the "classic" signals of the top-quark: top decays and $t\bar{t}$ pair-production which was not accessible to LEP2 energies and at the LHC is driven by gg - and $q\bar{q}$ -fusion. An exception is for the operators involving left-handed quark isodoublets for which gauge invariance relates the $t\ell\ell$ and $b\ell\ell$ 4-Fermi FC interactions. In particular, among the operators in Eq. 5, the $(\bar{L}L)(\bar{L}L)$ operators $\mathcal{O}_{\ell q}^{(1)}$, $\mathcal{O}_{\ell q}^{(3)}$ and the $(\bar{L}R)(\bar{R}L)$ one \mathcal{O}_{qe} , include both the $t\ell\ell$ and $b\ell\ell$ interactions. Thus, referring to Eq. 1, it then follows that the V_{LL} and V_{RL} couplings for the t and b quarks are related: $V_{LL}(t\ell\ell) = \alpha_{\ell q}^{(1)}(\ell\ell 33) - \alpha_{\ell q}^{(3)}(\ell\ell 33)$, $V_{LL}(b\ell\ell) = -\alpha_{\ell q}^{(1)}(\ell\ell 33) - \alpha_{\ell q}^{(3)}(\ell\ell 33)$ and $V_{RL}(t\ell\ell) = V_{RL}(b\ell\ell) = \alpha_{qe}(\ell\ell 33)$, and the corresponding scales Λ are, therefore, the same.⁶ Thus, gauge invariance can be used to cast limits on the V_{LL} and V_{RL} $t\ell\ell$ operators from B-decays [158] and from high- p_T di-lepton searches [105]: $\Lambda \gtrsim 1.5 - 2$ TeV for the $t\ell e$ and $t\ell\mu$ 4-Fermi V_{LL} and V_{RL} terms in Eq. 1, for natural $\mathcal{O}(1)$ corresponding Wilson coefficient, see also [27, 52].

A recent interesting search for top-quark production with additional leptons was performed by CMS in [118], and was used to constrain several types of dimension six operators involving the top-quark, including the 4-Fermi $t\ell\ell$ ones. The typical sensitivity that they obtained is

$\Lambda \gtrsim 500$ GeV for the scalar (with $S_{RR} = 1$) and vector (with $V_{ij} = 1$) $t\ell\ell$ operators in Eq. 1 and $\Lambda \gtrsim 1$ TeV for the tensor one (with $T_{RR} = 1$).

Finally, we have performed a re-interpretation of the recent ATLAS measurements of the 3ℓ and 4ℓ signals in [117] to obtain bounds on our $t\ell\ell$ 4-Fermi terms. In particular, we have applied the same set of selections and kinematic cuts that was used in this search to our NP signals in these multi-lepton categories, using MADGRAPH5_AMC@NLO [159] at LO parton-level as our events generator and DELPHES for detector simulation (see below for a detailed description of our simulated event samples). We then obtain the best sensitivity using their " 3ℓ , off-Z, $\cancel{E}_T > 50$ GeV" selection in the $m_{3\ell} > 600$ GeV bin, for which ATLAS obtained a 95% CL upper limit on the NP event yield of $N_{95}(\text{obs.}) = 14$ (see Table 5 in [160]). Thus, for example, our expected NP signal yield for the tensor operator with $\Lambda/\sqrt{T_{RR}} = 1$ TeV (i.e., after applying exactly the ATLAS set of cuts and selections and with $\mathcal{L} = 140 \text{ fb}^{-1}$), is $N_{NP}(\Lambda/\sqrt{T_{RR}} = 1 \text{ TeV}) = 20$, so that, in this case also, we obtain a bound of $\Lambda \gtrsim (20/14)^{1/4} \sim 1.1$ TeV for the tensor operator with $T_{RR} \sim 1$ and sub-TeV level bounds for the scale of the scalar and vector operators with natural $\mathcal{O}(1)$ couplings. Note that the NP effects which we study here (from the $t\ell\ell$ 4-Fermi operators) have not been considered in these recent CMS and ATLAS searches. Indeed, as we show below, a significantly better sensitivity to these $t\ell\ell$ 4-Fermi terms can be obtained from a search of the $pp \rightarrow t\bar{t}\ell^+\ell^-$ process with the di-, tri-lepton and four-leptons selections and with proper jets multiplicity selections, as well as dedicated selections on the minimum of the invariant mass of the hard di-leptons from the $t\ell\ell$ vertex.

V. SIGNAL AND BACKGROUND ANALYSIS

A. Calculation setup and numerical session

For the cross-sections of the multi-lepton processes in Eq. 3 we will use an $m_{\ell\ell}^{\text{min}}$ cumulative cross-section,

⁶ Note that the correlation between operators involving the top-quark and operators involving the b -quark should be taken with caution, since sign differences can lead to e.g., a cancellation of effects for operators involving b_L and an enhancement for those involving t_L (or vice-versa).

selecting events with $m_{\ell\ell}^{OSSF(nt)} > m_{\ell\ell}^{\min}$:

$$\sigma_{n\ell}^{\text{cum}} \equiv \int_{m_{\ell\ell}^{OSSF(nt)} \geq m_{\ell\ell}^{\min}} dm_{\ell\ell} \frac{d\sigma_{n\ell}}{dm_{\ell\ell}}, \quad (9)$$

where $m_{\ell\ell}^{OSSF(nt)}$ is the invariant mass of the "none-top" OSSF di-leptons of the underlying hard process, which are produced from the $t\ell\ell$ vertex and not from the top-quark decays (see also below), and $\sigma_{n\ell}$ is the cross-section of the n -leptons final state, e.g., $\sigma_{3\ell}$ corresponds to the tri-lepton signal. In particular, $m_{\ell\ell}^{\min}$ will be selected later on to optimize the sensitivity to the NP.

The generic form of the cumulative cross-section for the multi-leptons single-top and top-pair production processes, in the presence of the $t\ell\ell$ 4-Fermi operators, is:

$$\sigma_{n\ell}^{\text{cum}} = \sigma_{n\ell}^{\text{cum,SM}} + c^{\text{INT}} \cdot \sigma_{n\ell}^{\text{cum,INT}} + c^{\text{NP}} \cdot \sigma_{n\ell}^{\text{cum,NP}}, \quad (10)$$

where $\sigma_{n\ell}^{\text{cum,SM}}$, $\sigma_{n\ell}^{\text{cum,INT}}$ and $\sigma_{n\ell}^{\text{cum,NP}}$ are the cumulative SM, SM \times NP interference and NP² terms, respectively, and c^{INT} , c^{NP} are the corresponding dimensionless NP couplings, given by:

$$\begin{array}{ll} & c^{\text{INT}} & c^{\text{NP}} \\ \text{scalar} & 0 & S_{RR}^2/\Lambda_{\text{TeV}}^4, \\ \text{tensor} & 0 & T_{RR}^2/\Lambda_{\text{TeV}}^4, \\ \text{vector} & V_{ij}/\Lambda_{\text{TeV}}^2 & V_{ij}^2/\Lambda_{\text{TeV}}^4. \end{array} \quad (11)$$

In particular, no interference terms are generated for the scalar and tensor operators, while both constructive and destructive interference is possible for the vector operators (i.e., depending on the sign of V_{ij} in Eq. 1). As mentioned above, in the following we will study the sensitivity only to the S_{RR} , V_{RR} and T_{RR} 4-Fermi interactions; the sensitivity and reach for the other 4-Fermi vector currents, V_{LL} , V_{RL} and V_{LR} is similar to that of the V_{RR} operator. We recall that the scalar leptoquarks S_1 and R_2 can generate both S_{RR} and T_{RR} terms, while S_1 can also generate the V_{RR} term in Eq. 11. Also, as indicated in Table I, the vector leptoquark U_1 cannot generate any of the NP terms in Eq. 11.

B. Simulated Event Samples

All event samples were generated using MADGRAPH5_AMC@NLO [159] at LO parton-level and a dedicated universal FeynRules output (UFO) model for the EFT framework was produced using FEYNRULES [161]. The 5-flavor scheme was used for the generation of all samples, both signal and background, with the NNPDF30LO PDF set [162]. The default MADGRAPH5_AMC@NLO LO dynamical scale was used, which is the transverse mass calculated by a k_T -clustering of the final-state partons. The events were then interfaced with the PYTHIA 8 [163] parton shower. Events of different jet-multiplicities were matched us-

ing the MLM scheme [164] with the default MADGRAPH5_AMC@NLO parameters and all samples were processed through DELPHES 3 [165], which simulates the detector effects, applies simplified reconstruction algorithms and was used for the reconstruction of electrons, muons and hadronic jets.

For the leptons (electrons and muons) the reconstruction was based on transverse momentum (p_T)- and pseudo-rapidity (η)-dependent efficiency parametrization and an isolation from other energy-flow objects was applied in a cone of $\Delta R = 0.4$ with a minimum p_T requirement of 25 GeV for each lepton. Jets were reconstructed using the anti- k_t [166] clustering algorithm with radius parameter of $R = 0.4$ implemented in FastJet [167, 168], and were required to have transverse momentum of $p_T > 30$ GeV and pseudo-rapidity $|\eta| < 2.4$. In cases where a selection of a b -jet was used, the identification of b -tagged jets was done by applying a p_T -dependent weight based on the jet's associated flavor, and the MV2c20 tagging algorithm [169] in the 70% working point.

The dominant types of background processes were considered, depending on the number of leptons in the final state as well as the irreducible SM background from $pp \rightarrow t\bar{t}Z/\gamma^*$ for all channels. In particular, we found that the dominant background for the $(t\ell\ell)_{2\ell}$ sample is $pp \rightarrow t\bar{t}$ (where both top-quarks decay hadronically), for the $(t\ell\ell)_{3\ell}$ sample it is $pp \rightarrow WZ$ (where both vector-bosons decay leptonically) and for the $(t\ell\ell)_{4\ell}$ sample it is $pp \rightarrow ZZ$ followed by $ZZ \rightarrow 4\ell$ (see e.g., [117, 118]). All other SM backgrounds (e.g., Z +jets production in the case of the di-lepton signal and $t\bar{t}$ production in the tri-lepton channel as well as $t\bar{t}W$ for both the di- and tri-leptons channels) were found to be negligible given the selections of the analysis, as described next.⁷

C. Event selection and background

As noted before, in order to optimize the sensitivity to our $t\ell\ell$ 4-Fermi operators, we will isolate the NP signals in the 2ℓ , 3ℓ and 4ℓ categories using a set of selections which are summarized in Table II, for both the SM background and the NP signals. In particular, an important discriminating variable is the invariant mass of the "none-top" OSSF muon pair $m_{\ell\ell}^{OSSF(nt)}$, where the "none-top" leptons are selected to be the ones with the smallest angular separation between them, ΔR . As mentioned above, we then use a minimum value of $m_{\ell\ell}^{OSSF(nt)}$, noted as $m_{\ell\ell}^{\min}$, and select events only if $m_{\ell\ell}^{OSSF(nt)} \geq m_{\ell\ell}^{\min}$, see

⁷ We note that the background from the $t\bar{t}W$ channel is comparable to the SM irreducible background from $t\bar{t}Z$ in the case of the 3ℓ and 2ℓ signals. However, both the $t\bar{t}W$ and the $t\bar{t}Z$ backgrounds are much smaller than the leading WZ and $t\bar{t}$ ones for these channels.

also Eq. 9. For the tri-lepton and four-lepton channels, we also tested the invariant mass of all three and four leptons, respectively, as the discriminating variable, but found a reduced sensitivity to the NP in these cases, as can be seen from the lower plots of Fig. 3. This is because the leptons from the top-quark decay are considerably softer than the leptons from the "hard-process" (i.e., from the $t\bar{t}\mu\mu$ vertex), so that the invariant mass spectrum of all three or four-leptons is significantly milder and is, therefore, not as effective as the none-top di-muons for isolating the NP signal from the SM background.

Finally, as indicated in Table II, we require a minimum number of jets and b -tagged jets. For the 3ℓ and 4ℓ channels, we require at least two jets with at least one b -tagged jet; requiring a higher value of b -tagged jets in these samples was found to reduce the sensitivity due to selection efficiency effects. For the 2ℓ channel, we select at least three jets, with at least one b -tagged jet. Here, the selection of at least three jets was found to significantly reduce the di-leptonic $t\bar{t}$ background, while keeping a large fraction of the signal, as it involves a fully-hadronic top-pair decay.

TABLE II: Selections for the tri- and four-lepton events. $m_{\ell\ell}^{OSSF(nt)}$ refers to the invariant mass of the "none-top" OSSF muon pair, which are selected to be the OSSF di-muons with the smallest angular separation between them, ΔR . See also text.

Selection	2ℓ	3ℓ	4ℓ
Number of Leptons: exactly 2	exactly 3	exactly 4	
Jet multiplicity:	≥ 3	≥ 2	≥ 2
Number of b -jets:	≥ 1	≥ 1	≥ 1
$m_{\ell\ell}^{OSSF(nt)}$:	$> m_{\ell\ell}^{\min}$		

In Fig. 3 we plot the resulting di-, tri- and four-leptons event yields for the SM irreducible contribution and dominant backgrounds ($t\bar{t}$, WZ and ZZ , respectively), as well as for the NP contributions, i.e., from the interference and pure NP parts of the cross-sections (see Eqs. 10 and 11), after applying the jet selections of Table II and for an integrated luminosity of 3000 fb^{-1} . The event yields are plotted for the cumulative cross-section of Eq. 9, as a function of the lower cut on invariant mass of the none-top di-muons, $m_{\mu\mu}^{\min}$. To demonstrate the effectiveness of the lower cut selection on the invariant mass of the none-top di-muons, $m_{\mu\mu}^{\min}$, we also show in Fig. 3 the event yields in the tri- and four-leptons channels, as a function of the lower cut on the invariant mass of *all* 3-leptons and 4-leptons, respectively.

We see that in all multi-lepton channels the SM irreducible part and background sharply drop with $m_{\mu\mu}^{\min}$. In particular, we find that the SM cross-section is very sensitive to the $m_{\mu\mu}^{\min}$ selection, while the sensitivity of the various backgrounds (from $pp \rightarrow t\bar{t}$, WZ , ZZ) to the $m_{\mu\mu}^{\min}$ selection arises mainly due to our additional jet selections

of Table II.

D. Domain of validity of the EFT setup

The basic assumption underlying the EFT approach is that the mass of the lightest heavy particle from the underlying heavy theory is larger than Λ , so that none of these particles can be directly produced in the processes being investigated. This leads to the requirement $\Lambda^2 \gtrsim \hat{s}$, where $\sqrt{\hat{s}}$ is the center-of-mass energy of the hard process. Alternatively, it is required that the NP cross-sections do not violate tree-level unitarity bounds, which leads to similar constraints (for the case at hand the $tt\ell\ell$ 4-Fermi operators generate a cross-section that grows with energy $\sigma_{tt\ell\ell}^{\text{NP}} \propto \hat{s}$). These criteria, however, are not precise enough for our purposes for the following reasons:

- The 4-fermion operators that we consider can be generated either by a Z -like heavy particle coupling to lepton and quark pairs (*eg.* $t\bar{t} \rightarrow X \rightarrow \ell\ell$), or by a leptoquark coupling to quark-lepton pairs (*eg.* $t\ell \rightarrow \text{LQ} \rightarrow t\ell$). In the first case the EFT is applicable when $\Lambda > m_{\ell\ell}^{\max}$ and in the second case when $\Lambda > m_{t\ell}^{\max}$, where $m_{t\ell}$ is the invariant mass of the top-lepton pair from the $tt\ell\ell$ contact interaction.
- The constraints we derive will be on the effective scale $\Lambda_{\text{eff}} = \Lambda/\sqrt{f}$, whence the EFT applicability conditions become $\Lambda_{\text{eff}} > m_{\ell\ell}^{\max}/\sqrt{f}$ or $\Lambda_{\text{eff}} > m_{q\ell}^{\max}/\sqrt{f}$. Thus, the EFT approach remains applicable even for situations where Λ_{eff} is of the same order, or even somewhat smaller than $m_{q\ell}^{\max}$. This corresponds to NP scenarios with $f > 1$ (while still remaining perturbative). Note for example that applying the naive EFT validity criteria, $s < \Lambda_{\text{eff}}^2$, to the Fermi theory of weak interactions would give $s < (246 \text{ GeV})^2$ if $f = 1$, but in reality $f \sim 0.3$ and therefore $s \lesssim (100 \text{ GeV})^2$.

Based on this we can define the region of applicability by demanding $\Lambda > m_{\ell\ell}^{\max}$ or $\Lambda > m_{q\ell}^{\max}$, and allow Λ_{eff} to be smaller than $m_{q\ell}^{\max}$ by an $O(1)$ factor.

To close this section we note that dimension 8 operators that interfere with the SM also generate $\mathcal{O}(\Lambda^{-4})$ contributions to the $pp \rightarrow t\bar{t}\ell^+\ell^-$ cross section. These, however, can be ignored compared to the $\mathcal{O}(\Lambda^{-4})$ NP(dim.6) \times NP(dim.6) terms that we keep, because the SM amplitude is much suppressed for the high $m_{\ell\ell}^{\min}$ selections that we use (see below).

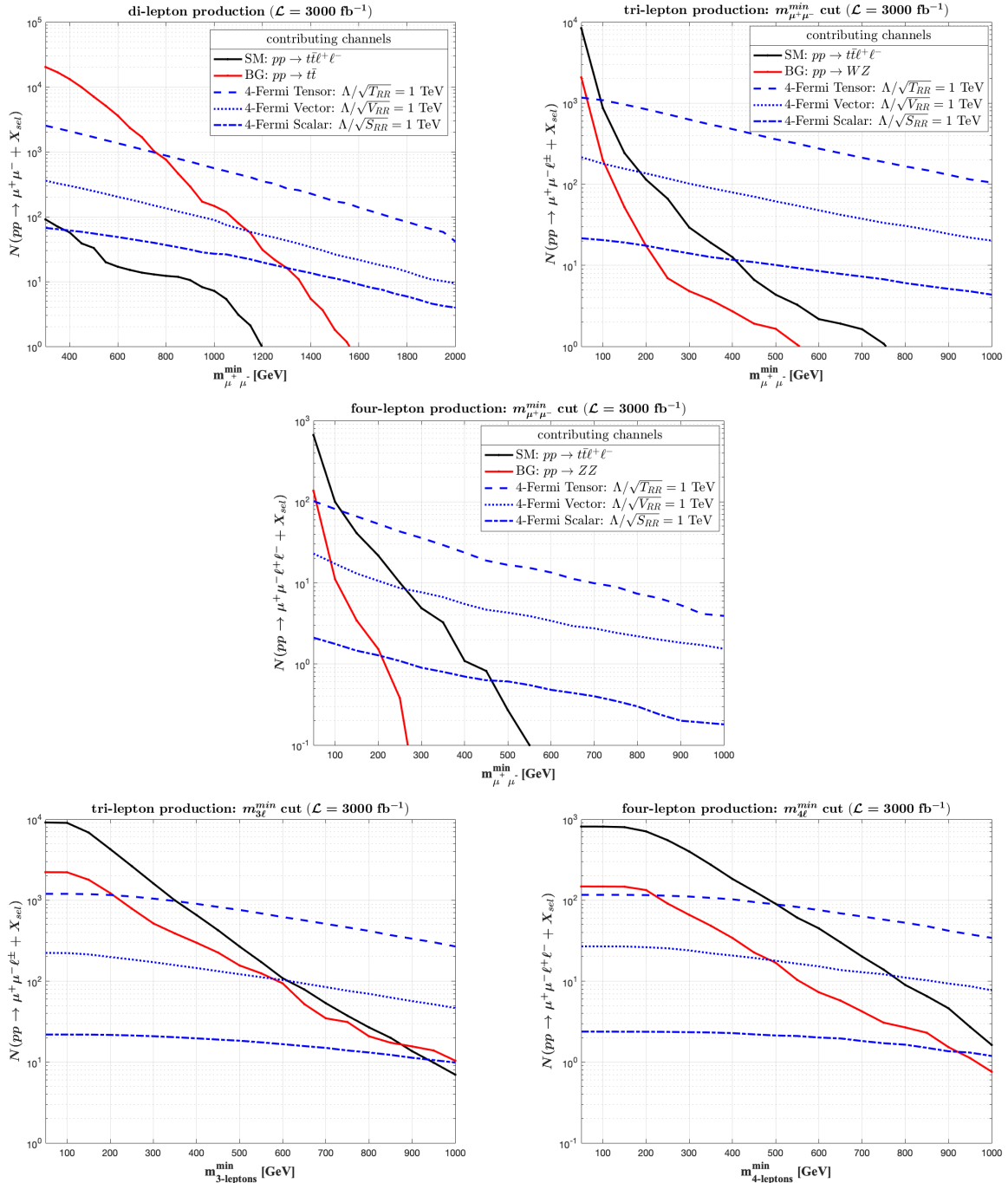


FIG. 3: Expected number of SM, NP and Background event yields for the di-, tri- and four-leptons signals at the HL-LHC with an integrated luminosity of $\mathcal{L} = 3000 \text{ fb}^{-1}$. The event yields are plotted as a function of the lower cut on the invariant mass of the none-top di-muon pair $m_{\mu^+\mu^-}^{\min}$ (upper plots) and as a function of the lower cut on the invariant mass of all leptons in the final state in the tri-lepton and four-leptons channels (lower plot), $m_{3\ell}^{\min}$ and $m_{4\ell}^{\min}$, respectively. The jet selections of Table II for each channel are applied. See also text.

VI. RESULTS

A. Cut-and-Count Study

The sensitivity to the $ttll$ 4-Fermi NP operators is estimated using a "cut and count" analysis, as described

below, for the di-lepton, tri-lepton and four-lepton signals. The methods used here are similar to the ones used in our previous works [56, 58]. For definiteness we will assume here that the NP couples only to muons, i.e. that the effect of the $tt\mu\mu$ operator dominates, but it should

be kept in mind that a similar analysis for NP which couples to electrons will only differ in selection efficiency and detector acceptance effects. If the NP is LFU and couples equally to both electrons and muons, then we expect a slightly improved sensitivity when applying our analysis to the corresponding final states containing both electrons and muons.

We calculate the expected Z -value, which is defined as the number of standard deviations from the background-only hypothesis given a signal yield and background uncertainty, using the `BinomialExpZ` function by `RootFit` [170]. We then find an optimized selection $m_{\mu^+\mu^-}^{\min}$ by maximizing the expected Z -value for each signal hypothesis, where at least one expected event was demanded for the signal. An example of the expected Z -value from the tri-lepton signal is plotted in Fig. 4, as a function of Λ for the case of the tensor $tt\mu\mu$ operator ($T_{RR} = 1$) and for several values of the relative overall background uncertainty, $\sigma_B = 25\%$, 50% and 100% , with the currently available integrated luminosity of 140 fb^{-1} . Clearly, the sensitivity to the NP depends on the relative uncertainty. Keeping that in mind, we analyze below all signal channels with a benchmark value of $\sigma_B = 25\%$ (see e.g., [56, 58]), assuming that the signal uncertainty is included within σ_B .

In order to set the expected bound on the scale of NP, we calculated the p -value for each signal and background hypothesis using the `BinomialExpP` function by `RootFit` [170]. In particular, we calculate the p -value of the background-only and background+signal hypotheses for each point and then perform a CL_s test [171] to determine the 95% Confidence Level (CL) exclusion values for Λ .

In Table III we summarize our results for the expected 95% CL bounds on the scale Λ of the scalar, vector and tensor $tt\mu\mu$ operators, with natural couplings of: $S_{RR} = 1$, $V_{RR} = \pm 1$ and $T_{RR} = 1$, respectively, and for three integrated luminosity scenarios of $\mathcal{L} = 140, 300$ and 3000 fb^{-1} , which correspond to the data collected so far, the data expected to be available at the end of Run-3, and the data expected to be recorded at the HL-LHC. We also depict in Fig. 5 the 95% CL bounds on the scale of the scalar, vector and tensor $tt\mu\mu$ operators, obtained via the tri-lepton channel at the HL-LHC with $\mathcal{L} = 3000 \text{ fb}^{-1}$, for the optimized $m_{\mu^+\mu^-}^{\min}$ selection which yields the best expected limit for this case, along with the $\pm 1\sigma$ and $\pm 2\sigma$ band.

Evidently, the optimized (best) $m_{\mu^+\mu^-}^{\min}$ selection is considerably milder in the tri- and four-lepton channels, since in these cases the signal rates are reduced (partly due to the smaller branching ratio for the top to decay to leptons). We also see that the sensitivity to the NP in the di- and tri-lepton channels is comparable with a slight advantage for the tri-lepton signal in the cases of the tensor and vector operators, where it is possible to reach a sensitivity of up to $\Lambda \sim 2(3) \text{ TeV}$ with $\mathcal{L} = 300(3000) \text{ fb}^{-1}$ for the tensor case and $\Lambda \sim 1.3(2) \text{ TeV}$ with $\mathcal{L} = 300(3000) \text{ fb}^{-1}$ for the vector case. Fi-

nally, notice the rather negligible sensitivity to interference term in the vector 4-Fermi case ($\sigma_{nl}^{\text{cum,INT}}$ in Eq. 10), which is due to our set of selections that are designed to minimize the SM contribution/amplitude.

Finally, we note that, in the di-lepton channel, the optimized $m_{\mu^+\mu^-}^{\min}$ values exceed Λ_{\min}/\sqrt{f} for $f \sim 1$, where $f = V_{RR}, S_{RR}, T_{RR}$ (see Table III). While this might still be within the validity regime of the EFT setup, as explained in section VD above, the results obtained in this channel may be "questionable" in that respect. Therefore, the better sensitivities that we obtain in the 3ℓ channel are also more reliable, since in this case (and also in the 4ℓ case) $m_{\mu^+\mu^-}^{\min} < \Lambda_{\min}$.

In the next section we will perform a sensitivity analysis which combines the information from all three channels, i.e., the di-, tri- and four-leptons channels and which focuses on LFUV signals of the $tt\mu\mu$ 4-Fermi operators.

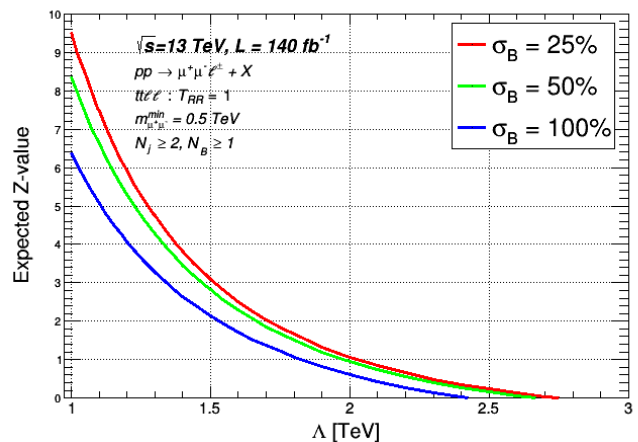


FIG. 4: Expected Z -value (defined as the number of standard deviations from the background-only hypothesis given a signal yield and background uncertainty) for the signal hypotheses varied with respect to the scale Λ of the $tt\mu\mu$ tensor operators with $T_{RR} = 1$, for a selection of three leptons with $m_{\mu^+\mu^-}^{\min} = 0.5 \text{ TeV}$ and an integrated luminosity of 140 fb^{-1} .

B. Ratio observables and LFUV

As mentioned earlier, the 4-Fermi operators of Eq. 1 may generate LFUV effects, in particular, asymmetric rates of the multi-lepton signals in Eq. 3 involving muons versus electrons, which are otherwise (i.e., within the SM) expected to be equal.

It is, therefore, useful to define generic LFU tests for multi-lepton production at the LHC, which are sensitive to the new $ttll$ 4-Fermi interactions and which can measure the differences between muons/electrons-asymmetric final states. For this purpose we define the

TABLE III: Expected maximum 95% CL sensitivity ranges to the scale Λ (denoted as $\Lambda_{\min}(95\% CL)$), of the $t\bar{t}\mu\mu$ 4-Fermi operator, obtained via the di-, tri- and four-leptons channels with the corresponding optimal $m_{\mu^+\mu^-}^{\min}$ selection. Results are shown for the 3 signal scenarios of each operator: $S_{RR} = 1, T_{RR} = 1, V_{RR} = \pm 1$. See also text.

	Jet Selections: $N_j \geq 3, N_b \geq 1$				Jet Selections: $N_j \geq 2, N_b \geq 1$			
	Final State	$pp \rightarrow \mu^+\mu^- + X$		$pp \rightarrow \mu^+\mu^-\ell^\pm + X$		$pp \rightarrow \mu^+\mu^-\ell^\pm\ell'^\mp + X$		
	Coupling	$m_{\mu^+\mu^-}^{\min}$ [GeV]	$\Lambda_{\min}(95\% CL)$ [TeV]	$m_{\mu^+\mu^-}^{\min}$ [GeV]	$\Lambda_{\min}(95\% CL)$ [TeV]	$m_{\mu^+\mu^-}^{\min}$ [GeV]	$\Lambda_{\min}(95\% CL)$ [TeV]	
$\mathcal{L} = 140 \text{ fb}^{-1}$	$S_{RR} = 1$		0.8		0.7		0.4	
	$T_{RR} = 1$	1400	1.6	500	1.8	300	1.0	
	$V_{RR} = 1(-1)$		1.0 (1.0)		1.1 (1.1)		0.7 (0.7)	
$\mathcal{L} = 300 \text{ fb}^{-1}$	$S_{RR} = 1$		0.9		0.8		0.5	
	$T_{RR} = 1$	1400	1.8	500	2.0	300	1.1	
	$V_{RR} = 1(-1)$		1.1(1.1)		1.3(1.2)		0.8(0.7)	
$\mathcal{L} = 3000 \text{ fb}^{-1}$	$S_{RR} = 1$		1.4		1.3		0.8	
	$T_{RR} = 1$	1600	2.8	800	2.9	500	1.8	
	$V_{RR} = 1(-1)$		1.8(1.7)		2.0(1.9)		1.3(1.2)	

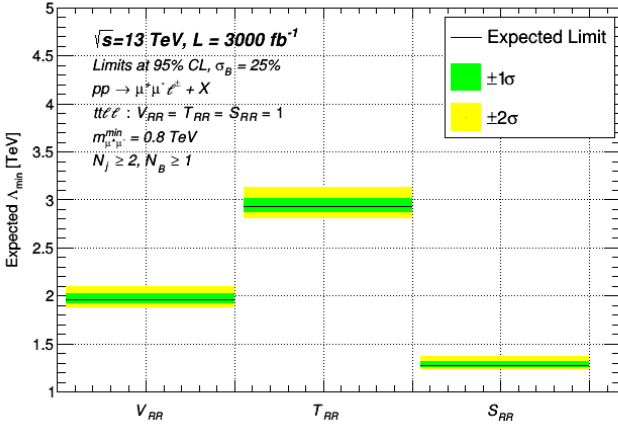


FIG. 5: Expected 95% CL upper limit on Λ , $\Lambda_{\min}(95\% CL)$, of the $t\bar{t}\mu\mu$ operator for 3 signal scenarios: $S_{RR} = 1, T_{RR} = 1$ and $V_{RR} = 1$, with a selection of three leptons, what a total integrated luminosity of 3000 fb^{-1} and with the optimized $m_{\mu^+\mu^-}^{\min} > 0.8 \text{ TeV}$ selection (see also Table III). For all cases the overall uncertainty is chosen to be 25% at 1σ , as explained in the text.

following ratio observables of cross-sections:

$$R_{\mu/e}^{2l} = \frac{\sigma(pp \rightarrow \mu^+\mu^- + X)}{\sigma(pp \rightarrow e^+e^- + X)}, \quad (12)$$

$$R_{\mu/e}^{3l} = \frac{\sum_{\ell=e,\mu} \sigma(pp \rightarrow \ell^\pm\mu^+\mu^- + X)}{\sum_{\ell=e,\mu} \sigma(pp \rightarrow \ell^\pm e^+e^- + X)}, \quad (13)$$

$$R_{\mu/e}^{4l} = \frac{\sum_{\ell,\ell'=e,\mu} \sigma(pp \rightarrow \ell^\pm\ell'^\mp\mu^+\mu^- + X)}{\sum_{\ell=e,\mu} \sigma(pp \rightarrow \ell^\pm\ell'^\mp e^+e^- + X)}, \quad (14)$$

where $\ell, \ell' = e, \mu$ and X contains the accompanied jets and missing energy, which depends on the various underlying processes that contribute to these ratios. As

described above, X is different for the NP signals and for the background and this will be used here also by applying the channel-dependent jet selections of Table II on X and using, as well, a lower cut on the invariant mass of the "none-top" OSSF di-leptons to further isolate the signals from the background, as described below.

These ratio observables are particularly useful and reliable probes of LFUV NP, since they potentially minimize the effects of the theoretical uncertainties involved in the calculation of the corresponding cross-sections (see e.g., [57]) as well as the experimental systematic uncertainties.⁸ In particular, the new $t\bar{t}\mu\mu$ 4-Fermi terms contribute only to the numerators of the ratios in Eq. 12, Eq. 13 and Eq. 14, thus leading to $R_{\mu/e}^{nl} \neq 1$. On the other hand in the SM, deviations from unity for all these ratio observables, e.g., through the non-universal Higgs-lepton Yukawa couplings to leptons, are much smaller than the expected experimental accuracy – as is the case, *in particular*, for high p_T events which are our primary interest in this work. Effects of non-universal reconstruction efficiencies and acceptance for the different leptonic final states will be included in the overall uncertainty assumed below for the measurement of $R_{\mu/e}^{nl}$ in Eq. 12 - Eq. 14.

For each ratio observable in Eq. 12 - Eq. 14 we have (this holds also in the case of NP scenarios that are universal in lepton flavors)

$$R_{\mu/e}^{nl} \sim 1 + \delta(\Lambda), \quad (15)$$

where the NP effect is contained in $\delta(\Lambda)$ and, using the

⁸ Lepton flavor independent uncertainties from NLO QCD effects, loop corrections from EFT operators (see e.g., [172]) as well as PDF uncertainties are expected to be canceled to a large extent in such ratio observables. Even so, the impact of the theoretical uncertainties is accounted for in our analysis, as a part of the total overall uncertainties that we consider below.

cumulative cross-section of Eq. 10, we have:

$$\delta(\Lambda) \propto \frac{c^{\text{INT}} \cdot \sigma_{nl}^{\text{INT}} + c^{\text{NP}} \cdot \sigma_{nl}^{\text{NP}}}{\sigma_{nl}^{\text{SM}}}, \quad (16)$$

where c^{INT} and c^{NP} are the NP couplings of the interference and NP² terms, respectively, as given in Eq. 11.

To study the sensitivity to the potential LFUV signal we then define the following χ^2 -like test (dropping the subscript μ/e hear after):

$$\chi^2 = \sum_{n=2,3,4} \frac{[R^{nl}(\Lambda) - R^{nl}(\text{exp})]^2}{(\delta R^{nl})^2}, \quad (17)$$

where $R^{nl}(\text{exp})$ is the expected experimental measured value of the ratio (see discussion below) and δR^{nl} denotes the corresponding overall (experimental plus theoretical) statistic + systematic 1σ uncertainty.

Then, based on the expectation from the corresponding irreducible SM + background cross-sections (i.e., assuming no NP in the data), we use in our χ^2 -like test a lower cut ($m_{\ell\ell}^{\text{min}}$) on the invariant mass of the "none-top" OSSF di-leptons, i.e., $m_{\ell+\ell^-}^{\text{OSSF}(nt)} > m_{\ell\ell}^{\text{min}}$, that ensures at least five event in each channel for a given luminosity, e.g., $(\sigma^{\text{SM}} + \sigma^{\text{WZ}}) \cdot \mathcal{L} > 5$ in the tri-lepton case. The resulting channel and luminosity dependent $m_{\ell\ell}^{\text{min}}$ cuts are listed in Table IV.

TABLE IV: The luminosity and channel dependent $m_{\ell\ell}^{\text{min}}$ selections on the invariant mass of the "none-top" OSSF di-lepton, i.e., $m_{\ell\ell}^{\text{OSSF}(nt)} > m_{\ell\ell}^{\text{min}}$, that were used in the χ^2 -like test of Eq. 17, for the different multi-lepton channels. See also text.

\mathcal{L} [fb ⁻¹]	$m_{\ell\ell}^{\text{min}}$ [GeV]		
	2 ℓ	3 ℓ	4 ℓ
140	1000	200	100
300	1100	200	100
3000	1400	500	300

For the purpose of extracting a bound on Λ we assume that, on average, no NP is observed. In this case we expect the experimental values $R^{nl}(\text{exp})$ to be normally distributed with unit mean and standard deviation δR^{nl} . Thus, if $\mathcal{P}_{\text{exp}}^{3l}$ denotes the probability distribution function (PDF) for $R^{nl}(\text{exp})$, then

$$\mathcal{P}_{\text{exp}}^{nl} = \mathcal{N}\left(1, (\delta R^{nl})^2\right), \quad (18)$$

where $\mathcal{N}(a, s^2)$ denotes the normal distribution for average a and standard deviation s .

We don't know the actual uncertainties of the experiment and we, therefore, choose two potentially realistic benchmark values for the overall uncertainties δR^{nl} of the data samples (see e.g., [94]): $\delta R^{nl} = 15\%, 25\%$ for all channels, i.e., assuming for simplicity a common overall uncertainty in the di-, tri- and four-leptons ra-

tios. We assume that these benchmark uncertainties account for both the experimental and the theoretical systematic uncertainties, where the latter is expected to be minimized due to the use of ratio observables (see also discussion above). Moreover, we assume in Eq. 17 that the systematic uncertainties in each channel are uncorrelated, since the information about the correlation matrix of the uncertainties is not yet available for the measurements/channels used in our χ^2 -like test.⁹

The expected bounds on Λ are then obtained by first generating $O(10^4)$ values of $R^{nl}(\text{exp})$ distributed according to $\mathcal{P}_{\text{exp}}^{nl}$ in Eq. 18. Then, for each of these $O(10^4)$ realizations of $R^{nl}(\text{exp})$ we determine the value of Λ that minimizes χ^2 in Eq. 17, which we denote as Λ_{min} ; the distribution of the Λ_{min} is also expected to be Gaussian, an example is shown in Fig. 6. Finally, the expected bounds on Λ are extracted from this Gaussian distribution of Λ_{min} . The resulting bounds on the scale of the scalar, vector and tensor 4-Fermi operators are given in Table V for three LHC integrated luminosity scenarios: $\mathcal{L} = 140, 300, 3000$ fb⁻¹, corresponding to the currently accumulated LHC luminosity, the RUN-3 projections and the planned HL-LHC luminosity, respectively. We see that the sensitivity obtained on the scale of the $t\mu\mu$ 4-Fermi operators using our LFUV χ^2 -like test NP is slightly better than those obtained using the "cut and count" method of the previous chapter; this is because the χ^2 -like test of Eq. 17 is using all the three multi-lepton channels, thus exploiting the fact that these channels are theoretically correlated, i.e., that the NP signals in the di-, tri- and four-leptons channels that we considered are sourced from the same underlying heavy physics - same 4-Fermi operator.

⁹ In the general case, where the correlation matrix for the systematic uncertainties is provided, the χ^2 -test reads instead: $\chi^2 = \sum_{ij} (R^{nl}(\Lambda) - R^{nl}(\text{exp})) \sigma_{nm}^{-2} (R^{ml}(\Lambda) - R^{ml}(\text{exp}))$, where n, m denote the different multi-lepton channels, $\sigma_{nm}^{-2} = (\delta R^{nl} \rho^{nm} \delta R^{ml})^{-1}$ and ρ^{nm} is the correlation matrix provided by the experiment. Correlations among the systematic uncertainties in the various channels used below will degrade the sensitivity to the NP, since they effectively reduce the number of observables/channels.

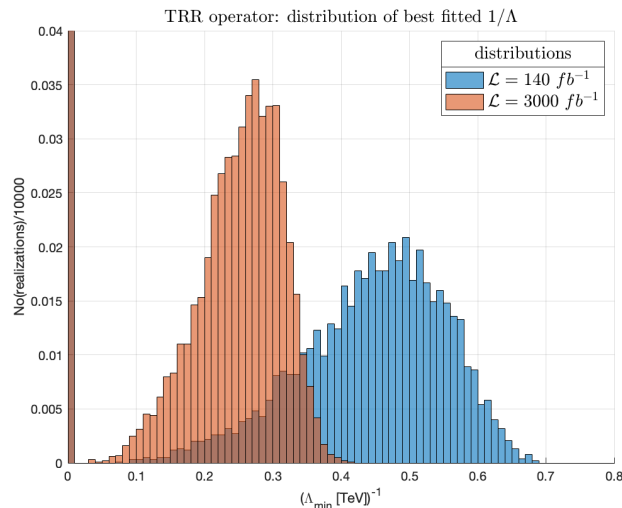


FIG. 6: An example of the normalized distribution of the inverse value for the best fitted Λ of the T_{RR} tensor operator, that minimizes the χ^2 -like test. The distributions are given for the cases $\mathcal{L} = 140$ and 3000 fb^{-1} and for $\delta R^{n\ell} = 50\%$. See also text.

TABLE V: Expected bounds on the scale of the 4-Fermi $tt\mu\mu$ with $S_{RR} = 1, T_{RR} = 1, V_{RR} = \pm 1$, obtained from the χ^2 -like test of Eq. 17, using the ratios $R_{\mu/e}^{n\ell}$ ($n = 2, 3, 4$) of Eqs. 12 - 14 for the di-, tri- and four-leptons signals. Results are shown for integrated luminosities of $\mathcal{L} = 140, 300$ and 3000 fb^{-1} and for two choices of the overall uncertainty $\delta R^{n\ell} = 15\%$ and $\delta R^{n\ell} = 25\%$, assuming a common uncertainty for all channels $n = 2, 3, 4$. See also text.

\mathcal{L} [fb^{-1}]	95% bounds on Λ [TeV]		
	NP \Downarrow	$\delta R^{n\ell} = 25\%$	$\delta R^{n\ell} = 15\%$
140	$S_{RR} = 1$	0.9	1
	$T_{RR} = 1$	2.1	2.3
	$V_{RR} = 1(-1)$	1.3(1.2)	1.6(1.3)
300	$S_{RR} = 1$	0.9	1.1
	$T_{RR} = 1$	2.2	2.4
	$V_{RR} = 1(-1)$	1.4(1.2)	1.6(1.4)
3000	$S_{RR} = 1$	1.7	1.9
	$T_{RR} = 1$	3.7	4.2
	$V_{RR} = 1(-1)$	2.5(2.2)	2.9(2.4)

VII. SUMMARY

We have studied the effects of new 4-Fermi $ttll$ flavor diagonal interactions, which can be generated from

different types of underlying heavy physics containing e.g. heavy scalars and/or vectors. We showed that these higher-dimensional $ttll$ contact interactions can lead to new high- p_T events of opposite-sign same-flavor (OSSF) di-leptons in multi-lepton production accompanied by high jet-multiplicity at the LHC, in the di-, tri- and four-lepton channels: $pp \rightarrow t\bar{t}\ell^+\ell^- \rightarrow n \cdot \ell + m \cdot j_b + p \cdot j + \cancel{E}_T$, where $n = 2, 3, 4$, $m = 1, 2$, $p = 1 - 4$ and $j(j_b) = \text{light}(b)$ -jet.

We have studied in some detail the SM background to these multi-leptons signatures and showed that a very efficient separation between the NP signals and the background can be obtained with an optimal jet-multiplicity selection and, in addition, a selection of events with high invariant mass of the OSSF di-leptons, e.g., $m_{\ell^+\ell^-}^{\text{min}}(\text{OSSF}) > 500(1500) \text{ TeV}$ in the tri-lepton(di-lepton) channels at the LHC RUN3 with $\mathcal{L} = 300 \text{ fb}^{-1}$.

We have shown that the current bounds on the scales of the tensor $ttll$ operator, $\Lambda(\text{tensor}) \gtrsim 1 \text{ TeV}$, and the scalar and vector ones, $\Lambda(\text{scalar/vector}) \gtrsim 0.5 \text{ TeV}$, can be improved by a factor of 2-3, using our "cut and count" analysis. For example, 95% CL bounds of $\Lambda \gtrsim 1.8(1.1) \text{ TeV}$ are expected on the scale of a tensor (vector) $tt\mu\mu$ interaction, already with the current $\sim 140 \text{ fb}^{-1}$ of LHC data, via the tri-lepton $pp \rightarrow \ell^\pm\mu^+\mu^- + 2 \cdot j_b + 2 \cdot j + \cancel{E}_T$ signal; this is an improvement by a factor of ~ 2 with respect to the current bounds on these operators. The expected reach at the HL-LHC with 3000 fb^{-1} of data is $\Lambda \gtrsim 3(2) \text{ TeV}$ for the tensor (vector) $ttll$ operators.

We furthermore explored potential searches for lepton flavor universal universality violation (LFUV) effects from the higher dimensional $ttll$ 4-Fermi operators, that can be detected via our multi-lepton signals. In particular, we have defined ratio observables for all three di-, tri- and four-lepton channels, which can be used to search for new LFUV effects via a χ^2 -like test that exploits the theoretical correlation between the LFUV signals in these three multi-lepton channels. We find that the sensitivity to the scale of the LFUV $ttll$ operators is comparable to that obtained with the "cut and count" search, using our χ^2 -like test. For example, it is possible to obtain 95% CL bounds on the LFUV tensor $ttll$ interactions of $\Lambda \gtrsim 2 \text{ TeV}$ with the current LHC data of $\mathcal{L} = 140 \text{ fb}^{-1}$ and of $\Lambda \gtrsim 3.5 \text{ TeV}$ at the HL-LHC with 3000 fb^{-1} .

Finally, we believe that the sensitivity obtained in this paper to the new $ttll$ 4-Fermi operators using the di-, tri- and four-leptons signals from the underlying $pp \rightarrow t\bar{t}\ell^+\ell^-$ process, can be improved with further optimization of the selections that isolate the NP signals in these channels from the SM background.

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Appendix A: Cut-flow tables

We present below cut-flow tables of the number of events for the signals and the dominant backgrounds considered in this work, in the di-, tri- and four-lepton channels, in Tables VI, VII, VIII.

In all cases we assume an integrated luminosity of $\mathcal{L} = 300 \text{ fb}^{-1}$ and start with a baseline value of $m_{\mu^+\mu^-}^{\text{min}} = 300 \text{ GeV}$ for the di-muon invariant mass lower cut. Then, for each case we list the number of events after imposing the optimal di-muon invariant mass lower cut and the chosen jet selections (see main text for further details).

Cuts	Background Events		Signal Events		
	$t\bar{t}Z$ (irreducible)	$t\bar{t}$	$T_{RR} = 1$	$V_{RR} = 1$ (-1)	$S_{RR} = 1$
$m_{\mu^+\mu^-}^{\text{min}} = 300 \text{ GeV}$	9.1	6221.4	379.0	44.7 (33.4)	9.2
$m_{\mu^+\mu^-}^{\text{min}} = 1400 \text{ GeV}$	0.0	1.1	36.8	4.4 (4.2)	2.0
$N_j \geq 3, N_b \geq 1$	0.0	0.5	22.7	3.4 (3.3)	1.4

TABLE VI: Cut-flow table for the selection of 2 leptons. The number of events appears after each selection is for an integrated luminosity of $\mathcal{L} = 300 \text{ fb}^{-1}$.

Cuts	Background Events		Signal Events		
	$t\bar{t}Z$ (irreducible)	WZ	$T_{RR} = 1$	$V_{RR} = 1$ (-1)	$S_{RR} = 1$
$m_{\mu^+\mu^-}^{\text{min}} = 300 \text{ GeV}$	4.8	45.5	91.4	13.5 (10.2)	2.1
$m_{\mu^+\mu^-}^{\text{min}} = 500 \text{ GeV}$	0.8	12.5	52.4	8.2 (7.1)	1.5
$N_j \geq 2, N_b \geq 1$	0.4	0.2	35.8	6.1 (5.4)	1.1

TABLE VII: Cut-flow table for the selection of 3 leptons. The number of events appears after each selection is for an integrated luminosity of $\mathcal{L} = 300 \text{ fb}^{-1}$.

Cuts	Background Events		Signal Events		
	$t\bar{t}Z$ (irreducible)	ZZ	$T_{RR} = 1$	$V_{RR} = 1$ (-1)	$S_{RR} = 1$
$m_{\mu^+\mu^-}^{\text{min}} = 300 \text{ GeV}$	0.8	3.5	5.7	1.2 (0.9)	0.2
$N_j \geq 2, N_b \geq 1$	0.0	0.0	3.6	0.8 (0.6)	0.1

TABLE VIII: Cut-flow table for the selection of 4 leptons. The number of events appears after each selection is for an integrated luminosity of $\mathcal{L} = 300 \text{ fb}^{-1}$.