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One of the important goals at the future e^+e^- colliders is to measure the top-quark mass and width in a scan of the pair production threshold. Presented in this work is the most general approach to the top-quark mass determination from the threshold scan at CLIC, with all relevant model parameters and selected systematic uncertainties included in the fit procedure. In the baseline scan scenario the top-quark mass can be extracted with precision of the order of 30 to 40 MeV, already for 100 fb^{-1} of data collected at the threshold. We present the optimisation procedure based on the genetic algorithm with which the statistical uncertainty of the mass measurement can be reduced by about 20%.

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Top-quark mass determination in the optimised threshold scan

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Abstract

One of the important goals at the future e^+e^- colliders is to measure the top-quark mass and width in a scan of the pair production threshold. Presented in this work is the most general approach to the top-quark mass determination from the threshold scan at CLIC, with all relevant model parameters and selected systematic uncertainties included in the fit procedure. In the baseline scan scenario the top-quark mass can be extracted with precision of the order of 30 to 40 MeV, already for 100 fb^{-1} of data collected at the threshold. We present the optimisation procedure based on the genetic algorithm with which the statistical uncertainty of the mass measurement can be reduced by about 20%.

1 Introduction

The threshold scan is expected to be the most precise way to measure the top-quark mass. However, the threshold cross-section shape depends not only on the top-quark mass and width but also on other model parameters, such as the top Yukawa coupling and the strong coupling constant. It can also be affected by many systematic effects. Dedicated fit procedures have been developed for the top-quark threshold scan analysis at CLIC [1,2]. The new fit procedure is more flexible than the one used in the previous study [3] and allows to include all relevant model parameters as well as additional constraints on model parameters, coming e.g. from earlier measurements, and constraints on data normalisation.

At the first energy stage, CLIC running is assumed to include a dedicated scan of the $t\bar{t}$ threshold with total integrated luminosity of 100 fb^{-1} . The baseline scenario of the threshold scan assumes running at 10 equidistant energy points taking 10 fb^{-1} of data for each value of collision energy. This running scenario seems to be conservative and the aim of the presented study was to investigate to what extent statistical uncertainties can be reduced when using the optimised running scenario. The scan optimisation assumes that the top-quark mass is already known to $O(100 \text{ MeV})$.

2 Genetic algorithm

When looking for the best scenario of the top-quark threshold scan at CLIC (or at any other future e^+e^- collider) one needs to take into account many different aspects of the measurement.

The top quark mass is just one of the parameters that are to be constrained from the collected data (with the best possible statistical uncertainty). There are other model parameters, measurement of which needs to be optimised at the same time. In a Genetic algorithm, a set of proposed solutions to an optimisation problem, called *Individuals*, is evolved towards better solutions. Each Individual has a defined set of properties, called *genotype*, which can be mutated and altered, and a set of measurable traits, called *phenotype*, that are determined by the genotype. Phenotype consists of traits that are used to evaluate their performance and choose the best Individuals to the next generation. During consecutive iterations of the algorithm, population evolves towards better solutions. Ultimately, after a finite number of iterations, the population should converge to an optimal solution. We decided to use the Non dominated sorting genetic algorithm II, proposed by Kalyanmoy Deb in 2002. Thanks to the use of an efficient non dominated sorting algorithm it was possible to lower the time complexity from original $O(MN^2)$ [4] to $O(MN \log^{M-1} N)$ [5], where M is number of objectives and N is the size of the population. For more details refer to [2].

3 NSGA-II set-up

One scan scenario was assumed as an Individual, which genotype is represented by a scan sequence, set of centre-of-mass energy points. Each scan point can be considered a chromosome. Constant total integrated luminosity of 100 fb^{-1} was assumed and it is equally distributed among all scan points. An initial population was created from the baseline scenario assuming ten scan points equally separated from each other by 1 GeV, starting at 340 GeV. This scenario was studied in detailed in [2, 3]. The population size is set to 2000 and number of generations to 30. All results presented here were calculated assuming normalisation uncertainty of $\Delta = 0.1\%$, strong coupling constant uncertainty of $\sigma_{\alpha_s} = 0.001$ and background level uncertainty of $\sigma_{f_{bg}} = 2\%$. When measurement of the top Yukawa coupling was not included in the optimisation objectives, an uncertainty of $\sigma_{y_t} = 0.1$ was assumed. In order to rule out results that could be not representative of Individual's performance, each uncertainty was computed three times and the worst result was chosen.

4 Optimisation

Described in this contribution are the results of the two objective optimisation procedures, optimised for top-quark mass and width or mass and Yukawa coupling measurements. For results of single objective optimisation please refer to [2].

When considering scan optimisation for the mass-width pair, an improvement of around 20-25% could be observed in the final generation for both parameters. For the top-quark mass the uncertainty was reduced from 32 MeV to 26 MeV, while for the width, from 58 MeV to 44 MeV (see Fig 1). If we look at the histogram of measurement points from the last generation (see Fig 1) we can clearly observe three distinct regions on the threshold. One below, one in the middle and one above the threshold. We conclude that cross section measurements in those regions are most sensitive to the two considered model parameters, mass and width.

When optimizing the threshold scan procedure for mass and Yukawa coupling measurements, we can observe a similar behaviour. The mass uncertainty changes from 32 MeV to 28 MeV, while the Yukawa coupling uncertainty changes from 0.18 to 0.16. The very small improvement for the Yukawa coupling can be explained, when we look at Fig. 2. On the left plot we can clearly see an additional region above the threshold, which is responsible for the determination of the Yukawa coupling. The benchmark scenario from the initial generation

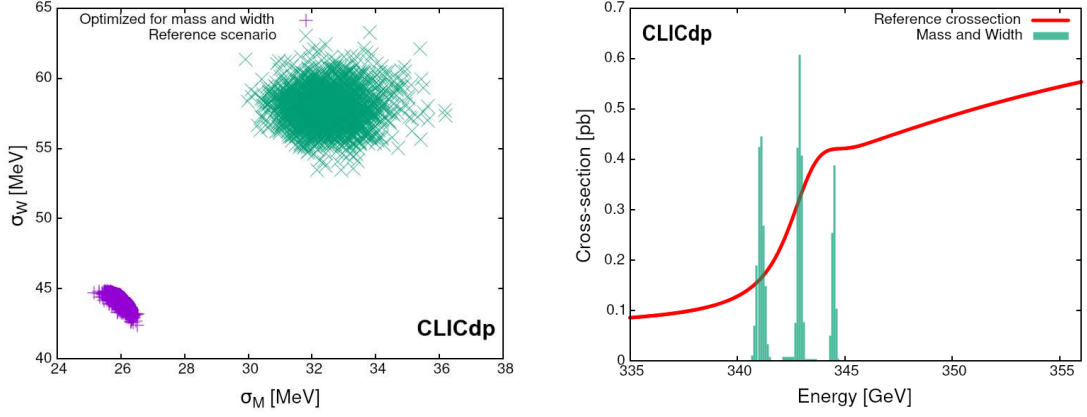


Figure 1: Left: mass and width uncertainty distribution in the first (green) and the last (blue) generation for scan optimised for mass and width determination. Right: distribution of the measurement points from the last generation (arbitrary scale) compared with the reference cross section template.

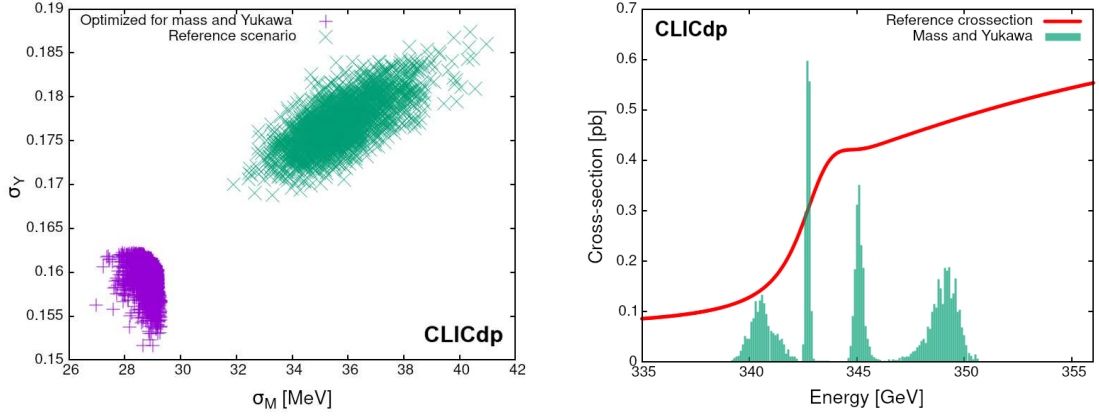


Figure 2: As in Fig. 1 but for scan optimised for mass and Yukawa coupling determination.

has half of its points in this region, not making significant improvement possible.

5 Optimised scan scenarios

To verify the optimisation results we select one test scenario from the final generation for each of the two considered optimisation configurations (See Fig. 3). The algorithm converged well in both cases. For mass and width optimisation 99% of final generation scenarios had 5 scan points, while for mass and Yukawa 97% of them had 9 or 10 scan points. To confirm optimisation results we generated 20 000 pseudo-experiments using selected running scenarios.

Results obtained with a large number of pseudo-experiments confirm estimates from the optimisation procedure (where each scenario was evaluated based on three pseudo-data sets only). For the optimised mass-width scenario the average expected mass uncertainty is around 26 MeV, while for width it is around 44 MeV, see Fig. 4. Furthermore, uncertainty distributions are narrower than those for the reference scenario confirming that the fit is very stable and less sensitive to the statistical fluctuations, which is the result of including three pseudo-experiments for each Individual.

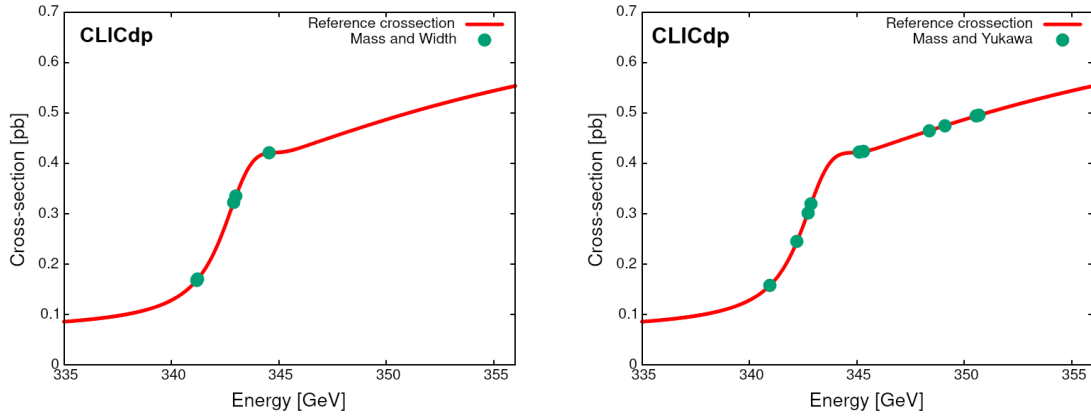


Figure 3: Scan energy points for the “best scenarios” taken from the last generation compared with the reference cross section template: (left) 5 point scenario optimised for mass and width determination precision (two points below, two in the middle and one above the threshold) and (right) 10 point scenario optimised for mass and Yukawa coupling determination precision.

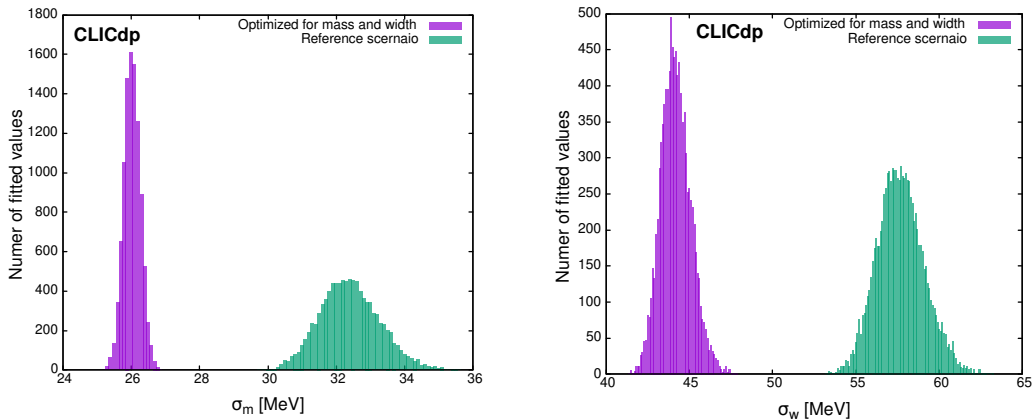


Figure 4: Uncertainty distribution for mass (left) and width (right) measurement, for five-point scan scenario optimised for mass and width measurement (see Fig. 3), compared with the distributions for the reference scenario.

For scenario optimised for mass and Yukawa coupling measurement, results obtained from 20 000 of pseudo-experiments, shown in Fig. 5 are again in good agreement with optimisation results (see Fig. 2). However, uncertainty distribution for the mass measurement is significantly wider than the one obtained for mass and width optimised scenario (Fig. 4). It is also slightly asymmetric, with a larger tail towards high uncertainty values. Nevertheless, the optimised scenario provides better mass measurement precision than the reference one in every case.

6 Conclusions

An optimisation procedure using a non-dominated sorting genetic algorithm II has been applied to the top-quark pair-production threshold scan. Each measurement scenario (set of energy points with total equally distributed luminosity of 100 fb^{-1}) is considered a genotype and results of the fit procedure constitute a phenotype. Starting from the benchmark scenario

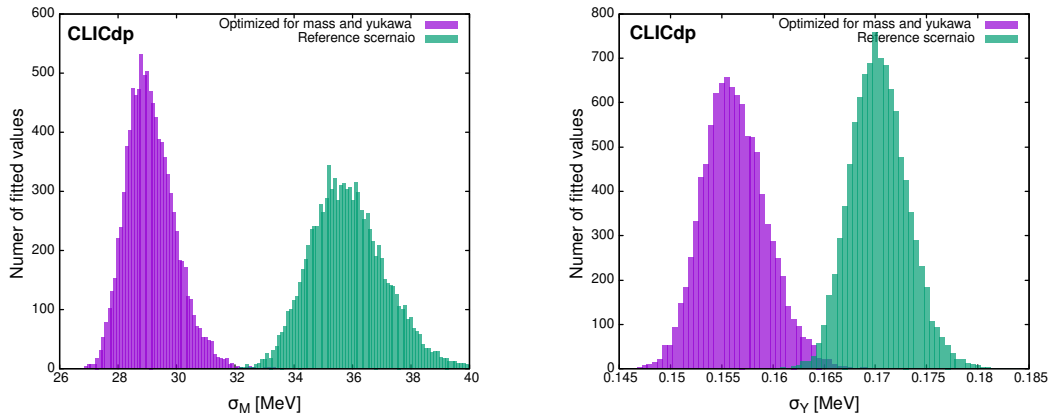


Figure 5: Uncertainty distribution for mass (left) and Yukawa coupling (right) measurement, for 8 point scan scenario optimised for mass and Yukawa coupling measurement (see Fig. 3), compared with the distributions for the reference scenario.

(10 scan points, equally separated from each other), stable optimisation results are obtained from the genetic evolution for 30 generations and population size of 2000. By using this optimisation procedure, it was shown that it is possible to reduce the top-quark mass uncertainty by up to 20%, without increase of luminosity or loss of precision in determination of other parameters.

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