

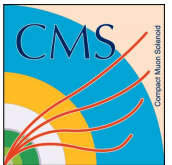
Jet fragmentation and substructure at the LHC

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for the ATLAS & CMS collaborations

PANIC 2021, 8 September 2021



University
of Glasgow



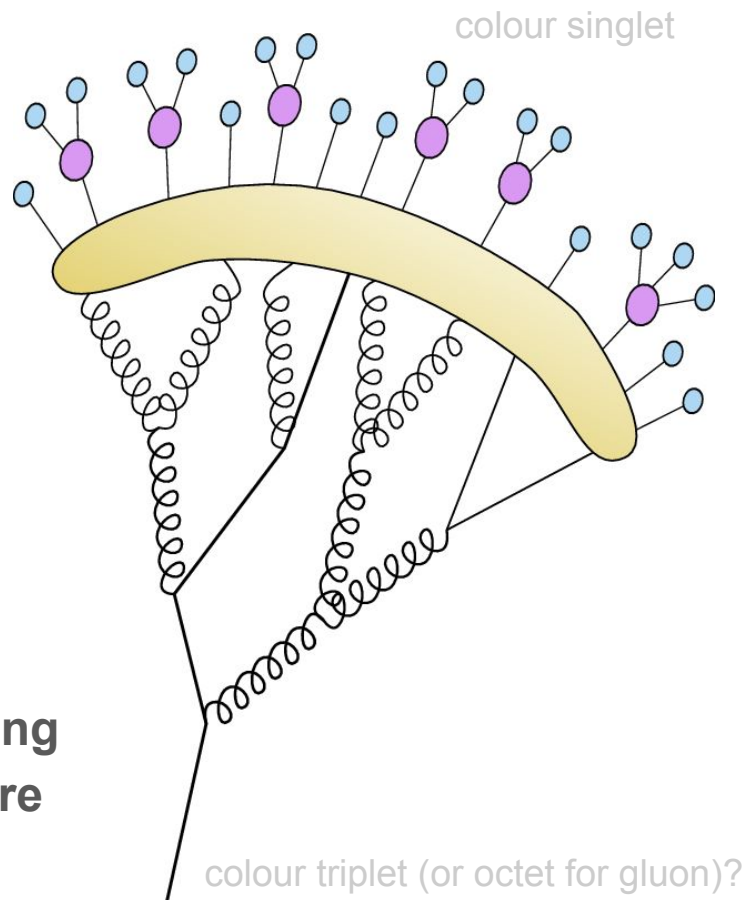
Jet fragmentation

In fixed-order QCD, well-separated jets and partons are exactly equivalent

Broken by evolution from fixed-order to “real” jets, including both perturbative QCD radiation and non-perturbative hadronisation

Collectively this process can be considered as the *fragmentation* of a parton into the multi-hadron spray of a particle-level jet

Measuring jet fragmentation \Rightarrow understanding the emergence of jet structure from a mixture of parton flavours and configurations



Light-jet fragmentation

Earlier jet fragmentation measurements

Previous LHC measurements of jet fragmentation:

Eur. Phys. J. C 76 (2016) 322 — Measurement of the charged-particle multiplicity inside jets from $\sqrt{s} = 8$ TeV pp collisions with the ATLAS detector [arXiv:1602.00988](#)

Phys. Rev. D 93 (2016) 052003 — Measurement of jet charge in dijet events from $\sqrt{s}=8$ TeV pp collisions with the ATLAS detector, [arXiv:1509.05190](#)

Eur. Phys. J. C 71 (2011) 1795 — Measurement of the jet fragmentation function and transverse profile in proton-proton collisions at a center-of-mass energy of 7 TeV with the ATLAS detector, [arXiv:1109.5816](#)

Phys.Rev.D 83 (2011) 052003 — Study of jet shapes in inclusive jet production at 7 TeV with the ATLAS detector, [arXiv:1101.0070](#)

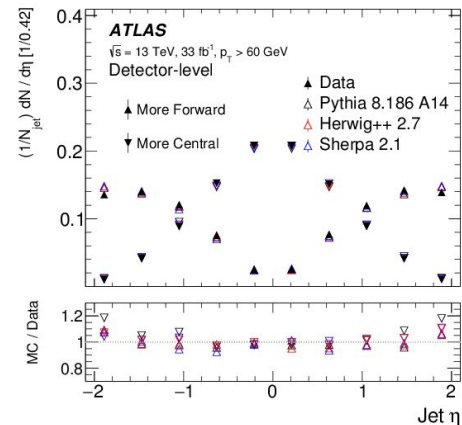
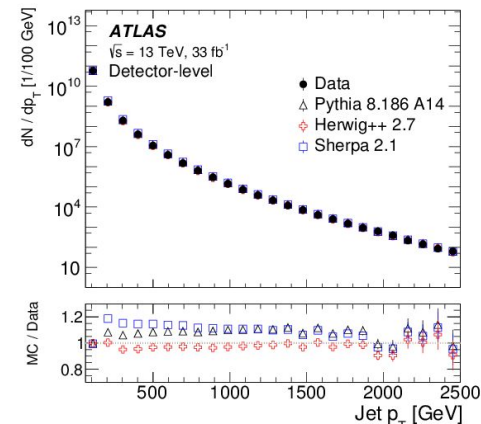
ATLAS jet fragmentation at 13 TeV — arXiv:1906.09254

Uses 33 fb^{-1} dataset of 13 TeV pp collisions from 2016

- Increased phase space & jet p_T reach wrt 7, 8 TeV
- Makes use of Run 2 tracker upgrades, e.g. IBL
- Dense-environment tracking, for $\langle \mu \rangle \approx 25$

At least two reco jets with $|\eta| < 2.1$, and $p_T > 60 \text{ GeV}$

- $|\eta|$ requirement for full containment in tracker
- $p_{T1}/p_{T2} < 1.5$ balance to simplify interpretation
- $p_T > 100 \text{ GeV}$ at fiducial level
- Charged tracks ghost-associated to calo jets



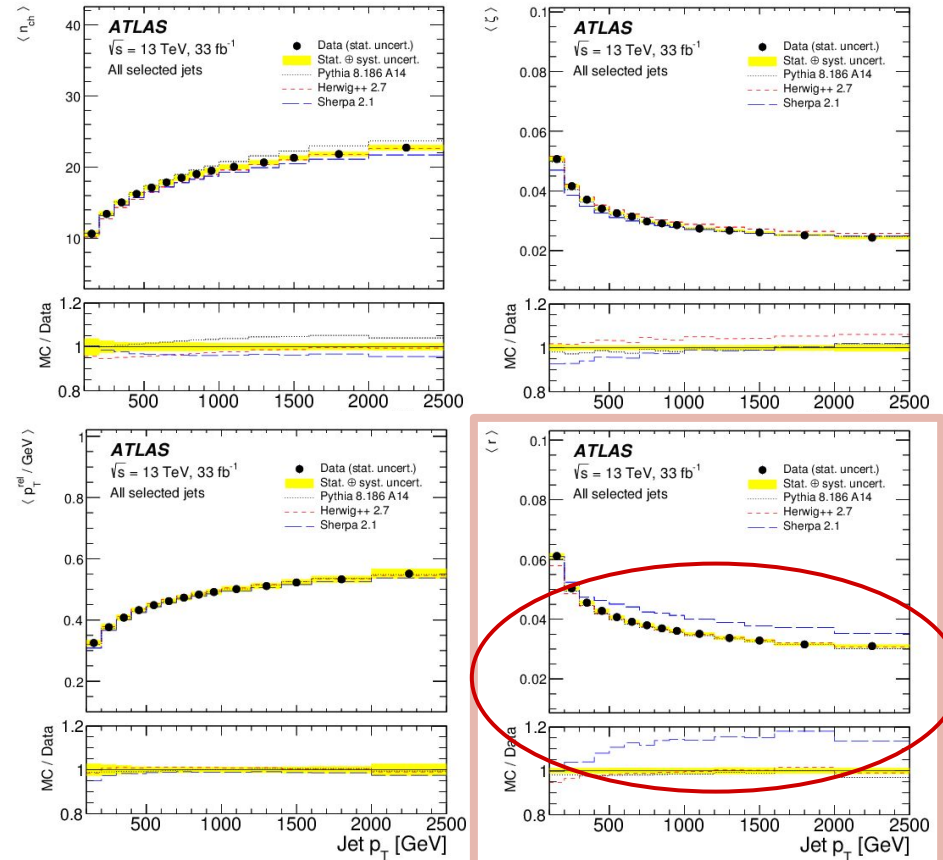
Unfolded average observables

Average observables vs p_T
generally well-described by
main shower MC codes

(Pythia8.1xx, Herwig++ and Sherpa 2.1)

Hints of deviation from Sherpa,
particularly in radial profiles —
standard component of MC via 7 TeV
jet shapes ... for jet $p_T < 500$ GeV!

Need to check vs Sherpa 2.2.x



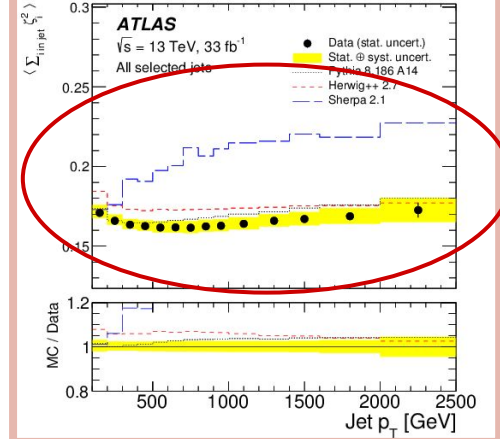
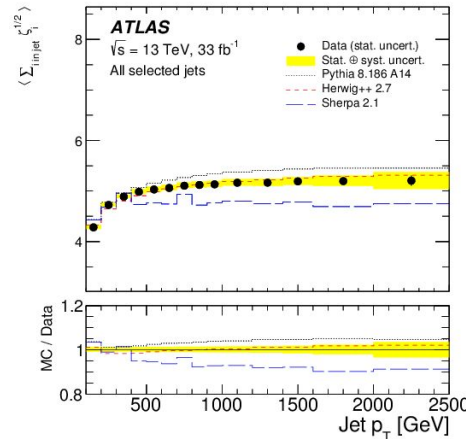
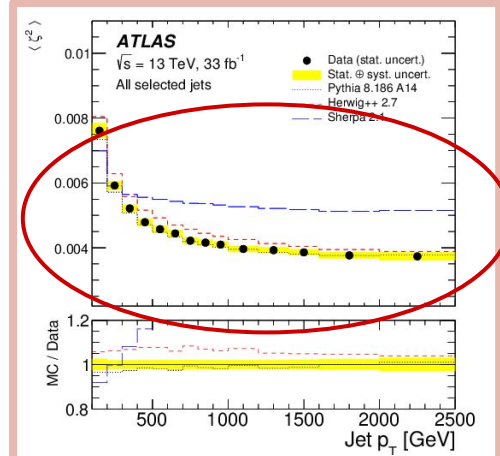
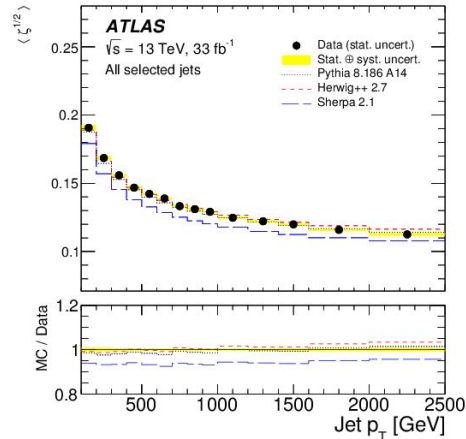
Unfolded observable moments & weighted sums

Also observables computed as moments and weighted sums with the p_T fraction ζ raised to powers $\kappa = 0.5$ and $\kappa = 2$:

$$\langle \zeta^\kappa \rangle = \int \zeta^\kappa F(\zeta) d\zeta / \int F(\zeta) d\zeta$$

$$\langle \sum_{i \in \text{jet}} \zeta_i^\kappa \rangle = \int \zeta^\kappa F(\zeta) d\zeta$$

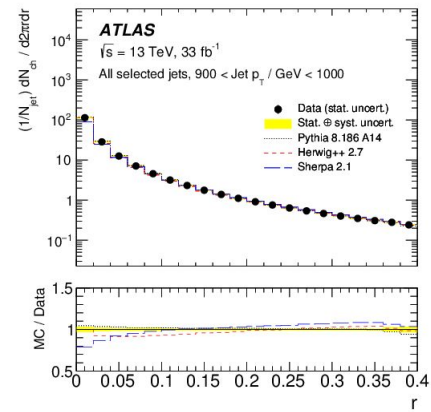
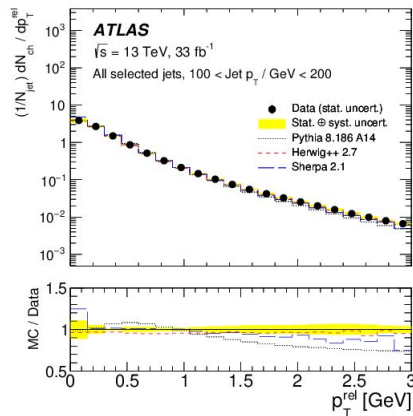
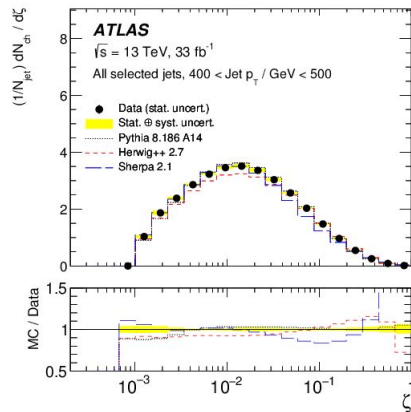
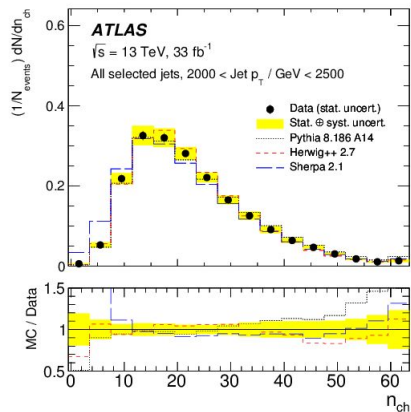
Pythia 8 and Herwig++ mostly well-behaved; major discrepancies seen for Sherpa 2.1, esp. for $\kappa = 2$ [effectively a $\text{var}(\zeta)$ measurement]



And more!

Differential distributions of every core variable in bins of jet p_T

A treasure-trove of data for jet modelling & resummation studies! **Rivet soon**



CMS quark & gluon jet substructure

[CMS-PAS-SMP-20-010](#)

36 fb⁻¹, 13 TeV pp dataset, using akT4 & 8 jets
with $p_T > 30$ GeV, $|y| < 1.7$ (cf. tracker acceptance)

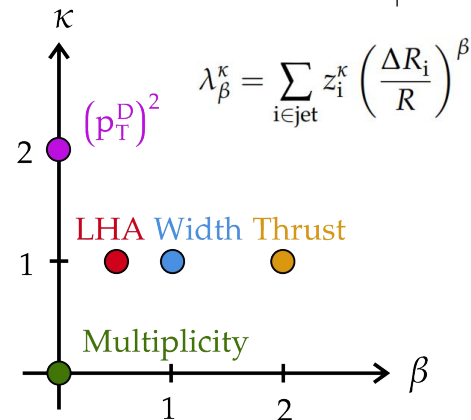
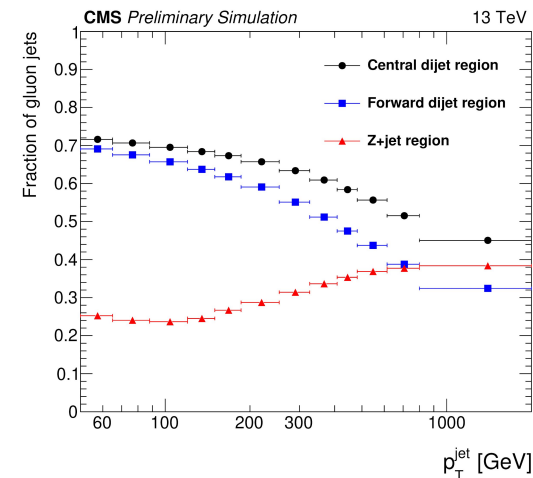
Dual event selection: dijets and Z+jets

(two OS muons, $p_T > 26$ GeV, $|m_{\mu\mu} - m_Z| < 20$ GeV)

JJ and ZJ asymmetry and separation required

Compare to LO event simulations with MG5+Py8 (+ ≤ 4 partons) and H++. Higher multiplicity MG5+Py8 unsurprisingly describes p_T spectra better \Rightarrow used as nominal MC

5 x generalised angularity observables cf. diagram:

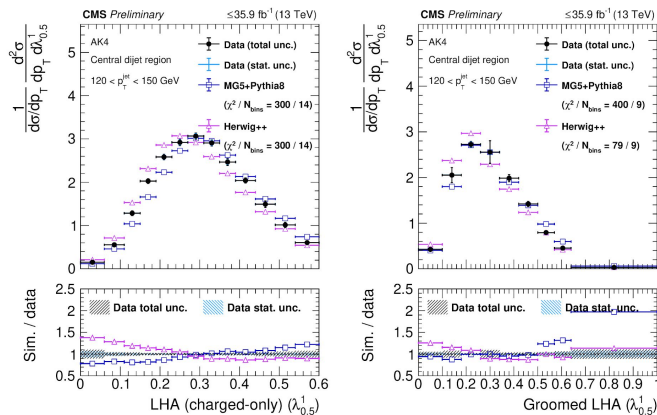
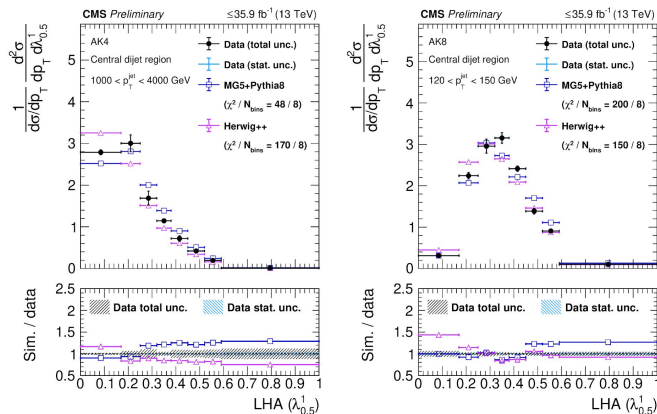


CMS quark & gluon jet substructure

CMS-PAS-SMP-20-010

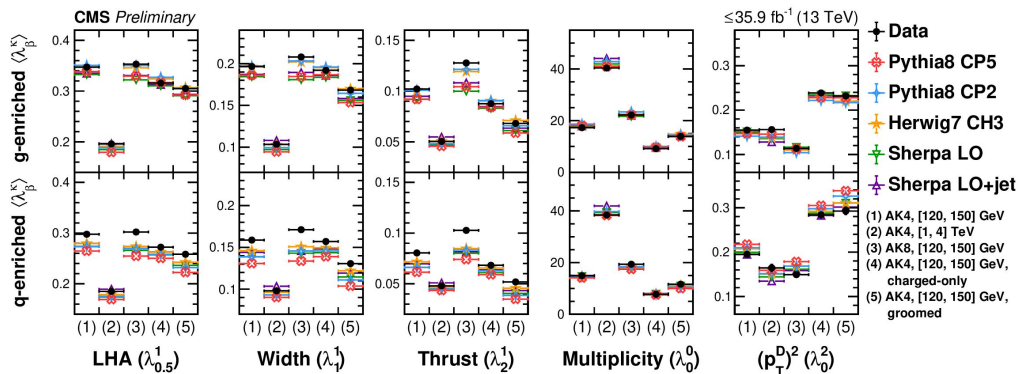
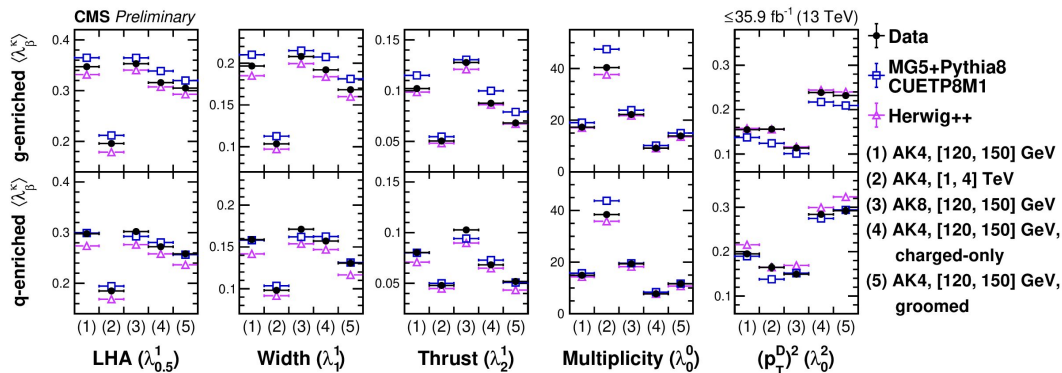
Observables distinguished by:

- event-selection
- central/forward dijet-event jet
- p_T -bin, and
- reco method: particle-flow, charged-only, and groomed



CMS quark & gluon jet substructure

CMS-PAS-SMP-20-010



Selections identified with q/g enhancement:

- “gluon” = central jet in dijet events
- “quark” = Z+jet at low- p_T (regions 1,3-5), and forward jet of dijet system at high p_T

Mean rates: MCs follow data trends, some large spreads. q worse? \Rightarrow tuning

b-jet fragmentation

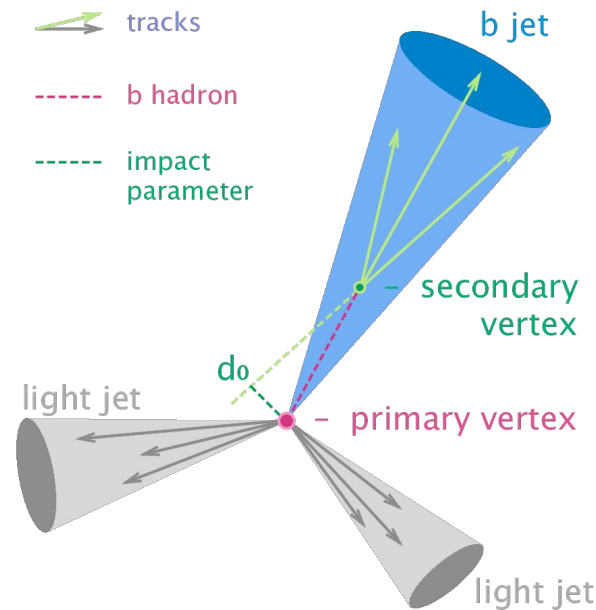
b-jet fragmentation

Heavy quark/jet production crucial both for QCD and EW/BSM physics

EW/BSM: *b*-jet signatures ubiquitous in many BSM models, top-quarks, and SM & BSM $H \rightarrow bb$ channels

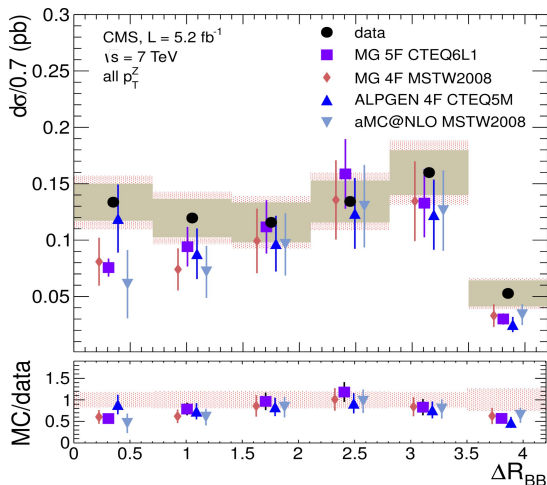
QCD: sensitivities to, for example...

- hard-scatter formalism between PDF / ME
- PS scale choices and mass effect on radiation pattern
- *b*-hadron production fractions



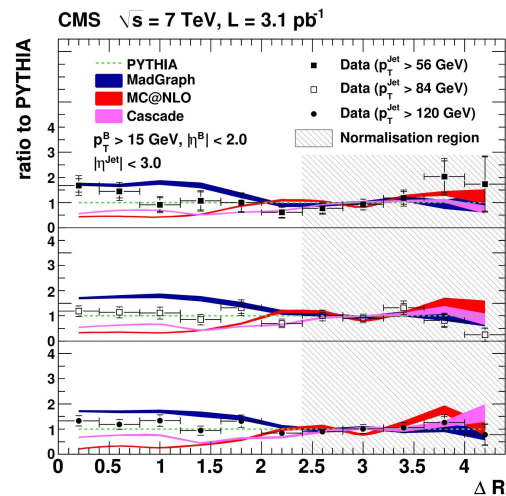
Earlier b -tagged jet fragmentation measurements

Previous measurements of b -jet fragmentation:



JHEP 12 (2013) 039 — CMS angular correlations in Z-boson with b -hadrons, arXiv:1310.1349

JHEP 03 (2011) 136 — CMS BB angular correlations from SV reconstruction, arXiv:1102.3194



ATLAS b -fragmentation in $t\bar{t}$

b -jet fragmentation moments, via secondary vertices and track-jets

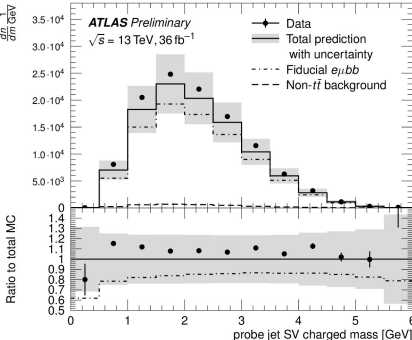
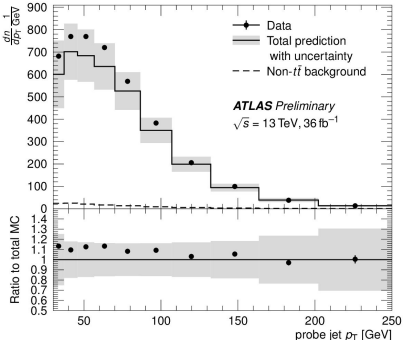
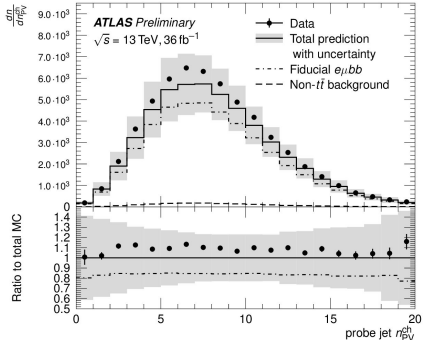
13 TeV analysis, partial Run 2 dataset of 36/fb

- $R = 0.4$ calo jets with standard ATLAS b -tagging (70% eff)
- Event selection: = 2 OS $e+\mu$, = 2 jets, $\Delta R_{jj} > 0.5$; tag & probe, *both ways*
- Variable-radius track jets ghost-associated to calo jets
- Track-jet PV and SV tracks: $SV/(PV+SV) \sim b\text{-hadron}/b\text{-quark}$

$$z_{T,b}^{\text{ch}} = \frac{p_{T,b}^{\text{ch}}}{p_{T,\text{jet}}^{\text{ch}}}$$

$$z_{L,b}^{\text{ch}} = \frac{\vec{p}_b^{\text{ch}} \cdot \vec{p}_{\text{jet}}^{\text{ch}}}{|p_{\text{jet}}^{\text{ch}}|^2}$$

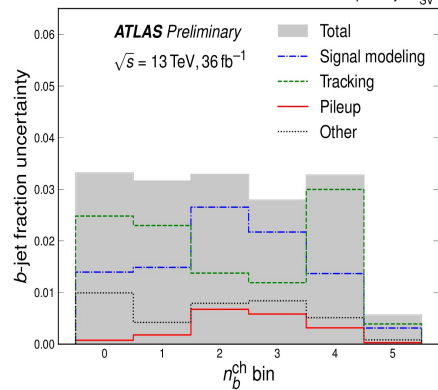
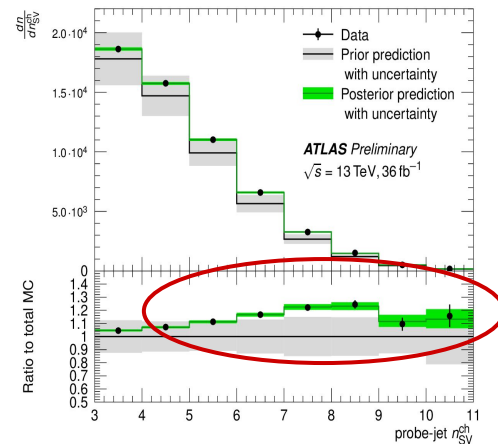
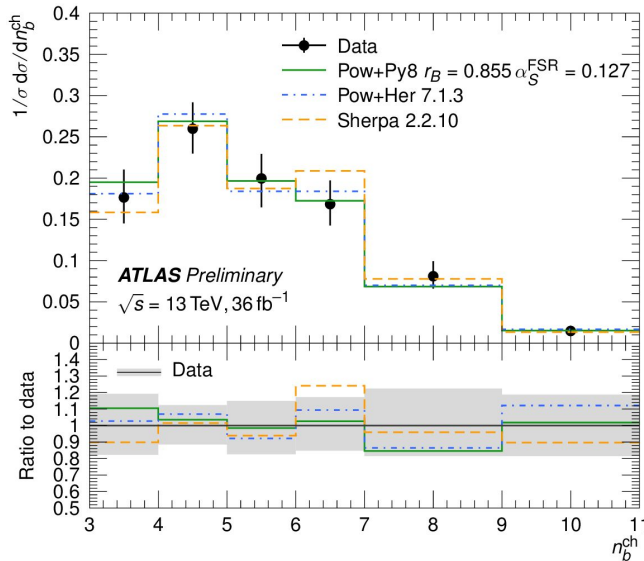
$$\rho = \frac{2p_{T,b}^{\text{ch}}}{p_T^e + p_T^\mu}$$



ATLAS b -fragmentation in $t\bar{t}$

n_{ch} moment

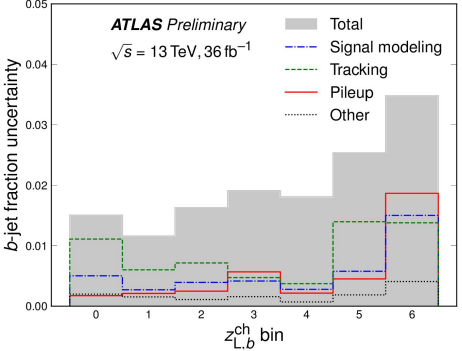
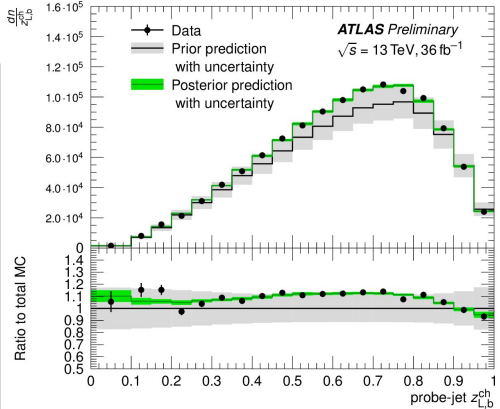
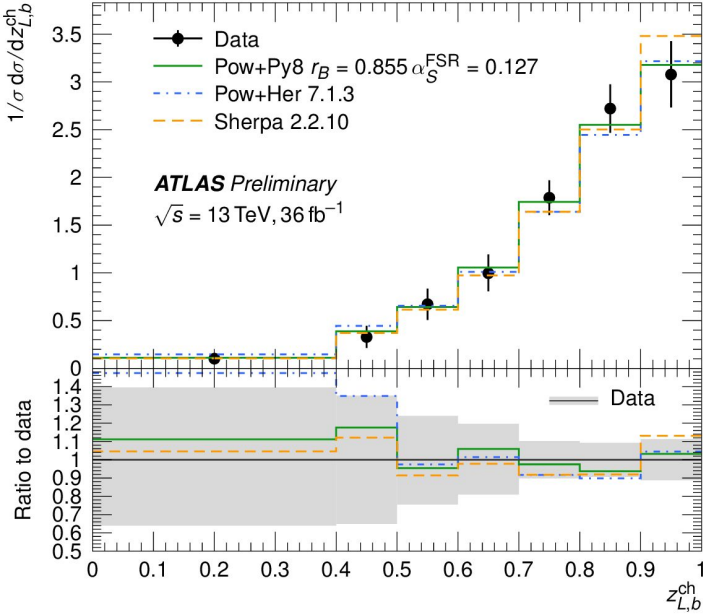
- #SV tracks $\approx b$ -hadron
- Fit shifts away from the input-MC prior
- Reweightings of Pow+Py8 to probe-jet n_{SV} as systematic
- Check of hadron fractions & decays: Sherpa > 2.2.8 improvements



ATLAS b -fragmentation in $t\bar{t}$

$z_{ch,L}$ (longitudinal) moment

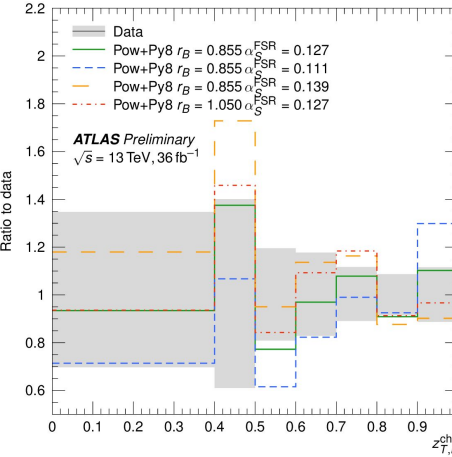
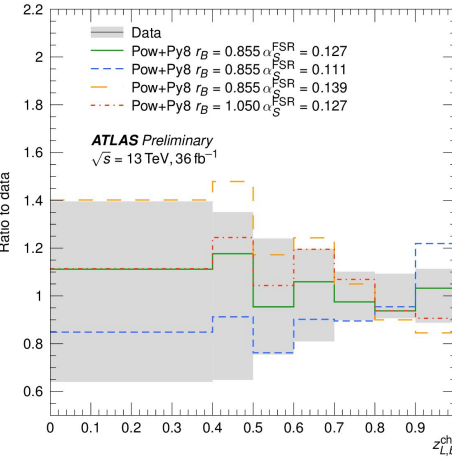
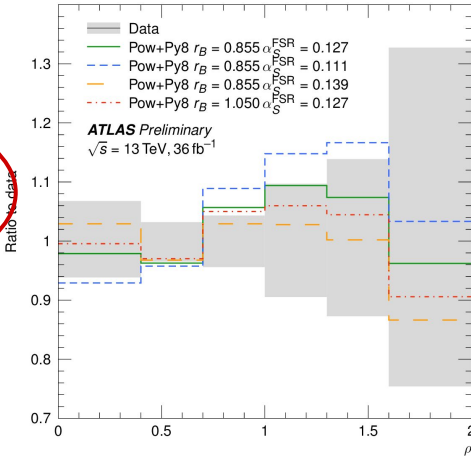
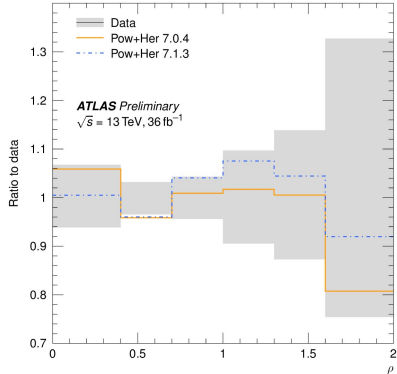
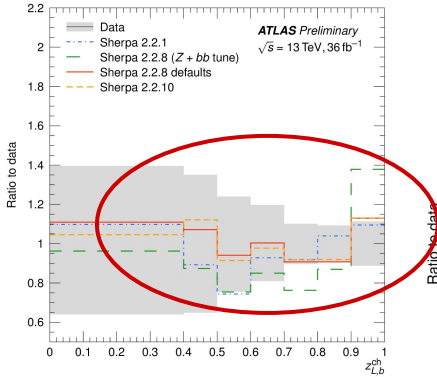
- Experimental proxy for the theoretical fragmentation function: **tunings from LEP and SLD valid?**
- Descriptions generally good, with Herwig a slight outsider (much improved from v7.0.4)



ATLAS b -fragmentation in $t\bar{t}$

Sensitivities to Sherpa tunes, Pw+Hw versions, Pw+Py8 r_B tunes, α_S variations:

z variables: little sensitivity to r_B param



- Latest Sherpa models b -frag better
- Smooth effects of FSR α_S and frag function parameters on Py8 data/MC agreement: perfect tuning inputs

ATLAS b -fragmentation with mesons

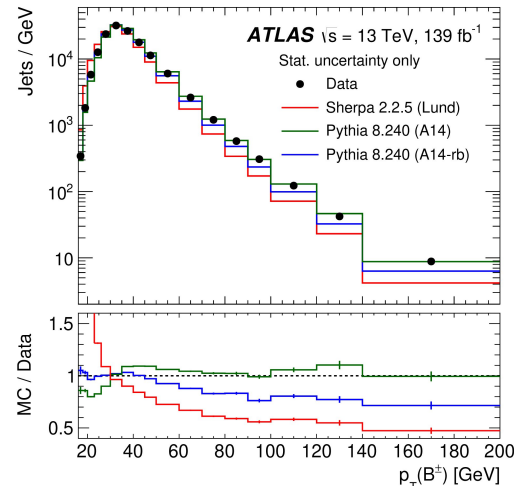
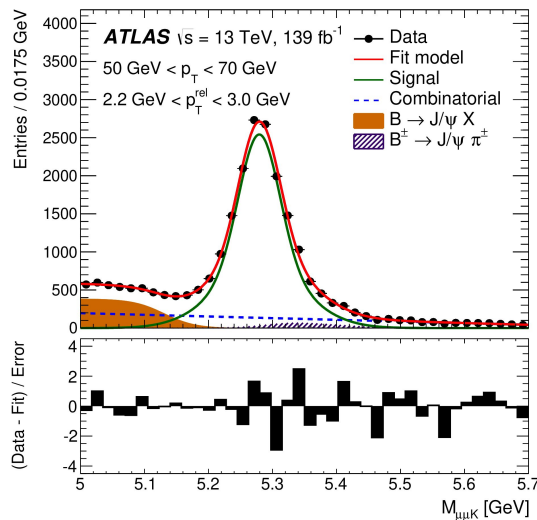
Explicit reconstruction of $B^\pm \rightarrow J/\psi K$ decay channel

- Two muons: $p_T > 6$ GeV,
 $2 < m_{\mu\mu} < 9$ GeV
- Third track, cuts on vtx
 χ^2 & pair/triplet masses

Unfold to particle-level with
kin cuts on μ and $K p_T$

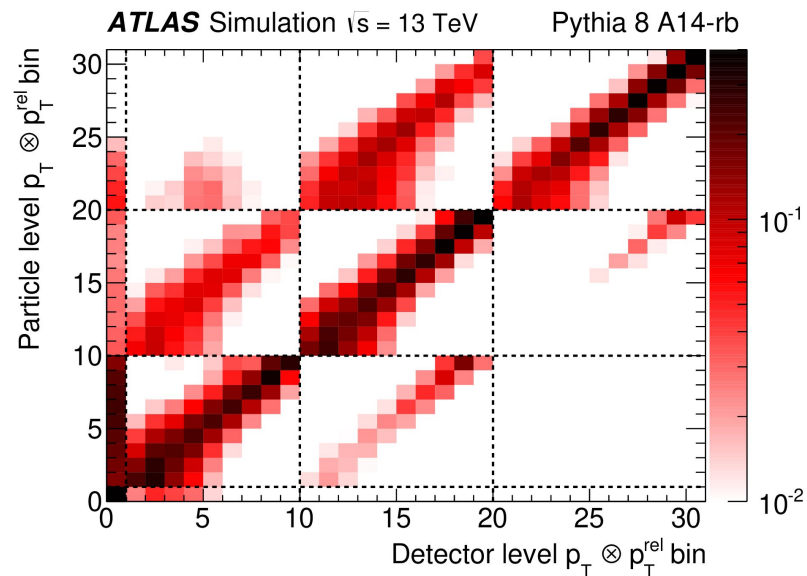
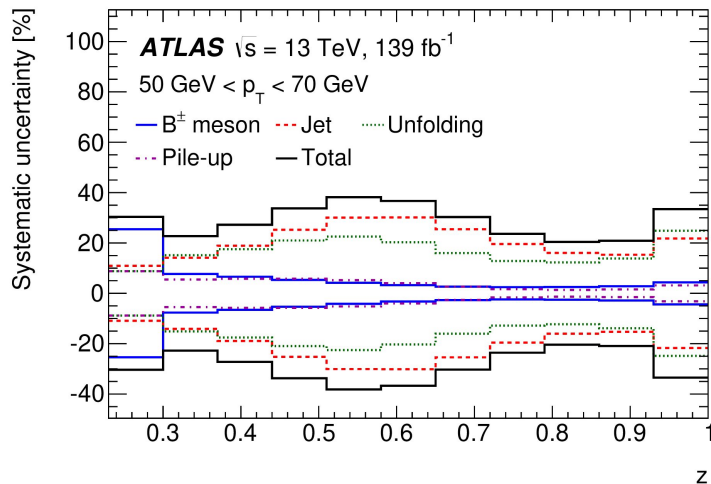
Measure fragmentation
functions:

$$z = \frac{\vec{p}_B \cdot \vec{p}_j}{|\vec{p}_j|^2}; \quad p_T^{\text{rel}} = \frac{|\vec{p}_B \times \vec{p}_j|}{|\vec{p}_j|}$$



ATLAS b -fragmentation with mesons

Unfolding more limited by transfer resolution for $p_{T,rel}$ than z



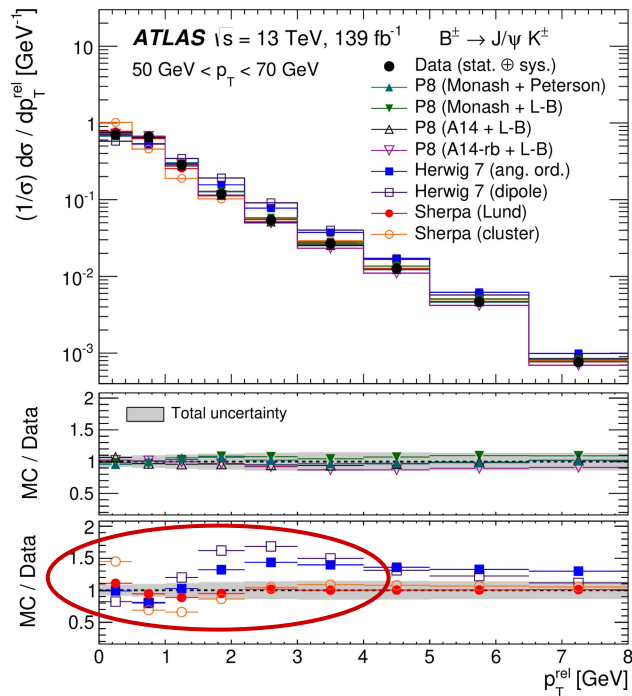
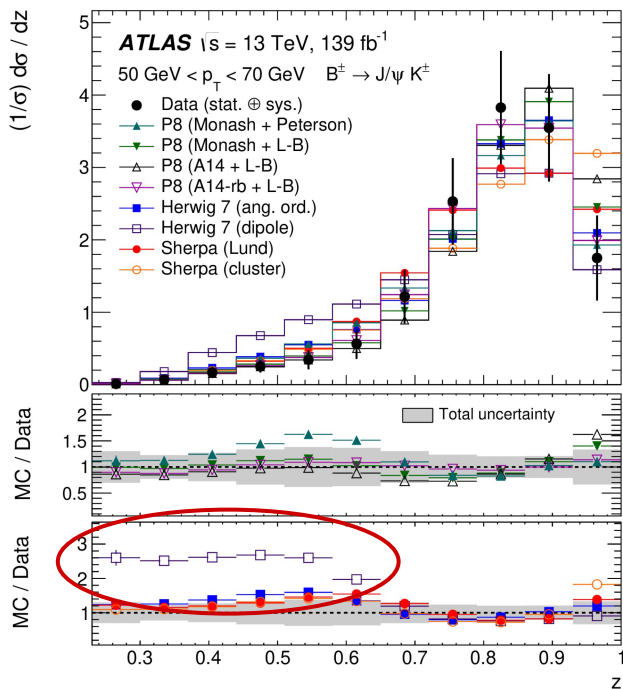
Limiting systematics a balance btw B reco, jet reco, and unfolding uncertainties

Obs and p_T dependence

ATLAS b -fragmentation with mesons

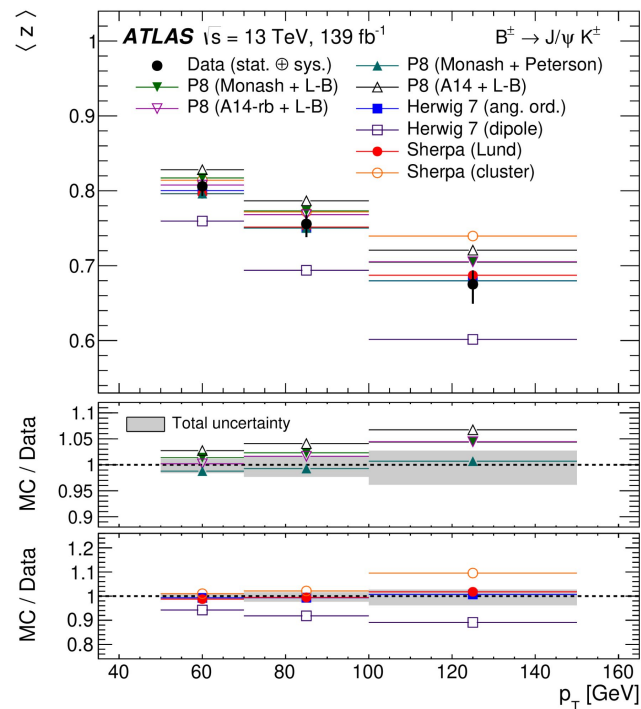
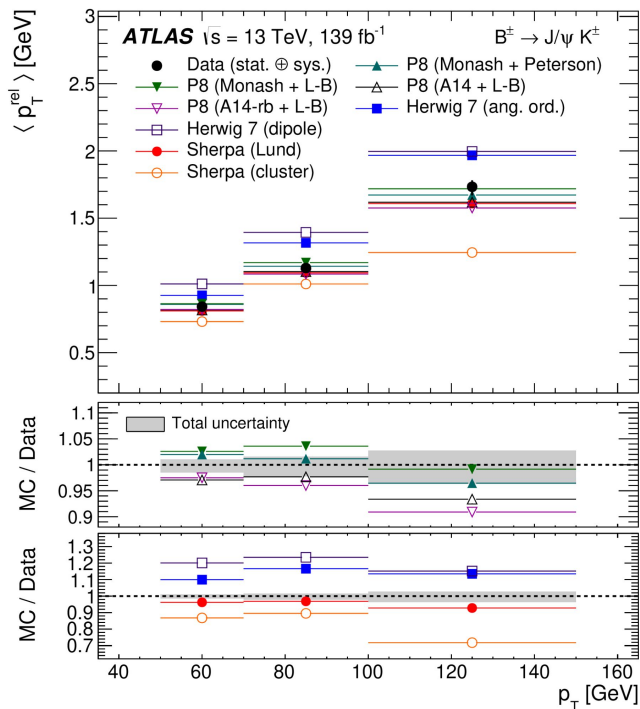
Longitudinal and transverse frag functions in jet- p_T bins

⇒ Herwig7 showers and Sherpa cluster hadronisation show deviations wrt data



ATLAS b -fragmentation with mesons

Average values of frag functions vs jet $p_T \Rightarrow$ flags O(10%) mismodelling



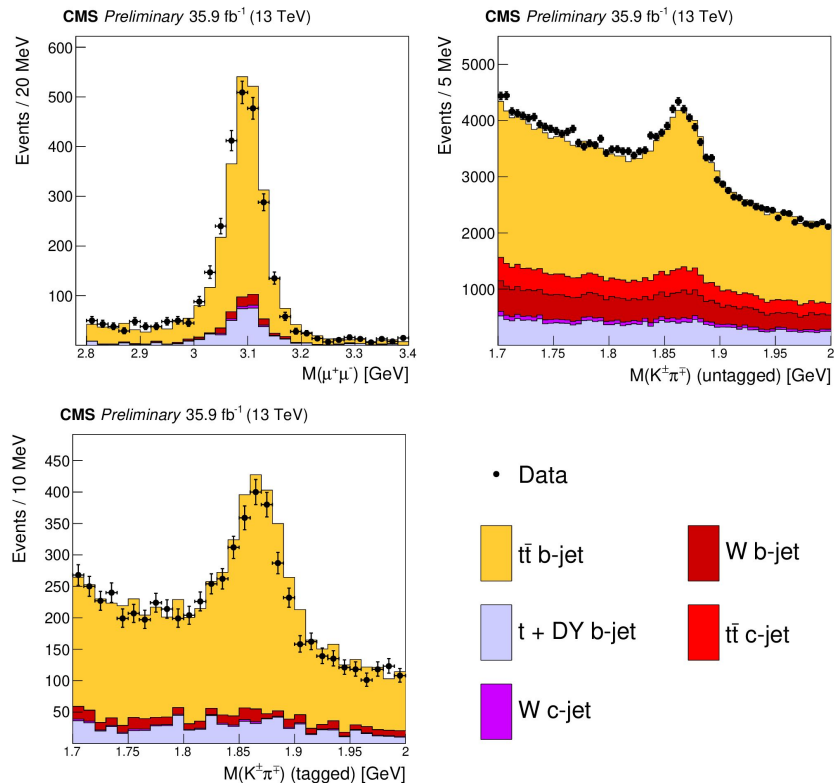
CMS b -jet fragmentation from tt decays

CMS-PAS-TOP-18-012

CMS' version is more directly tied to the Lund-Bowler fragmentation function ansatz and fitting of its r_b parameter

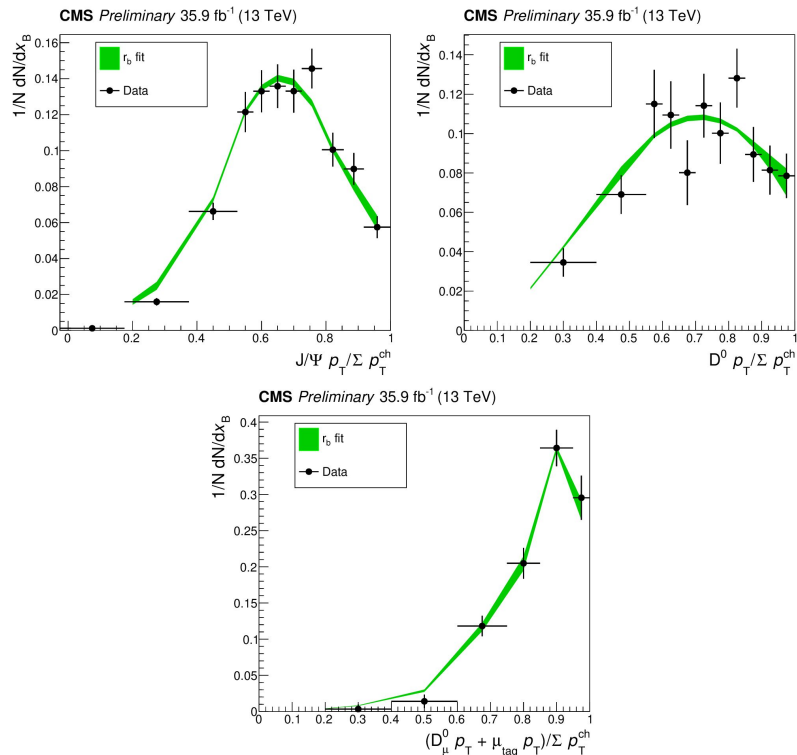
Explicit reconstruction of J/ψ and D^0 mesons (the latter with and without a muon-tagged decay)

Use mesons as final-state proxies for the decayed b -hadron. Distributions of momentum fractions used to fit r_b



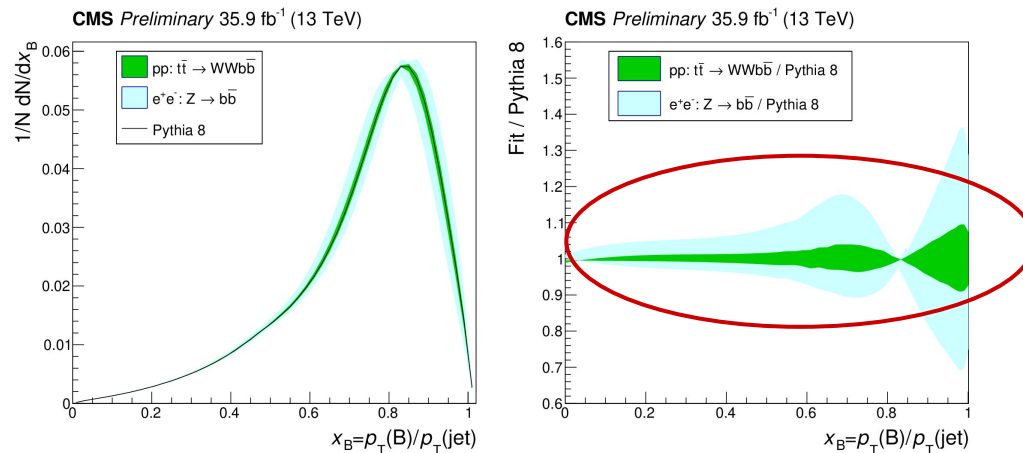
CMS b -jet fragmentation from tt decays

CMS-PAS-TOP-18-012



Set of three proxy fragmentation fractions extracted, used to constrain x_B

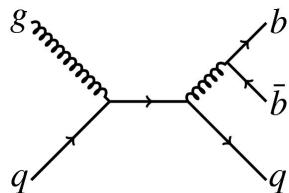
Significant precision improvements wrt LEP/SLD Z-pole tunes:



ATLAS $g \rightarrow bb$ at small opening angles

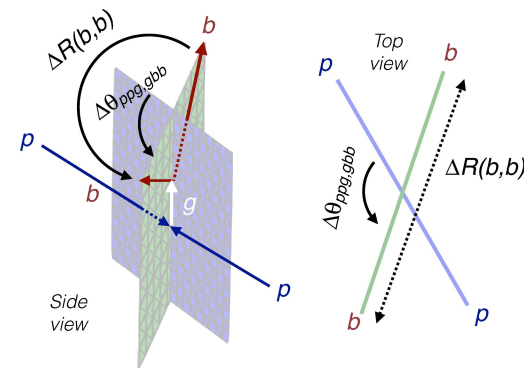
Focus on final-state $g \rightarrow bb$ splitting kinematics in boosted region

$p_T > 450$ GeV $R=1$ akT jets, 33/fb of 13 TeV pp data



Observables:

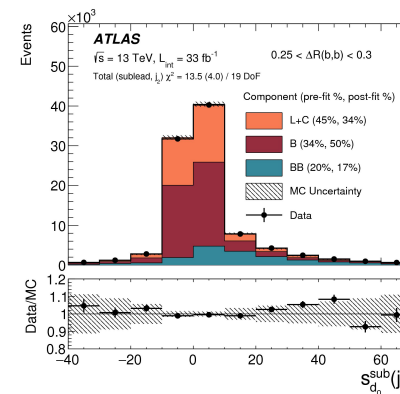
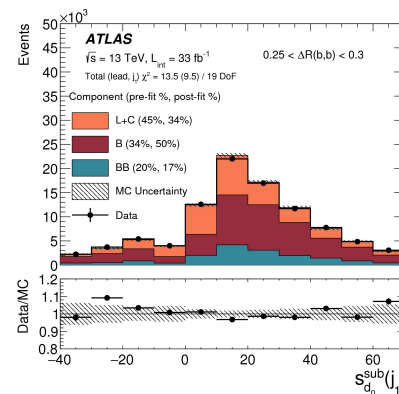
- m_{bb} / p_T
- $z(p_T)$
- ΔR_{bb}
- Polarisation angle $\Delta\theta \Rightarrow$



Require two b -tagged, ghost-assoc VR track-jets as b proxies, 60% working point

Flavour fit, via signed-impact-parameter distributions for subleading track, per observable bin, e.g. ΔR_{bb} right:

Mostly slight BB -fraction overestimates



ATLAS $g \rightarrow bb$ at small opening angles

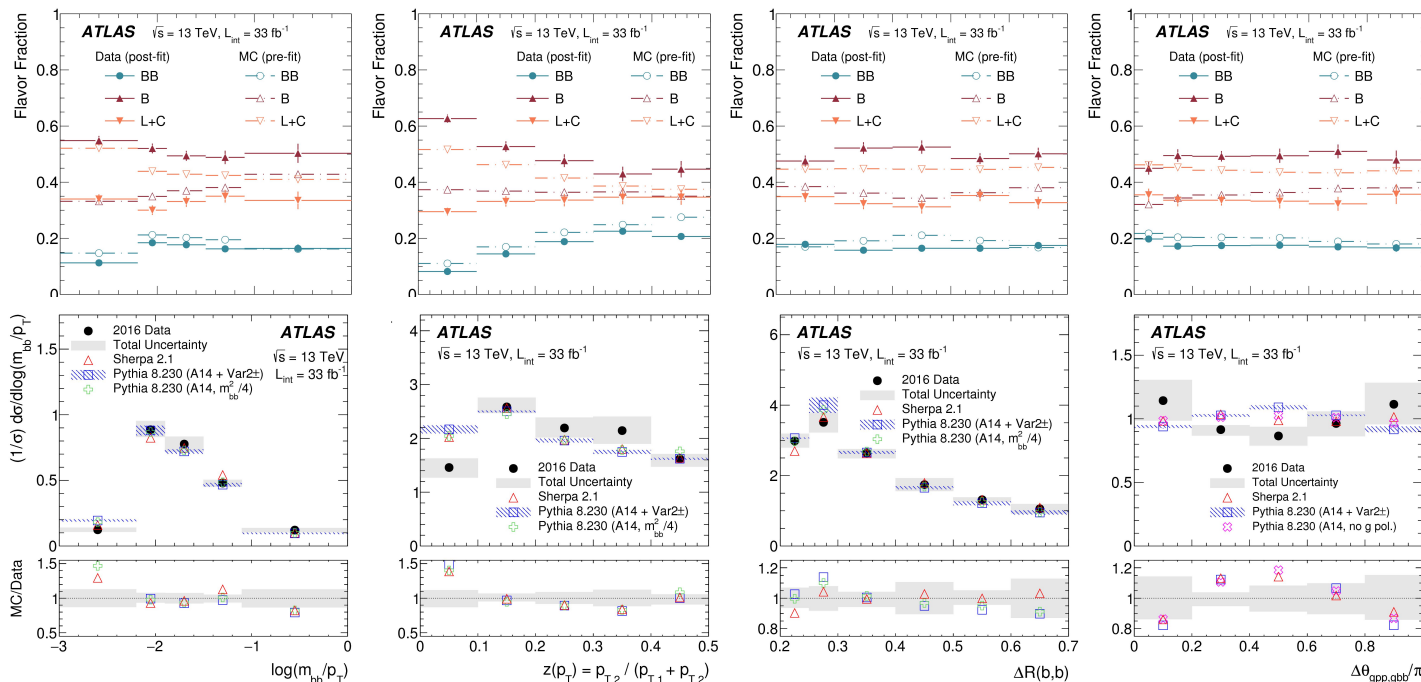
Phys. Rev. D 99 (2019) 052004,

arXiv:1812.09283,

[Plot page](#)

Flavour-fraction fits, per bin of each observable

(BB ~good, large differences in B and L+C)



Jet fragmentation in *tt*

CMS jet substructure in $t\bar{t}$ at 13 TeV

arXiv:1808.07340 / Phys. Rev. D 98 (2018) 092014



“one to rule them all...”

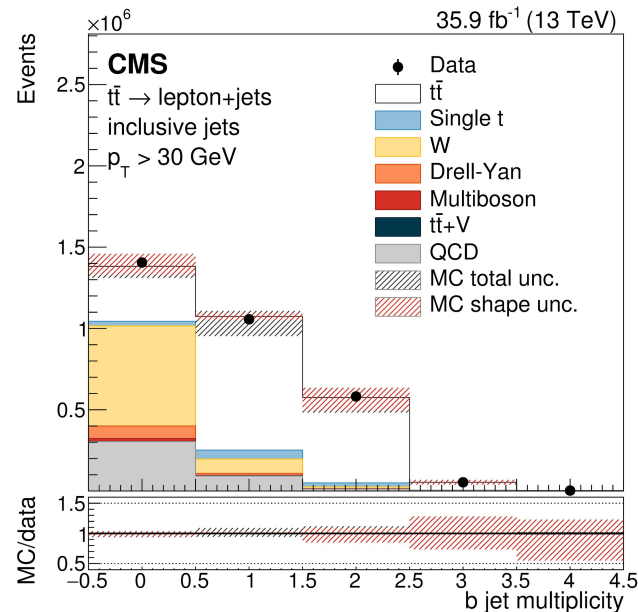
36 fb⁻¹ of 13 TeV pp dataset, with semileptonic top-pair selection

Exactly 1 tight, isolated lepton; 63% b -tag working point \Rightarrow 94%-pure $t\bar{t}$

akT4 jets, $p_T > 30$ GeV, flavour groups:

- inclusive
- b -jet: via tag, incl $g \rightarrow bb$
- q -enh: via W -mass window, 50% pure
- g -enh: neither of the above, 58% pure

Particle-level flavour \Rightarrow ghost matching & m_{jj}



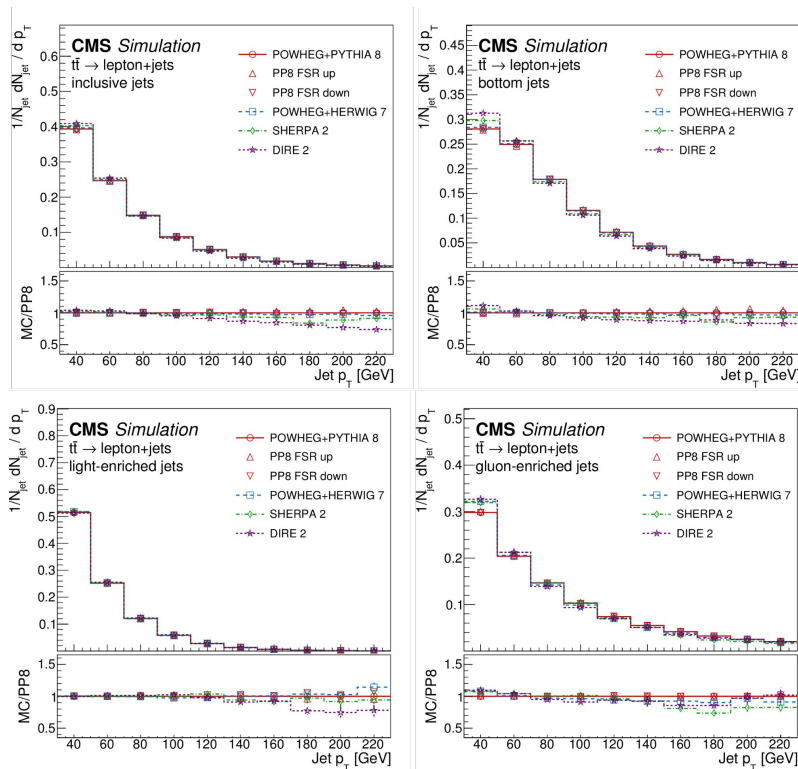
CMS jet substructure in $t\bar{t}$ at 13 TeV

arXiv:1808.07340 / Phys. Rev. D 98 (2018) 092014

Lots of substructure observables:

- constituent-multiplicity & p_T -dispersion
- angularities: width, LHA, jet thrust
- eccentricity
- soft-drop fraction and groomed N_{ch}
- groomed-subjet angles
- N -subjettiness ratios
- ECFs $C_{1,2,3}$, M_2 , $N_{2,3}$

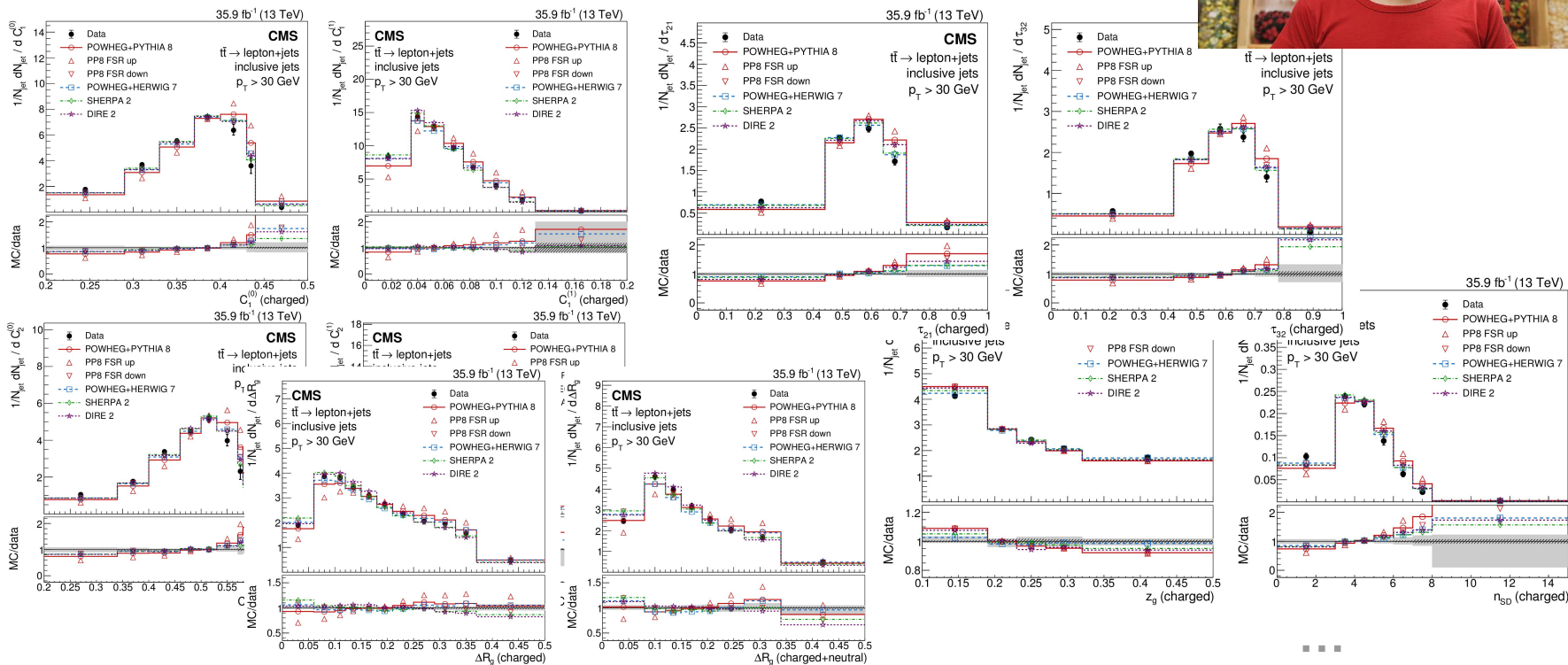
Several observables measured for both charged and charged+neutral constituents!



CMS jet substructure in $t\bar{t}$ at 13 TeV

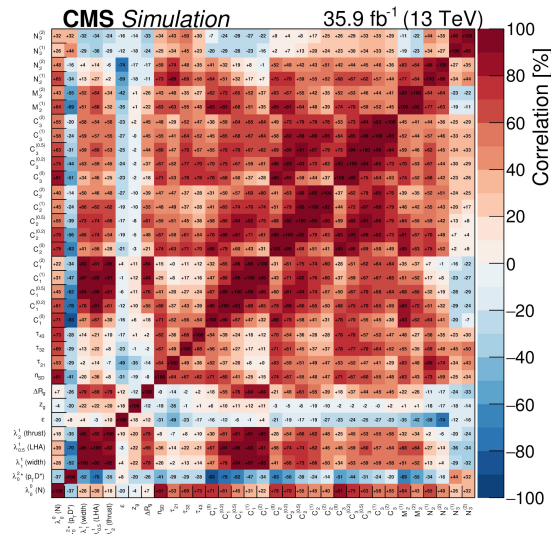
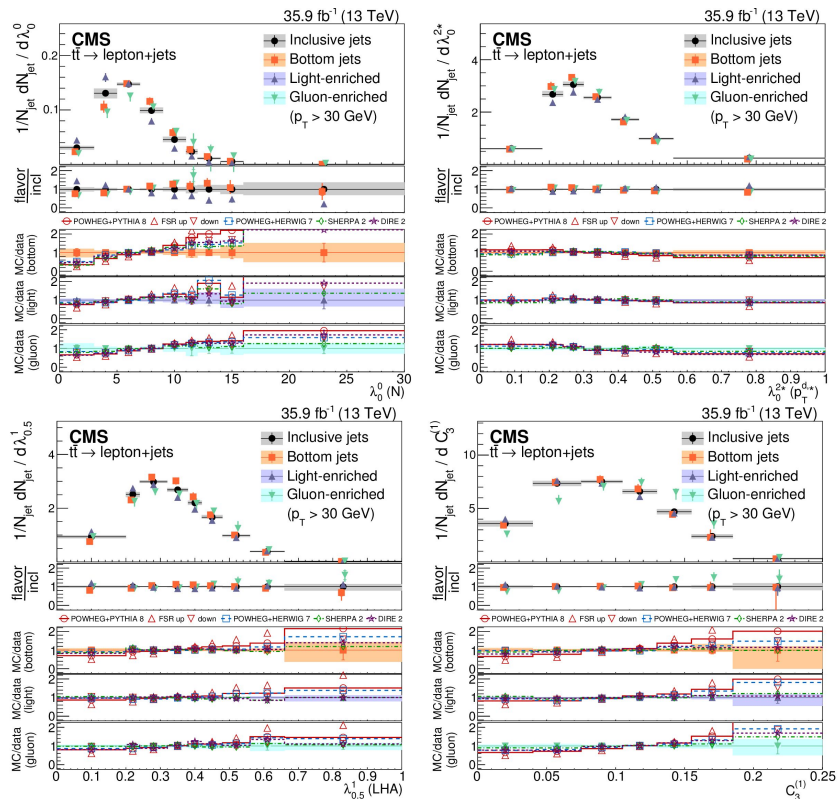
arXiv:1808.07340 / Phys. Rev. D 98 (2018) 092014

Exceptional resource for model development & validation!



CMS jet substructure in $t\bar{t}$ at 13 TeV

arXiv:1808.07340 / Phys. Rev. D 98 (2018) 092014



Breakdowns of observables by flavour category, plus correlations: will be ideal for MC dev & tuning via Rivet

Other jet structure measurements

Top-decay

Eur. Phys. J. C 78 (2018) 847 — ATLAS 13 TeV measurement of colour flow between $W \rightarrow qq'$ jets in $t\bar{t}$ with jet-pull observables [arXiv:1805.02935](https://arxiv.org/abs/1805.02935)

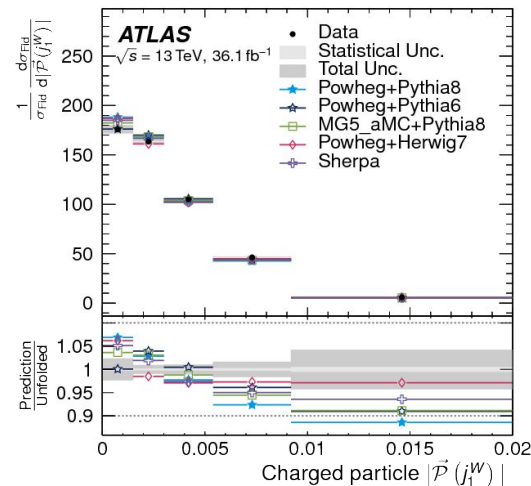
Boosted large- R jets

JHEP 08 (2019) 033 — ATLAS 13 TeV measurements of jet substructure in top-quark, W -boson, and light jets [arXiv:1903.02942](https://arxiv.org/abs/1903.02942)

JHEP 11 (2018) 113 — CMS 13 TeV jet mass distributions in dijet events, [arXiv:1807.05974](https://arxiv.org/abs/1807.05974)

Phys. Rev. D 86 (2012) 072006 — ATLAS 7 TeV properties of boosted jets [arXiv:1206.5369](https://arxiv.org/abs/1206.5369)

JHEP 1205 (2012) 128 — ATLAS 7 TeV jet mass and substructure [arXiv:1203.4606](https://arxiv.org/abs/1203.4606)



Conclusions

- **Measurements sensitive to jet fragmentation have grown far beyond direct measurements cf. LEP**
 - A multitude of angularities, correlation functions, substructure observables from both ATLAS and CMS
 - Use of track-based & all-particle reconstructions, and dig into jet-flavour dependence
 - Ghost-association of track-jets or reconstructed hadrons, esp. for b -quark studies
 - Grooming algorithms reduce pile-up dependence, provide another facet
 - Also large- R jets and boosted phase-space
- **Ways to improve syst precision? Most analyses only 36/fb so far!!**
- **Dawn of Run 3 a good time to revisit 7 TeV MC tunes & studies**

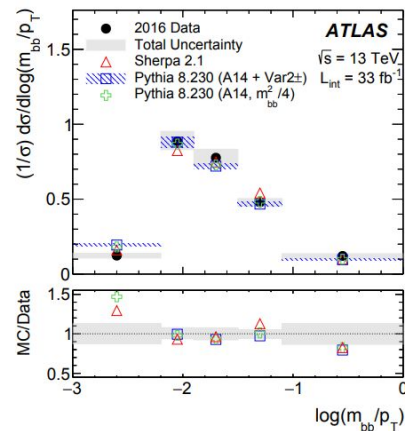
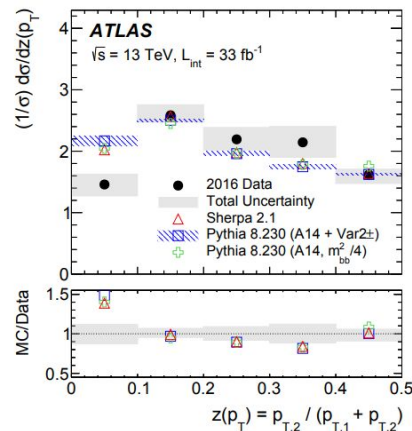
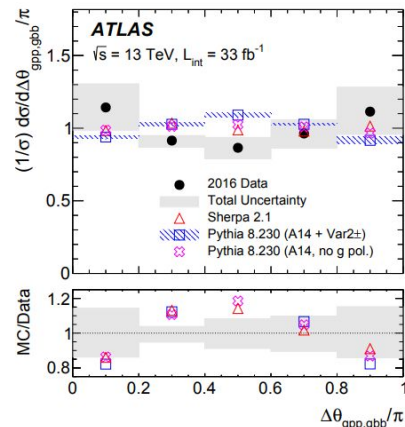
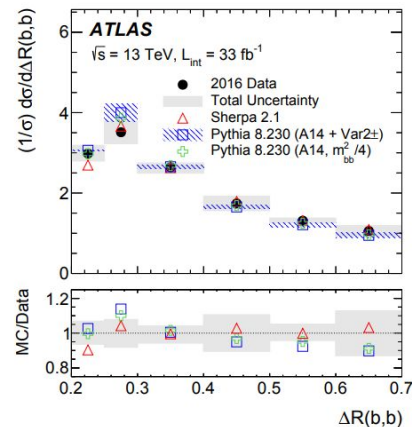
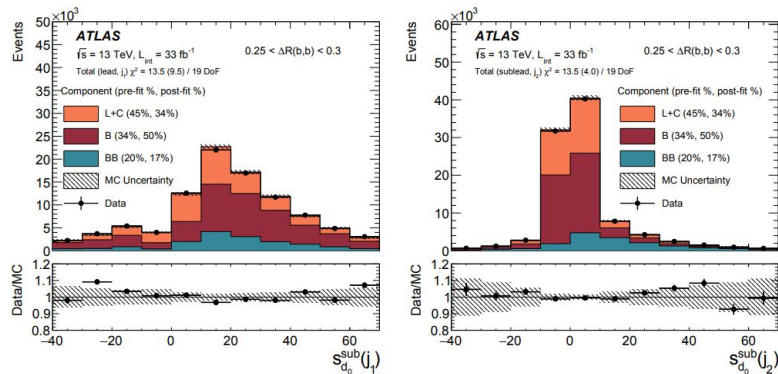
Backup

ATLAS $g \rightarrow b\bar{b}$ fragmentation — arXiv:1812.09283

Super-quick summary: b-tagged track subjets in boosted jets

Fiducial differential cross-sections in b-subjet separation, mass, p_T balance, and polarisation angle

Key: flavour fit via signed impact param



Observables

Fragmentation function D defined vs $\zeta = p_{\perp}$ fraction of hadron h wrt its containing jet p_{\perp} , from parton p
 \Rightarrow DGLAP pQCD evolution; mirror image of PDFs

This paper uses charged hadrons, but full (calo) jet
 $\Rightarrow \langle n_{\text{ch}} \rangle$ and differential $1/N_{\text{jet}} dN_{\text{jet}}/d\langle n_{\text{ch}} \rangle$

+ **summed fragmentation function:**
 differential in p_{\perp} fraction ζ and jet $p_{\perp} \Rightarrow$ **extract partial fractions, moments & weighted sums**

+ **Relative transverse momentum**
Radial profile (non- p_{\perp} -weighted)

$$\mu \frac{\partial}{\partial \mu} D_p^h(\zeta, \mu) = \sum_{p'} \int_{\zeta}^1 \frac{d\zeta'}{\zeta'} \frac{\alpha_S(\mu) P_{p' \leftarrow p}(\zeta', \mu)}{\pi} D_{p'}^h\left(\frac{\zeta}{\zeta'}, \mu\right)$$

$$\langle n_{\text{ch}} \rangle(p_{\perp}^{\text{jet}}) = \sum_p f_p(p_{\perp}^{\text{jet}}) \sum_{h \text{ charged}} \int_{\text{threshold}/p_{\perp}^{\text{jet}}}^1 d\zeta D_p^h(\zeta, p_{\perp}^{\text{jet}})$$

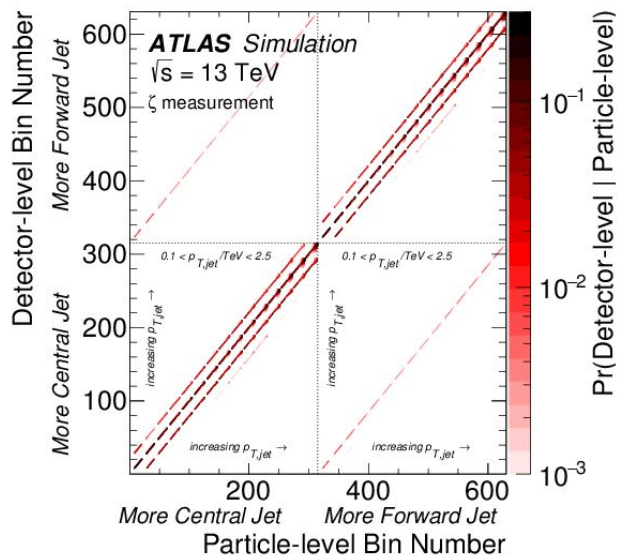
$$F(\zeta, p_{\perp}^{\text{jet}}) = \sum_p f_p(p_{\perp}^{\text{jet}}) \sum_{h \text{ charged}} D_p^h(\zeta, p_{\perp}^{\text{jet}})$$

$$p_{\perp}^{\text{rel}} \equiv p_{\perp}^{\text{charged particle}} \sin \Delta\phi$$

$$\rho_{\text{ch}}(r, p_{\perp}^{\text{jet}}) = (1/\bar{N}_{\text{jet}}) dn_{\text{ch}}/2\pi r dr$$

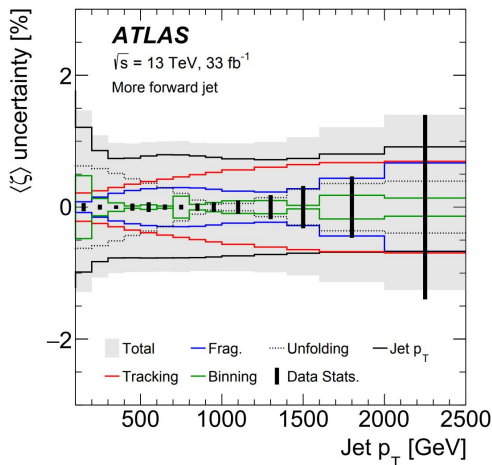
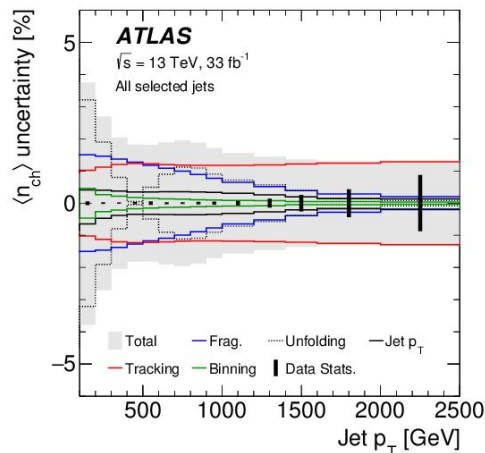
Detector correction & uncertainties

Unfolding from detector obs to fiducial phase space:
 particle-level tracks & jets from particles with
 $ct_0 > 10$ mm; muons and neutrinos excluded from jets



Unfolding by 2D iterative
 Bayes method (1 iter)
 sandwiched by explicit
 in/out migration corr.

Main uncertainties:
 tracking, jet scale,
 binning & unfolding,
 depending on observable

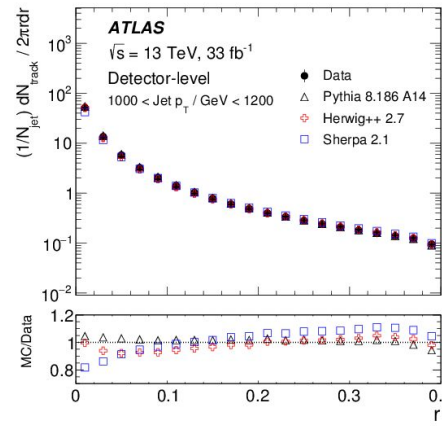
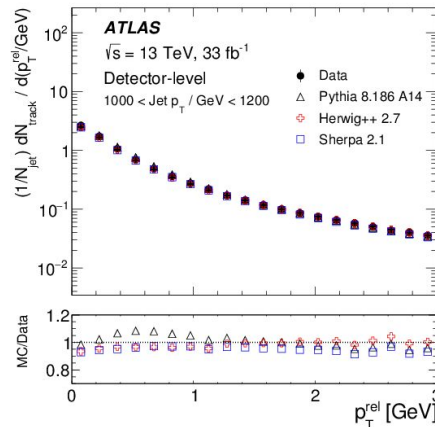
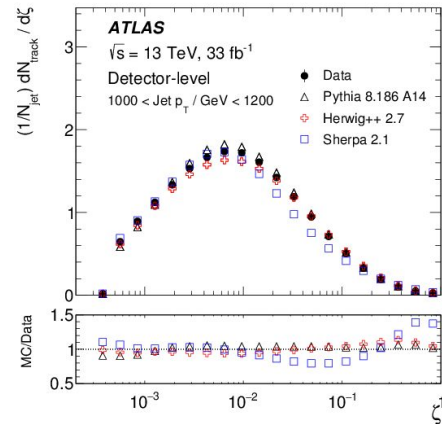
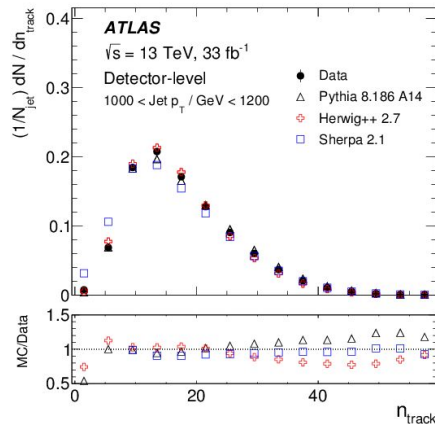


Detector-level variables

Raw distributions of n_{trk} , track momentum fraction, track $p_{\text{T,rel}}$, and track radial profile

For a 1 TeV jet, most probable n_{trk} is ~ 15 , and most probable momentum fraction $\sim 1\%$

Track $p_{\text{T,rel}}$ and r (radial profile) distributions peak at zero since radiation dominantly collinear

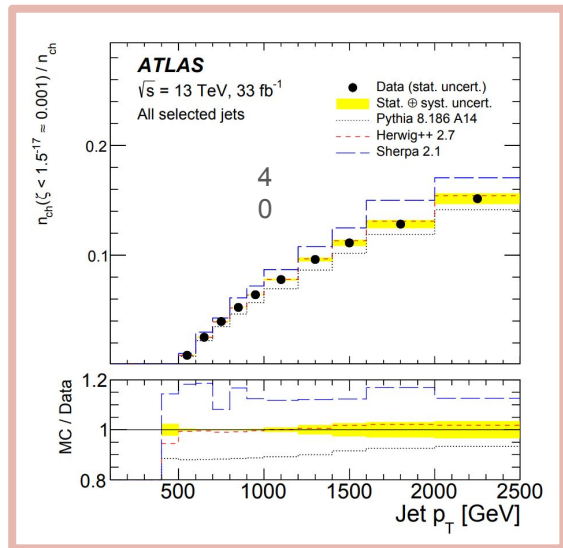
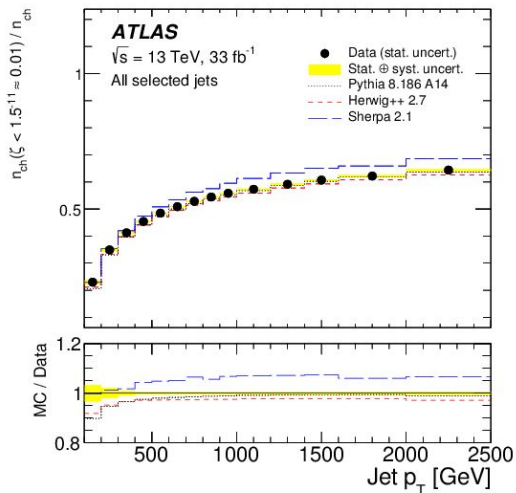
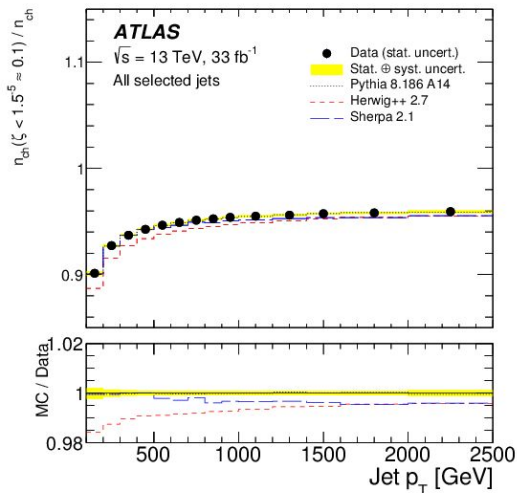


Unfolded partial sums: n_{ch} fraction in bins of ζ

$$\int_0^X F(\zeta) d\zeta / \int F(\zeta) d\zeta = n_{\text{ch}}(\zeta < X) / n_{\text{ch}}$$

Fractions of charged particles with $\zeta \lesssim 10\%$, 1% , and 0.1% vs jet p_T

Fraction of small-fraction particles increases with jet p_T , cf. hadronisation scale
 Small mismodelling of 10% by Herwig; with Sherpa & Py8 in less inclusive bins

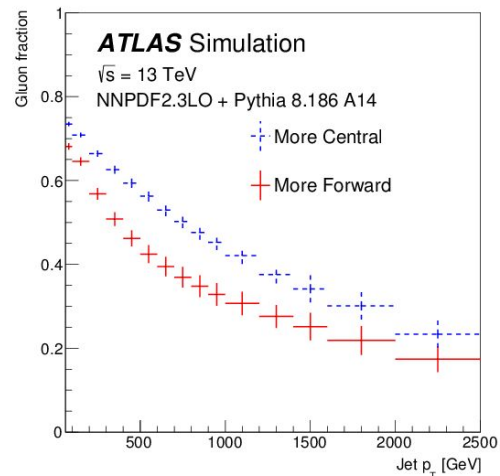
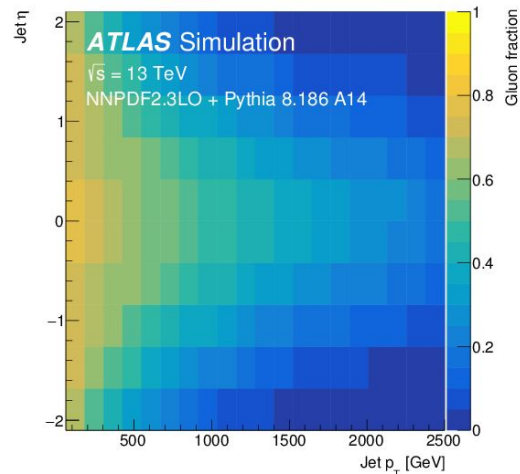


Quark/gluon jet discrimination

An important application of jet structure data is development of methods to extract information about quark/gluon jet origins

Ideally in a well-defined, QCD-aware way!

- **Central/forward jet:** roughly, central and low- p_T jets are more likely to be gluon-initiated
- \Rightarrow Extract q/g components with an MC-template procedure
- **New:** model-independent q/g extraction by data-driven “topic” modelling

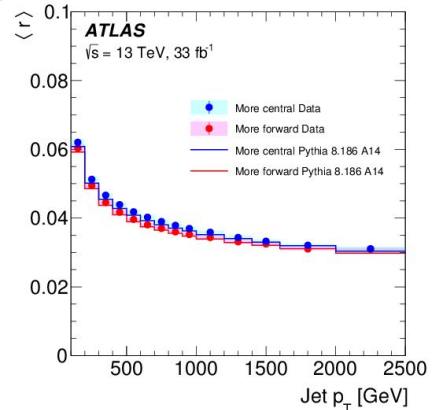
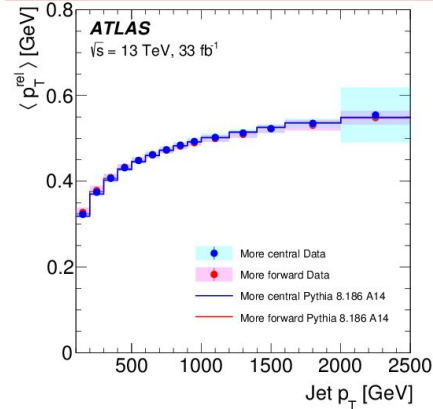
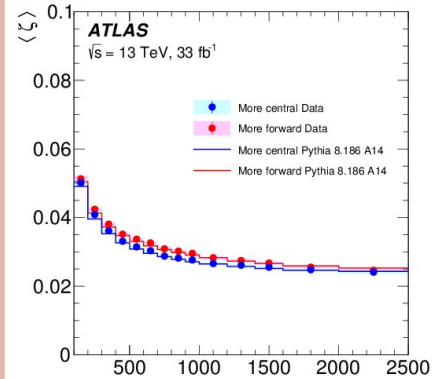
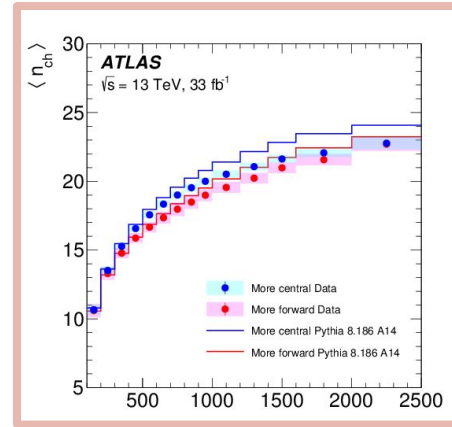


Mean observables with central/forward-jet split

Aim of central/forward jet distinction is to bias quark or gluon jet origin

Biases allow extraction of separate q/g-like fragmentation functions by comparison of forward and central jet ones

Note Pythia mismodelling of split n_{ch} distributions, unlike inclusive. Most c/f-split mean observables are well-described



Model-dependent quark/gluon jet characterisation

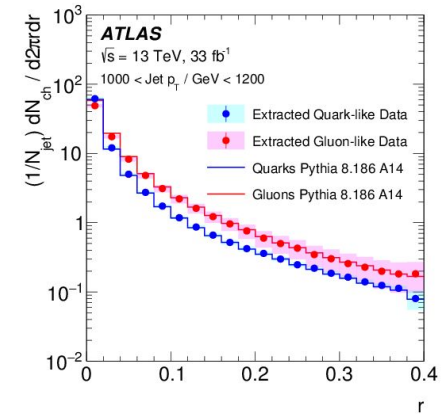
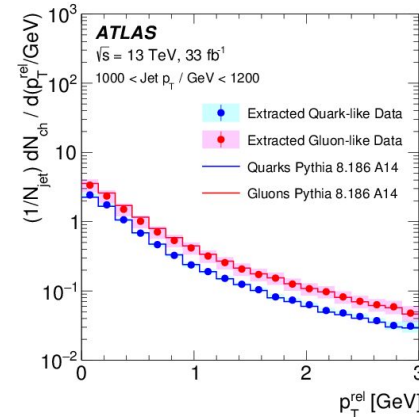
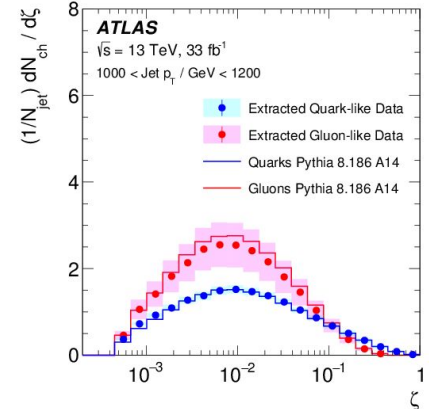
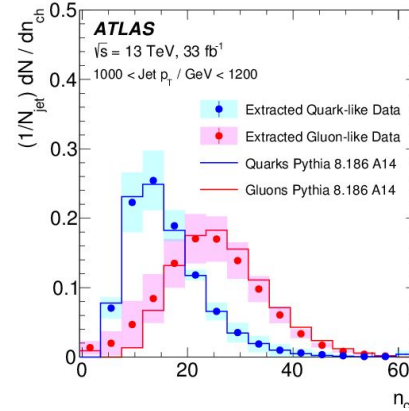
q/g extraction by use of MC flavour fractions f , nominally from Pythia:

$$h_i^f = f_q^f h_i^q + (1 - f_q^f) h_i^g$$

$$h_i^c = f_q^c h_i^q + (1 - f_q^c) h_i^g$$

Jet flavour defined by hardest parton geometrically associated to the jet: many theory issues, and potential sources of uncertainty

Extracted q/g-like fragmentation observables fit expectations:



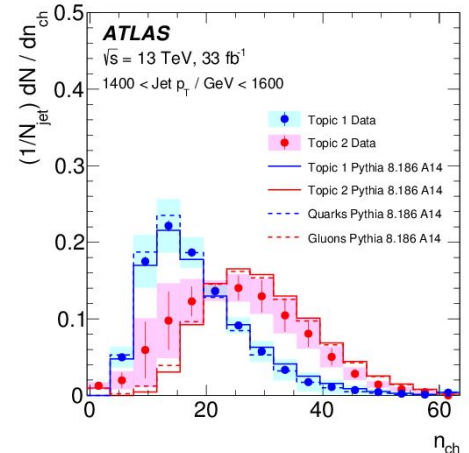
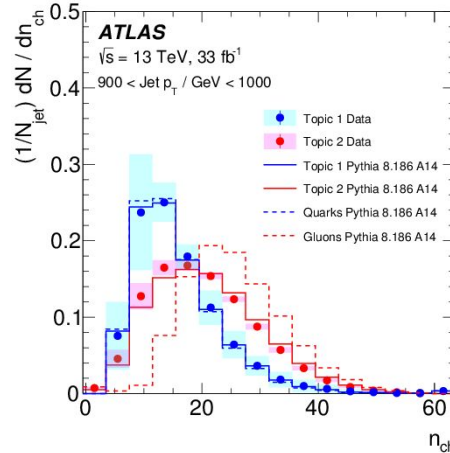
Model-independent quark/gluon jet characterisation

Novel approach is to use “topic modeling” extraction.

The categories are defined by data rather than MC internals:

$$h_i^{T_1} = \frac{h_i^f - \left(\min_j \{ h_j^f / h_j^c \} \right) \times h_i^c}{1 - \min_j h_j^f / h_j^c}$$

$$h_i^{T_2} = \frac{h_i^c - \left(\min_j \{ h_j^c / h_j^f \} \right) \times h_i^f}{1 - \min_j h_j^c / h_j^f}$$

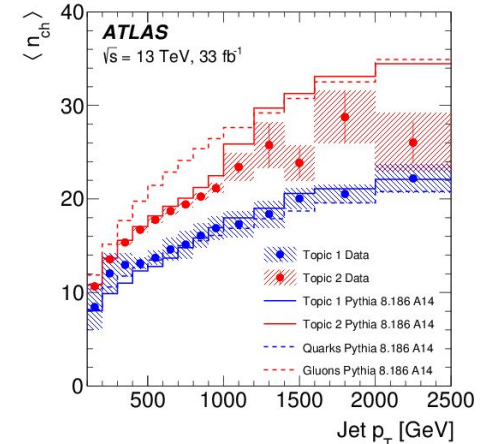
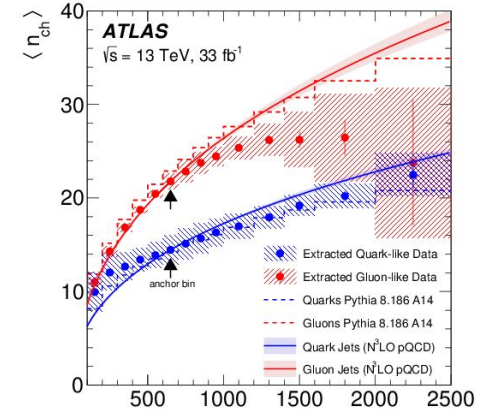
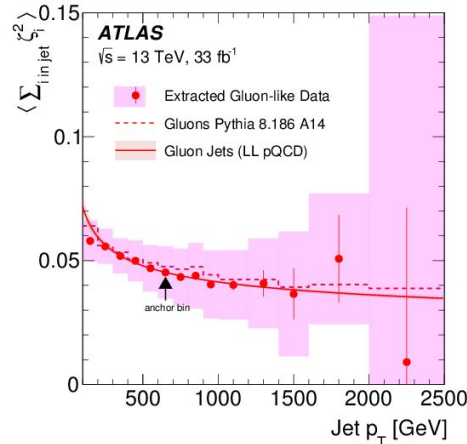
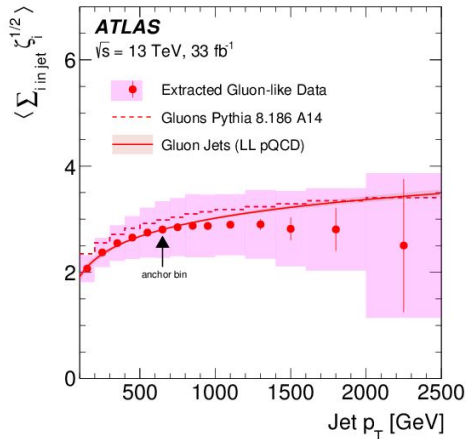


Interesting new approach. Limitation: alignment of topics to q and g template ideas relies on the existence of bins dominated by q or g: **applies to n_{ch} distribution only**

Comparing quark/gluon jet characterisations

Pythia-based vs topic modeling: good description by Pythia for quarks in both; less good for gluons. “Quark” topic also aligns well with quarks, worse for gluons.

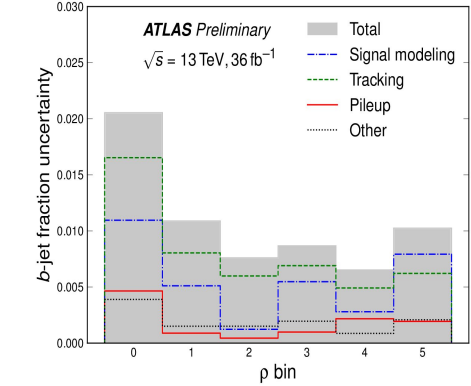
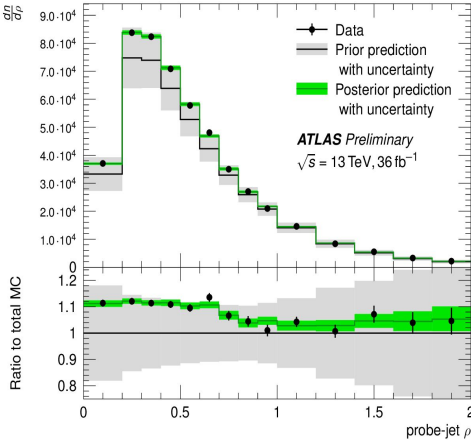
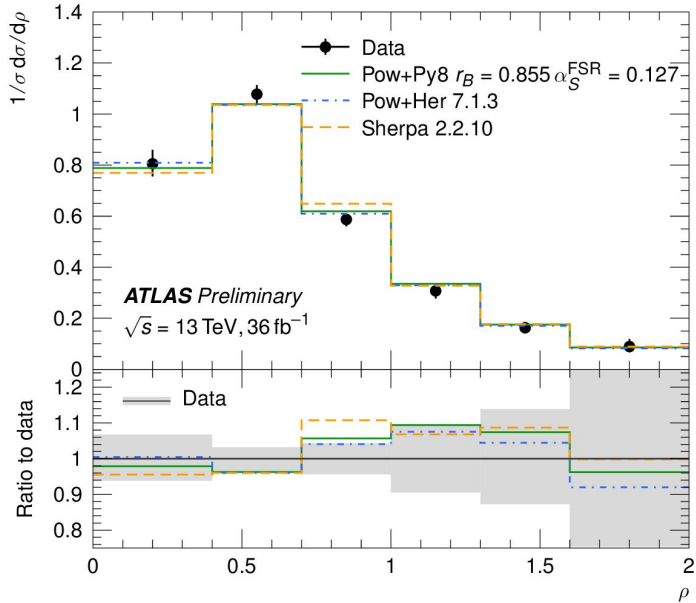
pQCD normalization-anchored, since can't handle non-perturbative physics: compares well to q/g extractions



ATLAS b -fragmentation

ρ moment

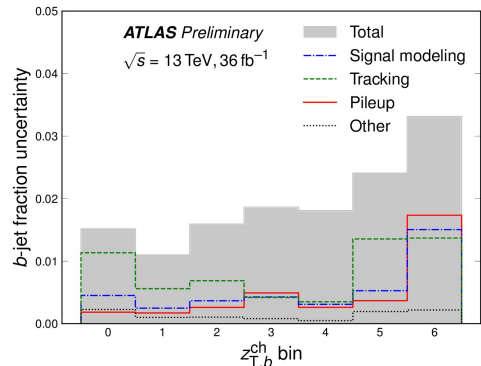
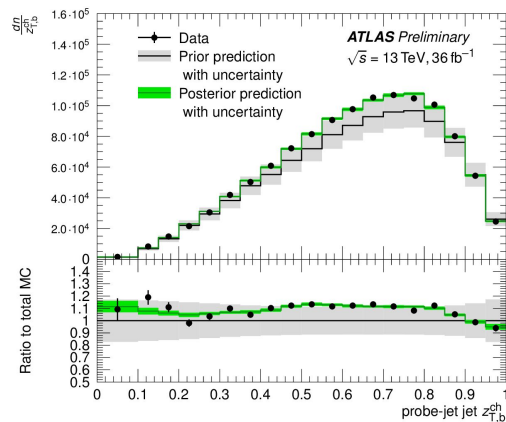
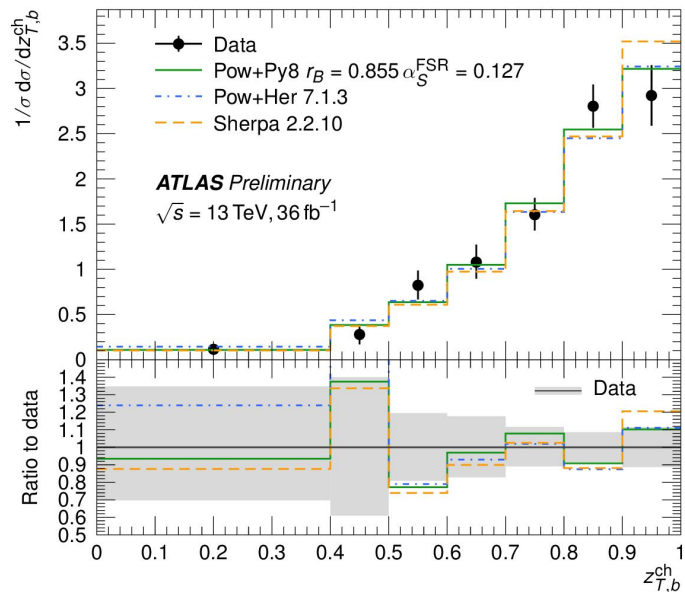
- Ratio of b -hadron p_T to average of charged lepton p_T 's — comparison of the b momentum to the tt parent event scale
- Lepton p_T more precisely measurable than b -jets or tt
- Sensitive to QCD radiation not contained in the b -jets



ATLAS b -fragmentation

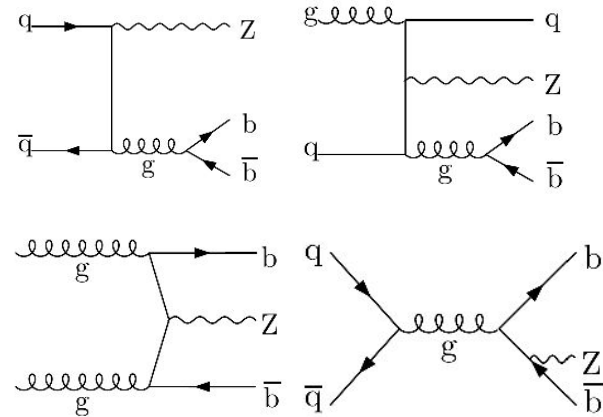
$z_{ch,T}$ (transverse) moment

- $p_{T,rel}$ (projected p_T wrt the parent jet axis) proved difficult to measure
- Correlated with longitudinal projection, plus some residual information about directional kicks from radiation

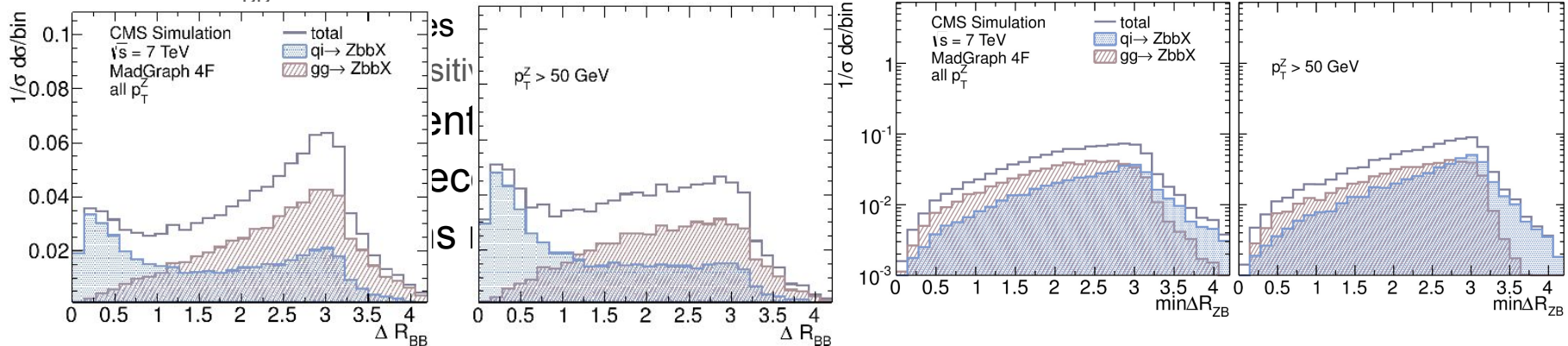


CMS Z+BB cross sections at 7 TeV

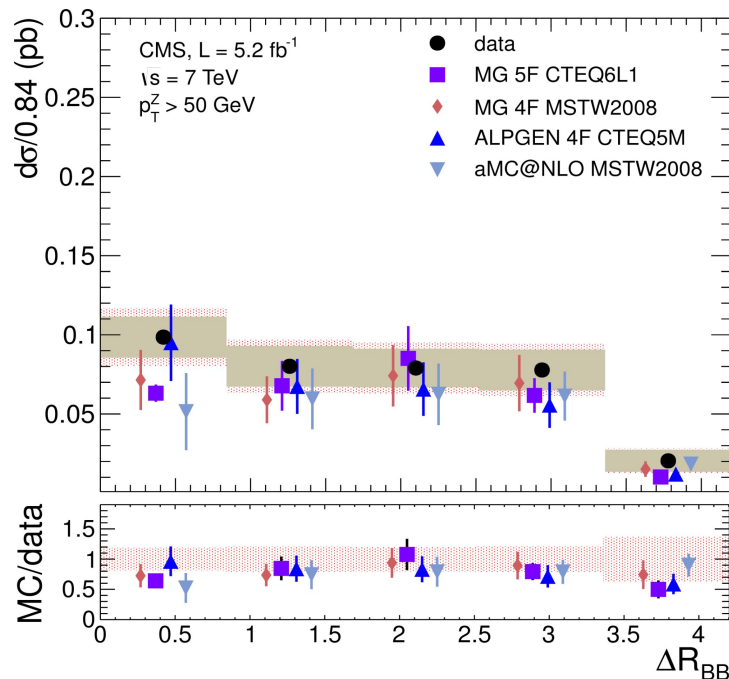
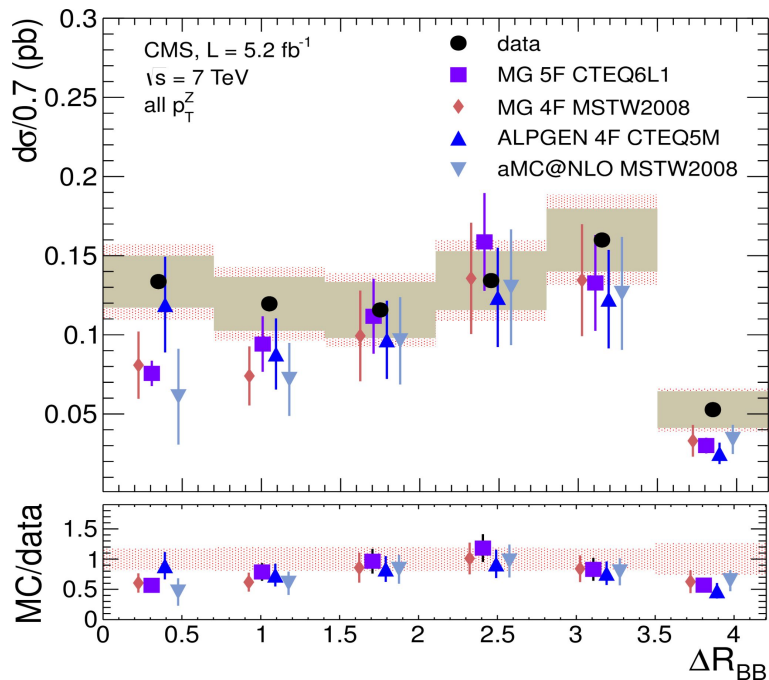
- Measure the production of a Z boson in association with B hadrons as a function of angular correlation especially the B-hadron pair production at small angular separation where there are significant theoretical uncertainties in the description of collinear production



○ ΔR_{BB} direct test of the modeling of different $pp \rightarrow ZbbX$

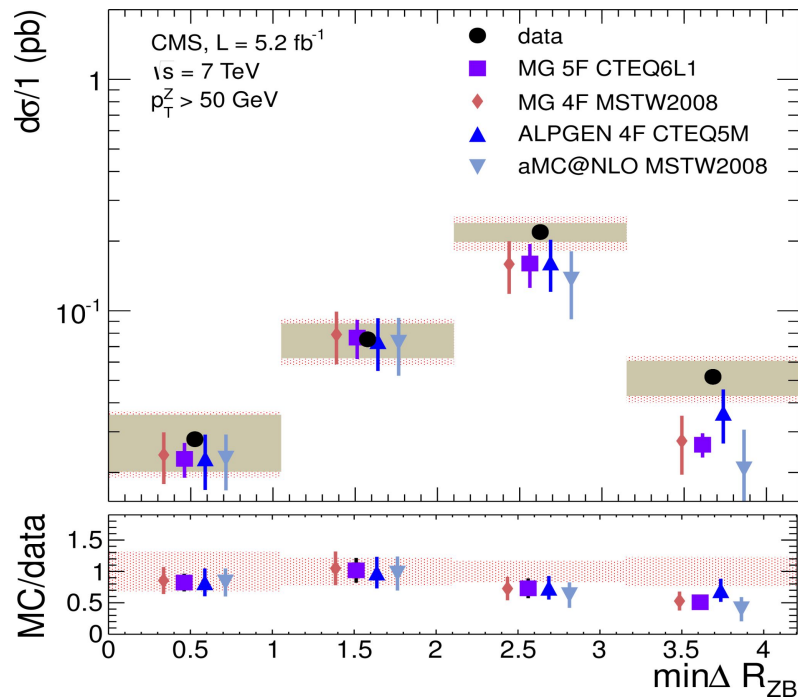
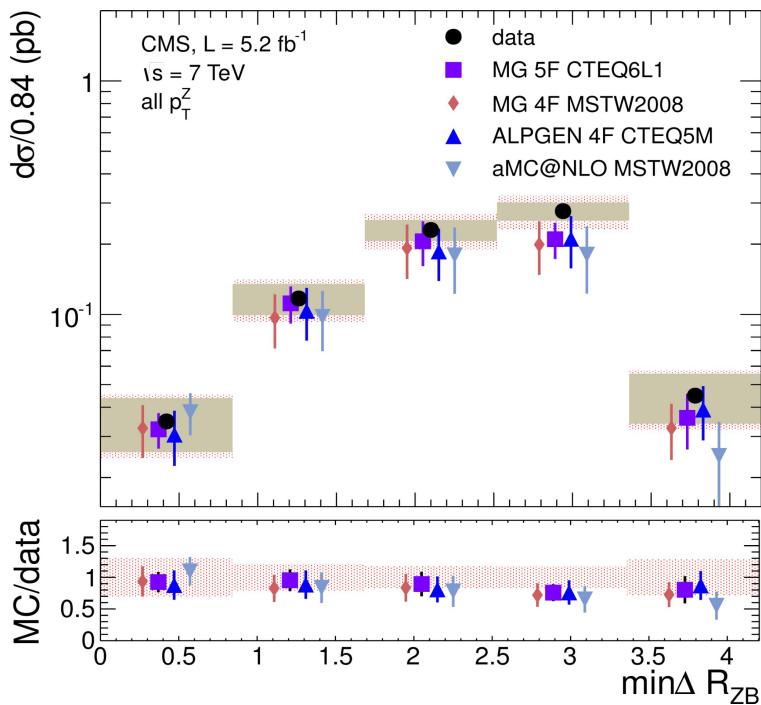


CMS $Z+BB$ cross sections at 7 TeV



- ALPGEN well describes data in collinear regions ($\Delta R_{BB} < 0.7$) while MADGRAPH and amc@NLO are lower than data
- At large ΔR_{BB} , all predictions agree with data

CMS $Z+BB$ cross sections at 7 TeV

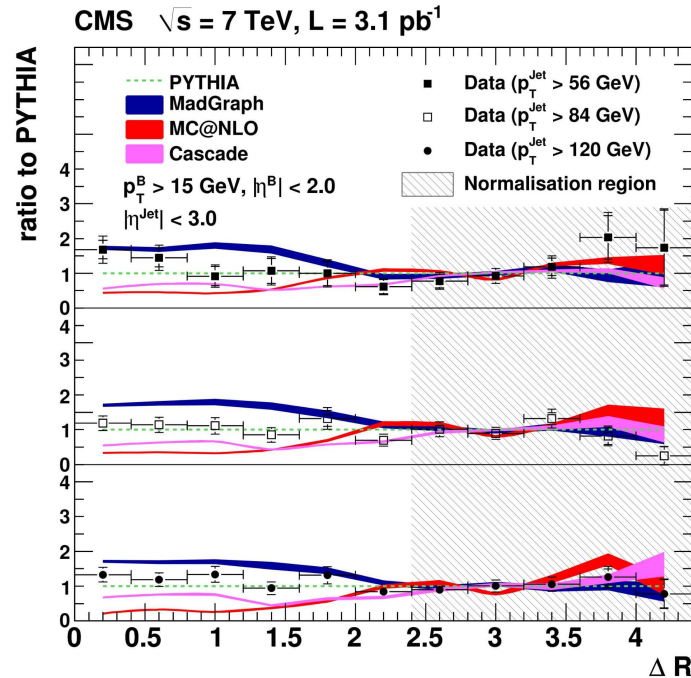


- Data are consistent with predictions in $\min\Delta R_{ZBB}$ except for region above 2

CMS angular correlations between BB at 7 TeV

JHEP03 (2011) 136

- BB production at 7 TeV
- B hadrons are identified using reconstructed secondary vertex \rightarrow probe small separation angle
- Simulation is normalized to regions > 2.4

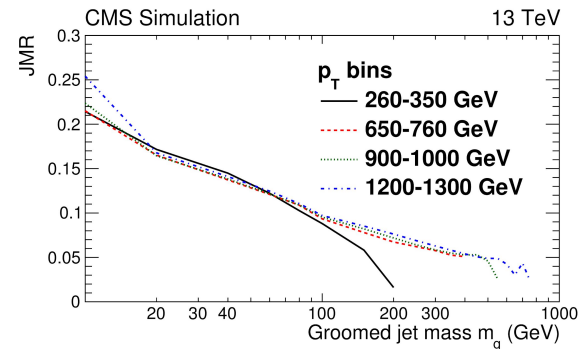
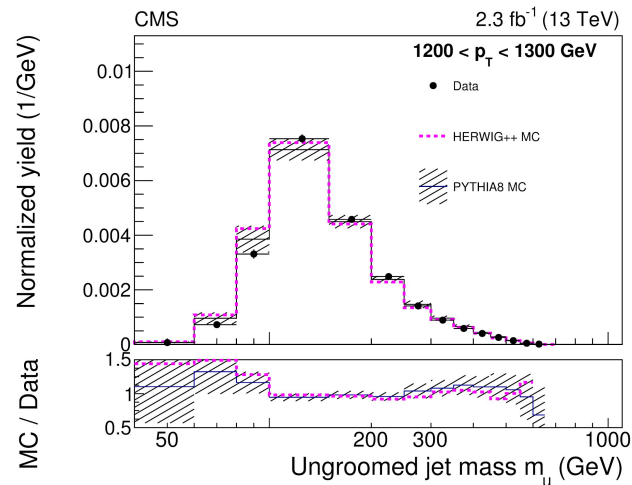


- None of the predictions describe the data very well
- mc@NLO mismodels at small angle where gluon splitting is significant

CMS jet mass in dijet events at 13 TeV

arXiv:1807.05974

Uses 33 fb^{-1} dataset of 13 TeV pp collisions



CMS jet mass in dijet events at 13 TeV

arXiv:1807.05974

Uses 33 fb⁻¹ dataset of 13 TeV pp collisions

