

Interpretation of the LHCb P_c States as Hadronic Molecules and Hints of a Narrow $P_c(4380)$

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Three hidden-charm pentaquark P_c states, $P_c(4312)$, $P_c(4440)$, and $P_c(4457)$ were revealed in the $\Lambda_b^0 \rightarrow J/\psi p K^-$ process measured by LHCb using both run I and run II data. Their nature is under lively discussion, and their quantum numbers have not been determined. We analyze the $J/\psi p$ invariant mass distributions under the assumption that the crossed-channel effects provide a smooth background. For the first time, such an analysis is performed employing a coupled-channel formalism with the scattering potential involving both one-pion exchange as well as short-range operators constrained by heavy quark spin symmetry. We find that the data can be well described in the hadronic molecular picture, which predicts seven $\Sigma_c^{(*)}\bar{D}^{(*)}$ molecular states in two spin multiplets, such that the $P_c(4312)$ is mainly a $\Sigma_c\bar{D}$ bound state with $J^P = 1/2^-$, while $P_c(4440)$ and $P_c(4457)$ are $\Sigma_c\bar{D}^*$ bound states with quantum numbers $3/2^-$ and $1/2^-$, respectively. We also show that there is evidence for a narrow $\Sigma_c^*\bar{D}$ bound state in the data which we call $P_c(4380)$, different from the broad one reported by LHCb in 2015. With this state included, all predicted $\Sigma_c\bar{D}$, $\Sigma_c^*\bar{D}$, and $\Sigma_c\bar{D}^*$ hadronic molecules are seen in the data, while the missing three $\Sigma_c^*\bar{D}^*$ states are expected to be found in future runs of the LHC or in photoproduction experiments.

Introduction.—The confinement property of quantum chromodynamics (QCD) in principle allows for the existence of a large variety of color neutral objects. However, it is not clear yet which configurations are realized in nature. As a result, searching for multi-quark exotic hadrons beyond the conventional quark model has been one of the central issues in the study of the strong interactions. Tremendous developments have been made in the new era since 2003 when the B factories discovered the $D_{s0}^*(2317)$ [1] and $X(3872)$ [2], whose properties are in notable contradiction with quark model predictions. The interest in studying such exotic hadrons was further boosted by the LHCb discovery of the hidden-charm pentaquarks $P_c(4450)$ and $P_c(4380)$ decaying into $J/\psi p$ in the $\Lambda_b^0 \rightarrow K^- J/\psi p$ process in 2015 [3]. The experimental and theoretical efforts are summarized in a number of comprehensive reviews [4–16]. When LHCb updated their measurements with a one-order-of-magnitude larger data sample [17], the narrow $P_c(4450)$ appeared to be split into two narrower structures $P_c(4440)$ and $P_c(4457)$, and a third narrow peak $P_c(4312)$ showed up. At the same time, the broad $P_c(4380)$ (whose existence needs to be verified in a complete amplitude analysis that is

under way) lost its significance. A cornucopia of theoretical interpretations followed these new discoveries, including models of hadronic molecules [18–39], compact pentaquark states [40–45], and hadrocharmonia [46]. An amplitude analysis was performed in Ref. [47] focusing on the $P_c(4312)$ which was suggested to be a virtual state. Among the explanations, the hadronic molecular model stands out as it explains all of the three narrow P_c states simultaneously as $\Sigma_c\bar{D}$ [for $P_c(4312)$ and $\Sigma_c\bar{D}^*$ [for $P_c(4440)$ and $P_c(4457)$] bound states, see, e.g., Refs. [21, 26, 32], employing the approximate heavy quark spin symmetry (HQSS) of QCD. However, the model predicts in addition four more states, including one $\Sigma_c^*\bar{D}$ state at around 4.37 to 4.38 GeV and three states slightly below the $\Sigma_c^*\bar{D}^*$ threshold. These seven P_c states are contained in two heavy quark spin multiplets, labeled as j_ℓ^P , with j_ℓ and P the total angular momentum of the light degrees of freedom and parity, respectively: three with $j_\ell^P = \frac{1}{2}^-$ and four with $j_\ell^P = \frac{3}{2}^-$. States in these two multiplets with the same spin mix because the $\Sigma_c(\bar{D})$ is not degenerate with the $\Sigma_c^*(\bar{D}^*)$. While only three of the states correspond to the ones reported by

LHCb, it is crucial to check whether the existence of the whole two multiplets is consistent with the $J/\psi p$ distribution measured by LHCb. This is the question addressed in this Letter: by constructing coupled-channel amplitudes analogous to those used in the analysis of the Z_b states [48–51], we show that the observed $J/\psi p$ invariant mass distribution can be well described in the hadronic molecular scenario with seven $\Sigma_c^{(*)}\bar{D}^{(*)}$ molecules, where the $P_c(4312)$ and $P_c(4440)/P_c(4457)$ are $\Sigma_c\bar{D}$ and $\Sigma_c\bar{D}^*$ bound states, respectively. For the first time, we point out a clear signal from data for the existence of a narrow $P_c(4380)$ as a $\Sigma_c^*\bar{D}$ bound state. The three predicted $\Sigma_c^*\bar{D}^*$ states still await discovery. In addition, we emphasize that the inclusion of the one-pion exchange (OPE) allows one to single out a unique solution corresponding to the global minimum instead of two equivalent solutions present in the pure contact case.

Framework.— In order to describe the measured $J/\psi p$ distribution, we construct coupled-channel amplitudes considering all the $\Sigma_c^{(*)}\bar{D}^{(*)}$ channels (called elastic channels [48, 49], since their thresholds are close to the P_c masses) and the $J/\psi p$ channels (inelastic channels). HQSS is used to relate all the $\Sigma_c^{(*)}\bar{D}^{(*)}$ channels [21, 32, 52, 53], and their couplings to the $J/\psi p$ [31, 32]. We also allow for additional inelastic channels not included explicitly in the amplitudes. To this end, we expand the two-particle states in the basis of HQSS eigenstates $|s_Q \otimes j_\ell\rangle$, with s_Q and j_ℓ representing the total spin of the heavy quarks and total angular momentum of light degrees of freedom, respectively. In this notation, the $\Sigma^{(*)}$ and $\bar{D}^{(*)}$ spin multiplets are $|\frac{1}{2} \otimes 1\rangle$ and $|\frac{1}{2} \otimes \frac{1}{2}\rangle$, respectively. One can rewrite the S -wave $\Sigma_c^{(*)}\bar{D}^{(*)}$ systems in terms of $|s_Q \otimes j_\ell\rangle$ as [32, 52]

$$\begin{pmatrix} |\Sigma_c\bar{D}\rangle \\ |\Sigma_c\bar{D}^*\rangle \\ |\Sigma_c^*\bar{D}^*\rangle \end{pmatrix}_{\frac{1}{2}} = \begin{pmatrix} \frac{1}{2} & \frac{-1}{2\sqrt{3}} & \sqrt{\frac{2}{3}} \\ \frac{-1}{2\sqrt{3}} & \frac{5}{6} & \frac{\sqrt{2}}{3} \\ \sqrt{\frac{2}{3}} & \frac{\sqrt{2}}{3} & -\frac{1}{3} \end{pmatrix} \begin{pmatrix} |0 \otimes \frac{1}{2}\rangle \\ |1 \otimes \frac{1}{2}\rangle \\ |1 \otimes \frac{3}{2}\rangle \end{pmatrix}, \quad (1)$$

$$\begin{pmatrix} |\Sigma_c\bar{D}^*\rangle \\ |\Sigma_c^*\bar{D}\rangle \\ |\Sigma_c^*\bar{D}^*\rangle \end{pmatrix}_{\frac{3}{2}} = \begin{pmatrix} \frac{-1}{\sqrt{3}} & \frac{1}{3} & \frac{\sqrt{5}}{3} \\ \frac{1}{2} & \frac{-1}{\sqrt{3}} & \frac{1}{2}\sqrt{\frac{5}{3}} \\ \frac{1}{2}\sqrt{\frac{5}{3}} & \frac{\sqrt{5}}{3} & \frac{1}{6} \end{pmatrix} \begin{pmatrix} |0 \otimes \frac{3}{2}\rangle \\ |1 \otimes \frac{1}{2}\rangle \\ |1 \otimes \frac{3}{2}\rangle \end{pmatrix}, \quad (2)$$

$$|\Sigma_c^*\bar{D}^*\rangle_{\frac{5}{2}} = |1 \otimes \frac{3}{2}\rangle, \quad (3)$$

where the subscripts on the left-hand side represent the total angular momentum $J = \frac{1}{2}, \frac{3}{2},$ and $\frac{5}{2}$. The rotation matrices in Eqs. (1)–(3) will be denoted as R^J in the following. One can obtain the contact terms for S -wave interactions of the elastic channels in terms of two

independent matrix elements,

$$C_{\frac{1}{2}} \equiv \langle s_Q \otimes \frac{1}{2} | \hat{\mathcal{H}}_I | s_Q \otimes \frac{1}{2} \rangle, \quad C_{\frac{3}{2}} \equiv \langle s_Q \otimes \frac{3}{2} | \hat{\mathcal{H}}_I | s_Q \otimes \frac{3}{2} \rangle,$$

with $\hat{\mathcal{H}}_I$ the effective Hamiltonian respecting HQSS. In the heavy quark limit, the contact interactions defined above are independent of $s_Q = 0, 1$. Since we work to leading order, the above matrix elements are constants. In particular, the D -wave $\Sigma_c^{(*)}\bar{D}^{(*)}$ contact terms, which turned out to be necessary in the study of the Z_b states [51], will be neglected since data in the inelastic channels are insensitive to such operators. The contact terms in the particle basis are

$$C_{\alpha\beta}^J = \sum_{n_J} R_{\alpha n_J}^J C_{j_\ell(n_J)} (R^J)_{n_J \beta}^T, \quad (4)$$

where $j_\ell(n_J)$ denotes the light-quark spin of the n th channel for a given J multiplet.

The OPE potential can be obtained using the effective Lagrangian for the axial coupling of the pions to the charmed mesons and baryons [54, 55]

$$\mathcal{L} = \frac{g}{4} \langle \boldsymbol{\sigma} \cdot \mathbf{u}_{ab} \bar{H}_b \bar{H}_a^\dagger \rangle - ig_1 \epsilon^{ijk} \text{Tr} [S_i^\dagger u_j S_k], \quad (5)$$

where $\langle \cdot \rangle$ and $\text{Tr}[\cdot]$ denote traces in the spinor and isospin spaces, respectively, $\boldsymbol{\sigma}$ represents the Pauli matrices, S_i and \bar{H} are the heavy quark spin doublets for ground states (Σ_c, Σ_c^*) and (\bar{D}, \bar{D}^*) [56],

$$\mathbf{S} = \frac{1}{\sqrt{3}} \boldsymbol{\sigma} \Sigma_c + \Sigma_c^*, \quad \bar{\mathbf{H}} = -\bar{D} + \boldsymbol{\sigma} \cdot \bar{D}^*, \quad (6)$$

$\mathbf{u} = -i\nabla\Phi/F_\pi + \mathcal{O}(\Phi^3)$, $\Phi = \boldsymbol{\tau} \cdot \boldsymbol{\pi}$ with $\boldsymbol{\tau}$ and $\boldsymbol{\pi}$ the Pauli matrices in the isospin space and the pion fields, in order, and $F_\pi = 92.1$ MeV is the pion decay constant. From the measured width of $D^{*+} \rightarrow D^0 \pi^+$ one gets $g = 0.57$ [57], and the coupling $g_1 = 0.42$ is taken from the lattice QCD calculation [58]. The OPE contributes to both S and D waves and can be important for describing the line shapes around thresholds [50, 51, 59].

Also the transitions between the elastic and inelastic channels can be related via HQSS. While the $|1 \otimes \frac{1}{2}\rangle$ component in Eqs. (1)–(3) couples to $J/\psi p$ in the S wave in the heavy quark limit, the $|1 \otimes \frac{3}{2}\rangle$ only couples to $J/\psi p$ in the D wave. We introduce two coupling strengths,

$$g_S \equiv \langle 1 \otimes \frac{1}{2} | \hat{\mathcal{H}}_I | J/\psi p \rangle_S, \quad g_{Dk^2} \equiv \langle 1 \otimes \frac{3}{2} | \hat{\mathcal{H}}_I | J/\psi p \rangle_D,$$

where k is the magnitude of the J/ψ three-momentum in the c.m. frame of $J/\psi p$. Then, the transition vertices $\mathcal{V}_{\alpha i}^J$ between the α th elastic and i th inelastic channel, with $i = 1, 2$ denoting the S -wave and D -wave $J/\psi p$, respectively, can be easily obtained by virtue of the de-

compositions in Eqs. (1)–(3) as

$$\begin{aligned} \mathcal{V}_{\alpha 1}^J &= g_S R_{\alpha 2}^J, & \mathcal{V}_{\alpha 2}^J(k) &= g_D k^2 R_{\alpha 3}^J, & J &= \frac{1}{2}, \frac{3}{2}, \\ \mathcal{V}_{\alpha 1}^J &= 0, & \mathcal{V}_{\alpha 2}^J(k) &= g_D k^2, & J &= \frac{5}{2}. \end{aligned} \quad (7)$$

The direct $J/\psi p$ interaction is Okubo-Zweig-Iizuka suppressed and found very weak in a recent lattice QCD study [60]. Thus, the inelastic $J/\psi p$ channel is only included through its coupling to the elastic channels [48–51, 61]. While the real part of its contribution can be absorbed by redefining the contact terms $C_{\alpha\beta}^J$ [51], the imaginary part cannot. We thus introduce

$$V_{J/\psi p, \alpha\beta}^J(E) = -\frac{i}{2\pi E} \sum_{j=1}^2 m_{J/\psi} m_p \mathcal{V}_{\alpha j}^J \mathcal{V}_{\beta j}^J k \quad (8)$$

into the effective elastic potential. It is expected that, in addition to the $J/\psi p$ channels, there are more inelastic channels, most prominently $\Lambda_c \bar{D}^{(*)}$ and η_{cp} [31, 62, 63]. While the latter is connected to the $J/\psi p$ channels via HQSS, the former is not and thus we are obliged to parametrize especially those via an additional imaginary part of the two contact terms. This introduces two more parameters. Thus the scattering problem contains in total 6 parameters and the full effective potential for the elastic channels can be written as

$$V^J(E, p, q) = C^J + V_{J/\psi p}^J(E) + V_{\text{OPE}}^J(E, p, q), \quad (9)$$

with q and p for the incoming and outgoing relative momenta of the corresponding channels, respectively, and E for the total energy. The explicit expressions for the matrix $V_{\text{OPE}}^J(E, p, q)$ are provided in Ref. [64].

For the weak production amplitude for $\Lambda_b \rightarrow K^- \Sigma_c^{(*)} \bar{D}^{(*)}$ we only consider the elastic $\Sigma_c^{(*)} \bar{D}^{(*)}$ channels produced in an S wave, since the energy region of interest is close to the $\Sigma_c^{(*)} \bar{D}^{(*)}$ thresholds. Then the weak production matrix elements may be expressed as $\mathcal{F}_n^J = \langle \Lambda_b | \hat{\mathcal{H}}_W | K^- (s_Q \otimes j_\ell)_n^J \rangle$, where $(s_Q \otimes j_\ell)_n^J$ refers to the n th state in the $|s_Q \otimes j_\ell\rangle$ basis in Eqs. (1)–(3). The production contact term for the α th elastic channel for a given J then reads

$$P_\alpha^J = \sum_n R_{\alpha n}^J \mathcal{F}_n^J. \quad (10)$$

In total, there are additional seven parameters \mathcal{F}_n^J .

With the above ingredients, one can obtain the production amplitude, U_α^J , for the α th elastic channel by solving the following Lippmann-Schwinger equations (LSEs),

$$U_\alpha^J(E, p) = P_\alpha^J - \sum_\beta \int \frac{d^3 \mathbf{q}}{(2\pi)^3} V_{\alpha\beta}^J(E, p, q) G_\beta(E, q) U_\beta^J(E, q), \quad (11)$$

and for the i th $J/\psi p$ inelastic channel U_i^J via

$$U_i^J(E, k) = - \sum_\beta \int \frac{d^3 \mathbf{q}}{(2\pi)^3} \mathcal{V}_{i\beta}^J(k) G_\beta(E, q) U_\beta^J(E, q). \quad (12)$$

The two-body propagator is

$$G_\beta(E, q) = \frac{2\mu_\beta}{q^2 - p_\beta^2 - i\epsilon}, \quad p_\beta^2 \equiv 2\mu_\beta(E - m_{\text{th}}^\beta), \quad (13)$$

with μ_β and m_{th}^β the reduced mass and the threshold of the β th elastic channel. The $\Sigma_c^{(*)}$ widths of 1.86 MeV (15 MeV) [57] are accounted for using a complex mass $m - i\Gamma/2$ in m_{th}^β . The LSE is regularized using a hard cutoff, varied in the range from 1 to 1.5 GeV. Since the results barely depend on its value (effects of the cutoff variation can be largely absorbed into the refitted contact terms), the final results will be presented for the cutoff of 1 GeV. The equations given are unitary as long as the additional imaginary parts of the contact terms are omitted. Unitarity can be restored once data on the $\Lambda_c \bar{D}^{(*)}$ channels are available, and we checked that introducing the $\Lambda_c \bar{D}^*$ channel in the way of Eq. (8) did not produce a sizable difference.

In order to fit the $J/\psi p$ invariant mass distribution, an incoherent smooth background is used to model possible contributions from misidentified non- Λ_b^0 events, the Λ^* resonances coupled to pK^- , and possibly additional broad P_c^+ structures. Here we use the form

$$f_{\text{bgd}}(E) = b_0 + b_1 E^2 + b_2 E^4 + \left| \frac{g_r}{m^2 - E^2 - i\Gamma E} \right|^2, \quad (14)$$

which contains the parameters b_0 , b_1 , b_2 , g_r , m , and Γ . The backgrounds used in the experimental analysis [17] are also considered, and the results are similar, which will be included in the uncertainties. We perform fits employing the potential of Eq. (9) either omitting (scheme I) or including (scheme II) V_{OPE}^J .

Results and discussions.—In this analysis, we do not consider isospin symmetry breaking effects which can be important to give rise to isospin-breaking decay modes [20, 65] but have little effect on the description of the line shapes in the isospin-conserving $J/\psi p$ channel. Convolution with the experimental energy resolution is considered. For scheme I we find two solutions, denoted as A and B , describing the data almost equally well (with $\chi^2/\text{d.o.f.} = 1.01$ and 1.03 , respectively). The corresponding best fits are shown in the left panel of Fig. 1. The two solutions produce different values of the parameters, in particular $C_{\frac{1}{2}}$ and $C_{\frac{3}{2}}$ (in fact, the values of $C_{\frac{1}{2}}$ and $C_{\frac{3}{2}}$ in solution A are very close to those of $C_{\frac{3}{2}}$ and $C_{\frac{1}{2}}$ in solution B, respectively), and thus give different pole locations. However, both solutions give seven poles in the $\Sigma_c^{(*)} \bar{D}^{(*)}$ scattering amplitudes, i.e., seven P_c states: three with $J = 1/2$, three with $J = 3/2$ and one with

TABLE I. The names of the states, their quantum numbers found from the fits within scheme II, the pole positions (on the sheets close to the physical one), the dominant channels (DCs) and their thresholds, the dimensionless couplings of the resonances in the DCs (from the T -matrix residues and defined as G_{DC}), and the resonance couplings to the source derived from the residues, which are normalized by the event numbers and thus only the relative values are meaningful. The uncertainties given are from taking different backgrounds, the uncertainties from the fit for a given background are negligible. The $P_c(4380)$ in boldface is the new state we advocate in this work.

Scheme II	J^P	Pole [MeV]	DC (threshold [MeV])	G_{DC}	Production
$P_c(4312)$	$\frac{1}{2}^-$	$4314(2) - 5(2)i$	$\Sigma_c \bar{D}$ (4321.6)	$2.86(12) - 0.44(24)i$	$636(73) - 98(53)i$
$P_c(4380)$	$\frac{3}{2}^-$	$4378(2) - 13(3)i$	$\Sigma_c^* \bar{D}$ (4386.2)	$3.00(12) - 0.49(27)i$	$618(373) - 181(95)i$
$P_c(4440)$	$\frac{3}{2}^-$	$4441(2) - 11(3)i$	$\Sigma_c \bar{D}^*$ (4462.1)	$3.91(11) - 0.62(19)i$	$999(140) - 15(18)i$
$P_c(4457)$	$\frac{1}{2}^-$	$4459(2) - 4(1)i$	$\Sigma_c \bar{D}^*$ (4462.1)	$2.09(17) - 0.46(18)i$	$-918(68) + 159(78)i$
P_c	$\frac{1}{2}^-$	$4524(2) - 9(1)i$	$\Sigma_c^* \bar{D}^*$ (4526.7)	$1.90(23) - 0.28(21)i$	$-228(384) + 22(23)i$
P_c	$\frac{3}{2}^-$	$4518(2) - 11(2)i$	$\Sigma_c^* \bar{D}^*$ (4526.7)	$2.83(16) - 0.43(18)i$	$-156(517) - 58(43)i$
P_c	$\frac{5}{2}^-$	$4498(5) - 35(17)i$	$\Sigma_c^* \bar{D}^*$ (4526.7)	$4.66(55) - 1.12(32)i$	$-393(620) - 2(26)i$

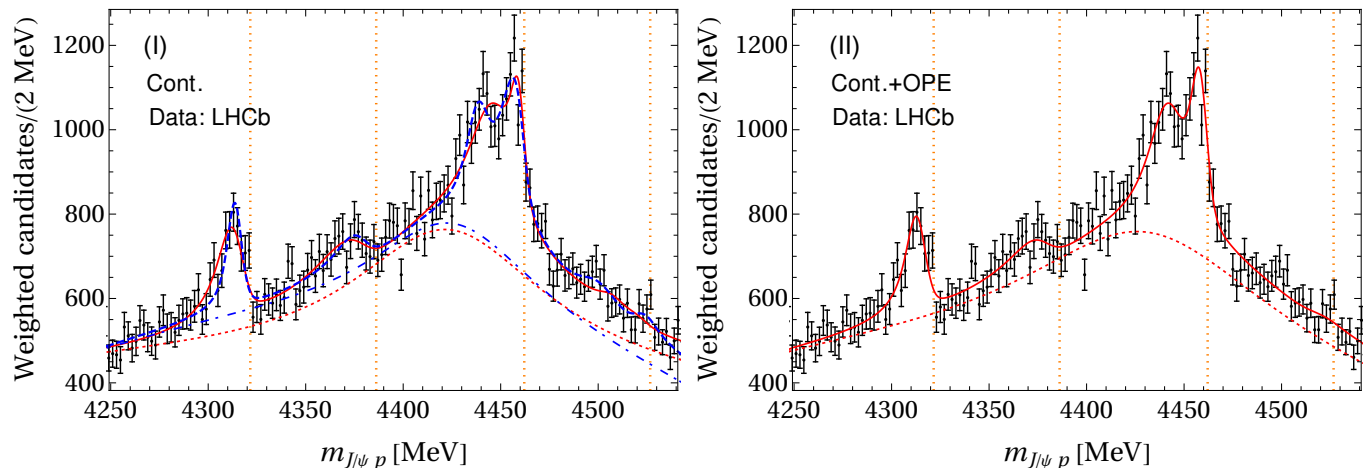


FIG. 1. Left panel: the fitted invariant mass distributions versus the weighted experimental data [17] for both solution A (blue dashed curves) and solution B (red solid ones) of scheme I. The corresponding backgrounds are shown as blue dash-dotted and red dotted curves, respectively. Right panel: the best fit for scheme II with the dotted curve representing the background. The vertical dashed lines in both panels from left to right are the $\Sigma_c \bar{D}$, $\Sigma_c^* \bar{D}$, $\Sigma_c \bar{D}^*$, and $\Sigma_c^* \bar{D}^*$ thresholds, respectively.

$J = 5/2$. The masses of the generated P_c states in solutions A and B are close to those of scenarios A and B for the corresponding quantum numbers in Refs. [21, 32], respectively, though the widths are larger due to the inelastic channels and the $\Sigma_c^{(*)}$ widths, and thus are not shown here.

In both solutions, among the seven poles, the lowest one corresponds to the $P_c(4312)$ with $\frac{1}{2}^-$, and is a $\Sigma_c \bar{D}$ bound state: it is located in the second Riemann sheet (of the $J/\psi p$ channel), and would become a real bound state pole in the first Riemann sheet if the $J/\psi p$ channel were switched off. This is different from the virtual state scenario of $\Sigma_c \bar{D}$ in Ref. [47] which only fits to data around the $\Sigma_c \bar{D}$ threshold.

There are two $\Sigma_c \bar{D}^*$ bound states with quantum numbers $\frac{1}{2}^-$ and $\frac{3}{2}^-$, corresponding to the $P_c(4440)$ and the $P_c(4457)$, respectively, in solution A and interchanged

in solution B . The mass pattern of the three P_c states dominated by the $\Sigma_c^* \bar{D}^*$ channel is analogous to that of the $\Sigma_c \bar{D}^*$ channel, i.e., $m_{\frac{1}{2}^-} < m_{\frac{3}{2}^-} < m_{\frac{5}{2}^-}$ for solution A and the opposite for solution B . In both solutions, there is a narrow pole around 4.38 GeV whose dominant component is $\Sigma_c^* \bar{D}$ (see also Ref. [26]). This means that HQSS requires the existence of a $P_c(4380)$ resonance which, however, is narrow and thus different from the broad resonance reported by LHCb in 2015 [3].

In scheme II the OPE is included. The importance of its tensor force is well known for the nucleon-nucleon interaction. It leads to the mixing between S and D waves and can have a sizable impact on the line shape between thresholds [50, 51, 59]. Unlike in scheme I, once the full OPE is included, there is only one solution corresponding to the best fit with $\chi^2/\text{d.o.f.} = 0.98$, shown in the right panel of Fig. 1. It leads to poles presented

in Table I which are similar to those in solution *B* of scheme I (see also Refs. [35, 66]). The pole positions, the dominant channels (DCs) having the largest effective couplings (derived from residues of the T matrix), and effective couplings of these are listed in Table I. The results are insensitive to the form of the background, and the effects of using different backgrounds give the errors in Table I (the statistical errors propagating from the data are much smaller).

One sees that the $P_c(4312)$ couples dominantly to $\Sigma_c \bar{D}$ with $J^P = \frac{1}{2}^-$, and both the $P_c(4440)$ and $P_c(4457)$ couple dominantly to the $\Sigma_c \bar{D}^*$ with quantum numbers $\frac{3}{2}^-$ and $\frac{1}{2}^-$, respectively. They are all bound state poles and should be understood as hadronic molecules of the corresponding channels [11]. Comparing the fits from scheme I and scheme II, one sees that the OPE helps making the dip between the $P_c(4440)$ and $P_c(4457)$ more evident. In both schemes there is a narrow $P_c(4380)$ located at the right position where the data show a peak, though less prominent than those of the well-known three P_c states. Its existence and properties are a consequence of HQSS in the hadronic molecular picture. We have checked that it persists no matter whether or not the data around 4.38 GeV are included in the fit. The absolute value of the production strength of the $P_c(4380)$ shown in the last column of the table differs from zero by 1.7σ which might be taken as a measure of the significance of this resonance in the data. The three $\Sigma_c^* \bar{D}^*$ molecules, which are expected to exist [21, 32, 37, 52, 53], do not have any unambiguous signal in the data. Their production strengths related to the residues of the production amplitude U_α^J at the pole suggest that they are less strongly produced in Λ_b decays. One possible reason could be that the production of the three most pronounced P_c structures gets enhanced by nearby triangle singularities discussed in Refs. [17, 67–69].

Summary and outlook.—In summary, we investigated for the first time whether the appealing hadronic molecular model for the observed P_c states is consistent with the LHCb data. A coupled-channel formalism is used to analyze the $J/\psi p$ invariant mass distribution, which contains much more information than the extracted pentaquark masses only. The relevant effective potential constructed based on HQSS involves all transitions between the elastic $\Sigma_c^{(*)} \bar{D}^{(*)}$ channels, transitions from the elastic to the S - and D -wave $J/\psi p$ inelastic channels as well as the coupling to additional effective inelastic channels. We find that the data can be well described. In addition to the three established states, in our analysis a narrow $P_c(4380)$ state, identified as a $\frac{3}{2}^- \Sigma_c \bar{D}$ molecule, with its properties fixed by HQSS, shows up as a clear signal in the data. The three $\Sigma_c^* \bar{D}^*$ bound states with masses from around 4.49 to 4.52 GeV are almost invisible because of their relatively low production rates in the Λ_b decays. We expect that they can be resolved in the forth-

coming data to be collected at the LHC run-3 period or other production processes, such as the J/ψ photoproduction [63, 70–78]. It should be stressed that, if the P_c states indeed are hadronic molecules, they have to show up as prominent structures also in the elastic channels, and data for those would therefore be extremely valuable. To further refine our approach, data are needed in the $\Lambda_c \bar{D}^{(*)}$ as well as in the $\eta_c p$ channels. The latter would provide additional information on the amount of spin symmetry violation in the system. All these studies will shed important light on our understanding of how QCD forms hadrons.

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Interpretation of the LHCb P_c States as Hadronic Molecules and Hints of a Narrow $P_c(4380)$

Supplementary Material

Contact Potentials

The decompositions of the S -wave $\Sigma_c^{(*)}\bar{D}^{(*)}$ two-body systems in terms of the heavy and light degrees of freedom $|s_Q \otimes j_\ell\rangle$ are

$$\begin{aligned}
|\Sigma_c\bar{D}\rangle_{\frac{1}{2}^-} &= \frac{1}{2} \left| 0 \otimes \frac{1}{2} \right\rangle - \frac{1}{2\sqrt{3}} \left| 1 \otimes \frac{1}{2} \right\rangle + \sqrt{\frac{2}{3}} \left| 1 \otimes \frac{3}{2} \right\rangle, \\
|\Sigma_c\bar{D}^*\rangle_{\frac{1}{2}^-} &= -\frac{1}{2\sqrt{3}} \left| 0 \otimes \frac{1}{2} \right\rangle + \frac{5}{6} \left| 1 \otimes \frac{1}{2} \right\rangle + \frac{\sqrt{2}}{3} \left| 1 \otimes \frac{3}{2} \right\rangle, \\
|\Sigma_c^*\bar{D}\rangle_{\frac{1}{2}^-} &= \sqrt{\frac{2}{3}} \left| 0 \otimes \frac{1}{2} \right\rangle + \frac{\sqrt{2}}{3} \left| 1 \otimes \frac{1}{2} \right\rangle - \frac{1}{3} \left| 1 \otimes \frac{3}{2} \right\rangle, \\
|\Sigma_c\bar{D}^*\rangle_{\frac{3}{2}^-} &= -\frac{1}{\sqrt{3}} \left| 0 \otimes \frac{3}{2} \right\rangle + \frac{1}{3} \left| 1 \otimes \frac{1}{2} \right\rangle + \frac{\sqrt{5}}{3} \left| 1 \otimes \frac{3}{2} \right\rangle, \\
|\Sigma_c^*\bar{D}\rangle_{\frac{3}{2}^-} &= \frac{1}{2} \left| 0 \otimes \frac{3}{2} \right\rangle - \frac{1}{\sqrt{3}} \left| 1 \otimes \frac{1}{2} \right\rangle + \frac{1}{2} \sqrt{\frac{5}{3}} \left| 1 \otimes \frac{3}{2} \right\rangle, \\
|\Sigma_c^*\bar{D}^*\rangle_{\frac{3}{2}^-} &= \frac{1}{2} \sqrt{\frac{5}{3}} \left| 0 \otimes \frac{3}{2} \right\rangle + \frac{1}{3} \sqrt{5} \left| 1 \otimes \frac{1}{2} \right\rangle + \frac{1}{6} \left| 1 \otimes \frac{3}{2} \right\rangle, \\
|\Sigma_c^*\bar{D}^*\rangle_{\frac{5}{2}^-} &= \left| 1 \otimes \frac{3}{2} \right\rangle,
\end{aligned}$$

where the subindex is the total angular momentum, and s_Q and j_ℓ represent the total spin of the heavy quarks and total angular momentum of light degrees of freedom, respectively.

By defining the contact potentials

$$C_{\frac{1}{2}} \equiv \left\langle s_Q \otimes \frac{1}{2} \left| \hat{H}_I \right| s_Q \otimes \frac{1}{2} \right\rangle, \quad C_{\frac{3}{2}} \equiv \left\langle s_Q \otimes \frac{3}{2} \left| \hat{H}_I \right| s_Q \otimes \frac{3}{2} \right\rangle,$$

one can obtain the effective contact potentials as

$$V_{\frac{1}{2}^-}^C = \begin{pmatrix} \frac{1}{3}C_{\frac{1}{2}} + \frac{2}{3}C_{\frac{3}{2}} & -\frac{2}{3\sqrt{3}}C_{\frac{1}{2}} + \frac{2}{3\sqrt{3}}C_{\frac{3}{2}} & \frac{1}{3}\sqrt{\frac{2}{3}}C_{\frac{1}{2}} - \frac{1}{3}\sqrt{\frac{2}{3}}C_{\frac{3}{2}} \\ -\frac{2}{3\sqrt{3}}C_{\frac{1}{2}} + \frac{2}{3\sqrt{3}}C_{\frac{3}{2}} & \frac{7}{9}C_{\frac{1}{2}} + \frac{2}{9}C_{\frac{3}{2}} & \frac{\sqrt{2}}{9}C_{\frac{1}{2}} - \frac{\sqrt{2}}{9}C_{\frac{3}{2}} \\ \frac{1}{9}\sqrt{\frac{2}{3}}C_{\frac{1}{2}} - \frac{1}{3}\sqrt{\frac{2}{3}}C_{\frac{3}{2}} & \frac{\sqrt{2}}{9}C_{\frac{1}{2}} - \frac{\sqrt{2}}{9}C_{\frac{3}{2}} & \frac{8}{9}C_{\frac{1}{2}} + \frac{1}{9}C_{\frac{3}{2}} \end{pmatrix}, \quad (15)$$

$$V_{\frac{3}{2}^-}^C = \begin{pmatrix} \frac{1}{9}C_{\frac{1}{2}} + \frac{8}{9}C_{\frac{3}{2}} & -\frac{1}{3\sqrt{3}}C_{\frac{1}{2}} + \frac{1}{3\sqrt{3}}C_{\frac{3}{2}} & \frac{\sqrt{5}}{9}C_{\frac{1}{2}} - \frac{\sqrt{5}}{9}C_{\frac{3}{2}} \\ -\frac{1}{3\sqrt{3}}C_{\frac{1}{2}} + \frac{1}{3\sqrt{3}}C_{\frac{3}{2}} & \frac{1}{3}C_{\frac{1}{2}} + \frac{2}{3}C_{\frac{3}{2}} & -\frac{1}{3}\sqrt{\frac{5}{3}}C_{\frac{1}{2}} + \frac{1}{3}\sqrt{\frac{5}{3}}C_{\frac{3}{2}} \\ \frac{\sqrt{5}}{9}C_{\frac{1}{2}} - \frac{\sqrt{5}}{9}C_{\frac{3}{2}} & -\frac{1}{3}\sqrt{\frac{5}{3}}C_{\frac{1}{2}} + \frac{1}{3}\sqrt{\frac{5}{3}}C_{\frac{3}{2}} & \frac{5}{9}C_{\frac{1}{2}} + \frac{4}{9}C_{\frac{3}{2}} \end{pmatrix}, \quad (16)$$

$$V_{\frac{5}{2}^-}^C = C_{\frac{3}{2}}. \quad (17)$$

One-pion-exchange potentials

Once the one-pion-exchange potentials (OPEs) are included, the mixing between the S -wave and D -wave needs to be considered. The quantum numbers of the $\Sigma_c^{(*)}\bar{D}^{(*)}$ systems taken into account in this work are listed in Table II.

TABLE II. Coupled channels for both the S - and D -wave $\Sigma_c^{(*)}\bar{D}^{(*)}$ systems. The subindices denote the total spin of the two particles.

J^P	S -wave	D -wave
$\left(\frac{1}{2}\right)^-$	$\Sigma_c\bar{D}, \Sigma_c\bar{D}^*, \Sigma_c^*\bar{D}^*$	$\Sigma_c\bar{D}^*, \Sigma_c^*\bar{D}, (\Sigma_c^*\bar{D}^*)_{\frac{3}{2}}, (\Sigma_c^*\bar{D}^*)_{\frac{5}{2}}$
$\left(\frac{3}{2}\right)^-$	$\Sigma_c\bar{D}^*, \Sigma_c^*\bar{D}, \Sigma_c^*\bar{D}^*$	$\Sigma_c\bar{D}, (\Sigma_c\bar{D}^*)_{\frac{1}{2}}, (\Sigma_c\bar{D}^*)_{\frac{3}{2}}, \Sigma_c^*\bar{D}, (\Sigma_c^*\bar{D}^*)_{\frac{1}{2}}, (\Sigma_c^*\bar{D}^*)_{\frac{3}{2}}, (\Sigma_c^*\bar{D}^*)_{\frac{5}{2}}$
$\left(\frac{5}{2}\right)^-$	$\Sigma_c^*\bar{D}^*$	$\Sigma_c\bar{D}, (\Sigma_c\bar{D}^*)_{\frac{1}{2}}, (\Sigma_c\bar{D}^*)_{\frac{3}{2}}, \Sigma_c^*\bar{D}, (\Sigma_c^*\bar{D}^*)_{\frac{1}{2}}, (\Sigma_c^*\bar{D}^*)_{\frac{3}{2}}, (\Sigma_c^*\bar{D}^*)_{\frac{5}{2}}$

The isospin wave function for the P_c^+ is

$$P_c^+ = -\sqrt{\frac{1}{3}}\Sigma_c^{(*)+}\bar{D}^{(*)0} + \sqrt{\frac{2}{3}}\Sigma_c^{(*)++}D^{(*)-}. \quad (18)$$

The corresponding potential can be written as

$$\begin{aligned} V_{\Sigma_c^{(*)}\bar{D}^{(*)}} &= \frac{1}{3}V_{\Sigma_c^{(*)+}\bar{D}^{(*)0}\rightarrow\Sigma_c^{(*)+}\bar{D}^{(*)0}} + \frac{2}{3}V_{\Sigma_c^{(*)++}D^{(*)-}\rightarrow\Sigma_c^{(*)++}D^{(*)-}} \\ &\quad - \frac{\sqrt{2}}{3}V_{\Sigma_c^{(*)+}\bar{D}^{(*)0}\rightarrow\Sigma_c^{(*)++}D^{(*)-}} - \frac{\sqrt{2}}{3}V_{\Sigma_c^{(*)++}D^{(*)-}\rightarrow\Sigma_c^{(*)+}\bar{D}^{(*)0}} \\ &= 2V_{\Sigma_c^{(*)++}D^{(*)-}\rightarrow\Sigma_c^{(*)++}D^{(*)-}}, \end{aligned} \quad (19)$$

with

$$\begin{aligned} V_{\Sigma_c^{(*)+}\bar{D}^{(*)0}\rightarrow\Sigma_c^{(*)+}\bar{D}^{(*)0}} &= 0 \\ V_{\Sigma_c^{(*)++}D^{(*)-}\rightarrow\Sigma_c^{(*)++}D^{(*)-}} &= -\frac{1}{\sqrt{2}}V_{\Sigma_c^{(*)+}\bar{D}^{(*)0}\rightarrow\Sigma_c^{(*)++}D^{(*)-}} = -\frac{1}{\sqrt{2}}V_{\Sigma_c^{(*)++}D^{(*)-}\rightarrow\Sigma_c^{(*)+}\bar{D}^{(*)0}}. \end{aligned}$$

A state $|JM, L\Sigma\rangle$ with J (M) the total angular momentum (its third component), L the orbital angular momentum and Σ the total spin can be written as

$$|JM, L\Sigma\rangle = \frac{1}{\sqrt{4\pi}} \sum_{\sigma_1, \sigma_2, \Sigma_3, L_3} \int d\Omega_{\mathbf{p}} Y_L^{L_3}(\Omega_{\mathbf{p}}) \langle s_1 s_2 \sigma_1 \sigma_2 | \Sigma \Sigma_3 \rangle \langle L \Sigma L_3 \Sigma_3 | JM \rangle | \mathbf{p} \sigma_1 \sigma_2 \rangle \quad (20)$$

in terms of $| \mathbf{p} \sigma_1 \sigma_2 \rangle$, which is the direct product of the one-particle states $| \mathbf{p}, \sigma_1 \rangle$ and $| -\mathbf{p}, \sigma_2 \rangle$ with σ_i the third component of spin s_i for the i^{th} particle in that channel; \mathbf{p} is the momentum in the c.m. frame. In general, all the transitions between states with the same J need to be included with the transition matrix elements

$$T_{L\Sigma, L'\Sigma'}^J = \langle JM, L\Sigma | \hat{T} | JM, L'\Sigma' \rangle, \quad (21)$$

where \hat{T} is the transition operator. Furthermore, the partial-wave amplitude can be obtained through

$$\begin{aligned} T_{L\Sigma, L'\Sigma'}^J &= \frac{1}{4\pi} \sum_{\sigma_1 \sigma_2 \Sigma_3 L_3} \sum_{\sigma'_1 \sigma'_2 \Sigma'_3 L'_3} \int d\Omega_{\mathbf{p}} Y_L^{L_3}(\Omega_{\mathbf{p}}) \langle s_1 s_2 \sigma_1 \sigma_2 | \Sigma \Sigma_3 \rangle \langle L \Sigma L_3 \Sigma_3 | JM \rangle \\ &\quad \times \int d\Omega_{\mathbf{p}'} Y_{L'}^{L'_3}(\Omega_{\mathbf{p}'}) \langle s'_1 s'_2 \sigma'_1 \sigma'_2 | \Sigma' \Sigma'_3 \rangle \langle L' \Sigma' L'_3 \Sigma'_3 | JM \rangle \langle \mathbf{p}' \sigma'_1 \sigma'_2 | \hat{T} | \mathbf{p} \sigma_1 \sigma_2 \rangle. \end{aligned} \quad (22)$$

In the framework of the time-ordered perturbation theory (TOPT), the OPE potential acquires two contributions [50]. For the scattering process $12 \rightarrow 1'2'$ with E the total energy of the system, and p, \bar{p} the incoming and

outgoing three-momenta, we define

$$V_{SS}(E, p, \tilde{p}) \equiv \frac{1}{2} \int_{-1}^1 d \cos \theta \frac{\tilde{p}^2 + p^2 - 2\tilde{p}p \cos \theta}{2E_\pi(p_\pi)} [D_a^\pi(E, p, \tilde{p}, \theta) + D_b^\pi(E, p, \tilde{p}, \theta)], \quad (23)$$

$$V_{SD}(E, p, \tilde{p}) \equiv \frac{1}{2} \int_{-1}^1 d \cos \theta \frac{4\tilde{p}^2 + p^2 - 8\tilde{p}p \cos \theta + 3p^2 \cos 2\theta}{2E_\pi(p_\pi)} [D_a^\pi(E, p, \tilde{p}, \theta) + D_b^\pi(E, p, \tilde{p}, \theta)], \quad (24)$$

$$V_{DS}(E, p, \tilde{p}) \equiv \frac{1}{2} \int_{-1}^1 d \cos \theta \frac{\tilde{p}^2 + 4p^2 - 8\tilde{p}p \cos \theta + 3p^2 \cos 2\theta}{2E_\pi(p_\pi)} [D_a^\pi(E, p, \tilde{p}, \theta) + D_b^\pi(E, p, \tilde{p}, \theta)], \quad (25)$$

$$V_{DD}^{(c_1, c_2, c_3, c_4)}(E, p, \tilde{p}) \equiv \frac{1}{2} \int_{-1}^1 d \cos \theta \frac{c_1(\tilde{p}^2 + p^2) - c_2 \tilde{p}p \cos \theta + c_3(\tilde{p}^2 + p^2) \cos 2\theta - c_4 \tilde{p}p \cos 3\theta}{2E_\pi(p_\pi)} \times [D_a^\pi(E, p, \tilde{p}, \theta) + D_b^\pi(E, p, \tilde{p}, \theta)], \quad (26)$$

where θ denotes the angle between the three-momenta $\tilde{\mathbf{p}}$ and \mathbf{p} . The values for the $c_i (i = 1, \dots, 4)$ coefficients are specified below for each value of the total angular momentum J . Moreover,

$$D_a^\pi(E, p, \tilde{p}, \theta) = \frac{1}{E_\pi(p_\pi) + E_{1'}(\tilde{p}) + E_2(p) - E},$$

$$D_b^\pi(E, p, \tilde{p}, \theta) = \frac{1}{E_\pi(p_\pi) + E_1(p) + E_{2'}(\tilde{p}) - E} \quad (27)$$

are the contributions of the two TOPT orderings with $p_\pi = \sqrt{p^2 + \tilde{p}^2 - 2p\tilde{p} \cos \theta}$ and $E_i = \sqrt{p_i^2 + m_i^2}$. The OPE potentials in the elastic channels listed in Table II for $J^P = \frac{1}{2}^-$ can be written in the matrix form (where the columns and rows given by the channels listed in order in the table) as

$$V_{\frac{1}{2}^-}^{\text{OPE}} = -2 \frac{gg_1}{f_\pi^2} \begin{pmatrix} V_{\frac{1}{2}^-}^{SS} & V_{\frac{1}{2}^-}^{SD} \\ V_{\frac{1}{2}^-}^{DS} & V_{\frac{1}{2}^-}^{DD} \end{pmatrix}, \quad (28)$$

with

$$V_{\frac{1}{2}^-}^{SS} = \begin{pmatrix} 0 & \frac{1}{4\sqrt{3}} V_{SS} & -\frac{1}{4\sqrt{6}} V_{SS} \\ \frac{1}{4\sqrt{3}} V_{SS} & -\frac{1}{6} V_{SS} & -\frac{1}{12\sqrt{2}} V_{SS} \\ -\frac{1}{4\sqrt{6}} V_{SS} & -\frac{1}{12\sqrt{2}} V_{SS} & -\frac{5}{24} V_{SS} \end{pmatrix},$$

$$V_{\frac{1}{2}^-}^{SD} = \begin{pmatrix} \frac{1}{8\sqrt{6}} V_{SD} & 0 & \frac{1}{16\sqrt{30}} V_{SD} & \frac{1}{16} \sqrt{\frac{3}{10}} V_{SD} \\ \frac{1}{24\sqrt{2}} V_{SD} & -\frac{1}{16\sqrt{6}} V_{SD} & \frac{1}{12\sqrt{10}} V_{SD} & -\frac{1}{16\sqrt{10}} V_{SD} \\ \frac{1}{96} V_{DS} & \frac{1}{32\sqrt{3}} V_{SD} & -\frac{7}{96\sqrt{5}} V_{SD} & -\frac{1}{16\sqrt{5}} V_{SD} \end{pmatrix},$$

$$V_{\frac{1}{2}^-}^{DS} = \begin{pmatrix} \frac{1}{8\sqrt{6}} V_{DS} & \frac{1}{24\sqrt{2}} V_{DS} & \frac{1}{96} V_{DS} \\ 0 & -\frac{1}{16\sqrt{6}} V_{DS} & \frac{1}{32\sqrt{3}} V_{DS} \\ \frac{1}{16\sqrt{30}} V_{DS} & \frac{1}{12\sqrt{10}} V_{DS} & -\frac{7}{96\sqrt{5}} V_{DS} \\ \frac{1}{16} \sqrt{\frac{3}{10}} V_{DS} & -\frac{1}{16\sqrt{10}} V_{DS} & -\frac{1}{16\sqrt{5}} V_{DS} \end{pmatrix},$$

$$V_{\frac{1}{2}^-}^{DD} = \begin{pmatrix} -\frac{1}{48} V_{DD}^{(1,8,3,0)} & \frac{1}{64\sqrt{3}} V_{DD}^{(4,23,12,9)} & -\frac{1}{192\sqrt{5}} V_{DD}^{(8,37,24,27)} & \frac{1}{64\sqrt{5}} V_{DD}^{(2,13,6,3)} \\ \frac{1}{64\sqrt{3}} V_{DD}^{(4,23,12,9)} & 0 & \frac{1}{32\sqrt{15}} V_{DD}^{(1,-1,3,9)} & \frac{1}{64} \sqrt{\frac{3}{5}} V_{DD}^{(2,13,6,3)} \\ -\frac{1}{192\sqrt{5}} V_{DD}^{(8,37,24,27)} & \frac{1}{32\sqrt{15}} V_{DD}^{(1,-1,3,9)} & -\frac{1}{240} V_{DD}^{(13,77,39,27)} & -\frac{1}{320} V_{DD}^{(2,13,6,3)} \\ \frac{1}{64\sqrt{5}} V_{DD}^{(2,13,6,3)} & \frac{1}{64} \sqrt{\frac{3}{5}} V_{DD}^{(2,13,6,3)} & -\frac{1}{320} V_{DD}^{(2,13,6,3)} & -\frac{3}{160} V_{DD}^{(1,9,3,-1)} \end{pmatrix}.$$

The OPE potentials in the elastic channels listed in Table II for $J^P = \frac{3}{2}^-$ read

$$V_{\frac{3}{2}^-}^{\text{OPE}} = -2 \frac{gg_1}{f_\pi^2} \begin{pmatrix} V_{\frac{3}{2}^-}^{SS} & V_{\frac{3}{2}^-}^{SD} \\ V_{\frac{3}{2}^-}^{DS} & V_{\frac{3}{2}^-}^{DD} \end{pmatrix}, \quad (29)$$

where

$$V_{\frac{3}{2}^-}^{SS} = \begin{pmatrix} \frac{1}{12} V_{SS} & \frac{1}{8\sqrt{3}} V_{SS} & -\frac{\sqrt{5}}{24} V_{SS} \\ \frac{1}{8\sqrt{3}} V_{SS} & 0 & \frac{1}{8} \sqrt{\frac{5}{3}} V_{SS} \\ -\frac{\sqrt{5}}{24} V_{SS} & \frac{1}{8} \sqrt{\frac{5}{3}} V_{SS} & -\frac{1}{12} V_{SS} \end{pmatrix},$$

$$V_{\frac{3}{2}^-}^{SD} = \begin{pmatrix} -\frac{1}{16\sqrt{3}} V_{SD} & -\frac{1}{48} V_{SD} & \frac{1}{24} V_{SD} & -\frac{1}{32\sqrt{3}} V_{SD} & -\frac{1}{96\sqrt{2}} V_{SD} & -\frac{1}{96\sqrt{5}} V_{SD} & \frac{1}{32} \sqrt{\frac{7}{10}} V_{SD} \\ 0 & -\frac{1}{32\sqrt{3}} V_{SD} & -\frac{1}{32\sqrt{3}} V_{SD} & 0 & \frac{1}{32\sqrt{6}} V_{SD} & \frac{1}{8\sqrt{15}} V_{SD} & \frac{1}{32} \sqrt{\frac{21}{10}} V_{SD} \\ -\frac{1}{32\sqrt{15}} V_{SD} & -\frac{1}{24\sqrt{5}} V_{SD} & -\frac{1}{96\sqrt{5}} V_{SD} & \frac{1}{8\sqrt{15}} V_{SD} & \frac{7}{96\sqrt{10}} V_{SD} & \frac{1}{30} V_{SD} & -\frac{1}{160} \sqrt{\frac{7}{2}} V_{SD} \end{pmatrix},$$

$$V_{\frac{3}{2}^-}^{DS} = \begin{pmatrix} -\frac{1}{16\sqrt{3}} V_{DS} & 0 & -\frac{1}{32\sqrt{15}} V_{DS} \\ -\frac{1}{48} V_{DS} & -\frac{1}{32\sqrt{3}} V_{DS} & -\frac{1}{24\sqrt{5}} V_{DS} \\ \frac{1}{24} V_{DS} & -\frac{1}{32\sqrt{3}} V_{DS} & -\frac{1}{96\sqrt{5}} V_{DS} \\ -\frac{1}{32\sqrt{3}} V_{DS} & 0 & \frac{1}{8\sqrt{15}} V_{DS} \\ -\frac{1}{96\sqrt{2}} V_{DS} & \frac{1}{32\sqrt{6}} V_{DS} & \frac{7}{96\sqrt{10}} V_{DS} \\ -\frac{1}{96\sqrt{5}} V_{DS} & \frac{1}{8\sqrt{15}} V_{DS} & \frac{1}{30} V_{DS} \\ \frac{1}{32} \sqrt{\frac{7}{10}} V_{DS} & \frac{1}{32} \sqrt{\frac{21}{10}} V_{DS} & -\frac{1}{160} \sqrt{\frac{7}{2}} V_{DS} \end{pmatrix},$$

$$V_{\frac{3}{2}^-}^{DD} = \begin{pmatrix} 0 & \frac{V_{DD}^{(1,5,3,3)}}{16\sqrt{3}} & \frac{V_{DD}^{(2,13,6,3)}}{32\sqrt{3}} & 0 & -\frac{V_{DD}^{(1,5,3,3)}}{16\sqrt{6}} & \frac{V_{DD}^{(2,13,6,3)}}{64\sqrt{15}} & -\sqrt{\frac{6}{35}} \frac{V_{DD}^{(2,13,6,3)}}{64} \\ \frac{V_{DD}^{(1,5,3,3)}}{16\sqrt{3}} & -\frac{V_{DD}^{(1,5,3,3)}}{24} & \frac{V_{DD}^{(2,13,6,3)}}{96} & \frac{V_{DD}^{(2,13,6,3)}}{64\sqrt{3}} & -\frac{V_{DD}^{(1,5,3,3)}}{48\sqrt{2}} & \frac{V_{DD}^{(2,13,6,3)}}{48\sqrt{5}} & \frac{V_{DD}^{(2,13,6,3)}}{32\sqrt{70}} \\ \frac{V_{DD}^{(2,13,6,3)}}{32\sqrt{3}} & \frac{V_{DD}^{(2,13,6,3)}}{96} & \frac{V_{DD}^{(1,5,3,3)}}{48} & \frac{V_{DD}^{(1,5,3,3)}}{32\sqrt{3}} & \frac{V_{DD}^{(2,13,6,3)}}{192\sqrt{2}} & -\frac{\sqrt{5}}{96} V_{DD}^{(1,5,3,3)} & \sqrt{\frac{5}{14}} \frac{V_{DD}^{(2,13,6,3)}}{64} \\ 0 & \frac{V_{DD}^{(2,13,6,3)}}{64\sqrt{3}} & \frac{V_{DD}^{(1,5,3,3)}}{32\sqrt{3}} & 0 & -\frac{V_{DD}^{(2,13,6,3)}}{64\sqrt{6}} & \frac{\sqrt{3}}{32} V_{DD}^{(1,5,3,3)} & \sqrt{\frac{15}{14}} \frac{V_{DD}^{(2,13,6,3)}}{64} \\ -\frac{V_{DD}^{(1,5,3,3)}}{16\sqrt{6}} & -\frac{V_{DD}^{(1,5,3,3)}}{48\sqrt{2}} & \frac{V_{DD}^{(2,13,6,3)}}{192\sqrt{2}} & -\frac{V_{DD}^{(2,13,6,3)}}{64\sqrt{6}} & -\frac{5}{96} V_{DD}^{(1,5,3,3)} & -\frac{7V_{DD}^{(2,13,6,3)}}{192\sqrt{10}} & \frac{V_{DD}^{(2,13,6,3)}}{32\sqrt{35}} \\ \frac{V_{DD}^{(2,13,6,3)}}{64\sqrt{15}} & \frac{V_{DD}^{(2,13,6,3)}}{48\sqrt{5}} & -\frac{\sqrt{5}}{96} V_{DD}^{(1,5,3,3)} & \sqrt{\frac{5}{3}} \frac{V_{DD}^{(1,5,3,3)}}{32} & -\frac{7V_{DD}^{(2,13,6,3)}}{192\sqrt{10}} & -\frac{V_{DD}^{(1,5,3,3)}}{48} & -\frac{V_{DD}^{(2,13,6,3)}}{64\sqrt{14}} \\ -\sqrt{\frac{6}{35}} \frac{V_{DD}^{(2,13,6,3)}}{64} & \frac{V_{DD}^{(2,13,6,3)}}{32\sqrt{70}} & \sqrt{\frac{5}{14}} \frac{V_{DD}^{(2,13,6,3)}}{64} & \sqrt{\frac{15}{14}} \frac{V_{DD}^{(2,13,6,3)}}{64} & \frac{V_{DD}^{(2,13,6,3)}}{32\sqrt{35}} & -\frac{V_{DD}^{(2,13,6,3)}}{64\sqrt{14}} & \frac{3}{224} V_{DD}^{(1,3,3,5)} \end{pmatrix}.$$

The OPE potentials in the elastic channels in order listed in Table II for $J^P = \frac{5}{2}^-$ read

$$V_{\frac{5}{2}^-}^{\text{OPE}} = -2 \frac{gg_1}{f_\pi^2} \begin{pmatrix} V_{\frac{5}{2}^-}^{SS} & V_{\frac{5}{2}^-}^{SD} \\ V_{\frac{5}{2}^-}^{DS} & V_{\frac{5}{2}^-}^{DD} \end{pmatrix}, \quad (30)$$

where

$$V_{\frac{5}{2}^-}^{SS} = \frac{1}{8} V_{SS},$$

$$V_{\frac{5}{2}^-}^{SD} = \left(-\frac{1}{16\sqrt{10}} V_{SD} \quad -\frac{1}{32} \sqrt{\frac{2}{15}} V_{SD} \quad -\frac{1}{32} \sqrt{\frac{7}{15}} V_{SD} \quad \frac{1}{32} \sqrt{\frac{7}{5}} V_{SD} \quad -\frac{1}{16\sqrt{15}} V_{SD} \quad \frac{1}{160} \sqrt{\frac{7}{3}} V_{SD} \quad \frac{1}{40} \sqrt{\frac{7}{2}} V_{SD} \right),$$

$$V_{\frac{5}{2}^-}^{DS} = \left(-\frac{1}{16\sqrt{10}}V_{DS} \quad -\frac{1}{32}\sqrt{\frac{2}{15}}V_{DS} \quad -\frac{1}{32}\sqrt{\frac{7}{15}}V_{DS} \quad \frac{1}{32}\sqrt{\frac{7}{5}}V_{DS} \quad -\frac{1}{16\sqrt{15}}V_{DS} \quad \frac{1}{160}\sqrt{\frac{7}{3}}V_{DS} \quad \frac{1}{40}\sqrt{\frac{7}{2}}V_{DS} \right)^T,$$

$$V_{\frac{5}{2}^-}^{DD} = \begin{pmatrix} 0 & \frac{V_{DD}^{(1,5,3,3)}}{16\sqrt{3}} & -\frac{V_{DD}^{(2,13,6,3)}}{16\sqrt{42}} & 0 & -\frac{V_{DD}^{(1,5,3,3)}}{16\sqrt{6}} & -\frac{V_{DD}^{(2,13,6,3)}}{32\sqrt{210}} & -\frac{V_{DD}^{(2,13,6,3)}}{16\sqrt{35}} \\ \frac{V_{DD}^{(1,5,3,3)}}{16\sqrt{3}} & -\frac{V_{DD}^{(1,5,3,3)}}{24} & -\frac{V_{DD}^{(2,13,6,3)}}{48\sqrt{14}} & -\frac{V_{DD}^{(2,13,6,3)}}{32\sqrt{42}} & -\frac{V_{DD}^{(1,5,3,3)}}{48\sqrt{2}} & \frac{V_{DD}^{(2,13,6,3)}}{24\sqrt{70}} & \frac{V_{DD}^{(2,13,6,3)}}{16\sqrt{105}} \\ -\frac{V_{DD}^{(2,13,6,3)}}{16\sqrt{42}} & -\frac{V_{DD}^{(2,13,6,3)}}{48\sqrt{14}} & \frac{V_{DD}^{(17,100,51,36)}}{336} & \frac{V_{DD}^{(4,5,12,27)}}{448\sqrt{3}} & -\frac{V_{DD}^{(2,13,6,3)}}{192\sqrt{7}} & -\frac{\sqrt{5}V_{DD}^{(16,83,48,45)}}{1344} & \sqrt{\frac{5}{6}}\frac{V_{DD}^{(2,13,6,3)}}{224} \\ 0 & -\frac{V_{DD}^{(2,13,6,3)}}{32\sqrt{42}} & \frac{V_{DD}^{(4,5,12,27)}}{448\sqrt{3}} & 0 & \frac{V_{DD}^{(2,13,6,3)}}{64\sqrt{21}} & \sqrt{\frac{5}{3}}\frac{V_{DD}^{(11,61,33,27)}}{224} & \frac{\sqrt{10}}{448}V_{DD}^{(2,13,6,3)} \\ -\frac{V_{DD}^{(1,5,3,3)}}{16\sqrt{6}} & -\frac{V_{DD}^{(1,5,3,3)}}{48\sqrt{2}} & -\frac{V_{DD}^{(2,13,6,3)}}{192\sqrt{7}} & \frac{V_{DD}^{(2,13,6,3)}}{64\sqrt{21}} & -\frac{5}{96}V_{DD}^{(1,5,3,3)} & \sqrt{\frac{7}{5}}\frac{V_{DD}^{(2,13,6,3)}}{192} & \frac{V_{DD}^{(2,13,6,3)}}{8\sqrt{210}} \\ -\frac{V_{DD}^{(2,13,6,3)}}{32\sqrt{210}} & -\frac{V_{DD}^{(2,13,6,3)}}{24\sqrt{70}} & -\frac{\sqrt{5}}{1344}V_{DD}^{(16,83,48,45)} & \sqrt{\frac{5}{3}}\frac{V_{DD}^{(11,61,33,27)}}{224} & \sqrt{\frac{7}{5}}\frac{V_{DD}^{(2,13,6,3)}}{192} & \frac{V_{DD}^{(1,17,3,-9)}}{336} & -\frac{V_{DD}^{(2,13,6,3)}}{224\sqrt{6}} \\ -\frac{V_{DD}^{(2,13,6,3)}}{16\sqrt{35}} & \frac{V_{DD}^{(2,13,6,3)}}{16\sqrt{105}} & \sqrt{\frac{5}{6}}\frac{V_{DD}^{(2,13,6,3)}}{224} & \frac{\sqrt{10}}{448}V_{DD}^{(2,13,6,3)} & \frac{V_{DD}^{(2,13,6,3)}}{8\sqrt{210}} & -\frac{V_{DD}^{(2,13,6,3)}}{224\sqrt{6}} & \frac{V_{DD}^{(11,61,33,27)}}{224} \end{pmatrix}.$$

Weak production amplitudes

Since the energy region of interest is close the $\Sigma_c^{(*)}\bar{D}^{(*)}$ thresholds, we only consider the elastic $\Sigma_c^{(*)}\bar{D}^{(*)}$ channels produced in an S -wave. We parametrize the weak production of the $|s_Q \otimes j_\ell\rangle$ states with the total angular momentum J , $\mathcal{F}_{s_Q, j_\ell}^J = \langle \Lambda_b | \hat{H}_W | K^-(s_Q \otimes j_\ell)^J \rangle$, as constants, where $(s_Q \otimes j_\ell)^J$ refers to the state with J in the $|s_Q \otimes j_\ell\rangle$ basis. Specifically, the production contact terms for the $J = \frac{1}{2}$ channels are parametrized as

$$P_1^{\frac{1}{2}} = \frac{1}{2}\mathcal{F}_{0, \frac{1}{2}}^{\frac{1}{2}} - \frac{1}{2\sqrt{3}}\mathcal{F}_{1, \frac{1}{2}}^{\frac{1}{2}} + \sqrt{\frac{2}{3}}\mathcal{F}_{1, \frac{3}{2}}^{\frac{1}{2}}, \quad (31)$$

$$P_2^{\frac{1}{2}} = -\frac{1}{2\sqrt{3}}\mathcal{F}_{0, \frac{1}{2}}^{\frac{1}{2}} + \frac{5}{6}\mathcal{F}_{1, \frac{1}{2}}^{\frac{1}{2}} + \frac{\sqrt{2}}{3}\mathcal{F}_{1, \frac{3}{2}}^{\frac{1}{2}}, \quad (32)$$

$$P_3^{\frac{1}{2}} = \sqrt{\frac{2}{3}}\mathcal{F}_{0, \frac{1}{2}}^{\frac{1}{2}} + \frac{\sqrt{2}}{3}\mathcal{F}_{1, \frac{1}{2}}^{\frac{1}{2}} - \frac{1}{3}\mathcal{F}_{1, \frac{3}{2}}^{\frac{1}{2}}, \quad (33)$$

where the indices $i = 1, 2, 3$ in $P_i^{\frac{1}{2}}$ represent the weak production for the S -wave $\Sigma_c\bar{D}$, $\Sigma_c\bar{D}^*$ and $\Sigma_c^*\bar{D}^*$, respectively. Analogously, the weak production for the S -wave $\Sigma_c\bar{D}^*$, $\Sigma_c^*\bar{D}$ and $\Sigma_c^*\bar{D}^*$ for $J = \frac{3}{2}$ are written as

$$P_1^{\frac{3}{2}} = -\frac{1}{\sqrt{3}}\mathcal{F}_{0, \frac{3}{2}}^{\frac{3}{2}} + \frac{1}{3}\mathcal{F}_{1, \frac{1}{2}}^{\frac{3}{2}} + \frac{\sqrt{5}}{3}\mathcal{F}_{1, \frac{3}{2}}^{\frac{3}{2}}, \quad (34)$$

$$P_2^{\frac{3}{2}} = \frac{1}{2}\mathcal{F}_{0, \frac{3}{2}}^{\frac{3}{2}} - \frac{1}{\sqrt{3}}\mathcal{F}_{1, \frac{1}{2}}^{\frac{3}{2}} + \frac{1}{2}\sqrt{\frac{5}{3}}\mathcal{F}_{1, \frac{3}{2}}^{\frac{3}{2}}, \quad (35)$$

$$P_3^{\frac{3}{2}} = \frac{1}{2}\sqrt{\frac{5}{3}}\mathcal{F}_{0, \frac{3}{2}}^{\frac{3}{2}} + \frac{\sqrt{5}}{3}\mathcal{F}_{1, \frac{1}{2}}^{\frac{3}{2}} + \frac{1}{6}\mathcal{F}_{1, \frac{3}{2}}^{\frac{3}{2}}, \quad (36)$$

in order. The $J = \frac{5}{2}$ production for the S -wave $\Sigma_c^*\bar{D}^*$ is

$$P_{\frac{5}{2}}^{\frac{5}{2}} = \mathcal{F}_{1, \frac{3}{2}}^{\frac{5}{2}}. \quad (37)$$

Additional fits to the $J/\psi p$ invariant mass distributions

To check the stability of the results and the significance of the the narrow $P_c(4380)$ structure, in addition to the fits reported in the main text, we also fit to the inclusive and $m_{Kp} > 1.9$ GeV $J/\psi p$ distributions reported by LHCb [17]. As pointed out in the LHCb analysis, in the latter case, the cut employed to constraint the energy range of m_{Kp} removes over 80% of the Λ^* -resonance contributions. The signal amplitudes and the background used in the fits are

evaluated as described in the main article, see Eqs. (12) and (14), respectively, and the discussion around them. The results of the fits are displayed in Fig. 2. These two data sets can also be described well within the molecular approach, as formulated in the main article, and show a signal of the narrow $P_c(4380)$, too, though the peak in the inclusive case (right panel) is a bit less prominent. The poles and residues for all P_c states extracted from additional fits agree within errors with the ones shown in Table I in the main article.

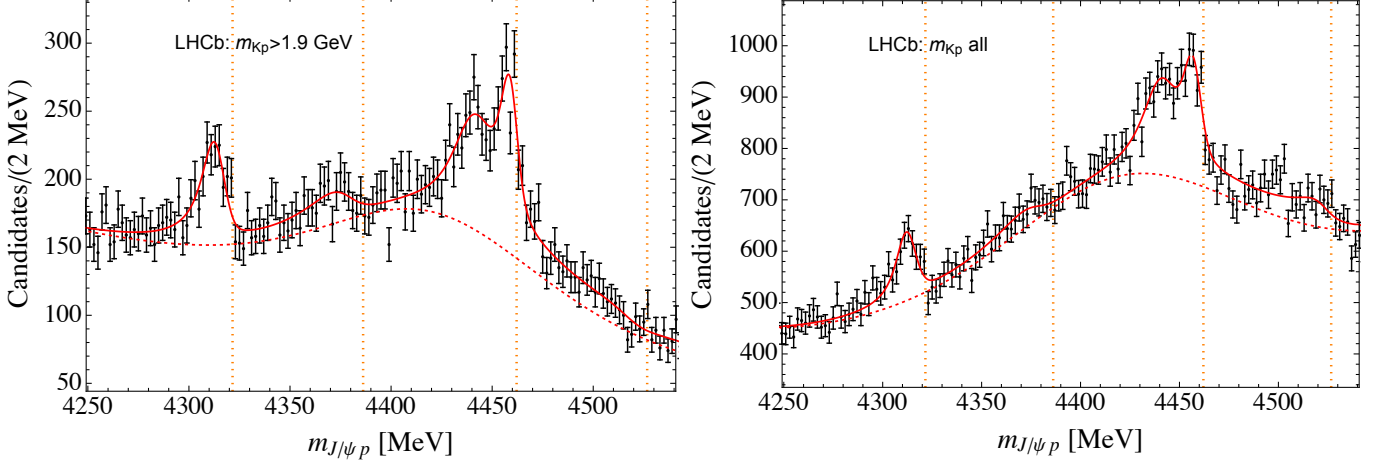


FIG. 2. Left panel: the fitted invariant mass distributions versus the experimental data [17] with the $m_{Kp} > 1.9$ GeV cut. Right panel: the fitted invariant mass distributions versus the inclusive experimental data [17] (without cuts and weighting).

Formalism

The product of the effective couplings $g_\alpha g_\gamma$ of a given P_c state to channels α and γ of the $\Sigma_c^{(*)} \bar{D}^{(*)}$ coupled channels is obtained from the residue of the scattering amplitude $T_{\alpha\gamma}^J(E)$ at the pole of that P_c , i.e.,

$$g_\alpha g_\gamma = \lim_{E \rightarrow E_{\text{pole}}} (E^2 - E_{\text{pole}}^2) T_{\alpha\gamma}^J(E). \quad (38)$$

Here the T -matrix of the $\Sigma_c^{(*)} \bar{D}^{(*)} \rightarrow \Sigma_c^{(*)} \bar{D}^{(*)}$ scattering is given by

$$T_{\alpha\gamma}^J(E, p, \tilde{p}) = V_{\alpha\gamma}^J(E, p, \tilde{p}) - \sum_c \int \frac{d^3 \mathbf{q}}{(2\pi)^3} V_{\alpha\beta}^J(E, p, q) G_\beta(E, q) T_{\beta\gamma}^J(E, q, \tilde{p}). \quad (39)$$

The production strengths P_{pole} for a resonance P_c is then defined as

$$P_{\text{pole}} g_\alpha = \lim_{E \rightarrow E_{\text{pole}}} (E^2 - E_{\text{pole}}^2) U_\alpha^J(E), \quad (40)$$

where $U_\alpha^J(E)$ represents the on-shell elastic production amplitude $U_\alpha^J(E, p)$. To account for the widths of $\Sigma_c^{(*)}$ of 1.86 MeV (15 MeV) which play an important role in giving the correct widths of resonances, we use a complex mass $m - i\Gamma/2$ in the two-body propagator, i.e.,

$$G_\beta(E, q) = \frac{2\mu_\beta}{q^2 - p_\beta^2 - i\epsilon}, \quad p_\beta^2 = 2\mu_\beta(E - m_{\text{th}}^\beta + i\Gamma^\beta/2), \quad (41)$$

with μ_β , m_{th}^β and Γ^β the reduced mass, threshold mass and the width of $\Sigma_c^{(*)}$ of the β^{th} elastic channel.