

# 1 TCAD Device Simulations of Irradiated Silicon 2 Detectors

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**F.R.Palomo\***

*School of Engineering, U. of Sevilla, Spain*

*E-mail: [fpalomo@us.es](mailto:fpalomo@us.es)*

**M.Moll**

*CERN, Geneva, Switzerland*

*E-mail: [michael.moll@cern.ch](mailto:michael.moll@cern.ch)*

**J.Schwandt**

*Institute of Experimental Physics, U.of Hamburg, Germany*

*E-mail: [joern.schwandt@desy.de](mailto:joern.schwandt@desy.de)*

**E.Giulio Villani**

*STFC Rutherford Appleton Laboratory, United Kingdom*

*E-mail: [Enrico.Giulio.Villani@cern.ch](mailto:Enrico.Giulio.Villani@cern.ch)*

**Y.Gurinskaya**

*CERN, Geneva, Switzerland*

*E-mail: [yana.gurinskaya@cern.ch](mailto:yana.gurinskaya@cern.ch)*

**R.Millán**

*School of Engineering, U. of Sevilla, Spain*

*E-mail: [rmillan@us.es](mailto:rmillan@us.es)*

The high hadron fluences expected during the HL-LHC programme will impose strong constraints in terms of radiation damage on silicon detectors. New TCAD simulation models are needed to predict the expected detector performances. This review examines the challenges ahead for different types of detector devices, with emphasis on the acceptor removal effect in LGADs, surface damage in Monolithic and Strip sensors and bulk damage in all sensor types.

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\*Speaker.

### 3 1. Introduction

4 To observe rare high energy physics (HEP) processes we need large statistical datasets which  
5 means a high particle-flux environment. The detectors have to withstand the cumulated radiation  
6 damage, maintaining their quality of operation for years. The High Luminosity LHC (HL-LHC)  
7 programme, an upgrade of the existing LHC expected to start operation in 2027, will have an  
8 integrated luminosity of  $4000 \text{ fb}^{-1}$  over 10 years of operation<sup>1</sup>. For the innermost pixel sensors,  
9 for a typical radii of 3 cm, over their lifetime, this would translate into an expected hadron fluence<sup>2</sup>  
10 around  $2 \times 10^{16} \text{ n}_{\text{eq}}/\text{cm}^2$  and ionizing doses about 1 Grad [1]. The RD50 collaboration is focused  
11 on the development of new solid state particle detectors for HL-LHC upgrade and possibly beyond  
12 (FCC programme).

13 One of the tools to predict the performances of detectors and to improve their design in such  
14 a harsh radiation environment is Technology Computer-Aided Design (TCAD) device simulation.  
15 A silicon particle detector can be viewed as the solid state analogue of an ionization chamber: the  
16 electric field strength is critical to separate the electron-hole pairs created by ionization, avoiding  
17 their recombination. The differentiation with ionization chambers comes in the carrier transport,  
18 governed by the laws of the crystal drift-diffusion model (the simplest one, but thermal and hydro-  
19 dynamic carrier transport could also be considered). Using finite element analysis in a geometrical  
20 device model, the simulation solves the combined partial differential equations of charge continuity  
21 for charge transport and the Poisson equation for the electrostatic potential. In general, radiation  
22 damage modifies silicon detector performance; TCAD aims to predict such changes by means of  
23 I-V/C-V (current vs voltage, capacitance vs voltage), charge collection efficiency (CCE) simula-  
24 tions and predicts the signal shape, which can be used as input to the front-end<sup>3</sup>. Radiation damage  
25 affects the carrier generation-recombination mechanism, the charge carriers mobility and also the  
26 electric field by means of charge accumulation in dielectrics and traps.

27 In order to make reliable HEP device simulations, a thorough understanding of crystal defects  
28 introduced by Displacement Damage Dose (DDD) and Total Ionization Dose (TID) is necessary.  
29 TID effects appear when the incident particles lose energy by ionization (Ionizing Energy Loss,  
30 IEL) and can be described as purely electrostatic due to accumulation of holes in device dielectrics  
31 and the appearance of defects in the semiconductor-dielectric interface. Usually, TID effects are  
32 the most relevant in MOS electronics while displacement damage is more relevant in solid state  
33 detectors. Device simulation can easily deal with electrostatic effects, simply by considering new  
34 charge densities for the Poisson equation.

35 Displacement damage appears when the incident particles lose energy by non-ionizing mech-  
36 anisms (Non Ionizing Energy Loss, NIEL) and is a complex problem because it affects not only  
37 the Poisson equation (by adding new charge densities due to the carrier trapping by defects) but  
38 also the carrier transport equations, specifically carrier mobility and the generation-recombination  
39 terms. The LHC radiation environment consists of  $\gamma$  rays, electrons, and hadrons (mainly pions,

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<sup>1</sup>One inverse femtobarn ( $\text{fb}^{-1}$ ) corresponds approximately to  $8 \times 10^{13}$  proton-proton interactions, assuming a proton inelastic cross section of 80 mb. The instantaneous luminosity of the HL-LHC is  $5 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$  or at least five times the LHC instantaneous luminosity. The center of mass energy,  $\sqrt{s}$  is 14 TeV.

<sup>2</sup>Integrated flux in terms of 1 MeV equivalent neutrons for displacement damage

<sup>3</sup>in mixed mode simulations TCAD can also include the first stage of the front-end as a circuit simulation

40 protons and neutrons). The amount and type of crystalline damage is different for every particle  
41 type [2]. Radiation produces a distribution of primary knock-on atoms (PKAs) displaced from  
42 their lattice positions. The minimum energy in silicon necessary to create a Frenkel pair (vacancy  
43 plus separated Si interstitial) or point defect displacement energy, is  $\sim 25$  eV. The threshold energy  
44 to produce densely packed displacement regions (clusters) is  $\sim 5$  keV. Gamma rays generate se-  
45 condary Compton electrons responsible for a recoil PKA spectrum that peaks at  $< 1$  keV so point  
46 defects are dominant. For electrons, the PKA spectrum depends on the initial energy, for example,  
47 15 MeV electrons produce a maximum PKA energy of 250 keV so defect clusters will also appear.  
48 Coulomb interaction is the main mechanism of energy loss by charged hadrons so the PKA spec-  
49 trum extends from point defects (low energy) to defect clusters (large energy). Finally, neutron  
50 interactions are dominated by head-on collisions; for a 1 MeV neutron the mean energy transfer to  
51 a Si atom is  $\sim 50$  keV so they will produce a high density of clusters.

52 A further complication arises from the fact that only a subset of defects is important: those  
53 responsible for the macroscopic effects at the device functional level, as active electrical defects  
54 (also known as traps). The traps are able to modify the charge transport (see for example [3] for  
55 an updated list of traps in Si): by reducing the carrier mobility or by deactivating dopants via kick-  
56 out reactions (particularly relevant for the acceptor removal effect). Traps produce charge trapping  
57 and changes in the leakage current,  $I_{leak}$  and in the effective space charge density,  $N_{eff}$ , see Fig. 1.  
58 Higher leakage current is essentially produced by the defects with energy levels close to the middle  
59 of the bandgap. Increased leakage current implies more noise and more power consumption at the  
60 device level.

61 The effective space charge density  $N_{eff}$  in undamaged detectors is just the bulk doping. In  
62 damaged detectors,  $\Delta N_{eff}$  is mainly due to charged defects: acceptors in the lower half of the  
63 bandgap tend to contribute with negative space charge and donors in the upper half tend to con-  
64 tribute with positive space charge. The  $\Delta N_{eff}$  will shift the depletion voltage value (because  
65  $V_{dep} = e|N_{eff}|d^2/2\epsilon\epsilon_0$ ) and will also change the electric field configuration within the device.  
66 A non-homogeneous space charge distribution can lead to new effects such as the occurrence of a  
67 double junction, possible underdepletion or shift of the electric field maximum to unwanted device  
68 regions. If the electric field locally exceeds 300 kV/cm, impact ionization phenomena appear that  
69 could lead to a device breakdown.

70 Charge trapping by defect levels (donors and acceptors) reduces the available carriers. If  
71 the concentration of trapping centers and the detrapping time is long compared to the detector  
72 signal collection, the device will have a reduction in the Signal to Noise Ratio (SNR) and in the  
73 CCE. For defect clusters, a charge transfer appears between levels of neighbouring defects, also  
74 known as inter-centre charge (ICC) transfer [4]. This mechanism is beyond the Shockley-Read-  
75 Hall (SRH) mechanism where carriers are captured by a single defect level. A first approach to  
76 inter-centre charge transfer is the coupled defect-level (CDL) recombination, available in TCAD  
77 [5] that considers transitions between two defect levels. Further modelization of ICC is beyond  
78 standard TCAD although there are efforts [6], to define new recombination models to be included  
79 in TCAD<sup>4</sup>. ICC is most visible in the increase of the leakage current so it can be taken into account,

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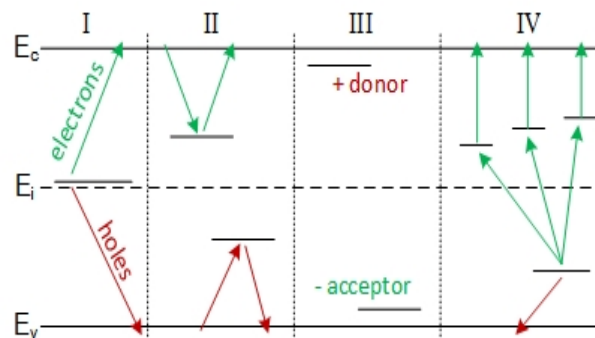
<sup>4</sup>TCAD software packages include the possibility that advanced users can add new functions by means of dynami-  
cally linked libraries.

80 in an ad-hoc manner, as an enhancement of the SRH generation rate [7] (the usual model for leakage  
81 current density is  $J_{leak} = qG_{SRH}$ ).

82 For bulk p-type devices radiation damage shows two effects: a removal of the initial acceptor  
83 density and the appearance of usually acceptor-like defects due to the creation of the deep traps [8]  
84 shown in Eq. (1.1) :

$$N_{eff}(\Phi, x) = g_{eff}\Phi + N_A(0, x)e^{-c\Phi} \quad (1.1)$$

85 where  $N_A(0, x)$  is the initial acceptor density,  $\Phi$  is the radiation fluence ( $1\text{MeV n}_{eq}/\text{cm}^2$ ),  $g_{eff} \sim$   
86  $0.02\text{ cm}^{-1}$  is the introduction rate and  $c$  is the acceptor removal constant (in a particular parame-  
87 terization [8]  $c$  can be understood as  $c = 1/\Phi_0$ , where  $\Phi_0$  is the fluence needed to reduce  $N_A(0, x)$   
88 by a factor of  $1/e$ ). The acceptor removal effect [9] is responsible for a deactivation of the initial  
89 boron dopant density because boron atoms are displaced from the substitutional lattice site and  
90 deactivated as shallow dopants. It is still under study [10] but the measurements are in agreement  
91 with the deactivation of boron atoms via the formation of ion-acceptor complexes, in a two step  
92 process: (i) the radiation induced creation of an interstitial Si atom and (ii) the deactivation of the  
93 boron via a Watkins kick-out reaction. The amount of removed boron does not change with long  
term annealing close to room temperature.



**Figure 1:** I. Increase of leakage current, II. Charge Trapping and CCE, III. Change of internal field and depletion voltage, IV. Enhanced generation by inter-center charge transfer. Defects energy levels are referenced to the Intrinsic Fermi level,  $E_i$  and to the valence and conduction bands energies,  $E_v, E_c$ .

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To summarise, radiation damage will degrade the device performance. Bulk damage by NIEL relates to point and cluster defects in the silicon lattice. As a consequence the device will show a change in  $I_{leak}$  and  $V_{dep}$ , modifications in the electric field configuration and trapping of drifting charge. The trapping will reduce the CCE and reduce the SNR. Those effects are relevant for pad sensors and DC coupled strips and pixel detectors. For LGAD-type sensors [11] acceptor removal is responsible for gain reduction. Surface damage produced by NIEL is responsible for the build up of dielectric (oxide) charges and border and interface traps. It results in an increase of the surface current, the change of the electric field and charge trapping near the semiconductor ( $Si$ )-dielectric ( $SiO_2$ ) interface. Surface damage is relevant in MOS capacitors, MOSFET transistors and gate controlled diodes, AC coupled detectors and particularly in MAPS/HVCMOS [12] detectors because they combine bulk detectors with MOSFET electronics in the same die.

Section 2 is dedicated to the TCAD modeling of radiation damage, Section 3 shows the most important high fluence TCAD defect models including the particularization of acceptor removal

108 for LGAD type detectors and Section 4 summarizes different simulation examples with emphasis  
109 on MAPS detectors.

## 110 2. TCAD modeling of radiation damage

111 TCAD software tools are designed for physical simulation of the charge transport and elec-  
112 trical behavior of semiconductor devices. There are various commercial packages available, for  
113 example Silvaco Atlas or Synopsys Sentaurus. TCAD device simulation implements the semi-  
114 classical approach to electronic transport in semiconductors<sup>5</sup>. The most used set of equations [13]  
115 considers the Poisson equation (2.1) for the electric field, dependant on the instantaneous charge  
116 density, the current continuity in a semiconductor, Eqs.(2.2), (2.3), and the traps occupation dy-  
117 namics, Eqs.(2.4) to (2.6):

$$\nabla \cdot (\epsilon \nabla \phi) = -q(p - n + N_D(1 - f_D^n) - N_A f_A^n) - q \sum_j N_{tj}(\delta_j - f_{tj}^n) \quad (2.1)$$

$$\frac{\partial n}{\partial t} - N_D \frac{\partial f_D^n}{\partial t} = (G_{net,n} - \sum_j R_n^{tj} - R_{au}) + \frac{1}{q} \nabla \cdot \vec{J}_n \quad (2.2)$$

$$\frac{\partial p}{\partial t} + N_A \frac{\partial f_A^n}{\partial t} = (G_{net,p} - \sum_j R_p^{tj} - R_{au}) - \frac{1}{q} \nabla \cdot \vec{J}_p \quad (2.3)$$

$$N_{tj} \frac{\partial f_{tj}^n}{\partial t} = R_n^{tj} - R_p^{tj} \quad \text{for each trap } j, \text{ where:} \quad (2.4)$$

$$R_n^{tj} = c_{nj} n N_{tj} (1 - f_{tj}^n) - e_{nj} N_{tj} f_{tj}^n \quad (2.5)$$

$$R_p^{tj} = c_{pj} p N_{tj} f_{tj}^n - e_{pj} N_{tj} (1 - f_{tj}^n) \quad (2.6)$$

118 where  $f_{tj}^n$  means the electron occupation fraction of trap  $j$  (in general  $f_j^n = 1 - f_j^p$  for every trap  
119  $j$  with  $f_j^p$  the complementary hole occupation fraction of the trap). The symbols  $f_D^n$ ,  $f_A^n$  are the  
120 occupancies for dopant donors and acceptors (if dopants are totally ionized,  $f_D^n = 0$ ,  $f_A^n = 1$ ). Even  
121 in the absence of traps coming from defects, Si has an indirect bandgap so a deep trap in the  
122 intrinsic level is considered to take into account phonon assisted recombination (the typical SRH  
123 recombination term, see [14]).  $R_{au}$  is the Auger recombination and  $R_n^{tj}$ ,  $R_p^{tj}$  are the electron and  
124 hole recombination rates for the trap  $j$ .  $G_{net,n}$ ,  $G_{net,p}$  are the net generation rates for electrons and  
125 holes, including optical, radiation, impact ionization and other available generation mechanisms.  
126 The summation term in Eq.(2.1) is  $\rho_{trap}$ , the trapped net charge, where  $\delta_j = 1$  if the trap  $j$  is of  
127 donor type,  $\delta_j = 0$  if the trap  $j$  is of acceptor type. In Eqs.(2.5, 2.6)  $c_{nj}$ ,  $c_{pj}$  are the electron/hole  
128 capture terms and  $e_{nj}$ ,  $e_{pj}$  are the electron/hole emission terms for trap  $j$ .

129 The different transport models have different expressions to calculate  $\vec{J}_n$  and  $\vec{J}_p$ . Sentaurus  
130 Device presents four models: Drift-Diffusion (DD), ThermoDynamic (TD), HydroDynamic (HD)  
131 and MonteCarlo (MC) [15]. DD is appropriate for simulations of low power devices with long  
132 active regions, as silicon particle detectors, in isothermal conditions. For semiconductors it is  
133 common to define Quasi-Fermi potentials,  $\Phi_n$ ,  $\Phi_p$  [16] to represent the carrier distribution functions  
134 which are slightly out of equilibrium so the DD currents [17], are:

$$\vec{J}_n = -nq\mu_n \nabla \Phi_n = \mu_n (n \nabla E_c - \frac{3}{2} nKT \nabla \ln m_n) + D_n (\nabla n - n \nabla \ln \gamma_n) \quad (2.7)$$

<sup>5</sup>particularized here to Silicon

$$\vec{J}_p = -pq\mu_p\nabla\Phi_p = \mu_p(n\nabla E_v - \frac{3}{2}nKT\nabla\ln m_p) - D_p(\nabla p - p\nabla\ln\gamma_p) \quad (2.8)$$

135 where Sentaurus takes into account the contribution from drift, diffusion and also spatial variations  
136 of the effective mass and Fermi-Dirac statistics (the Fermi-Dirac degeneracy terms,  $\gamma_n, \gamma_p$  are equal  
137 to 1 by using Maxwell-Boltzmann statistics, appropriate for non-degenerate semiconductors).

138 In order to get a glimpse of the modifications added to the semiconductor equations, let us  
139 consider a simple 2 trap model (acceptor and donor), like the classical EVL [18] defined with 8  
140 parameters: trap energy levels ( $E_a, E_d$ ), concentrations ( $N_a, N_d$ ) and capture cross sections ( $\sigma_e^a,$   
141  $\sigma_h^a, \sigma_e^d, \sigma_h^d$ ). For our two trap model, we need to solve the trap occupation dynamics,  $df_a^n/dt,$   
142  $df_d^p/dt$ , where  $f_a^n$  means electron trap occupation fraction of an acceptor trap,  $f_d^p$  means hole trap  
143 occupation fraction of a donor trap. Now the Poisson equation has an explicit  $\rho_{trap}$ , Eq.(2.9). In  
144 steady state, the trap occupancies converge to (2.10, 2.11), with effective trapping times given  
145 by (2.12) and the net recombination equations for the two traps converge to a SRH type term,  
146 Eq.(2.13):

$$\rho_{trap} = q[N_d f_d^p - N_a f_a^n] \quad (2.9)$$

$$f_d^p = \frac{v_h \sigma_h^d p + v_e \sigma_e^d N_c e^{(E_d - E_c)/kT}}{v_e \sigma_e^d (n + N_c e^{(E_d - E_c)/kT}) + v_h \sigma_h^d (p + N_v e^{(E_v - E_d)/kT})} \quad (2.10)$$

$$f_a^n = \frac{v_e \sigma_e^a n + v_h \sigma_h^a N_v e^{(E_v - E_a)/kT}}{v_e \sigma_e^a (n + N_c e^{(E_a - E_c)/kT}) + v_h \sigma_h^a (p + N_v e^{(E_v - E_a)/kT})} \quad (2.11)$$

$$\Gamma_h = \frac{1}{\tau_{eff,h}} = v_h [\sigma_h^d N_d (1 - f_d^p) + \sigma_h^a N_a f_a^n] \quad ; \quad \Gamma_e = \frac{1}{\tau_{eff,e}} = v_e [\sigma_e^a N_a (1 - f_a^n) + \sigma_e^d N_d f_d^p] \quad (2.12)$$

$$R_{net} = \frac{v_h v_e \sigma_h^d \sigma_e^d N_d (np - n_i^2)}{v_e \sigma_e^d (n + N_c e^{(E_d - E_c)/kT}) + v_h \sigma_h^d (p + N_v e^{(E_v - E_d)/kT})} + \frac{v_h v_e \sigma_h^a \sigma_e^a N_a (np - n_i^2)}{v_e \sigma_e^a (n + N_c e^{(E_a - E_c)/kT}) + v_h \sigma_h^a (p + N_v e^{(E_v - E_a)/kT})} \quad (2.13)$$

147 From the previous exposition of the mathematics involved in a TCAD simulation it is clear that  
148 the full set of traps coming from physical studies, for example given in [19], is non-practical in  
149 terms of computing resources. It is compulsory to choose an effective set of traps for modeling the  
150 measured and identified point and cluster defects. The mobility has also to take into account the  
151 traps (in Sentaurus, for example, using the Philips mobility model), specially when the detector is  
152 not fully depleted (i.e. when the carrier velocities are not saturated). Last but not least, the SRH  
153 trap statistics is not optimal in case of clusters so a parameter tweaking is also needed, in particular  
154 for deep traps that are responsible for the leakage current generation.

### 155 3. High fluence models

156 Recently the community presented several radiation damage models adjusted for the expected  
157 HL-LHC fluence. Fluence,  $\Phi$  is linearly related to trap density,  $N(\text{cm}^{-3}) = \eta\Phi$ , where  $\eta$  is the  
158 introduction rate. The three models discussed here use the Van Overstraeten-De Man avalanche  
159 model for impact ionization effects due to the high field strength in highly irradiated detectors (other

Defect Number	Type	Energy level (eV)	$\sigma_e[\text{cm}^{-2}]$	$\sigma_h[\text{cm}^{-2}]$	$\eta[\text{cm}^{-1}]$
1	Donor	$E_v + 0.48$	$2 \times 10^{-14}$	$1 \times 10^{-14}$	4
2	Acceptor	$E_c - 0.525$	$5 \times 10^{-15}$	$1 \times 10^{-14}$	0.75
3	Acceptor	$E_v + 0.90$	$1 \times 10^{-16}$	$1 \times 10^{-16}$	36

**Table 1:** LHCb high fluence defect model [20].

Type	Energy level (eV)	$\sigma_e(\text{cm}^{-2})$			$\sigma_h(\text{cm}^{-2})$			$\eta[\text{cm}^{-1}]$
		r1	r2	r3	r1	r2	r3	
Acceptor	$E_c - 0.42$	$1 \times 10^{-15}$	$1 \times 10^{-15}$	$1 \times 10^{-15}$	$1 \times 10^{-14}$	$1 \times 10^{-14}$	$1 \times 10^{-14}$	1.613
Acceptor	$E_c - 0.46$	$7 \times 10^{-15}$	$3 \times 10^{-15}$	$1.5 \times 10^{-15}$	$7 \times 10^{-14}$	$3 \times 10^{-14}$	$1.5 \times 10^{-14}$	0.9
Donor	$E_v + 0.36$	$3.23 \times 10^{-13}$	$3.23 \times 10^{-13}$	$3.23 \times 10^{-13}$	$3.23 \times 10^{-14}$	$3.23 \times 10^{-14}$	$3.23 \times 10^{-14}$	0.9

**Table 2:** "New Perugia" bulk damage, for three fluence ranges, r1: up to  $7 \times 10^{15} \text{ n}_{\text{eq}}/\text{cm}^2$ , r2:  $7 \times 10^{15} - 2.2 \times 10^{16} \text{ n}_{\text{eq}}/\text{cm}^2$  and r3:  $1.6 \times 10^{16} - 2.2 \times 10^{16} \text{ n}_{\text{eq}}/\text{cm}^2$ . For a given fluence range there is a capture cross section value associated for electrons and holes [21].

Interface Defect	Level(eV)	Concentration
Acceptor	$E_c - 0.4$	$N_{it} = 0.4 \times 0.85 \times N_{ox}$
Acceptor	$E_c - 0.6$	$N_{it} = 0.6 \times 0.85 \times N_{ox}$
Donor	$E_v + 0.7$	$N_{it} = 0.85 \times N_{ox}$

**Table 3:** "New Perugia" Interface Damage (oxide charge density  $N_{ox}$ , interface trap density  $N_{it}$ ) [22].

160 impact ionization models give 3-4% variation in CCE). The simplest one is explained in [20], from  
 161 the LHCb collaboration, and applied to VELO pixel detectors, valid up to  $8 \times 10^{15} \text{ n}_{\text{eq}}/\text{cm}^2$ . They  
 162 add a third acceptor level (3 in Table 1) to the EVL model. Cross sections are adjusted to experi-  
 163 mental results, with measurements from 200  $\mu\text{m}$  thick n-on-p sensors bump bonded to a TimePix3  
 164 readout chip. The model is able to capture the transition from a linear electric field/saturating I-V  
 165 curve to a double junction electric field/non-saturating I-V curve as a consequence of avalanche  
 166 generation in the high field regions of double junctions. For a center pixel hit the estimated CCE  
 167 has less than 10% of error compared with the measurements.

168 The "New Perugia" model, presented in 2015, [21, 22] is appropriate for higher fluences (up  
 169 to  $2.2 \times 10^{16} \text{ n}_{\text{eq}}/\text{cm}^2$ ), with one set of parameters for fluences up to  $7 \times 10^{15} \text{ n}_{\text{eq}}/\text{cm}^2$  and for the  
 170 range  $7 \times 10^{15} - 2.2 \times 10^{16} \text{ n}_{\text{eq}}/\text{cm}^2$ . It includes a modeling of bulk and also surface damage in the  
 171  $\text{Si} - \text{SiO}_2$  interface (in case of microelectronics or AC coupled detectors). The bulk model, Table  
 172 (2), derives from the "Old Perugia" model [23] and a literature survey made by the Perugia group.  
 173 The surface model, Table (3), was obtained from experimental measurements on gated diodes and  
 174 MOS capacitors, p-type substrate after  $\gamma$  irradiation (50-100 Mrad).

175 The latest damage model is the Hamburg PentaTrap Model (HPTM) (2018 [24]), see Table  
 176 4. It intends to describe at the same time I-V, C-V and CCE measurements on pad diodes irra-  
 177 diated with 24 GeV/c protons with fluences  $> 10^{15} \text{ n}_{\text{eq}}/\text{cm}^2$ . It is based on 5 traps, both cross  
 178 sections for E30K and the electron cross section for  $\text{C}_i\text{O}_i$  fixed and 12 free parameters adjusted to  
 179 simulation by optimization with the non-linear simplex method. The Sentaurus TCAD optimizer  
 180 minimize the relative deviation between the simulations and measurements over a large voltage

Defect	Type	Energy level (eV)	$\eta$ [cm <sup>-1</sup> ]	$\sigma_e$ [cm <sup>-2</sup> ]	$\sigma_h$ [cm <sup>-2</sup> ]
<i>E30K</i>	Donor	$E_c - 0.1$	0.0497	$2.300 \times 10^{-14}$	$2.920 \times 10^{-16}$
$V_3$	Acceptor	$E_c - 0.458$	0.6447	$2.551 \times 10^{-14}$	$1.511 \times 10^{-13}$
$I_p$	Acceptor	$E_c - 0.545$	0.4335	$4.478 \times 10^{-15}$	$6.790 \times 10^{-15}$
<i>H220</i>	Donor	$E_v + 0.48$	0.5978	$4.166 \times 10^{-15}$	$1.965 \times 10^{-16}$
$C_iO_i$	Donor	$E_v + 0.36$	0.3780	$3.230 \times 10^{-17}$	$2.036 \times 10^{-14}$

**Table 4:** Hamburg Pentatrap Model [24].

181 range, specifically it minimizes F in Eq.(3.1):

$$F = \sum_{i,j} w_i^j \int_{V_{min}}^{V_{max}} \left(1 - \frac{Q_{i,sim}^j}{Q_{i,meas}^j}\right)^2 dV \quad (3.1)$$

182 where  $i$  runs over different fluences,  $j$  runs over the different measurements with  $Q_{i,sim}^j$  and  $Q_{i,meas}^j$   
 183 are the simulated and measured quantities (currents, capacitances and CCE's).  $V_{min}, V_{max}$  are the  
 184 minimum and maximum voltages and  $w_i^j$  are weighting factors to weight the different kind of  
 185 measurements. The simulations for optimization were made at  $-20^\circ\text{C}$  with Slotboom bandgap  
 186 narrowing, TAT Hurkx with tunnel mass of  $0.25 m_e$  (default value  $0.5 m_e$ ) for defect  $I_p$ , relative  
 187 permittivity of Silicon 11.9 (default value 11.7). The calibration measurements were made on  $2 \times 2$   
 188 and  $5 \times 5 \text{ mm}^2$   $200 \mu\text{m}$  thick float zone p-type pad diodes (with p-stop and p-spray). The electrical  
 189 characterization was made after 80 min of annealing at  $60^\circ\text{C}$ . Measurements were performed at  
 190  $-20^\circ\text{C}$ , consisting in I-V up to 1000 V (reverse) and up to a current limit of 0.5 mA (forward),  
 191 C/G-V measurements with 100 Hz-2MHz of excitation frequency and laser TCT measurements at  
 192 670 nm (red) and 1064 nm (IR) wavelengths.

193 The I-V/C-V and the CCE-V simulations agree with the measurement results within 20% for  
 194 all fluences ( $0.3$  to  $13 \times 10^{15} \text{ n}_{eq}/\text{cm}^2$ ) in the voltage range (-1000 to 0 V). It also reproduces the  
 195 double peak structure (E-field vs position) for fluences  $\geq 3 \times 10^{15} \text{ n}_{eq}/\text{cm}^2$ , with a peak field of  
 196  $\simeq 2 \times 10^5 \text{ V}/\text{cm}$  at the highest fluence, responsible for impact ionization.

197 The previous defect models were not able to simulate the acceptor removal effect, specially  
 198 relevant in LGAD-type devices [25]. At the present state of knowledge, we use Eq.(1.1) to redefine  
 199 the p-gain layer doping profile,  $N_{A,p\text{gain}}$  in the device model previous to the simulation. A full sim-  
 200 ulation of an irradiated LGAD-type sensor also has to include a defect model to take into account  
 201 the traps introduced due to radiation.

## 202 4. Simulation Examples

203 As an example of the combination of the "New Perugia" model with the acceptor removal  
 204 effect, we present a simulation effort for LGAD devices [26] made with TCAD Sentaurus from  
 205 Synopsys, see Table 5. The objective for that work was to show that radiation damage in LGAD  
 206 can reduce the charge gain when approaching to high fluences due to the acceptor removal effect  
 207 (with minor influence due to the appearance of the double junction effect). For that work we  
 208 made a 2D simulation of a  $300 \mu\text{m}$  thick LGAD, 5 mm length, biased to 400 V, at 253K with an  
 209 acceptor removal constant  $c = 4 \times 10^{-16} \text{ cm}^2$ . The detector model excitation was a red laser pulse,



Fluence n/cm <sup>2</sup>	Charge LGAD(C)	Charge PIN(C)	Gain $Q_{lgad}/Q_{pin}$
No Irrad	9.86e-15	2.01e-15	4.91
$1 \times 10^{13}$	9.46e-15	2.00e-15	4.72
$1 \times 10^{14}$	6.77e-15	1.95e-15	3.46
$1 \times 10^{15}$	1.74e-15	1.22e-15	1.42
$2 \times 10^{15}$	1.28e-15	1.19e-15	1.08

**Table 5:** LGAD simulation example [26].

210 illuminating through the p<sup>++</sup> layer,  $\lambda = 670$  nm, 10  $\mu$ m of spot radius, 50 W/cm<sup>2</sup> and 200 ps of  
 211 duration. We compared the simulations of the LGAD (Van Overstraeten-De Man avalanche model)  
 212 with its associated PIN (same device but without the gain p-layer), defining the gain as the quotient  
 213 of the cumulated charges, Gain =  $Q_{lgad}/Q_{pin}$ .

214 The LGAD device evolved to the iLGAD [27]. The iLGAD is a strip detector with intrinsic  
 215 gain generated in a gain layer on the non-segmented side of the sensor. Conventional segmentation  
 216 of a LGAD, at the n+ ohmic side, means also non-uniformities in the multiplication. The iLGAD  
 217 has the segmentation at the p+ ohmic side so the p-multiplication layer is continuous below the n+  
 218 ohmic side. The CCE simulation [28] showed the iLGAD at room temperature (300K, "New Pe-  
 219 rugia" defect model) and at the expected operation temperature (HPTM defect model, specifically  
 220 appropriated at 253K), with 300 V bias, under same laser excitation (red laser hit at the right center  
 221 strip segment) and higher damage fluences (acceptor removal constant  $c = 4 \times 10^{-16}$  cm<sup>2</sup>). The  
 222 results are shown in Table 6 where we see an improvement of the CCE at 253K. The agreement  
 223 with measurements is around 20%.

224 The last example, presented at [29] and also made with TCAD Sentaurus, simulates a mono-  
 225 lithic detector called OVERMOS. It is a CMOS Monolithic Active Pixel Sensor (MAPS) fabricated  
 226 with the Tower Jazz 180 nm technology kit. The novelty of this simulation is it also has to take into  
 227 account TID effects because there are dielectrics (SiO<sub>2</sub>) over the active regions. In the simulation  
 228 model the impact ionization was considered with the UniBo model to take into account possible  
 229 avalanche effects due to a high concentration of defects. The model for defects is twofold: HPTM  
 230 for the bulk region (with a factor of 1.66 multiplying all the HPTM introduction rates to account  
 231 for neutron irradiation) and the "New Perugia" for the interface traps [22]. The TID model includes  
 232 fixed oxide charge,  $N_{ox}$  and interface traps,  $N_{it}$  with  $N_{ox} = 1.2 \times 10^{11}$  cm<sup>-3</sup> and  $N_{it} = 0.85 \times N_{ox}$ . The  
 233 interface traps have a gaussian distribution with  $\sigma = 0.7$  eV and a cross-section of  $1 \times 10^{-15}$  cm<sup>-2</sup>.

234 The breakdown voltage, defined as  $(\Delta I/\Delta V)_{max}$ , shows an agreement up to  $\sim 4$  V. The I-V  
 235 simulations show a  $\sim 30\%$  agreement with the measurements, for fluences in the range  $10^{13}$ - $10^{15}$   
 236 n<sub>eq</sub>/cm<sup>2</sup>. For CCE simulations using laser injection (center pixel hit,  $\lambda = 1064$  nm, pulse energy 25  
 237 pJ, pulse width 7.8 ns, laser window  $5 \times 5 \mu$ m<sup>2</sup>) the agreement is acceptable between the measured  
 238 and simulated collected charge,  $Q_{coll}$ , as shown in Table 7.

## 239 5. Conclusions

240 Simulation of irradiated sensors under HL-LHC expected high fluences is an ongoing work in  
 241 the RD50 collaboration. The TCAD software is well understood, specially in the case of TCAD

Fluence $n/cm^2$	Charge(fC)(300K)	% reduction	Charge (fC)(253K)	% reduction
No Irrad	$8.24 \times 10^{-1}$	-	1.08	-
$1 \times 10^{14}$	$5.26 \times 10^{-1}$	63.8%	$7.41 \times 10^{-1}$	68.6%
$1 \times 10^{15}$	$2.79 \times 10^{-1}$	33.8%	$5.67 \times 10^{-1}$	52.5%
$7.5 \times 10^{15}$	$6.69 \times 10^{-2}$	8.1%	$1.5 \times 10^{-1}$	13.8%

**Table 6:** iLGAD simulation example [28]“New Perugia” defect model for 300K, HPTM defect model for 253K, acceptor removal constant  $c = 4 \times 10^{-16} cm^2$ , red laser:  $\lambda = 670$  nm,  $10 \mu m$  of spot radius,  $50 W/cm^2$ , 200 ps of pulse width..

Fluence ( $n_{eq}/cm^2$ )	$Q_{coll}$ (fC) Test	$Q_{coll}$ (fC) Simulation	$\Delta\%$
No Irrad	153	166	-8.4
$1 \times 10^{13}$	110	143	-30
$5 \times 10^{13}$	106	82	22
$1 \times 10^{14}$	65	53	18
$5 \times 10^{14}$	27	23	-14
$1 \times 10^{15}$	10	17	70

**Table 7:** CCE OVERMOS pixel simulation, 1064 nm laser hit [29].

242 Sentaurus from Synopsys, and incremental improvements has been added by means of tailor made  
 243 functions. The available defect models give a reasonable precision in terms of general behavior  
 244 but with errors around 20% when compared with measurements for bulk devices. The simulations  
 245 for non-irradiated MAPS devices show the same 20% agreement but there are bigger discrepancies  
 246 for the irradiated ones. Besides that, every device needs a specific defect modeling, for example  
 247 acceptor removal effect for the LGAD family or surface defects for MAPS. TCAD simulation is an  
 248 excellent tool to understand the device behavior under radiation damage but the predictive power  
 249 needs to be improved. The RD50 collaboration is actively working in that direction.

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