

Searching for exotic B -meson decays enabled by the CMS L1 track trigger

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The CMS phase II track trigger may allow for a displaced dimuon vertex trigger with qualitatively lower p_T thresholds than existing dimuon triggers. With this technique, we show that the CMS reach for exotic B -meson decays involving a displaced dimuon resonance, such as a light, Higgs-mixed scalar, can be competitive with that of LHCb and Belle II.

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I. INTRODUCTION

The high luminosity runs of the LHC will deliver an enormous sample of $\sim 10^{15}$ B mesons to both ATLAS and CMS, far exceeding the number attainable at any other experiment in the near future. Capitalizing on this scientific opportunity will require the experiments to circumvent the trigger and background limitations inherent to a high energy hadron collider. The LHCb collaboration will do so through high precision tracking in the forward region, sophisticated online event reconstruction, and an order of magnitude reduction in instantaneous luminosity relative to ATLAS and CMS. The phase II upgrades of ATLAS and CMS on the other hand will enable tracking at the hardware trigger [1,2], which may substantially enhance their sensitivity to exotic B decays [2,3].

Concretely, it has been shown that the CMS L1 track trigger could conceivably be configured to enable the reconstruction of displaced tracks with impact parameters as large as a few cm [2,4,5]. This opens up qualitatively new opportunities to trigger on signatures involving displaced jets [2,4–7]. The L1 tracks can moreover be matched to the muon chamber [2], and it has been argued that as a result the background rate for a low threshold, dimuon vertex trigger may also not be prohibitive [3]. Concretely, identifying the dimuon displaced vertex already at the L1 trigger would enable CMS to significantly lower the p_T thresholds on the muons, which is crucial for signatures from exotic B -meson decays.

In this paper, we explore the off-line discovery potential of such a trigger in the context of exotic B -meson decays, with the aim of further motivating the experimental developments in this direction. In particular, we assert that the theory motivation for this program is very strong: a number of models feature a new dimuon resonance below the B mass (see, e.g., [8–13]), which is likely to be long lived, providing an excellent handle to reject backgrounds. For example, one of the most minimal extensions to the Standard Model (SM) adds a singlet scalar field ϕ , which mixes with the SM Higgs through either

$$\begin{aligned} \mathcal{L} &\supset m\phi H^\dagger H \quad \text{with } m \ll m_W, \quad \text{or} \\ \mathcal{L} &\supset -\mu^2\phi^2 + \epsilon\phi^2 H^\dagger H \quad \text{with } \mu^2 > 0. \end{aligned} \quad (1)$$

In either case, in the mass basis, ϕ couples to all SM fermions proportional to their masses, but suppressed by the mixing angle (s_θ) between ϕ and the SM Higgs. For $m_K - m_\pi < m_\phi < m_B - m_K$, the dominant production mode at a hadron collider is through an electroweak penguin inducing the $B \rightarrow \phi X_s$ decay [14–16]. Due to the extremely small width of the B meson, this branching ratio can be large even for $s_\theta \ll 1$. The branching ratio for $\phi \rightarrow \mu\mu$ is moreover between 0.1 and 0.01 for most of the relevant mass range [17], although it is subject to substantial theoretical uncertainties. Importantly, existing limits on s_θ [18,19] already bound the minimal allowed lifetime of ϕ to be of the order of ~ 1 cm. Displaced searches are therefore vital to probe this model any further.

The LHCb collaboration has already performed dedicated searches for this model in the exclusive $B^+ \rightarrow K^+\mu^+\mu^-$ [18] and $B^0 \rightarrow K^*\mu^+\mu^-$ [19] channels, and has robustly excluded lifetimes $c\tau \lesssim 1$ cm for $m_\phi \lesssim 3$ GeV. Our proof-of-concept analysis differs from the LHCb approach in two crucial points: (i) we suggest an *inclusive*

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search, which increases the signal acceptance, and (ii) the background will instead be suppressed by imposing isolation requirements and a hard cut on the transverse displacement of ϕ 's decay vertex. Though it requires higher p_T thresholds than LHCb, the geometric acceptance of a cylindrical detector such as CMS is substantially higher than that of LHCb's vertex locator for transverse displacements of more than a few cm.¹ When the additional selections imposed in the LHCb exclusive searches are also considered, we find a comparable signal efficiency in both cases, giving CMS an advantage due to its higher overall integrated luminosity.

This paper is organized as follows: in Sec. II we define the signal model and the corresponding event generation. The main backgrounds are discussed in Sec. III and the analysis strategy is presented in Sec. IV. We present our results in Sec. V.

II. SIGNAL DEFINITION

For the model in (1), the production of the exotic state ϕ occurs through an electroweak penguin, with an estimated inclusive branching ratio of $\text{Br}[B \rightarrow X_s \phi] \approx 6.2 \times s_\theta^2$ [14–16]. One of the main features of an inclusive analysis at CMS is that it would be relatively insensitive to the particular decay mode of the B^0/B^\pm , since only the daughter muons of ϕ are being used. There is however a mild dependence on the exclusive decay channels of B^0/B^\pm due to the isolation criteria on the muons. For this reason, we implement the most important exclusive branching ratios [23] in our simulation of the signal (see Table I). For the total branching ratio of B^\pm/B^0 into ϕ we will conservatively use the sum of the exclusive modes, which is about a factor of two smaller than the inclusive calculation. For the differential distributions we rely on PYTHIA8 [24], which we normalize to the overall inclusive cross section as computed with FONLL [25–28].

The decays of ϕ are determined by its effective Yukawa couplings to the lower generations of the SM fermion as well as through mixing with (broad) QCD spin 0 resonances. (See [17] for a recent calculation.) The theoretical uncertainties on the lifetime of ϕ and branching fraction into muons are substantial, however these uncertainties will ultimately drop out from the projected limits we obtain in the s_θ vs m_ϕ plane, as explained in Sec. V. While the model is fully specified by the mass and the mixing angle (m_ϕ, s_θ) , we will also present the result in a more model independent fashion, as is customary in the experimental literature. Concretely, the reach will be parametrized in

¹For dark photon models on the other hand, $c\tau$ tends to be smaller and production is more forward, allowing substantial progress to be expected at LHCb in run 3 and beyond [20–22]. We suspect that in particular the exclusive approach of LHCb [20] will outperform an inclusive strategy at CMS, but a detailed study of this scenario is left for future work.

TABLE I. $\text{Br}[B^\pm \rightarrow \phi X_s]/s_\theta^2$ for the dominant exclusive channels [23]. The branching ratios for various K^* , K_1 , and K_0^* resonances were summed together. Analogous branching ratios for B^0 can be obtained by multiplying with 0.93. The last line shows $\text{Br}[\phi \rightarrow \mu\mu]$ as computed in [17].

Channel	$m_\phi = 0.5$ GeV	$m_\phi = 2$ GeV
$B^\pm \rightarrow \phi K_1^\pm$	0.94	0.86
$B^\pm \rightarrow \phi K_0^{*\pm}$	0.86	0.97
$B^\pm \rightarrow \phi K^{*\pm}$	0.81	0.73
$B^\pm \rightarrow \phi K^\pm$	0.43	0.47
$B^\pm \rightarrow \phi K_2^{*\pm}$	0.29	0.11
$B^\pm \rightarrow \phi \pi^\pm$	0.012	0.014
Total	3.35	3.16
$\phi \rightarrow \mu\mu$	0.12	0.18

terms of m_ϕ , $\text{Br}[B \rightarrow X_s \phi] \times \text{Br}[\phi \rightarrow \mu\mu]$, and $c\tau$, where the latter is the proper lifetime of ϕ .

It is very computationally inefficient to compute the signal acceptance by generating separate samples for each different value of $c\tau$. Instead, we generate samples with a stable ϕ and analytically compute the weight for each event by evaluating

$$w_{c\tau} = \int_{L_{xy}^-}^{L_{xy}^+} dL_{xy} \epsilon(L_{xy}) e^{\frac{-L_{xy} \cosh \eta_\phi}{\beta\gamma c\tau}}, \quad (2)$$

with L_{xy} the distance of the vertex to the beam line. η_ϕ and $\beta\gamma$ are the pseudorapidity and the boost of ϕ . L_{xy}^- and L_{xy}^+ represent the boundaries of the fiducial region under consideration and $\epsilon(L_{xy})$ is the estimated trigger efficiency from the Appendix of [3], which is above 0.8 over the region of interest.

III. BACKGROUNDS

There are many potential backgrounds that can mimic the displaced dimuon signal, which can be usefully classified into two categories: non- B and B backgrounds. Non- B backgrounds include overlapping pileup muons, fake vertices, cosmic muons, and secondary vertices from interactions with the detector material. In what follows we assume these non- B backgrounds can be removed with techniques such as masking known detector material, vetoing muon pairs with large opening angles, etc., that we further assume will have a negligible impact on the signal efficiency. These assumptions are perhaps bold, but are supported by the many ingenious searches for long-lived particles that have already been performed (see, e.g., [29–33]). The background assumption in particular has moreover proven to be valid in a recent ATLAS search [34], though the selection and luminosity we assume here are certainly more aggressive than those in [34].

The B backgrounds are all dimuon signatures that originate from a parent b quark. The displacement in these scenarios is mostly, if not entirely, due to the finite lifetime of the B meson itself, with $c\tau_B \sim 500 \mu\text{m}$. A hard cut on the displacement of the secondary vertex implies that the B mesons which do decay in the signal region are typically very boosted. The daughter muons of the B are therefore usually not isolated. The B backgrounds include $b \rightarrow X_s \mu^+ \mu^-$, $b \rightarrow X + \psi(nS) \rightarrow \mu^+ \mu^-$, and $b \rightarrow \mu\nu(X_c \rightarrow \mu\nu X_s)$. We will discuss these backgrounds in the following paragraphs.

The $\text{BR}(b \rightarrow X_s \mu^+ \mu^-) \sim 4 \times 10^{-6}$ is small enough to suppress it far below the other two major B backgrounds. The $J/\psi(1S)$ resonance on the other hand appears in over 1% of all B meson decays, and nearly 6% of those decay into $\mu^+ \mu^-$. This large background, along with other resonances, including the η , ω , $\phi(1020)$, and higher $\psi(nS)$, are confined the narrow mass peak and could be vetoed easily if needed.² However, the cuts we will apply in Sec. IV seem effective at controlling even the J/ψ background without vetoing the mass window.

The largest contribution to the continuum of the dimuon invariant mass distribution is from events where the B undergoes a semileptonic decay, $b \rightarrow \mu\nu X_c$, followed by a semileptonic D decay providing the second muon. As each semileptonic branching fraction is a little over 10% to muons, naively 10^{13} B s at the HL-LHC would result in this signature. However, there are some useful ways to reduce this background. First, due to the secondary displacement of the D meson, the muon tracks from the B and D do not originate from the same point. While it is often the case that the resulting vertexing fit is of high enough quality to mimic a common point of origin, a sizable fraction can be discarded based on a vertexing requirement. We impose a conservative vertexing quality cut of $\sigma_v = 100 \mu\text{m}$, i.e., that the distance of closest approach for the two tracks is less than σ_v ,³ which rejects $\sim 50\%$ of the background. Second, the p_T values of the two muons are typically fairly different, which is not the case for the signal. In practice this means that the muon from the D meson decay often falls below our p_T threshold.

The B background differential distributions were simulated with PYTHIA8 [24], and its overall cross section normalized to $500 \mu\text{b}$. Figure 1 shows the resulting invariant mass spectrum, subjected to the various cuts outlined in Sec. IV. (See Table II for a summary.) The J/ψ resonance is clearly visible. The ω , ρ , ϕ , and η mesons were also explicitly included, but their contribution after cuts proved to be negligible compared to the continuum.

²The ρ in particular may be too broad for a mass veto, and tightening the L_{xy} cut could be more a more promising alternative.

³For all our background samples, we conservatively assume 100% reconstruction and trigger efficiency for both muons, regardless of their impact parameters.

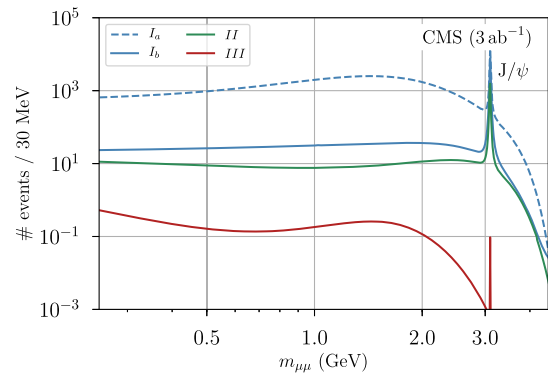


FIG. 1. Background component from B -meson decays for the cuts specified in Table II. (See Sec. IV for details.)

The solid (dashed) blue curves assume only a few baseline cuts with (without) imposing an isolation criterion on both muons. The green and red curves indicate the effects of additional cuts on the ϕ 's impact parameter and the muon p_T , respectively, as detailed in the next section.

IV. ANALYSIS STRATEGY

Nearly all of the B background can be controlled by simply cutting very hard on the transverse distance between the decay vertex and the beam line (L_{xy}). In addition we suggest a few additional cuts that could further reduce the background by a few orders of magnitude at minimal cost to the signal efficiency. The cut flow is summarized in Table II. The definition of our variables is explained in the text below.

The CMS L1 track trigger may reasonably record dimuon pairs with a p_T as low as roughly 4 GeV each [3]. To reduce uncertainties due to so far unknown trigger efficiency turn-on near threshold, we will require $p_T > 4.5$ GeV. Both muons are moreover required to satisfy $|\eta| < 2.4$. For the estimated efficiency of the trigger we follow [3], which is based on a simplified simulation of the L1 track trigger developed in [4]. For the L_{xy} and p_T range

TABLE II. Efficiency of each consecutive set of cuts, relative to the preceding set or cuts, for $m_\phi = 2$ GeV, $c\tau = 5$ cm. The isolation variable δ is defined in (3). I_a and I_b represent the baseline cuts without and with isolation, respectively. The I_a selection was normalized with respect to the inclusive B -meson cross section of $500 \mu\text{b}$ times $\text{Br}[B \rightarrow X_s \phi] \times \text{Br}[\phi \rightarrow \mu\mu]$. The cuts II and III in particular further reduce the background (see Fig. 1) without significantly impacting the signal efficiency.

	Cuts	Signal efficiency
I_a	$p_T > 4.5$ GeV and $ \eta < 2.4$ and $L_{xy} > 7.5$ cm	2×10^{-3}
I_b	I_a and $\delta < 0.1$	0.68
II	I_b and $L_{xy}/d_\phi > 200$	0.96
III	II and $\sum p_{T_\mu} < 25$ GeV	0.98

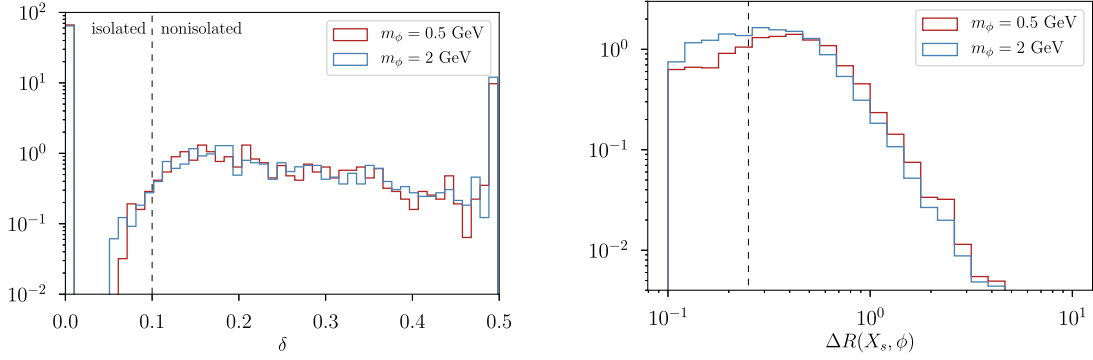


FIG. 2. Left: isolation variable δ for two signal benchmarks. The rightmost bin is an overflow bin, containing all events with $\delta > 0.5$. The isolation efficiencies for the $m_\phi = 0.5$ GeV and $m_\phi = 2$ GeV benchmarks are 0.68 and 0.66, respectively. Right: truth level ΔR between ϕ and its sister meson. The vertical dashed line indicates the isolation cone of $\Delta R = 0.25$.

of interest to us, this corresponds to a flat trigger efficiency of roughly 85%. In particular, for $L_{xy} > 35$ cm the efficiency drops to zero as the muons leave an insufficient number of stubs in the outer tracker to reliably reconstruct a track. We require $L_{xy} < 30$ cm and take $L_{xy} > 7.5$ cm as a baseline cut to suppress the B background.⁴

We further define an isolation variable (δ) for each muon as the scalar sum of the p_T of each track with $p_T > 0.7$ GeV within a cone defined by $\Delta R < 0.25$, divided by the muon p_T :

$$\delta \equiv \sum_{i \in \text{tracks}} \frac{p_{T_i}}{p_{T_\mu}} \quad \text{with} \quad \begin{array}{l} p_{T_i} > 0.7 \text{ GeV} \\ \Delta R < 0.25 \end{array}. \quad (3)$$

The muons themselves are not counted towards each others isolation variable δ . A muon is considered isolated if $\delta < 0.1$; we require both muons to satisfy this criterion. Although the dimuon pair originates from a B decay, both muons are nevertheless isolated in about two out of three events passing the other fiducial selections outlined above. Due to the mild p_T requirements, the B mesons which produce most of the signal only have a boost of $\mathcal{O}(\text{few})$, leading to relatively wide opening angles between ϕ and its strange sister meson. This is shown in the right-hand panel of Fig. 2, for the exclusive decay paths in Table I. While this feature must be verified in data, e.g., by making use of $B \rightarrow J/\psi X$ transitions; in simulation, it is robust when initial and final state radiation are included.

Aside from the simple baseline selection laid out above, we suggest two additional cuts which prove very effective at reducing the B backgrounds. First, one observes that in the limit where $c\tau_B \rightarrow 0$ and perfect reconstruction, the reconstructed trajectory of ϕ should point back to the primary vertex. Defining the parameter d_ϕ as the distance of closest approach between the primary vertex and the

reconstructed ϕ trajectory, we thus find the following scaling

	Background	Signal
L_{xy}	$\sim c\tau_B$	$\sim c\tau_\phi$
d_ϕ	$\sim c\tau_B$	$\sim c\tau_B$

in the limit where $c\tau_\phi \gg c\tau_B$. As shown by the green curve in Fig. 1, a hard cut on the dimensionless ratio $L_{xy}/d_\phi > 200$ is therefore very effective at further suppressing the B -meson background, with only $\sim 4\%$ reduction in signal efficiency.

Finally, given that $c\tau_B \ll 7.5$ cm, any background events that pass the above set of cuts are typically very boosted. Cutting on the scalar sum of the muon p_T , $\sum p_{T_\mu} < 25$ GeV, removes any residual, boosted background events, without reducing the signal efficiency. The distributions of the L_{xy}/d_ϕ and $\sum p_{T_\mu}$ variables and their correlations are shown in Fig. 3 for signal and background. Due to the substantial anticorrelation of these two cuts on the background, they are most effective when applied together.

V. RESULTS

In our reach estimates, we impose the most stringent selection, corresponding to signal region III in Table II. This corresponds to the red curve in Fig. 1, where we see that the B -meson background can be reduced to negligible levels, assuming an invariant mass resolution of ~ 30 MeV [36]. The resulting sensitivity in the model-independent parametrization is shown in Fig. 4. The CMS HL LHC data will improve the existing limits by several orders of magnitude, and could moreover outperform LHCb's HL LHC reach.⁵ For this comparison, we extrapolated the

⁴Alternatively, one may cut on the transverse impact parameter of the individual tracks ($|d_0|$), as was done for in the CMS search for displaced lepton jets [35].

⁵Should a signal be found with the inclusive approach we advocate, a follow-up analysis where the full decay chain is reconstructed will still be important to validate and characterize the signal.

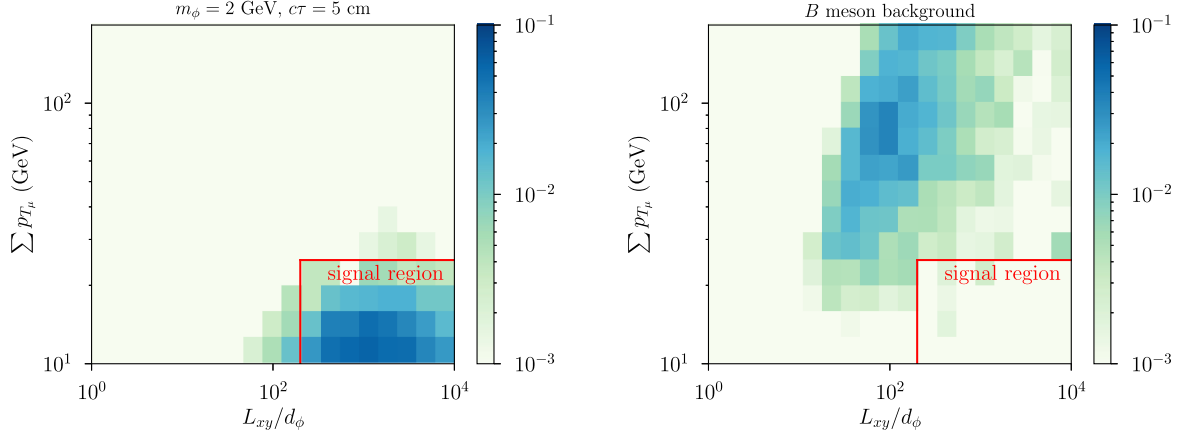


FIG. 3. Distribution of a signal benchmark (left) and background (right) for the L_{xy}/d_{ϕ} and $\sum p_{T_{\mu}}$ variables, after imposing the baseline cuts and isolation requirements (L_b in Table II). The red box indicates the signal region.

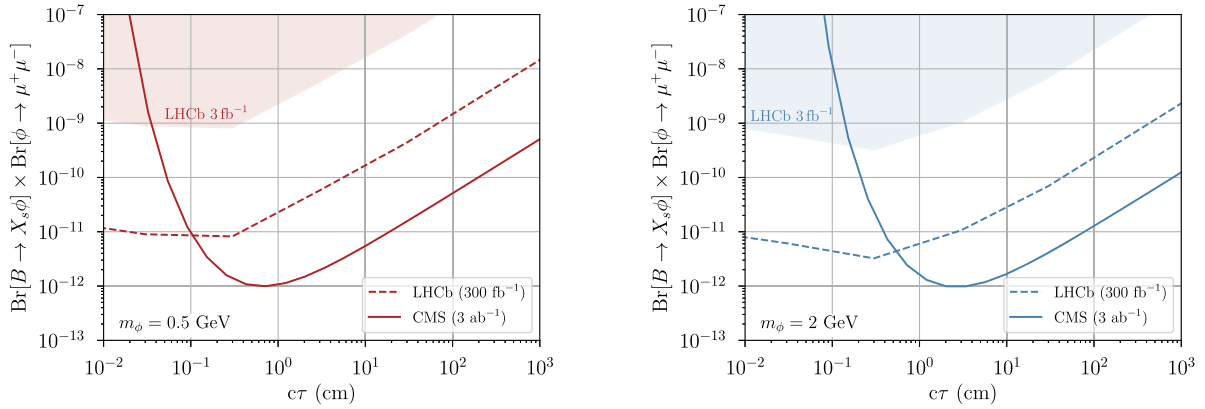


FIG. 4. Projected reach in the model independent parametrization, for the cuts in Table II. Left: $m_{\phi} = 0.5$ GeV; Right: $m_{\phi} = 2$ GeV. Shaded region and dashed line represent the existing LHCb limits [18] and an optimistic extrapolation of the LHCb reach. (See text.)

LHCb reach to 300 fb^{-1} in the most optimistic manner by assuming that the existing analysis continues to be largely background free, with negligible losses in signal efficiency. We reiterate however that our results for CMS are also optimistic, since we assumed that the non- B backgrounds can be suppressed to negligible levels, which, while plausible, may not be attainable in practice.

In the regime where the lab frame flight distance of ϕ exceeds the lower cut on L_{xy} , the reach scales as $\sim c\tau/(L_{xy}^+ - L_{xy}^-)$ with L_{xy}^+ (L_{xy}^-) the upper (lower) cut on L_{xy} . It is therefore natural to ask whether the L_{xy} upper cut can be relaxed further by using stand-alone muons. Searches of this sort in fact already [37,38] exist, but due to the reduced momentum and vertex resolutions for stand-alone muons, we suspect that this type of analysis would have substantially larger backgrounds or would require higher p_T thresholds.

In addition to the model-independent parametrization, it is useful to map the reach on the concrete model of a light scalar mixing with the Higgs, as defined by Eq. (1).

The resulting reach is shown in Fig. 5. In addition to the existing bounds from LHCb [18] and LSND [39], we furthermore show contours of the proper lifetime of ϕ in this model. In the lower edge of the reach, this reveals that the typical lab frame flight distance of ϕ exceeds the spatial dimensions of the fiducial volume. This implies the signal yield is proportional to

$$N_{\text{sig}} \sim \text{Br}[B \rightarrow X_s \phi] \times \text{Br}[\phi \rightarrow \mu\mu] \times \frac{L_{xy}^+ - L_{xy}^-}{c\tau} \times \mathcal{L} \\ \sim \frac{\Gamma_{\phi \rightarrow \mu\mu}}{s_{\theta}^2} \times (L_{xy}^+ - L_{xy}^-) \times s_{\theta}^4 \times \mathcal{L}, \quad (4)$$

where $\Gamma_{\phi \rightarrow \mu\mu}$ is the partial width of ϕ to muons and \mathcal{L} is the integrated luminosity. Since the $\Gamma_{\phi \rightarrow \mu\mu}/s_{\theta}^2$ combination is independent of s_{θ} , this makes explicit that the reach, when mapped on to (m_{ϕ}, s_{θ}) , scales as the fourth root of the luminosity, under the assumption of zero background. In addition, the total width of ϕ drops from the

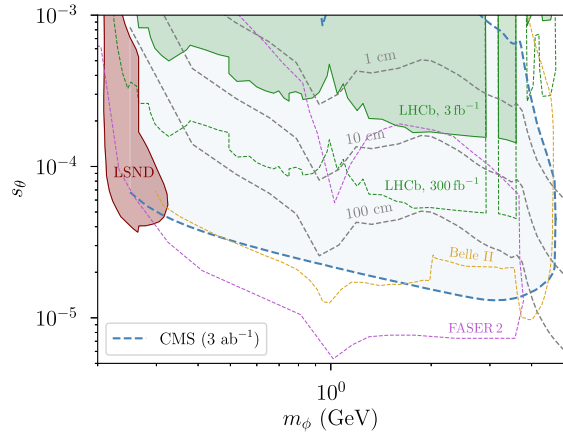


FIG. 5. Projected reach in terms of the mass (m_ϕ) and mixing angle (s_θ) of a light scalar mixing with the SM Higgs. Shaded regions represent the existing LHCb [18] and LSND [39] limits. The dashed gray contours indicate the proper lifetime of ϕ [17]. We also show projections for Belle II [40] and the FASER upgrade [41].

expression, greatly reducing the theoretical uncertainties. This moreover explains why the projected limit is a relatively featureless curve, especially in comparison to the more complex lifetime contours.

Looking ahead, both LHCb and Belle II are in strong positions to (further) weigh in on this signature. LHCb in

particular is expected to continue to provide the best limits for $c\tau \lesssim 1 \text{ cm} \times \frac{m_\phi}{\text{GeV}}$, while Belle II is expected to further improve limits in the long lifetime regime, especially with their ultimate dataset [40,42,43]. More broadly, low mass dimuon resonances may be produced in a variety of other ways, such as through exotic Higgs decays or as part of more elaborate hidden sectors. The HL LHC in general and CMS in particular could have excellent reach for such resonances, regardless how they are being produced.

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