

ATLAS measurements of transverse and longitudinal flow fluctuations

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arXiv:2001.04201

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For the ATLAS Collaboration

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Hard Probes 2020



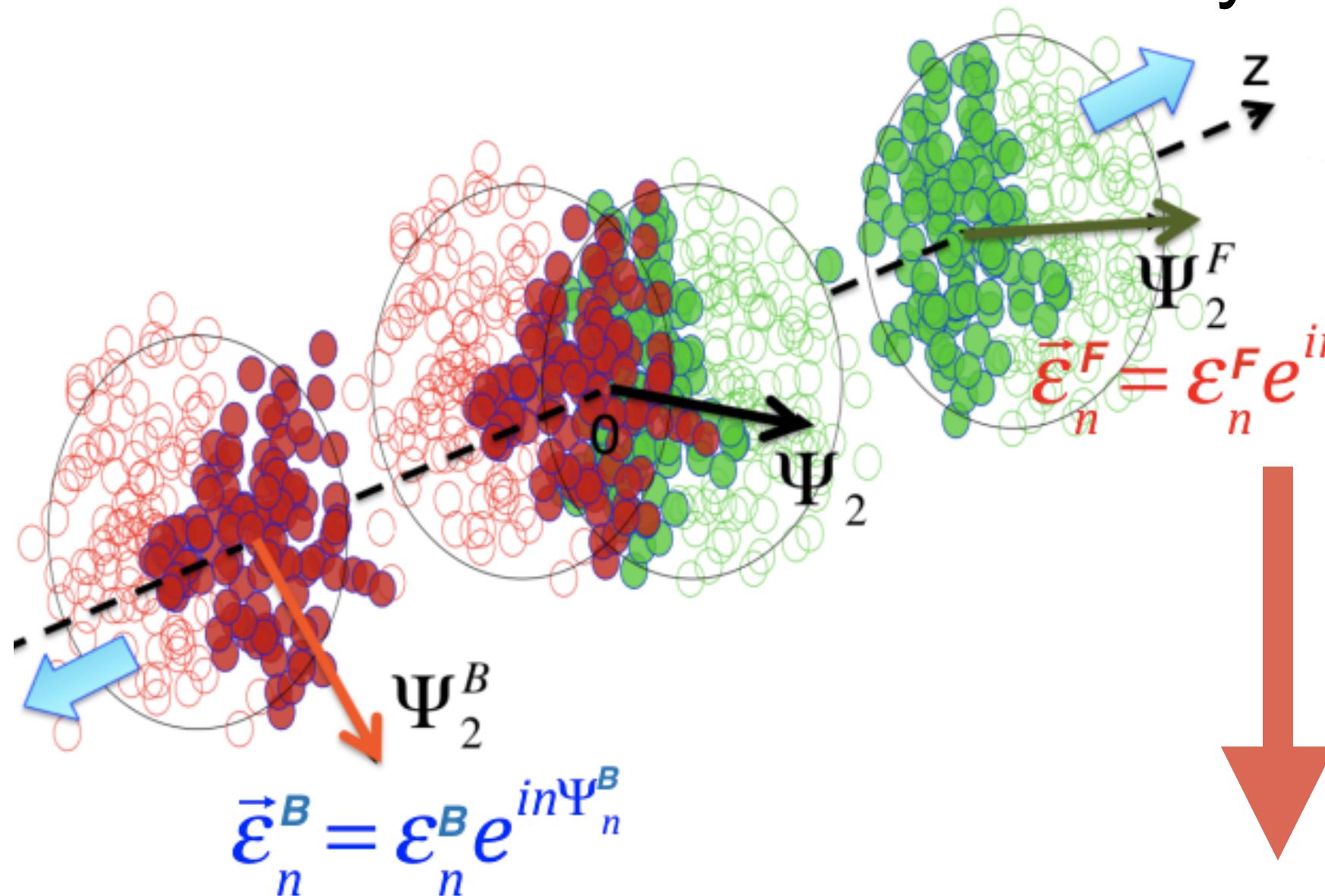
Stony Brook
University



Flow - Flow and Decorrelation

2

- Initial state fluctuations - FB asymmetry in eccentricities



$$\vec{\epsilon}_n^F \neq \vec{\epsilon}_n^B$$

$$\vec{\epsilon}_{n+} = (\vec{\epsilon}_n^F + \vec{\epsilon}_n^B)/2 \implies \text{Average Flow}$$

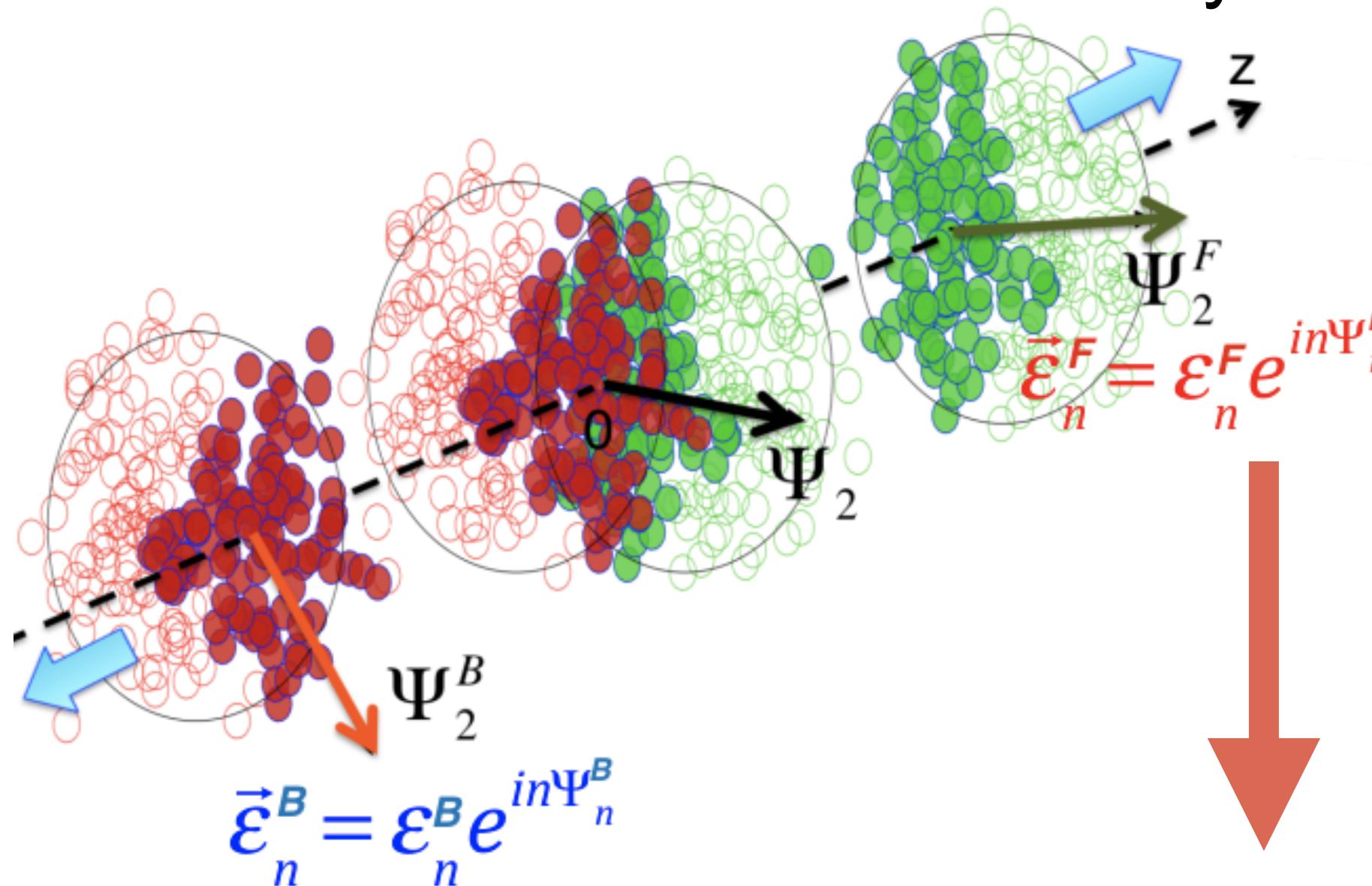
$$\vec{\epsilon}_{n-} = (\vec{\epsilon}_n^F - \vec{\epsilon}_n^B)/2 \implies \text{Longitudinal Fluctuation}$$

arXiv:1701.02183

Flow - Flow and Decorrelation

2

- Initial state fluctuations - FB asymmetry in eccentricities



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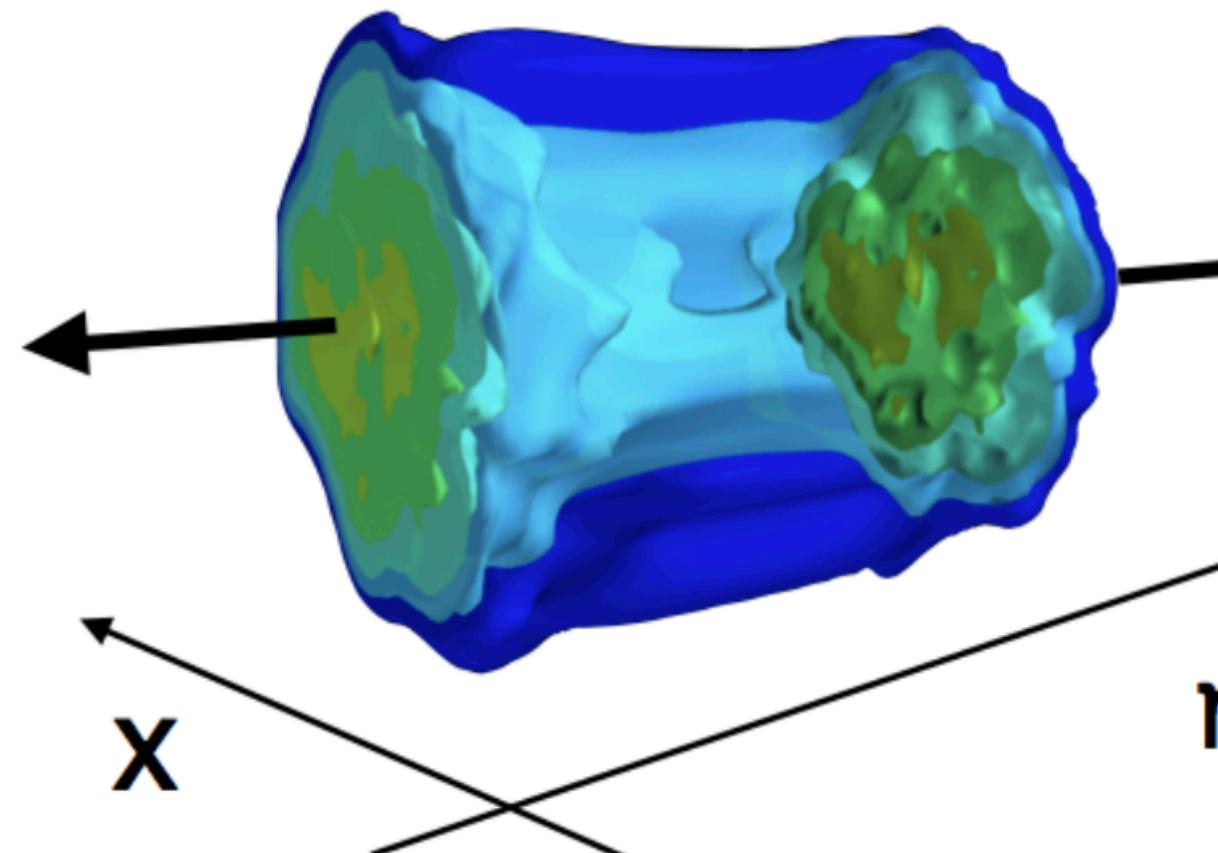
$$\vec{\epsilon}_n^F \neq \vec{\epsilon}_n^B$$

$$\vec{\epsilon}_{n+} = (\vec{\epsilon}_n^F + \vec{\epsilon}_n^B)/2 \implies \text{Average Flow}$$

$$\vec{\epsilon}_{n-} = (\vec{\epsilon}_n^F - \vec{\epsilon}_n^B)/2 \implies \text{Longitudinal Fluctuation}$$

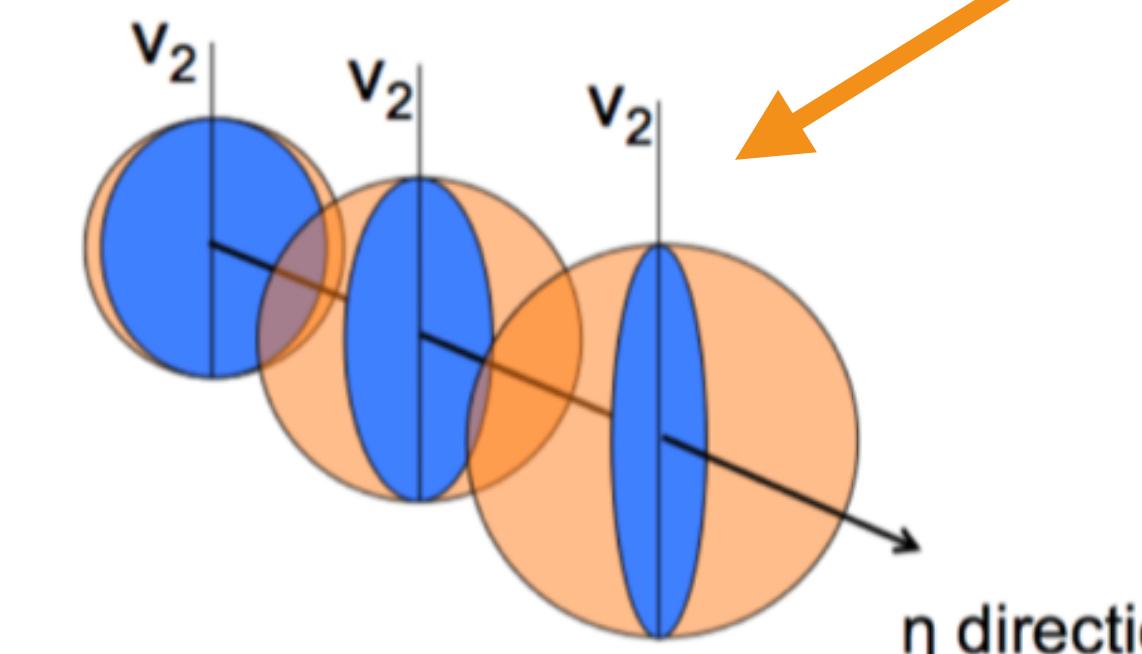
- Hydro evolution of QGP (3+1D)

$$\vec{v}_n = \kappa_n \vec{\epsilon}_n \quad \vec{v}_n(\eta) = v_n(\eta) e^{in\Psi_n(\eta)}$$

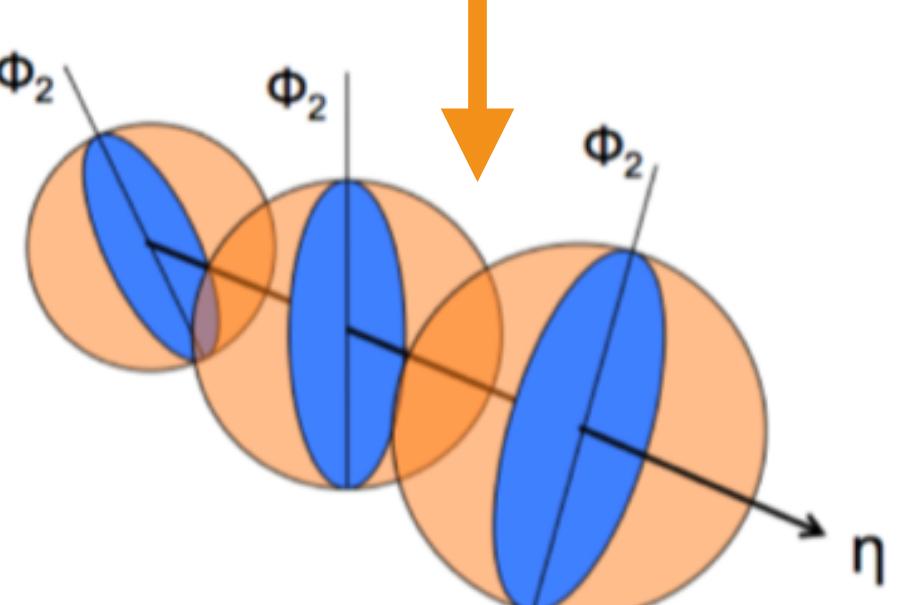


- Final State - average v_n and Ψ_n decorrelation

$$\vec{v}_n(\eta) \approx \vec{v}_n(0)(1 + \alpha_n \eta) e^{i\beta_n \eta}$$



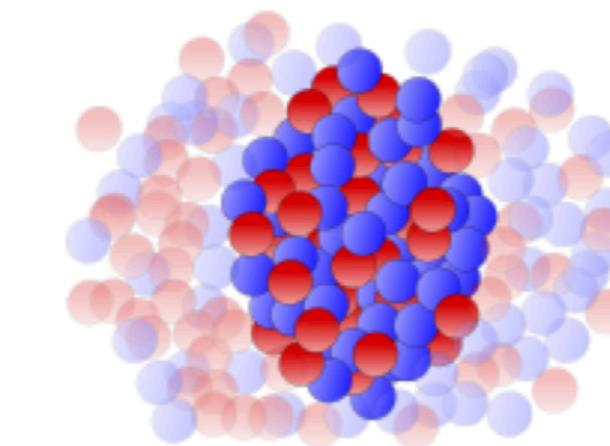
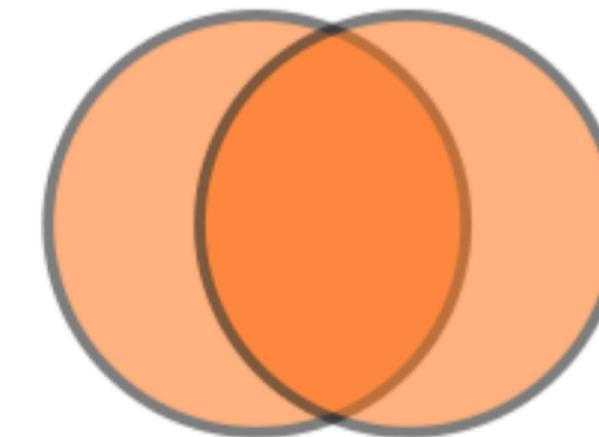
$$v_n(\eta_1) \neq v_n(\eta_2)$$



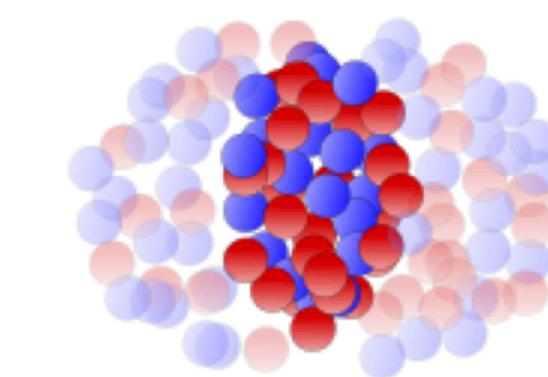
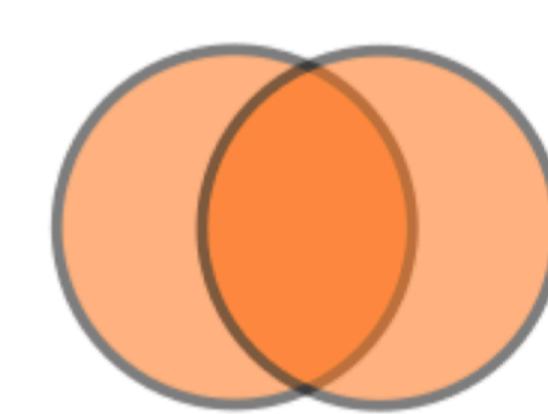
$$\Psi_n(\eta_1) \neq \Psi_n(\eta_2)$$

System-size Dependence

Pb+Pb
A=208, R=6.62 fm



Xe+Xe
A=129, R=5.42 fm



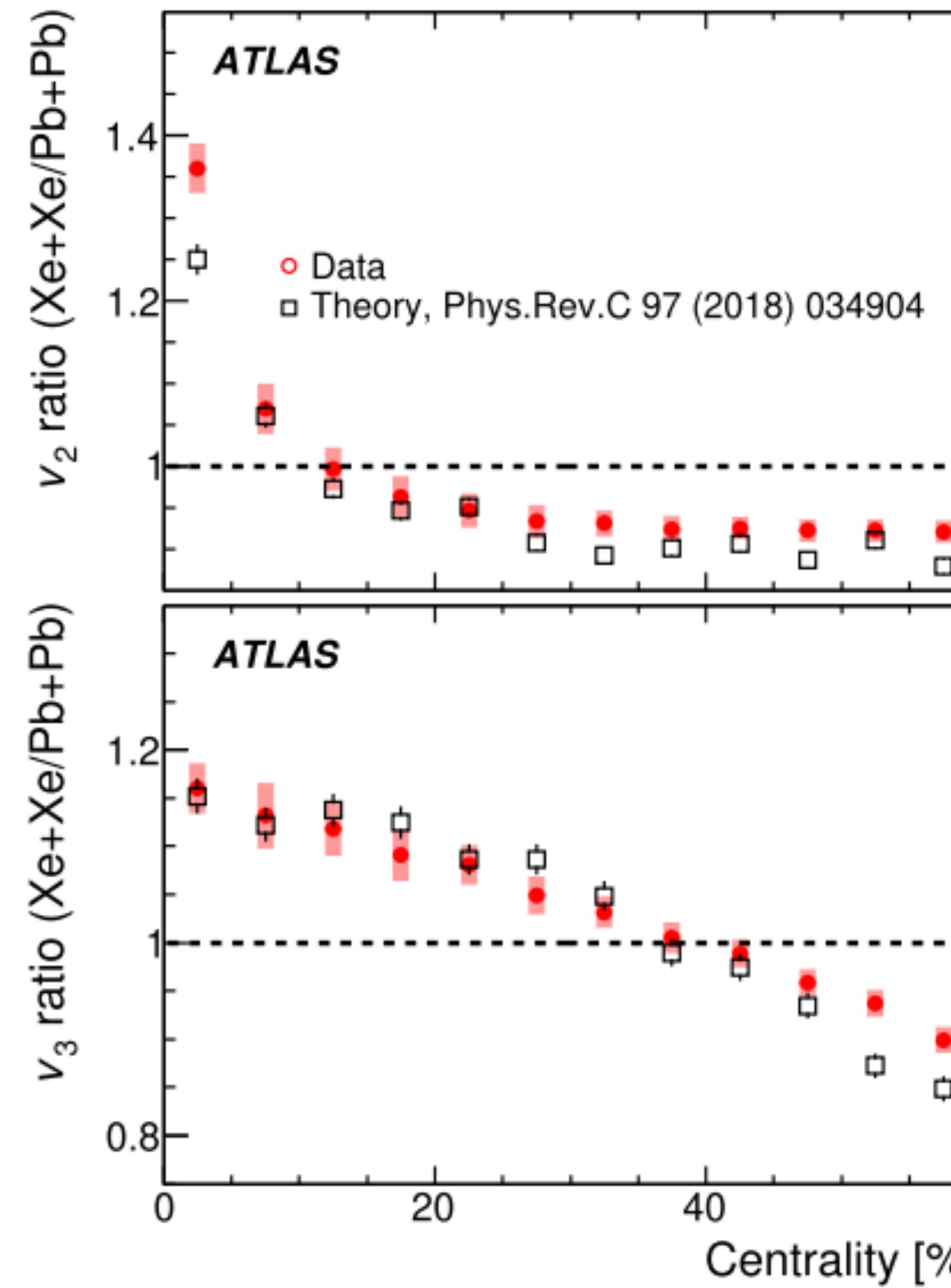
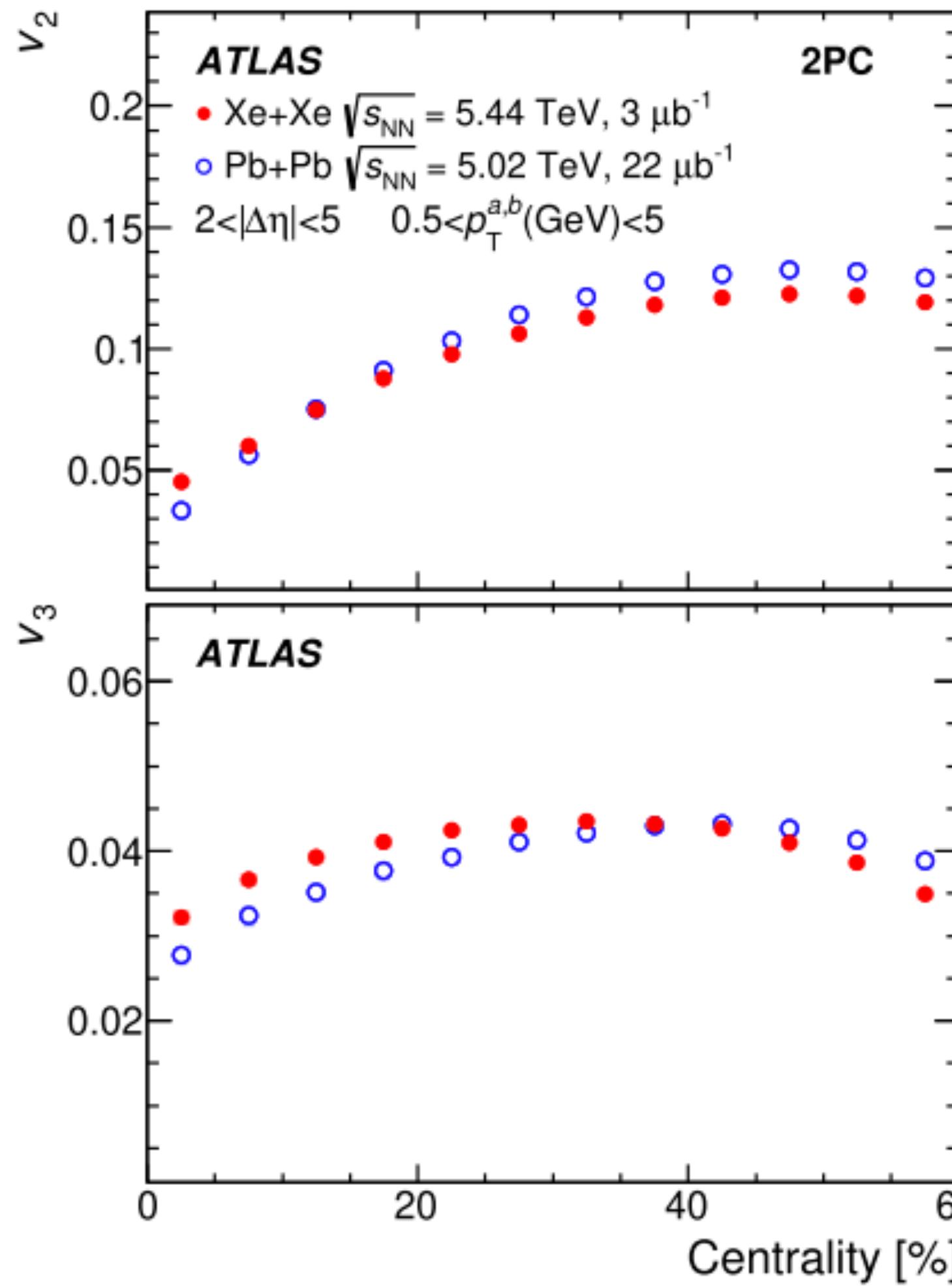
- Different factors can affect the v_n and decorrelation -
 - Initial state geometry
 - Initial momentum anisotropy
 - Shear viscosity
 - Hydrodynamic fluctuations
- How flow and decorrelation are related?
- What is the effect of nuclear deformation (Xe+Xe)?
- Is the dependence same for different harmonics?
- How to disentangle early-time and late-time effects?

♦ System-size dependence of v_n and v_n decorrelation : Xe+Xe vs Pb+Pb

♦ Ratio between the two systems - disentangle initial and final-state contributions

Centrality dependence - Xe+Xe vs Pb+Pb

- Method - 2-particle correlation technique



- Central - Geometry dominates, Non-central - Viscous effect dominates

v₂

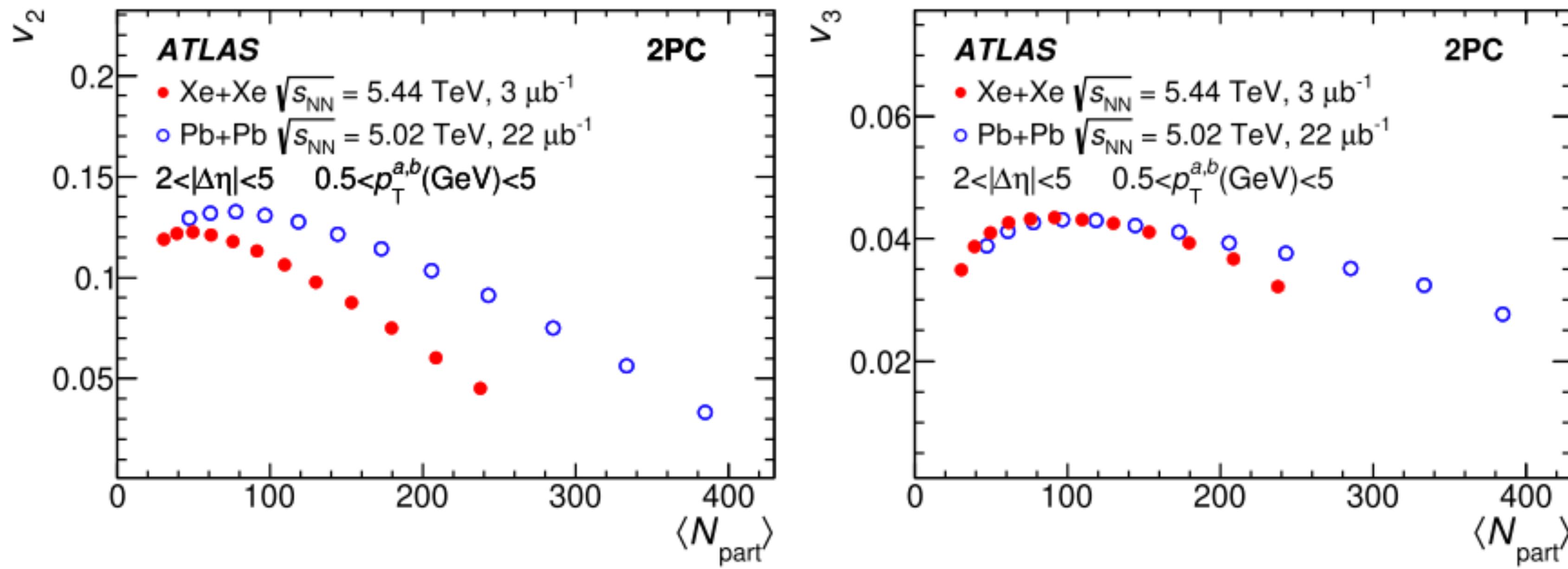
- Most Central events - Xe+Xe
 $v_2 > \text{Pb+Pb } v_2$
- From central to mid-central events, the ratio for v_2 decreases, becomes < 1 after 15% centrality

- Peripheral events - ratio seems to saturate

v₃

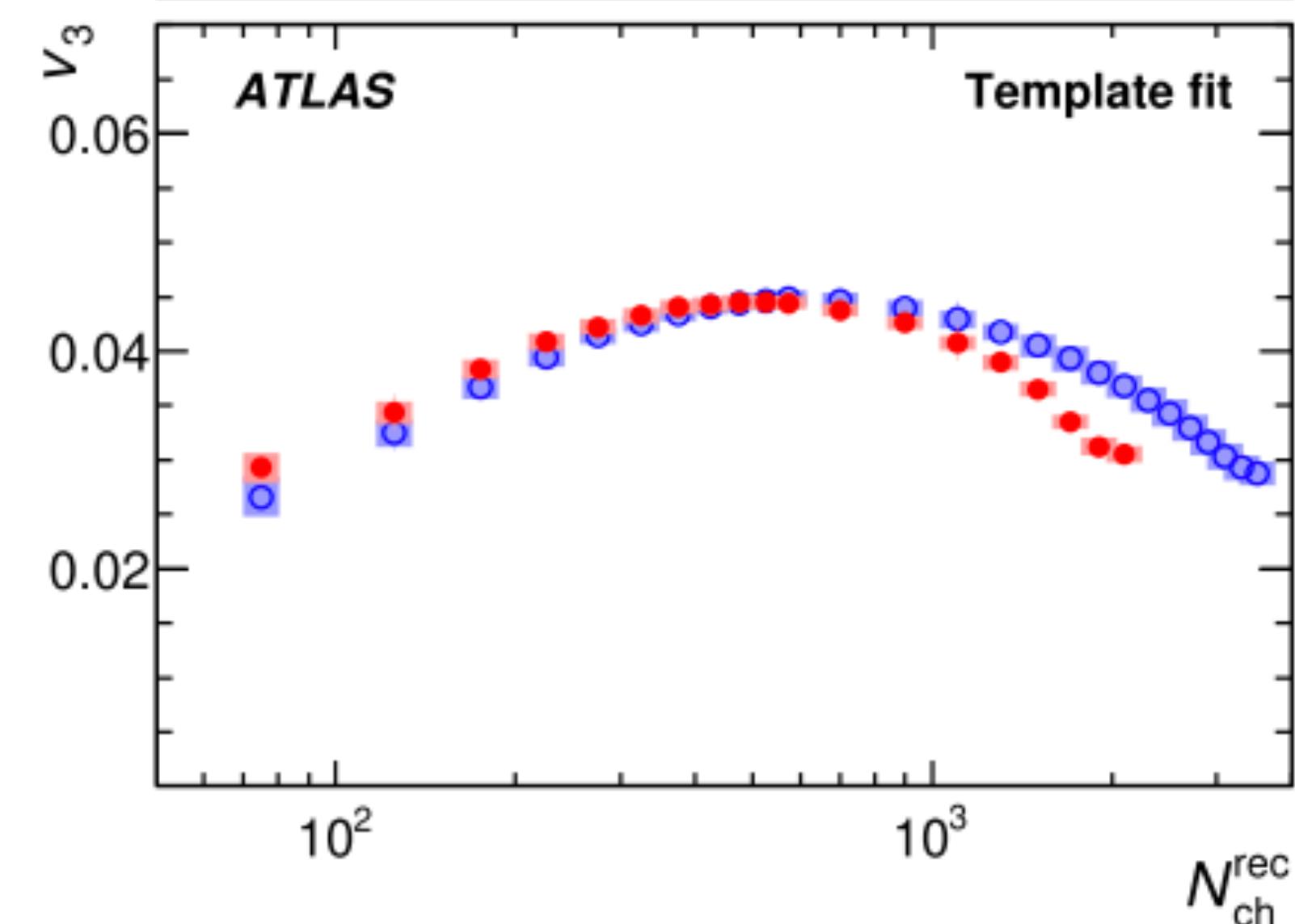
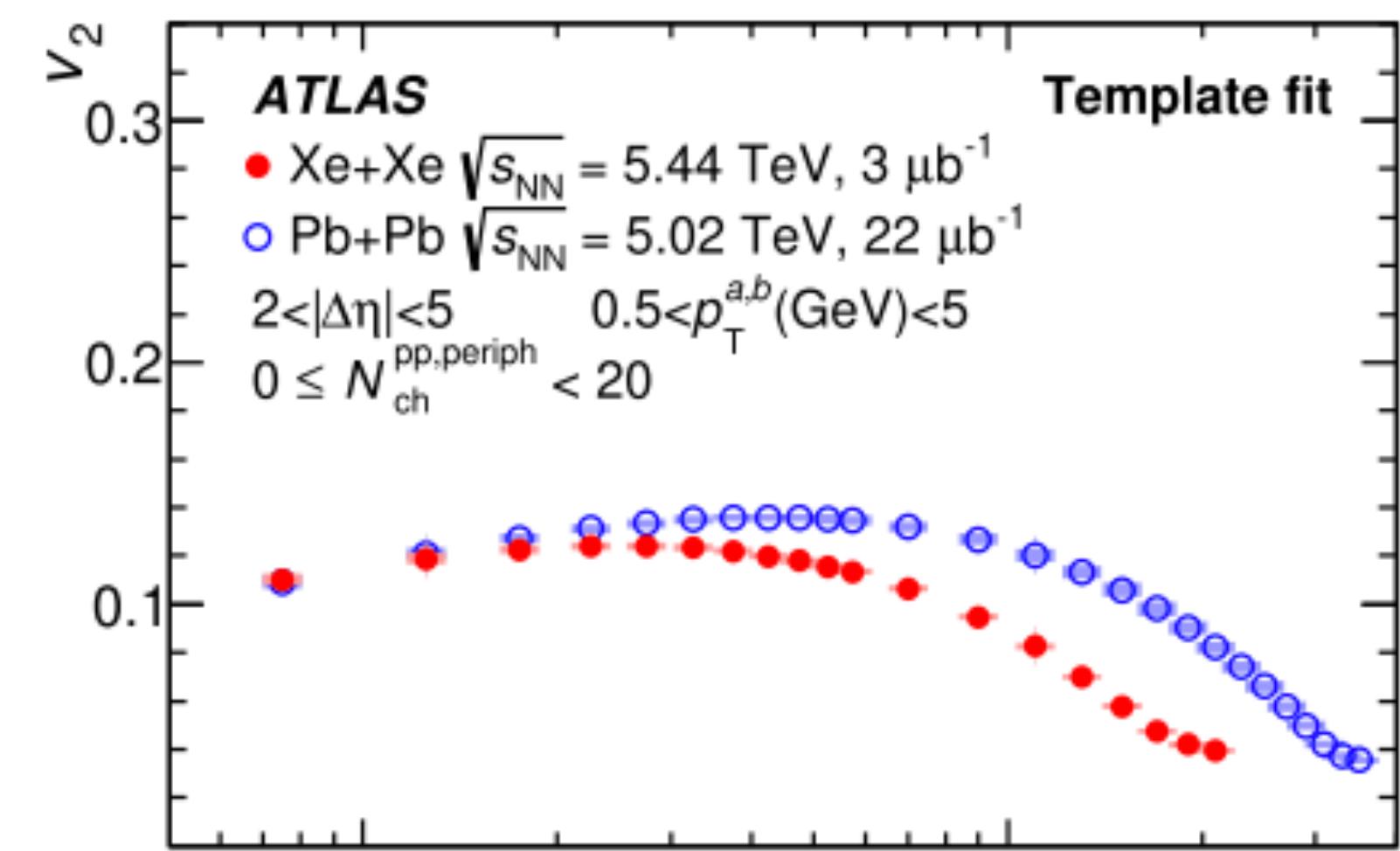
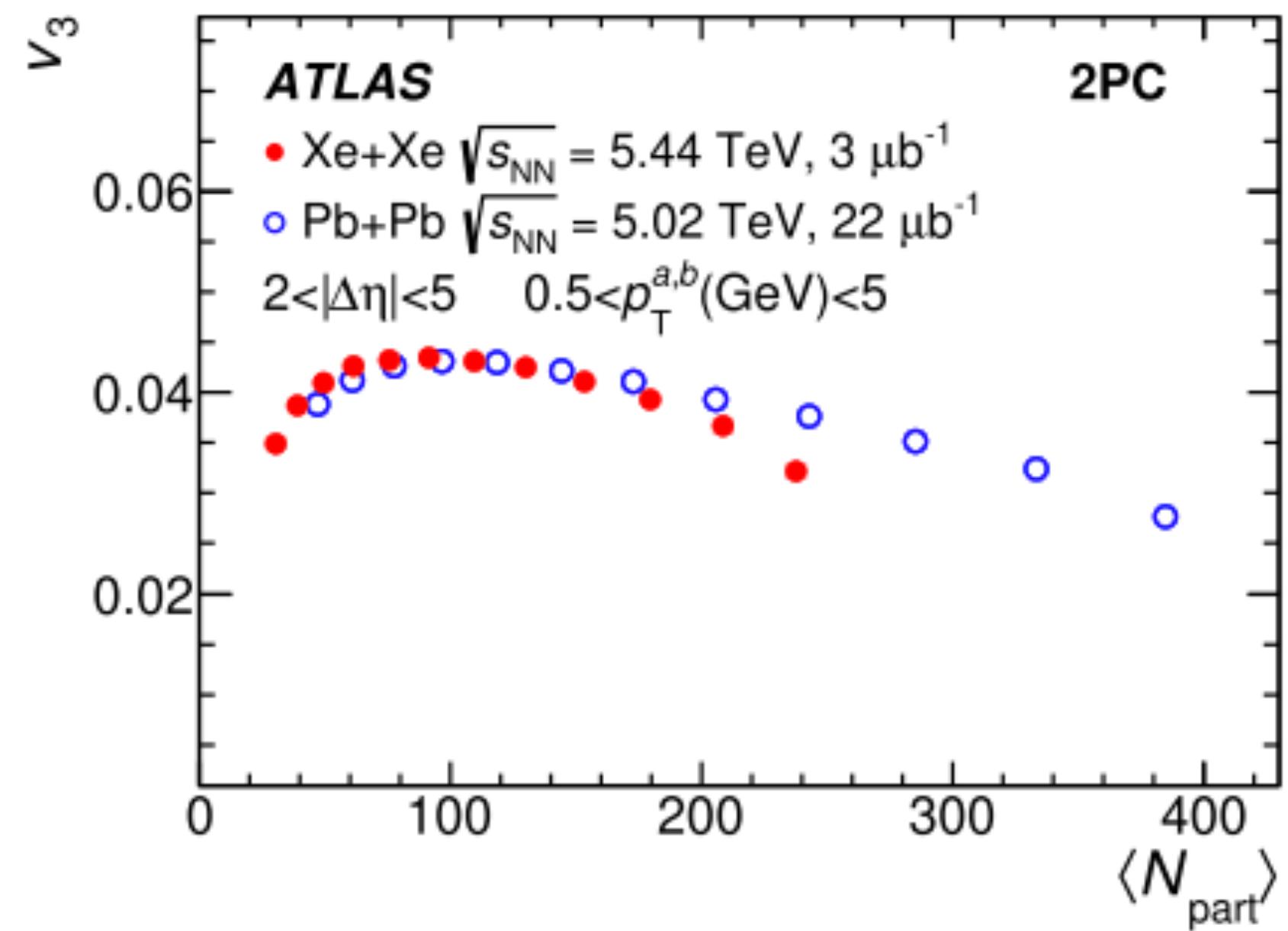
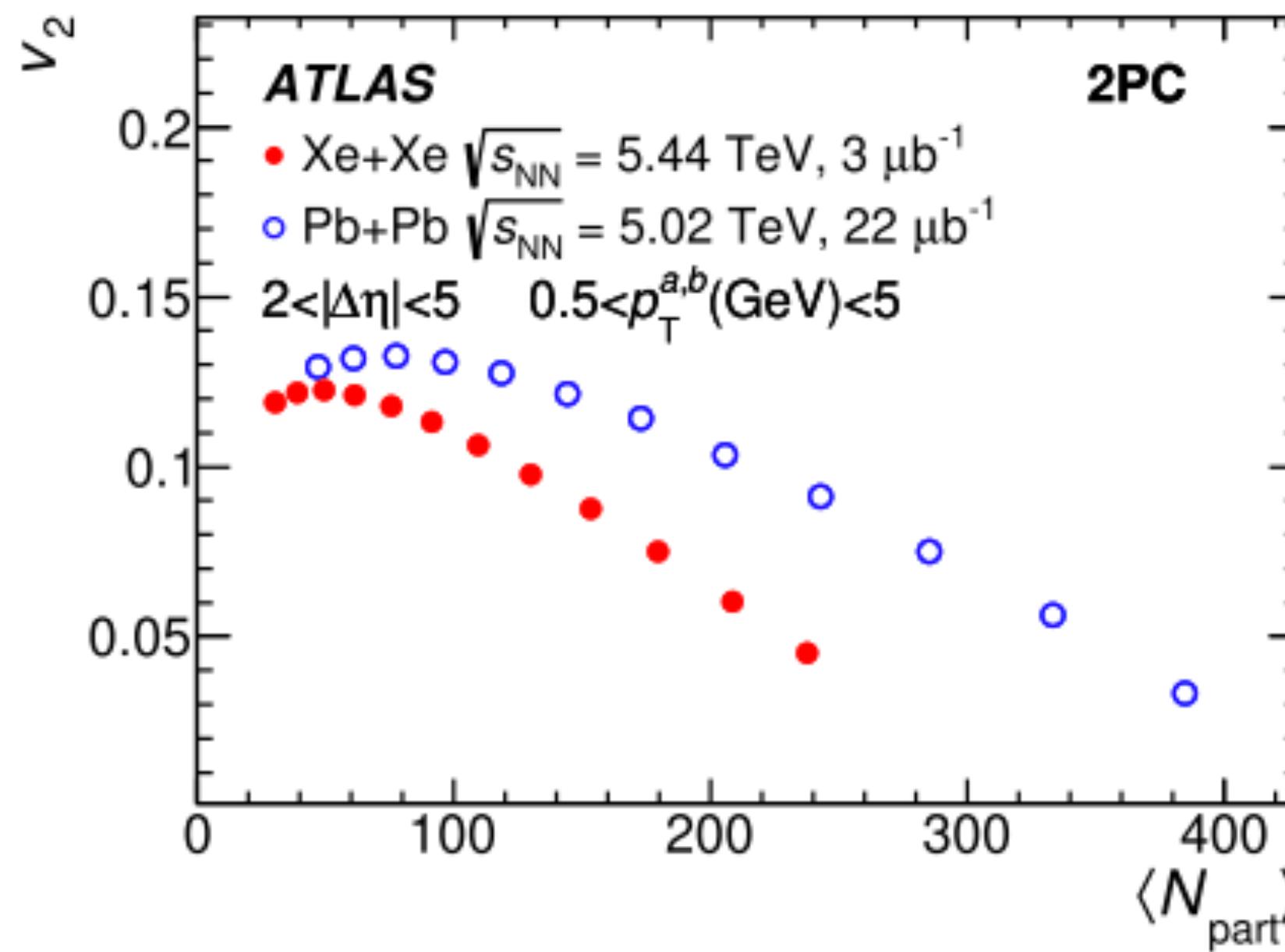
- Similar qualitative trends
- Ratio < 1 after 35% centrality

N_{part} and N_{ch} dependence - Xe+Xe vs Pb+Pb



- v_2 - smaller in Xe+Xe than Pb+Pb
- v_3 - similar values except in large N_{part}
- Low N_{part} - all v_n similar values between Xe+Xe and Pb+Pb

N_{part} and N_{ch} dependence - Xe+Xe vs Pb+Pb

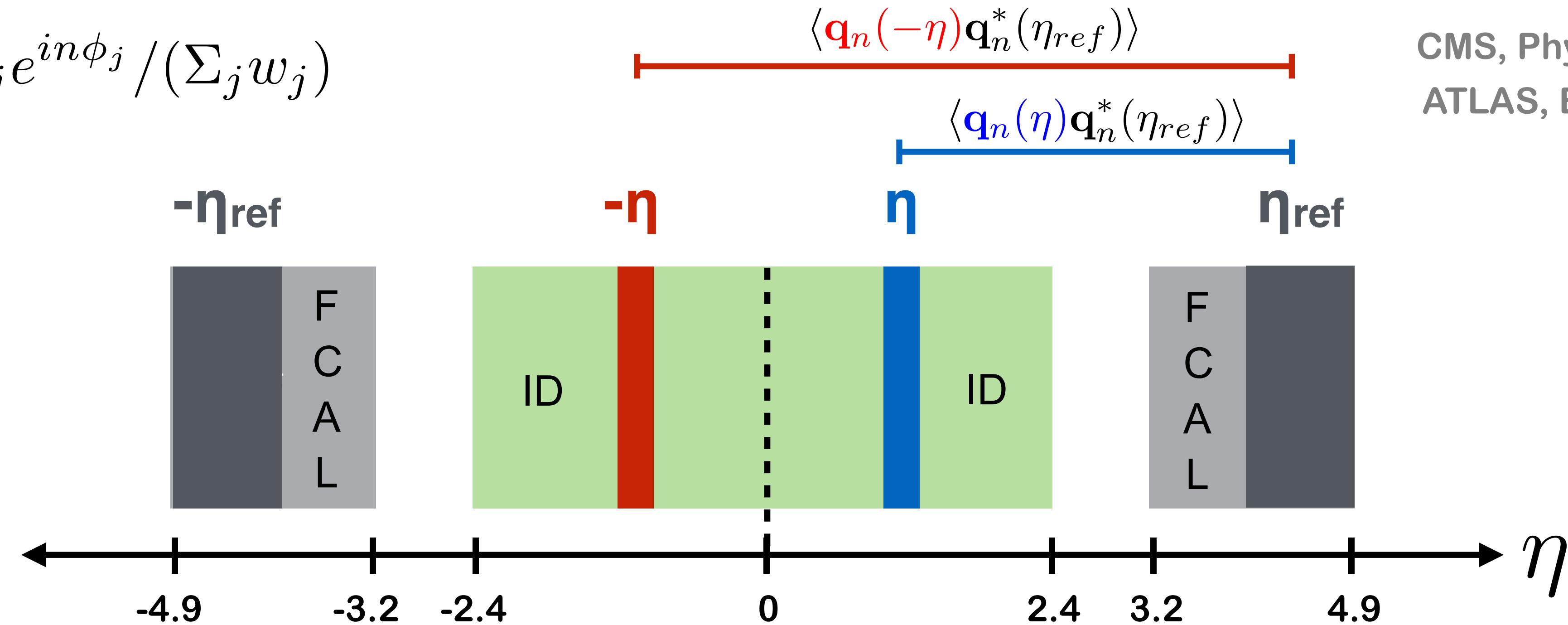


- v_2 - smaller in Xe+Xe than Pb+Pb
- v_3 - similar values except in large N_{part}
- Low N_{part} - all v_n similar values between Xe+Xe and Pb+Pb
- N_{ch} dependence - follow similar behavior as N_{part}

Decorrelation Method

- Flow vector

$$\mathbf{q}_n \equiv \sum_j w_j e^{in\phi_j} / (\sum_j w_j)$$



$$r_{n|n}(\eta) = \frac{\langle \mathbf{q}_n(-\eta) \mathbf{q}_n^*(\eta_{ref}) \rangle}{\langle \mathbf{q}_n(\eta) \mathbf{q}_n^*(\eta_{ref}) \rangle} = \frac{\langle v_n(-\eta) v_n(\eta_{ref}) \cos n(\Psi_n(-\eta) - \Psi_n(\eta_{ref})) \rangle}{\langle v_n(\eta) v_n(\eta_{ref}) \cos n(\Psi_n(\eta) - \Psi_n(\eta_{ref})) \rangle}$$

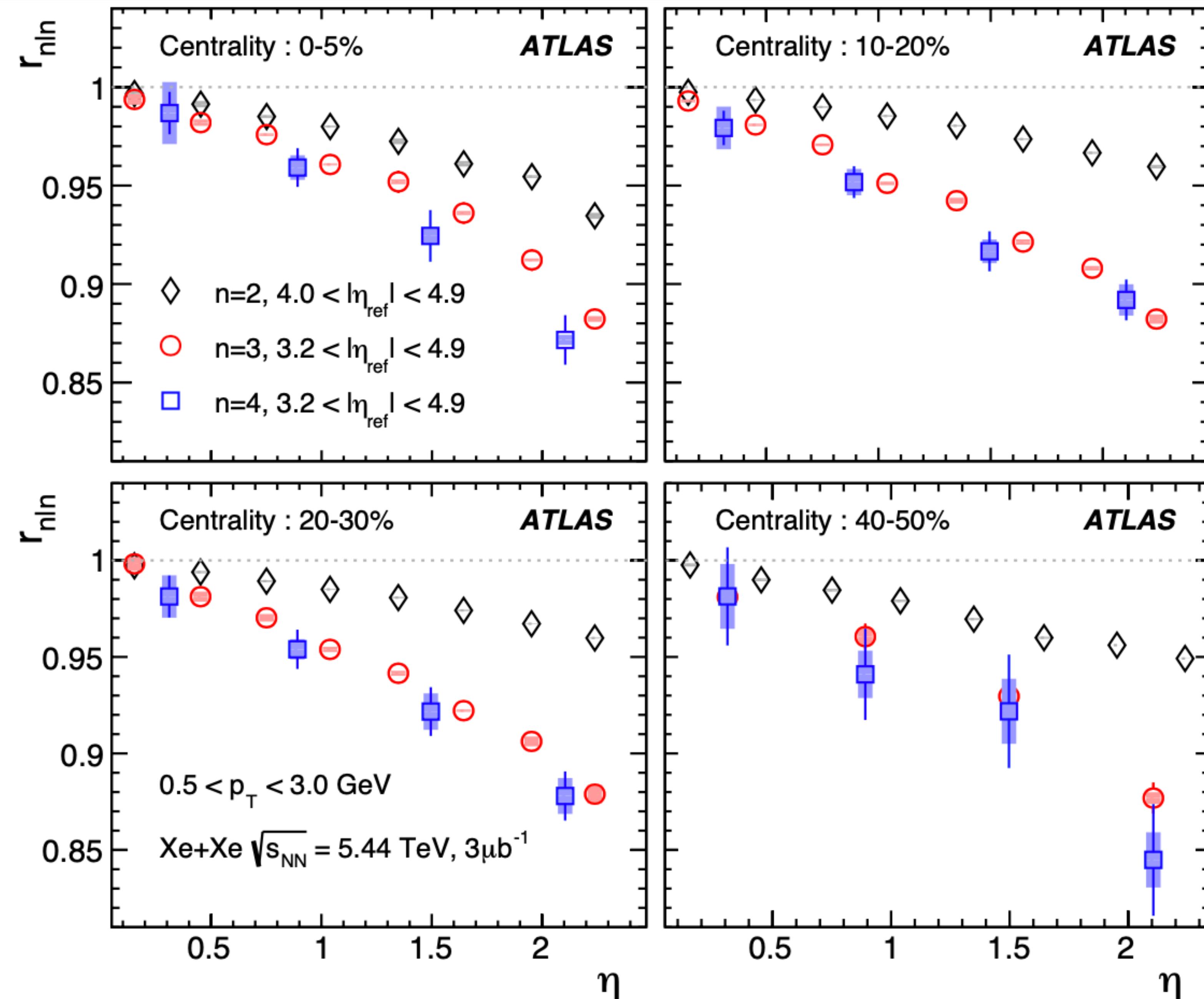
$$r_{n|n}(\eta) \leq 1$$

Measures decorrelation between $-\eta$ and η

Decorrelation in Xe+Xe

7

- $r_{2|2} > r_{3|3} > r_{4|4}$ - Linear decrease with η
- $r_{2|2}$ strong centrality dependence - larger in mid-central
- $r_{3|3}$ and $r_{4|4}$ - weak centrality dependence
- Similar behavior as 5 TeV Pb+Pb



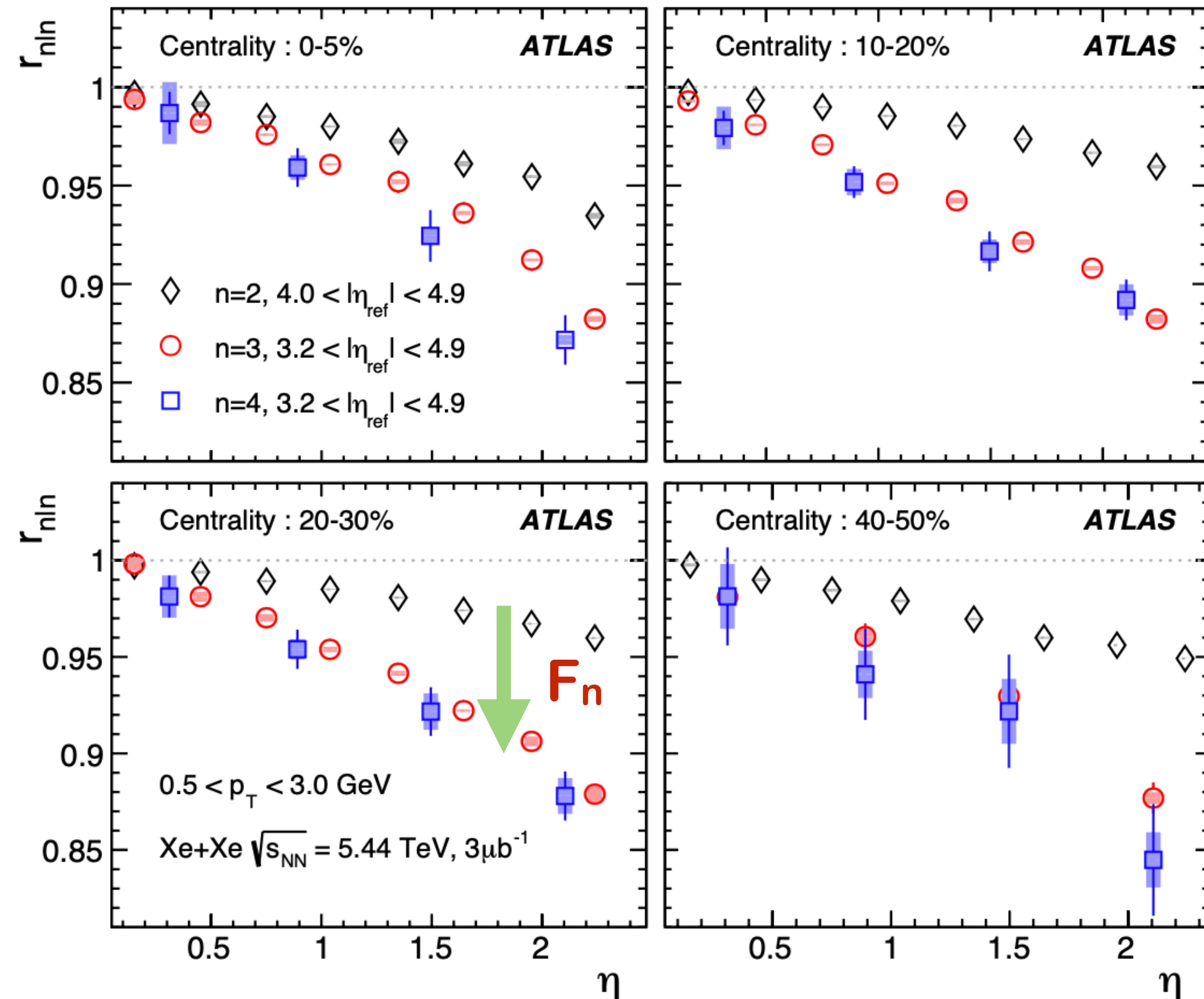
Decorrelation in Xe+Xe

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$$r_{n|n}(\eta) = 1 - 2F_n \eta$$

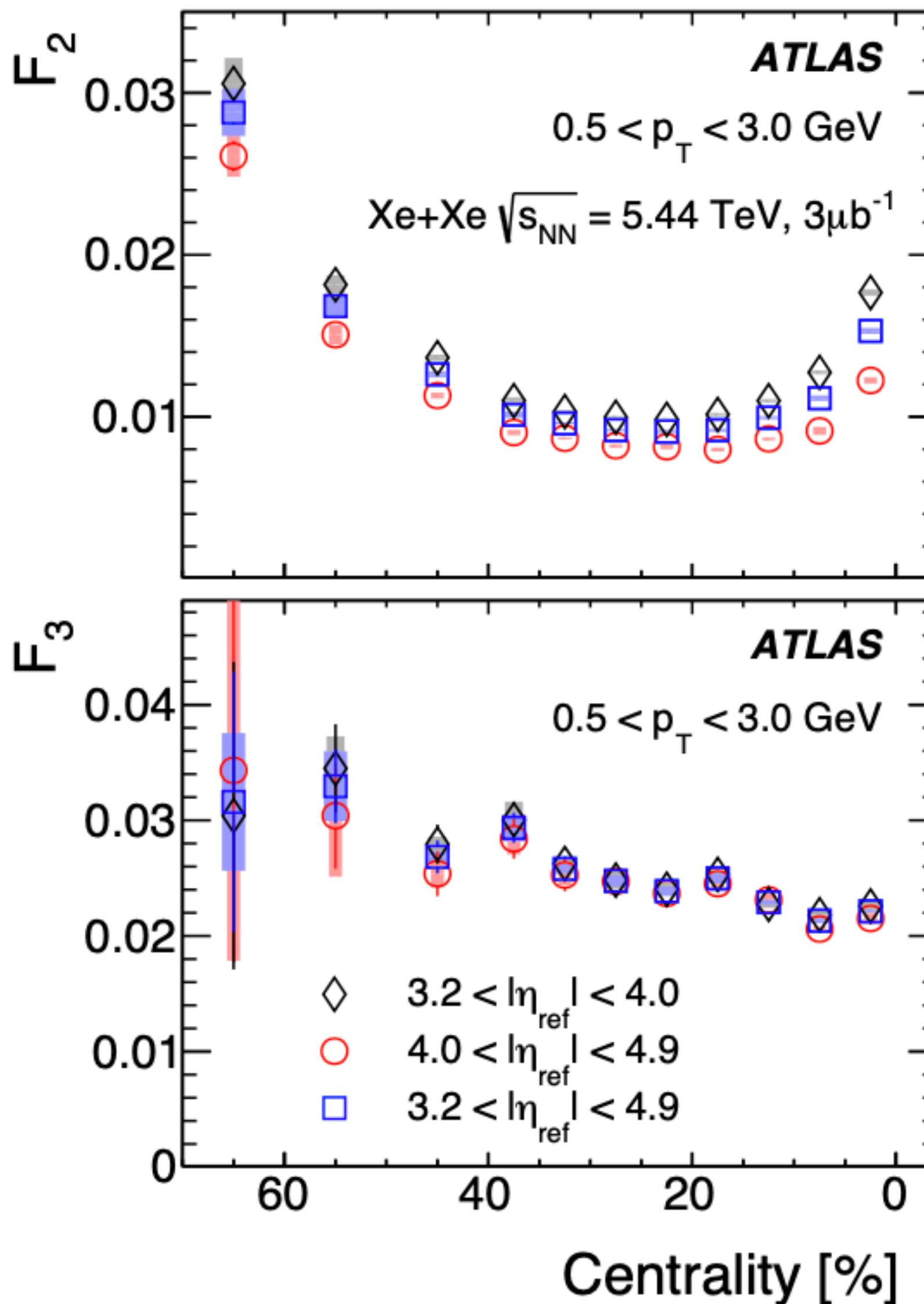
↓
Decorrelation strength



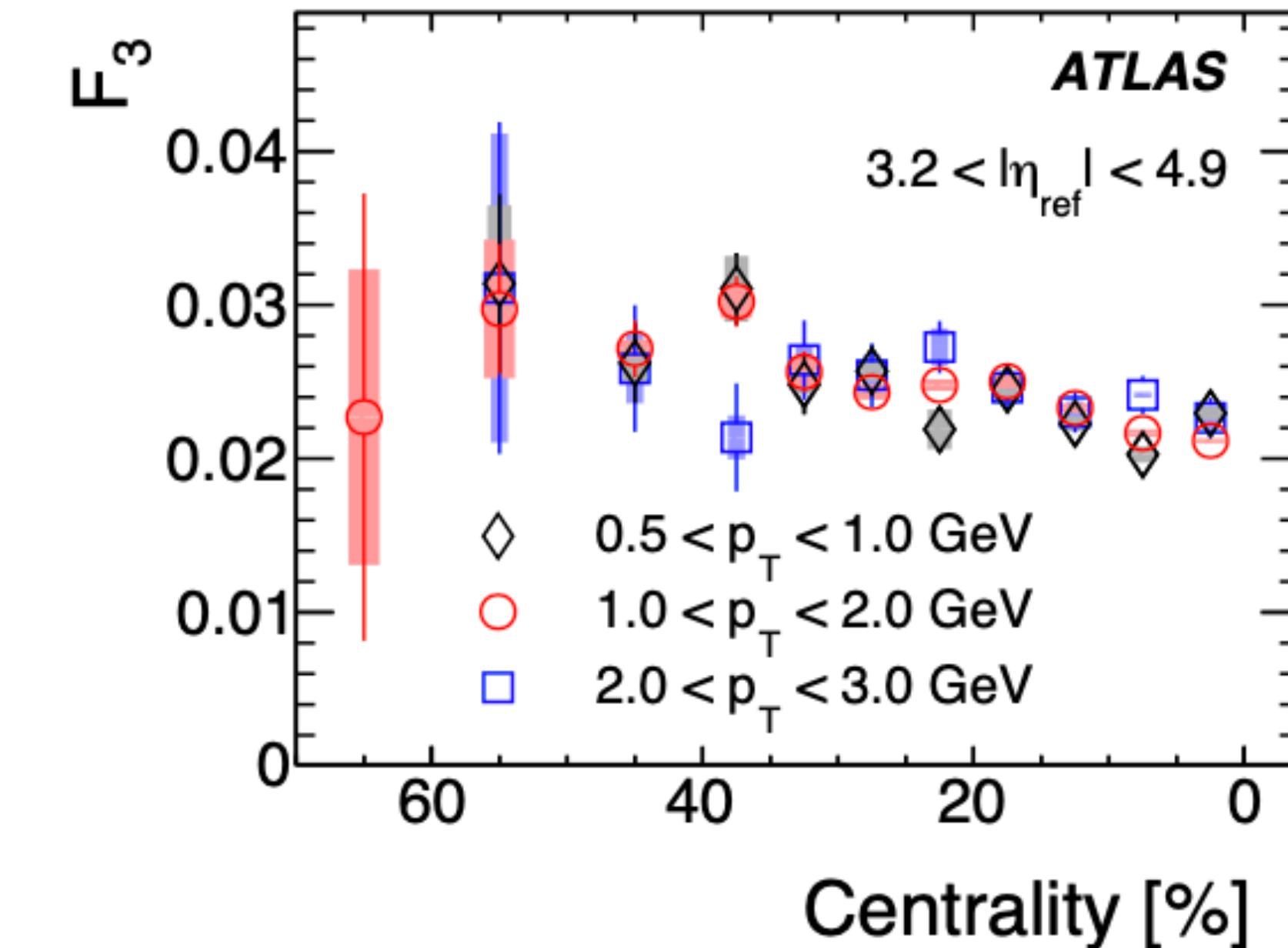
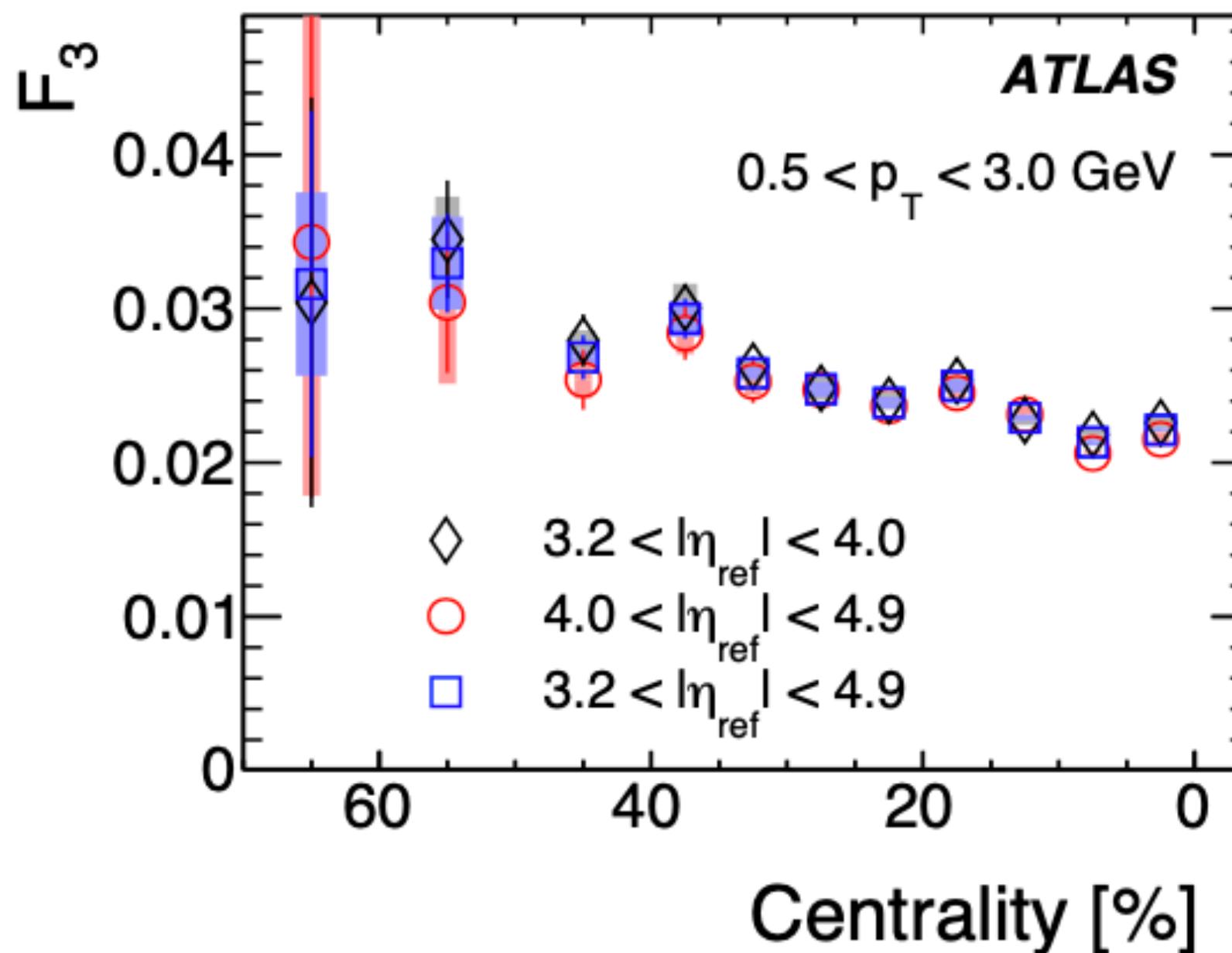
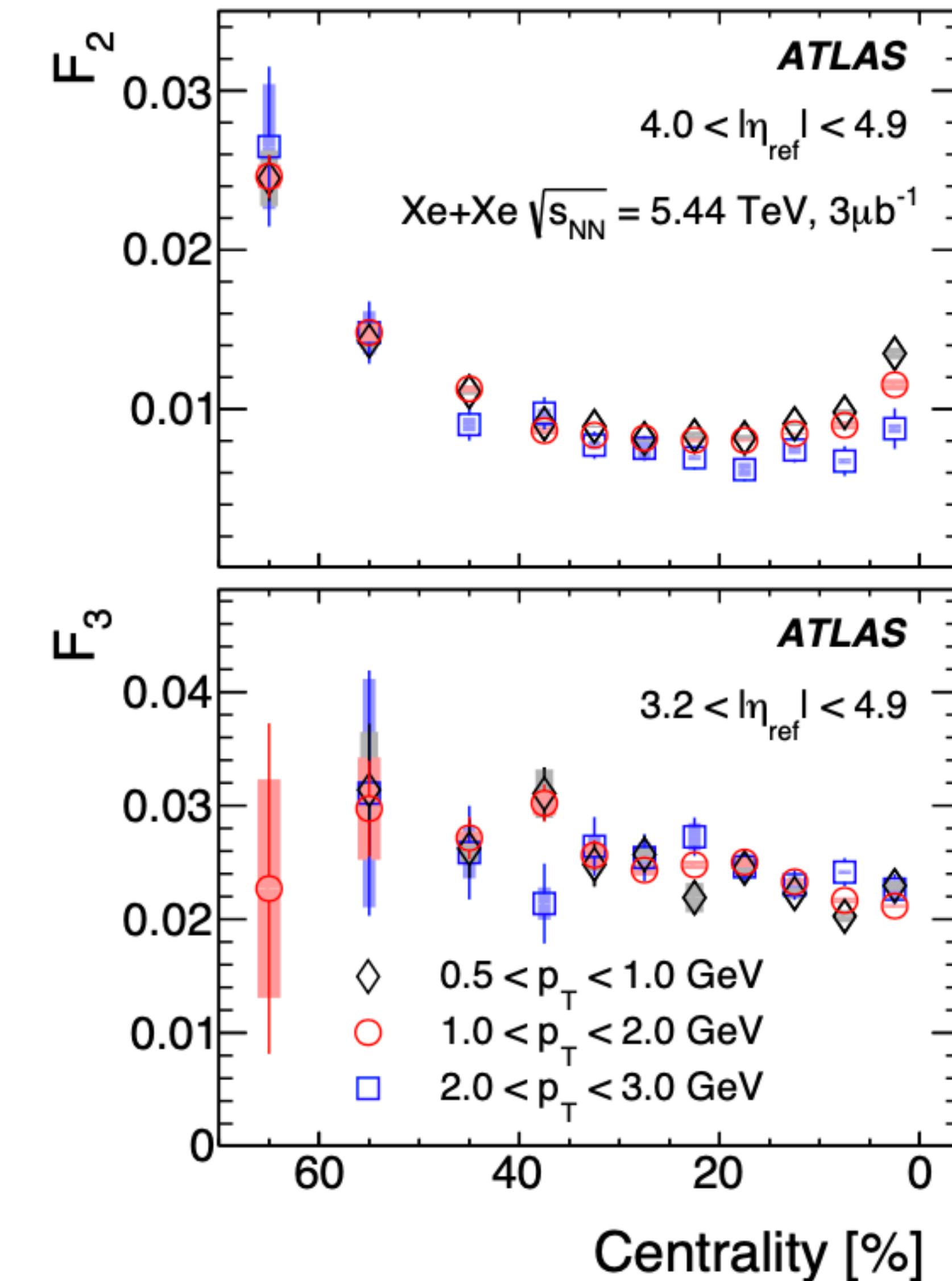
Slope $F_n - |\eta_{\text{ref}}|$ and p_T dependence

- Non-flow (dijets) at small $|\eta_{\text{ref}}|$ or large p_T

$$r_{n|n}(\eta) = \frac{\langle \mathbf{q}_n(-\eta) \mathbf{q}_n^*(\eta_{\text{ref}}) \rangle}{\langle \mathbf{q}_n(\eta) \mathbf{q}_n^*(\eta_{\text{ref}}) \rangle} \xrightarrow{\uparrow \text{NF}} F_n \uparrow$$



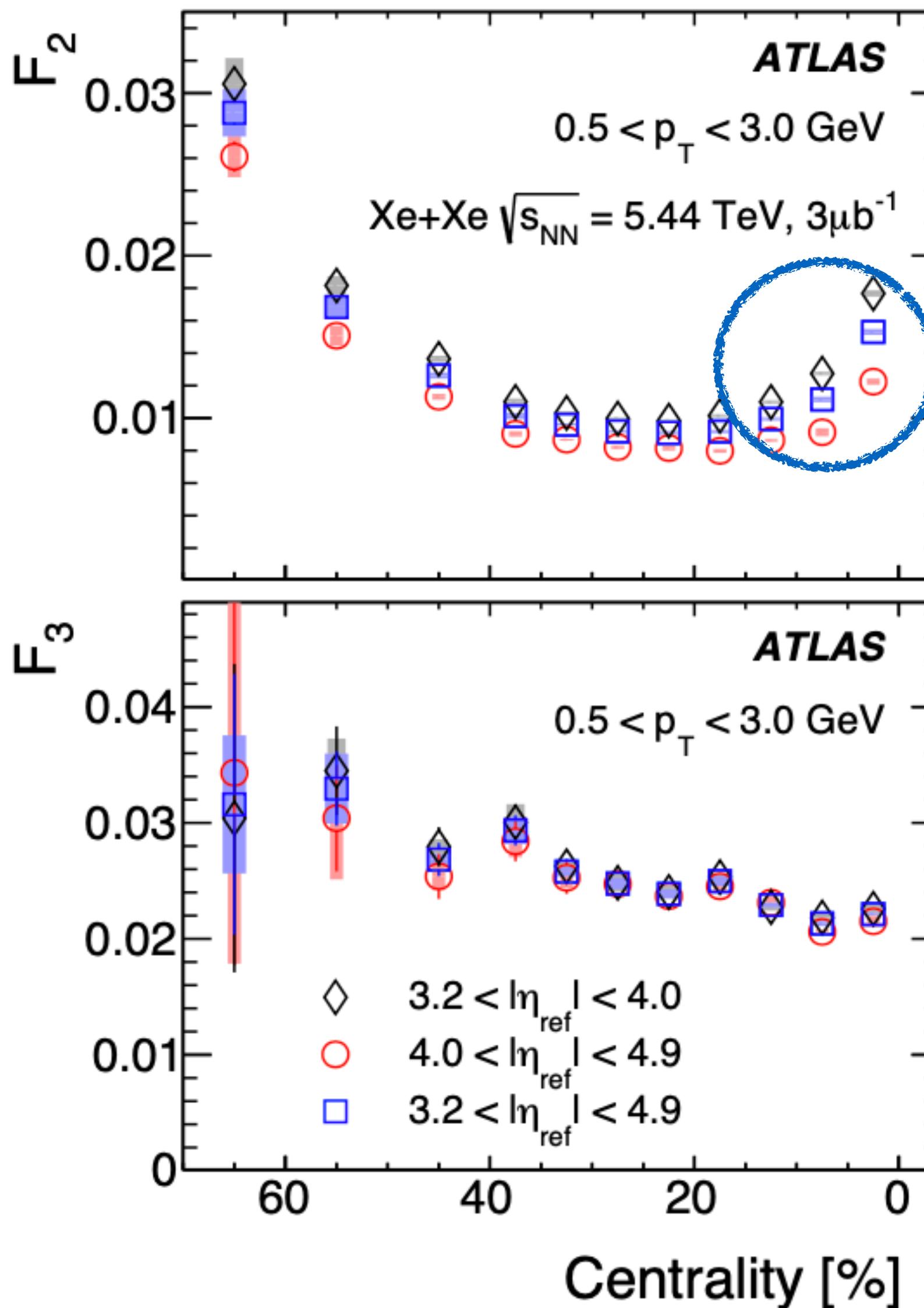
- Larger F_2 at smaller $|\eta_{\text{ref}}|$ - NF



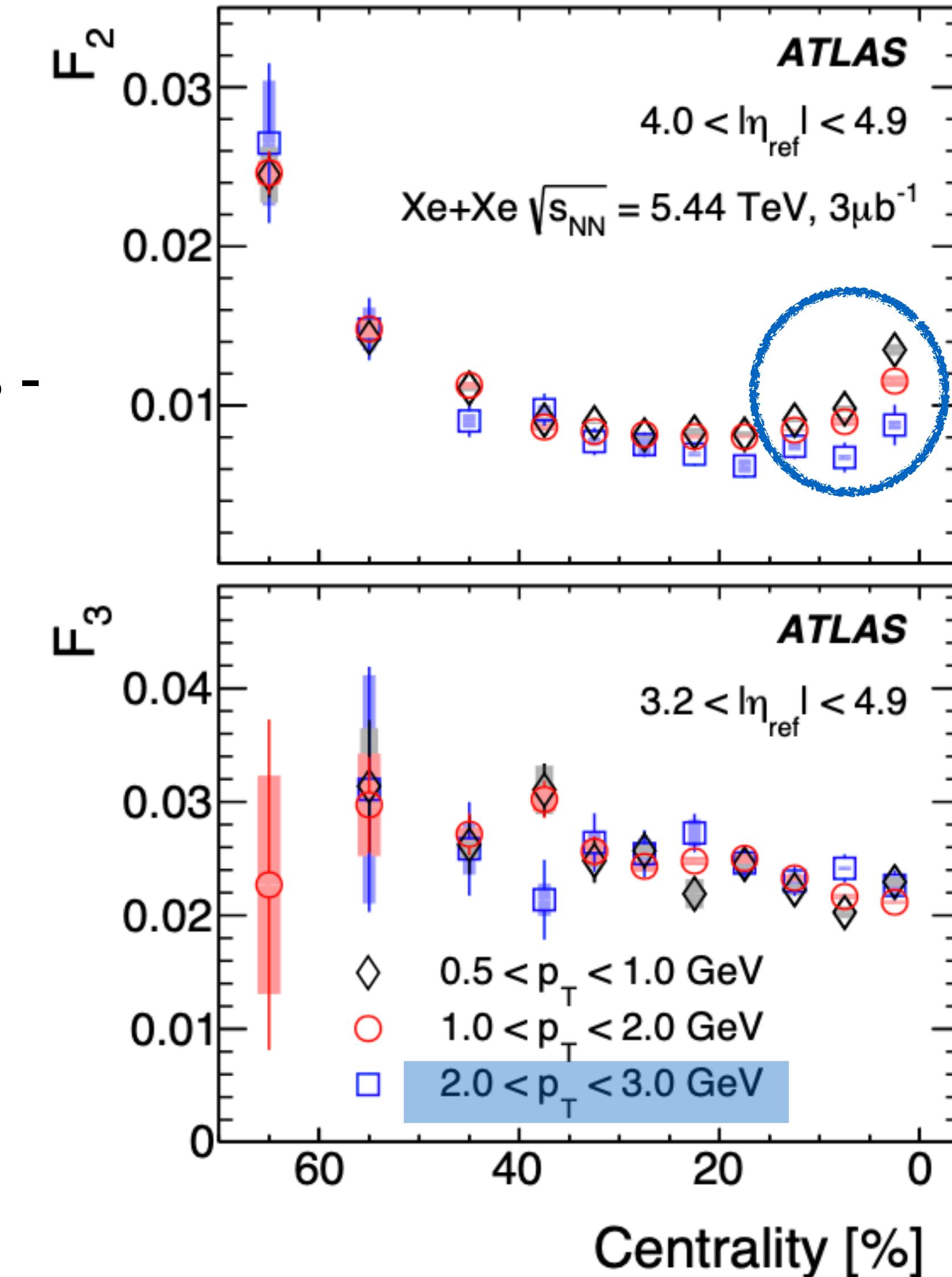
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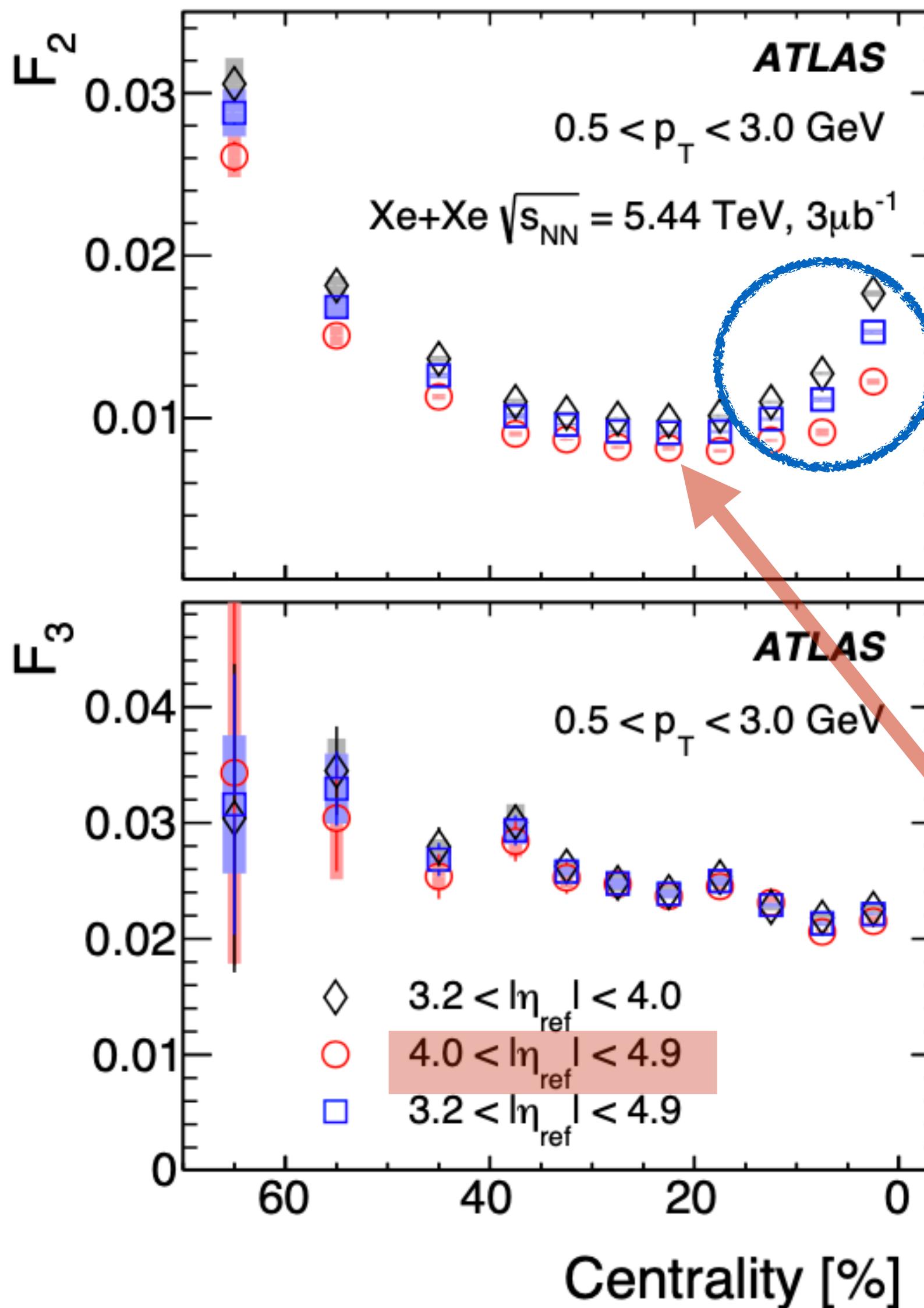
- Larger F_2 at smaller $|\eta_{\text{ref}}|$ - NF
- Smaller F_2 at larger p_T - not NF
- Effect larger in central collisions - could be due to non-linear v_2 decorrelation
- F_3 - not affected by NF



Slope $F_n - |\eta_{\text{ref}}|$ and p_T dependence

- Non-flow (dijets) at small $|\eta_{\text{ref}}|$ or large p_T

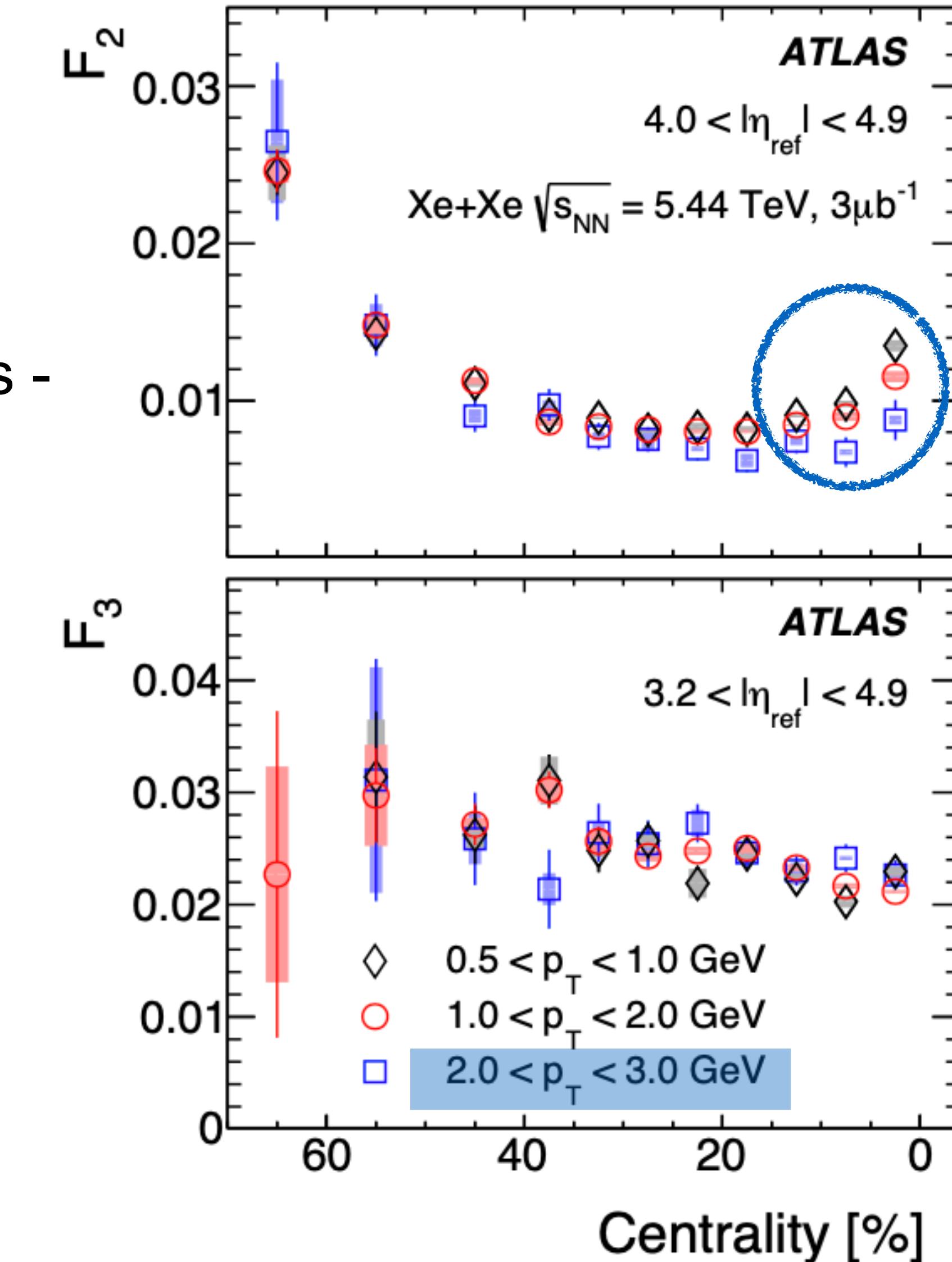
$$r_{n|n}(\eta) = \frac{\langle \mathbf{q}_n(-\eta) \mathbf{q}_n^*(\eta_{\text{ref}}) \rangle}{\langle \mathbf{q}_n(\eta) \mathbf{q}_n^*(\eta_{\text{ref}}) \rangle} \xrightarrow{\uparrow \text{NF}} F_n \uparrow$$



- Larger F_2 at smaller $|\eta_{\text{ref}}|$ - NF
- Smaller F_2 at larger p_T - not NF
- Effect larger in central collisions - could be due to non-linear v_2 decorrelation

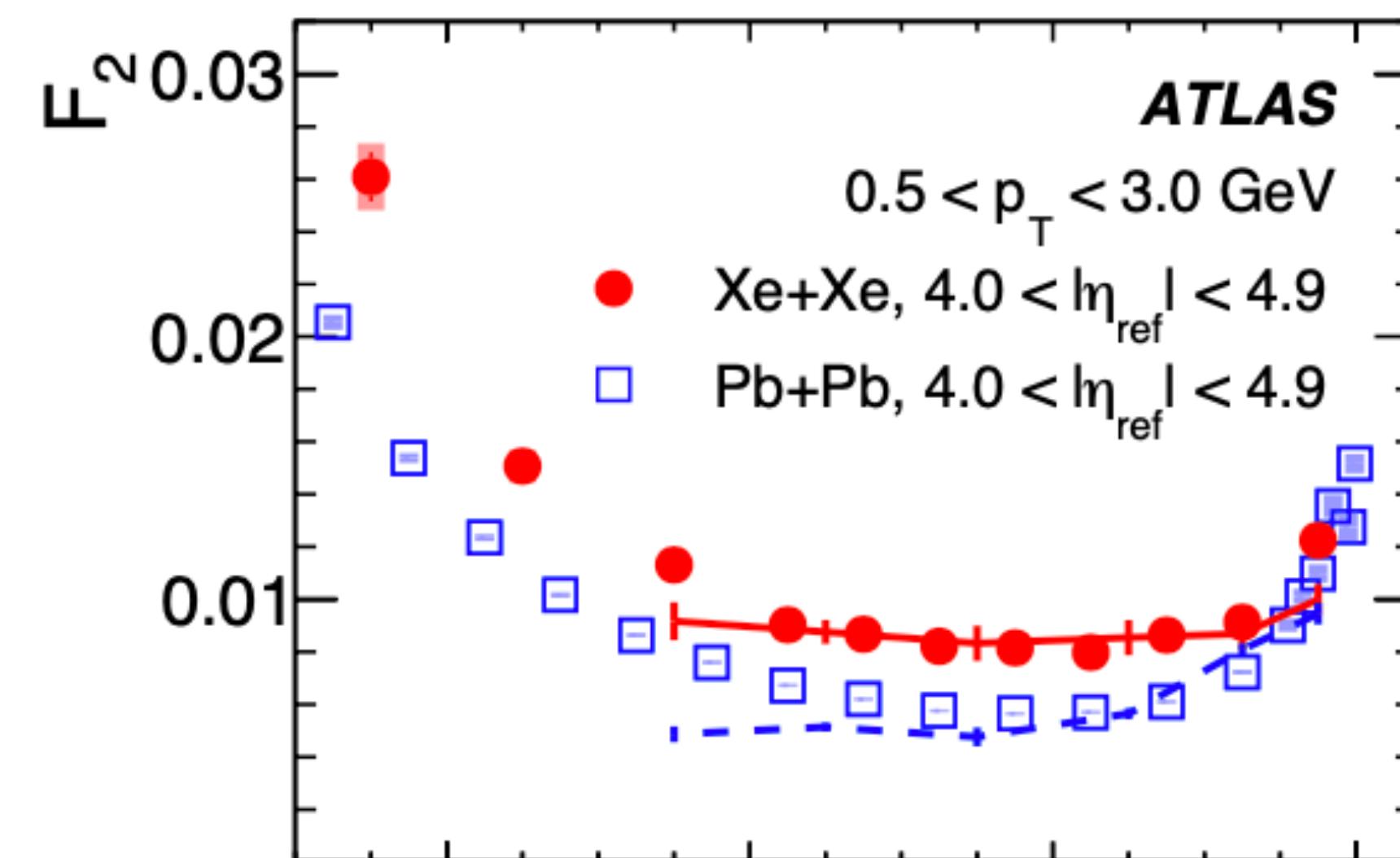
- F_3 - not affected by NF
- Suppress these variations

$F_2 \rightarrow 4.0 < |\eta_{\text{ref}}| < 4.9$
 $F_3 \rightarrow 3.2 < |\eta_{\text{ref}}| < 4.9$



Comparison with Pb+Pb and Hydro

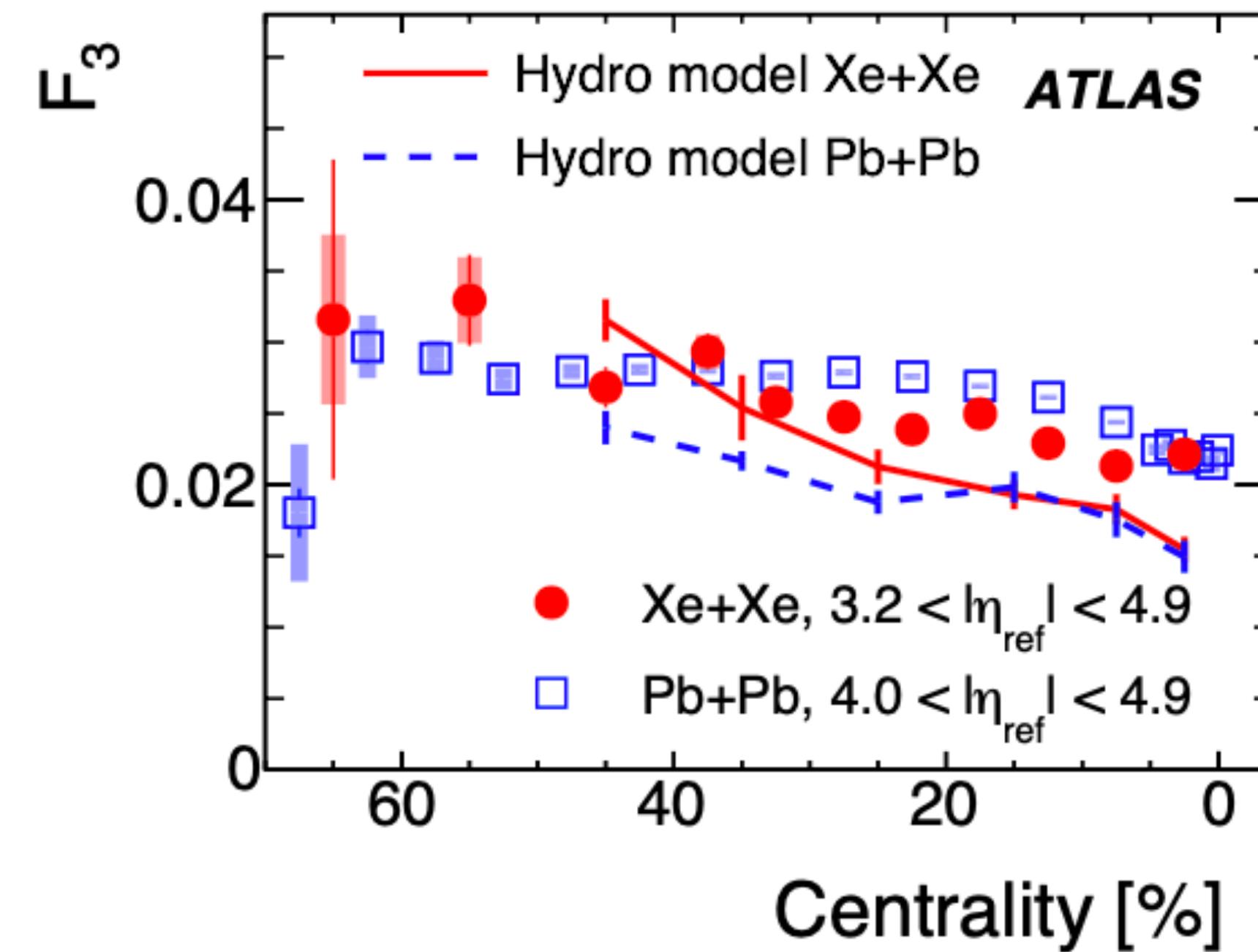
Centrality (avg. geometry)



- Reverse ordering for n=2 and 3

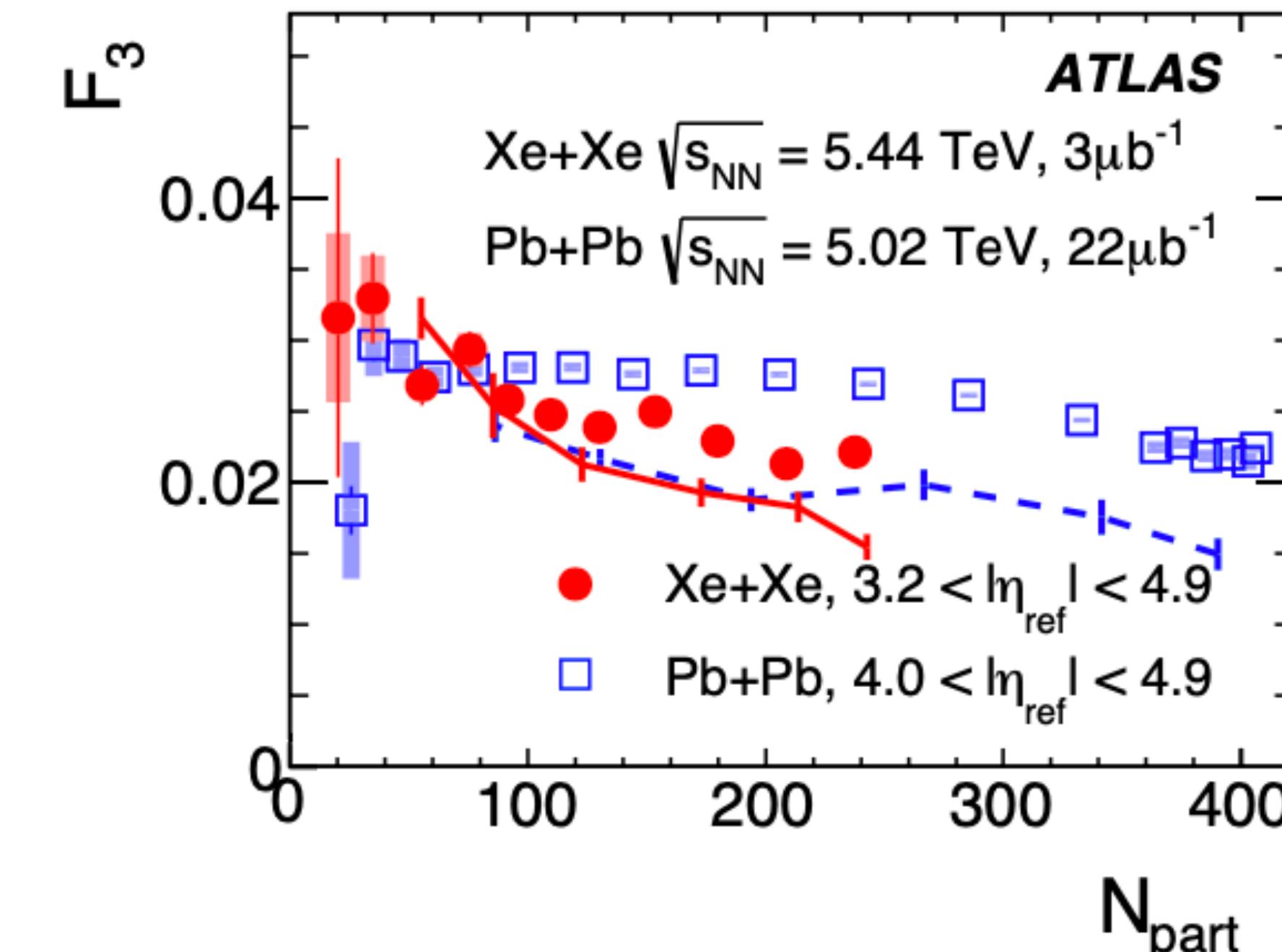
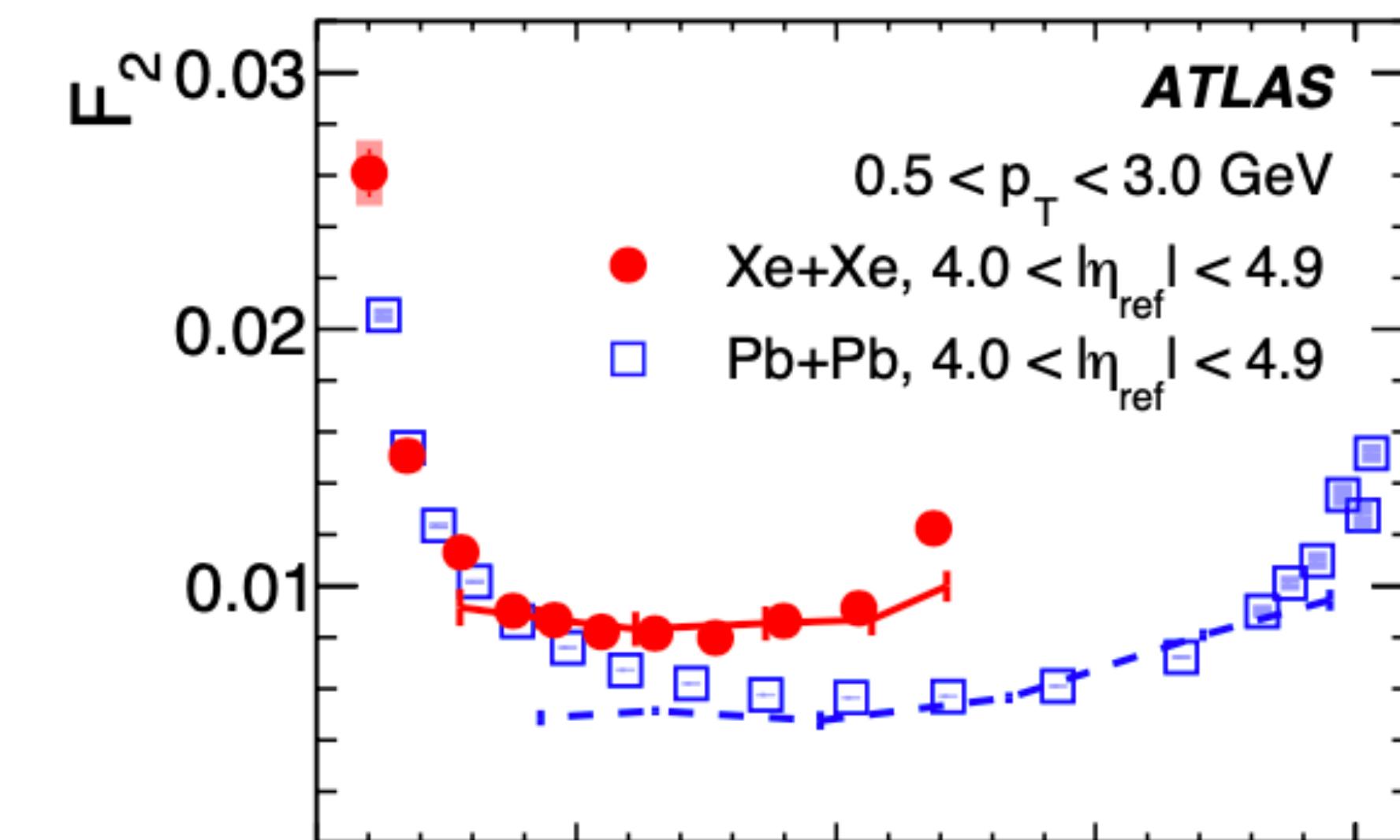
$$F_2^{XeXe} > F_2^{PbPb}$$

$$F_3^{XeXe} < F_3^{PbPb}$$



- F_2 and F_3 match - in 0-5% centrality or $N_{\text{part}} < 80$

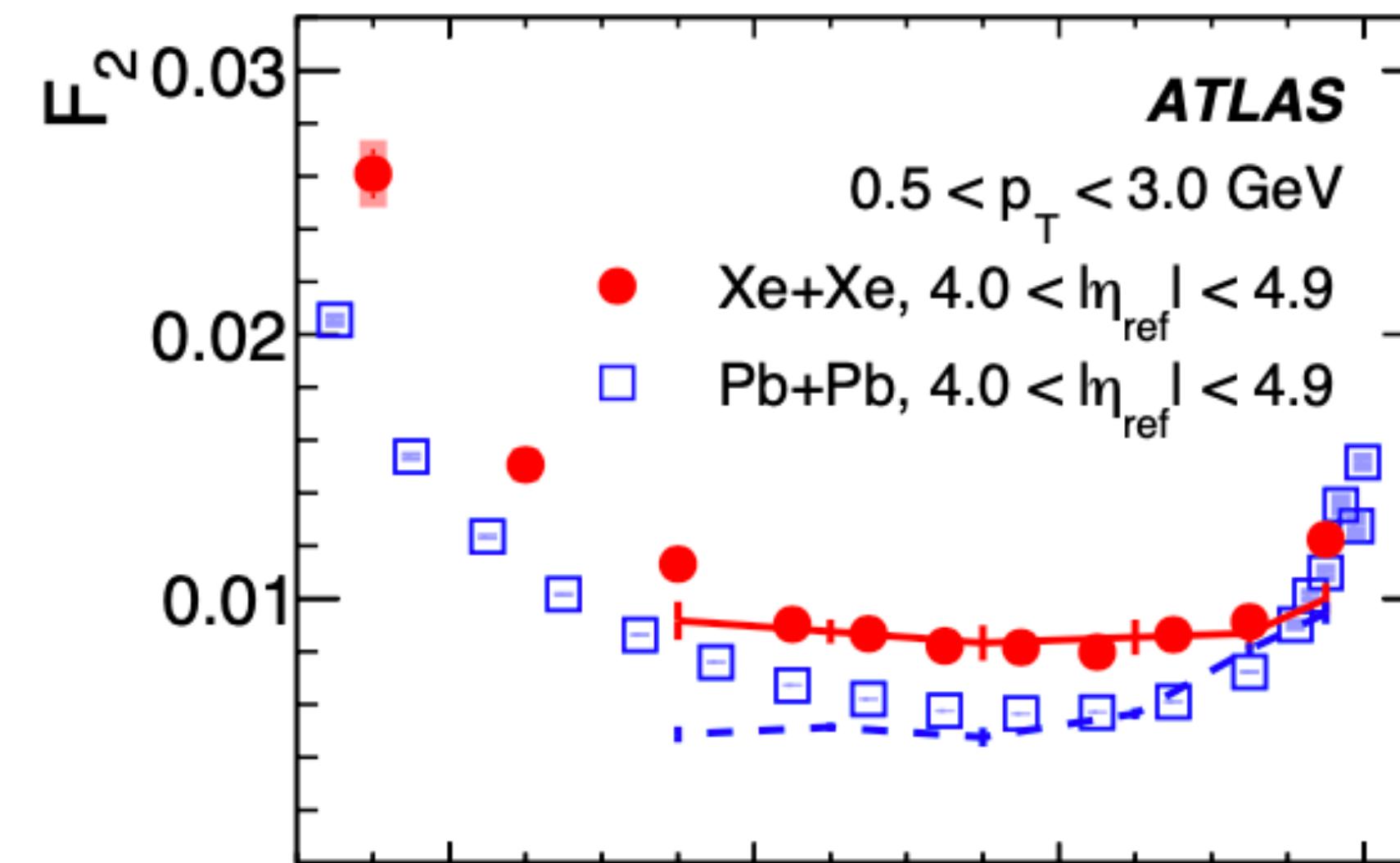
N_{part} (system-size)



Comparison with Pb+Pb and Hydro

9

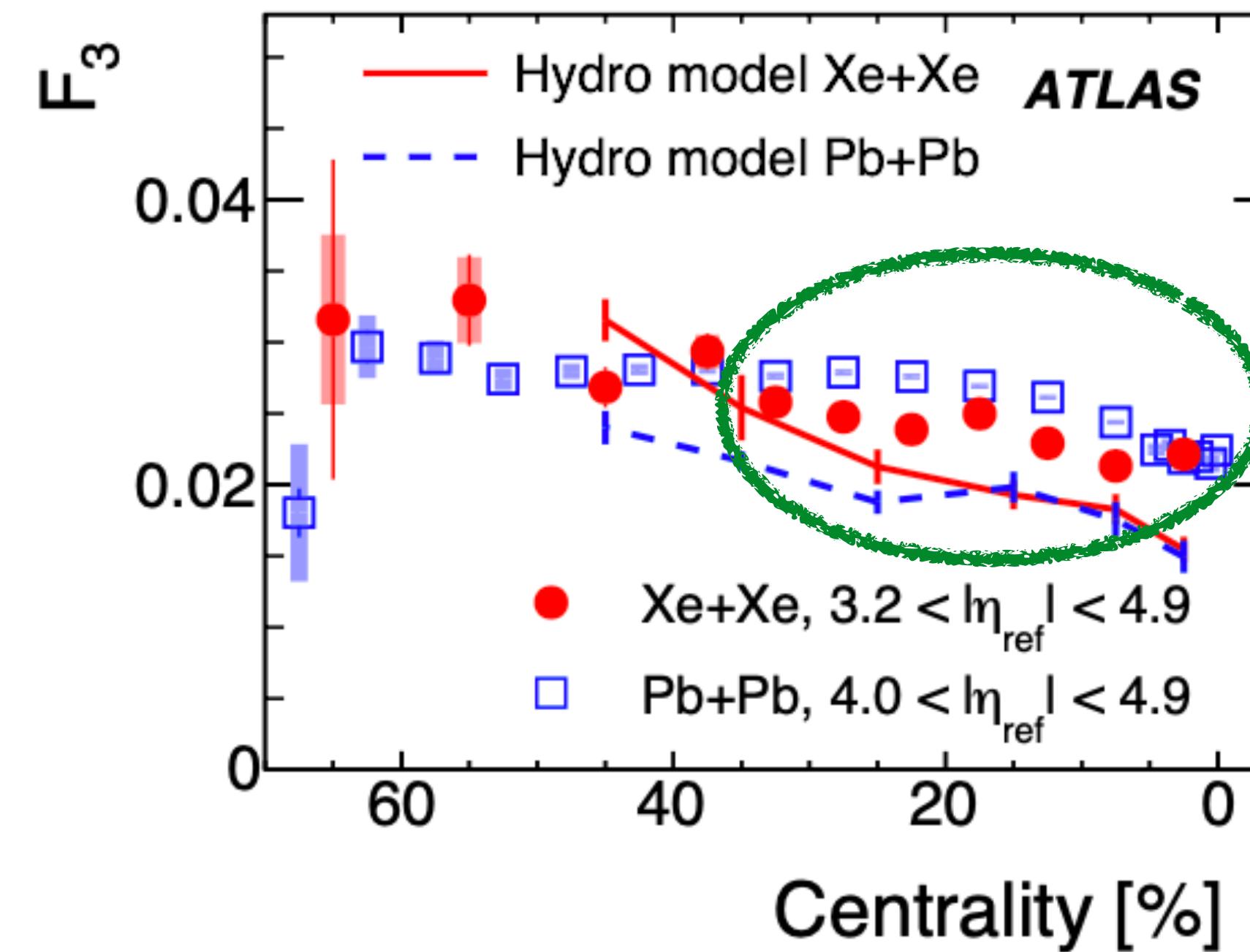
Centrality (avg. geometry)



- Reverse ordering for n=2 and 3

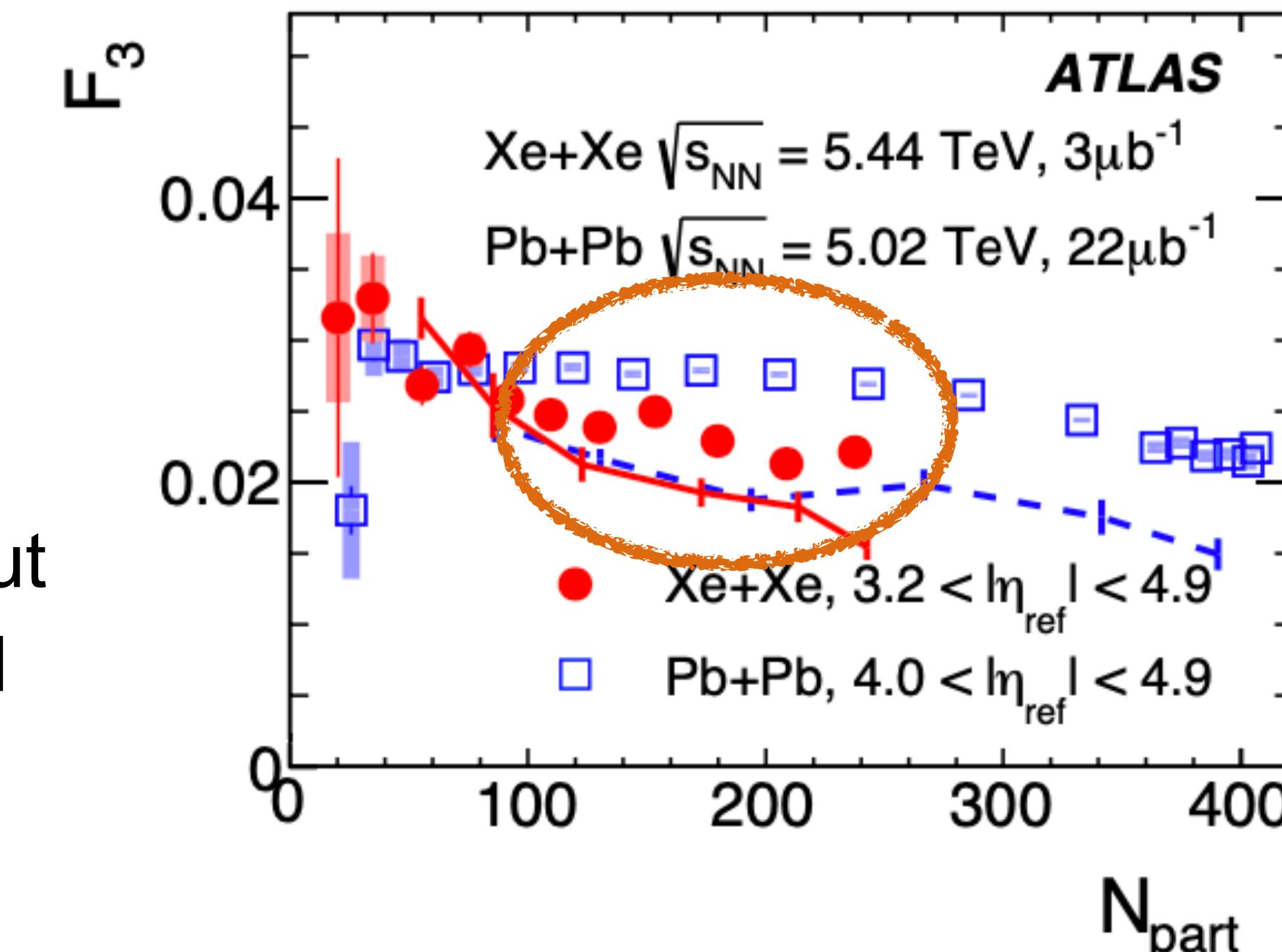
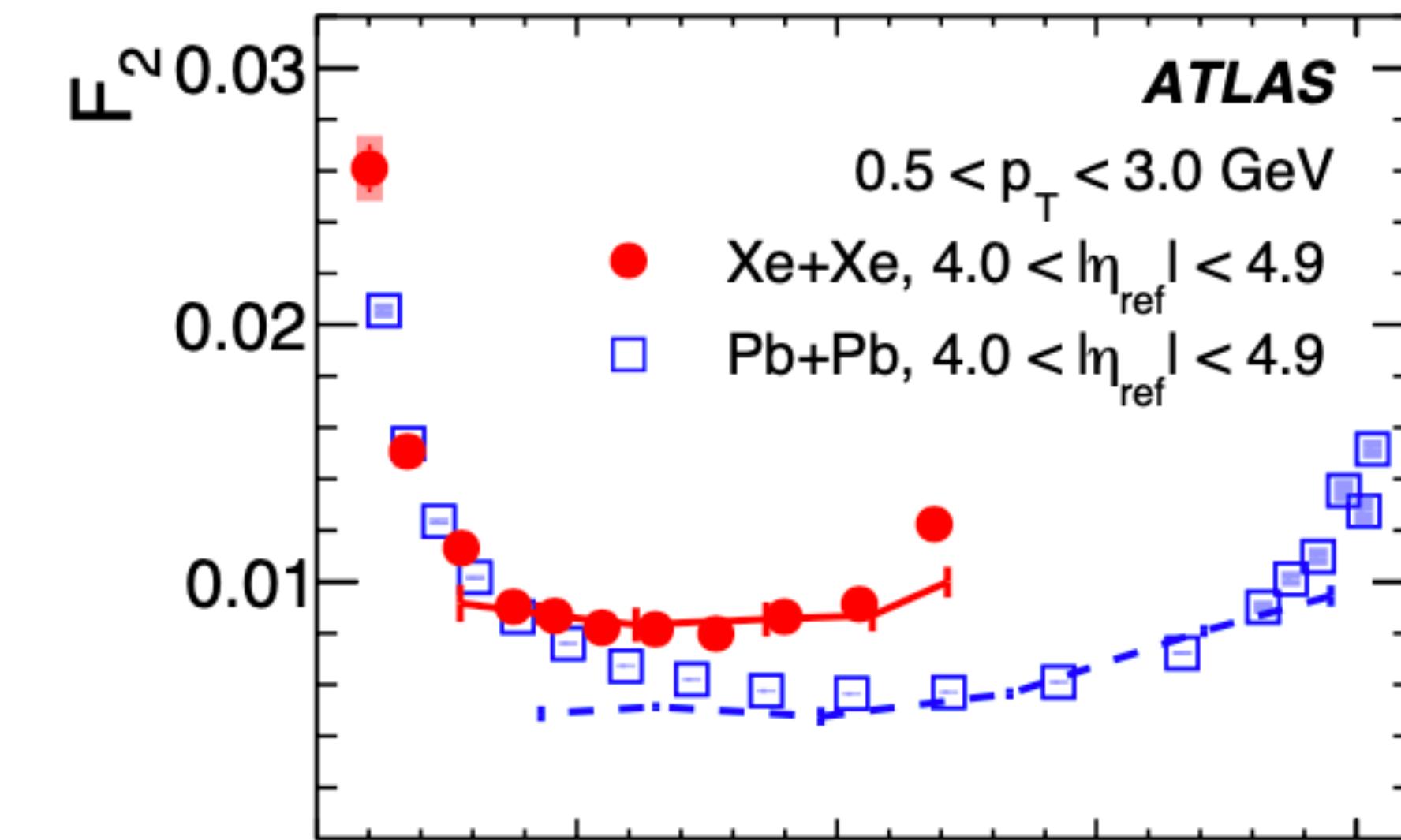
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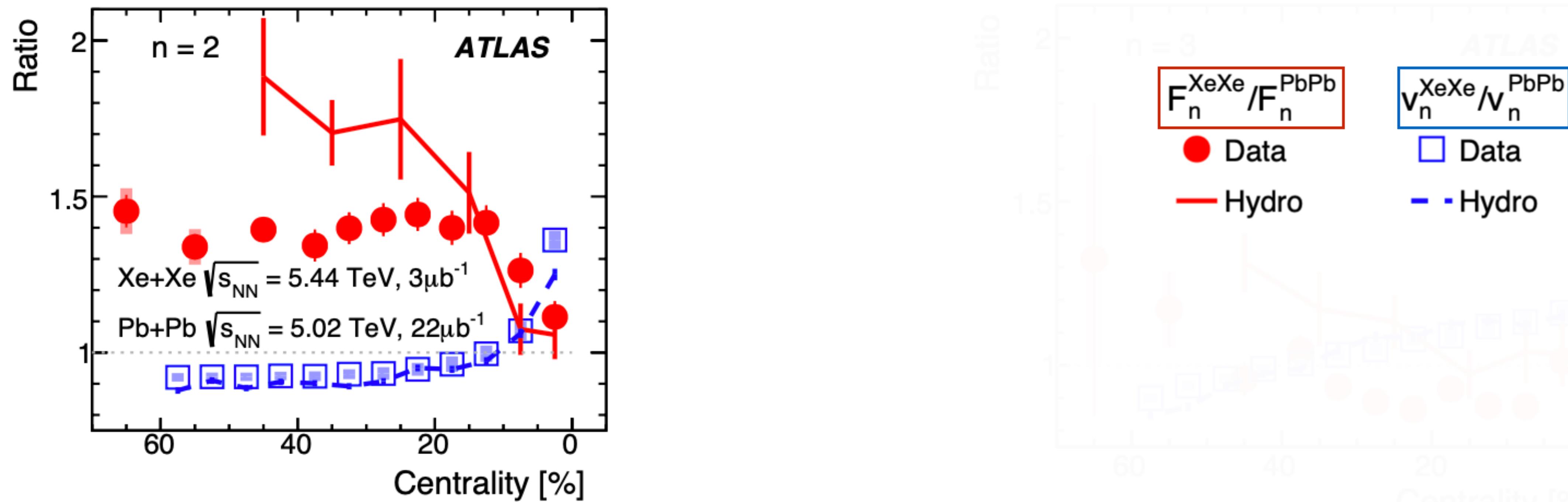
- F_2 and F_3 match - in 0-5% centrality or $N_{\text{part}} < 80$
- Hydro model works for F_2 but fails for F_3 in magnitude and splitting

N_{part} (system-size)



Comparison of v_n and F_n ratios

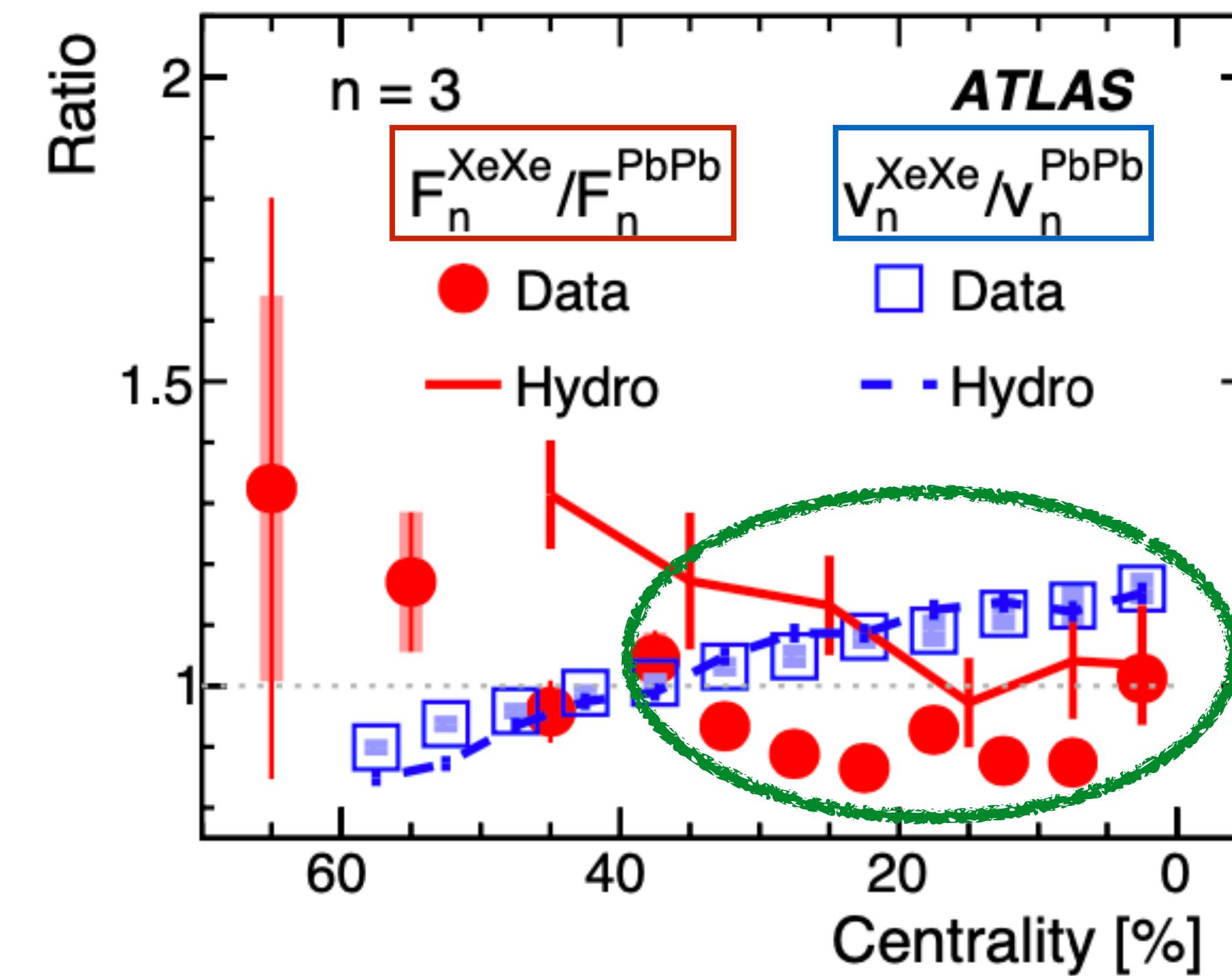
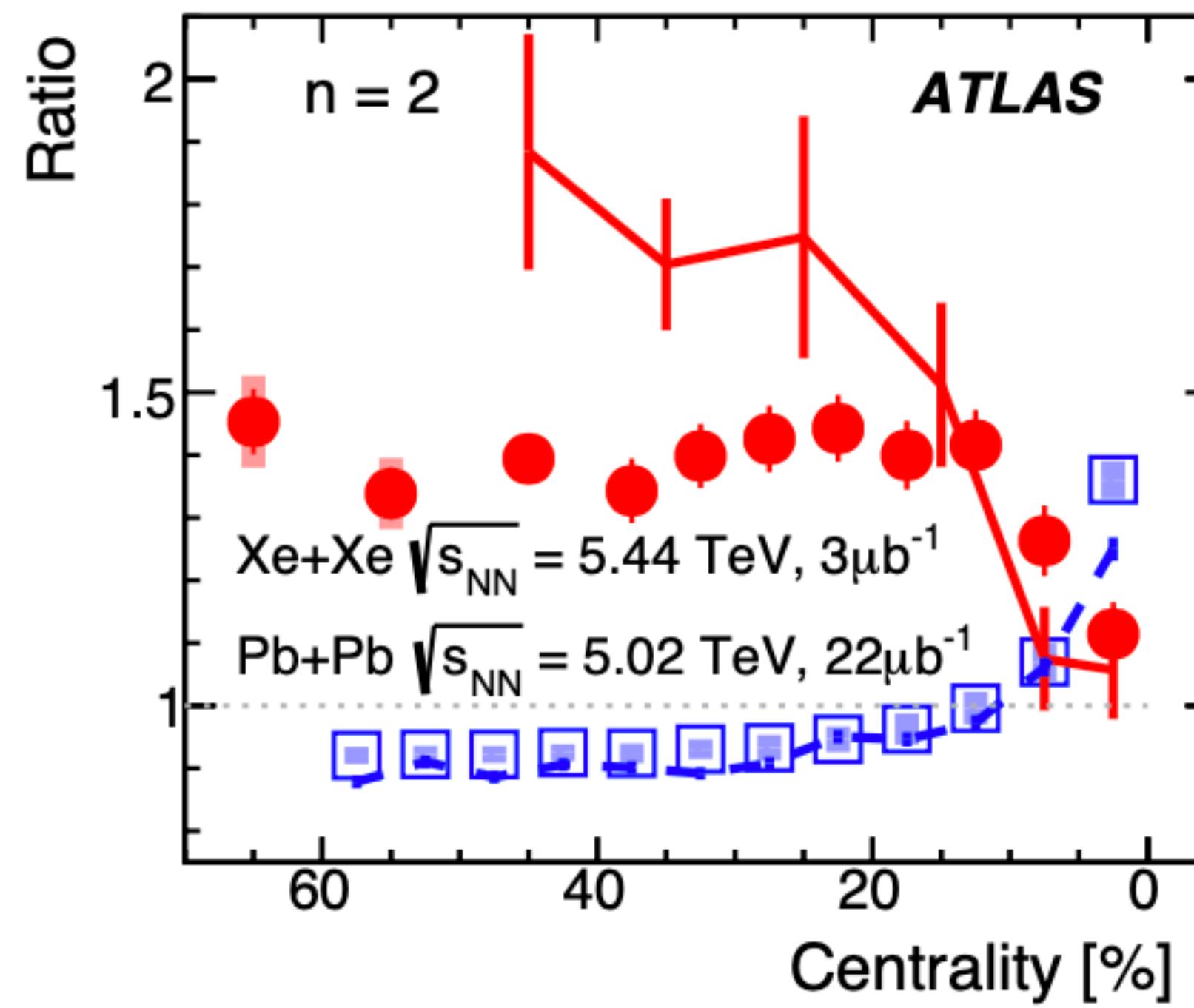
10



- Anti-correlation between v_n and F_n - opposite centrality dependence

Comparison of v_n and F_n ratios

11



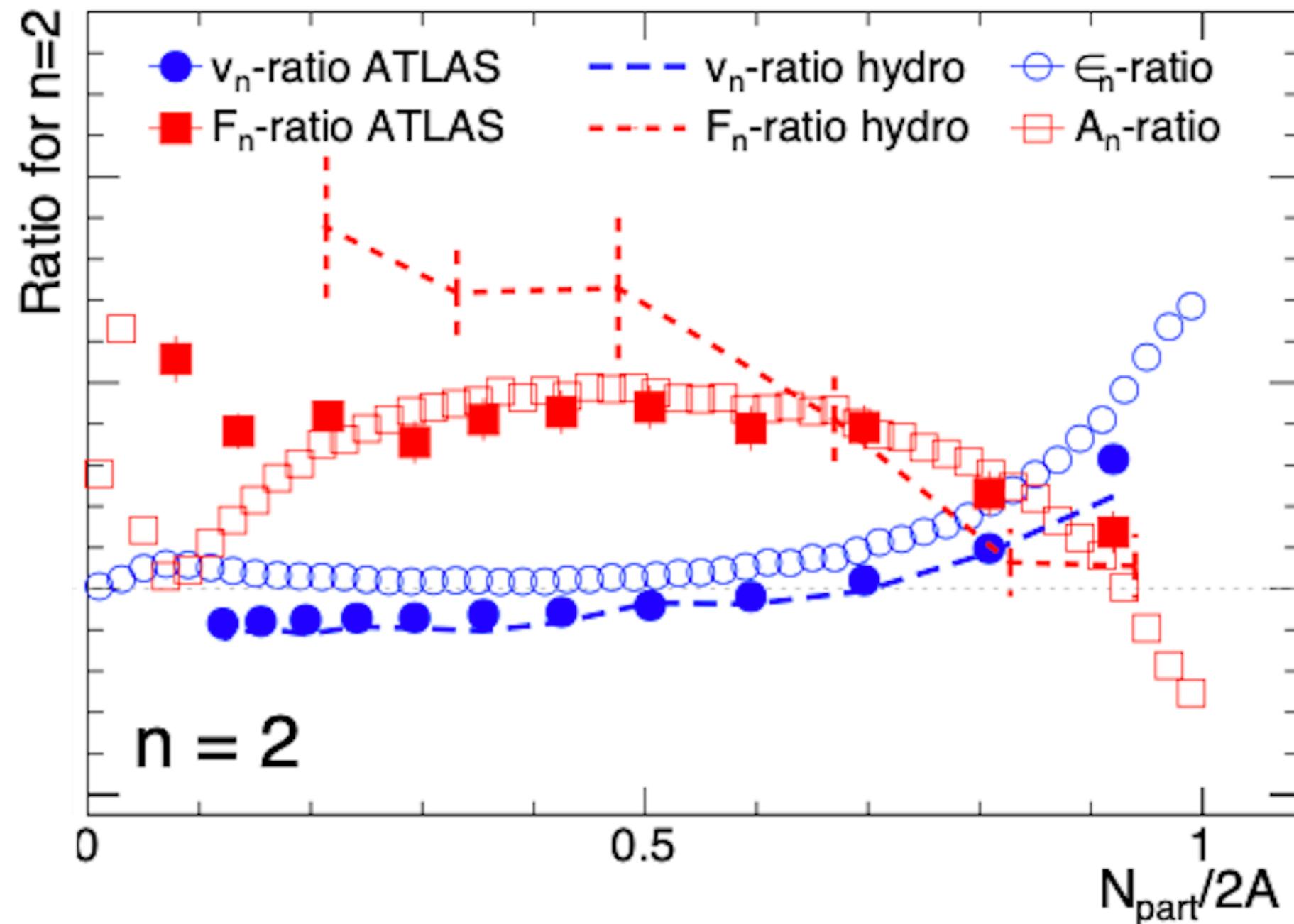
- Anti-correlation between v_n and F_n - opposite centrality dependence
- Reverse ordering of F_2 and F_3 ratios
- Hydro explains v_n ratio very well but fails to explain F_n ratio accurately
- What's the origin of the reverse ordering ?

$$F_2^{XeXe}/F_2^{PbPb} > 1 \quad F_3^{XeXe}/F_3^{PbPb} < 1$$

Comparison with Glauber (Initial State)

12

- Eccentricity ε_n and eccentricity decorrelation A_n from subnucleon-Glauber model arXiv:2003.04340



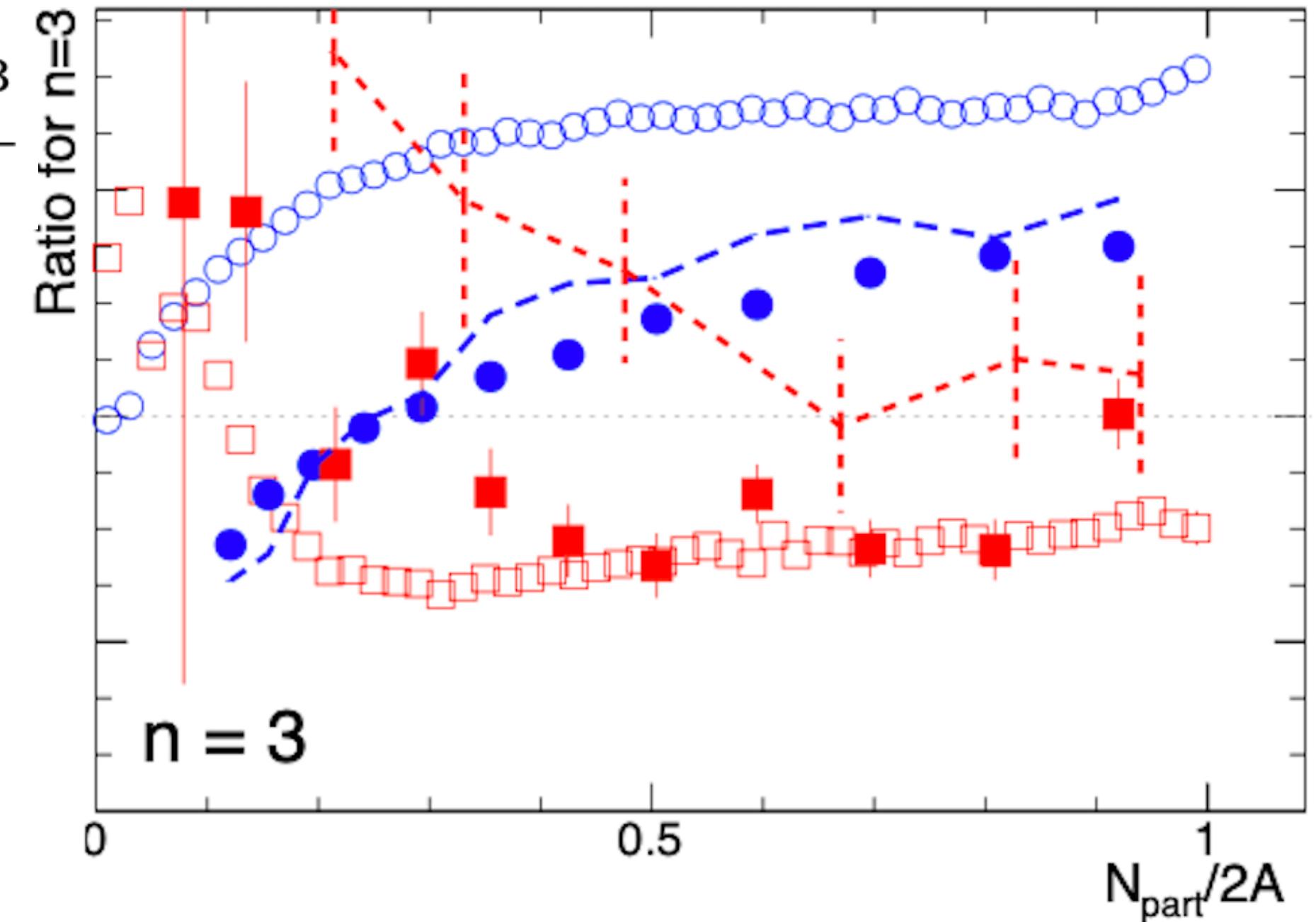
$$\mathcal{E}_{n+} = \frac{\mathcal{E}_n^F + \mathcal{E}_n^B}{2} \quad \mathcal{E}_{n-} = \frac{\mathcal{E}_n^F - \mathcal{E}_n^B}{2}$$

$$A_n \equiv \frac{\langle \varepsilon_{n-}^2 \rangle}{\langle \varepsilon_{n+}^2 \rangle + \langle \varepsilon_{n-}^2 \rangle} \approx \frac{\langle \varepsilon_{n-}^2 \rangle}{\langle \varepsilon_n^2 \rangle}$$

$\varepsilon_n \longrightarrow v_n$

$A_n \longrightarrow F_n$

$N_{\text{part}}/2A \longrightarrow \text{Centrality}$

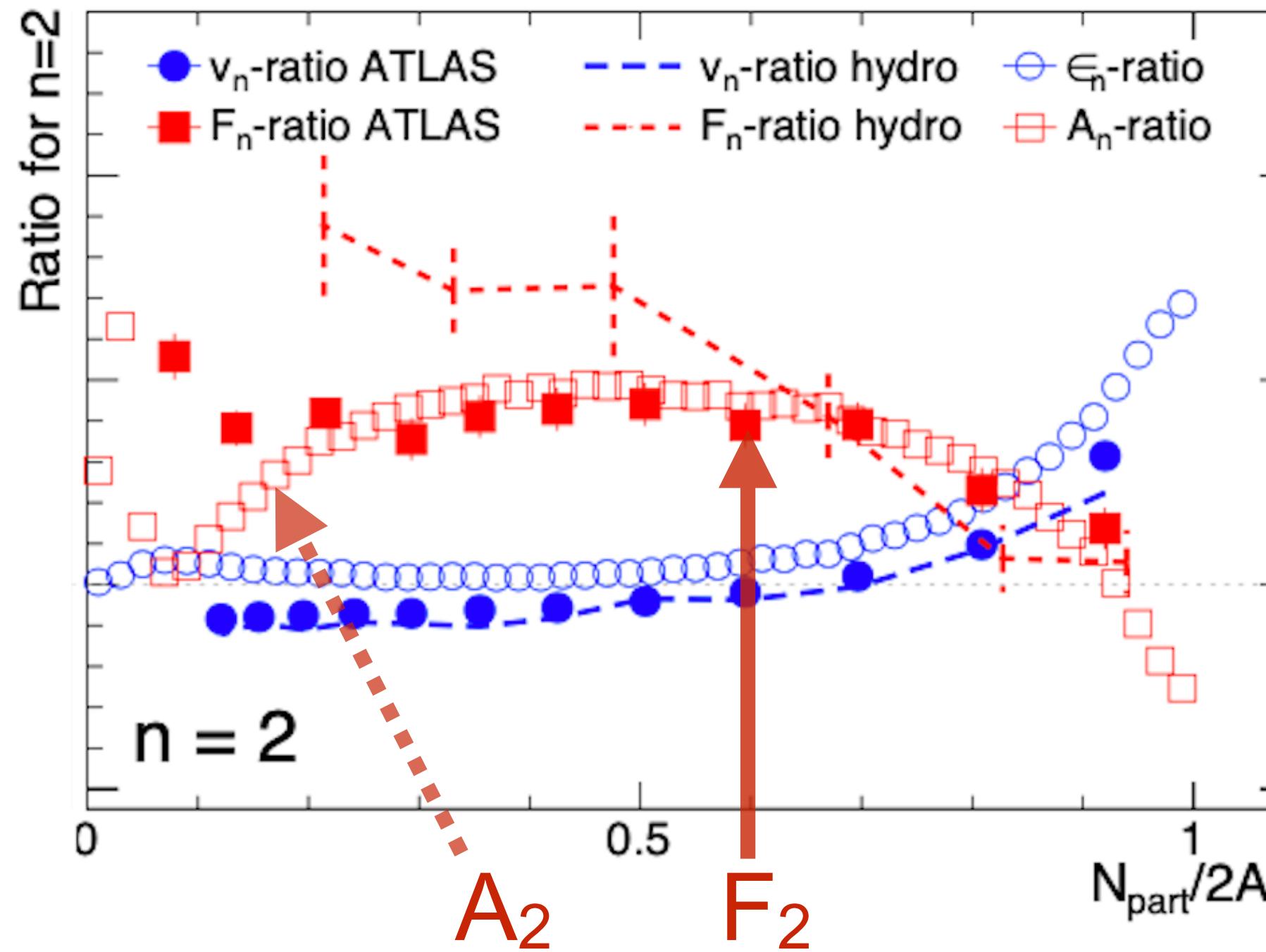


- Difference between v_n and ε_n ratios - Late time effects

Comparison with Glauber (Initial State)

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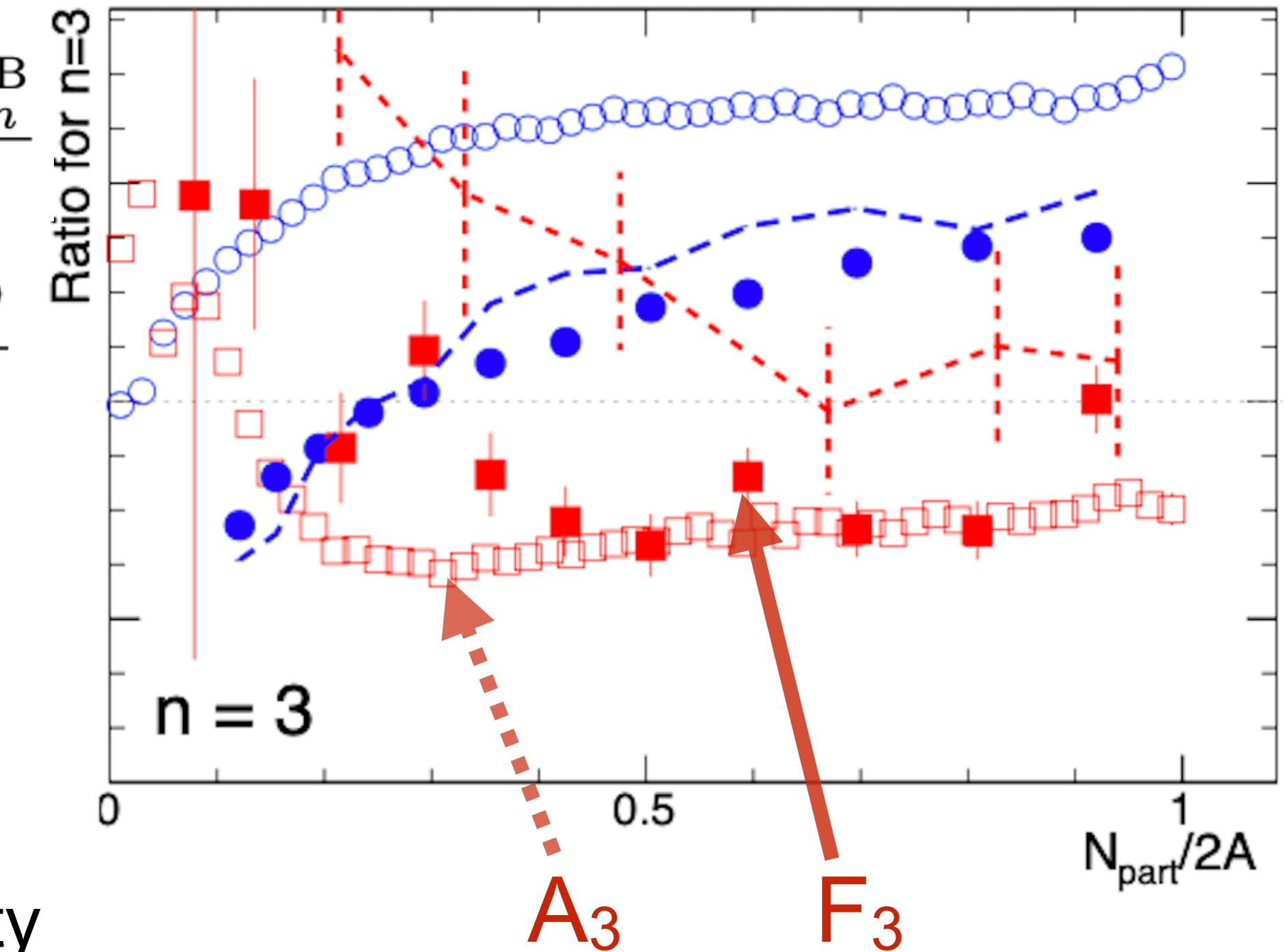
$$\mathcal{E}_{n+} = \frac{\mathcal{E}_n^F + \mathcal{E}_n^B}{2} \quad \mathcal{E}_{n-} = \frac{\mathcal{E}_n^F - \mathcal{E}_n^B}{2}$$

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$\varepsilon_n \longrightarrow v_n$

$A_n \longrightarrow F_n$

$N_{\text{part}}/2A \longrightarrow \text{Centrality}$



- Difference between v_n and ε_n ratios - Late time effects
- F_n and A_n ratios show good agreement - insensitive to late time effects
- Reverse ordering of ATLAS F_2 - F_3 ratios are explained by the Glauber A_2 - A_3 ratios
- System-size dependence of F_n - depends mainly on initial state

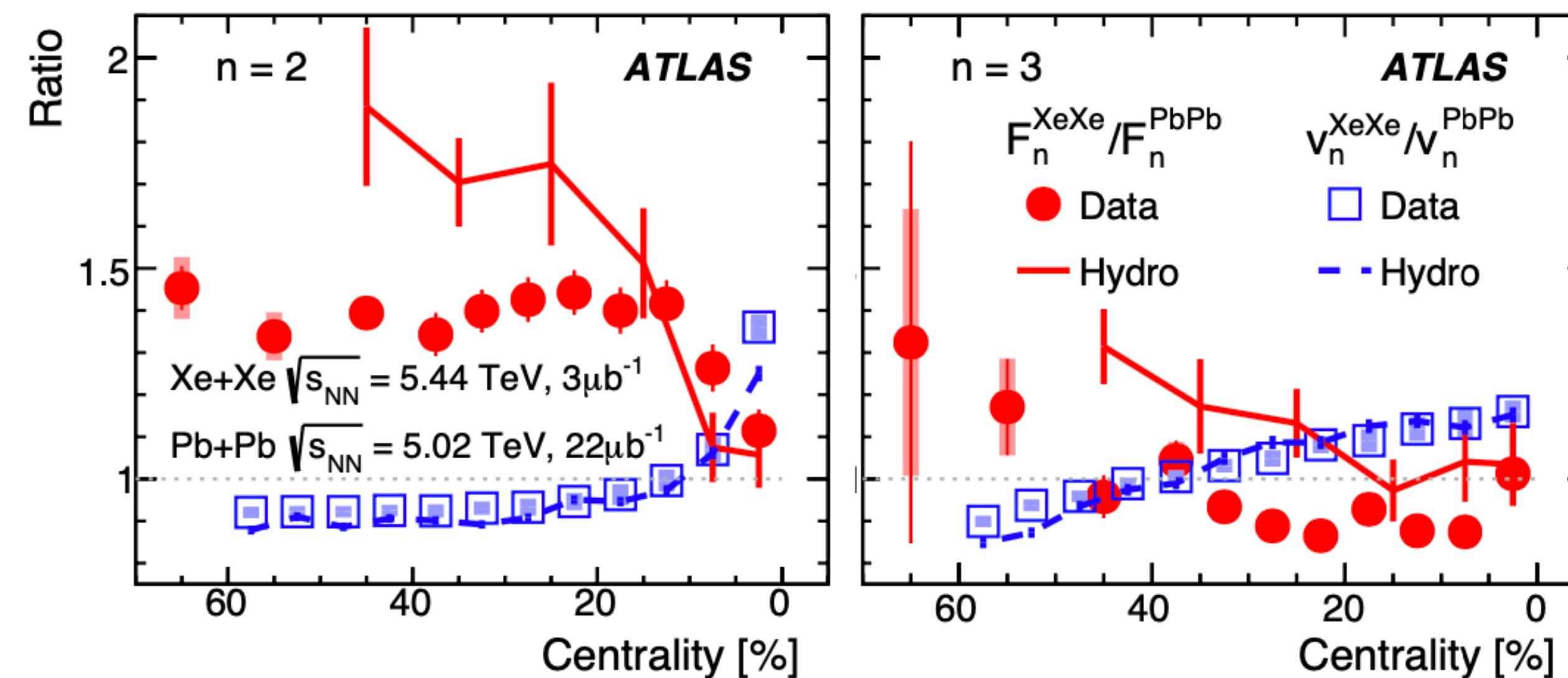
Summary

13

- Strong system-size dependence (Xe+Xe vs Pb+Pb) in ATLAS - both v_n and F_n
- Direct comparison v_n and F_n ratios - **anti-correlation**
- v_n ratios - IS Geometry dominant (central) , Viscous effects dominant (non-central)
- $n=2$ vs $n=3$ - same ordering for v_n ratios **but reverse ordering for F_n ratios**

$$F_2^{XeXe} > F_2^{PbPb}$$

$$F_3^{XeXe} < F_3^{PbPb}$$



- Current Hydro models tuned for v_n ratio cannot explain F_n ratio accurately
- Glauber Calculation - F_n ratio insensitive to late-time effects, Reverse ordering of $n=2,n=3$ due to eccentricity decorrelation
- Measurements can constrain different flow models and help develop full 3+1D initial conditions

Backup

Glauber model comparison

15

- Glauber model calculations compared with ATLAS data and hydro calculations

$$\mathcal{E}_n(\eta) = \mathcal{E}_{n+} + f_n(\eta)\mathcal{E}_{n-}, \quad \mathcal{E}_{n+} = \frac{\mathcal{E}_n^F + \mathcal{E}_n^B}{2} \quad \mathcal{E}_{n-} = \frac{\mathcal{E}_n^F - \mathcal{E}_n^B}{2}$$

$$r_n^s(\eta) \approx 1 - 2\eta a_n A_n, \quad a_n = \left\langle \frac{\partial f_n}{\partial \eta} \Big|_{\eta=0} f_n(\eta_r) \right\rangle,$$

$$A_n \equiv \frac{\langle \varepsilon_{n-}^2 \rangle}{\langle \varepsilon_{n+}^2 \rangle + \langle \varepsilon_{n-}^2 \rangle} \approx \frac{\langle \varepsilon_{n-}^2 \rangle}{\langle \varepsilon_n^2 \rangle}$$

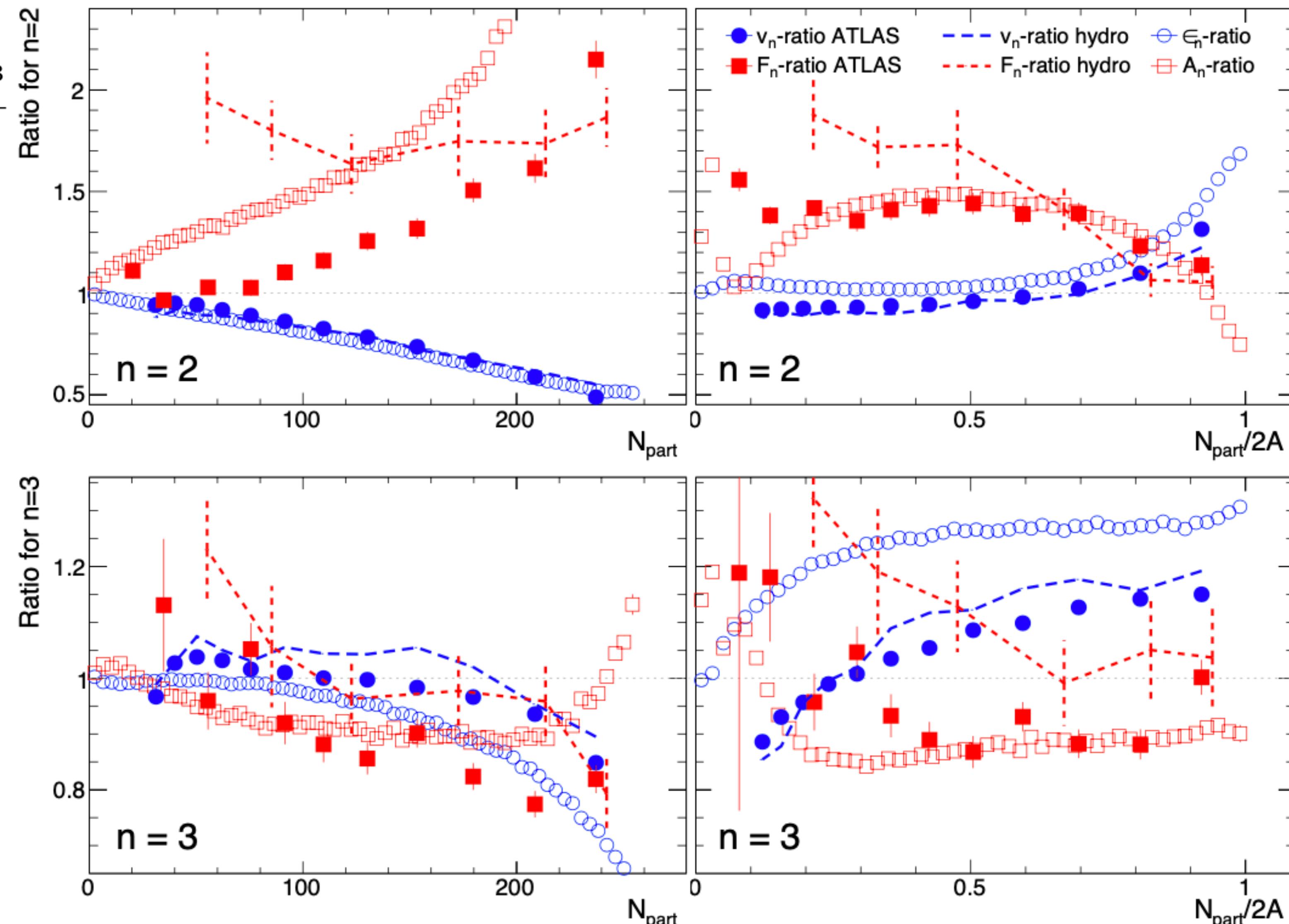
$$\sqrt{\langle v_n^2 \rangle} = \kappa_n \sqrt{\langle \varepsilon_n^2 \rangle}$$

$$F_n = \kappa'_n A_n$$

$$\frac{v_n^{A+A}}{v_n^{B+B}} = \frac{\kappa_n^{A+A}}{\kappa_n^{B+B}} \frac{\varepsilon_n^{A+A}}{\varepsilon_n^{B+B}}, \quad \frac{F_n^{A+A}}{F_n^{B+B}} = \frac{\kappa'_n{}^{A+A}}{\kappa'_n{}^{B+B}} \frac{A_n^{A+A}}{A_n^{B+B}}$$

- Opposite ordering of F_2 and F_3 ratios are well reproduced by ϵ_n and A_n

arXiv:2003.04340



Method - 2PC

16

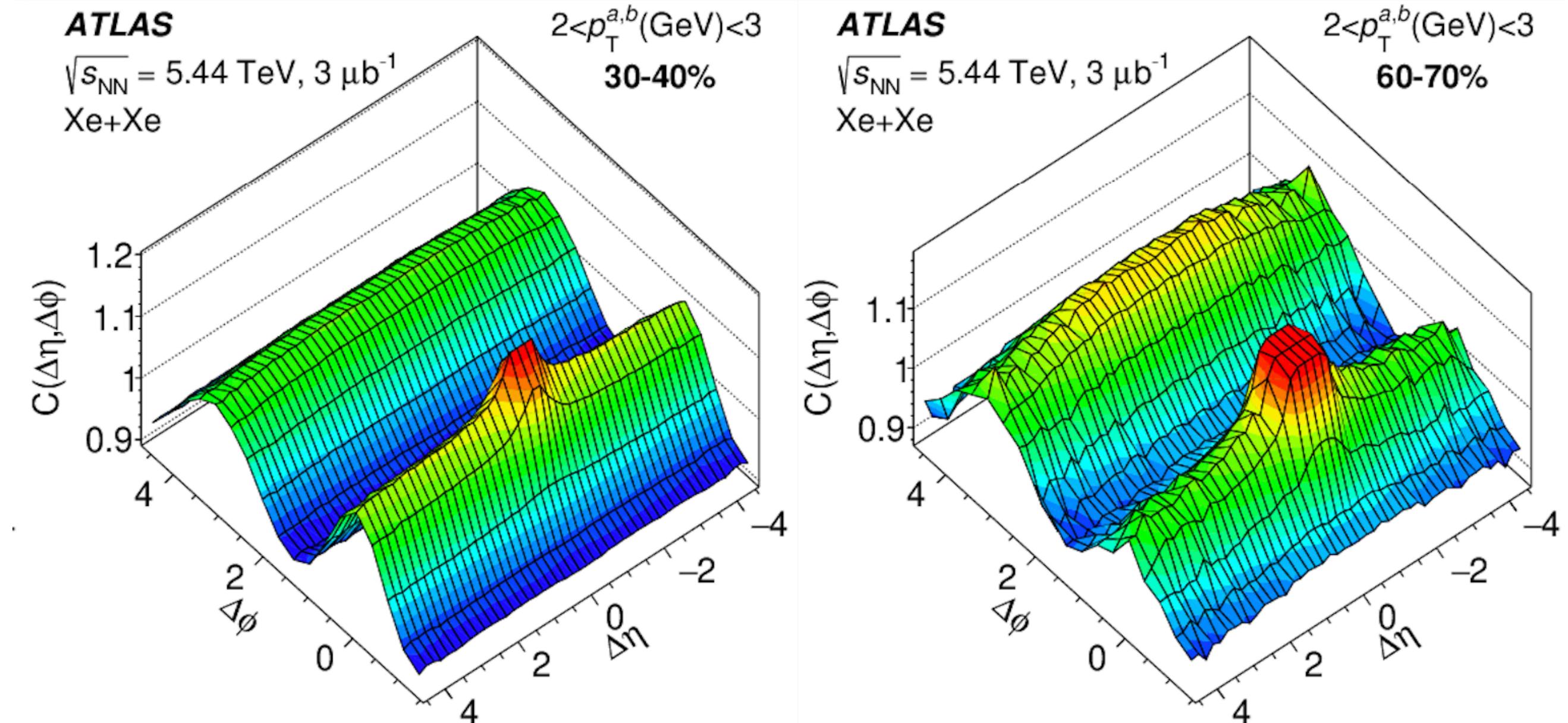
- 2-particle Correlation

$$C(\Delta\eta, \Delta\phi) = \frac{S(\Delta\eta, \Delta\phi)}{B(\Delta\eta, \Delta\phi)}$$

Integrate with $|\Delta\eta| > 2$ - remove short-range non-flow

$$C(\Delta\phi) = C_0 [1 + 2 \sum_{n=1}^{\infty} v_{n,n}(p_T^a, p_T^b) \cos(n\Delta\phi)]$$

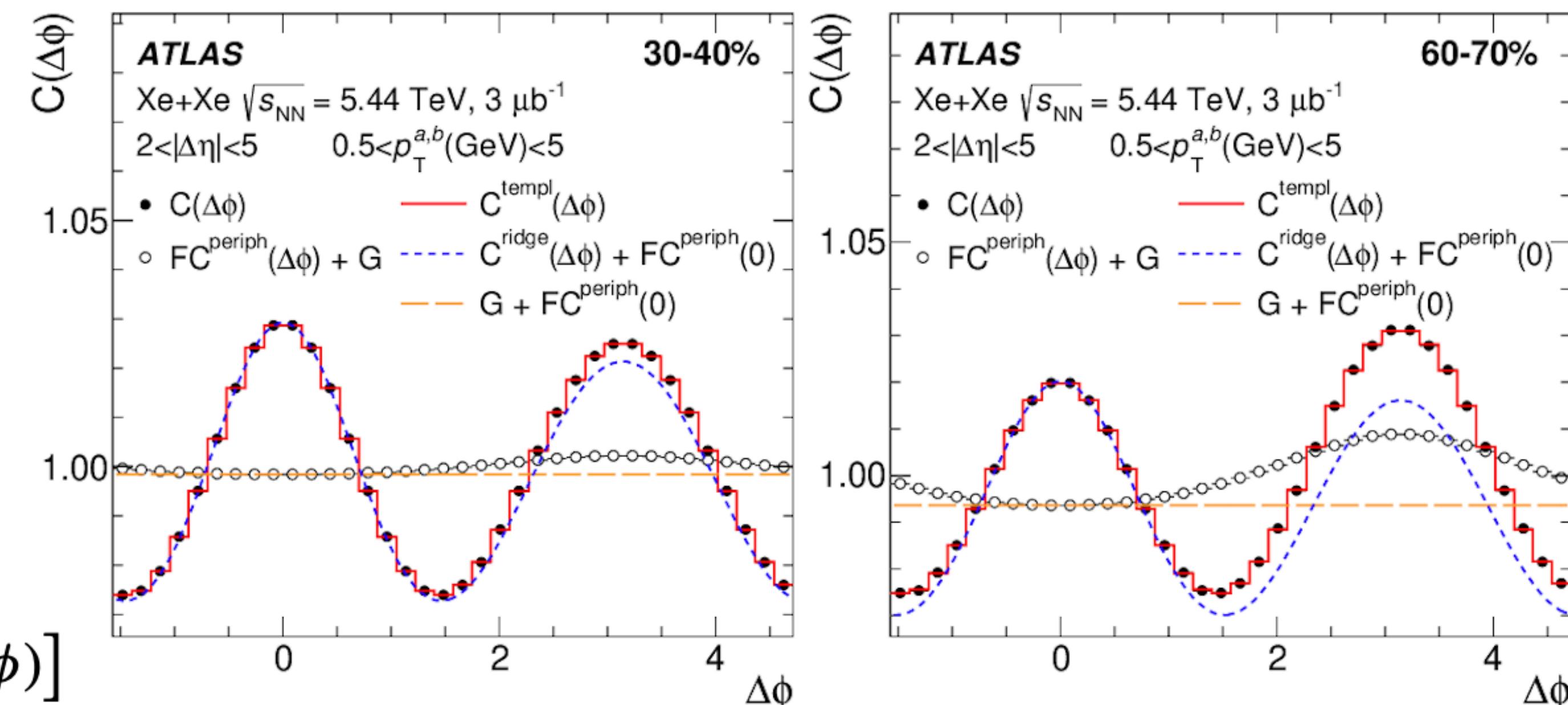
- ◆ Long-range Non-flow (dijets) - peripheral collisions and/or at $p_T > 4\text{GeV}$



- Template fit method is also implemented

- ◆ Developed for pp collisions
- ◆ Can be applied to estimate dijet correlation bias in v_n measurements
- ◆ Significant for Xe+Xe collisions

$$\begin{aligned} C^{\text{templ}}(\Delta\phi) &\equiv F C^{\text{periph}}(\Delta\phi) + C^{\text{ridge}}(\Delta\phi) \\ &= F C^{\text{periph}}(\Delta\phi) + G [1 + 2 \sum_{n=2}^{\infty} v_{n,n} \cos(n\Delta\phi)] \end{aligned}$$



Differential $v_n(p_T)$

17

- Assume factorization

$$v_n(p_T^b) = \frac{v_{n,n}(p_T^a, p_T^b)}{v_n(p_T^a)} = \frac{v_{n,n}(p_T^a, p_T^b)}{\sqrt{v_{n,n}(p_T^a, p_T^a)}}$$

- Plots - p_T dependence of v_n obtained from 2PC and from template fitting (with and without ZYAM)

- 2PC - Large jet-bias at high- p_T in peripheral collisions, most prominent for v_2 and v_4

- Template fitting - reduces this jet bias

