Search for *CP* violation and observation of *P* violation in $\Lambda_b^0 \to p\pi^-\pi^+\pi^-$ decays

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A search for *CP* violation in the $\Lambda_b^0 \to p\pi^-\pi^+\pi^-$ decay is performed using LHCb data corresponding to an integrated luminosity of 6.6 fb^{-1} collected in pp collisions at center-of-mass energies of 7, 8 and 13 TeV. The analysis uses both triple product asymmetries and the unbinned energy test method. The highest significances of *CP* asymmetry are 2.9 standard deviations from triple product asymmetries and 3.0 standard deviations for the energy test method. Once the global *p*-value is considered, all results are consistent with no *CP* violation. Parity violation is observed at a significance of 5.5 standard deviations for the triple product asymmetry method and 5.3 standard deviations for the energy test method. The reported deviations are given in regions of phase space.

The violation of *CP* symmetry, where *C* and *P* are the charge-conjugation and parity operators, is a well-established phenomenon in the decays of *K* and *B* mesons [1–3]. Recently, it has also been observed in the decays of *D* mesons by the LHCb collaboration [4]. However, *CP* violation has yet to be established in baryonic decays, although first evidence was recently found [5]. Such decays offer a novel environment to probe the mechanism for quark-flavor mixing and for *CP* violation, which is regulated by the Cabibbo-Kobayashi-Maskawa (CKM) matrix in the Standard Model (SM) [6,7].

In this paper searches for *CP* and *P* violation with $\Lambda_b^0 \to p\pi^-\pi^+\pi^-$ decays are reported. Throughout, the inclusion of charge-conjugate processes is implied, unless otherwise indicated. This decay is mediated mainly by tree and loop processes of similar magnitudes, proportional to the product of the CKM matrix elements $V_{ub} V_{ud}^*$ and $V_{tb} V_{td}^*$, respectively. This allows for significant interference effects with a relative weak phase α of the unitary triangle between the amplitudes. If matter and antimatter exhibit different effects, *CP* violation manifests as either global asymmetries in decay rates, or as local asymmetries within the phase space. The $\Lambda_b^0 \to p\pi^-\pi^+\pi^-$ decay is particularly well suited for *CP*-violation searches [8] due to a rich resonant structure in the decay. The dominant contributions proceed through the $N^{*+} \to \Delta^{++}(1234)\pi^-$ (referred as

Δ^{++} hereinafter), $\Delta^{++} \to p\pi^+$, $a_1^-(1260) \to \rho^0(770)\pi^-$ and $\rho^0(770) \to \pi^+\pi^-$ decays, where the proton excited states are indicated as N^{*+}. The searches for *CP* violation are performed by separating the *P*-odd and *P*-even contributions [9], as discussed below. In these studies, a large control sample of Cabibbo-favored $\Lambda_b^0 \to \Lambda_c^+(\to pK^-\pi^+)\pi^-$ decays is used, where no *CP* violation is expected, to assess potential experimental biases and systematic effects.

The LHCb collaboration has previously studied the $\Lambda_b^0 \to p\pi^-\pi^+\pi^-$ decay and found evidence for *CP* violation with a significance of 3.3 standard deviations including systematic uncertainties [5]. This paper supersedes the previous results using pp collision data corresponding to an integrated luminosity of 6.6 fb^{-1} collected from 2011 to 2017 at center-of-mass energies of 7, 8 and 13 TeV that represents a four times larger sample in signal yield.

The LHCb detector [10,11] is a single-arm forward spectrometer covering the pseudorapidity range $2 < \eta < 5$, designed for the study of particles containing *b* or *c* quarks. The detector elements that are particularly relevant to this analysis are: a silicon-strip vertex detector surrounding the pp interaction region that allows *b* hadrons to be identified from their characteristically long flight distance; a tracking system that provides a measurement of the momentum, *p*, of charged particles; and two ring-imaging Cherenkov detectors that are able to discriminate between different species of charged hadrons. Simulation is required to model the effects of the detector acceptance and the selection requirements. The pp collisions are generated using PYTHIA [12] with a specific LHCb configuration [13], and neither *CP*—nor *P*-violating effects are present in the signal channel. Decays of unstable particles are described by EVTGEN [14], in which final-state radiation is generated

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using PHOTOS [15]. The interaction of the generated particles with the detector, and its response, are implemented using the GEANT4 toolkit [16] as described in Ref. [17].

The analysis searches for *CP* and *P* violation by measuring triple product asymmetries (TPA) and by exploiting the unbinned energy test method [18–24]. In the TPA analysis, both local and integrated asymmetries are considered. The analysis also benefits from additional studies of amplitude models [9,25] to maximize the sensitivity. The energy test method is designed to look for localized differences in the phase space between two samples. The Λ_b^0 polarization has been measured to be compatible with zero in a previous LHCb analysis [26] and is neglected in these measurements.

The scalar triple products are defined as $C_{\hat{T}} \equiv \vec{p}_p \cdot (\vec{p}_{\pi_{\text{fast}}^-} \times \vec{p}_{\pi^+})$ and $\bar{C}_{\hat{T}} \equiv \vec{p}_{\bar{p}} \cdot (\vec{p}_{\pi_{\text{fast}}^+} \times \vec{p}_{\pi^-})$, for Λ_b^0 and $\bar{\Lambda}_b^0$ respectively. Hereinafter π_{fast}^- (π_{slow}^-) refers to the faster (slower) of two negative pions in the Λ_b^0 rest frame. Following these definitions, four statistically independent subsamples are considered, labeled with *I* for $C_{\hat{T}} > 0$, *II* for $C_{\hat{T}} < 0$, *III* for $-\bar{C}_{\hat{T}} > 0$ and *IV* for $-\bar{C}_{\hat{T}} < 0$. Samples *I* and *III* are related by a *CP* transformation, as are samples *II* and *IV*. Samples *I* and *II* are related by a *P* transformation, as are samples *III* and *IV*. Both *CP*—and *P*-violating effects appear as differences between the triple product observables related by *CP* and *P* transformations. The $\hat{T}$ operator reverses momentum and spin three-vectors [27,28]. The quantities $C_{\hat{T}}$ and $\bar{C}_{\hat{T}}$ are odd under this operator. This enables studies of the *P*-odd *CP* violation, which occurs via interference of the $\hat{T}$-even and $\hat{T}$-odd amplitudes with different *CP*-odd ("weak") phases [9,25,27,28].

The TPA are defined as

$$A_{\hat{T}} = \frac{N(C_{\hat{T}} > 0) - N(C_{\hat{T}} < 0)}{N(C_{\hat{T}} > 0) + N(C_{\hat{T}} < 0)},$$

$$\bar{A}_{\hat{T}} = \frac{\bar{N}(-\bar{C}_{\hat{T}} > 0) - \bar{N}(-\bar{C}_{\hat{T}} < 0)}{\bar{N}(-\bar{C}_{\hat{T}} > 0) + \bar{N}(-\bar{C}_{\hat{T}} < 0)}, \qquad (1)$$

where N and $\bar{N}$ are the yields of Λ_b^0 and $\bar{\Lambda}_b^0$ decays, respectively. The *CP*—and *P*-violating asymmetries are then defined as

$$a_{CP}^{\hat{T}\text{-odd}} = \frac{1}{2}(A_{\hat{T}} - \bar{A}_{\hat{T}}), \qquad a_P^{\hat{T}\text{-odd}} = \frac{1}{2}(A_{\hat{T}} + \bar{A}_{\hat{T}}). \quad (2)$$

Two types of asymmetries are determined from data. The first are localized in the phase space in order to enhance sensitivity to local effects and the second are integrated over the whole phase space. By construction, such asymmetries are largely insensitive to particle-antiparticle production and detector-induced asymmetries [29].

The previous LHCb result [5] showed evidence for a dependence of the *CP* asymmetry as a function of $|\Phi|$, the absolute value of the angle between the planes defined by the $p\pi_{\text{fast}}^-$ and $\pi^+\pi_{\text{slow}}^-$ systems in the Λ_b^0 rest frame. In the present analysis a binning scheme, labeled *A*, is considered, based on the results of an approximate amplitude analysis performed on $\Lambda_b^0 \to p\pi^-\pi^+\pi^-$ decays. The binning scheme consists in dividing the data sample into 16 subsamples to explore the distribution of the polar and azimuthal angles of the proton (Δ^{++}) in the Δ^{++} (N^{*+}) rest frame. A detailed description can be found in the Appendix. A second binning scheme, labeled *B*, is used to probe the asymmetries as a function of $|\Phi|$, dividing the data sample into ten subsamples uniformly distributed in the range $[0, \pi]$. The invariant-mass regions $m(p\pi^+\pi_{\text{slow}}^-) > 2.8$ GeV/c^2 (samples A_1, B_1), dominated by the a_1 resonance, and $m(p\pi^+\pi_{\text{slow}}^-) < 2.8$ GeV/c^2 (samples A_2, B_2), dominated by the N^{*+} decay, are studied separately. The compatibility of the measured asymmetries with *CP* and *P* conservation is checked by means of a χ^2 test taking into account statistical and systematic effects.

The energy test is a model-independent unbinned test sensitive to local differences between two samples, as might arise from *CP* violation. It can provide superior discriminating power between different samples than traditional χ^2 tests [21,22]. The test is performed through the calculation of a test statistic

$$T \equiv \frac{1}{2n(n-1)}\sum_{i \neq j}^{n}\psi_{ij} + \frac{1}{2\bar{n}(\bar{n}-1)}\sum_{i \neq j}^{\bar{n}}\psi_{ij} - \frac{1}{n\bar{n}}\sum_{i=1}^{n}\sum_{j=1}^{\bar{n}}\psi_{ij},$$

$$(3)$$

where there are n ($\bar{n}$) candidates in the first (second) sample. The first (second) term sums over pairs of candidates drawn from the first (second) sample and the final term sums over pairs with one candidate drawn from each sample. Each pair of candidates ij is assigned a weight $\psi_{ij} = e^{-d_{ij}^2/2\delta^2}$, where d_{ij} is their Euclidean distance in phase space, while the tunable parameter δ determines the distance scale probed using the energy test. The phase space is defined using the squared masses $m^2(p\pi^+)$, $m^2(\pi^+\pi_{\text{slow}}^-)$, $m^2(p\pi^+\pi_{\text{slow}}^-)$, $m^2(\pi^+\pi_{\text{slow}}^-\pi_{\text{fast}}^-)$ and $m^2(p\pi_{\text{slow}}^-)$. The value of T is large when there are significant localized differences between samples and has an expectation of zero when there are no differences. The distribution of T under the hypothesis of no sample differences, and the assignment of *p*-values, are determined using a permutation method [21,23].

Similarly to the TPA method, the comparison of subsamples *I* and *IV* to subsamples *II* and *III* allows for a *P*-odd and *CP*-odd test; the comparison of subsamples *I* and *II* to subsamples *III* and *IV* for a *P*-even and *CP*-odd test. The *P* violation is also tested by comparing the combination of subsamples *I* and *III* with the combination of subsamples *II* and *IV*. This provides three test configurations described in detail in Ref. [22] and illustrated in

figures therein. The length scale at which *CP* violation might appear is not known. Therefore three different scales are probed in each configuration, chosen following Refs. [21,22] as $\delta = 1.6$ GeV^2/c^4, 2.7 GeV^2/c^4 and 13 GeV^2/c^4. The sensitivity of the chosen scales was confirmed using simulated events. For each of the three test configurations all three scales are probed, such that nine tests are made overall: six tests for effects arising from *CP* violation (three probing *P*-even *CP* violation and three *P*-odd *CP* violation) and three tests for effects arising from *P* violation.

The candidate $\Lambda_b^0 \to p\pi^-\pi^+\pi^-$ decays are formed by combining tracks with transverse (total) momentum greater than 250 MeV/c (1.5 GeV/c) identified as protons and pions that originate from a common vertex displaced from the primary vertex. A cut on the invariant-mass $m(pK^-\pi^+) \in [2.26, 2.30]$ GeV/c^2 is applied to select $\Lambda_b^0 \to \Lambda_c^+(\to pK^-\pi^+)\pi^-$ decay candidates used as a control sample. A boosted decision tree classifier [30] (BDT), independently optimized for different center-of-mass energies, is constructed from a set of kinematic variables that discriminate between signal and background. The result of an unbinned extended maximum-likelihood fit to the invariant-mass distribution, $m(p\pi^-\pi^+\pi^-)$, is shown in Fig. 1 for the dataset integrated over the phase space. The invariant-mass distribution of the signal is modelled by a Gaussian function core with power-law tails [31], with the mean and width of the Gaussian function determined from the fit to data. All other parameters of the signal fit model are taken from simulation except for the yields. The combinatorial background is parametrized with an
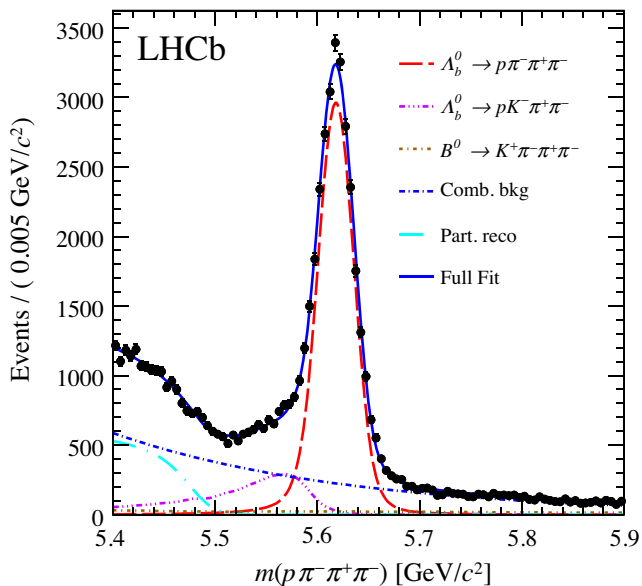
exponential function where the parameters are left free to vary in the fits. Partially reconstructed Λ_b^0 decays, as for example $\Lambda_b^0 \to p\pi^-\pi^+\pi^-\pi^0$, are described by an ARGUS function [32] convolved with a Gaussian function to account for resolution effects. The shapes of backgrounds from other *b*-hadron decays due to incorrectly identified particles, e.g., kaons identified as pions or protons identified as kaons, are modeled using simulated events. These consist mainly of $\Lambda_b^0 \to pK^-\pi^+\pi^-$ and $B^0 \to K^+\pi^-\pi^+\pi^-$ decays. Their yields are obtained from fits to data where the invariant-mass distributions are reconstructed under the appropriate mass hypotheses and then fixed in the baseline fits. The signal yields for the $\Lambda_b^0 \to p\pi^-\pi^+\pi^-$ decay and the $\Lambda_b^0 \to \Lambda_c^+(\to pK^-\pi^+)\pi^-$ control sample are 27600 ± 200 and 434500 ± 800, respectively. Fits in bins of phase space are also performed to determine asymmetries $A_{\hat{T}}$ and $\bar{A}_{\hat{T}}$ in each region, assigning signal candidates to four categories according to Λ_b^0 or $\bar{\Lambda}_b^0$ flavor and sign of $C_{\hat{T}}$ or $\bar{C}_{\hat{T}}$. The asymmetries $A_{\hat{T}}$ and $\bar{A}_{\hat{T}}$ are found to be uncorrelated. Corresponding asymmetries for each of the background components are also determined in the fit; they are found to be consistent with zero, and do not lead to significant systematic uncertainties in the signal asymmetries. Artificial asymmetries are generated for signal events using a parametrized simulated sample, and used to perform checks of the sensitivity of the methods applied. When *P*-odd *CP* violation is injected via the N^* resonances in such studies, both the triple product asymmetry method and the energy test are able to provide a clear rejection of the no-*CP* violation hypothesis. When *P*-even *CP* violation is injected in the simulated samples via the a_1 resonance, the energy test is also able to observe this effect.

For the energy test, Λ_b^0 candidates are selected in a window corresponding to 2.5 standard deviations of the Gaussian function around the known Λ_b^0 mass [33], which optimizes the sensitivity to *CP* violation. The background component with this selection is small and does not affect the analysis.

The reconstruction efficiency for signal candidates with $C_{\hat{T}} > 0$ is consistent with that for candidates with $C_{\hat{T}} < 0$. This indicates that the detector and the reconstruction algorithms do not bias the measurements. This is confirmed using the control sample and a large sample of simulated events. The same check is performed for the $\bar{C}_{\hat{T}}$ observable. As a general cross-check, the *CP* asymmetry is measured in the control sample and found to be compatible with zero, $a_{CP}^{\hat{T}\text{-odd}}(\Lambda_c^+\pi^-) = (+0.04 \pm 0.16)\%$.

The main sources of systematic uncertainties in the TPA analysis are selection criteria, reconstruction and detector acceptance. They are evaluated using the control sample. In the TPA analysis, a systematic uncertainty of 0.16% is assigned for the integrated measurements, while uncertainties in the range (0.6–2.5)% are assigned for local

FIG. 1. Invariant-mass distribution for $\Lambda_b^0 \to p\pi^-\pi^+\pi^-$ candidates with the result of the fit overlaid. The solid and dotted lines describe the projections of the fit results for various components as listed in the legend.

measurements. The systematic uncertainty arising from the experimental resolution of the triple products $C_{\hat{T}}$ and $\bar{C}_{\hat{T}}$, which could introduce a migration of candidates between bins, is estimated from simulation. The difference between the reconstructed and generated asymmetries, 0.01%, is taken as a systematic uncertainty in the TPA analysis. To assess the systematic uncertainty associated with the fit model, an alternative is used to compare the results measured on pseudoexperiments with respect to the baseline model. A value of 0.06% (0.08%) for $a_{CP}^{\hat{T}\text{-odd}}/a_{P}^{\hat{T}\text{-odd}}$ ($A_{\hat{T}}/\bar{A}_{\hat{T}}$) is assigned as systematic uncertainty. No significant differences are observed comparing results from different running conditions, trigger requirements and selection criteria.

Several studies are made to confirm the reliability of the energy test method. The method is insensitive to global asymmetries, and so is not affected by differences between Λ_b^0 and $\bar{\Lambda}_b^0$ production rates. However, local asymmetries due to detector effects may yield significant results that would lead to an incorrect conclusion. The potential presence of such effects is studied using the control sample. No evidence is found for any local asymmetry.

Contributions from background decays are considered, in case they contain localized asymmetries not related to CP violation. A high-mass selection is applied $(5.75 < m(p\pi^-\pi^+\pi^-) < 6.10 \text{ GeV}/c^2)$ to identify candidates predominantly produced by random combinations of particles. No significant effect is found in the six configurations of the energy test probing the CP-conserving hypothesis. Moreover, a small independent sample of the dominant peaking background $(\Lambda_b^0 \to pK^-\pi^+\pi^-)$ is selected using the same requirements as in Ref. [5], with the number of candidates corresponding to the size of the relevant background in the $\Lambda_b^0 \to p\pi^-\pi^+\pi^-$ sample. Again, no p-values corresponding to a significance above 3 standard deviations are observed when the six configurations of the energy test probing CP violation are applied to this sample. The background contribution from the $B^0 \to K^+\pi^-\pi^+\pi^-$ decay is negligible within the mass window selected for the energy test.

Finally, the proton detection asymmetry in simulation is replicated in the $\Lambda_b^0 \to p\pi^-\pi^+\pi^-$ data sample by setting the Λ_b^0 flavor in the data sample at random to create the same asymmetry. The P-even and P-odd configurations of the energy test are then run for all three distance scales to test for effects that might lead to an incorrect rejection of the CP-conserving hypothesis. This is repeated multiple times for each test with different flavor assignments for the Λ_b^0 candidates. In all six tests the distribution of p-values is consistent with being uniform, so no evidence for any bias from the proton detection asymmetry is found.

The measured TPA from the fit to the full data set are $a_{CP}^{\hat{T}\text{-odd}} = (-0.7 \pm 0.7 \pm 0.2)\%$ and $a_{P}^{\hat{T}\text{-odd}} = (-4.0 \pm 0.7 \pm 0.2)\%$. Consistency with the CP-conserving hypothesis is observed, while a significant nonzero value for the $a_{P}^{\hat{T}\text{-odd}}$
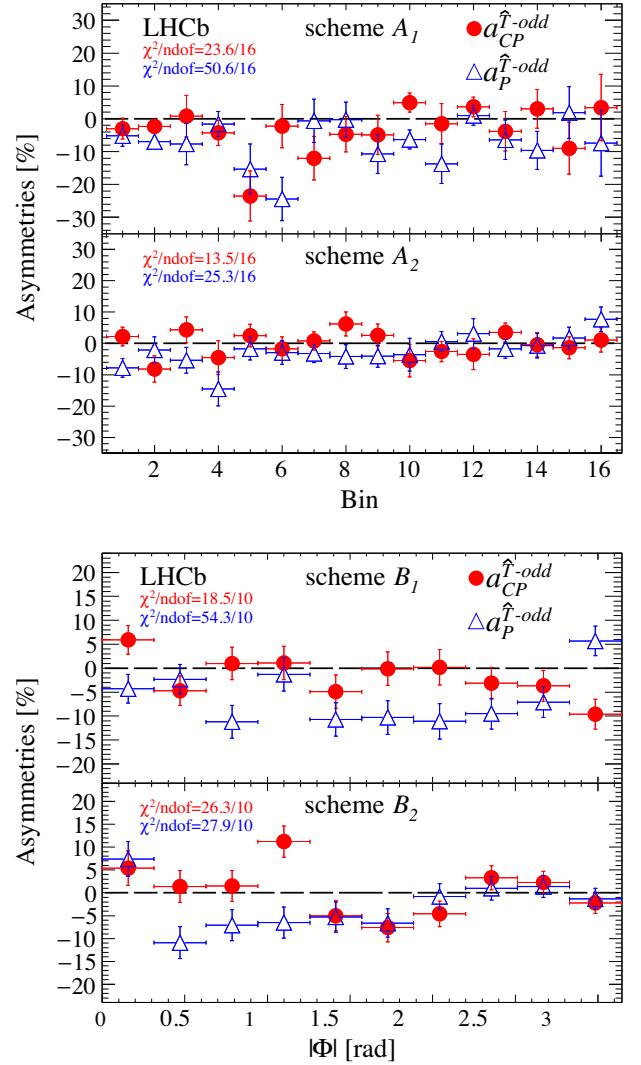

FIG. 2. Measured asymmetries for the binning scheme (top) A_1 and A_2 and (bottom) B_1 and B_2. The error bars represent the sum in quadrature of the statistical and systematic uncertainties. The χ^2 per ndof is calculated with respect to the null hypothesis and includes statistical and systematic uncertainties.

asymmetry is found. The effect, estimated with the profile likelihood-ratio test, has a significance of 5.5 standard deviations and indicates parity violation in the $\Lambda_b^0 \to p\pi^-\pi^+\pi^-$ decay.

The values of the TPA for the binning schemes A_1, A_2, B_1 and B_2 are shown in Fig. 2. In the binning schemes A_2 and B_2 the contribution from multiple N^{*+} resonances dominates and therefore larger CP asymmetries are possible relative to the A_1 and B_1 binning schemes where the single a_1 resonance contributes. However, in the A_2 and B_2 phase-space regions, p-values with respect to the CP-conserving hypothesis corresponding to statistical significances of 0.5 and 2.9 standard deviations are measured, respectively. The evidence of CP violation previously observed [5] is therefore not established.

TABLE I.   The *p*-values from the energy test for different distance scales and test configurations.

Distance scale δ	1.6 GeV$^2/c^4$	2.7 GeV$^2/c^4$	13 GeV$^2/c^4$
p-value (*CP* conservation, *P* even)	3.1×10^{-2}	2.7×10^{-3}	1.3×10^{-2}
p-value (*CP* conservation, *P* odd)	1.5×10^{-1}	6.9×10^{-2}	6.5×10^{-2}
p-value (*P* conservation)	1.3×10^{-7}	4.0×10^{-7}	1.6×10^{-1}

The binning scheme B, which does not separate the a_1 and the N^{*+} contributions, provides a deviation at 2.8 and 5.1 standard deviations from the *CP* and *P* conserving hypothesis, respectively. The compatibility of these results with the previous published measurements [5], based on the same binning scheme, is determined to be at 2.6 standard deviations, a value which decreases to 2.1 when the same BDT selection is applied. Pseudoexperiments are generated by randomly assigning the flavor and $C_{\hat{T}}$ sign to each candidate. The asymmetries are extracted and the difference between the Run 1 and full datasets is determined as a χ^2 value. The fraction of pseudoexperiments with a χ^2 value greater than the observed χ^2 in data represents the *p*-value.

The *p*-values measured in the case of binning schemes A_1 and B_1 indicate that the *P* violation has a large contribution from the $\Lambda_b^0 \to p a_1(1260)^-$ decay, for which the statistical significance is 5.5 standard deviations.

The *p*-values obtained for different configurations of the energy test are summarized in Table I. All *CP*-violation searches using the energy test result in *p*-values with a significance of 3 standard deviations or smaller. Given the reported *p*-value for the *P*-even configuration of the energy test at a distance scale of 2.7 GeV$^2/c^4$ is marginally consistent with the *CP*-conserving hypothesis, the different distance scales considered are combined to obtain a global *p*-value for the *P*-even configuration. A new test statistic is defined as $Q = p_1 p_2 p_3$, where p_i corresponds to a *p*-value for a distance scale i. The value of Q observed in data is then compared to the corresponding values from permutations, considering correlations between the different distance scales. The combined *p*-value for the *P*-even energy test configuration is 4.6×10^{-3}. In addition, the test for parity violation is also performed using the same three distance scales with the energy test. The results are reported in Table I. The *p*-values found with this study correspond to the observation of local parity violation for the two smaller distance scales probed with the highest significance observed to be 5.3 standard deviations.

In conclusion, this paper reports the searches for *CP* violation in $\Lambda_b^0 \to p\pi^-\pi^+\pi^-$ decays both globally and in regions of phase space, using two different methods.

The results are marginally compatible with the no *CP*-violation hypothesis. Violation of *P* symmetry is observed using both methods, locally with a significance of over 5 standard deviations, and, when the triple product asymmetries are evaluated having integrated over the entire sample, with a significance of 5.5 standard deviations.

APPENDIX: DEFINITION OF THE BINNING SCHEME A

The definition of the binning scheme A is reported in Table II.

TABLE II. Definition of binning scheme A. This binning scheme is based on the helicity angles of the decay topology $\Lambda_b^0 \rightarrow (N^{*+} \rightarrow (\Delta^{++} \rightarrow p\pi^+)\pi^-)\pi^-$ where φ is the azimuthal angle of the proton in the Δ^{++} rest frame and $\theta_{\Delta^{++}}$ (θ_p) is the polar angle of the Δ^{++} (p) in the N^{*+} (Δ^{++}) rest frame.

Bin number	Polar angles	Azimuthal angles
1	$\theta_p \in [0, \pi/4]$ and $\theta_{\Delta^{++}} \in [0, \pi/4]$ $\theta_p \in [\pi/2, 3\pi/4]$ and $\theta_{\Delta^{++}} \in [\pi/2, 3\pi/4]$	$|\varphi| \in [0, \pi/2]$
2	$\theta_p \in [0, \pi/4]$ and $\theta_{\Delta^{++}} \in [\pi/4, \pi/2]$ $\theta_p \in [\pi/2, 3\pi/4]$ and $\theta_{\Delta^{++}} \in [3\pi/4, \pi]$	$|\varphi| \in [0, \pi/2]$
3	$\theta_p \in [0, \pi/4]$ and $\theta_{\Delta^{++}} \in [\pi/2, 3\pi/4]$ $\theta_p \in [\pi/2, 3\pi/4]$ and $\theta_{\Delta^{++}} \in [0, \pi/4]$	$|\varphi| \in [0, \pi/2]$
4	$\theta_p \in [0, \pi/4]$ and $\theta_{\Delta^{++}} \in [3\pi/4, \pi]$ $\theta_p \in [\pi/2, 3\pi/4]$ and $\theta_{\Delta^{++}} \in [\pi/4, \pi/2]$	$|\varphi| \in [0, \pi/2]$
5	$\theta_p \in [\pi/4, \pi/2]$ and $\theta_{\Delta^{++}} \in [0, \pi/4]$ $\theta_p \in [3\pi/4, \pi]$ and $\theta_{\Delta^{++}} \in [\pi/2, 3\pi/4]$	$|\varphi| \in [0, \pi/2]$
6	$\theta_p \in [\pi/4, \pi/2]$ and $\theta_{\Delta^{++}} \in [\pi/4, \pi/2]$ $\theta_p \in [3\pi/4, \pi]$ and $\theta_{\Delta^{++}} \in [3\pi/4, \pi]$	$|\varphi| \in [0, \pi/2]$
7	$\theta_p \in [\pi/4, \pi/2]$ and $\theta_{\Delta^{++}} \in [\pi/2, 3\pi/4]$ $\theta_p \in [3\pi/4, \pi]$ and $\theta_{\Delta^{++}} \in [0, \pi/4]$	$|\varphi| \in [0, \pi/2]$
8	$\theta_p \in [\pi/4, \pi/2]$ and $\theta_{\Delta^{++}} \in [3\pi/4, \pi]$ $\theta_p \in [3\pi/4, \pi]$ and $\theta_{\Delta^{++}} \in [\pi/4, \pi/2]$	$|\varphi| \in [0, \pi/2]$
9	$\theta_p \in [0, \pi/4]$ and $\theta_{\Delta^{++}} \in [0, \pi/4]$ $\theta_p \in [\pi/2, 3\pi/4]$ and $\theta_{\Delta^{++}} \in [\pi/2, 3\pi/4]$	$|\varphi| \in [\pi/2, \pi]$
10	$\theta_p \in [0, \pi/4]$ and $\theta_{\Delta^{++}} \in [\pi/4, \pi/2]$ $\theta_p \in [\pi/2, 3\pi/4]$ and $\theta_{\Delta^{++}} \in [3\pi/4, \pi]$	$|\varphi| \in [\pi/2, \pi]$
11	$\theta_p \in [0, \pi/4]$ and $\theta_{\Delta^{++}} \in [\pi/2, 3\pi/4]$ $\theta_p \in [\pi/2, 3\pi/4]$ and $\theta_{\Delta^{++}} \in [0, \pi/4]$	$|\varphi| \in [\pi/2, \pi]$
12	$\theta_p \in [0, \pi/4]$ and $\theta_{\Delta^{++}} \in [3\pi/4, \pi]$ $\theta_p \in [\pi/2, 3\pi/4]$ and $\theta_{\Delta^{++}} \in [\pi/4, \pi/2]$	$|\varphi| \in [\pi/2, \pi]$
13	$\theta_p \in [\pi/4, \pi/2]$ and $\theta_{\Delta^{++}} \in [0, \pi/4]$ $\theta_p \in [3\pi/4, \pi]$ and $\theta_{\Delta^{++}} \in [\pi/2, 3\pi/4]$	$|\varphi| \in [\pi/2, \pi]$
14	$\theta_p \in [\pi/4, \pi/2]$ and $\theta_{\Delta^{++}} \in [\pi/4, \pi/2]$ $\theta_p \in [3\pi/4, \pi]$ and $\theta_{\Delta^{++}} \in [3\pi/4, \pi]$	$|\varphi| \in [\pi/2, \pi]$
15	$\theta_p \in [\pi/4, \pi/2]$ and $\theta_{\Delta^{++}} \in [\pi/2, 3\pi/4]$ $\theta_p \in [3\pi/4, \pi]$ and $\theta_{\Delta^{++}} \in [0, \pi/4]$	$|\varphi| \in [\pi/2, \pi]$
16	$\theta_p \in [\pi/4, \pi/2]$ and $\theta_{\Delta^{++}} \in [3\pi/4, \pi]$ $\theta_p \in [3\pi/4, \pi]$ and $\theta_{\Delta^{++}} \in [\pi/4, \pi/2]$	$|\varphi| \in [\pi/2, \pi]$

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