

# Higher-order corrections on diboson production processes with MATRIX

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**Stefan Kallweit\***, **Marius Wiesemann**

*TH Division, Physics Department, CERN,  
CH-1211 Geneva 23, Switzerland*

*E-mail: [stefan.kallweit@cern.ch](mailto:stefan.kallweit@cern.ch), [marius.wiesemann@cern.ch](mailto:marius.wiesemann@cern.ch)*

**Massimiliano Grazzini**

*Physics Department, University of Zürich,  
Winterthurerstrasse 190, CH-8057 Zürich, Switzerland*

*E-mail: [grazzini@physik.uzh.ch](mailto:grazzini@physik.uzh.ch)*

We review the calculations of the next-to-next-to-leading order (NNLO) QCD corrections to vector-boson pair production processes in proton–proton collisions and their implementation in the computational framework MATRIX [1, 2], which has been publicly released recently. Our calculations include the leptonic decays of  $W$  and  $Z$  bosons, consistently taking into account spin correlations, off-shell effects and non-resonant contributions. We present inclusive cross sections for the production of massive vector-boson pairs, applying the respective mass windows chosen by ATLAS and CMS to define  $Z$  bosons from their leptonic decay products, as well as total cross sections for stable bosons. Moreover, we show some examples of differential distributions in fiducial phase-space regions inspired by typical selection cuts used by the LHC experiments. For the vast majority of measurements, the inclusion of NNLO corrections significantly improves the agreement of the Standard Model predictions with data.

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\*Speaker.

## 1. Introduction

Vector-boson pair production at the Large Hadron Collider (LHC) provides an important test of the electroweak (EW) sector of the Standard Model (SM) at the TeV scale. As these processes are sensitive to the gauge-boson self-interactions, any small deviation in observed rates or in kinematical distributions could give a hint towards new physics, which can be modelled through anomalous couplings. Vector-boson pair production processes also constitute backgrounds in many direct new-physics searches, and, in Higgs-boson studies, the neutral final states represent irreducible backgrounds in the respective decay channels  $H \rightarrow ZZ/W^+W^-/Z\gamma$ .

In this contribution, we give an overview of the applications of the framework MATRIX[1, 2] to vector-boson pair production processes at NNLO QCD accuracy. Besides a summary of the most relevant phenomenological results for the inclusive cross sections and distributions, we discuss the implementation of automated  $q_T$  subtraction (and resummation) for both the quark- and gluon-induced production of colour singlets and review the status as well as the capabilities of the code.

## 2. NNLO corrections through automated $q_T$ subtraction

The cancellation of singularities across the various IR-divergent contributions, located in phase-spaces with different parton multiplicities, is a highly non-trivial task in an NNLO computation. Suitable subtraction schemes have been devised to deal with the additional complications arising at NNLO with respect to next-to-leading order (NLO). In order to achieve automation in a numerical code, such schemes must fulfill certain requirements: Firstly, they should cover a reasonable number of applicable processes; their formulation must be unspecific to the process; the procedure must be sufficiently simple to render a numerical implementation feasible; their numerical convergence may not exceed the limits set by the current technological status of computers/clusters. All these features perfectly apply to the  $q_T$ -subtraction formalism.

At variance with the fully local subtraction methods, such as antenna subtraction [3, 4, 5, 6], colourful subtraction [7, 8, 9], and residue-improved sector decomposition [10, 11, 12, 13],  $q_T$  subtraction corresponds to a non-local subtraction scheme.<sup>1</sup> It starts from an NLO calculation with one additional parton (jet) in the final state, making use of the highly sophisticated automation and numerical control we have by now on the computation of NLO cross sections, and devises suitable subtractions of the remaining logarithmic divergences in  $q_T$  to render the cross section finite at NNLO QCD accuracy.

The  $q_T$ -subtraction formalism [16] deals with the production of an arbitrary number of colour singlets<sup>2</sup> at hadron colliders. Denoting the system of colourless final states by  $F$ , the  $pp \rightarrow F + X$  cross section at (N)NLO in this framework can be written as

$$d\sigma_{(N)\text{NLO}}^F = \left[ d\sigma_{(N)\text{LO}}^{F+\text{jet}} - d\sigma_{(N)\text{NLO}}^{\text{CT}} \right] + \mathcal{H}_{(N)\text{NLO}}^F \otimes d\sigma_{\text{LO}}^F. \quad (2.1)$$

<sup>1</sup> $N$ -jettiness subtraction [14, 15], which extends the basic idea of  $q_T$  subtraction to processes including light partons at the leading order by using the  $N$ -jettiness observable instead of the transverse momentum of the colourless system, also belongs to the class of non-local subtraction schemes.

<sup>2</sup>The extension to heavy-quark production has been discussed in Ref. [17].

The term  $d\sigma_{(N)\text{LO}}^{F+\text{jet}}$  represents the cross section for the production of the system  $F$  plus one jet at (N)LO accuracy. The counterterm  $d\sigma_{(N)\text{NLO}}^{\text{CT}}$  is obtained from the fixed-order expansion of the resummation formula for logarithmically enhanced contributions at small transverse momenta [18] and guarantees the cancellation of the remaining IR divergences of the  $F$ +jet cross section. The hard-collinear coefficient  $\mathcal{H}_{(N)\text{NLO}}^F$  is a perturbative function in  $\alpha_s$ , whose general structure is known at NLO [19] and NNLO [20].<sup>3</sup>  $\mathcal{H}_{(N)\text{NLO}}^F$  entails the one-loop (and two-loop) virtual corrections to the Born-level process and compensates for the subtraction of  $d\sigma_{(N)\text{NLO}}^{\text{CT}}$ . The last term of Eq. (2.1) therefore adds all the contributions missing at vanishing transverse momentum of  $F$  to obtain full (N)NLO QCD accuracy.

In the same framework automated transverse-momentum resummation of the colourless system is obtained by replacing the last term of Eq. (2.1) by the suitable small- $p_T$  resummation formula of Ref. [18]. The latter is independent of the respective process apart from the inclusion of the  $\mathcal{H}_{(N)\text{NLO}}^F$  coefficient, whose process dependence is fully determined by the loop corrections to the Born-level process.

### 3. The MATRIX code

MATRIX[1, 2]<sup>4</sup> is a computational framework based on the Monte Carlo program MUNICH<sup>5</sup>, interfaced with the OPENLOOPS<sup>6</sup> generator of one-loop scattering amplitudes [23], and includes an automated implementation of  $q_T$  subtraction and resummation, as introduced in the previous section. This widely automated framework is limited only by the two-loop amplitudes entering  $\mathcal{H}_{\text{NNLO}}^F$  in Eq. (2.1). MATRIX has already been used, in combination with the two-loop scattering amplitudes of Refs. [24, 25], for the calculations of  $Z\gamma$  [26, 27],  $W^\pm\gamma$  [27],  $ZZ$  [28, 29],  $W^+W^-$  [30, 31],  $W^\pm Z$  [32, 33] and  $HH$  [34] production at NNLO QCD as well as in the resummed computations of the  $ZZ$  and  $W^+W^-$  transverse-momentum spectra [35] at NNLL+NNLO.

After a closed beta phase, where the MATRIX code was already extensively used by several experimental groups for direct physics applications, a first public version of MATRIX has been released recently [1]. This first public release features calculations at NNLO QCD accuracy for a large number of single-boson and boson-pair production processes, as listed in Tab. 1. The code is engineered in a very user-friendly way that guides you from the very first execution of MATRIX to the very end of a run of a specific process. Details on the usage of MATRIX are given in Ref. [2] and in the manual shipped with the code.

### 4. Results

All calculations reviewed in this article have been carried out in the MATRIX framework introduced in the previous section.

<sup>3</sup>The latter exploits the explicit NNLO results for Higgs [21] and vector-boson [22] production.

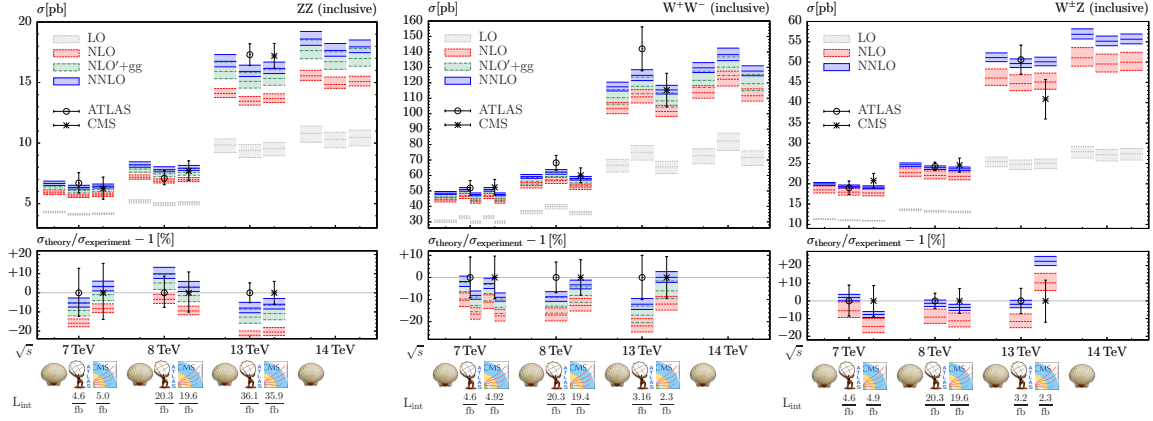
<sup>4</sup>MATRIX is the abbreviation of “MUNICH Automates  $q_T$  subtraction and Resummation to Integrate X-sections”, by M. Grazzini, S. Kallweit, and M. Wiesemann.

<sup>5</sup>MUNICH is the abbreviation of “MULti-chaNnel Integrator at Swiss (CH) precision”—an automated parton level NLO generator by S. Kallweit. In preparation.

<sup>6</sup>The OPENLOOPS one-loop generator, by F. Cascioli, J. Lindert, P. Maierhöfer, and S. Pozzorini, is publicly available at <http://openloops.hepforge.org>.

ID	process	description
pph21	$pp \rightarrow H$	on-shell Higgs boson production
ppz01	$pp \rightarrow Z$	on-shell Z production
ppw01	$pp \rightarrow W^-$	on-shell $W^-$ production with CKM
ppwx01	$pp \rightarrow W^+$	on-shell $W^+$ production with CKM
ppeex02	$pp \rightarrow e^- e^+$	Z production with decay
ppnenex02	$pp \rightarrow \nu_e \bar{\nu}_e$	Z production with decay
ppenex02	$pp \rightarrow e^- \bar{\nu}_e$	$W^-$ production with decay and CKM
ppexne02	$pp \rightarrow e^+ \nu_e$	$W^+$ production with decay and CKM
ppaa02	$pp \rightarrow \gamma\gamma$	on-shell $\gamma\gamma$ production
ppeexa03	$pp \rightarrow e^- e^+ \gamma$	$Z\gamma$ production with decay
ppnenexa03	$pp \rightarrow \nu_e \bar{\nu}_e \gamma$	$Z\gamma$ production with decay
ppenexa03	$pp \rightarrow e^- \bar{\nu}_e \gamma$	$W^- \gamma$ with decay
ppexnea03	$pp \rightarrow e^+ \nu_e \gamma$	$W^+ \gamma$ with decay
ppzz02	$pp \rightarrow ZZ$	on-shell ZZ production
ppwxw02	$pp \rightarrow W^+ W^-$	on-shell $W^+ W^-$ production
ppemexmx04	$pp \rightarrow e^- \mu^- e^+ \mu^+$	ZZ production with decay
ppeeeex04	$pp \rightarrow e^- e^- e^+ e^+$	ZZ production with decay
ppeexnmnm04	$pp \rightarrow e^- e^+ \nu_\mu \bar{\nu}_\mu$	ZZ production with decay
ppemxnmnex04	$pp \rightarrow e^- \mu^+ \nu_\mu \bar{\nu}_e$	$W^+ W^-$ production with decay
ppeexnenex04	$pp \rightarrow e^- e^+ \nu_e \bar{\nu}_e$	ZZ / $W^+ W^-$ production with decay
ppemexnm04	$pp \rightarrow e^- \mu^- e^+ \bar{\nu}_\mu$	$W^- Z$ production with decay
ppeeexnex04	$pp \rightarrow e^- e^- e^+ \bar{\nu}_e$	$W^- Z$ production with decay
ppeexmxnm04	$pp \rightarrow e^- e^+ \mu^+ \nu_\mu$	$W^+ Z$ production with decay
ppeexexne04	$pp \rightarrow e^- e^+ e^+ \nu_e$	$W^+ Z$ production with decay

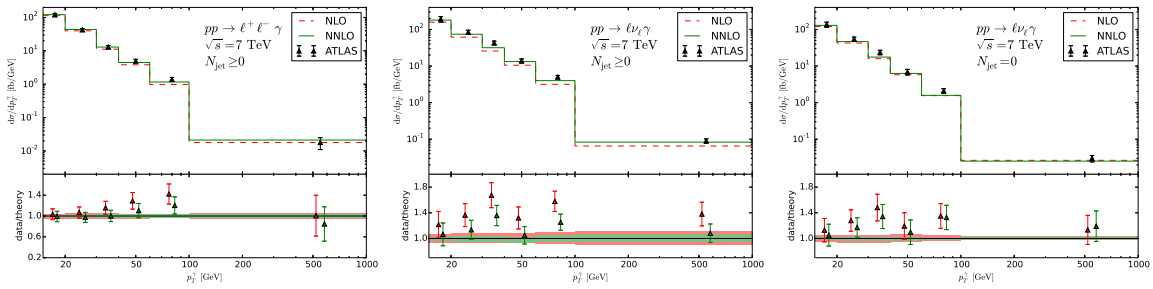
**Table 1:** Processes available in the first MATRIX release.



**Figure 1:** Total cross sections at LO, NLO, NLO' +  $gg$  (NLO plus loop-induced  $gg$  contribution, evaluated with NNLO PDFs) and NNLO for  $ZZ$  (left),  $W^+W^-$  (center) and  $W^\pm Z$  (right) production, with uncertainties from conventional 7-point scale variations, are shown and compared to experimental results from ATLAS and CMS, where available. For each collider energy, the left column refers to cross sections evaluated with on-shell  $W$  and/or  $Z$  bosons, while the second (third) column gives fully inclusive off-shell results for four-lepton final states, corrected for their branching ratios, with only mass-window cuts corresponding to the respective ATLAS (CMS) analyses applied. In case of  $W^+W^-$  production, the  $H \rightarrow WW^*$  production cross section predicted in NNLO QCD (from Ref. [31]) is added to the ATLAS predictions for  $\sqrt{s} = 8, 13$  and  $14$  TeV, but not to the CMS predictions, in line with the published experimental setups. At  $\sqrt{s} = 7$  TeV results both with (left) and without (right) the Higgs-mediated contribution are shown.

In Figure 1 we provide predictions for the inclusive  $ZZ$ ,  $W^+W^-$  and  $W^\pm Z$  cross sections at different orders in QCD perturbation theory for the relevant centre-of-mass energies. All these results are calculated with NNPDF3.0 parton distribution functions (PDFs) [36], and compared to the cross sections determined by ATLAS and CMS from their respective measurements. Our findings are briefly discussed in Sections 4.2–4.4. The histograms in Figures 2–5 are taken from the original publications and thus use the respective input parameters as specified therein.

#### 4.1 Fiducial cross sections and differential distributions for $Z\gamma$ and $W^\pm\gamma$ production

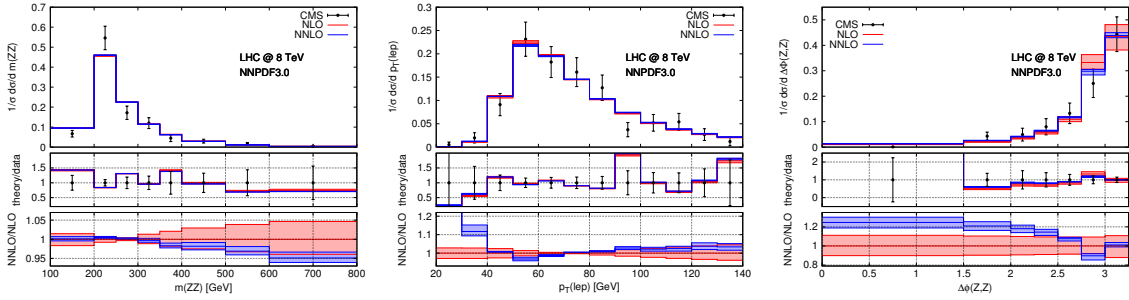


**Figure 2:** Distributions in the transverse momentum of the photon in  $Z\gamma$  production (left), and in  $W^\pm\gamma$  production without (center) and with (right) a jet veto applied are shown, and compared to ATLAS data [37].

Measurements of  $V\gamma$  final states have been carried out by ATLAS and CMS using the data sets at centre-of-mass energies of 7 TeV [37, 38, 39] and 8 TeV [40, 41]. Due to the massless photon in the final state, a total cross section cannot be defined. Instead, we investigate cross sections in the fiducial phase-space regions chosen by the experiments (see Refs. [26, 27]). The higher-

order corrections for  $W^\pm\gamma$  are significantly larger than those for  $Z\gamma$ : This can be traced back to a suppression of the  $W^\pm\gamma$  Born contributions due to a *radiation zero* [42], which is broken only beyond leading order (LO). The loop-induced gluon–gluon contribution to  $Z\gamma$  production amounts to only about 10% of the  $\mathcal{O}(\alpha_s^2)$  corrections. We find significantly larger corrections if the applied selection cuts suppress resonant configurations with the photon emitted from the final-state leptons in Born kinematics. As expected, a jet veto results in a serious reduction of the higher-order effects. The agreement with experimental data is significantly improved, in particular for inclusive  $W^\pm\gamma$  production. Figure 2 illustrates these findings by means of the transverse-momentum distribution of the photon in  $Z\gamma$  and  $W^\pm\gamma$  production.

#### 4.2 Inclusive cross sections and normalized differential distributions for $ZZ$ production

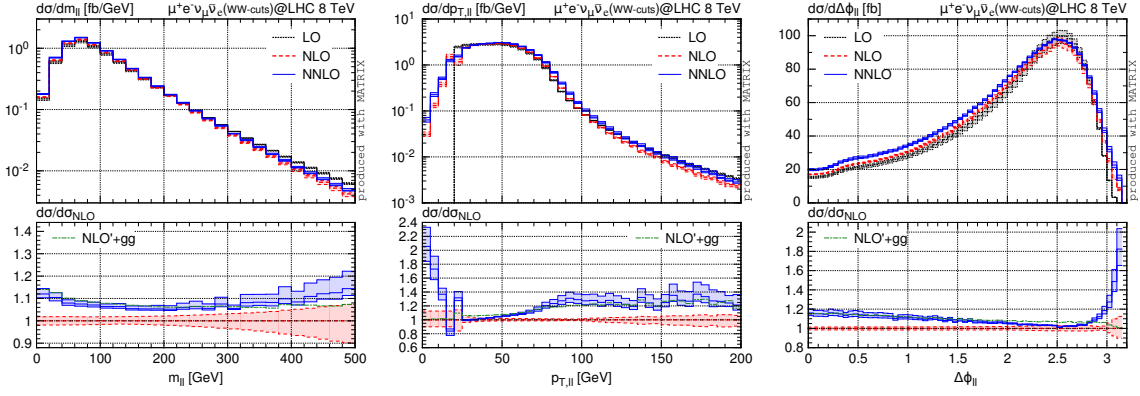


**Figure 3:** Normalized distributions in the four-lepton invariant mass (left), the leading-lepton  $p_T$  (center) and the azimuthal angle between the two reconstructed  $Z$  bosons (right) are shown, and compared to CMS data [43].

Various measurements of  $ZZ$  hadroproduction in the leptonic decay channel have been carried out at the LHC by both ATLAS and CMS at centre-of-mass energies of 7 TeV [44, 45], 8 TeV [46, 43, 47] and 13 TeV [48, 49, 50, 51], which are in good agreement with NNLO QCD predictions. With typical definitions of fiducial phase-space regions, the higher-order corrections within fiducial cuts [29] mimic those ones found for the fully inclusive results [28] (see Figure 1). The loop-induced gluon–gluon contribution amounts to about 60% of the full  $\mathcal{O}(\alpha_s^2)$  corrections. In Figure 3 we show normalized distributions in the four-lepton invariant mass, the leading-lepton  $p_T$  and the azimuthal angle between the two reconstructed  $Z$  bosons, compared to CMS data [43]. Due to the large experimental uncertainties, a slightly improved shape agreement can be found only for the last one, which is non-trivial only beyond LO, and thus more affected by the NNLO corrections. Further distributions produced with MATRIX are compared to ATLAS 13 TeV data in Ref. [49] and CMS 13 TeV data in Ref. [51], and good agreement is found in the phase-space regions where fixed-order calculations are predictive.

#### 4.3 Inclusive cross sections and differential distributions for $W^+W^-$ production

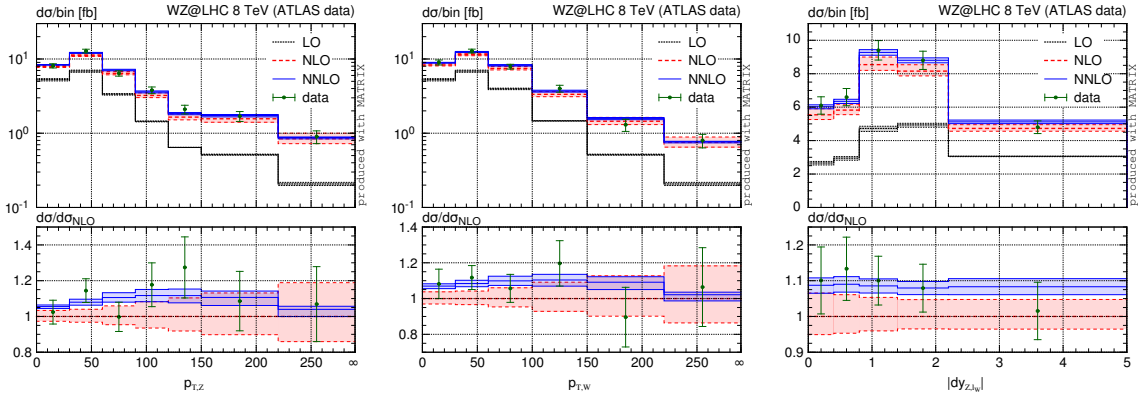
The  $W^+W^-$  cross section has been measured at the LHC by both ATLAS and CMS at centre-of-mass energies of 7 TeV [53, 54], 8 TeV [52, 55, 56] and 13 TeV [57, 58], agreeing well with the respective SM predictions at NNLO QCD accuracy. In order to suppress the enormous background from top-quark pairs, typical fiducial cuts imply a jet veto. Consequently, higher-order effects



**Figure 4:** Distributions in the dilepton invariant mass (left), the  $p_T$  of the dilepton system (center) and the azimuthal angle between the two leptons (right) are shown. The applied phase-space cuts are inspired by the ATLAS analysis [52], but we do not apply any lepton-isolation criteria with respect to hadronic activity.

are quite different for inclusive results [30] (see Figure 1) and predictions within fiducial phase-space regions [31]: Whereas the loop-induced gluon–gluon contribution amounts to only about one third of the  $\mathcal{O}(\alpha_s^2)$  effects in the inclusive case, it dominates if a jet veto is applied, and the genuine corrections to the  $q\bar{q}$  channel become even negative. In Figure 4 we show distributions in the dilepton invariant mass, the  $p_T$  of the dilepton system and the azimuthal angle between the two leptons. By and large the  $\text{NLO}' + gg$  approximation, which was considered the best prediction before full NNLO results were known, reproduces the NNLO result quite well. However, we find shape distortions of up to about 10% throughout. In phase-space regions that imply the presence of QCD radiation,  $\text{NLO}' + gg$  cannot approximate the shapes of full NNLO corrections.

#### 4.4 Inclusive cross sections and differential distributions for $W^\pm Z$ production



**Figure 5:** Distributions in the transverse momenta of the reconstructed Z (left) and W (center) bosons and the absolute rapidity separation between the reconstructed Z boson and the lepton from the W-boson decay (right) are shown and compared to ATLAS data [59].

The inclusive  $W^\pm Z$  cross section has been measured with good precision at the LHC by ATLAS and CMS at centre-of-mass energies of 7 TeV [60, 61] and 8 TeV [59, 61]. Also early measurements at 13 TeV [62, 63, 64] by ATLAS and CMS are already available. The agreement with theory predictions is significantly improved by including the recently calculated NNLO corrections [32]

(see Figure 1), in particular for LHC Run 1 data. As for  $W^\pm\gamma$  production, the large corrections are explained by a *radiation zero* [65], here in the leading helicity amplitudes at Born level, which is overcome only beyond LO. In Figure 5 we show some sample distributions calculated at NNLO QCD accuracy with MATRIX in Ref. [33], compared to the corresponding measurement by ATLAS at 8 TeV [59]. We find significantly reduced scale-variation uncertainties at the NNLO compared to NLO, and typically the agreement between theory and data is improved, mainly driven by the overall normalization though.

## 5. Summary

In this article, we have presented the current status of the MATRIX code, which allows for the computation of NNLO QCD corrections to a number of colour-singlet production processes with one or two Higgs and vector bosons in the final state. The most relevant physics results obtained with this code for vector-boson pair production processes have been summarized by presenting both total cross sections and distributions in the fiducial phase spaces. By and large, the NNLO corrections significantly improve the agreement with the experimental measurements.

A first public version of MATRIX [1, 2] has been released recently. Besides the inclusion of resummation at small transverse momenta through NNLL for all the available colour-singlet processes, which is currently under validation, further developments are possible: These involve the inclusion of electroweak corrections, higher-order corrections to the gluon-induced channels, and the extension of the code to deal with coloured final states.

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