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# by Resonant Depolarization Accurate Determination of the LEP Beam Energy

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#### Abstract

explanations for the changes of the beam energy during the year will be described. up to 20 MeV. Results from the energy calibrations will be presented and possible evolution of the beam energies in the course of the year showed a large variation of and a regular tracking of the beam energies throughout the scan was possible. The tegrated luminosity was recorded in calibrated fills below and above the resonance accuracy of each calibration is better than 1 MeV. About one third of the total in energies. 24 energy calibrations were performed at the end of physics fills. The tion by resonant depolarization was successfully commissioned for all three beam points roughly 880 MeV below and above the peak. Operational energy calibra beam energy scan, with one point close to the peak of the Z resonance and two 1993 Large Electron Positron Collider (LEP) run was devoted to a three point To improve the measurements of the Z boson mass and resonance width, the

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 $\label{eq:2.1} \mathcal{L}(\mathbf{r}) = \mathcal{L}(\mathbf{r}) \left[ \mathcal{L}(\mathbf{r}) \right] \mathcal{L}(\mathbf{r}) = \mathcal{L}(\mathbf{r}) \mathcal{L}(\mathbf{r})$ 

 $\sim 10$ 

 $\mathcal{L}^{\text{max}}_{\text{max}}$ 

## 1 Introduction

scan. errors due to a better knowledge of the LEP beam energy compared to the 1991 LEP energy measurements of the Z mass and resonance width, with a significant reduction of the systematic resonant depolarization, the 1993 LEP run was devoted to a 3 point energy scan to improve the the end of 1992 it was possible to envisage a continuous monitoring of the beam energy using energy scale of LEP was reduced to 6 MeV for the 1991 LEP energy scan [4, 5]. Since by a result the systematic error on the mass of the Z boson due to the knowledge of the absolute polarized beams and to implement energy calibration by resonant depolarization [1, 2, 3]. As Between 1990 and 1992 extensive studies were performed at LEP to establish transversely

calibration in LEP are published elsewhere derstanding of depolarizing effects. The procedures to establish polarized beams for energy fills thanks to the spin compensation of the experimental solenoids [13] and an improved un points for the 1993 scan. Transversely polarized beams were obtained at the end of physics Harmonic Spin Matching [12] allowed to establish transverse polarization on all three energy and the beam orbit monitors [10, 11] as well as the successful implementation of deterministic Improvements on the LEP polarimeter  $[6, 7, 8]$ , the vertical alignment of the quadrupoles  $[9]$ 

first test measurement of the positron energy was obtained. dumped for the calibrations, two vertically separated beams were kept during the last week. A variations were studied in parallel to energy calibration. While usually the positron beam was 5% of the total running time. Systematic effects of the spin dynamics and of the beam energy successfully performed on the electron beams at the end of physics fills, using approximately During the 1993 energy scan which lasted from July to November, 24 calibrations were

1993. parameters that affect the beam energy and the evolution of the beam energy during the year We report here on the energy calibration procedure and its accuracy, the measurement of

## 2 Principle of energy calibration by resonant depolarization

bration by resonant depolarization.<br>The motion of the spin vector  $\vec{S}$  of a relativistic electron in electromagnetic fields  $\vec{E}$  and  $\vec{B}$ calibration by resonant depolarization. than that provided by other existing methods  $[5]$ . We will first describe the principle of energy average beam energy. The attainable precision is more than one order of magnitude better Transverse beam polarization in LEP opens the possibility for accurate measurements of the

is described by the Thomas—BMT equation [14] :

$$
\frac{d\vec{S}}{dt} = \vec{\Omega}_{\text{BMT}} \times \vec{S}
$$

(2) 
$$
\vec{\Omega}_{\text{BMT}} = -\frac{e}{\gamma m} \left[ (1 + a\gamma) \vec{B}_{\perp} + (1 + a) \vec{B}_{\parallel} - \left( a\gamma + \frac{\gamma}{1 + \gamma} \right) \vec{\beta} \times \frac{\vec{E}}{c} \right]
$$

anomaly and  $\gamma$  the Lorentz factor of the electron. with respect to the particle's velocity  $\vec{\beta}c$ . e is the charge, m the mass, a the magnetic moment where  $\vec{B}_{\perp}$  and  $\vec{B}_{||}$  are the components of the magnetic field which are transverse and parallel



polarization vector is resonantly rotated away from the vertical direction. perturbation is in phase with the nominal spin precession (in this example  $f_{dep} = 0.5 \cdot f_{rev}$ ) the along the vertical direction. After being tilted  $\vec{P}$  precesses with  $\nu$  about its initial direction. If the perturbation  $\int b_z l$  from the RF-magnet. In an ideal storage ring the polarization vector is initially Figure 1: Resonance condition between the nominal spin precession with  $|\nu| = 0.5$  and the radial

energy  $E[15]$ : the spin tune. Its average value  $\nu$  for all electrons is directly proportional to the average beam particle will precess  $a\gamma$  times for one revolution in the storage ring, where the term  $a\gamma$  is called comparison of  $\Omega_c$  with the spin precession frequency  $\Omega_{\text{BMT}}$  shows that the spin vector of a of the particles in the storage ring is given by the cyclotron frequency  $\Omega_c = -(e/\gamma m)B_y$ . The produce vertical fields  $B_y$  and maintain the particles on circular orbits. The precession frequency The strongest magnetic fields in a storage ring arise from the dipole bending magnets, which

(3) 
$$
\nu = a\gamma = \frac{aE}{mc^2} = \frac{E[\text{MeV}]}{440.6486(1)[\text{MeV}]}
$$

be beam energies and not center-of-mass energies at the interaction points. discussed later. Throughout this report, if not otherwise stated, all energies are understood to This relation is exact only for ideal storage rings. Its limitations due to imperfections will be

perturbs the spin precession. of 92.4% [16]. Any radial magnetic field reduces the equilibrium degree of polarization and vector  $\vec{P}$ . Due to the Sokolov-Ternov effect vertical polarization can build up to a maximum spin vectors is conserved. The ensemble average of all spin vectors is defined as the polarization In an  $e^+e^-$  storage ring with purely vertical magnetic fields the vertical component of the

phase with the spin precession, the spin rotations about the radial direction add up coherently of the particle trajectories is  $\nu$  times smaller. If the perturbation from the RF-magnet is in  $2 \cdot 10^{-4}$  Tm is used to rotate the spin by 140  $\mu$ rad about the radial direction. The deflection the spin precession frequency at LEP. In standard conditions a radial field strength  $\int b_x l =$ An oscillating radial field from an RF-magnet is used for the resonant measurement of



flips to negative polarization were observed and checked by flipping them again. spin tune. The observed depolarizations locate the fractional spin tune close to 0.477. Partial spin with dotted lines. The frequency limits are indicated on top of the picture for each scan in units of measure the non-integer part of the spin tune. Frequency scans with the depolarizer are indicated Figure 2: Example of energy calibration by resonant depolarization. Several bunches are used to

frequency  $f_{\text{dep}}$  is in resonance with the spin precession if : and the beam polarization can only partially be flipped. The RF—magnet field oscillating at a radiation in  $e^+e^-$  storage rings, the horizontal component of the polarization vector is unstable into the horizontal plane, or twice as much to flip its direction. Due to stochastic synchrotron from turn to turn. About  $10^4$  turns ( $\approx$  1 second) are needed to turn the polarization vector

$$
(4) \t f_{\text{dep}} = (k \pm [\nu]) \cdot f_{\text{rev}}
$$

Because the polarization vector is the ensemble average over all spin vectors, the measured beam determined and not the beam energy of individual particles at the location of the RF-magnet. to notice that it is the precession frequency of the polarization vector over one turn which is energy calibrations and measurements of particle masses [17, 18, 19, 20, 21, 22]. lt is important energy calibration by resonant depolarization and has been used extensively for accurate beam the average beam energy  $E$  is obtained from equation 3. This method is often referred to as spin tune  $\nu = [\nu] + n$  can then be calculated with equation 4 from the measured  $f_{\text{dep}}$  and for  $[\nu] = 0.5$  in figure 1. The frequency  $f_{\text{dep}}$  is varied until a depolarization is observed. The  $0$  ( $f_{\text{dep}} = [\nu] \cdot f_{\text{rev}}$ ) or  $k = +1$  ( $f_{\text{dep}} = (1 - [\nu]) \cdot f_{\text{rev}}$ ). The resonance condition is illustrated the setting of the bending field. The frequencies  $f_{\text{dep}}$  used at LEP correspond to the cases  $k =$ integer.  $[\nu]$  denotes the non-integer part of the spin tune. Its integer part n is determined from where  $f_{rev}$  is the revolution frequency of the particles ( $f_{rev} = 11.25$  kHz at LEP) and k is an



energy and the synchrotron tune. mined uniquely by changing the beam energy can however always be deter Mirror on  $[1, Q_s]$  sideband resonances can appear  $= 0.0625$ . Depending on the value of ent central spin tunes in the case  $Q_i$ ,  $|1 - [v]$  onances are indicated for two differ- $\text{tune } [\mathbf{v}] = 0.48$   $\text{tiven } \mathbf{v}$  :  $\text{tivotron satellites and the mirror res-$ 

phase advance over one complete turn. They do not however bias the measured beam energy which is determined from the total spin at 45 GeV). Local energy variations like the energy sawtooth modify the spin phase advance. the individual particles and is not limited in accuracy by the LEP beam energy spread (35 MeV energy is to a very good approximation independent of betatron and synchrotron oscillations of

unchanged. Several partial spin flips are observed on different bunches. A single bunch can be depolarized selectively leaving the polarization of all other bunches shows an example of energy calibration where the fractional spin tune is located close to 0.477.  $\sigma_{\nu} = \Delta \nu_{\rm scan}/\sqrt{12}$ . On some occasions a resolution of  $\Delta \nu_{\rm scan} = 0.0005$  was achieved. Figure 2 Since the spin tune is not localized inside the frequency scan, the RMS error on  $\nu$  is given by corresponds to  $\Delta f_{dep} = 22.2$  Hz and to an accuracy on the energy of  $\Delta E_{scan} = 0.88$  MeV. of the spin tune measurement. For standard calibrations  $\Delta \nu_{\rm scan}$  could be set to 0.002 which range. The width  $\Delta f_{dep}$  of the frequency "scan" determines in practice the resolution  $\Delta \nu_{scan}$ Experimentally the frequency of the RF-magnet field is slowly varied with time over a given

shown in figure 3 for two different spin tunes  $\nu$ . of the synchrotron tune  $Q_{\rm s}$ . The locations of synchrotron satellites and mirror resonances are main resonance  $\nu$  can be separated from the satellites  $\nu_{side}$  because it is not shifted by a change can also occur on synchrotron satellites which appear at spin tunes of  $\nu_{side} = \nu \pm Q_s$ . The the magnetic set up the beam energy is varied by changing the RF frequency. Depolarization the beam energy is varied and the corresponding change of  $f_{dep}$  is measured. To avoid modifying spin tune  $[\nu]$  is compatible with a mirrored spin tune of  $1-[\nu]$ . To solve this mirror ambiguity a single energy calibration cannot resolve all ambiguities. A measured non-integer part of the Two additional measurements are required to uniquely determine the beam energy because

## 3 Energy calibration accuracy

larization for LEP. We now discuss the limitations and systematic errors of energy calibration by resonant depo

#### 3.1 Electron mass and magnetic moment anomaly

small enough that it can be neglected. The uncertainty on the electron magnetic moment anomaly [15]  $a = 1.159652193(10) \cdot 10^{-3}$  is on the accuracy of the method. This limit corresponds to a relative error of  $\Delta E/E = 3 \cdot 10^{-7}$ . The measurement of the electron mass [15]  $m = 0.51099906(15)$  MeV sets a fundamental limit

#### 3.2 Revolution frequency

 $10^{-10}$  which can be neglected.  $f_{\rm rev}$  of the particles must be known. The uncertainty in  $f_{\rm rev}$  introduces a relative error  $\Delta E / E =$ To convert the measured spin precession frequency into a spin tune the revolution frequency

#### 3.3 Frequency of the RF-magnet

of 2 Hz corresponding to  $\Delta E/E = 2 \cdot 10^{-6}$ .  $\Delta E/E = 2 \cdot 10^{-8}$ . Experimentally the setting of the frequency was verified with an accuracy Since the spin precession frequency is of the order of 1.1 MHz this leads to an uncertainty of cording to the instrument specifications  $f_{dep}$  is generated with an accuracy of  $25 \cdot 10^{-3}$  Hz. The frequency  $f_{dep}$  of the RF-magnet is produced with a synthesized function generator. Ac-

#### 3.4 Width of the excited spin resonance

slope of spin tune change with time  $\Delta \nu_{\rm scan}/\Delta t$  were considered. polarization  $P_{\text{final}}/P_{\text{initial}}$  was measured as a function of spin tune. Two different cases for the spin tune. The standard strength of the RF-magnet  $(2\cdot10^{-4}$  Tm) was used and the change in tune as  $\Delta\nu_{\rm scan}/\Delta t$ .  $\epsilon$  was explicitly measured with a reduced bin width  $\Delta\nu_{\rm scan}$  of 0.0005 in and on the frequency change of the RF-magnet field with time, which can be expressed in spin flipped. The width  $\epsilon$  of the excited spin resonance depends on the strength of the RF-magnet spin resonance the polarization vector is rotated and the polarization is destroyed or partially at a known location in spin tune. If the spin tune of the particles is inside the width of this The perturbation from the RF-magnet can be considered as an artificial spin resonance excited

remarkable when it is compared to the beam energy spread of about 35 MeV. energy calibration. The FWHM of the resonance is 0.2 MeV. This small width is especially Case (a) in figure 4 was measured with the same parameters that are used for a standard

increases to 0.8 MeV. time than for case  $(a)$ . This leads to a stronger excitation of the spin resonance whose FWHM perturbation from the RF-magnet was in phase with the precessing spin vectors for a longer Case (b) in figure 4 was measured with a slope  $\Delta\nu_{\rm scan}/\Delta t$  4 times smaller than case (a). The

ple approach we use it for electrons by adding a term  $e^{-T/\tau_{decoh}}$ , assuming that the effects of Their calculation is only valid for a single particle without synchrotron radiation. In a sim larization  $P_{\text{final}}/P_{\text{initial}}$  has been calculated from a formula obtained by Froissart and Stora [23]. From  $\Delta\nu_{\rm scan}/\Delta t$  and the measured width  $\epsilon$  of the excited spin resonance the change of po-



tings). (a)  $\Delta \nu_{scan}/\Delta t = 1.67 \cdot 10^{-4}s^{-1}$  (standard set (b)  $\Delta \nu_{scan}/\Delta t = 4.17 \cdot 10^{-5}s^{-1}$ .

were used to measure the resonance. They are indicated by different symbols. with time is four times smaller and the resonance excitation is stronger. In this case different bunches the beam energy during the 12 minutes of measurement. In case (b) the slope of spin tune change to a standard energy calibration. The slightly asymmetric resonance shape is due to tidal changes of Figure 4: Two measurements of the artificially excited spin resonance are shown. Case (a) corresponds



 $\Delta v_{scan}$  /  $\Delta t$  [s<sup>-1</sup>] decoherence time of 3 seconds.  $\frac{0.75}{0.15}$  magnet is  $2 \cdot 10^{-3}$  Tm. The dot-<br> $\frac{0.75}{0.10^{2}}$  ted line has been calculated for a magnet is  $2 \cdot 10^{-3}$  Tm. The dotsumed that the field of the RF-<br>sumed that the field of the RFtion was performed with a simple onance is indicated. The calcula the upper scale the correspond a function of  $\Delta \nu_{scan}/\Delta t$ . On

decoherence time  $\tau_{decoh}$ : the synchrotron radiation lead to a decay the horizontal component of the polarization with a

(5) 
$$
\frac{P_{\text{final}}}{P_{\text{initial}}} = e^{-T/\tau_{decoh}} \left[ 2 e^{-\chi} - 1 \right]
$$

(6) 
$$
\chi = \frac{\pi \epsilon^2}{2 \Delta \nu_{\text{scan}}/\Delta t}
$$

than 1 MeV and the depolarization is strong enough to be easily observed. LEP the width of the depolarizing resonance is sufficiently small to reach a precision better flips  $(P_{\text{final}}/P_{\text{initial}} = -1)$  have not been observed at LEP. For standard energy calibrations at simple model. In this model a decoherence time of a few seconds explains why complete spin the change in polarization  $P_{\text{final}}/P_{\text{initial}}$  is shown for LEP as a function of  $\Delta\nu_{\text{scan}}/\Delta t$  for this  $T$  is taken as the time needed to cross the half-width of the excited spin resonance. In figure 5

#### 3.5 Interference between depolarizing resonances

the vicinity of strong spin resonances : interference effects would disturb the expected relation between  $f_{RF}$  and the beam energy E in setting the beam energy was measured by resonant depolarization. Any significant shift due to The beam energy was changed by setting the RF-frequency  $f_{\rm RF}$  to different values. For each energy. The effect was studied experimentally by approaching strong natural spin resonances. natural spin resonances could result in a shift of the measured spin tune and a bias of the beam It was suggested in [24] that interferences between the artificially excited spin resonance and

(7) 
$$
\frac{\Delta E}{E} = -\frac{1}{\alpha} \frac{\Delta f_{\rm RF}}{f_{\rm RF}}
$$

calibrations due to interference of spin resonances can be excluded down to  $\Delta E/E = 2 \cdot 10^{-6}$ . any experiment performed in 1993. From the experimental results any bias of standard energy with the theoretical calculation. No significant shifts from interference effects were found in behavior was observed. The measured value of  $\alpha = (1.860 \pm 0.020) \cdot 10^{-4}$  is in excellent agreement were crossed and  $[\nu]$  was lowered down to 0.35 no significant deviation from the expected linear ment with resonant depolarization is shown in figure 6. Though several strong spin resonances The momentum compaction factor  $\alpha$  for LEP is calculated to be 1.859 · 10<sup>-4</sup> [12]. Its measure-

#### 3.6 Spin tune shifts due to longitudinal magnetic fields

In the general case the spin tune is given by : relation from equation 3 is not strictly valid any more and small spin tune shifts  $\delta\nu$  can occur. deviations mainly at the quadrupoles. Since three-dimensional rotations do not commute the fields arise from the experimental solenoids. Radial fields occur due to vertical closed orbit storage rings without any longitudinal and radial magnetic fields. In LEP strong longitudinal The relation between spin tune  $\nu$  and beam energy E given by equation 3 is only valid in ideal

(8) 
$$
\nu = \frac{E[\text{MeV}]}{440.6486(1)[\text{MeV}]} + \delta \nu
$$

experimental solenoids [25]. Around  $|\nu|=0.5$  the shift due to the solenoids is smaller than  $\delta\nu$  introduces a bias of the energy calibration. The effect was found to be small for the LEP



symbols used in this figure. shifts of the beam energy were observed. The errors on the energy measurements are smaller than the spin resonances indicated by the dotted lines were crossed during the measurement. No unexpected of  $f_{RF}$  are indicated. The nominal RF frequency used at LEP is 352 254 170 Hz. Two strong  $Q_s$ Figure 6: Measured beam energy E as a function of the RF frequency  $f_{RF}$ . Only the last four digits



from the Monte-Carlo calculation. curves) are compared to Monte-Carlo results (black squares). The bars on the points give the spread of the RMS deviation of the vertical closed orbit  $\sigma_v$  for  $\nu = 101.45$ . The analytical calculations (smooth Figure 7: The mean spin tune shift and its spread due to radial magnetic fields are shown as a function

matching.  $\delta\nu = 10^{-4}$  without spin matching of the solenoids and smaller than  $\delta\nu = 10^{-5}$  with spin

than before. immediately remeasured and found to be located in the same  $\Delta\nu_{\rm scan} = 0.002$  wide scan range the solenoids were switched off after a successful spin tune measurement. The spin tune was The theoretical prediction was tested experimentally when the spin matching bumps for

#### 3.7 Spin tune shifts due to radial magnetic fields

tune shifts  $\delta\nu$ . This problem was treated in [26]. beam is subject to random radial error fields mainly at the quadrupoles which can cause spin In a real storage ring the beam-line elements are not perfectly aligned. As a consequence the

cession. A spin tune shift  $\delta \nu$  can result with a RMS spread of : The radial fields produce spin rotations that do not commute with the nominal spin pre

$$
\sigma(\delta \nu) \approx 0.04 \,\nu^2 n_Q (KL)^2 \sigma_v^2
$$

to be close to 0.5. For accelerators with high beam energy  $\delta\nu$  can become large. KL the quadrupole strength. The effect from orbit correctors is neglected and  $[\nu]$  is assumed where  $n_Q$  is the number of quadrupoles,  $\sigma_y$  the RMS distortion of the vertical closed orbit and

cases. This introduces a relative uncertainty of  $\Delta E/E < 2 \cdot 10^{-6}$  on the energy calibration. spin tune shift due to the finite vertical closed orbit is smaller than 100 keV for all practical dependence of  $\sigma(\delta \nu)$  on the vertical closed orbit RMS is illustrated in figure 7. At LEP the for  $\nu = 100.45$ . The spread  $\sigma(\delta \nu)$  is estimated to be about 30 keV for  $\sigma_y = 0.5$  mm. The larization for LEP. Numerical estimates predict an average spin tune shift of less than 10 keV This effect puts a practical limit on the accuracy of energy calibration by resonant depo

experimental results are compatible with the calculated spread. to 0.5 MeV was seen. For all other measurements no significant effect was observed. The between 0.4 MeV and 1.2 MeV was found. In another experiment a change by 0.1 MeV after vertical closed orbit corrections. ln one case a significant change in the beam energy The effect was studied experimentally by looking for unexpected changes of the spin tune

and no shift was observed within the scan width of  $\Delta E_{\rm scan}= 0.88$  MeV. occasion the spin tune was measured with and without the Harmonic Spin Matching bumps shifts, but simulations show that their effect on the spin tune is totally negligible  $[12]$ . On one polarization optimization uses vertical  $\pi$ -bumps [8] which could potentially produce spin tune Harmonic Spin Matching was used routinely during energy calibration. This technique for

#### 3.8 Effects of electrostatic fields

to any significant bias of the energy calibration. small strength of the electrostatic fields, spin tune shifts due to electrostatic field do not lead ences are of the order of  $\sim 1/\gamma$ . Given the large  $\gamma$  factor  $(8.8 \cdot 10^4)$  of the LEP beams and the electrostatic fields affect the spin in a similar way than transverse magnetic fields. The differ certain positions in the ring to avoid parasitic collisions. According to equation 2, transverse Transverse electrostatic fields are used at LEP to separate the electron and positron beams at

#### 3.9 Effects of quadratic non-linearities

oscillations of the individual particles. This effect is expected to be very small. For LEP this Small systematic spin tune shifts can occur due to the spin tune spread related to synchrotron

Source	$\Delta E/E$	$\Delta E$ ( <i>E</i> =45.6 GeV)
Electron mass	$3 \cdot 10^{-7}$	$15 \; \mathrm{keV}$
Revolution frequency	$10^{-10}$	$0 \text{ keV}$
Frequency of the RF magnet	$2 \cdot 10^{-8}$	$1 \text{ keV}$
Width of excited resonance	$2 \cdot 10^{-6}$ $90 \text{ keV}$	
Interference of resonances	$2 \cdot 10^{-6}$	$90 \text{ keV}$
Spin tune shifts from long. fields	$1.1 \cdot 10^{-7}$	$5 \; \mathrm{keV}$
Spin tune shifts from hor. fields	$2 \cdot 10^{-6}$	$100 \text{ keV}$
Quadratic non-linearities	$10^{-7}$	$5 \; \mathrm{keV}$
Total error	$4.4 \cdot 10^{-6}$	$200 \text{ keV}$

is assumed. All errors are understood to be RMS errors. summarized for LEP. A standard energy calibration with a well corrected vertical closed orbit Table 1: The accuracy of the beam energy calibration method by resonant depolarization is



for the systematic error. only be verified with limited accuracy. Only an upper bound was established experimentally Table 2: Experimental tests of several systematic effects. The systematic errors in table 1 could

 $\ddot{\phantom{a}}$ 

 $\mathcal{L}(\mathcal{L}^{\mathcal{L}})$  , where  $\mathcal{L}^{\mathcal{L}}$  is the contribution of the contribution of  $\mathcal{L}^{\mathcal{L}}$ 

spin tune measurements. No change in energy was observed within  $\pm$  0.88 MeV. this effect in not important for LEP, the chromaticity was increased by about  $+10$  between two of quadratic non-linearities, e.g. the chromaticity of radial betatron oscillations. To verify that shift produces a relative error of  $\Delta E/E < 1 \cdot 10^{-7}$  [7, 27]. The effect is controlled by variation

#### 3.10 Summary on the calibration accuracy

storage ring settings. the systematic error to be better than 200 keV for a standard energy calibration in regular An experimental upper bound for the systematic error of 1.1 MeV was established. We estimate verification of these results could be performed with limited accuracy, as summarized in table 2. calibration with resonant depolarization was obtained using theoretical studies. Experimental resonant depolarization is estimated to be about 0.2 MeV on the Z pole. The systematic error on for the different sources of uncertainties. The total systematic error on energy calibration by Systematic errors on an individual the energy calibration at LEP are summarized in table 1

## 4 LEP settings for beam energy calibration

physics fill, the following modifications were introduced : settings to reduce possible systematic effects. For an energy calibration at the end of a LEP ibrations were performed with a minimum amount of modifications to the normal luminosity LEP settings are described in table 3 and are designated by Peak—2, Peak and Peak+2. Cal Operational energy calibrations were performed on the electron beam for three energies. The

- interaction points to avoid collisions. beams present in the ring. In these cases the two beams were vertically separated at the The positron beam is dumped. Only the last 4 calibrations were performed with both
- to special polarization tunes  $(Q_x, Q_y) = (90.1, 76.2)$ . • The betatron tunes are changed from the normal physics tunes  $(Q_x, Q_y) = (90.26, 76.18)$
- $\sigma_x \leq 0.5$  mm). • The vertical and horizontal closed orbits are corrected to a small RMS ( $\sigma_y \leq 0.3$  mm,
- The polarization level is improved with Harmonic Spin Matching bumps.
- to the experimental solenoids. Vertical solenoid compensation bumps are introduced to compensate the spin rotation due



due to different parameters that affect the LEP beam energy. (CM) energies.  $m_Z$  is the Z boson mass. The precise beam energy for a defined calibration can vary Table 3: Definition of the three LEP settings and the corresponding typical beam and center-of-mass

#### 4.1 Effects of LEP settings on beam energy

to verify the effects of accelerator parameters on the energy. discussed, but they may also shift the beam energy. A number of experiments were performed Accelerator settings can modify the spin tune without affecting the energy, as has already been

#### 4.1.1 PRETZEL omsirs

orbit, the oscillations would lengthen their orbit by [29] orbits make large horizontal betatron oscillations and if they were to stay on the same central the middle of the arcs, both beams evolve on horizontal pretzel orbits [28]. Particles on pretzel Since 1992 LEP is colliding 8 electron and 8 positron bunches. To avoid beam encounters in

(10) 
$$
\Delta C_c \simeq \frac{8q_x^2 x_p^2}{C_c} \simeq 0.1 \text{ mm}
$$

contributions with the opposite sign. The net energy change was calculated to be  $+0.2$  MeV [29]. equilibrium energy of the beams, but the large orbit excursions in the sextupoles give additional orbit position moves inward by  $\Delta C/2\pi$  to satisfy this constraint. This would lead to a lower reality, the RF frequency forces the length of the orbit to remain constant and the average where  $x_p$  is the pretzel amplitude and  $q_x = 84$  is the horizontal tune inside the pretzel. In

normal calibrations and the results, shown in table 4, agree with the theoretical expectation. shift of  $\Delta E = -1.7 \pm 0.7$  MeV [3, 29]. Two experiments were performed in 1993 at the end of ln 1992 a measurement of the energy variation due to the pretzel orbits gave a rather large

can be different from the theoretical estimate. excluded that due to field imperfections and misalignments, the real energy shift from Pretzel performed with normal orbits, are compared with the physics fills calibrations. It cannot be is not a critical error. It only plays a role when Machine Development (MD) calibrations, often Since calibrations at the end of physics fills were always performed with pretzel orbits, this

#### 4.1.2 BETATRON TUNES

calibrate with physics tunes, a careful and delicate adjustment of the energy is required to reach depolarizing resonances close to  $|\nu|=0.5$  where the highest polarization is obtained [8]. To from the standard physics tunes of  $\sim$  (0.26,0.18). This tune shift improves the pattern of Energy calibrations are performed with betatron tunes of  $(Q_x, Q_y) = (0.1, 0.2)$  which differ

Experiment	$\Delta E$ (MeV)	
1992 Measurement	$-1.7 \pm 0.7$	
<b>LEP Fill 1674</b>	$+0.1 \pm 0.6$	
<b>LEP Fill 1698</b>	$-0.4 \pm 0.6$	
1993 Average	$-0.2 \pm 0.4$	
Theor. Estimate	$+0.2$	

Table 4: Measurements of the energy change  $\Delta E = E(\text{pretzel}) - E(\text{no pretzel})$  due to pretzel orbits.

between the horizontal tune settings was measured to be : polarization was obtained with tunes (0.25, 0.2) close to physics tunes. The energy difference a good level of polarizations and to avoid depolarizing resonances. In a dedicated MD, good

(11) 
$$
E(Q_x = 90.25) - E(Q_x = 90.1) = -0.2 \pm 0.6 \text{ MeV}
$$

which shows that there is no significant bias due to the tune change.

#### 4.1.3 LOW BETA OPTICS

introduces a systematic error of about 2.5 MeV. The observed energy change was : in MD experiments. The effect of lowering  $\beta^*$  could only be compared with different fills which the same low beta conditions than physics fills, but LEP is usually operated with  $\beta^* = 20$  cm luminosity running should not affect the energy. Normal energy calibrations are performed in The reduction of the betatron function  $\beta^*$  at the interaction point from 20 cm to 5 cm for

(12) 
$$
E(\beta^* = 5cm) - E(\beta^* = 20cm) = 1.5 \pm 0.7 \pm 2.5 \text{ (fill-to-fill)} \text{ MeV}
$$

No effect of the  $\beta^*$  reduction was therefore observed within the large uncertainties.

#### 4.1.4 LOCAL MAGNETIC BUMPS

on the energy. steering is also used routinely between energy calibrations in a single fill without visible effect was observed in the same 0.88 MeV wide scan region than than without the bump. Local beam bump with an amplitude of 5 mm was introduced in another location of LEP, depolarization polarimeter laser and the electron bunches have been controlled. When a similar horizontal of the horizontal bumps used to steer the beam in the interaction region between the Compton beam and the change in path length does not lead to a significant change in energy. The effect A closed local magnetic bump does not change the beam energy : there is no net deflection of the

## 5 Models of energy variations and corrections

to a define reference situation. parameters that are necessary to compare energy calibrations and to correct the measurements of critical parameters (temperature, magnets currents). We will describe in this chapter some understanding and prediction of the effects (tidal deformations) and a continuous monitoring of the running conditions (temperature and excitation of the magnets, RF frequency), a good tal conditions". Their impact on the energy can be minimized or corrected by a tight control The beam energy of LEP is subject to fluctuations due to the LEP settings and to "environmen-

#### 5.1 Magnetic field measurements

from this average will be denoted by  $E_{NMR}$ . It can be used to track energy variations due to readings to a calibration with resonant depolarization have been averaged. The energy predicted series with the LEP main bending magnets. For the analysis of our data, the two closest NMR a reference magnet and read out every few minutes. This reference magnet is connected in A measurement of the LEP bending field is provided by a NMR probe which is installed inside

Experiment	$\alpha[\times 10^4]$	
LEP Fill 1717	$1.862 \pm 0.045$	
LEP Fill 1734	$1.860 \pm 0.020$	
Average	$1.860 \pm 0.018$	
Theory	1.859	

Table 5: Measurements of the momentum compaction factor of the  $90^{\circ}/60^{\circ}$ lattice.

probe can be found in appendix A. the NMR correspond to true field changes. More details on the problems related to the NMR is not completely understood and it is not entirely clear if all the variations measured with the main bending field inside a fill or between consecutive fills. Unfortunately, this instrument

#### 5.2 Momentum compaction factor

length  $L_o$  to the energy of the beam : The momentum compaction factor  $\alpha$  relates changes in the RF frequency  $f_{RF}$  or in the orbit

(13) 
$$
\frac{\Delta E}{E} = -\frac{1}{\alpha} \frac{\Delta f_{RF}}{f_{RF}} = \frac{1}{\alpha} \frac{\Delta L_o}{L_o}
$$

 $\alpha$  depends on the horizontal focusing and one has the useful approximate relations [30]:

(14) 
$$
\alpha \cong \frac{}{R} \approx \frac{1}{Q_x^2}
$$

about 4 orders of magnitude. circumference variations produce observable energy variations because they are enhanced by bending radius. The strong focusing produces a small momentum compaction factor. Tiny where  $\langle D_x \rangle \approx 70$  cm is the average horizontal dispersion in the arcs and R the average

the MAD program [31]. expectations of  $\alpha = 1.859 \cdot 10^{-4}$  for the 90°/60° lattice obtained from simulation of LEP with 6 in a previous section). The results shown in table 5 are in agreement with the theoretical extract  $\alpha$ . A second measurement was performed with a 75 Hz RF frequency scan (see figure the RF frequency was changed by  $+38$  Hz and the corresponding energy change was used to The momentum compaction factor was measured on two occasions. In a first experiment

#### 5.3 Terrestrial tides

beam energy  $\Delta E$  [33]: off-center in the quadrupoles where they receive an extra deflection. This leads to a change in fixed by the constant RF frequency, the change in circumference will force the particles to move The strain modifies the circumference  $C_c$  of LEP by 1 mm [32]. Since the length of the orbit is cm in the Geneva area. This corresponds to a local change of the earth radius of  $4 \cdot 10^{-8}$ . Terrestrial tides of the sun and the moon move the earth surface up and down by up to  $\sim$ 25

(15) 
$$
\frac{\Delta E}{E} = -\frac{1}{\alpha} \frac{\Delta C_c}{C_c}
$$



during full moon. corresponds to a situation close to half moon, while the November 1992 experiment was performed tide model. The average value of  $\kappa_{tide}$  has been used in all pictures. The October 1993 experiment November 1992, August and October 1993. The solid line is the predicted evolution from the CTE Figure 8: Evolution of the relative beam energy variation due to tides as a function of time in

 $\kappa_{tide}$  relates  $\Delta g$  to  $\Delta E$ : quantity that can be predicted by computer codes with good accuracy [34]. The tide coefficient In a good approximation, the horizontal strain is proportional to the change in gravity  $\Delta g$ , a

$$
\frac{\Delta E}{E} = \kappa_{tide} \Delta g
$$

value of  $\kappa_{tide}$  is extracted for the CTE model [36]: that may indicate small uncontrolled energy fluctuations. Using all measurements the following in figure 8. The energies follow the CTE tide predictions, with the exception of a few points from Earth tide measurements [35]. The results of 3 long and stable experiments are shown the tide potential into 505 terms, includes empirical amplitude corrections and phases obtained Tayler—Edden potential [34]) tide model was adopted. This model, a harmonic development of and the prediction from a very simple tide model. In 1993 a more accurate CTE (Cartwright in November 1992 [33] showed excellent agreement between the measured energy variations A high tide  $\Delta g$  exceeds 140 µgal in Geneva (1 gal = 1 cm s<sup>-2</sup>). A first experiment performed

(17) 
$$
\kappa_{tide} = (-8.6 \pm 0.8) \cdot 10^{-7} / \mu \text{gal}
$$

this information, we obtain an estimate for  $\kappa_{tide}$ : Earth elasticity show that about 16% of the gravity variation couples into lateral strain. Using tainties due to the use of the CTE potential to predict the tidal deformations. Measurements of where the error is estimated from the spread of the data and includes an estimate for uncer

(18) 
$$
\kappa_{tide} \approx \frac{-0.16}{\alpha g_0} = -9 \cdot 10^{-7} / \mu \text{gal}
$$

measurements. More details on the tide effects can be found in [34, 36]. where  $g_0 = 980$  gal is the average local gravity. This estimate is in good agreement with our

#### 5.4 Magnet temperature

coefficient  $\alpha_T$  as : perature because of the iron-concrete structure of the magnets  $[5]$ . We define the temperature The bending field of the LEP dipoles has a significant dependence on the magnet core tem

$$
\alpha_T = \frac{1}{E} \frac{\Delta E}{\Delta T}
$$

distributed in all octants. where T is the average temperature of 32 out of 3300 dipole cores. The 32 sensors are evenly

resonant depolarization The temperature coefficient  $\alpha_T$  of the LEP dipoles was measured on 3 occasions using

- shown in figure 9.  $\sim 0.3$ °C in 4 hours. The correlation between the beam energy and the temperature is • Experiment 1 (fill 1636) : The average temperature of the LEP dipoles increased by
- frequency shifts is shown as a function of temperature in figure 10. momentum compaction factor  $\alpha$ . The residual energy variation after correction for RF by  $\sim 0.4^{\circ}C$  during this energy scan experiment.  $\alpha_T$  was extracted together with the • Experiment 2 (fill 1734) : The average temperature of the LEP dipoles increased



rected beam energy in fil] temperature and the tide cor tween the average magnet

temperature (fill 1734). tion of the average magnet and tides) is shown as a func tion for RF frequency changes Figure 10: The residual en



of  $1.1 \cdot 10^{-4}$ . jumps (figure 12) with a slope tion inside each group of data show the expected correla  $2.5 \cdot 10^{-4}$ . The dashed lines sponds to a fit to the whole l772. The solid line corre Figure 11: Correlation be

ble  $6$ ). There are indications for 2 sudden energy jumps. temperature (coeff. from ta for tide, RF frequency and  $E_{pol} - E_{NMR}$  in fill 1772. The Figure 12: Evolution of

Experiment	$\alpha_T[10^{-4}/\text{deg}]$		
LEP fill 1636	$1.01\,\pm\,0.43$		
LEP fill 1734	$1.12 \pm 0.41$		
Average	$1.07 \pm 0.30$		

Table 6: Measurements of  $\alpha_T$ .

coefficient is about twice as large as the value extracted from the two first experiments. value of  $2.5 \cdot 10^{-4}$  with quite a good correlation between energy and temperature. This full data sample is used for the temperature analysis as shown in figure 11,  $\alpha_T$  reaches a were warming up after a technical stop and the temperature increase was  $\sim 0.6^{\circ}C$ . If the • Experiment 3 (fill 1772) : This experiment was performed while the LEP magnets

that could explain an energy jump [37]. demanded these adjustments. An analysis of the beam orbits revealed no orbit movement is not understood if those corrections were the cause of those jumps or if the energy jumps correlate these jumps with orbits corrections and small tune adjustments  $(\Delta Q_x \sim 0.02)$ , it with the exception of two sudden jumps (figure 12). Although there are indications to two experiments (table 6), the time evolution of the corrected energy is relatively fiat When the data is corrected with the temperature coefficient obtained from the previous

were observed inside a single fill. The origin and frequency of such jumps is unknown. But it is also the only occasion in 1993 when large  $(> 1 \text{ MeV})$  and abrupt energy changes lf the hypothesis of the 2 jumps is accepted, all the temperature data becomes consistent.

fills. the precision already obtained previously because of the small temperature lever arms in the The coefficients in table 6 are in agreement with other measurements [5]. They do not improve possible jumps in energy and we use the values of table 6 for the beam energy data analysis. The analysis of the temperature data in fill 1772 has turned out to be very subtle due to the

#### 5.5 QFQD compensation loop

or turned off on different occasions. sum of all tree currents should be zero, but during the 1993 LEP run,  $I_{Qfd}$  has been inverted asymmetry, a compensating current  $I_{Qfd}$  is flowing in a third bar next to the two others. The they are almost in the plane of the ring. To cancel the magnetic field created by the current current run next to the LEP ring at a distance of about 1 m from the vacuum chamber and in the D quadrupoles (hor. defocussing). The two bars that carry the quadrupole excitation  $(90^{\circ}/60^{\circ}$  optics), the excitation current in the F quadrupoles (hor. focussing) is larger than When LEP is running with different phase advances in the horizontal and vertical planes

bending strength of  $\sim 0.025$  Tm for 33 A [38, 39]. length over which this field is acting was estimated to be about 3750 m and corresponds to a creates a field of 6.6  $\mu$ T at the position of the beam in the vacuum chamber. The effective When  $I_{Qfd}$  is zero, the net current in the bars is about 33 A. A wire carrying such a current

Reversing the current in the loop induced a change  $\Delta E = -3.0 \pm 1.4$  MeV on average, in The effect of  $I_{Qfd}$  was measured on two occasions by inverting  $I_{Qfd}$  from 32 A to -39 A.

Experiment	$C_{Qfd}$ (MeV/A)
LEP fill 1845	$0.025 \pm 0.009$
LEP fill 1888	$0.062 \pm 0.010$
Average	$0.042 \pm 0.020$
Theor. Estimate	$0.037 \pm 0.008$

average is estimated from the spread of the 2 fills. Table 7: Correction factor  $C_{Qfd}$  for the effect of the quadrupole current asymmetry. The error on the

spread of the two experiments. The correction coefficient  $C_{Qfd}$ surements show a significant difference. The error has been estimated conservatively from the agreement with the theoretical estimate of  $-2.6 \pm 0.5$  MeV [38], but the two individual mea-

$$
\Delta E = C_{Qfd} \,\Delta I_{Qfd}
$$

is given in table 7.

#### 5.6 Energy calibration reproducibility and correction quality

deviation  $\delta_E$ : all parameters that are known to affect the energy. We define for each corrected energy E the factors. For this analysis, each energy measurement is corrected to a reference situation for allows to estimate the reproducibility of the energy calibration and the quality of the correction On most occasions, the beam energy was measured repeatedly during the same fill. This

$$
\delta_E = \frac{E - E_{av}}{\Delta_E}
$$

reasons for the difference : exhibits a roughly Gaussian shape instead of the expected flat distribution. There are a few avoid a too strong bias towards  $\delta_E = 0$ . The experimental distribution, shown in figure 13, without any change in beam conditions, the second calibrations is not used for the analysis to depolarizations. When two calibrations are too close together in time (less than 15 mins) and  $+1$  if the measurements are uncorrelated and the energy is varying sufficiently between different particular depolarization scan. The distribution of  $\delta_E$  is expected to be flat between -1 and where  $E_{av}$  is the average corrected energy in a given the fill and  $\Delta_E$  the half-width of the

- bias  $\delta_E$  towards 0 and to decrease the RMS. beam energy and to get a clean depolarization in only one scan. This attitude tends to spin resonance. Usually the scan limits are then displaced to center the bin around the ization is also observed in the neighboring scan region because of the width of the excited When the energy of the beam is close to the edge of the depolarization scan, some depolar
- change much between two calibrations which are then strongly correlated. • Some of the measurements are taken close together. In that case, the energy does not
- not monitored, the distribution will acquire tails beyond  $-1$  and  $+1$ . If the energy of the beam fluctuates because of effects which are not under our control or



Daytime

hatch) and the full sample (white). hatch),  $\Delta_E \leq 0.22$  MeV (light data with  $\Delta_E = 0.11$  MeV (dense the full distribution is 0.84. The all the 1993 data. The RMS of Figure 13: Distribution of  $\delta_E$  for

 $(\pm \Delta_E).$ the width of the frequency scan errors shown here correspond to 7) and 115  $\mu$ A (bunch 6). The distributed between 85  $\mu$ A (bunch energy. The bunch currents were fimction of time are corrected for points). The energies shown as a x 3 765 4 2 8 ergies of different bunches (indi

 $\Delta\Delta\sim 10$ 

Experiment	$\mathbf{Date}$	Duration	Reproducibility
(LEP fil)		(hours)	
1636	20-06-93	4	Better than 0.3 MeV
1734	5-08-93	4.5	Better than 0.2 MeV
1772	29-08-93	21.5	2 and 1.3 MeV jumps,
			up to 0.8 MeV deviations
1811	12-09-93	5.5	$0.6 \text{ MeV}$ jump
1849	11-10-93	11	up to 0.8 MeV deviations

Table 8: Medium term beam energy measurement reproducibility.

error on the energy : measurement. We use this estimate to define for each individual calibration inside a fill the of 0.6. This corresponds to a typical systematic point to point error of  $\simeq 0.3$  MeV on each is expected to be  $1/\sqrt{3} = 0.57$ . The difference can be attributed to a systematic error  $\sigma_{\delta}$ The  $\delta_E$  distribution of figure 13 has an RMS of 0.84 while the RMS of a flat distribution

(22) 
$$
\sigma_E = \sqrt{\frac{\Delta_E^2}{3} + (0.3 \text{ MeV})^2}
$$

fill. For a standard calibration  $\Delta_E = 0.44$  MeV, leading to  $\sigma_E = 0.4$  MeV. the RMS error on an individual calibration with respect to the other calibrations of the same This relation includes reproducibility and correction errors and was used in this report to obtain

short term reproducibility of the beam energy calibration. within  $\pm 100$  keV over a 30 minutes time interval (figure 14). This experiment shows an excellent The energies of different bunches were compared during stable conditions and were identical

sufficiently clear to apply a correction algorithm. indications to correlate several of these jumps to orbit corrections, those correlations are not given in table 8. Some of the jumps are visible in figures in this document. While there are occasionally when the energy is tracked for some hours. A summary of such observations is 24 hours) is typically  $\sim 0.5$  MeV. Some steps or deviations of this importance are observed The medium term reproducibility of the beam energy measurement inside a single fill (6-

## 6 Positron beam energy

seconds. It is believed that oscillations of the mirrors due to vibrations of the vacuum chamber were observed in the rate of Compton photons scattered from the positron beam within a few fortunately the operation of the system was more difficult than anticipated. Large fluctuations downstream from the interaction point between the positron bunches and the laser beam. Un positron beam. The backscattered Compton photons are detected in a detector  $\sim$  390 m beam polarization is reflected back by a concave mirror to allow head-on collisions with the missioned in the following months. The same laser beam that is used to measure the electron A positron polarimeter was installed during the LEP September 1993 technical stop and com

effect. This problem should be solved in 1994. produced important changes in the position of the laser focus and could be at the origin of the

it is only possible to give the following range for the difference of the energies : to solve the ambiguities of the depolarization procedure for the positron beam. For this reason, electron beam was confirmed. Due to a lack of time, it was not possible to change  $Q_s$  and  $f_{RF}$ the expected energy from the electron calibration was observed. Finally the calibration of the was first carefully measured. Then the positron beam was depolarized. A shift with respect to beams were present in LEP with a polarization of  $\sim$  15%. The energy of the electron beam lt was still possible to perform a single test calibration when both electron and positron

(23) 
$$
0.5 \text{ MeV} < |E_{e^-} - E_{e^+}| < 3.2 \text{ MeV}
$$

understand the positron energy. The cause for this energy shift is not known and more experiments are planned in 1994 to

### 7 Beam energy calibration results in 1993

Numerical results for the calibration of all fills are given in appendix B. contribution to the error on the energy due to the uncertainties on the correction coefficients. weighted average is calculated. The average correction for each parameter is used to obtain the temperature. For a given fill, all energies are corrected to the reference situation before the physics fills. The reference magnet temperature was chosen to be close to the average calibration LEP defined in table 9. The reference RF frequency corresponds to the setting used in normal To combine the 1993 energy calibrations, all results are corrected to a reference situation for

they do not show the same amplitude of the variation as a function of time. average at the begin of the LEP energy scan. The two energy points evolve in parallel, but been subtracted from the energies at  $Peak+2$  and  $Peak-2$  to make the energies coincide on as a function of time, corrected to the reference values of table 9. Two constant offsets have In figure 15 the evolution of the energy  $E_{pol}$  obtained from resonant depolarization is shown

for  $E_{pol}$  alone. over time. Figure 16 shows that this is not the case. The variations are roughly the same than and if the NMR probe tracks this field correctly, the difference  $E_{pol}-E_{NMR}$  should be constant If the bending field of the main dipoles is the cause of the energy variations seen in figure 15

Parameter	Reference value	Correction factor
RF frequency	352 254 170 Hz	$\alpha = (1.860 \pm 0.020) \cdot 10^{-4}$
Tide	$0 \mu$ gal	$\kappa_{tide} = (-8.5 \pm 0.8) \cdot 10^{-7} / \mu \text{gal}$
Av. Magnet Temperature	$24^{\circ}C$	$\alpha_T = (1.1 \pm 0.3) \cdot 10^{-4}/\text{deg}$
$QFQD$ comp. loop $(Peak-2)$	$+32$ A	$C_{Qfd} = (4.2 \pm 2.0) \cdot 10^{-2}$ MeV/A
$QFQD$ comp. loop $(Peak+2)$	$+33$ A	

used to correct  $E_{pol}$  are given in column 3. Table 9: Reference values of the parameters that affect the LEP beam energy. The correction factors



Peak+2 have been shifted to The energies for Peak—2 and of time in 1993. The time energy measured by resonant Figure 15: Evolution of the

a function of time. larization and by the NMR as



 $\langle \ldots \rangle$  and

 $\mathcal{L}^{\text{max}}_{\text{max}}$  and



 $0.7 \text{ MeV}.$ Conversion factor : 1 Hz  $\simeq$ 





Figure 19: Evolution of the radial orbit position in the LEP arcs (average for both time in physics fills. There which is correlated with the energy variations observed by the resonant depolarization  $\wedge$  Peak calibrations. As expected the orbit evolution is identical for

frequency is the critical period of the largest energy drifts. ln the absence of tides the average central RF large change in the LEP circumference (figure 18). Unfortunately measurements are missing in that are not due to tides. The evolution of  $f_{RF}^c$  as a function of time shows no evidence of a spread of the data is larger than the measurement errors, which could be due to ring movements The observed values of  $f_{RF}^c$  show the expected correlation with the tides (figure 17), but the frequency, that could also explain the energy drift, can be directly measured with  $f_{RF}^c$  [40, 41]. the beams on the central orbit. A change of the circumference of LEP or a drift of the RF vanishes. The central RF frequency  $f_{RF}^c$  corresponds to the RF frequency setting which brings and sextupoles. On this orbit the net bending field from quadrupole and sextupole magnets A particle on the central orbit moves on average through the center of all the quadrupoles

(24) 
$$
f_{RF}^{c} (\Delta g = 0) = 352254162.6 \pm 2.5 \text{ Hz}
$$

which corresponds to a LEP circumference of :

والمستحدث المتار

(25) 
$$
C_c (\Delta g = 0) = \frac{c h}{f_{RF}^c (\Delta g = 0)} = 26655.4686 \pm 0.0002 \text{ m}
$$

velocity of light. The central beam revolution frequency is 11 246.94 Hz. where  $h = 31320$  is the harmonic number of the LEP accelerating RF system and c is the

tions of the average radial beam position  $\Delta X_{ARC}$  at the arc pickups and of the energy  $\Delta E$  are 11], an analysis of orbits measured during all LEP physics fills was performed [37]. The varia With the improved electronics of the Narrow Band LEP Beam Orbit Monitors (BOMs) [10, related through :

(26) 
$$
\Delta X_{ABC} = D_x^{pu} \frac{\Delta E}{E} \cong 12.5 \ (\mu \text{m}) \cdot \Delta E[\text{MeV}]
$$

deformations are correlated with rainfall [42, 43]. variations are significantly reduced (figure 20 and table 10). There are indications that the ring beam energy is corrected for the movement of the orbit according to equation 26, the residual drift of the beam position that is correlated with the evolution of  $E_{pol}$  (figure 19). When the example of such deformations that are now well understood. The analysis of  $X_{ARC}$  reveals a in energy due to the bending field in quadrupoles and sextupoles. The terrestrial tides are an beam to change its position in the quadrupoles and in the BOM pickups and induce a change  $D_x^{pu} \cong 57$  cm is the average horizontal dispersion at the pickups. Ring deformations force the

 $\sim 10^{-4}$ . the difference is  $\sim 4.7$  MeV, which corresponds to a precision of the Flux-Loop calibration of agree within the errors. The two calibration methods are compared in table 10. The RMS of  $E_{fl}$  is +6.8  $\pm$  8 MeV. Figure 21 shows that Flux-Loop and resonant depolarization calibrations of 352 254 170 Hz and the average tide-corrected central frequency. The total correction on been corrected by  $-5.2$  MeV to account for the difference between the reference RF frequency for the effect of Nickel layer in the LEP vacuum chamber [46]. The Flux-Loop data has also account for aging of the concrete-iron dipole magnet cores, for the Earth magnetic field and this reason, the measured Flux-Loop energies  $E_{fl}$  have been corrected by +12  $\pm$  8 MeV to static magnetic fields and of the quadrupole and sextupole magnets on non-central orbits. For for LEP energy calibration  $[5]$ . The Flux-Loop calibrations are insensitive to the effects of the integrated bending field of the LEP dipole magnets [44, 45]. It has been used extensively The Flux-Loop consists of electrical loops threading all LEP dipoles which allow to measure

the evolution of the beam energy in every fill [37]. position in the arcs and the quadrupole current can therefore be used to track and understand with being due to magnetic fields within about  $\pm 2.5$  MeV. The combination of the beam orbit the 1993 data. The good correlation shows that the remaining energy variations are consistent shows the resulting correlation between the measured beam energy and quadrupole current for current of the arc quadrupoles required to set the tunes to their nominal values. Figure 22 tunes and energy was observed in [37], where the tune change was tracked by the excitation magnets will be mismatched and the betatron tunes will vary. The resulting correlation between (0.1, 0.2). If a beam energy change is induced by magnetic fields, the strength of the quadrupole For resonant depolarization calibrations the betatron tunes were carefully set to  $(Q_x, Q_y)$  =



MeV for Peak+2. fills are shown in these figures. The RMS spread of the data points is 3.4 MeV for Peak—2 and 1.7 movement shown in figure 19. Only calibrations performed in normal conditions at the end of physics Figure 20: Evolution as a function of time of the beam energy after correction for the radial orbit

Quantity	Average (MeV)	RMS (MeV)
$E_{fl} - E_{NMR}$ (45 GeV)	$-27.9 \pm 1.7$	5.3
$E_{pol}-E_{NMR}$ (Peak-2)	$-28.9 \pm 0.8$	3.4
$E_{pol}-E_{NMR}$ (Peak+2)	$-31.2 \pm 0.5$	1.7
$E_{fl}-E_{pol}$ (Peak-2)	$-1.8 \pm 1.5$	4.8
$E_{fl}-E_{pol}$ (Peak+2)	$+0.4 \pm 1.5$	4.6

before and after a Flux-Loop calibration. to be added to  $E_{fl}$ . For the differences  $E_{fl} - E_{pol}$ ,  $E_{pol}$  was averaged using the 2 closest measurements the orbit movement observed with the BOM system. In each case, a systematic error of  $\pm$  8 MeV has Table 10: Comparison of Flux-Loop and resonant depolarization calibrations.  $E_{pol}$  is corrected for



the absolute scale of the Flux-Loop an additional error of  $\pm$  8 MeV on ment shown in figure 19. There is rected for the radial orbit move Flux-Loop.  $E_{pol}$  has been cor-Figure 2l: Comparison of all the

 $\pm 2.5$  MeV.  $\circ$  Peak - 2  $\circ$  to magnetic bending fields within good correlation shows that the reexpected slope of  $\approx$  0.6. The The dashed line corresponds to the tidal deformations and for the or in quadrupole excitation current.  $\begin{array}{c|c|c|c|c|c|c|c|c} & & & \text{if } & & \text{if } & \$ 

31

## 8 Conclusions

LEP beam energy. Some important points include : The energy calibration program of 1993 has provided a wealth of data on the behavior of the

- calibrations were performed at the end of physics fills within 3 to 4 hours. Operational energy calibration was successfully commissioned for 3 energies and 24 energy
- energy calibration was shown to be smaller than 1.1 MeV. Several systematic effects have been studied in detail and the systematic error on a single
- determined. The energy dependence of the LEP beams on different physical parameters have been
- difference between electron and positron energies. A first test measurement of the positron beam energy was performed, indicating a possible
- year. Unexpected energy variations of up to 20 MeV have been monitored in the course of the

calibrations are not understood at present, but they might be due to magnetic fields. with rainfall during the second half of the year 1993. The remaining fluctuations of the energy MeV for Peak+2. There are indications that this change in the orbit circumference is correlated the remaining RMS spread of the energy calibrations is about 3.4 MeV for Peak—2 and 1.7 to a change in the circumference of the LEP ring. After correction for this orbit lengthening, MeV  $(4 \times 10^{-4})$  observed between August and October. Part of this variations can be attributed A surprising aspect of the 1993 beam energy data is the rather large variation of up to 20

beam energies during certain parts of the physics fills. to obtain transverse polarization with colliding beams. This would allow a monitoring of the fasten the energy calibration procedure and to improve its accuracy, experiments are planned energy has not been measured accurately. For these reasons, the studies will be pursued. To explained. The behavior of the NMR probe reference is not yet well understood. The positron a few problems remain. The sudden energy jumps during the temperature experiment are not The understanding of the LEP beam energy has been improved substantially in 1993, but

## 9 Acknowledgments

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## References

- [1] L. Knudsen et al., Phys. Lett. B270 (1991) 97.
- [2] L. Arnaudon. et al., Phys. Lett. B284 (1992) 431.
- shop on LEP Performance, J. Poole Editor, CERN SL/93-19 (DI) (1993) 281. {3] M. Placidi et al., "Polarization Results and Future Perspectives", Proc. of the Third Work
- and OPAL, Phys. Lett. B 307 (1993) 187. [4} The Working Group on LEP Energy and the LEP Collaborations ALEPH, DELPHI, L3
- [5] L. Arnaudon et al., "The energy Calibration of LEP in 1991", CERN-PPE/92-125 (1992).
- [6] M. Placidi and R. Rossmanith, Nucl. Instr. Meth. A274 (1989) 79.
- Maximilians-Universitat Miinchen, 1994, to be published. Präzisionsbestimmung der Masse des Z-Teilchens", PhD thesis at the Ludwigs-[7] B. Dehning, "Elektronen- und Positronen-Polarisation im LEP-Speicherring und
- [8] R. Assmann et al., "Polarization Studies at LEP in 1993", CERN-SL/94-08 (AP) (1994).
- Workshop on LEP Performance, J. Poole Editor, CERN SL/93-19 (DI) (1993) 147. {9] M. Mayout and A. Verdier, "Survey and correction of LEP elements", Proc. of the Third
- mance, J. Poole Editor, CERN-SL/93-19 (DI) (1993) 219. [10] J. Borer, "BOM system hardware status", Proc. of the Third Workshop on LEP Perfor-
- London, July 1994. surement system", Contribution to the 1994 European Particle Accelerator Conference, [11] G. Vismara, "The new front-end Narrow-Band electronics for the LEP Beam Orbit Mea
- Miinchen, 1994, to be published. fiir Prazisionsmessungen bei LEP", PhD thesis at the Ludwigs-Maximilians-Universitat [12] R. Assmann, "Transversa1e Strahlpolarisation und ihre Anwendung
- Solenoids", LEP Note 629 (1990). [13] A. Blondel, "Compensation of Integer Spin Resonances Created by Experimental
- [14] V. Bargmann, L. Michel and V.L. Telegdi, Phys. Rev. Lett. 10 (1959) 435.
- [15] The Particle Data Group, Phys. Rev. D45, Part 2 (1992).
- [16] A.A. Sokolov and I.M. Ternov, Sov. Phys. Dokl. 8 (1964) 1203.
- {17] V. N. Baier and Y.F. Orlov, Sov. Phys. Dokl. 10 (1966) 1145.
- [18] A.A. Zholentz et al., Phys. Lett. 96B (1980) 214.
- {19] A.S. Artamonov et al., Phys. Lett. 118B (1982) 225.
- [20] Y.M. Shatunov and A.N. Skrinsky, Particle World, Vol. 1, No. 2 (1989) 35.
- [21] D.P. Barber et al., Phys. Lett. 135B (1984) 498.
- [22] W.W McKay et al., Phys. Rev. D29 (1984) 2483.
- [23] M. Froissart and R. Stora, Nucl. Instr. Meth. 7 (1960) 297.
- rections to Perturbed Spin Motion in Synchrotrons and Storage Rings", LAL-RT 87-09. [24] J. Buon, "Interference Effects between Depolarization Resonances and Higher-Order Cor
- [25] J.P. Koutchouk, "Spin Tune Shifts due to Solenoids", CERN SL-Note/93-26 (AP) (1993).
- SL/94-13 (AP) (1994). [26] R. Assmann and J.P. Koutchouk, "Spin Tune Shifts due to Optics Imperfections", CERN-
- 12-17, 1988, AIP Conf. Proc. No. 187, p. 1023. Proc. 8th International Symposium on High Energy Spin Physics, Minneapolis, September [27] I.A. Koop et al., "Investigation of the Spin Precession Tune Spread in the Storage Ring".
- LEP", J.M. Jowett Editor, CERN 91-02 (1991). [28] Report of the working group on high luminosities at LEP, "High-Luminosity Options for
- on LEP Performance, J. Poole Editor, CERN SL/93-19 (DI) (1993) 341. [29] J. Jowett, "Effect of Pretzel Orbits on Energy Calibration", Proc. of the Third Workshop
- 28 (1970). [30] M. Sands, "The Physics of Electron Storage Rings. An Introduction", SLAC-121 and UC
- ${31}$  H. Grote, C. Iselin, The MAD program V8.10, CERN-SL/90-13 Rev. 3 (AP).
- Second Workshop on LEP Performance, J. Poole Editor, CERN-SL/92-29 (DI) (1992). [32] G. Fischer and A. Hofmann, "Effects of tidal forces on the LEP energy", Proc. of the
- 1993 Particle Accelerator Conference, May 1993, Washington. [33] L. Arnaudon et al., "Effects of Tidal Forces on the Beam Energy in LEP". Proc. of the
- [24} P. Melchior, "The Tides of the Planet Earth", 2nd edition, Pergamon Press, 1983.
- Belgium. [35] Program and input data from P. Melchior, International Center for Earth Tides, Bruxelles,
- 07 (BI) (1994). [36] L. Arnaudon et al., "Effects of Terrestrial Tides on the LEP Beam Energy", CERN-SL/94-
- SL/94-14 (BI) (1994). [37] J. Wenninger, "Study of the LEP Beam Energy with Beam Orbits and Tunes". CERN-
- 105 (1993). [38] P. Collier, "Effect of QF-QD Compensation On LEP Beam Energy", CERN SL-MD Note
- [39] J. Poole, "Effects of QF-QD Compensator", CERN SL-MD Note 131 (1994).
- Conference, Nice, France (1990) and CERN SL/90-95. [40] R. Bailey et al., "LEP Energy Calibration", Proc. of the 2nd European Particle Accelerator
- (1993). [41] H. Schmickler, "Measurements of the Central Frequency of LEP", CERN SL-MD Note 89
- Working Group, Oct. 1992. [42] M. Placidi and J. Pinfold, Minutes of the 38th meeting of the LEP Energy Calibration
- Working Group, Feb. 1993. [43] L. Rolandi and M. Vandon, Minutes of the 50th meeting of the LEP Energy Calibration
- (1991) and CERN-AT-MA-91-03. measurements", Proc. of the 1991 Particle Accelerator Conference, San Francisco, CA [44] J. Billan et al., "Determination of the particle momentum in LEP from precise magnet
- Workshop on LEP Performance, J. Poole Editor, CERN-SL/93-19 (DI) (1993) 329. [45] K. Henrichsen, "Field Display and Flux-Loop Performance in 1992", Proc. of the Third
- Dec. 1993. [46] J. Gascon, Minutes of the 44th meeting of the LEP Energy Calibration Working Group,
- on LEP Performance, J. Poole Editor, CERN-SL/93-19 (DI) (1993) 325. [47] R. Forest, "Main Bend Power Converter Current Stability", Proc. of the Third Workshop
- Dec. 1993. [48] P. Renton, Minutes of the 46th meeting of the LEP Energy Calibration Working Group,
- Group, Oct. 1993. [49] A. Beuret at al., Minutes of the 39th meeting of the LEP Energy Calibration Working



rected for tide effects. quency scans.  $E_{pol}$  has been corcorrespond to the limits of the fre NMR showed a 4 MeV energy nets current supply. Only the duced on the main bending mag ing 23:55 current spikes were in "current spike experiment". Start energy measured by resonant de Figure 23: Evolution of  $E_{pol}$ , the

## A Appendix : Magnetic field reference

Tm at 45 GeV). Two devices are available for this task : running period, it is useful to be able to track relative changes of the LEP bending field ( $\sim 950$ To improve the understanding of the time evolution of the energy during fills or for a whole

- through all the main bending magnets with a resolution of  $\sim 0.5$  MeV. • The DCCTs (Direct Current Current Transformers [47]) measure the current flowing
- MeV. The reference magnet is connected in series with the main bending magnets. • A NMR probe measures the field inside a reference magnet with a resolution of  $\sim 0.1$

during 1993. fills and over time. The current setting of the LEP main bending magnets was extremely stable account for hysteresis effects in the magnets. Only tiny current variations were observed inside The reading of the DCCTs was very stable in 1993 for each energy point [48], but it cannot

the beam energy measurement from resonant depolarization (figure 23). This behavior might power supply. The NMR readings showed a clear  $+4$  MeV jump, but no effect was observed on a specific experiment was performed where current spikes were deliberately applied on the main determine if these jumps correspond also to a real field increase for the LEP bending magnets, be produced by current spikes on the power supply of the main bending magnets [49]. To in 5 to 10% of all physics fills. As a possible explanation, it was shown that such jumps can readings. All jumps correspond to an increase of the field. In 1993, such jumps were observed analysis of the NMR data shows sudden "jumps" of up to  $+5$  MeV between two consecutive the measures the field of the reference magnet and takes into account the magnetic hysteresis. The A better tracking of the bending field could be provided by the NMR probe. This probe



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data, jumps larger than 1 MeV between two consecutive readings have been corrected out. is still not clear if these correspond to real field variations. For the analysis of the calibration method. Unfortunately, no spontaneous jump was observed during energy calibrations and it the beams were lost after a spike with an amplitude of  $\sim 20$  MeV was applied with the same be due to a shielding effect of the beam pipe, but it cannot explain why in a previous test,

the extrapolated beam energy at the beginning of the experiment. 1849. Without the use of the NMR, there is a 2.5 MeV discrepancy between the measured and the beam energy is extrapolated backward in time starting from the last calibration in LEP fill that these slow drifts correspond to true field changes. This is demonstrated in figure 24 where drifts towards higher fields. The drifts can reach a few MeV after 12 hours. We have indications The NMR displays another characteristic behavior. During fills, it almost always shows

by comparing the results obtained using this reference or only the dipole current readings. during LEP runs. The resulting systematic error on the Z mass and width can be estimated These observations cast a doubt on whether the NMR can be used to track the bending field

beam energy ramp. The result of such an experiment was (figure 25) non-linearity can be measured with successive energy calibrations inside the same fill using a seen in figures 16 and 20. We define this as the non-linearity of the reference magnet. The energy measured by depolarization and by the NMR probe depends on the energy, as can be are aging, their average field calibration varies. As a consequence the difference between the LEP bending magnets at the time of the installation in the tunnel. Because the tunnel magnets The LEP reference magnet has been calibrated with the total dipole field of all the normal

(27) 
$$
\alpha_{nl} = \frac{(E_{pol} - E_{NMR})^{P+2} - (E_{pol} - E_{NMR})^{P-2}}{E_{pol}^{P+2} - E_{pol}^{P-2}} = (-3.20 \pm 0.47) \times 10^{-3}
$$

perturb the measurements of the non-linearity. non-linearity might have varied with time or that other unknown causes for energy variations lower value of  $\alpha_{nl} = (-1.3 \pm 0.6) \times 10^{-3}$  is obtained. But figure 20 seems to indicate that the From the average difference between energy calibrations at Peak-2 and Peak+2 (table 10), a

## B Appendix : Calibrated fill energies

the end of physics fills. experiments which are not always performed with the same LEP settings than calibrations at Fills marked with a  $*$  correspond to LEP Machine Development (MD) calibrations or special temperature  $T_{mag}$  and the setting of the quadrupole compensation loop  $I_{Qfd}$  are also indicated. as indicated in table 9.  $\sigma_E$  is dominated by the extrapolation errors. The average magnet The RMS error  $\sigma_E$  includes the contributions from the errors on the correction coefficients  $E_{pol}$  are corrected to the reference values of the different parameters according to table 9. The following three tables contain the list of energies for all calibrated LEP fills. The energies

Fill	Date	$E_{pol}$ (MeV)	$\sigma_E$ (MeV)	$T_{mag}$ (deg)	$I_{Qfd}(\text{A})$
1579*	02-06-93	44720.6	1.6	23.16	
1589*	04-06-93	44723.5	1.2	23.01	
1616*	14-06-93	44712.2	0.9	23.29	
1617*	14-06-93	44713.5	0.9	23.25	
1636*	20-06-93	44717.8	1.4	22.84	
1637*	21-06-93	44712.3	1.2	23.18	
1660	05-07-93	44717.3	0.4	23.85	32.
1674	12-07-93	44718.9	0.6	23.87	32.
1694	19-07-93	44720.4	1.6	24.03	$-40.$
1734*	04-08-93	44709.0	0.6	23.56	32.
1745	12-08-93	44709.8	1.5	23.90	$-40.$
1764	21-08-93	44708.2	1.5	24.07	$-40.$
1771*	28-08-93	44709.6	1.4	22.79	32.
1772*	29-08-93	44709.0	1.2	22.98	32.
		44711.3	1.0	23.23	32.
		44713.0	0.7	23.44	32.
1794	04-09-93	44717.2	1.5	23.75	$-40.$
1837	05-10-93	44722.2	0.9	23.55	1.
1849	11-10-93	44726.6	0.5	23.73	32.
1861	$16-10-93$	44729.4	0.5	23.76	32.
1892	29-10-93	44722.8	0.4	23.83	32.
1927	09-11-93	44715.7	0.6	23.60	32.
1928	$10-11-93$	44715.8	0.5	23.75	32.
1937	15-11-93	44710.9	0.8	23.76	$-1.$

Table 11: Energies for all Peak-2 fills calibrated in 1993. In fill 1745, the beam energy was ramped from Peak-2 to Peak and Peak+2. For fill 1772 (the third experiment on the temperature coefficient) the 3 average energies before and after each energy jump are shown. For the first six fills,  $I_{Qfd}$  was not monitored.

Fill	Date			$\left E_{pol}~(\textrm{MeV})~\right ~\sigma_E~(\textrm{MeV})~\left ~T_{mag}~(\textrm{deg})~\right $	$I_{Qfd}(\text{A})$
1745*	$04 - 08 - 93$	45594.2	1.5	23.91	$-41.$
1935	14-11-93	45593.8	0.8	23.79	

Table 12: Energies for the 2 Peak fills calibrated in 1993. In fill 1745, the beam energy was ramped from Peak-2 to Peak and Peak+2.

Fill	Date	$E_{pol}$ (MeV)	$\sigma_E$ (MeV)	$T_{mag}$ (deg)	$I_{Qfd}(\text{A})$
1658	03-07-93	46512.1	0.4	23.81	33.
1672	10-07-93	46510.4	0.4	24.01	33.
1698	23-07-93	46510.4	1.5	24.14	$-41.$
1717	30-07-93	46509.3	1.5	24.21	$-41.$
1745*	04-08-93	46502.2	1.5	23.92	$-41.$
1761	18-08-93	46504.5	1.5	24.23	$-41.$
1811	12-09-93	46506.2	1.5	24.00	$-41.$
1845	10-10-93	46509.6	0.4	23.73	33.
1876	21-10-93	46515.4	0.5	23.84	33.
1888	26-10-93	46518.5	0.4	23.86	33.
1891	28-10-93	46514.6	0.4	23.90	33.
1930	11-11-93	46505.4	0.9	23.90	0.

Table 13: Energies for all Peak+2 fills calibrated in 1993. In fill 1745, the beam energy was ramped from Peak $-2$  to Peak and Peak $+2$ .

 $\mathcal{A}^{\mathcal{A}}$  and  $\mathcal{A}^{\mathcal{A}}$  are the subset of the set of  $\mathcal{A}$ 

 $\label{eq:1} \left\langle \left\langle \hat{r} \right\rangle \right\rangle = \left\langle \hat{r} \right\rangle \left\langle \hat{r}$ 

 $\mathcal{L}=\frac{1}{2} \sum_{i=1}^{n} \mathcal{L}^{(i)}_{i} \mathcal{L}^{(i)}_{i}$  , where  $\mathcal{L}^{(i)}_{i}$ 

 $\mathcal{L}^{\text{max}}(\mathbf{A})$ 

 $\sim 10^6$