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Limits on neutrino Lorentz violation from multimessenger observations of TXS 0506+056



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ABSTRACT

The observation by the IceCube Collaboration of a high-energy ($E \gtrsim 200$ TeV) neutrino from the direction of the blazar TXS 0506+056 and the coincident observations of enhanced γ -ray emissions from the same object by MAGIC and other experiments can be used to set stringent constraints on Lorentz violation in the propagation of neutrinos that is linear in the neutrino energy: $\Delta v = -E/M_1$, where Δv is the deviation from the velocity of light, and M_1 is an unknown high energy scale to be constrained by experiment. Allowing for a difference in neutrino and photon propagation times of ~ 10 days, we find that $M_1 \gtrsim 3 \times 10^{16}$ GeV. This improves on previous limits on linear Lorentz violation in neutrino propagation by many orders of magnitude, and the same is true for quadratic Lorentz violation.

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It is desirable to probe fundamental physical principles as sensitively as possible, and Lorentz invariance is no exception. Specifically, one may ask how accurately we know that different species of massless particles travel at the speed of light, and how accurately we know that massive particles travel at the same speed in the high-energy limit. Over the past two decades, since the publication of [1], considerable effort has been put by many experimental collaborations into constraining different forms of Lorentz violation, and specifically a linear coefficient M_1 in the velocity vof energetic photons: $\Delta v = -E/M_1$, using distant time-dependent astrophysical sources of energetic photons such as pulsars, gammaray bursts (GRBs) and active galactic nuclei (AGNs). However, analyses of possible Lorentz violation in photon propagation have been

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beset by difficulties in disentangling intrinsic time delays in the sources from time delays accumulated during propagation, and we consider that the strongest robust limit on M_1 for photons is between 10^{17} and 10^{18} GeV [2]. There have also been analyses of possible Lorentz violation in neutrino propagation from Supernova 1987A and in a terrestrial neutrino beam, but these are sensitive only to $M_1 \sim 2 \times 10^{11}$ GeV and potentially $\sim 4 \times 10^8$ GeV, respectively [3]. More recently, data on the first observed black-hole binary merger [5] were used to set the much weaker limit $M_1 \gtrsim 100$ keV for graviton propagation [6], and the near-coincidence of gravitational waves and γ -rays from a neutron-star binary merger has been used to establish that their velocities are the same to within $\sim 10^{-17}$ [7].

Very recently, the IceCube Collaboration has reported the observation of an ultra-high-energy neutrino from the direction of the blazar TXS 0506+056, and together with a number of other groups, most notably the MAGIC Collaboration, have reported [8] an enhanced level of activity in γ -ray and photon emission from

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this source, which is located at a distance $\sim 4 \times 10^9$ ly. As we discuss in this paper, the great distance of TXS 0506+056 and the high energy $\gtrsim 200$ TeV of the observed high-energy neutrino, in conjunction with the γ -ray observations, provides unique sensitivity to Lorentz violation in neutrino propagation, which almost rivals that to linear Lorentz violation in photon propagation.¹ The sensitivity to linear Lorentz violation in neutrino propagation is to $M_1 \gtrsim 3 \times 10^{16}$ GeV, approaching the Planck energy scale that might be characteristic of the possible quantum-gravity effects that were the original motivation for [1].

We first review the observations of TXS 0506+056 reported by the IceCube Collaboration and the teams studying its electromagnetic emissions [8]. The primary observation by IceCube was that of a single neutrino with energy ~ 290 TeV (90% CL lower limit 183 TeV) on 22 September 2017, dubbed IceCube-170922A, coming from a direction within 0.1° of the catalogued γ -ray source TXS 0506+056, whose redshift $z = 0.3365 \pm 0.0010$. Several γ -ray experiments, notably MAGIC, VERITAS, HESS, Fermi-LAT, AGILE and Swift made observations showing that TXS 0506+056 was in a flaring state over a period within about 10 days of IceCube-170922A [8]. In particular, MAGIC reported a $6.2-\sigma$ excess within this time frame. The IceCube Collaboration has also reported an excess of neutrinos observed earlier from the direction of TXS 0506+056, confirming this as the source of IceCube-170922A [13], and analyses have supported the hypothesis that a single astrophysical mechanism is responsible for emitting both the neutrino and the γ -rays [14].

The similarity in arrival times of IceCube-170922A and the electromagnetic emissions can be used immediately to estimate the corresponding sensitivity to a difference $\Delta v_{\nu\gamma}$ in the propagation speeds *in vacuo* of the neutrino and photons, assuming that both speeds are independent of energy. We assume a distance of 4×10^9 ly and an illustrative time difference of 10 days,² so that $\Delta v_{\nu\gamma}/c \sim 10$ days/ 4×10^9 years $\sim 10^{-11.3}$ This is six orders of magnitude worse than the corresponding constraint on the difference in propagation speeds of gravitational waves and photons derived from the near-simultaneous observations of the binary neutron-star merger: $\Delta v_{GW\gamma} \lesssim 10^{-17}$ [7]. However, it is much better than the corresponding sensitivity to an energy-independent $\Delta v_{\nu\gamma}$ from the observations of neutrinos emitted during the collapse of supernova 1987A: $\Delta v_{\nu\gamma} \lesssim 4$ hours/1.5 $\times 10^5$ years $\sim 3 \times 10^{-9.4}$

An energy-independent difference between the velocities of neutrinos (or gravitational waves) and photons would require the extremely radical step of abandoning the framework of special relativity. A less radical hypothesis would be that Lorentz invariance is an emergent symmetry in the low-energy limit, but is subject to modification that increases with energy. This is indeed the suggestion that has been made in a number of different theoretical frameworks, including the 'space-time foam' expected in models of quantum gravity [15], phenomenological models suggested by features of cosmic-ray physics [16] and other considerations [17], the suggestion that Lorentz invariance may be broken spontaneously [18,19], models of loop quantum gravity [20], doubly-special relativity theories [21] and quantum field theories of the Lifshitz type [22]. In such frameworks, Lorentz invariance is a good symmetry in the low-energy limit, but is violated increasingly at high energies. As discussed in [24], the interactions of particles with space-time foam are not represented by an effective field theory (EFT) with higher-dimensional operators such as the standard model extension [18], since they correspond to time-space uncertainty effects. Since other models of Lorentz violation may also not fall within an EFT framework, we take here a phenomenological approach in which the energy dependence of Lorentz violation is kept free, and the magnitude is allowed to be different for different particle species.

The first such possibility that we consider is that $\Delta v_{\nu\nu}$ increases linearly with energy: $\Delta v_{\nu\gamma} = -E/M_1$.⁵ The possibility of such a linear violation of Lorentz invariance was raised in [1, 24] on the basis of intuition about the properties of space-time foam suggested by a heuristic string-inspired model of quantumgravitational fluctuations in space-time. In such a case, one's first guess could be that M_1 would be comparable to the Planck mass: $M_1 \sim M_P \simeq 10^{19}$ GeV. However, the value of M_1 would depend in a string-inspired model on unknown quantities such as the string coupling, the density of defects in space-time, and the strength of particle interactions with such defects, which may not be universal between different particle species [25], so we maintain phenomenological open minds about the possible magnitude of M_1 . The model of space-time foam proposed in [24] would suggest that the velocities of neutrinos would deviate from the low-energy velocity of light less than photons, so that (in an obvious notation) $M_{1,\nu} \gg M_{1,\nu}$, because the photon would have stronger interactions with the space-time defects. This is because, in such a stringy model of space-time foam, only species that carry no non-trivial quantum numbers under the standard model group have unsuppressed interactions with the foam, in which case the fact that neutrinos are fermions with non-trivial $SU(2)_L$ properties renders space-time foamy effects invisible to them. However, initially we will be agnostic whether the photon velocity or the neutrino velocity deviates more from the low-energy velocity of light. When they are comparable, $M_1 = (M_{1,\gamma} \times M_{1,\nu})/(M_{1,\gamma} - M_{1,\nu})$, but when there is a hierarchy between them, $M_1 \rightarrow$ the smaller of $M_{1,\gamma}$ and $M_{1,\nu}$.

We recall that a difference in velocity $\Delta v = -E/M_1$ induces a difference in arrival time $\Delta t = \Delta v \times D = (E \times D)/M_1$, where *D* is the propagation distance. For our numerical purposes, we assume the value $E_{\nu} = 200$ TeV for the energy of the event IceCube-170922A [8], and note that the energies of the γ -rays measured by MAGIC and other experiments are negligible in comparison. A simple order-of-magnitude estimate then yields a sensitivity to

$$M_1 \gtrsim \frac{H_0^{-1}}{\Delta t} E \int_0^{z_{\rm src}} \frac{(1+z)}{\sqrt{\Omega_\Lambda + \Omega_M (1+z)^3}} dz \approx 3 \times 10^{16} \, \text{GeV}\,, \qquad (1)$$

which is over 6 orders of magnitude stronger than the limit obtained previously [3] from an analysis of the neutrino signal from

¹ For a previous test of Lorentz violation assuming that IceCube neutrino IC 35 [9] was emitted by a flare of the AGN PKS B1424-418 [10], see [11]. In that case, the chance coincidence probability was ~ 5%, so the identification could not be considered conclusive. We note also that a correlation between a flaring γ -ray source and the IceCube-160731 neutrino event was reported in [12], but it was not possible to identify the potential counterpart and make a quantitative analysis.

² The redshift of TXS 0506+056 is not very large, and the estimates of Δt and the energy of the neutrino are not very accurate, so this estimate does not include the small effects associated with the expansion of the Universe during propagation.

³ Henceforth, we use natural units in which the conventional velocity of light c = 1.

⁴ We note that a Fermi all-sky variability analysis reported significant brightening of TXS 0506+056 in the GeV band some five months previous to the observation of IceCube-170922A [8]. A conservative approach would be to allow for a time difference of 150 days between the photon and neutrino propagation times, which would relax our bound on $\Delta v_{\nu\gamma}$ by a factor \simeq 15. However, it would still be over an order of magnitude stronger than the bound from supernova 1987A.

⁵ Constraints on e^+e^- pair production *in vacuo* require $\Delta v < 0$ [23], as expected in the model of [24].

supernova 1987A.⁶ The sensitivity (1) is, nevertheless, an order of magnitude weaker than the robust limit on photon Lorentz violation [2], so refers directly to the neutrino.

It is instructive also to compare the sensitivity (1) to the possible improvement in the supernova limit, should another corecollapse supernova be observed in our galaxy. Multi-dimensional simulations of such events suggest that their neutrino emissions might exhibit time variations in the millisecond range, in which might attain case measurements a sensitivity to $M_1 \sim 2 \times 10^{13}$ GeV [26], still 3 orders of magnitude less than the IceCube-170922A/MAGIC sensitivity (1). This sensitivity is also far beyond that we can envisage using a terrestrial neutrino beam. It was estimated using the timing capabilities of the OPERA detector and assuming that timing information could be available for neutrino events upstream in rock that a sensitivity to $M_1 \sim 4 \times 10^8$ GeV could be attained [3].⁷ Thus the IceCube-170922A/MAGIC sensitivity seems to outclass the capabilities of terrestrial experiments as well as possible future supernova observations.

One can also consider a possible quadratic violation of Lorentz invariance: $\Delta v = -E^2/M_2^2$, which would be an option in some of the alternative models of Lorentz violation mentioned above [16–20, 22]. In this case, the IceCube-170922A/MAGIC sensitivity would be to

$$M_2 \gtrsim \left[\frac{3}{2}\frac{H_0^{-1}}{\Delta t}E^2\int_0^{z_{\rm src}} \frac{(1+z)^2}{\sqrt{\Omega_\Lambda + \Omega_M (1+z)^3}}dz\right]^{1/2} \approx 10^{11} \,\,{\rm GeV}\,,$$
(2)

which is over 5 orders of magnitude stronger than the corresponding limit from supernova 1987A [3]. In the case of quadratic Lorentz violation, the supernova 1987A limit was estimated to be to $M_2 \sim 4 \times 10^4$ GeV, the possible sensitivity of a future galactic supernova event was estimated to be to $M_2 \sim 10^6$, and the potential sensitivity of a terrestrial experiment was estimated to be to $M_2 \sim 7 \times 10^5$ GeV.⁸ Again, the large distance of TXS 0506+056 and the high energy of the IceCube-170922A event enable it to outclass the competition.

For completeness, before closing we comment briefly on previous discussions of neutrino Lorentz violation in the context of EFT and the Standard Model Extension (SME) [18]. This has been mentioned [31] as an explanation of a possible drop in PeV neutrinos suggested by IceCube data [32], which might correspond to a SME dimension-6 term with coefficient $\geq -5.2 \times 10^{-35} \text{ GeV}^{-2}$ (see also [33] for a review). However, we regard the existence of this drop and its interpretation as questionable. An overview of this and other aspects of SME applications to neutrinos is given in [34], though without a quantitative discussion.

We conclude that the advent of multimessenger neutrino/photon astronomy [8,13] has not only launched a new era in the study of the origins of high-energy cosmic rays, but also made possible a breakthrough in the exploration of Lorentz symmetry using neutrinos. We may anticipate that more coincidences between high-energy neutrino events and electromagnetic emissions will be observed, enabling the rough estimates made here to be refined and improved. Such coincidences would contribute to fundamental physics as well as resolving important issues in astrophysics.

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 $^{^7}$ In fact, we are unaware of neutrino experiments that have sought to test Lorentz invariance in the way proposed here. For alternative searches for Lorentz violation using neutrinos, see [27–29], see also [30,31]. We are grateful to Francesca Di Lodovico, Brian Rebel and Jenny Thomas for discussions on this subject.

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