

Dimension-six electroweak top-loop effects in Higgs production and decay

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ABSTRACT: We study the next-to-leading order electroweak corrections to Higgs processes from dimension-six top-quark operators in the Standard Model Effective Field Theory approach. We consider the major production channels, including WH , ZH , and VBF production at the LHC, and ZH , VBF production at future lepton colliders, as well as the major decay channels including $H \rightarrow \gamma\gamma, \gamma Z, Wl\nu, Zll, b\bar{b}, \mu\mu, \tau\tau$. The results show that within the current constraints, top-quark operators can shift the signal strength of the loop-induced processes, i.e. $H \rightarrow \gamma\gamma, \gamma Z$, by factors of $\sim \mathcal{O}(1) - \mathcal{O}(10)$, and that of the tree-level processes, i.e. all remaining production and decay channels, by $\sim 5 - 10\%$ at the LHC, and up to $\sim 15\%$ at future lepton colliders. This implies that essentially all Higgs channels have started to become sensitive to top-quark couplings, and in particular, Higgs observables at high luminosity LHC as well as future lepton colliders, even below the $t\bar{t}$ threshold, will improve our knowledge of top-quark couplings. We derive the sensitivities of Higgs measurements to top-quark operators at the high luminosity LHC, using projections for both inclusive and differential measurements. We conclude that treating the dimension-six top-quark sector and the Higgs/electroweak sector separately may not continue to be a good strategy. A global analysis combining Higgs and top-quark measurements is desirable, and our calculation and implementation provide an automatic and realistic simulation tool for this purpose.

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1 Introduction

Deviations in the top-quark and Higgs couplings are often studied within the Standard Model Effective Field Theory (SMEFT) approach [1–3]. Even though the SMEFT is a global approach where different measurements are supposed to be combined and studied together, in practice, several main sectors are often considered separately. Dimension-six (dim-6) operators in the top-quark sector are analysed with top measurements [4–15], while those in the Higgs sector are analysed with Higgs and triple gauge-boson coupling (TGC) measurements [16–23], the rationale behind being that the interplay between the two sectors is negligible with the accuracy of the current measurements.

This assumption may not continue to be true as the LHC experiments improve on higher integrated luminosities and higher energies. Once the precision reaches the point where loop corrections become relevant, the top- and the Higgs-sectors should not be viewed separately. In particular, top-quark operators could play a role in Higgs measurements through electroweak (EW) top and bottom loops and have non-trivial impacts. The goal of this paper is to answer the following two questions: 1) will this happen at the LHC,

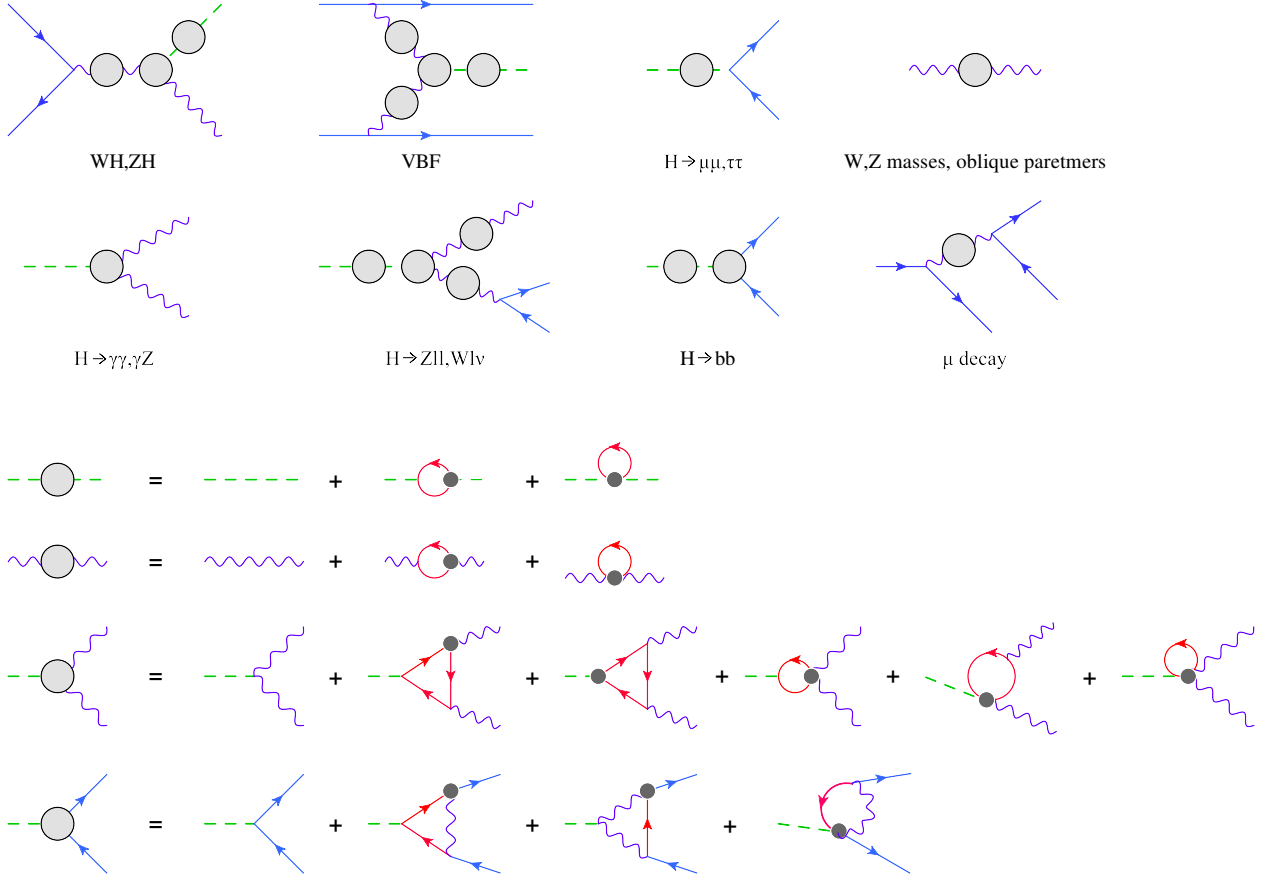


Figure 1. Electroweak contributions from two-fermion top-quark operators to the production and decay of the Higgs boson, the oblique parameters, and the SM input parameters which we will take as M_W , M_Z and G_F (from muon decay). Here blue fermion lines represent light fermions, and red fermion lines represent the top quark. Large grey blobs denote collectively the SM contributions and dim-6 EW corrections from top-quark loops, as illustrated below the processes. Dark small blobs represent the dim-6 operator insertions. Diagrams that can be obtained by crossing legs or reversing fermion flows are not shown.

and/or future lepton colliders? and 2) can Higgs measurements help to constrain top-quark couplings?

To answer these two questions, in this work we compute the EW loop-induced contributions from dim-6 top-quark two-fermion operators in the following main Higgs production and decay processes:

production at LHC: VBF, WH , ZH

production at lepton collider: ZH , VBF

decay: $H \rightarrow \gamma\gamma$, γZ , $Wl\nu$, Zll , $b\bar{b}$, $\mu^+\mu^-$, $\tau^+\tau^-$.

All relevant contributions are shown in Figure 1.

Loop corrections in the SMEFT with dim-6 operators have been studied in the literature. The loop contributions in $gg \rightarrow H$ and $H \rightarrow gg$ have been presented in [24, 25]. Some of the decay processes, including $H \rightarrow WW^*, ZZ^*, \gamma\gamma$ and $Z\gamma$, have been studied in Refs. [26–29]. All other results in this work, in particular the next-to-leading order (NLO) EW corrections for the production channels, are new and are relevant for future Higgs and top studies at the LHC. Note that loop corrections to $H \rightarrow b\bar{b}$ and $\tau^+\tau^-$ from four-fermion operators have been computed in [30], while the NLO QCD corrections to WH, ZH, VBF and $t\bar{t}H$ production processes are also known [31–33], but they are not relevant for the purpose of this work. We do not consider $t\bar{t}H$ production because its leading contribution comes from the tree level top Yukawa operator. Our approach is based on the MadGraph5_aMC@NLO (MG5_aMC) framework [34]. It is part of the ongoing efforts of automating NLO EFT simulations for colliders [32, 33, 35–40], and is a first step towards including NLO EW corrections.

Formally, the top loop contributions in Higgs measurements are part of the NLO EW corrections to the dim-6 operators. One might think that the effects must be small relative to the tree level contributions from other EW and Higgs operators. However, they could be important because the top quark operators enter for the first time at the one-loop level, and in this sense these are leading order (LO) contributions. Therefore it is important to know their sizes. An interesting and similar example in the Higgs sector is that one can set bounds on the Higgs self coupling λ_3 , by using the λ_3 -dependent EW corrections, which enter the single Higgs boson cross section starting at the one-loop level [41–45]. The problem we consider in this work is in analogy. The one-loop contribution of some top operator, O_t , relative to the tree level ones from another, say, Higgs operator O_H , are proportional to the ratio of their coefficients, i.e. $\mathcal{O}(\alpha_{EW}C_t/C_H)$ instead of just $\mathcal{O}(\alpha_{EW})$. Given that the current constraints on the Higgs operators are in general much stronger than those on the top operators, it is likely that the C_t/C_H factor enhances the top-loop induced contributions, so that they are of more physical relevance. This is one of the reasons why we would like to focus on the top-quark operators at one loop instead of the regular NLO EW corrections to Higgs and EW operators, as the latter are naively of order $\mathcal{O}(\alpha_{EW})$, and therefore less important. Another reason is that there are processes that are loop-induced in the SM, such as $gg \rightarrow H$ and $H \rightarrow \gamma\gamma$, and for them the top-loop induced dim-6 contributions are not small.

The collider sensitivity to the loop contributions from effective operators may depend on our assumptions. Let us briefly comment on this. Once including one-loop top operator contributions, the cross section (or decay width) of the Higgs boson takes the following form:

$$\sigma = C_H(\mu_{EFT})\sigma_{\text{tree}} + C_t \frac{\alpha_{EW}}{\pi} \left(\log \frac{Q^2}{\mu_{EFT}^2} \sigma_{\text{log}} + \sigma_{\text{fin}} \right) \quad (1.1)$$

where $C_H(\mu_{EFT})$ is the coefficient of some Higgs operator, O_H , that enters the process at the tree level and μ_{EFT} is the scale at which it is defined. C_t is the coefficient of some top-quark operator O_t which mixes into O_H . Q^2 is the energy of the process. A measurement of σ will give us information about a linear combination of C_H and C_t . Even though one

cannot immediately infer the constraint on C_t , this piece of information itself is already useful, as it can be combined with other measurements, and eventually the degeneracy will be lifted. It is however important to have all measured quantities in such a fit expressed in terms of operator coefficients defined at a common scale μ_{EFT} , as one can clearly see from Eq. (1.1), the linear combination of C_H and C_t depends on the scale μ_{EFT} .

In this work, as a first step, we will focus on studying the collider sensitivity to the loop effects. We do not perform any global fit, and we will ignore the C_H coefficient, except for two Higgs operators which we will use as examples to demonstrate that distinguishing between tree-level and loop-level contributions is in principle possible only by using Higgs data. The experimental sensitivity on C_t depends on the scale μ_{EFT} at which C_H is set to 0. We consider two options:

- Take $\mu_{EFT} = \Lambda$. The underlying assumption is that new physics effects at high scale are mainly captured by top-quark operators. The large scale μ_{EFT} in this case can be considered as a proxy of renormalisation group (RG) running and mixing effects to the scale of measurement. The contributions from C_t will be relatively large due to the logarithmic terms, leading to relatively tighter limits. This however does not mean that the finite terms are not important, see for example discussions in [26, 33, 38]. The disadvantage of this approach is that resulting limits rely on strong assumptions, and in particular it is difficult to combine these limits with other analyses, as the assumptions at scale Λ can be different.
- Take $\mu_{EFT}^2 = Q^2$, where Q is the scale of the measurement. This is a bottom-up point of view, where the coefficient C_H is assumed to have already evolved down to scale Q^2 to absorb the σ_{\log} contributions. The resulting sensitivity will become weaker, but it is a fair estimate of the expected sensitivity in a global analysis. As we will discuss later, this is because the finite terms are crucial for discriminating the top-loop induced effects from the tree-level contributions of other Higgs operators, which cannot be avoided in a real bottom-up global SMEFT fit.

In this work we will present results for both options. For the first we will take $\mu_{EFT} = \Lambda = 1$ TeV and for the second $\mu_{EFT} = m_H = 125$ GeV. Besides, we will also show that, even with Higgs operators included, by combining observables at different energies or using differential measurements, it is possible to lift the degeneracy between top and Higgs operators. This is because the finite term $\sigma_{fin}/\sigma_{tree}$ is process dependent, unlike the logarithmic term $\sigma_{log}/\sigma_{tree}$.

While we are mostly interested in LHC physics, for completeness we will also discuss the same effects at possible future lepton colliders. An e^+e^- collider is an ideal machine for determining possible deviations in the Higgs sector. Several proposals of such Higgs factories have been made, including the Circular Electron Positron Collider (CEPC) in China [46], the Future Circular Collider with e^+e^- (FCC-ee) at CERN [47], and the International Linear Collider (ILC) in Japan [48]. The Compact Linear Collider (CLIC) at CERN [49] could also run at higher center-of-mass energies. The precision on Higgs signal strengths at these machines could reach $\mathcal{O}(1\%) - \mathcal{O}(0.1\%)$ level, and therefore one has to carefully

investigate possible loop contributions from deviations in the top-quark sector. We will show that our results imply that future lepton colliders will be sensitive to top-quark couplings even below the $t\bar{t}$ threshold.

This paper is organised as follows. In Section 2 we discuss the relevant effective operators in this study. In Section 3 we briefly outline our calculation strategy, implementation and validation, and in particular discuss the renormalisation scheme. We present our major numerical results in Section 4. Section 5 is devoted to a discussion of the physics implications of our results, including impacts at the LHC, at future lepton colliders, the potential sensitivities at high-luminosity LHC, possible improvements by using differential distributions, and the possibilities to discriminate between tree-level and loop-level operator contributions. In Section 6 we conclude.

2 Operators

We consider the effective Lagrangian at dim-6

$$\mathcal{L}_{EFT} = \mathcal{L}_{SM} + \sum_i \frac{C_i}{\Lambda^2} O_i + \dots \quad (2.1)$$

Two classes of operators are relevant in this work. The first is the set of two-fermion top-quark operators that could enter Higgs measurements via loop effects, including [50]

$$\begin{aligned} O_{t\varphi} &= \bar{Q}t\tilde{\varphi} (\varphi^\dagger\varphi) + h.c., & O_{\varphi Q}^{(1)} &= (\varphi^\dagger \overleftrightarrow{D}_\mu \varphi)(\bar{Q}\gamma^\mu Q), \\ O_{\varphi Q}^{(3)} &= (\varphi^\dagger \overleftrightarrow{D}_\mu^I \varphi)(\bar{Q}\gamma^\mu \tau^I Q), & O_{\varphi t} &= (\varphi^\dagger \overleftrightarrow{D}_\mu \varphi)(\bar{t}\gamma^\mu t), \\ O_{\varphi tb} &= (\tilde{\varphi}^\dagger iD_\mu \varphi)(\bar{t}\gamma^\mu b) + h.c., & O_{tW} &= (\bar{Q}\sigma^{\mu\nu} \tau^I t) \tilde{\varphi} W_{\mu\nu}^I + h.c., \\ O_{tB} &= (\bar{Q}\sigma^{\mu\nu} t) \tilde{\varphi} B_{\mu\nu} + h.c., \end{aligned} \quad (2.2)$$

and we define

$$O_{\varphi Q}^{(+)} \equiv \frac{1}{2} (O_{\varphi Q}^{(1)} + O_{\varphi Q}^{(3)}) \quad O_{\varphi Q}^{(-)} \equiv \frac{1}{2} (O_{\varphi Q}^{(1)} - O_{\varphi Q}^{(3)}), \quad (2.3)$$

so that the operators $O_{\varphi Q}^{(+)}$ and $O_{\varphi Q}^{(-)}$ modify the Zbb and Ztt couplings respectively. The coefficient of $O_{\varphi Q}^{(+)}$ is constrained by the LEP experiment [51], but we include it for a complete study of the loop-induced sensitivity. Four-fermion operators could have similar loop-effects in Higgs measurements, but we will leave them for future study. The chromo-dipole operator,

$$O_{tG} = (\bar{Q}\sigma^{\mu\nu} T^A t) \tilde{\varphi} G_{\mu\nu}^A \quad (2.4)$$

enters ggH at one loop. Since its contribution has been studied up to two loops [25], we will not include it in this study. When presenting the physics impact in Section 5, the ggH loop will be included as it is the dominant production channel, but we will only consider the contribution from $O_{t\varphi}$, which is a simple rescaling factor.

The above operators are the main objects of this study. To correctly take into account their impact on Higgs measurements, RG running and mixing effects [52–54] need to be

considered. We thus introduce the second set of operators that enter the same processes at the tree level and will provide the corresponding counter terms:

$$\begin{aligned}
O_{\varphi WB} &= \varphi^\dagger \tau^I \varphi W_{\mu\nu}^I B^{\mu\nu}, & O_{\varphi W} &= \varphi^\dagger \varphi W_{\mu\nu}^I W^{I\mu\nu}, \\
O_{\varphi B} &= \varphi^\dagger \varphi B_{\mu\nu} B^{\mu\nu}, & O_{\varphi \square} &= (\varphi^\dagger \varphi) \square (\varphi^\dagger \varphi), \\
O_{\varphi D} &= (\varphi^\dagger D^\mu \varphi)^* (\varphi^\dagger D_\mu \varphi), & O_W &= i D^\mu \varphi^\dagger \tau^I D^\nu \varphi W_{\mu\nu}^I, \\
O_B &= i D^\mu \varphi^\dagger D^\nu \varphi B_{\mu\nu}, & O_{b\varphi} &= (\varphi^\dagger \varphi) \bar{Q} b \varphi, \\
O_{\mu\varphi} &= (\varphi^\dagger \varphi) \bar{l}_2 e_2 \varphi, & O_{\tau\varphi} &= (\varphi^\dagger \varphi) \bar{l}_3 e_3 \varphi,
\end{aligned} \tag{2.5}$$

where the subscripts 2,3 for the lepton doublet l and singlet e are flavour indices. The above operators are sufficient to provide all mixing counter terms needed in this study to guarantee physically meaningful results at the loop level. Note that in the Warsaw basis [50], top quark operators could mix into light-fermion operators, in particular the ones that involve EW gauge bosons. This is slightly inconvenient for a study of the loop-induced Higgs couplings, as some of the counter terms manifest as light-fermion interactions. Fortunately, these effects turn out to be universal, in the sense that they can be captured by dim-6 operators which involve SM bosons only, up to suitable field redefinitions [55]. For this reason, instead of introducing these light-fermion operators in our basis, we follow [56] and include O_W and O_B with a slightly different convention. This means we replace the following two combinations of Warsaw basis operators

$$O_{\varphi q}^{(3)} + O_{\varphi l}^{(3)}, \tag{2.6}$$

$$\frac{1}{6} O_{\varphi q}^{(1)} - \frac{1}{2} O_{\varphi l}^{(1)} + \frac{2}{3} O_{\varphi u} - \frac{1}{3} O_{\varphi d} - O_{\varphi e}, \tag{2.7}$$

by O_W and O_B , using the equations of motion. The counter terms provided by them are equivalent, but the physical interpretation is more clear. Note that these two operators project out the flat directions from the precision EW tests [57, 58], and so in this basis it is clear that the precision constraints only apply to two operators, i.e. $O_{\varphi WB}$ and $O_{\varphi D}$, which is convenient for our analysis. Note also that in this basis the mixing pattern of the EW operators becomes different than in the Warsaw basis.

Throughout the paper we will refer to the first class (Eq. 2.2) as top operators, and the second (Eq. 2.5) as Higgs operators.

3 Calculation and renormalisation

In this section we briefly describe our calculation for the EW corrections in Higgs processes and precision EW observables from top-quark operators. All relevant Feynman diagrams are shown in Figure 1.

At dim-6 at one loop, of all the operators we study, the $gg \rightarrow H$ production and $H \rightarrow gg$ decay channels receive a contribution only from $O_{t\varphi}$, which is easy to include with a rescaling factor. All other processes, except for $H \rightarrow bb$, share the same kinds of contributions from top-loop operators, shown as the large grey circles in Figure 1. Thus a very efficient way

to obtain results is to implement all these contributions in MG5_aMC [34], with the help of FeynRules [59], and use the reweighting functionality [60] in MG5_aMC to compute the dim-6 loop contributions. The reweighting is particularly simple in this case because there are no real corrections. For the loop computation we need to provide the corresponding electroweak UV and R2 counter terms. The R2 counter terms need to be provided only for the HH , VV two-point functions and HVV three-point functions. These are computed by using FeynArts [61] interfaced with FeynCalc [62, 63]. For terms involving γ^5 we follow the scheme of [64–66], and have checked that our results for the SM pieces agree with Ref. [67]. The UV counter terms come from the renormalisation of the theory, which we will describe in the following subsections. In particular, the UV counter terms needed for our purpose are HH , VV , HVV , ffV , and ffH .

Finally, $h \rightarrow bb$ has a unique contribution from $W - t$ loops, not shared with other channels. We compute it by using FeynArts and FormCalc [68]. The renormalisation is similar to the other channels. For the contribution from the $O_{\varphi tb}$, our result for the finite part agrees with that of Ref. [9].

We have validated our implementation by computing the $H \rightarrow 4l$ and $H \rightarrow 2l2\nu$ decay processes and comparing with FormCalc. The implementation provides a simulation tool for all processes shown in Figure 1, allowing us to generate events associated with weights corresponding to dim-6 top-loop contributions, apart from $H \rightarrow b\bar{b}$. Both total rates as well as differential distributions can be efficiently obtained from the weighted events. Note that this implementation can also be used to compute other non-Higgs processes involving dim-6 top loops, such as Z -pole processes as well as Drell-Yan at the LHC, provided that no additional counter terms are needed.

3.1 Dim-6 renormalisation

The dim-6 operator coefficients can be renormalised using the \overline{MS} scheme

$$C_i \Rightarrow Z_{ij} C_j = C_i + \delta Z_{ij} C_j, \quad (3.1)$$

$$\delta Z_{ij} = \frac{\alpha}{2\pi} \Delta(\mu_{EFT}) \frac{1}{\epsilon} \gamma_{ij} \quad (3.2)$$

with δZ_{ij} the anomalous dimension matrix, which has been obtained in Refs. [52–54] in the Warsaw basis. Under our operator basis, the relevant terms in matrix γ_{ij} are:

	$O_j = O_{\varphi t}$	$O_{\varphi Q}^{(+)}$	$O_{\varphi Q}^{(-)}$	$O_{\varphi tb}$	O_{tW}	O_{tB}	$O_{t\varphi}$
$O_i = O_{\varphi WB}$	$\frac{1}{3s_W c_W}$	$\frac{1}{3s_W c_W}$	$-\frac{1}{6s_W c_W}$	0	$-\frac{5y_t}{2ec_W}$	$-\frac{3y_t}{2es_W}$	0
$O_{\varphi D}$	$-6\frac{y_t^2}{e^2}$	$3\frac{y_t^2 - y_b^2}{e^2}$	$3\frac{y_t^2 - y_b^2}{e^2}$	$-6\frac{y_t y_b}{e^2}$	0	0	0
$O_{\varphi \square}$	$-\frac{3}{2}\frac{y_t^2}{e^2}$	$-\frac{3y_t^2 + 6y_b^2}{2e^2}$	$\frac{6y_t^2 + 3y_b^2}{2e^2}$	$3\frac{y_t y_b}{e^2}$	0	0	0
$O_{\varphi W}$	0	$\frac{1}{4s_W^2}$	$-\frac{1}{4s_W^2}$	0	$\frac{3y_t}{2es_W}$	0	0
$O_{\varphi B}$	$\frac{1}{3c_W^2}$	$\frac{1}{12c_W^2}$	$\frac{1}{12c_W^2}$	0	0	$\frac{5y_t}{2ec_W}$	0
O_W	0	$\frac{1}{es_W}$	$-\frac{1}{es_W}$	0	0	0	0
O_B	$\frac{4}{3ec_W}$	$\frac{1}{3ec_W}$	$\frac{1}{3ec_W}$	0	0	0	0
$O_{b\varphi}$	0	$-\frac{y_b}{2c_W^2}$ $+y_b\frac{8\lambda - 3y_t^2 - 5y_b^2}{4e^2}$	$y_b\frac{-4\lambda + 3y_t^2 + 7y_b^2}{4e^2}$	$\frac{3y_t}{4s_W^2}$ $-y_t\frac{2\lambda + y_t^2 - 6y_b^2}{2e^2}$	$\frac{y_t y_b}{2es_W}$	0	$\frac{3y_t y_b}{4e^2}$
$O_{\mu\varphi}$	0	$-\frac{3y_\mu(y_t^2 + y_b^2)}{2e^2}$	$\frac{3y_\mu(y_t^2 + y_b^2)}{2e^2}$	$\frac{3y_t y_b y_\mu}{e^2}$	0	0	$\frac{3y_t y_\mu}{2e^2}$
$O_{\tau\varphi}$	0	$-\frac{3y_\tau(y_t^2 + y_b^2)}{2e^2}$	$\frac{3y_\tau(y_t^2 + y_b^2)}{2e^2}$	$\frac{3y_t y_b y_\tau}{e^2}$	0	0	$\frac{3y_t y_\tau}{2e^2}$

with

$$\Delta(x) \equiv \Gamma(1 + \epsilon) \left(\frac{4\pi\mu^2}{x^2} \right)^\epsilon, \quad (3.3)$$

and the operator coefficients are defined at the scale μ_{EFT} .

In this work, we slightly modify the \overline{MS} scheme, by introducing the oblique parameters S and T as renormalisation conditions. This is done by modifying Eq. (3.2):

$$\delta Z_{ij} = \frac{\alpha}{2\pi} \Delta(\mu_{EFT}) \left(\frac{1}{\epsilon} + \Delta_{ij} \right) \gamma_{ij} \quad (3.4)$$

for $O_i = O_{\varphi WB}, O_{\varphi D}$, and fixing Δ_{ij} by requiring that the dim-6 contribution to S and T up to one loop is exactly the measured value. This can be done because we are using a basis which, apart from the top-quark operators that are not relevant in precision EW tests, includes only oblique operators. Therefore S and T can be defined as the outcome of a global fit for the EW sector, under the oblique assumption, as described in [51]. At the tree level, they correspond exactly to the coefficients of $O_{\varphi WB}$ and $O_{\varphi D}$.

The main reason for doing this, is that we are interested in the top-quark loop effects in the directions that do not lead to severe inconsistency with precision EW observables. This implies that $C_{\varphi WB}$ and $C_{\varphi D}$ should always take the values that minimise the inconsistency between top-loop effects and precision EW measurements. A complete global fit for the EW sector is required to fully address this problem [14], but in this work we take a simplified approach. We assume BSM effects are dominated by operators in Eqs. (2.2)-(2.5), i.e. they are oblique, and so the oblique parameters summarise the main constraints from precision EW observables. The S and T parameters can be used to fix the values of $C_{\varphi WB}$ and

$C_{\varphi D}$, by simply setting $S = T = 0$. This approach implicitly assumes that gauge boson self-energy corrections from top-quark loops are approximately linear functions of q^2 , which is not strictly true, but is enough for a sensitivity study.

In the \overline{MS} scheme, $S = T = 0$ does not imply that we can simply drop $C_{\varphi WB}(\mu_{EFT})$ and $C_{\varphi D}(\mu_{EFT})$ in our analysis. Instead, due to the top-quark operators contributing to S and T at the loop level, this approximation implies that we need to set the coefficients of $C_{\varphi WB}(\mu_{EFT})$ and $C_{\varphi D}(\mu_{EFT})$ to values that exactly cancel the contributions from top-quark operators at one loop. These coefficients will then give other contributions in other Higgs processes. A more convenient way to take these additional contributions into account, is simply to use S and T as renormalisation conditions, so that the renormalised values for $C_{\varphi WB}$ and $C_{\varphi D}$ correspond to the physical values of S and T , and so with our approximation they can be excluded from the analysis. The physical results are always independent of renormalisation scheme at the order of this calculation. The numerical results of S and T parameters in terms of top operator coefficients are given in Section 4.

3.2 SM renormalisation

The SM parameters are renormalised in the on-shell scheme, following [69]. In particular, the following parameters are split into renormalised quantities and renormalisation constants:

$$e_0 = (1 + \delta Z_e)e, \quad (3.5)$$

$$M_{W,0}^2 = M_W^2 + \delta M_W^2 \quad (3.6)$$

$$M_{Z,0}^2 = M_Z^2 + \delta M_Z^2 \quad (3.7)$$

$$M_{H,0}^2 = M_H^2 + \delta M_H^2. \quad (3.8)$$

Wave function renormalisation is defined as follows:

$$W_0^\pm = \left(1 + \frac{1}{2}\delta Z_W\right) W^\pm \quad (3.9)$$

$$Z_0 = \left(1 + \frac{1}{2}\delta Z_{ZZ}\right) Z + \frac{1}{2}\delta Z_{ZA}A \quad (3.10)$$

$$A_0 = \frac{1}{2}\delta Z_{AZ}Z + \left(1 + \frac{1}{2}\delta Z_{AA}\right) A \quad (3.11)$$

$$H_0 = \left(1 + \frac{1}{2}\delta Z_H\right) H. \quad (3.12)$$

To determine the dim-6 contributions in the renormalisation constants, we compute the two-point functions of the gauge bosons and the Higgs boson, from the top-quark operators. They can be written as

$$\begin{aligned} \bar{\Sigma}_{VV}^{(6)}(q^2) &= \Sigma_{VV}^{(6)}(q^2) + \Sigma_{VV}^{CT}(q^2) \\ &= \sum_i C_i \Sigma_{VV}^{i,loop}(q^2) + \sum_{i,j} \delta Z_{ji} C_i \Sigma_{VV}^{j,tree}(q^2) \end{aligned} \quad (3.13)$$

where in the last line, index i runs over all top-quark operators, and j runs over all Higgs operators that are needed to provide counter terms. $\Sigma_{VV}^{i/j,loop/tree}(q^2)$ are the corresponding operator contributions to the VV transverse two-point function. The Higgs-boson self energy $\bar{\Sigma}_{HH}$ is defined similarly. The dim-6 contributions in the renormalisation constants (denoted by the superscript (6)) are determined by these two-point functions, namely

$$\begin{aligned}
\delta M_W^{2(6)} &= \Re \bar{\Sigma}_{WW}^{(6)}(M_W^2), & \delta M_Z^{2(6)} &= \Re \bar{\Sigma}_{ZZ}^{(6)}(M_Z^2), \\
\delta M_H^{2(6)} &= \Re \bar{\Sigma}_{HH}^{(6)}(M_H^2), & \delta Z_W^{(6)} &= -\Re \left. \frac{\partial \bar{\Sigma}_{WW}^{(6)}(k^2)}{\partial k^2} \right|_{k^2=M_W^2}, \\
\delta Z_{ZZ}^{(6)} &= -\Re \left. \frac{\partial \bar{\Sigma}_{ZZ}^{(6)}(k^2)}{\partial k^2} \right|_{k^2=M_Z^2}, & \delta Z_{AA}^{(6)} &= -\left. \frac{\partial \bar{\Sigma}_{AA}^{(6)}(k^2)}{\partial k^2} \right|_{k^2=0}, \\
\delta Z_{AZ}^{(6)} &= -2\Re \frac{\bar{\Sigma}_{AZ}^{(6)}(M_Z^2)}{M_Z^2}, & \delta Z_{ZA}^{(6)} &= 2\frac{\bar{\Sigma}_{AZ}^{(6)}(0)}{M_Z^2}, \\
\delta Z_H^{(6)} &= -\Re \left. \frac{\partial \bar{\Sigma}_{HH}^{(6)}(k^2)}{\partial k^2} \right|_{k^2=M_H^2}, & \delta Z_e^{(6)} &= \frac{1}{2} \left. \frac{\partial \bar{\Sigma}_{AA}^{(6)}(k^2)}{\partial k^2} \right|_{k^2=0} - \frac{s_W}{c_W} \frac{\bar{\Sigma}_{AZ}^{(6)}(0)}{M_Z^2}.
\end{aligned} \tag{3.14}$$

The last equation defines the electric charge at zero momentum transfer. For the operators we have included, there are no large logarithmic terms arising from the b -quark mass, and so there is no need to define the running electric charge to resum the logs, as we only need the dim-6 EW contributions from the top loop. Note that the explicit expressions for $\Sigma_{VV}^{(6)}(q^2)$ have been given in Ref. [14], with an overall minus sign due to different conventions.

The above renormalisation constants would be sufficient to determine all the relevant counter terms, if we used α , M_Z and M_W as the input parameters. Conventionally, EW corrections are often computed with α , M_Z and G_F as input parameters. In our case, however, it is more convenient to use M_W , M_Z and G_F instead. This is because M_W enters the final state phase space, and we do not want its mass to depend on the dim-6 coefficients, because it would be particularly inconvenient for using the reweighting technique. To switch to the M_W , M_Z and G_F scheme, we use

$$M_W^2 \left(1 - \frac{M_W^2}{M_Z^2} \right) = \frac{\pi\alpha}{\sqrt{2}G_F} (1 + \Delta r), \tag{3.15}$$

where the Δr contribution from the top-quark operators is

$$\Delta_r^{(6)} = \left. \frac{\partial \bar{\Sigma}_{AA}^{(6)}(k^2)}{\partial k^2} \right|_{k^2=0} - \frac{c_W^2}{s_W^2} \left(\frac{\bar{\Sigma}_{ZZ}^{(6)}(M_Z^2)}{M_Z^2} - \frac{\bar{\Sigma}_{WW}^{(6)}(M_W^2)}{M_W^2} \right) + \frac{\bar{\Sigma}_{WW}^{(6)}(0) - \bar{\Sigma}_{WW}^{(6)}(M_W^2)}{M_W^2}. \tag{3.16}$$

One can simply define

$$\bar{\alpha} = \alpha(1 + \Delta r) \tag{3.17}$$

so that the tree level relation between M_W , M_Z , G_F , and α holds. To switch to the new scheme, one just needs to modify the renormalisation constant for α :

$$\delta \bar{\alpha}^{(6)} = \delta \alpha^{(6)} + (\alpha - \bar{\alpha})_{dim-6}. \tag{3.18}$$

3.3 Counter terms

The counter term Feynman rules are determined by the renormalisation constants and the RG mixing matrix. For example, consider the HZZ vertex, whose tree level Feynman rule is

$$\Gamma_{HZZ}^{\mu\nu} = i \frac{eM_W}{s_W c_W^2} g^{\mu\nu} + \sum_i C_i \Gamma_{HZZ,i}^{\mu\nu}, \quad (3.19)$$

where the subscript i covers all Higgs operators that have a contribution, including $O_{\varphi WB}$, $O_{\varphi W}$, $O_{\varphi B}$, $O_{\varphi D}$, O_W , and O_B . The corresponding dim-6 counter term has two parts. The first is the dim-6 contribution in the SM renormalisation, given by

$$i \frac{eM_W}{s_W c_W^2} g^{\mu\nu} \left[\delta Z_e^{(6)} + \frac{\delta M_W^{2(6)}}{2M_W^2} - \frac{\delta s_W^{(6)}}{s_W} - \frac{2\delta c_W^{(6)}}{c_W} + \delta Z_{ZZ}^{(6)} + \frac{1}{2}\delta Z_H^{(6)} \right] \quad (3.20)$$

where

$$\delta c_W = \frac{c_W}{2} \left(\frac{\delta M_W^2}{M_W^2} - \frac{\delta M_Z^2}{M_Z^2} \right) \quad (3.21)$$

$$\delta s_W = -\frac{c_W}{s_W} \delta c_W \quad (3.22)$$

while the second is from the RG mixing between dim-6 coefficients, given by

$$\sum_{i,j} C_j \delta Z_{ij} \Gamma_{HZZ,i}^{\mu\nu} \quad (3.23)$$

where i runs over the Higgs operators and j runs over the top-quark operators.

4 Numerical results

We are now ready to present the numerical results of our computation. We use the following input parameters:

$$M_Z = 91.1876 \text{ GeV}, \quad M_W = 80.385 \text{ GeV}, \quad (4.1)$$

$$G_F = 1.16638 \times 10^{-5} \text{ GeV}^{-2}, \quad M_H = 125 \text{ GeV}, \quad (4.2)$$

$$M_t = 172.5 \text{ GeV}, \quad M_b = 4.7 \text{ GeV}. \quad (4.3)$$

As we have explained in the introduction, all channels are computed for two cases: $\mu_{EFT} = M_H = 125 \text{ GeV}$ and $\mu_{EFT} = \Lambda = 1000 \text{ GeV}$. Results will be displayed as ratios w.r.t to LO SM predictions:

$$\mu_i \equiv \frac{\sigma_i}{\sigma_{\text{SM}}} \text{ or } \frac{\Gamma_i}{\Gamma_{\text{SM}}} \equiv 1 + \sum_j C_j \left(\frac{1 \text{ TeV}^2}{\Lambda^2} \right) \mu_{ij} \quad (4.4)$$

where i denotes channel, j runs over all contributing operators. μ_{ij} is the relative deviation in channel i from operator j if $C_j/\Lambda^2 = 1/\text{TeV}^2$. μ_{ij} for all decay processes are given in percentage, in Table 1, and for all production processes at the LHC at 13 TeV and future lepton colliders are given in Tables 2-5. For lepton colliders we consider 250 and 350 GeV

channel	μ_{EFT} [GeV]	$O_{\varphi W}$	$O_{\varphi B}$	$O_{\varphi t}$	$O_{\varphi Q}^{(+)}$	$O_{\varphi Q}^{(-)}$	$O_{\varphi tb}$	O_{tW}	O_{tB}	$O_{t\varphi}$
$H \rightarrow bb$	125	0	0	-0.15	-0.06	0.24	-1.13	-0.28	0	-0.18
$H \rightarrow bb$	1000			0.79	0.54	-1.25	-8.16	0.34	0	0.29
$H \rightarrow \mu\mu, \tau\tau$	125	0	0	-0.15	0.001	0.15	0	0	0	-0.27
$H \rightarrow \mu\mu, \tau\tau$	1000			0.79	0.002	-0.79	0	0	0	0.68
$H \rightarrow \gamma\gamma$	125	-1378	-4806	-3.37	5.86	2.64	0	-56.4	-117.9	3.45
$H \rightarrow \gamma\gamma$	1000			6.95	16.2	-2.52	0	14.0	101.3	3.45
$H \rightarrow Z\gamma$	125	-1437	1437	0.51	2.20	2.74	0	-39.5	14.0	0.72
$H \rightarrow Z\gamma$	1000			4.35	6.04	0.83	0	33.9	-51.6	0.72
$H \rightarrow Zll$	125	2.79	-8.67	-0.54	-0.10	0.56	-0.00	0.19	-0.06	0.08
$H \rightarrow Zll$	1000			0.33	0.74	-1.25	-0.06	0.05	0.33	0.08
$H \rightarrow Wl\nu$	125	-9.00	0	-0.15	-0.24	0.38	0.00	-0.13	0	-0.03
$H \rightarrow Wl\nu$	1000			0.79	0.63	-1.42	-0.05	0.33	0	-0.03

Table 1. Percentage deviation μ_{ij} for decay channel i and operator j .

channel	μ_{EFT} [GeV]	$O_{\varphi W}$	$O_{\varphi B}$	$O_{\varphi t}$	$O_{\varphi Q}^{(+)}$	$O_{\varphi Q}^{(-)}$	$O_{\varphi tb}$	O_{tW}	O_{tB}	$O_{t\varphi}$
$pp \rightarrow ZH$	125	73.7	8.17	-0.30	0.21	0.21	-0.00	1.00	-0.06	-0.02
$pp \rightarrow ZH$	1000			0.57	0.11	-0.66	-0.06	-2.75	-0.44	-0.02
$pp \rightarrow WH$	125	88.6	0	-0.15	-0.04	0.19	0.00	0.43	0	-0.21
$pp \rightarrow WH$	1000			0.79	-0.27	-0.52	-0.05	-4.08	0	-0.21
$pp \rightarrow Hjj$	125	-4.52	-0.04	-0.26	-0.24	0.51	0.01	0.05	-0.00	0.03
$pp \rightarrow Hjj$	1000			0.68	0.94	-1.61	-0.04	0.28	-0.00	0.03

Table 2. Percentage deviation μ_{ij} for production channel i and operator j at LHC 13 TeV.

centre-of-mass energies, to cover possible scenarios at CEPC, FCC-ee, and ILC, which are planned to collect data at both 240~250 GeV and 350 GeV [70–73]. We present results for two beam polarisation configurations $P(e^+, e^-) = (\pm 30\%, \mp 80\%)$. In the 350 GeV case, we only consider the $O_{t\varphi}$ contributions, as the sensitivity to other operators is unlikely to compete with the direct production modes [74]. In all processes we set the renormalisation and factorisation scale to M_H . For VH production no cuts are applied, whilst for VBF we apply the following jet cuts at the LHC:

$$p_T^j > 20 \text{ GeV}, |y_j| < 5, |y_{j1} - y_{j2}| > 3, M_{jj} > 130 \text{ GeV}. \quad (4.5)$$

No cuts are applied for the lepton collider results. In both cases the Higgs and vector bosons are not decayed. Note that these results are computed with our modified \overline{MS} scheme. For completeness, in Appendix A we also present results computed with the standard \overline{MS} scheme.

From Tables 1-5 we see that loop-induced decay channels $H \rightarrow \gamma\gamma$ and $H \rightarrow Z\gamma$ can show large deviations from the SM. For all other processes, the relative deviation caused by a top operator with $C_j/\Lambda^2 = 1/\text{TeV}^2$ is around the percent level. One also observes that

channel	μ_{EFT} [GeV]	$O_{\varphi t}$	$O_{\varphi Q}^{(+)}$	$O_{\varphi Q}^{(-)}$	$O_{\varphi tb}$	O_{tW}	O_{tB}	$O_{t\varphi}$
$e^+e^- \rightarrow ZH$	125	-0.40	-0.21	0.22	-0.00	1.82	-0.25	0.01
$e^+e^- \rightarrow ZH$	1000	0.78	-0.10	-0.71	-0.05	-2.71	0.62	0.01
$e^+e^- \rightarrow H\nu\nu$	125	-0.15	-0.26	0.41	0.01	-0.08	0	-0.01
$e^+e^- \rightarrow H\nu\nu$	1000	0.79	0.76	-1.55	-0.04	0.13	0	-0.01
$e^+e^- \rightarrow He^+e^-$	125	-0.51	-0.27	0.56	0.00	0.72	0.79	0.08
$e^+e^- \rightarrow He^+e^-$	1000	0.28	0.76	-1.50	-0.05	0.77	-0.71	0.08

Table 3. Percentage deviation μ_{ij} for production channel i and operator j for 250 GeV and $P(e^+, e^-) = (30\%, -80\%)$.

channel	μ_{EFT} [GeV]	$O_{\varphi t}$	$O_{\varphi Q}^{(+)}$	$O_{\varphi Q}^{(-)}$	$O_{\varphi tb}$	O_{tW}	O_{tB}	$O_{t\varphi}$
$e^+e^- \rightarrow ZH$	125	-0.44	0.36	0.55	-0.01	-0.62	0.17	0.06
$e^+e^- \rightarrow ZH$	1000	0.00	1.14	-1.42	-0.06	-1.35	-2.35	0.06
$e^+e^- \rightarrow H\nu\nu$	125	-0.15	-0.26	0.41	0.01	-0.01	0	-0.01
$e^+e^- \rightarrow H\nu\nu$	1000	0.79	0.76	-1.55	-0.04	0.01	0	-0.01
$e^+e^- \rightarrow He^+e^-$	125	-0.62	0.14	0.66	-0.01	0.32	1.40	0.05
$e^+e^- \rightarrow He^+e^-$	1000	0.30	0.95	-1.08	-0.06	-0.60	-0.85	0.05

Table 4. Percentage deviation μ_{ij} for production channel i and operator j for 250 GeV and $P(e^+, e^-) = (-30\%, 80\%)$.

channel $O_{t\varphi}$	P(30%, -80%)	P(-30%, 80%)
$e^+e^- \rightarrow ZH$	-0.15	0.01
$e^+e^- \rightarrow H\nu\nu$	-0.01	-0.01
$e^+e^- \rightarrow He^+e^-$	0.10	0.08

Table 5. Percentage deviation μ_{ij} for production channel i and operator $O_{t\varphi}$ for 350 GeV and $P(e^+, e^-) = (\pm 30\%, \mp 80\%)$. The results are identical at any μ_{EFT} .

$\mu_{\text{EFT}} = 1000$ GeV results are in general larger than the $\mu_{\text{EFT}} = 125$ GeV ones, due to the logarithmic terms, but $\mu_{\text{EFT}} = 125$ GeV deviations are not negligible at all. There are also entries where the $\mu_{\text{EFT}} = 125$ GeV result is larger.

Another observation is that these results depend on the scheme of input parameters used in the calculation. For example, if we used the α , M_Z and G_F scheme, the operator O_{tB} would give a contribution to $H \rightarrow Wl\nu$ and $pp \rightarrow HW$, because its contribution to the ZZ two-point function could affect the Z mass, which in turn enters g_w and M_W . But these contributions vanish if we use the M_W , M_Z and G_F input scheme, because the renormalisation condition for G_F will fix the renormalisation constant of g_w so that it only depends on the WW two-point function, to which O_{tB} does not contribute. The same applies to $O_{\varphi t}$, i.e. $O_{\varphi t}$ gives no contribution in $H \rightarrow Wl\nu$ and $pp \rightarrow HW$ if the standard \overline{MS} scheme is used. However it does give a contribution to the T parameter, and because we use T as one of the renormalisation conditions to fix $C_{\varphi D}$, a non-zero contribution arises due to $O_{\varphi D}$ modifying the Higgs wave-function. In general, most results we have obtained

	$\mu_{\text{EFT}} [\text{GeV}]$	$O_{\varphi t}$	$O_{\varphi Q}^{(+)}$	$O_{\varphi Q}^{(-)}$	$O_{\varphi tb}$	O_{tW}	O_{tB}	$O_{t\varphi}$
S	125	-0.017	0.029	0.013	0	0.084	0.095	0
S	1000	0.035	0.081	-0.013	0	-0.504	-0.565	0
T	125	-0.186	0.022	0.165	0.003	0	0	0
T	1000	1.016	-0.579	-0.436	0.036	0	0	0
U	125	0.010	-0.048	-0.016	0.001	0.090	0	0
U	1000	0.010	-0.048	-0.016	0.001	0.090	0	0

Table 6. Deviation in S , T and U parameters due to top operators.

so far will depend on the input scheme used in the calculation. This is also why we want to include constraints from precision EW tests, so that the relation between α , M_W , M_Z and G_F is not significantly modified. In Table 6 we present results for S , T and U in the original \overline{MS} scheme. They are parameterised by

$$S \equiv \sum_j C_j \left(\frac{1 \text{ TeV}^2}{\Lambda^2} \right) S_j, \quad (4.6)$$

and similarly for T , U . Note that U is finite and is scheme independent [15].

The precision EW tests contain more information than S , T and U . This information is lost in the STU formalism simply because the two-point functions of gauge bosons are approximated as linear functions of the momentum squared. A complete analysis for precision EW data without using these oblique parameters can be performed to obtain better constraints, see Ref. [14] for more details. Since a global fit is not the goal of this study, in this paper we will only use the oblique parameters to simplify the analysis of the precision EW part, but one should keep in mind that in principle more information can be obtained.

We briefly demonstrate that physical results are scheme-independent. Consider $H \rightarrow \gamma\gamma$ with $\mu_{\text{EFT}} = 125 \text{ GeV}$ as an example. Taking the standard \overline{MS} results in Table 14 in Appendix A, we have the following dim-6 contributions to the width:

$$\Gamma_{\gamma\gamma}^{(6)} = \Gamma_{\gamma\gamma}^{\text{SM}} (1 + 25.74 C_{\varphi WB} - 0.733 C_{tW} - 1.367 C_{tB} + 0.0345 C_{t\varphi}) \quad (4.7)$$

where we have used that $O_{\varphi WB}$ gives the following $H \rightarrow \gamma\gamma$ amplitude:

$$4 \frac{C_{\varphi WB} s_W c_W}{\Lambda^2} \left(\frac{M_H^2}{2} \epsilon_1 \cdot \epsilon_2 - (p_1 \cdot \epsilon_2)(p_2 \cdot \epsilon_1) \right). \quad (4.8)$$

Following Table 6, the S parameter is given by

$$S = -12.9 C_{\varphi WB} - 0.017 C_{\varphi t} + 0.029 C_{\varphi Q}^{(+)} + 0.013 C_{\varphi Q}^{(-)} + 0.084 C_{tW} + 0.095 C_{tB} \quad (4.9)$$

where the coefficient of $C_{\varphi WB}$ is given by

$$\alpha_{EW} S = \frac{C_{\varphi WB} 4v^2 s_W c_W}{\Lambda^2}. \quad (4.10)$$

channel	μ_{EFT} [GeV]	$O_{\varphi t}$	$O_{\varphi Q}^{(+)}$	$O_{\varphi Q}^{(-)}$	$O_{\varphi tb}$	O_{tW}	O_{tB}	$O_{t\varphi}$
$pp \rightarrow ZH$	125	0.0014	0.0078	0.0041	4.0×10^{-8}	0.0085	0.0012	3.7×10^{-5}
$pp \rightarrow ZH$	1000	0.0022	0.0062	0.0047	7.5×10^{-6}	0.037	0.0054	3.7×10^{-5}

Table 7. Percentage deviation at $\mathcal{O}(1/\Lambda^4)$ for ZH production at LHC 13 TeV.

Combining Eqs. (4.7) and (4.9) and eliminating $C_{\varphi WB}$, we find the expression of $\Gamma_{\gamma\gamma}^{(6)}$ for a fixed S parameter, which agrees with results in Table 1. One can easily check the same relation holds for $\mu_{\text{EFT}} = 1000$ GeV and for $H \rightarrow \gamma Z$.

Finally, we note here that our results in Tables 1-6 provide the $\mathcal{O}(1/\Lambda^2)$ deviation from the SM predictions from the top operators. Our computational setup allows us to also obtain the $\mathcal{O}(1/\Lambda^4)$ contribution coming from squaring the 1-loop contributions. As an example in Table 7 we show the percentage deviation from the SM induced at $\mathcal{O}(1/\Lambda^4)$ by the top operators for $C_i = 1$ and $\Lambda = 1$ TeV for ZH production at the LHC. We find that these high-order contributions are suppressed by about two orders of magnitude compared to the $\mathcal{O}(1/\Lambda^2)$ contributions in Table 2. Given the current limits on the operator coefficients, we can safely ignore these contributions. A similar behaviour is expected also for the other processes studied in this work, except for loop-induced processes in the SM, i.e. $gg \rightarrow H$, $H \rightarrow \gamma\gamma, \gamma Z, gg$. For these processes, the SM contributions are suppressed, so dim-6 squared terms can be potentially important. Their quadratic dependence on the operator coefficients will be kept in Section 5.1 and 5.2, where we only use current limits to constrain top-quark operators.

5 Physics implications

In this section we discuss the impact of our numerical results.

5.1 Impact on Higgs measurements at the LHC

The first consequence of these loop contributions in Higgs measurements is that they can shift the measured signal strengths at the LHC. The current constraints on top-quark operator coefficients are not very stringent compared to Higgs operator constraints, and so within the allowed range, the loop-induced contributions could potentially affect the signal strengths of all Higgs channels. Without knowing exactly the coefficients of top-quark operators, these contributions can only be dealt with as theoretical uncertainties, and should be considered in all Higgs measurements that are analysed using a SMEFT approach. These theoretical uncertainties cannot be avoided in a bottom-up view of the SMEFT, as in general there is no strong motivation to overlook a certain type of operators [75], in particular at the energy scale of the measurements, where the RG effects will take place and mix different types of operators.

To estimate the size of possible contributions from top operators, we consider the current constraints on top-quark operator coefficients from direct measurements. These constraints originate from processes where these operators enter already at the tree level.

Operator	Top Fitter	RHCC	$\sigma_{t\bar{t}H}$ [33]
$C_{\varphi tb}$		[-5.28,5.28]	
$C_{\varphi Q}^{(3)}$	[-2.59,1.50]		
$C_{\varphi Q}^{(1)}$	[-3.10,3.10]		
$C_{\varphi t}$	[-9.78,8.18]		
C_{tW}	[-2.49,2.49]		
C_{tB}	[-7.09,4.68]		
$C_{t\varphi}$			[-6.5,1.3]

Table 8. Individual limits on operator coefficients, from the Top Fitter Collaboration [5], right-handed charged currents (RHCC) (tree-level only) [9], and $t\bar{t}H$ cross section [33]. $\Lambda = 1$ TeV is assumed.

First, the TopFitter collaboration performed a global fit (excluding $O_{\varphi tb}$) at LO using both Tevatron and LHC data for top production and decay [5]. Individual limits are given for each operator, by setting other operator coefficients to zero. In addition, the $O_{\varphi tb}$ operator gives rise to right handed Wtb coupling, which is constrained at tree-level by single top and top decay measurements, and indirectly at loop-level by B meson decay and $h \rightarrow b\bar{b}$ [9]. Here we only use the direct limits. For the Yukawa operator $O_{t\varphi}$, we follow the approach in Ref. [33], and update the analysis with the recent 13 TeV measurements in Refs. [76–79]. Again, we do not use the loop-induced $gg \rightarrow H$ process. In Table 8 we list these constraints.

Using all the individual direct constraints and neglecting correlations, we can approximately identify the allowed region in the 7-dimensional parameter space at 95% CL, by reconstructing a χ^2 . We shift all the intervals so that they are centred at zero. Within the range allowed by the constraints, using the results presented in Table 1 and Table 2, we find the maximum and minimum percentage deviations in signal strengths in all Higgs channels, taking $\mu_{EFT} = 125$ GeV, i.e. the scale of the measurements. These deviations are given in Table 9. For example, the interval shown in the 4th row and 3rd column means that in $pp \rightarrow ZH$, $H \rightarrow b\bar{b}$, the signal strength can be shifted by -7% to $+6\%$ by top-quark operators within the current constraints.

	$\gamma\gamma$	γZ	bb	WW*	ZZ*	$\tau\tau$	$\mu\mu$
gg	(-100%,1980%)	(-88%,200%)	(-40%,48%)	(-40%,47%)	(-40%,46%)	(-40%,48%)	(-40%,48%)
VBF	(-100%,1880%)	(-88%,170%)	(-6.1%,5.3%)	(-6.8%,6.7%)	(-8.8%,9.2%)	(-6.2%,5.9%)	(-6.2%,5.9%)
WH	(-100%,1880%)	(-88%,170%)	(-5.5%,4.2%)	(-6.1%,5.6%)	(-7.8%,7.9%)	(-5.8%,5.1%)	(-5.8%,5.1%)
ZH	(-100%,1880%)	(-87%,170%)	(-6.5%,5.9%)	(-7.1%,7.1%)	(-9.4%,9.9%)	(-6.8%,6.7%)	(-6.8%,6.7%)

Table 9. Possible deviations in signal strengths, due to top-quark operators, in major Higgs production and decay channels at the LHC. The top-quark operator coefficients are allowed to vary within the current constraints, described in Table 8.

We see that for the loop-induced processes, i.e. those in the first row and the first

two columns, the deviations are large. This simply demonstrates that for operators like O_{tB} , loop-induced constraints are much stronger than the tree-level ones. For example, the $gg \rightarrow H \rightarrow \gamma\gamma$ signal strength can deviate by a factor of ~ 20 and this is mainly driven by $|C_{tB}| \approx 6$. It implies that this channel is sensitive to C_{tB} and can be used to place much stronger bounds compared with the current ones. The same applies to other loop-induced channels.

For the remaining tree-level Higgs channels, the impact of top-operators through loops is in general weaker, but remains around $5 \sim 10\%$, and is not negligible even for the current precision. Although theory uncertainties of this size may not significantly change the result of a Higgs coupling analysis, they will become relevant from now on, and eventually, at the high luminosity scenario, become an important component of theory uncertainties in a bottom-up global SMEFT analysis.

This also implies that once the precision of Higgs measurements goes beyond $\sim 10\%$, we can even hope to use Higgs measurements to place useful constraints on top-quark operators. In Section 5.3 we discuss this possibility by estimating the sensitivity in the high luminosity scenario of LHC.

5.2 Impact on Higgs measurements at the future lepton colliders

As we have mentioned in the introduction, at lepton colliders, the estimated precision of Higgs signal strength measurements could reach $\mathcal{O}(1\%) - \mathcal{O}(0.1\%)$ level. For the Higgs measurements to make sense at this accuracy level, one has to check carefully the top-loop induced contributions. If the machine is planned to run at 350 GeV, it is likely that the top-quark operator coefficients will be determined directly through $t\bar{t}$ production, except for the $O_{t\varphi}$. However, for the CEPC case a 350 GeV run has not been officially planned, and therefore an interesting question is by how much the top-quark operators could change the Higgs cross sections below the $t\bar{t}$ threshold through loops, given the current constraints. In fact, in Table 3 we see that a top operator with a coefficient of order $1/\text{TeV}^2$ could already have visible effects.

In Tables 10, 11 and 12 we present the possible deviations at lepton colliders, in a way similar to Table 9 for the LHC. We consider two scenarios: 1) 250 GeV run only, and we allow all top operators to vary within the current constraints. These results are given in Table 10. 2) runs above $t\bar{t}$ threshold are planned, which will fix all operator coefficients by direct production, except for $C_{t\varphi}$, and so only $C_{t\varphi}$ is allowed to vary. Corresponding results are shown in Tables 11 and 12, for 250 and 350 GeV runs respectively. All these deviations are obtained with numerical results presented in Table 3. For each process, two polarisations for (e^+, e^-) are considered.

In the first scenario, apart from the large deviations in the loop-induced decay $\gamma\gamma$ and γZ , a $5 - 15\%$ level deviations are common in all channels. These results suggest that the current sensitivities to top-quark couplings can be already improved by up to an order of magnitude even with an e^+e^- collider below the $t\bar{t}$ threshold. In the second scenario, deviations are smaller at $\sim 5\%$, but are sufficient to further pin down the top Yukawa coupling. More reliable estimates of the potential constraints that can be placed

	$\gamma\gamma$	γZ	bb	WW*	ZZ*	$\tau\tau$	$\mu\mu$
ZH(+30%,-80%)	(-100%,1900%)	(-87%,160%)	(-7.5%,7.5%)	(-8.3%,8.6%)	(-11%,11%)	(-8%,8.3%)	(-8%,8.3%)
ZH(-30%,+80%)	(-100%,1870%)	(-88%,180%)	(-7.6%,7.1%)	(-8.1%,7.9%)	(-10%,11%)	(-7.6%,7.3%)	(-7.6%,7.3%)
WWF(+30%,-80%)	(-100%,1880%)	(-88%,170%)	(-5.7%,4.7%)	(-6.5%,6.2%)	(-8.1%,8.3%)	(-5.9%,5.3%)	(-5.9%,5.3%)
WWF(-30%,+80%)	(-100%,1880%)	(-88%,170%)	(-5.7%,4.7%)	(-6.5%,6.2%)	(-8.1%,8.3%)	(-5.9%,5.3%)	(-5.9%,5.3%)
ZZF(+30%,-80%)	(-100%,1790%)	(-88%,180%)	(-11%,8.6%)	(-11%,9.6%)	(-13%,12%)	(-11%,9%)	(-11%,9%)
ZZF(-30%,+80%)	(-100%,1730%)	(-88%,180%)	(-14%,11%)	(-14%,12%)	(-15%,15%)	(-14%,11%)	(-14%,11%)

Table 10. Possible deviations in signal strengths (in percent) caused by top-quark operators, in Higgs production (WWF for WW fusion and ZZF for ZZ fusion) and decay channels, at an e^+e^- collider at 250 GeV centre-of-mass energy. All top-quark operator coefficients are allowed to vary within the current constraints, described in Table 8.

	$\gamma\gamma$	γZ	bb	WW*	ZZ*	$\tau\tau$	$\mu\mu$
ZH(+30%,-80%)	(-17%,19%)	(-7.3%,7%)	(-4%,3.3%)	(-4.5%,4%)	(-4.9%,4.4%)	(-3.6%,3%)	(-3.6%,3%)
ZH(-30%,+80%)	(-17%,19%)	(-7.5%,7.2%)	(-4.1%,3.5%)	(-4.7%,4.2%)	(-5.1%,4.6%)	(-3.8%,3.2%)	(-3.8%,3.2%)
WWF(+30%,-80%)	(-17%,18%)	(-7.2%,7%)	(-3.9%,3.3%)	(-4.4%,3.9%)	(-4.9%,4.3%)	(-3.5%,2.9%)	(-3.5%,2.9%)
WWF(-30%,+80%)	(-17%,18%)	(-7.2%,7%)	(-3.9%,3.3%)	(-4.4%,3.9%)	(-4.9%,4.3%)	(-3.5%,2.9%)	(-3.5%,2.9%)
ZZF(+30%,-80%)	(-17%,19%)	(-7.6%,7.3%)	(-4.2%,3.6%)	(-4.8%,4.3%)	(-5.2%,4.7%)	(-3.9%,3.3%)	(-3.9%,3.3%)
ZZF(-30%,+80%)	(-17%,19%)	(-7.5%,7.2%)	(-4.1%,3.5%)	(-4.7%,4.2%)	(-5.1%,4.6%)	(-3.8%,3.2%)	(-3.8%,3.2%)

Table 11. Possible deviations in signal strengths (in percent) caused by top-quark operators, in Higgs production (WWF for WW fusion and ZZF for ZZ fusion) and decay channels, at an e^+e^- collider at 250 GeV centre-of-mass energy. Only the coefficient of $O_{t\varphi}$ is allowed to vary within the current constraints, described in Table 8.

	$\gamma\gamma$	γZ	bb	WW*	ZZ*	$\tau\tau$	$\mu\mu$
ZH(+30%,-80%)	(-17%,18%)	(-6.7%,6.4%)	(-3.4%,2.7%)	(-3.9%,3.3%)	(-4.4%,3.8%)	(-3%,2.4%)	(-3%,2.4%)
ZH(-30%,+80%)	(-17%,19%)	(-7.3%,7.1%)	(-4%,3.4%)	(-4.5%,4%)	(-5%,4.4%)	(-3.6%,3%)	(-3.6%,3%)
WWF(+30%,-80%)	(-17%,18%)	(-7.3%,7%)	(-3.9%,3.3%)	(-4.5%,3.9%)	(-4.9%,4.4%)	(-3.6%,2.9%)	(-3.6%,2.9%)
WWF(-30%,+80%)	(-17%,18%)	(-7.3%,7%)	(-3.9%,3.3%)	(-4.5%,3.9%)	(-4.9%,4.4%)	(-3.6%,2.9%)	(-3.6%,2.9%)
ZZF(+30%,-80%)	(-17%,19%)	(-7.7%,7.4%)	(-4.3%,3.7%)	(-4.9%,4.3%)	(-5.3%,4.8%)	(-4%,3.4%)	(-4%,3.4%)
ZZF(-30%,+80%)	(-17%,19%)	(-7.6%,7.4%)	(-4.3%,3.7%)	(-4.8%,4.3%)	(-5.2%,4.7%)	(-3.9%,3.3%)	(-3.9%,3.3%)

Table 12. Possible deviations in signal strengths (in percent) caused by top-quark operators, in Higgs production (WWF for WW fusion and ZZF for ZZ fusion) and decay channels, at an e^+e^- collider at 350 GeV centre-of-mass energy. Only the coefficient of $O_{t\varphi}$ is allowed to vary within the current constraints, described in Table 8.

on top-quark couplings would require a global analysis including both the Higgs and the top operators, which we will leave for future studies.

5.3 Potential at high luminosity LHC

Given that the precision of Higgs measurements will be largely improved at the high luminosity LHC (HL-LHC), the potential $\sim 5 - 10\%$ deviations in Higgs measurements can be

used to place constraints on the top-quark operator coefficients. This does not mean that we will have 7 more free parameters to fit in the Higgs sector, because the top operators are also constrained by direct top-quark measurements. However, it is likely that one has to combine the two sectors to obtain the correct exclusion limits on both top and Higgs operators. To see if this is the case, in this section we will estimate the sensitivity of dim-6 top-loop effects at the HL-LHC at 3000 fb^{-1} .

To this end, we perform a χ^2 analysis including all top operators but fixing all the Higgs operator coefficients to zero, at $\mu_{EFT} = M_H = 125 \text{ GeV}$ and at $\mu_{EFT} = \Lambda = 1000 \text{ GeV}$. As discussed in the introduction, the first scale choice gives an estimate of sensitivity from a bottom-up point of view, while the second is from a top-down point view taking into account RG running and mixing effects. In the χ^2 analysis we assume the measured values will be exactly the same as the SM predictions. For the projection of future signal strength measurements, we follow Ref. [80], where in Table 3 the statistical and systematic errors for $gg \rightarrow H$, VBF, WH and ZH production, with ZZ^* , $\gamma\gamma$, WW^* , $\tau\tau$, $\mu\mu$ decay channels are all documented. We take one half of the theory errors, to account for possible theory improvements in the future, and we have checked that in any case the resulting sensitivities are affected by theory errors only at the percent level. QCD corrections are potentially important, but they are likely to cancel in the signal strengths, when taking ratios w.r.t SM cross sections, so we will not consider them. For the $H \rightarrow bb$ channel we use Ref. [81], where we have assumed that two-lepton and one-lepton channels correspond exactly to ZH and WH production. Finally we consider the $Z\gamma$ signal strength taken from [82], assuming that the production channel is dominated by $gg \rightarrow H$.

Top-operator contributions to signal strengths can be easily computed using results presented in Tables 1 and 2. The modifications to the Higgs total width are taken into account. A specific X -like production channel may contain components from all five major production mechanisms, including ggF, VBF, WH , ZH and ttH . Numerical results for VBF, WH , ZH are presented in Table 2, while for the other two channels we only need to take into account the leading effect from the top Yukawa operator $O_{t\varphi}$, which rescales the total cross section.

As we have mentioned in Section 3.1, the consistency of precision EW observables is important for the results to be scheme independent. As explained in Section 3, to simplify the analysis we assume that the S and T parameters are measured accurately and set them to zero. Thanks to our renormalisation scheme, this approximation simply means that we can exclude the operators $O_{\varphi WB}$ and $O_{\varphi D}$ from the analysis. We however take into account the U parameter which is scheme-independent up to dim-6. The current bound is ± 0.1 , taken from the PDG [51].

A total χ^2 is constructed by using Higgs data plus the U parameter. We truncate the χ^2 at the quadratic order in C , the Wilson coefficients. The one-sigma interval for any single parameter is given by $\Delta\chi^2 = 1$. The individual sensitivities on operator coefficients are given in Table 13, where we compare the results of the two scenarios $\mu_{EFT} = M_H = 125 \text{ GeV}$, and $\mu_{EFT} = \Lambda = 1000 \text{ GeV}$, and the current constraints. Here, ‘‘sensitivity’’ is defined as one half of the size of interval of coefficient C_i at 95% CL, assuming $\Lambda = 1 \text{ TeV}$, and

Operator	$C_{\varphi t}$	$C_{\varphi Q}^{(+)}$	$C_{\varphi Q}^{(-)}$	$C_{\varphi tb}$	C_{tW}	C_{tB}	$C_{t\varphi}$
$\mu_{EFT} = 125$ GeV	2.5	1.3	3.2	9.3	0.2	0.07	0.9
$\mu_{EFT} = 1000$ GeV	1.3	0.5	4.3	1.3	0.6	0.08	0.9
Current	9.0	5.1	5.1	5.3	2.5	5.9	3.9

Table 13. Sensitivity of Higgs measurements at HL-LHC to top-quark operators, compared with current constraints. Here sensitivity is defined as one half of the size of interval of coefficient C_i at 95% CL, assuming $\Lambda = 1$ TeV, and all other operators coefficients are set to zero.

all other operators vanish.¹ We can see that sensitivities on the first four coefficients are comparable with the current direct measurements. The last three coefficients are even more tightly constrained. This is mainly because they enter $gg \rightarrow H$, $H \rightarrow \gamma\gamma$ and/or $H \rightarrow Z\gamma$, where the relative deviations at dim-6 are large due to the loop suppression of the SM. From Table 13 we can already conclude that Higgs measurements will provide useful information on top-quark operators.

The individual sensitivities do not fully reflect the constraining power of the combined analysis. To better study the structure of the χ^2 , we present the limits on each eigenstate of the quadratic terms of χ^2 . This is done by writing

$$\chi^2 = CMC^T \quad (5.1)$$

where

$$C = \left(C_{\varphi t} \ C_{\varphi Q}^{(+)} \ C_{\varphi Q}^{(-)} \ C_{\varphi tb} \ C_{tW} \ C_{tB} \ C_{t\varphi} \right). \quad (5.2)$$

By diagonalizing the matrix $M \rightarrow M^D$:

$$\chi^2 = CU^T M^D UC^T \quad (5.3)$$

we find seven linear combinations of operator coefficients, given by UC^T , which are statistically independent. Then for the i th linear combination, the χ^2 is given by $M_{ii}^D (UC^T)_i^2$, so the one-sigma limit on the i th combination will be $M_{ii}^{D-\frac{1}{2}}$. For $\mu_{EFT} = 125$ GeV, we

¹ We refrain from using words such as constraints, bounds, or limits because there is no data yet and because a real global fit would have to take into account the full set of Higgs operators in the same analysis. The results we present here reflect the sensitivities of measurements to top operators, but not the actual constraints.

find

$$\begin{pmatrix} -0.025 & 0.045 & 0.019 & 0.005 & -0.43 & -0.9 & -0.041 \\ 0.022 & -0.076 & -0.058 & -0.049 & 0.42 & -0.25 & 0.87 \\ 0.0012 & 0.18 & 0.068 & -0.033 & -0.77 & 0.35 & 0.49 \\ 0.26 & -0.91 & -0.26 & 0.0099 & -0.21 & 0.04 & 0.0099 \\ 0.42 & 0.27 & -0.54 & -0.68 & -0.002 & -0.0095 & -0.064 \\ -0.48 & -0.26 & 0.41 & -0.73 & -0.0039 & 0.0076 & -0.021 \\ 0.72 & -0.00077 & 0.68 & -0.095 & 0.047 & -0.028 & -0.0092 \end{pmatrix}
\times \frac{1\text{TeV}^2}{\Lambda^2}
\begin{pmatrix} C_{\varphi t} \\ C_{\varphi Q}^{(+)} \\ C_{\varphi Q}^{(-)} \\ C_{\varphi tb} \\ C_{tW} \\ C_{tB} \\ C_{t\varphi} \end{pmatrix}
= \pm \begin{pmatrix} 0.0326 \\ 0.548 \\ 0.637 \\ 2.62 \\ 7.31 \\ 19.8 \\ 79.6 \end{pmatrix} \quad (5.4)$$

We can see that all seven linear combinations can be constrained. Even though the last one may be too weak to be give meaningful constraints, we will show that it can be significantly improved once differential distributions are taken into account. The first five numbers are all quite constraining.

To see where exactly these constraints come from, for each of the eigenstates given above, we compute the contribution from each measurement to the eigenvalue of χ^2 . Since the sensitivities given in Eq. (5.4) are the inverse square root of these eigenvalues, the fraction for each measurement in the eigenvalue reflects the relative importance of that measurement in the direction that corresponds to the eigenvectors. To have a physical intuition about what is happening, below we give the most important operators in each of the seven eigenstates, and the measurements that contribute the largest fractions to the corresponding χ^2 :

Eigenstates	Coefficients	Channels
1st	C_{tB} (81%)	$gg \rightarrow H \rightarrow \gamma\gamma$ (84%)
2nd	$C_{t\varphi}$ (75%), C_{tW} (18%)	$gg \rightarrow H \rightarrow ZZ^*, \gamma Z, \mu\mu, WW^*$ (77%)
3rd	C_{tW} (59%), $C_{t\varphi}$ (24%)	$gg \rightarrow H \rightarrow \gamma Z$ (42%), U (25%)
4th	$C_{\varphi Q}^{(+)}$ (82%)	U (68%), $gg \rightarrow H \rightarrow \gamma Z$ (28%)
5th	$C_{\varphi tb}$ (46%), $C_{\varphi Q}^{(-)}$ (29%)	$VBF \rightarrow \tau\tau, ZZ^*, \gamma\gamma$ (64%), $WH \rightarrow ZZ^*, \gamma\gamma$ (16%)
6th	$C_{\varphi tb}$ (53%), $C_{\varphi t}$ (23%), $C_{\varphi Q}^{(-)}$ (17%)	$ZH, WH \rightarrow b\bar{b}$ (59%) $gg \rightarrow H \rightarrow \mu\mu$ (17%)
7th	$C_{\varphi t}$ (52%), $C_{\varphi Q}^{(-)}$ (47%)	$ggF, VBF \rightarrow WW^*$ (49%) $WH, ZH \rightarrow \gamma\gamma$ (18%)

We can see, for example, the most constrained eigenvector, i.e. the 1st one, is mainly due to $H \rightarrow \gamma\gamma$. From Eq. 5.4 we see that it places a constraint mainly on C_{tB} . This is due to

its relatively large contributions to $H \rightarrow \gamma\gamma$. Similarly, the second one comes mostly from $gg \rightarrow H$. The constraint is mostly on $C_{t\phi}$ as it enters the ggH loop. The third and the fourth are two combinations of U parameter and $gg \rightarrow H \rightarrow \gamma Z$, and from the sensitivities we know that in the latter it is the $H \rightarrow \gamma Z$ that leads to the bounds, on three most relevant operators. Until this point, the most useful information comes from processes that are loop-induced in the SM, from which tighter constraints are expected. The last three eigenvalues are dominated by corrections to tree-level processes in the SM, and mainly constrain the first four operators that give rise to vector-like ttV and tbW couplings. They rely mostly on the VH and VBF production channels and ZZ^* , WW^* and $b\bar{b}$ decay channels. This information is also given in Figure 2 left, where the heights of the bars are the constraints of each eigenstate (in terms of Λ/\sqrt{C}), and different colours indicate relative contributions of different measurements to this constraint, taking into account all decay channels and the U parameter measurement. For each decay channel all production modes are included. Similarly, the relative contributions from all production channels (with all decay modes grouped together) and the U parameter is given in Figure 2 right.

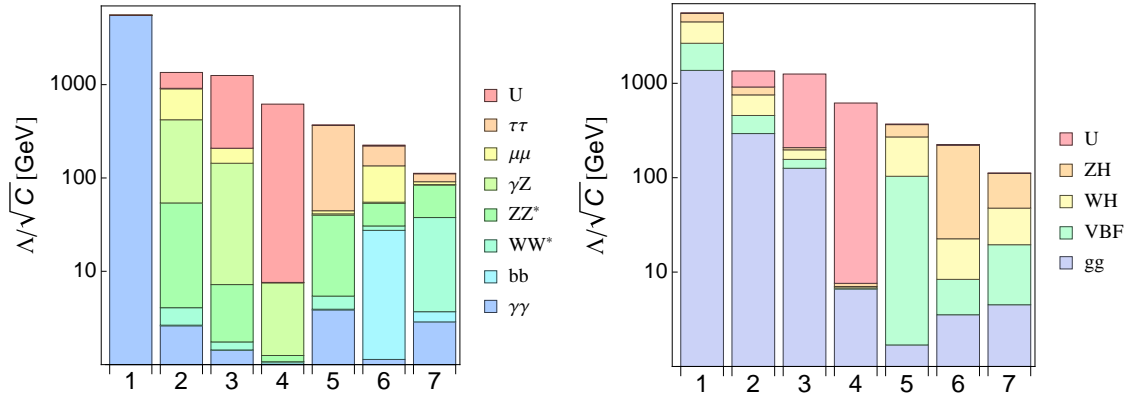


Figure 2. Sensitivities for each eigenstate, and the relative contributions from each channel for $\mu_{EFT} = 125$ GeV.

Following the same procedure for $\mu_{EFT} = 1000$ GeV, we find the following eigenstates:

$$\begin{pmatrix} -0.061 & -0.15 & 0.016 & -0.045 & -0.13 & -0.98 & 0.055 \\ -0.036 & -0.064 & 0.013 & -0.4 & -0.38 & 0.13 & 0.82 \\ 0.13 & 0.0054 & -0.018 & -0.17 & 0.9 & -0.099 & 0.36 \\ 0.11 & 0.46 & -0.091 & 0.77 & -0.048 & -0.087 & 0.4 \\ -0.019 & -0.84 & -0.31 & 0.41 & 0.035 & 0.11 & 0.14 \\ 0.61 & 0.12 & -0.73 & -0.21 & -0.11 & -0.051 & -0.097 \\ 0.77 & -0.2 & 0.6 & 0.072 & -0.083 & 0.0012 & 0.004 \end{pmatrix} \times \frac{1\text{TeV}^2}{\Lambda^2} = \pm \begin{pmatrix} C_{\varphi t} \\ C_{\varphi Q}^{(+)} \\ C_{\varphi Q}^{(-)} \\ C_{\varphi tb} \\ C_{tW} \\ C_{tB} \\ C_{t\varphi} \end{pmatrix} = \pm \begin{pmatrix} 0.041 \\ 0.487 \\ 0.638 \\ 1.45 \\ 1.55 \\ 5.84 \\ 12.7 \end{pmatrix} \quad (5.5)$$

The sensitivities are in general better due to the log enhanced terms. The most important channels for each eigenstate are slightly different. We show the channel decomposition in Figure 3.

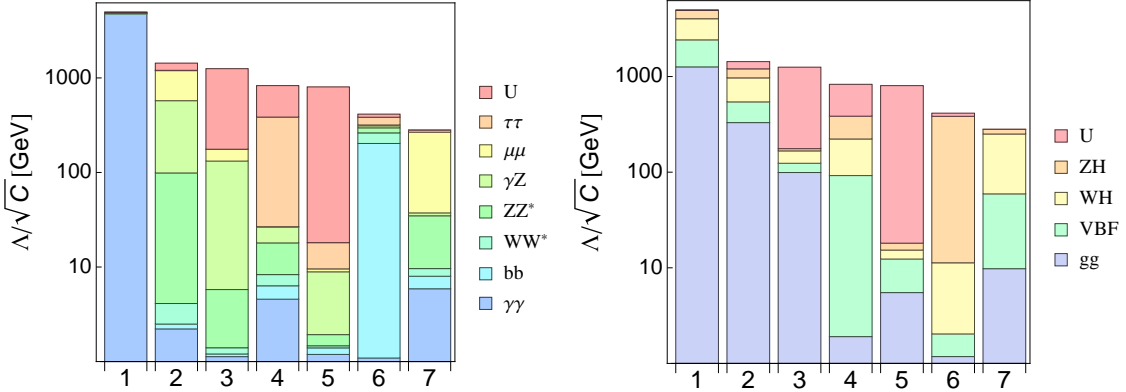


Figure 3. Sensitivities for each eigenstates, and the relative contributions from each channel for $\mu_{EFT} = 1000$ GeV.

5.4 Improvements with differential distributions

Higher dimensional operators typically lead to different differential distributions than the SM, due to different Lorentz structures and sometimes an E^2/Λ^2 enhancement. This is expected also at the loop order, and therefore to fully exploit this behaviour, we study differential observables for the Higgs production processes, which can be easily simulated thanks to our implementation. Again, we show results both for $\mu_{EFT} = \Lambda = 1$ TeV and for $\mu_{EFT} = M_H = 125$ GeV.

As a representative sample of distributions, we show the transverse momentum of the Higgs and invariant mass distribution of the ZH system in ZH in Figure 4, whilst the corresponding distributions for WH are shown in Figure 5. For VBF we show the Higgs and hardest jet transverse momentum distributions in Figure 6. The vertical axes are the bin-by-bin relative deviation w.r.t the LO SM prediction, i.e. following the definition in Eq. (4.4).

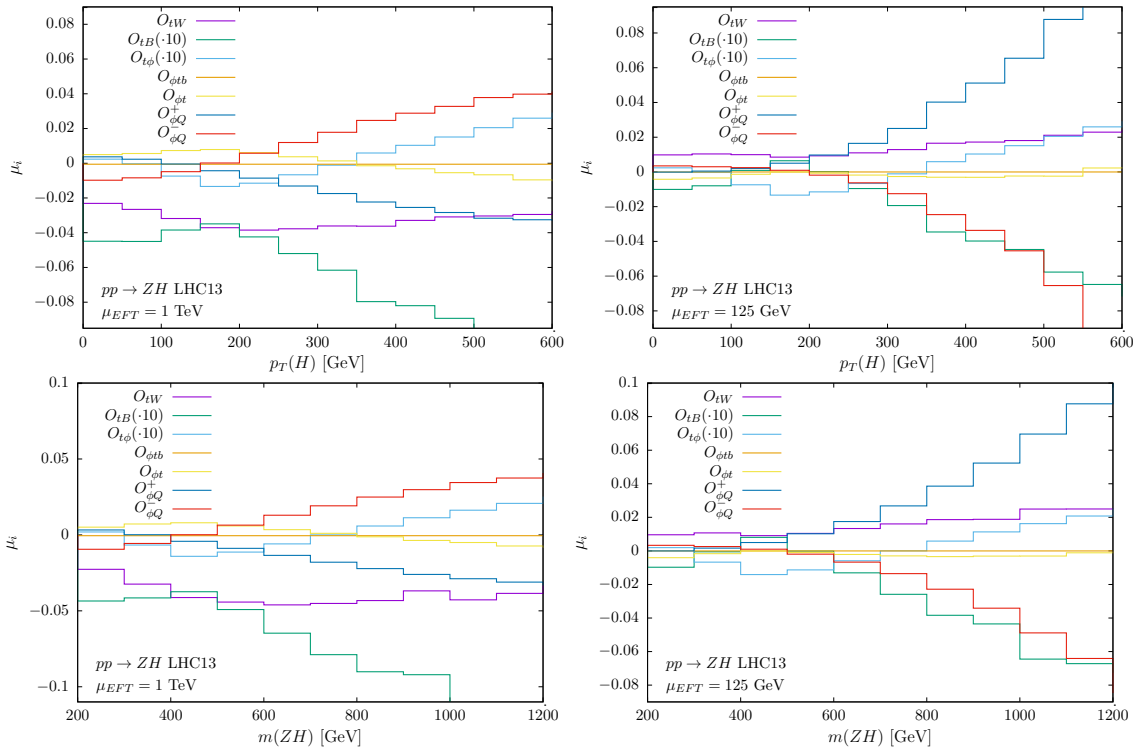


Figure 4. Sensitivity of the Higgs transverse momentum distribution (top) and ZH invariant mass distribution (bottom) in ZH production for the different operators at $\mu_{EFT} = 1000$ GeV (left) and $\mu_{EFT} = 125$ GeV (right).

We find that in most cases, the impact of the operators increases in the tails giving larger deviations from the SM prediction than those obtained at the inclusive level. By comparing the two μ_{EFT} scales we find significant differences related to the impact of the logarithmic terms, which are present in the predictions for $\mu_{EFT} = 1000$ GeV but absent at $\mu_{EFT} = 125$. In most cases the finite contributions which are the only ones present at $\mu_{EFT} = 125$ are far from negligible. For VH production we find that the two observables we consider, i.e. $p_T(H)$ and $m(VH)$ show similar sensitivities at $m(VH) \sim 2p_T(H)$. Similarly in VBF, the two p_T distributions show comparable effects but typically smaller than what is seen in VH production. An interesting observation is that $O_{\phi t}$ gives rise to a constant deviation in the WH production channel. As we have explained in Section 4, this is due to the renormalisation scheme we are using, and the contribution enters only through Higgs wave-function renormalisation, so no different kinematics can be generated.

Given that the top-quark operators give rise to harder $p_T(H)$ distributions, we could

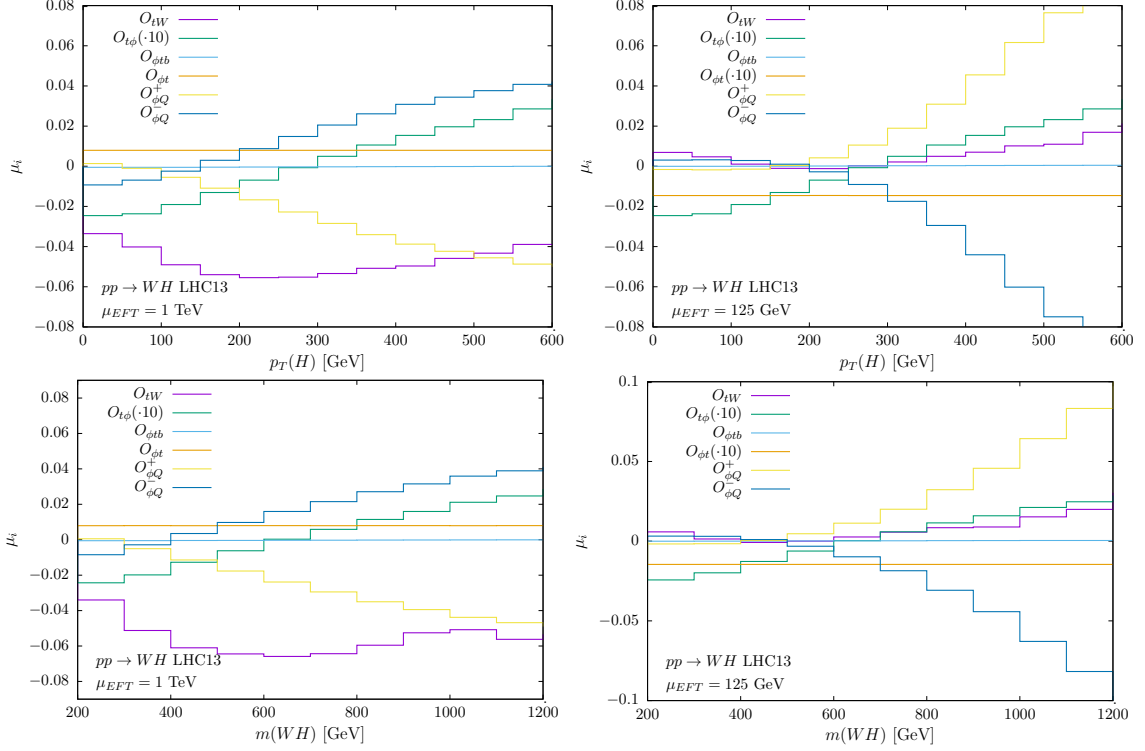


Figure 5. Sensitivity of the Higgs transverse momentum distribution (top) and WH invariant mass distribution (bottom) in WH production for the different operators at $\mu_{EFT} = 1000 \text{ GeV}$ (left) and $\mu_{EFT} = 125 \text{ GeV}$ (right).

use the differential information to improve the sensitivity at the HL-LHC. To estimate the potential of differential measurements at HL-LHC, again we follow the approach in Ref. [80], and assume that the number of events in the j th bin of an X -like measurement, from production channel i and decay channel f , is given by

$$N_{X\text{-like},i,f,j}^{SM} = r_j^X N_{X\text{-like},i,f}^{SM} \quad (5.6)$$

where r_j^X is the ratio of the cross section of the j th bin with the total cross section for process i . For each production-like mode we use r_j^X only for the dominant production process and decay. The same assumption is made for the background. Theoretical errors are taken to be the same as the inclusive ones. Systematic errors are also scaled using r_j^X . Unlike Ref. [80], we consider the differential distributions in all three channels: WH , VH and VBF, and use different binning. The r_j^X values as well as the deviations in the signal strength, i.e. μ_{ij} in each $p_T(H)$ bin, for all three production channels, are given in Tables 16 and 17 in Appendix A.

The resulting individual sensitivities are not significantly different than the inclusive analysis, as they are dominated by the loop-induced processes, such as $gg \rightarrow H$, $H \rightarrow \gamma\gamma, \gamma Z$ where no distributions can be used. However, by looking into the eigenvalues of the χ^2 we find improvements in particular in the last three eigenvalues, which are mainly driven

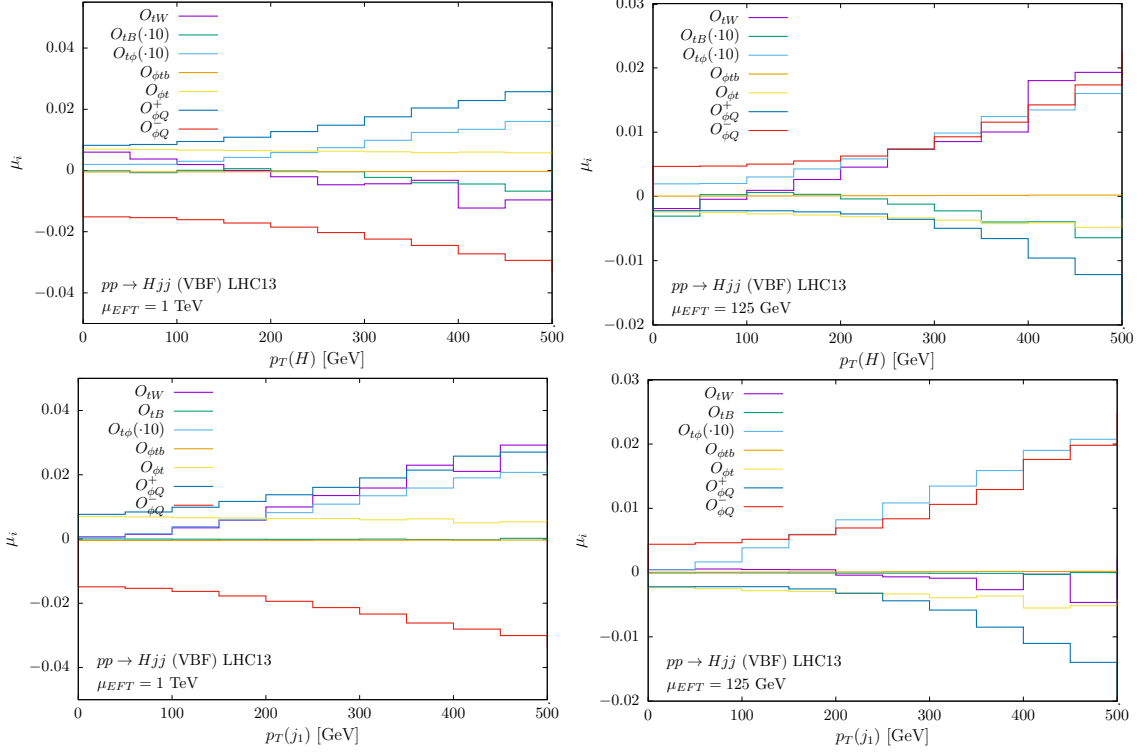


Figure 6. Sensitivity of the Higgs (top) and hardest jet (bottom) transverse momentum distribution in VBF Higgs production for the different operators at $\mu_{EFT} = 1000$ GeV (left) and $\mu_{EFT} = 125$ GeV (right).

by the top-loop corrections to SM tree-level processes. For $\mu_{EFT} = 125$ GeV we have

$$\begin{pmatrix}
 -0.025 & 0.045 & 0.019 & 0.005 & -0.43 & -0.9 & -0.041 \\
 0.024 & -0.073 & -0.058 & -0.051 & 0.4 & -0.24 & 0.88 \\
 0.00076 & 0.19 & 0.069 & -0.033 & -0.78 & 0.36 & 0.47 \\
 -0.26 & 0.91 & 0.24 & -0.0082 & 0.21 & -0.043 & -0.0097 \\
 0.39 & 0.28 & -0.64 & -0.6 & -0.0067 & -0.0076 & -0.064 \\
 0.13 & 0.2 & -0.57 & 0.78 & -0.016 & 0.0051 & 0.03 \\
 0.87 & 0.12 & 0.44 & 0.15 & 0.045 & -0.03 & -0.0043
 \end{pmatrix}
 \times \frac{1\text{TeV}^2}{\Lambda^2}
 \begin{pmatrix}
 C_{\varphi t} \\
 C_{\varphi Q}^{(+)} \\
 C_{\varphi Q}^{(-)} \\
 C_{\varphi Q} \\
 C_{\varphi tb} \\
 C_{tW} \\
 C_{tB} \\
 C_{t\varphi}
 \end{pmatrix}
 = \pm
 \begin{pmatrix}
 0.0325 \\
 0.543 \\
 0.63 \\
 2.53 \\
 6.03 \\
 14.8 \\
 32.1
 \end{pmatrix},
 \text{ compared with }
 \begin{pmatrix}
 0.0326 \\
 0.548 \\
 0.637 \\
 2.62 \\
 7.31 \\
 19.8 \\
 79.6
 \end{pmatrix}
 \text{ from inclusive measurements.}
 \tag{5.7}$$

The improvement on the last eigenstate is about a factor of 2.5. On average, the Global Determinant Parameter (GDP) [83] of this fit is improved by a factor of 0.81 compared to

the inclusive results, which is not huge, but it is very important that the weaker constraints receive larger improvements, which means that directions that were almost flat are now lifted. For $\mu_{EFT} = 1$ TeV we find:

$$\begin{pmatrix} -0.061 & -0.15 & 0.016 & -0.046 & -0.13 & -0.98 & 0.054 \\ -0.034 & -0.065 & 0.022 & -0.42 & -0.35 & 0.12 & 0.83 \\ 0.13 & -0.0042 & -0.016 & -0.17 & 0.92 & -0.1 & 0.32 \\ -0.12 & -0.24 & 0.2 & -0.83 & 0.03 & 0.058 & -0.45 \\ -0.042 & -0.93 & -0.28 & 0.2 & 0.037 & 0.13 & 0.032 \\ 0.52 & 0.14 & -0.79 & -0.25 & -0.099 & -0.049 & -0.11 \\ 0.83 & -0.18 & 0.51 & 0.056 & -0.096 & -0.0056 & -0.0042 \end{pmatrix} \times \frac{1\text{TeV}^2}{\Lambda^2} \begin{pmatrix} C_{\varphi t} \\ C_{\varphi Q}^{(+)} \\ C_{\varphi Q}^{(-)} \\ C_{\varphi t b} \\ C_{tW} \\ C_{tB} \\ C_{t\varphi} \end{pmatrix} \\ = \pm \begin{pmatrix} 0.0409 \\ 0.479 \\ 0.629 \\ 1.3 \\ 1.5 \\ 5.44 \\ 10.8 \end{pmatrix}, \text{ compared with } \begin{pmatrix} 0.041 \\ 0.487 \\ 0.638 \\ 1.45 \\ 1.55 \\ 5.84 \\ 12.7 \end{pmatrix} \text{ from inclusive measurements.} \quad (5.8)$$

Improvements are smaller than the $\mu_{EFT} = 125$ GeV case.

In summary, after taking into account differential distributions, the one-sigma constraints on the seven linear combinations of top operator coefficients span the range from $\mathcal{O}(10^{-2})\text{TeV}^{-2}$ to $\mathcal{O}(10)\text{TeV}^{-2}$. This reflects the HL-LHC potential on probing top-quark operators through EW loops. We summarise the individual and marginalised sensitivities in Figure 7. They are not stronger than the current ones from direct top-quark measurements, but are definitely competitive. This means that in the near future the loop-induced effects cannot be neglected, and the only way to correctly take them into account is to perform global SMEFT fits by combining both the top-quark and the Higgs-boson sectors.

5.5 Loop/tree discrimination

Until now we have focused on the sensitivities of the top operators, and have not considered the effects of Higgs operators at the tree level. In a real fit, one has to consider these contributions, and include sufficient observables so that no blind directions remain. In the following we briefly argue that, in principle, we can discriminate the tree-level contribution from Higgs operators and loop-level contribution from top operators, by only using Higgs measurements. This possibility relies on the finite non-logarithmic terms, σ_{fin} , in Eq. (1.1). The reason is that the logarithmic terms are completely captured by RG effects, and are thus process- and observable-independent. If one considers only these effects, the discrimination between top/Higgs operators would be impossible no matter how many observables are included.

As an example, consider the top-quark operator C_{tB} which mixes into $C_{\varphi B}$ and $C_{\varphi WB}$. The latter mixing does not exist in our scheme as we renormalise it to a physical quantity. Consider the measurements $H \rightarrow \gamma\gamma, \gamma Z, WW^*, ZZ^*$ and ZH/WH production. Another

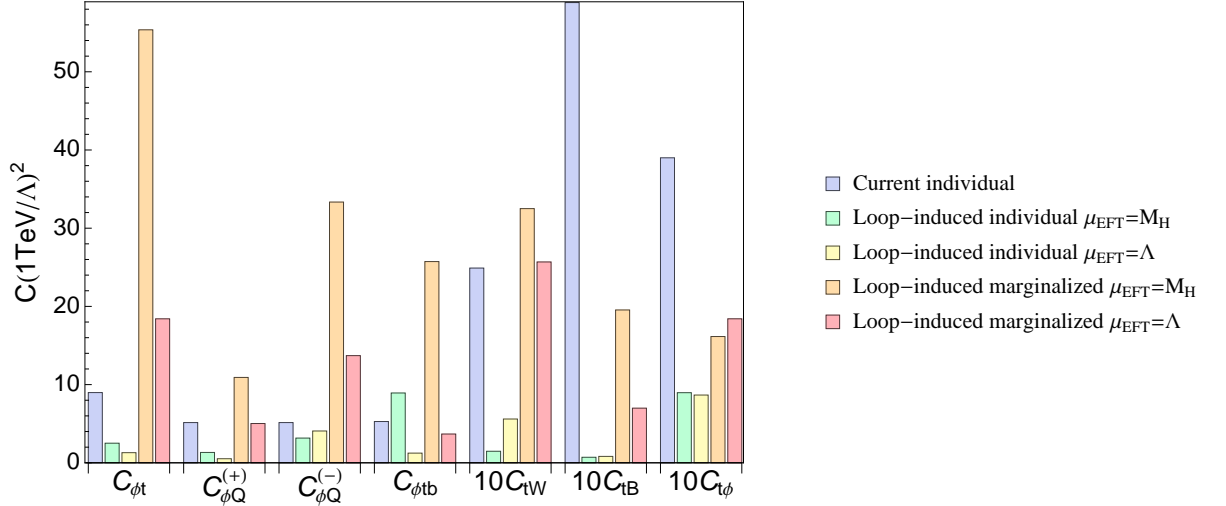


Figure 7. Individual and marginalised sensitivities (i.e. one-half of 95% CL interval) at HL-LHC through top loops, including differential measurements, compared with current individual limits. μ_{EFT} is set at either $M_H = 125$ GeV or $\Lambda = 1$ TeV.

operator that enters these observables is $O_{\varphi W}$. The contributions from $O_{\varphi W}$ and $O_{\varphi B}$ at the tree level are computed and given in Tables 1 and 2. Assuming all these processes are measured with 10% precision, we can construct a χ^2 and marginalise over the $O_{\varphi W}$ operator. Taking $\mu_{EFT} = 125$ GeV, after diagonalisation we find

$$C_{\varphi B} + 0.021C_{tB} = \pm 0.0022 (\Lambda/1\text{TeV})^2, \quad (5.9)$$

$$C_{tB} - 0.021C_{\varphi B} = \pm 6.7 (\Lambda/1\text{TeV})^2, \quad (5.10)$$

so both directions are constrained and no blind direction is left.

On the other hand, if one takes $\mu_{EFT} = 1$ TeV but only includes the logarithmic terms, the situation will be different. In this case we find

$$C_{\varphi B} - 0.046C_{tB} = \pm 0.0022 (\Lambda/1\text{TeV})^2, \quad (5.11)$$

$$C_{tB} + 0.046C_{\varphi B} = \pm \infty (\Lambda/1\text{TeV})^2, \quad (5.12)$$

so one combination is unconstrained. This demonstrates that the finite contributions in the SMEFT loop corrections are important, not only because their sizes can be large, but more importantly, because they allow us to discriminate the pure loop-induced effects from the tree-level contributions of other operators, into which they could mix, by combining various measurements, preferably at different energies, to eliminate possible unconstrained directions in a global fit. This is why we believe a study taking $\mu_{EFT} = M_H = 125$ GeV is a more reasonable estimate of sensitivities that can be achieved in a bottom-up global fit, where the discriminating power between loop- and tree-level effects is crucial for setting bounds on top operators. In Figure 8 we illustrate that the $H \rightarrow ZZ^*$ and ZH production are complementary in the $C_{\varphi B} - C_{tB}$ plane.

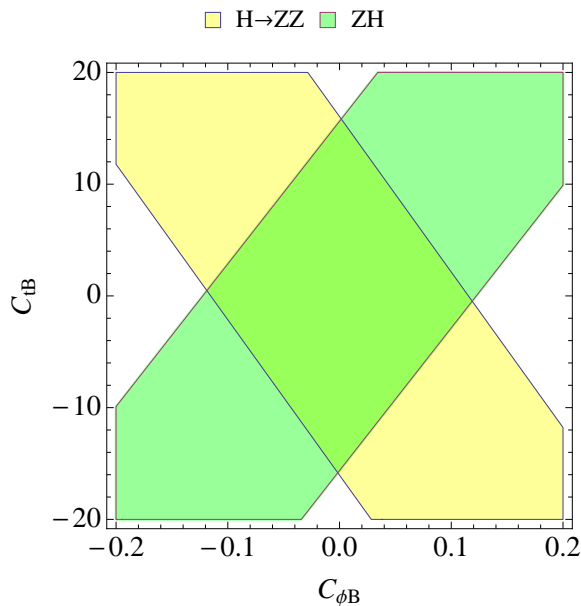


Figure 8. Constraining both C_{tB} (top operator, loop level) and $C_{\phi B}$ (Higgs operator, tree level) by combining $H \rightarrow ZZ^*$ and ZH production, assuming 1% precision on both. $\mu_{EFT} = 125$ GeV. $\Lambda = 1$ TeV.

Instead of combining several inclusive measurements, one could also use the differential information in one measurement. The differential distributions of the logarithmic terms can not be distinguished from the tree level ones, but they differ from the ones of the finite terms. In Figure 9 we compare the normalised distributions (over the SM) from finite and log terms for the operators which show the most promising energy dependence in VH production. These plots demonstrate that indeed the kinematic behaviour of the finite and logarithmic terms can be very different, and so the kinematic distributions will serve as discriminating observables in a global fit, lifting the degeneracy between loop and tree-level contributions.

6 Conclusion

We have computed the NLO EW corrections to Higgs production and decay processes from dim-6 top-quark operators in the SMEFT framework. We have studied the major production channels including VBF, WH and ZH at the LHC, ZH and VBF at e^+e^- colliders, and the major decay channels including $H \rightarrow \gamma\gamma, \gamma Z, Zll, Wl\nu, bb, \mu\mu, \tau\tau$. These results are part of the ongoing efforts of automating SMEFT simulations for colliders at NLO, and is a first step towards including EW corrections.

These results allow us to study whether the Higgs measurements at the LHC and future colliders are sensitive to possible deviations in the top-quark sector. We find that, within the current direct constraints on the top-quark sector, the top-quark operators can shift the signal strength of the loop-induced Higgs processes, i.e. $gg \rightarrow H$ and $H \rightarrow \gamma\gamma, \gamma Z$ by

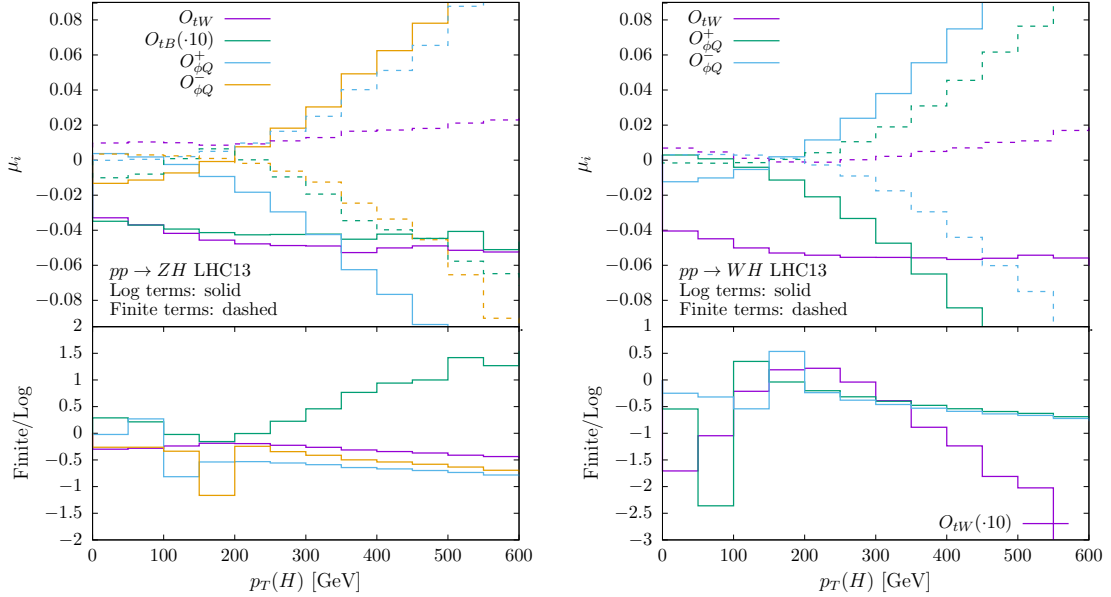


Figure 9. Comparison of logarithmic and finite terms in the Higgs transverse momentum distribution in ZH and WH production for the different operators. The lower panels show the ratio of the finite over the logarithmic terms.

factors $\sim \mathcal{O}(1) - \mathcal{O}(10)$, and that of the tree-level processes, i.e. all remaining production and decay channels, by $\sim 5 - 10\%$ through loop corrections at the LHC and up to 15% at future lepton colliders. This implies that with the current precision we can already learn about top-quark couplings by using EW loops in Higgs measurements, while in the future, at the high-luminosity scenario, all Higgs measurements can be sensitive to top-quark couplings. It also implies that at an e^+e^- collider, even measurements below the $t\bar{t}$ threshold can be sensitive to deviations in top-quark couplings. As a result, in a global fit for Higgs couplings based on the SMEFT approach, theoretical uncertainties due to unknown top-quark operators are not negligible and should be taken into account.

These results also allow us to quantitatively derive the experimental sensitivities to top-quark operators at the HL-LHC, by only using the Higgs observables. Using projected inclusive measurements, we are able to constrain all directions in the 7-dimensional parameter space spanned by all seven operator coefficients. We have also studied the change of differential distributions from top-quark operators, and have found that the signal/background ratio is enhanced at the tail of the distributions. By considering the $p_T(H)$ distributions in VBF, WH and ZH production processes, we have significantly improved the sensitivities on the most weakly constrained eigenvectors. The resulting one-sigma range on the seven eigenvectors of Wilson coefficients span the range from $\mathcal{O}(10^{-2})\text{TeV}^{-2}$ to $\mathcal{O}(10)\text{TeV}^{-2}$.

Finally, we have briefly discussed possible ways to discriminate the loop-level top-quark operator contributions from the tree-level Higgs operator contributions, which is necessary in a global fit. We have demonstrated that this can be done by combining several observables or looking into the differential distributions, and that the crucial information is supplied by the finite (i.e. non-logarithmic) terms in the full NLO EW corrections. Therefore, even

channel	μ_{EFT} [GeV]	$O_{\varphi t}$	$O_{\varphi Q}^{(+)}$	$O_{\varphi Q}^{(-)}$	$O_{\varphi tb}$	O_{tW}	O_{tB}	$O_{t\varphi}$
$H \rightarrow bb$	125	0	-0.07	0.11	-1.13	-0.28	0	-0.18
$H \rightarrow bb$	1000	0	-0.99	-0.91	-8.18	0.34	0	0.29
$H \rightarrow ll$	125	0	-0.02	0.02	-0.00	0	0	-0.27
$H \rightarrow ll$	1000	0	0.45	-0.45	-0.03	0	0	0.68
$H \rightarrow \gamma\gamma$	125	0	0	0	0	-73.3	-136.8	3.45
$H \rightarrow \gamma\gamma$	1000	0	0	0	0	114.6	214.0	3.45
$H \rightarrow Z\gamma$	125	1.77	0.03	1.77	0	-45.8	6.97	0.72
$H \rightarrow Z\gamma$	1000	1.77	0.03	1.77	0	71.3	-9.69	0.72
$H \rightarrow Zll$	125	-0.65	-0.07	0.65	-0.00	0.22	-0.02	0.08
$H \rightarrow Zll$	1000	0.88	0.47	-1.49	-0.04	-0.16	0.11	0.08
$H \rightarrow Wl\nu$	125	0	-0.25	0.25	0.00	-0.13	0	-0.03
$H \rightarrow Wl\nu$	1000	0	1.08	-1.08	-0.08	0.33	0	-0.03

Table 14. Percentage deviation μ_{ij} for decay channel i and operator j , in the \overline{MS} scheme.

though they cannot be obtained using the RG matrix, it is very important to compute these finite terms for an actual SMEFT fit.

In conclusion, as the experimental precision on Higgs measurements continues to improve, the NLO EW corrections from dim-6 top-quark operators via top-loop effects have started to become relevant. For this reason, treating the dim-6 top-quark sector and the Higgs/EW sector separately may not continue to be a good strategy. A global SMEFT analysis taking into account both sectors by combining Higgs and top-quark measurements is desirable. Our calculation is a first step towards this direction, and our implementation in the MG5_aMC framework provides an automatic and realistic simulation tool for this purpose.

Acknowledgements

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A More numerical results

In Tables 14 and 15 we present results similar to Tables 1 and 2 but with the standard \overline{MS} scheme. In Tables 16 and 17 we show the r_j^X values for the distributions we consider in Section 5.4, as well as the deviations in the signal strength, i.e. μ_{ij} in each $p_T(H)$ bin, for all three production channels.

channel	μ_{EFT} [GeV]	$O_{\varphi t}$	$O_{\varphi Q}^{(+)}$	$O_{\varphi Q}^{(-)}$	$O_{\varphi tb}$	O_{tW}	O_{tB}	$O_{t\varphi}$
$pp \rightarrow ZH$	125	-0.44	0.16	0.33	0.00	0.80	-0.29	-0.02
$pp \rightarrow ZH$	1000	1.45	-0.64	-1.05	-0.02	-1.53	0.93	-0.02
$pp \rightarrow WH$	125	0	-0.06	0.06	-0.00	0.43	0	-0.21
$pp \rightarrow WH$	1000	0	0.18	-0.18	-0.08	-4.09	0	-0.21
$pp \rightarrow Hjj$	125	-0.21	-0.25	0.46	0.01	0.04	-0.02	0.03
$pp \rightarrow Hjj$	1000	0.36	1.10	-1.48	-0.06	0.36	0.09	0.03

Table 15. Percentage deviation μ_{ij} for production channel i and operator j , in the \overline{MS} scheme.

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Bin [GeV]	Channel	r value	$O_{\varphi t}$	$O_{\varphi Q}^{(+)}$	$O_{\varphi Q}^{(-)}$	$O_{\varphi tb}$	O_{tW}	O_{tB}	$O_{t\varphi}$
0-50	VBF	0.22	-0.24	-0.22	0.47	0.01	-0.19	-0.03	0.02
	WH	0.35	-0.15	-0.16	0.31	0.00	0.69	0.00	-0.25
	ZH	0.34	-0.42	-0.01	0.35	0.00	0.98	-0.10	0.02
50-100	VBF	0.37	-0.25	-0.22	0.47	0.01	-0.04	0.00	0.02
	WH	0.38	-0.15	-0.18	0.32	0.00	0.47	0.00	-0.24
	ZH	0.38	-0.35	0.05	0.30	0.00	1.00	-0.08	0.00
100-150	VBF	0.23	-0.27	-0.22	0.50	0.01	0.09	0.01	0.03
	WH	0.16	-0.15	-0.14	0.29	0.00	0.11	0.00	-0.19
	ZH	0.17	-0.13	0.20	0.25	0.00	0.99	0.01	-0.07
150-200	VBF	0.1	-0.29	-0.24	0.55	0.01	0.26	0.00	0.04
	WH	0.062	-0.15	0.04	0.10	0.01	-0.10	0.00	-0.13
	ZH	0.066	0.00	0.50	0.09	0.00	0.85	0.06	-0.13
200-250	VBF	0.043	-0.32	-0.27	0.63	0.01	0.46	0.00	0.06
	WH	0.026	-0.15	0.42	-0.27	0.01	-0.12	0.00	-0.07
	ZH	0.027	-0.07	0.97	-0.19	0.00	0.93	0.00	-0.11
250-300	VBF	0.018	-0.33	-0.36	0.73	0.01	0.73	-0.01	0.07
	WH	0.012	-0.15	1.10	-0.91	0.02	0.02	0.00	-0.01
	ZH	0.012	-0.18	1.60	-0.63	0.00	1.10	-0.10	-0.07
300-350	VBF	0.0087	-0.37	-0.50	0.93	0.01	0.85	-0.02	0.10
	WH	0.0063	-0.15	1.90	-1.70	0.03	0.22	0.00	0.05
	ZH	0.0056	-0.26	2.50	-1.30	0.00	1.30	-0.19	-0.01
350-400	VBF	0.0038	-0.42	-0.66	1.20	0.02	1.00	-0.04	0.12
	WH	0.0034	-0.15	3.10	-2.90	0.03	0.49	0.00	0.11
	ZH	0.0033	-0.31	4.00	-2.50	0.00	1.70	-0.35	0.06
400-450	VBF	0.002	-0.41	-0.96	1.40	0.02	1.80	-0.04	0.13
	WH	0.002	-0.15	4.60	-4.40	0.04	0.70	0.00	0.15
	ZH	0.0017	-0.31	5.10	-3.40	0.00	1.70	-0.40	0.10
450-500	VBF	0.00098	-0.48	-1.20	1.70	0.02	1.90	-0.06	0.16
	WH	0.0014	-0.15	6.20	-6.00	0.04	1.00	0.00	0.20
	ZH	0.0011	-0.24	6.50	-4.50	0.00	1.80	-0.45	0.15
500+	VBF	0.0014	-0.58	-2.50	3.00	0.03	3.00	-0.10	0.21
	WH	0.0024	-0.15	14.00	-14.00	0.05	1.90	0.00	0.32
	ZH	0.0021	0.35	15.00	-12.00	0.00	2.40	-0.71	0.29

Table 16. r values and percentage deviations μ_{ij} for VBF, WH and ZH production in 11 bins of the $p_T(H)$ distribution at $\mu_{EFT} = 125$ GeV.

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Bin [GeV]	Channel	r value	$O_{\varphi t}$	$O_{\varphi Q}^{(+)}$	$O_{\varphi Q}^{(-)}$	$O_{\varphi tb}$	O_{tW}	O_{tB}	$O_{t\varphi}$
0-50	VBF	0.22	0.70	0.82	-1.50	-0.05	0.60	0.00	0.02
	WH	0.35	0.79	0.13	-0.93	-0.05	-3.40	0.00	-0.25
	ZH	0.34	0.50	0.37	-0.98	-0.05	-2.30	-0.45	0.02
50-100	VBF	0.37	0.69	0.85	-1.50	-0.05	0.37	-0.01	0.02
	WH	0.38	0.79	-0.10	-0.69	-0.05	-4.00	0.00	-0.24
	ZH	0.38	0.56	0.23	-0.84	-0.05	-2.70	-0.45	0.00
100-150	VBF	0.23	0.67	0.95	-1.60	-0.04	0.20	0.00	0.03
	WH	0.16	0.79	-0.55	-0.24	-0.05	-4.90	0.00	-0.19
	ZH	0.17	0.73	-0.05	-0.48	-0.05	-3.20	-0.38	-0.07
150-200	VBF	0.1	0.65	1.10	-1.70	-0.04	0.00	0.01	0.04
	WH	0.062	0.79	-1.10	0.30	-0.04	-5.40	0.00	-0.13
	ZH	0.066	0.79	-0.43	0.01	-0.05	-3.70	-0.35	-0.13
200-250	VBF	0.043	0.64	1.30	-1.90	-0.04	-0.20	0.00	0.06
	WH	0.026	0.79	-1.70	0.88	-0.04	-5.50	0.00	-0.07
	ZH	0.027	0.61	-0.86	0.58	-0.05	-3.80	-0.42	-0.11
250-300	VBF	0.018	0.63	1.50	-2.00	-0.04	-0.47	0.00	0.07
	WH	0.012	0.79	-2.30	1.50	-0.03	-5.50	0.00	-0.01
	ZH	0.012	0.37	-1.30	1.20	-0.05	-3.80	-0.52	-0.07
300-350	VBF	0.0087	0.61	1.80	-2.20	-0.04	-0.43	-0.02	0.10
	WH	0.0063	0.79	-2.80	2.10	-0.03	-5.30	0.00	0.05
	ZH	0.0056	0.13	-1.70	1.80	-0.05	-3.60	-0.62	-0.01
350-400	VBF	0.0038	0.58	2.00	-2.50	-0.04	-0.32	-0.04	0.12
	WH	0.0034	0.79	-3.40	2.60	-0.02	-5.10	0.00	0.11
	ZH	0.0033	-0.14	-2.20	2.50	-0.05	-3.60	-0.80	0.06
400-450	VBF	0.002	0.60	2.30	-2.70	-0.03	-1.20	-0.04	0.13
	WH	0.002	0.79	-3.90	3.10	-0.02	-5.00	0.00	0.15
	ZH	0.0017	-0.32	-2.50	2.90	-0.05	-3.30	-0.82	0.10
450-500	VBF	0.00098	0.58	2.60	-2.90	-0.03	-0.96	-0.07	0.16
	WH	0.0014	0.79	-4.20	3.40	-0.01	-4.60	0.00	0.20
	ZH	0.0011	-0.55	-2.80	3.30	-0.05	-3.10	-0.89	0.15
500+	VBF	0.0014	0.55	3.20	-3.50	-0.03	-1.30	-0.08	0.21
	WH	0.0024	0.79	-4.80	4.00	0.00	-3.70	0.00	0.32
	ZH	0.0021	-0.96	-3.10	4.00	-0.05	-2.80	-1.20	0.29

Table 17. r values and percentage deviations μ_{ij} for VBF, WH and ZH production in 11 bins of the $p_T(H)$ distribution at $\mu_{EFT} = 1$ TeV.

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