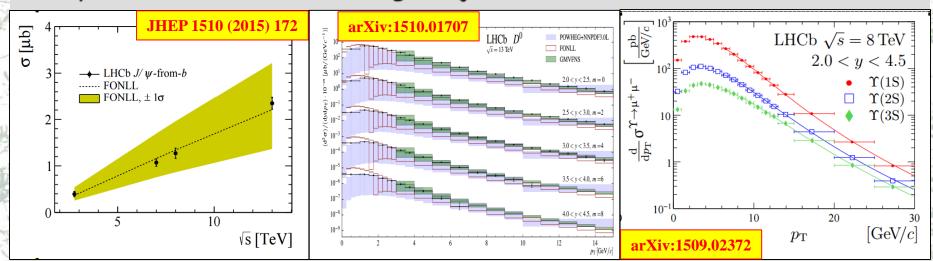




#### High energy hadron gluon collision



- Heavy flavour production at LHC is dominated by gg-fusion process
- Quarkonia: reasonably (rapidly improving) agreement with NR QCD
  - $J/\psi$ ,  $\psi$ ',  $\eta_c$ ,  $\chi_{c1,2}$ ,  $\chi_{b1,2}$ (nP), ....
- Open flavour: FONLL does good job



Heavy flavour production cross-section in forward region is large

$$\sigma(c\overline{c})_{p_{\rm T}<8\,{\rm GeV}/c,\,2.0< y<4.5} = 1419\pm12\,{\rm (stat)}\pm116\,{\rm (syst)}\pm65\,{\rm (frag)}\,\mu{\rm b},$$

VS

$$\sigma_{\text{inel}}^{\text{acc}}(p_{\text{T}} > 0.2 \text{ GeV/}c, \ 2.0 < \eta < 4.5) = 55.0 \pm 2.4 \text{ mb}$$
,

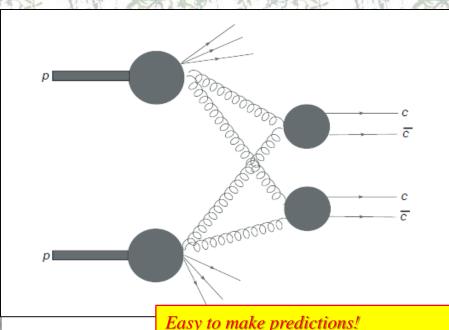
Nucl.Phys. B871 (2013) 1

JHEP 1502 (2015) 129



# DPS: simple paradigm





Two independent hard scattering processes Relations through (unknown) double PDF

$$\Gamma_{ij}(x_1, x_2; \mathbf{b_1}, \mathbf{b_2}; Q_1^2, Q_2^2) = D_h^{ij}(x_1, x_2; Q_1^2, Q_2^2) f(\mathbf{b_1}) f(\mathbf{b_2}),$$

Assume factorization of double PDFs

$$D_h^{ij}(x_1, x_2; Q_1^2, Q_2^2) = D_h^i(x_1; Q_1^2) D_h^j(x_2; Q_2^2).$$

(Can't be true for all  $x,Q^2$ )

Pocket formula

$$\sigma_{\mathrm{DPS}}^{AB} = \frac{m}{2} \frac{\sigma_{\mathrm{SPS}}^{A} \sigma_{\mathrm{SPS}}^{B}}{\sigma_{\mathrm{eff}}}.$$
 $m=1,2$ 

Universal (energy and process independent) factor)

$$1/\sigma_{eff} = \int d^2b F^2(b)$$

And the predictions are easy to test

$$\sigma_{\text{eff}}^{\text{DPS}} = 14.5 \pm 1.7^{+1.7}_{-2.3} \text{ mb}$$

CDF, F.Abe et al., PDR 56 3811 (1997)



#### **DPS**



- Simple pattern, a lot of powerful consequences and interesting predictions
- Pocket formula is also <u>valid for differential cross-sections</u>

$$\begin{split} \sigma^{\text{DPS}}(pp &\to c\bar{c}c\bar{c}X) \\ &= \frac{1}{2\sigma_{\text{eff}}} \sigma^{\text{SPS}}(pp \to c\bar{c}X_1) \cdot \sigma^{\text{SPS}}(pp \to c\bar{c}X_2). \end{split}$$

$$\frac{d\sigma^{\text{DPS}}(pp \to c\bar{c}c\bar{c}X)}{dy_{1}dy_{2}d^{2}p_{1,t}d^{2}p_{2,t}dy_{3}dy_{4}d^{2}p_{3,t}d^{2}p_{4,t}}$$

$$= \frac{1}{2\sigma_{\text{eff}}} \cdot \frac{d\sigma^{\text{SPS}}(pp \to c\bar{c}X_{1})}{dy_{1}dy_{2}d^{2}p_{1,t}d^{2}p_{2,t}} \cdot \frac{d\sigma^{\text{SPS}}(pp \to c\bar{c}X_{2})}{dy_{3}dy_{4}d^{2}p_{3,t}d^{2}p_{4,t}}.$$

- The effective cross-section is a property of proton (integral over transverse degrees of freedom)
  - Smaller than "proton size":  $\pi R^2 \approx 50 \text{mb}$
  - It is universal: energy and process independent
    - easy to compare Tevatron, GPD and LHCb

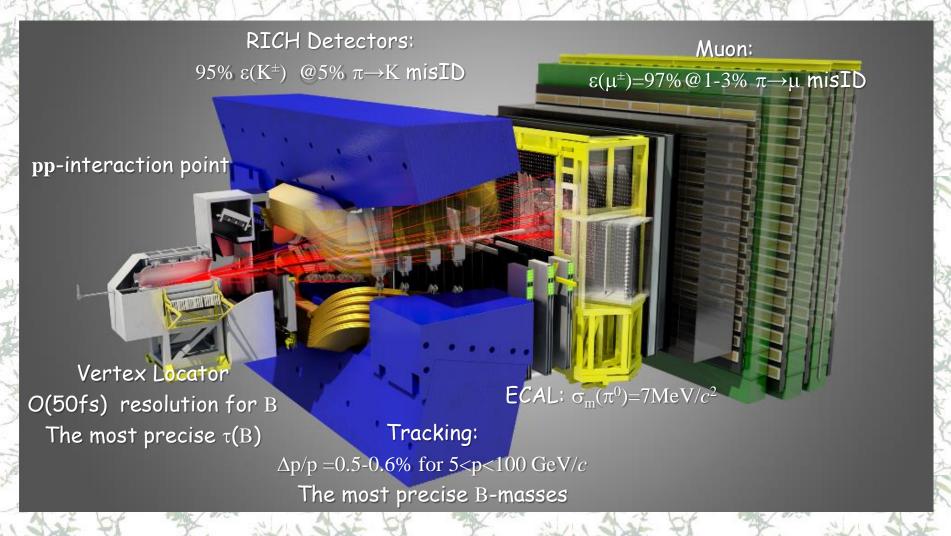
 $\sigma_{eff} \sim \frac{1}{4} \, \sigma_{in}$  production of cross-section for A+B is enhanced with <u>factor of four</u> with respect to naïve model

\* LHCb: 10% of all "hard" events (irrespectively from the process) have additional charm pair



## ~40% of heavy quarks in <4% of $4\pi$



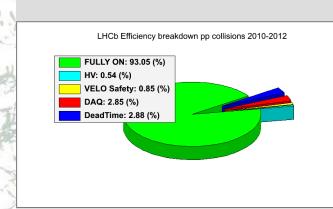


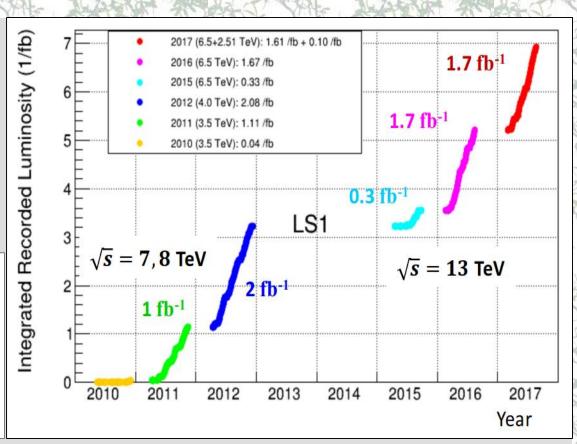


## Run I+II



1fb<sup>-1</sup>@7TeV 2fb<sup>-1</sup>@8TeV 3.5fb<sup>-1</sup> @13TeV





Thanks to LHC accelerator team for the excellent performance of machine

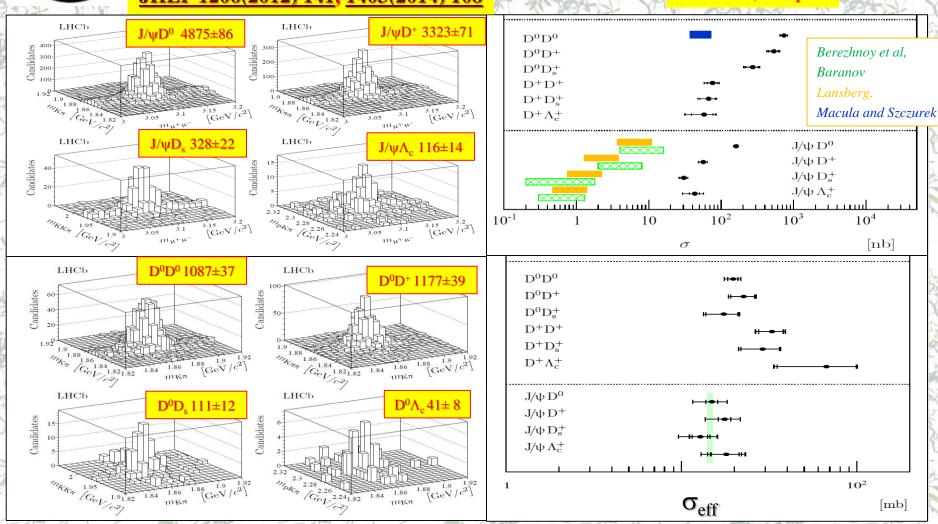


# $J/\psi + c\overline{c}$ and $2 \times c\overline{c}$



#### JHEP 1206(2012) 141, 1403(2014) 108

 $\sqrt{s}=7$ TeV, 355pb<sup>-1</sup>





$$\Upsilon + c\overline{c}$$



NRQCD SPS (Berezhnoy, Likhoded)

$$\frac{\sigma^{\Upsilon c\bar{c}}}{\sigma^{\Upsilon}} = (0.2 - 0.6) \%$$

• Gluon splitting:

$$(0.4-2.0)\%$$

• DPS:

$$rac{\sigma^{\Upsilon ext{c}\overline{ ext{c}}}}{\sigma^{\Upsilon}} = rac{\sigma^{ ext{c}\overline{ ext{c}}}}{\sigma_{ ext{eff}}}.$$

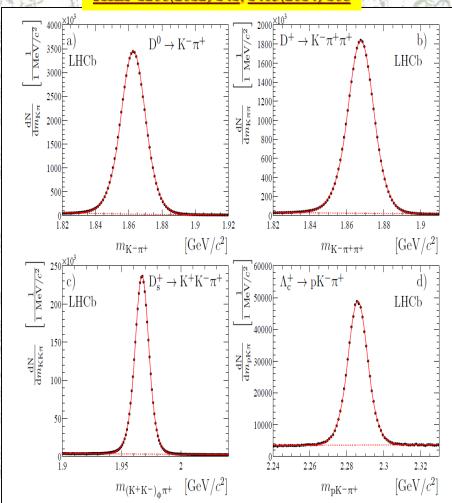
- Predictions are very different
- Expected to be dominated by DPS
- Different kinematic range from J/ψ+cc



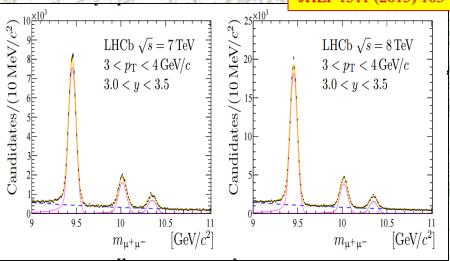
### $\Upsilon + c\overline{c}$



#### JHEP 1206(2012) 141, 1403(2014) 108



#### JHEP 1511 (2015) 103

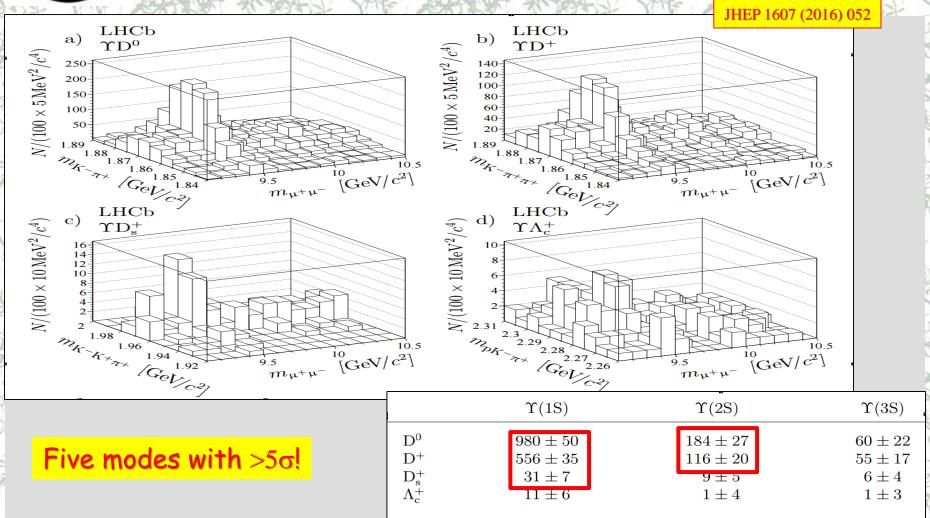


- Whole Run-I dataset: 1+2fb-1
  - $D^0 O(200M/fb^{-1})$
  - $D^+ O(100M/fb^{-1})$
  - $D_s O(10M/fb^{-1})$
  - $\Lambda_{\rm c}$   $O(20\text{M/fb}^{-1})$
  - $\Upsilon(1,2,3S)$ :  $O(3,0.7,0.3M/fb^{-1})$



#### $\Upsilon + c\overline{c}$







# Pileup?

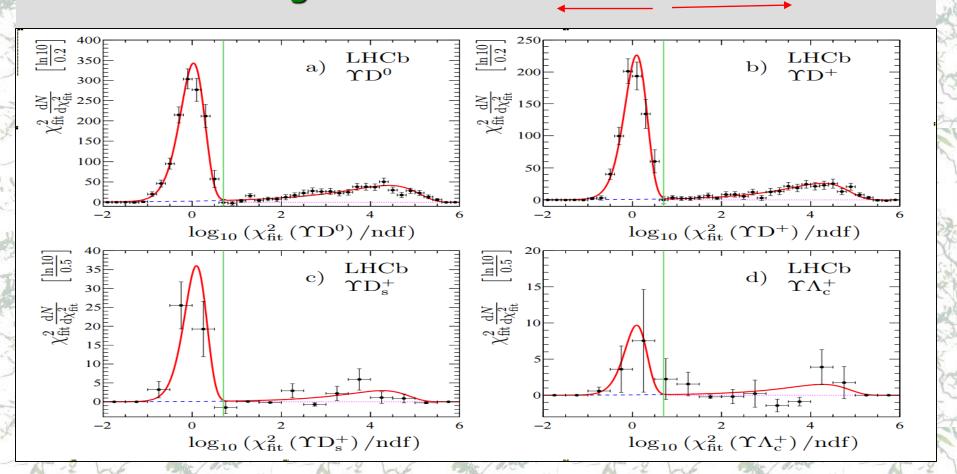


JHEP 1607 (2016) 052

Discriminating variable:

signal

pileup





#### Cross-sections



#### Model-independent

- Per-event efficiencies
  - mainly using data-driven techniques
- Major systematic contributions:
  - hadron interactions in the detector (3-4%) and trigger (2%)

$$\begin{array}{lcl} \mathscr{B}_{\mu^{+}\mu^{-}} \times \sigma^{\Upsilon(1S)D^{0}}_{\sqrt{s}=7\,\mathrm{TeV}} &=& 155 \pm 21\,(\mathrm{stat}) \pm & 7\,(\mathrm{syst})\,\mathrm{pb}\,, \\ \mathscr{B}_{\mu^{+}\mu^{-}} \times \sigma^{\Upsilon(1S)D^{+}}_{\sqrt{s}=7\,\mathrm{TeV}} &=& 82 \pm 19\,(\mathrm{stat}) \pm & 5\,(\mathrm{syst})\,\mathrm{pb}\,, \\ \mathscr{B}_{\mu^{+}\mu^{-}} \times \sigma^{\Upsilon(1S)D^{0}}_{\sqrt{s}=8\,\mathrm{TeV}} &=& 250 \pm 28\,(\mathrm{stat}) \pm 11\,(\mathrm{syst})\,\mathrm{pb}\,, \\ \mathscr{B}_{\mu^{+}\mu^{-}} \times \sigma^{\Upsilon(1S)D^{+}}_{\sqrt{s}=8\,\mathrm{TeV}} &=& 80 \pm 16\,(\mathrm{stat}) \pm & 5\,(\mathrm{syst})\,\mathrm{pb}\,, \end{array}$$

• Agrees with DPS using  $\sigma_{eff}(CDF)$ 

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Significantly exceeds SPS



# Cross-section ratios - I Reduced uncertainties

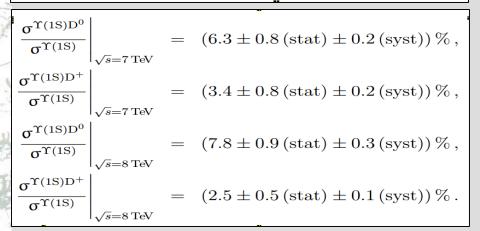


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$$\frac{\sigma_{\sqrt{s}=7 \text{ TeV}}^{\Upsilon(1\text{S})\text{D}^{0}}}{\sigma_{\sqrt{s}=7 \text{ TeV}}^{\Upsilon(1\text{S})\text{D}^{+}}} = 1.9 \pm 0.5 \text{ (stat)} \pm 0.1 \text{ (syst)}$$

$$\frac{\sigma_{\sqrt{s}=8 \text{ TeV}}^{\Upsilon(1\text{S})\text{D}^{0}}}{\sigma_{\sqrt{s}=8 \text{ TeV}}^{\Upsilon(1\text{S})\text{D}^{+}}} = 3.1 \pm 0.7 \text{ (stat)} \pm 0.1 \text{ (syst)}$$

$$\frac{\sigma^{\Upsilon D^0}}{\sigma^{\Upsilon D^+}} = \frac{\sigma^{D^0}}{\sigma^{D^+}} = 2.41 \pm 0.18$$





$$rac{\sigma^{\Upsilon^{{
m c}\overline{
m c}}}}{\sigma^{\Upsilon}} = rac{\sigma^{{
m c}\overline{
m c}}}{\sigma_{
m eff}}.$$

SPS

$$\frac{\sigma^{\Upsilon c \bar{c}}}{\sigma^{\Upsilon}} = (0.2 - 0.6) \%$$

$$\frac{\sigma^{\Upsilon(1\mathrm{S})c\bar{c}}}{\sigma^{\Upsilon(1\mathrm{S})}}\Big|_{\sqrt{s}=8\,\text{TeV}} = (5.5 \pm 1.7)\,\%,$$

$$\frac{\sigma^{\Upsilon(1\mathrm{S})c\bar{c}}}{\sigma^{\Upsilon(1\mathrm{S})}}\Big|_{\sqrt{s}=8\,\text{TeV}} = (6.2 \pm 0.7)\,\%,$$



#### Cross-section ratios - II



#### Reduced uncertainties

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DPS

$$\mathscr{B}_{2/1} imes rac{\sigma_{\sqrt{s}=7 \, {
m TeV}}^{\Upsilon(2{
m S}){
m D}^0}}{\sigma_{\sqrt{s}=7 \, {
m TeV}}^{\Upsilon(1{
m S}){
m D}^0}} = (13 \pm 5)\%,$$

$$\mathscr{B}_{2/1} \times \frac{\sigma_{\sqrt{s}=8 \text{ TeV}}^{\Upsilon(2S)D^0}}{\sigma_{\sqrt{s}=8 \text{ TeV}}^{\Upsilon(1S)D^0}} = (20 \pm 4)\%,$$

$$\mathscr{B}_{2/1} \times \frac{\sigma_{\sqrt{s}=7 \, {\rm TeV}}^{\Upsilon(2{\rm S}){\rm D}^{+}}}{\sigma_{\sqrt{s}=7 \, {\rm TeV}}^{\Upsilon(1{\rm S}){\rm D}^{+}}} = (22 \pm 7)\%,$$

$$\mathscr{B}_{2/1} \times \frac{\sigma_{\sqrt{s}=8\,\mathrm{TeV}}^{\Upsilon(2\mathrm{S})\mathrm{D}^{+}}}{\sigma_{\sqrt{s}=8\,\mathrm{TeV}}^{\Upsilon(1\mathrm{S})\mathrm{D}^{+}}} = (22\pm6)\%,$$

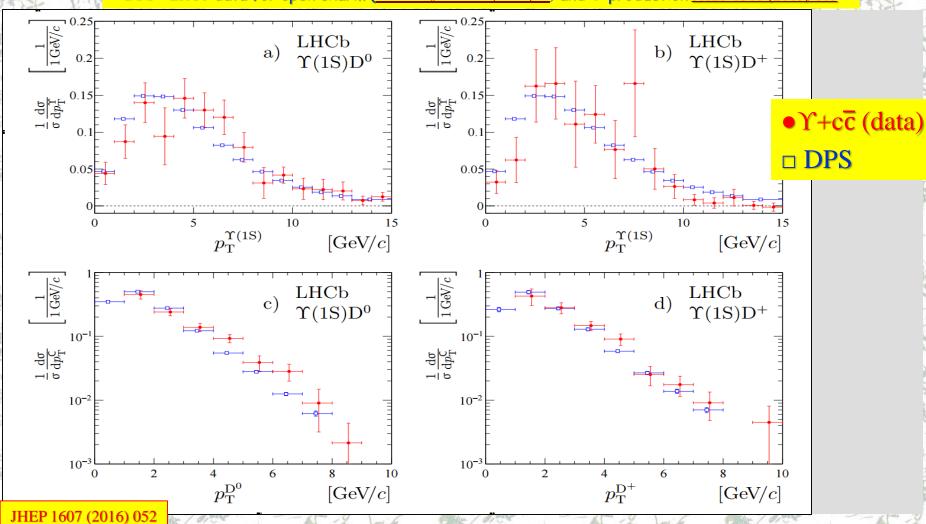


$$\mathscr{B}_{2/1} \frac{\sigma^{\Upsilon(2S)D^0}}{\sigma^{\Upsilon(1S)D^0}} = \mathscr{B}_{2/1} \frac{\sigma^{\Upsilon(2S)D^+}}{\sigma^{\Upsilon(1S)D^+}} = \mathscr{B}_{2/1} \frac{\sigma^{\Upsilon(2S)}}{\sigma^{\Upsilon(1S)}} = 0.249 \pm 0.033$$



## $\mathbf{p}_{\mathbf{T}}$ spectra

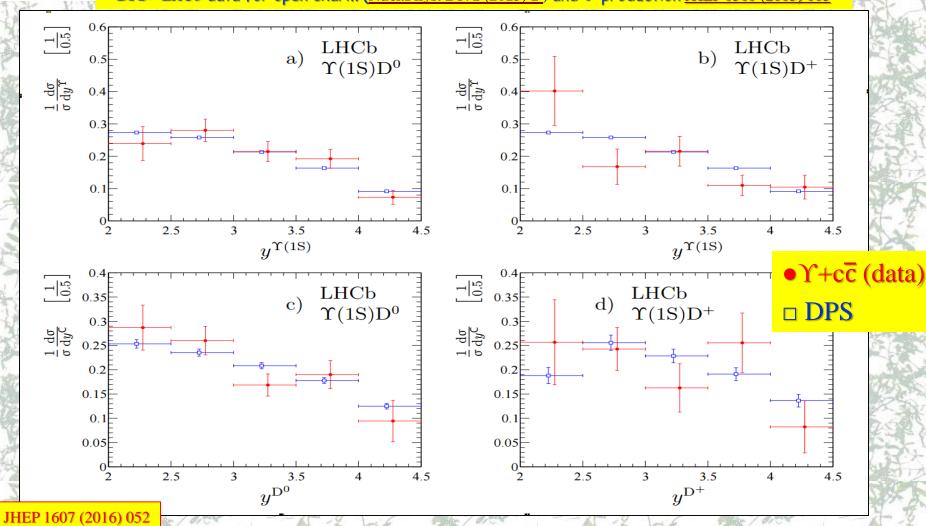






# Rapidity

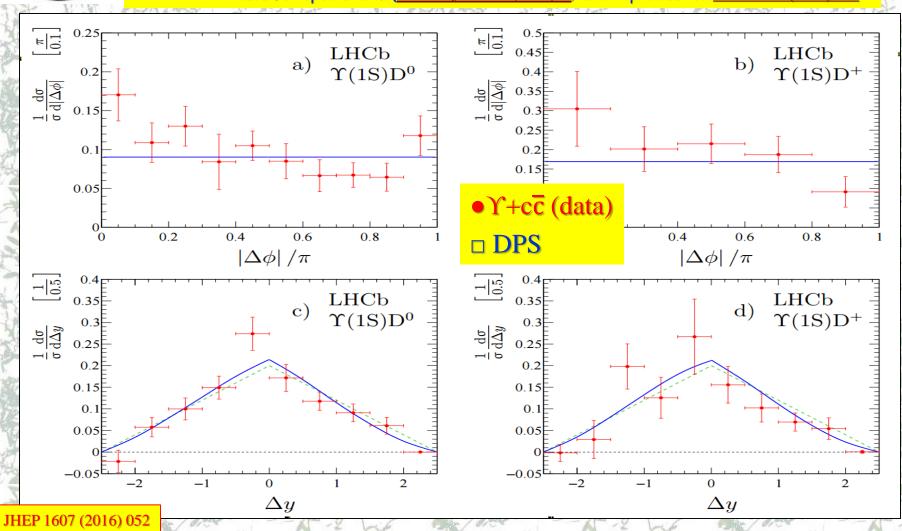






# $\Delta \phi$ and $\Delta y$

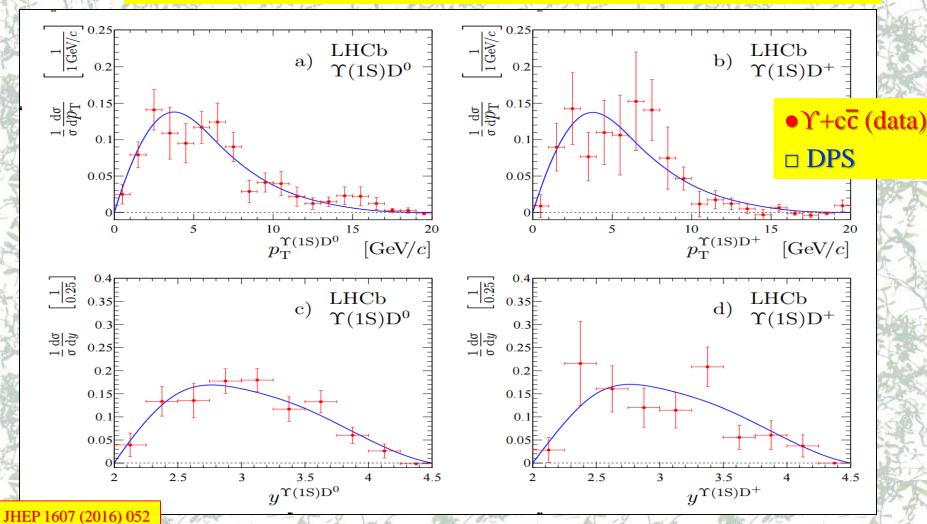






# p<sub>T</sub> and rapidity

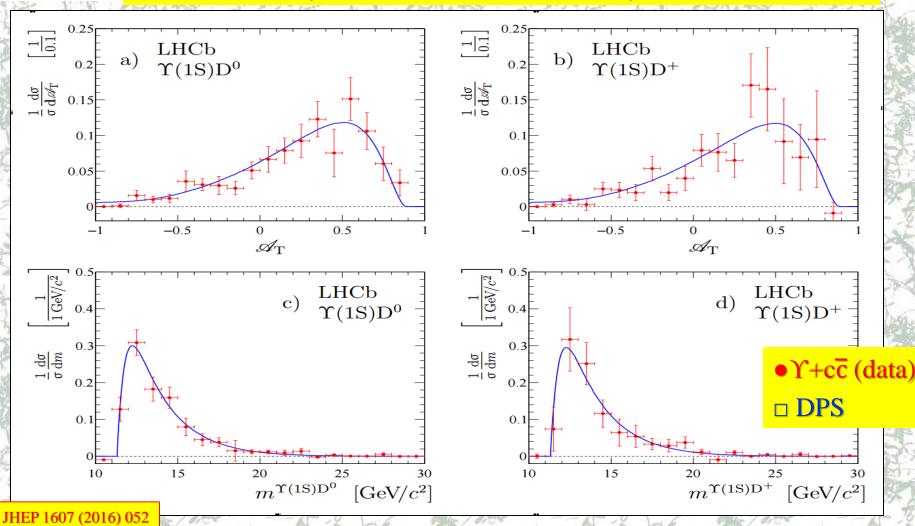






# **p<sub>T</sub>** asymmetry and mass







#### **DPS? DPS!**



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- $^{\bullet}$  Measured cross-section significantly exceeds SPS expectations, agrees with DPS with  $\sigma_{\rm eff}(CDF)$
- All cross-section ratios agree with DPS
- Differential distributions agree with DPS
- lacktriangle Measure  $\sigma_{
  m eff}$

7TeV

8TeV

$$\sigma_{\rm eff}|_{\Upsilon(1{\rm S}){\rm D}^0} = 19.4 \pm 2.6 \, ({\rm stat}) \pm 1.3 \, ({\rm syst}) \, {\rm mb} \, ,$$

$$\sigma_{\rm eff}|_{\Upsilon(1{\rm S}){\rm D}^+} = 15.2 \pm 3.6 \, ({\rm stat}) \pm 1.5 \, ({\rm syst}) \, {\rm mb} \, .$$

$$\begin{array}{lcl} \sigma_{\rm eff}|_{\Upsilon(1{\rm S}){\rm D}^0} & = & 17.2 \pm 1.9 \, ({\rm stat}) \pm 1.2 \, ({\rm syst}) \, {\rm mb} \, , \\ \sigma_{\rm eff}|_{\Upsilon(1{\rm S}){\rm D}^+} & = & 22.3 \pm 4.4 \, ({\rm stat}) \pm 2.2 \, ({\rm syst}) \, {\rm mb} \, , \end{array}$$

$$\sigma_{\rm eff}|_{\Upsilon(1{\rm S}){\rm D}^{0,+},\sqrt{s}=7\,{\rm TeV}}=18.0\pm2.1\,{\rm (stat)}\pm1.2\,{\rm (syst)}=18.0\pm2.4\,{\rm mb}$$
 .

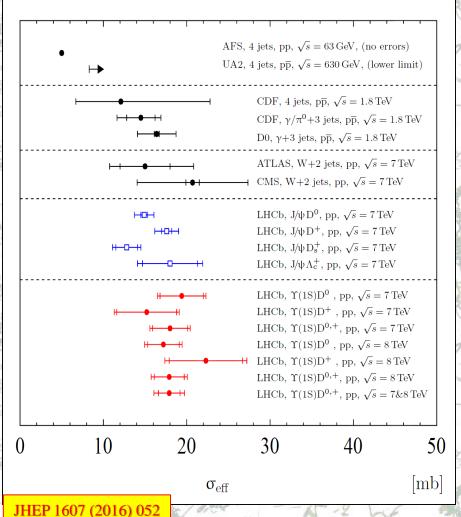
$$\sigma_{\rm eff}|_{\Upsilon(1S)D^{0,+},\sqrt{s}=8\,{\rm TeV}} = 17.9\pm1.8\,({\rm stat})\pm1.2\,({\rm syst}) = 17.9\pm2.1\,{\rm mb}\,,$$

$$\sigma_{\rm eff}|_{\Upsilon(1{\rm S}){\rm D}^{0,+}} = 18.0 \pm 1.3 \, ({\rm stat}) \pm 1.2 \, ({\rm syst}) = 18.0 \pm 1.8 \, {\rm mb} \, , \label{eq:sigma-fit}$$



#### **O**eff





- Excellent agreement with  $J/\psi + c\overline{c}$
- Agrees well with  $\gamma + 3jets$
- Agrees well with W+2jets

A kind of tension with

 $2 \times J/\psi$  8.2±2.0±2.9mb

(CMS+Lansberg,Shao)

 $2 \times J/\psi$  4.8±0.5±2.5mb D0

 $J/\psi + Y = 2.2 \pm 0.7 \pm 0.9 \text{mb}$ D0



### Summary



- Associative production of  $\Upsilon + c\overline{c}$  is observed
- For five modes with  $>5\sigma$  significance
- Cross-sections are measured for  $\Upsilon(1,2S)D^{0,+}$
- Cross-sections and their rations agree with DPS
- Cross-sections significantly exceed SPS
- Differential distributions supports DPS
- ullet Precise measurement of  $\sigma_{\!\scriptscriptstyle eff}$ 
  - In an excellent agreement with  $J/\psi+c\overline{c}$  results
- Other interesting measurements with Run-I data:
  - $Z+c\overline{c}$ ,  $2\times J/\psi$ , ....

13TeV data: importance of DPS is increasing Who waits **Triple Parton Scattering**?





# Thank you!



#### Refs



- A.V. Berezhnoy, A.K.Likhoded, "Associated production of Y and open charm at LHC", Int.J.Mod.Phys, A30 (2015) 1550125, arXiv:1503.04445
- \* A.V. Berezhnoy, V.V. Kiselev, A.K. Likhoded and A.I. Onishchenko, "Double charmed baryon production in hadronic experiments", Phys.Rev. D57(1998), 4385, arXiv:hep-ph/9710339
- S.P.Baranov, "Topics in associated  $J/\psi+c+\overline{c}$  production at modern colliders", Phys.Rev. D73 (2006) 074021
- J.P.Lansberg, "On mechanisms of heavy-quarkonium hadroproduction", Eur.Phys.J. C61 (2009) 693, arXiv:0811.4005
- \* R.Maciula and A.Szczurek, "Single and double charmed meson production at the LHC", EPJ Web Conf. 81 (2014) 01007



## Too simple?



Validity of factorization anzatz:

$$D_h^{ij}(x_1, x_2; Q_1^2, Q_2^2) = D_h^i(x_1; Q_1^2) D_h^j(x_2; Q_2^2).$$

- This anzatz allow  $x_1+x_2>1$ :
  - energy non-conservation. Need to suppress such configurations: at least  $\theta(1-x_1-x_2)$  factor is needed
  - Makes integration impossible
- Numerical studies within Lund dipole cascade model shows violation of factorization at large  $Q_1^2$  and/or  $Q_2^2$ 
  - up to 20% deviation from factorization in  $\gamma$ +jets cross-sections in Tevatron case
  - Up to 30-50% for certain kinematical ranges
- ullet For processes with (very) small x only factorization is fine

$$\begin{split} \Gamma_{gg}(b,x_1,x_2;\mu_1^2,\mu_2^2) \\ &= F_g(x_1,\mu_1^2) F_g(x_2,\mu_2^2) F(b;x_1,x_2,\mu_1^2,\mu_2^2), \end{split}$$

$$\sigma_{\text{eff}}(x_1, x_2, x_1', x_2', \mu_1^2, \mu_2^2)$$

$$= \left( \int d^2b F(b; x_1, x_2, \mu_1^2, \mu_2^2) F(b; x_1', x_2', \mu_1^2, \mu_2^2) \right)^{-1}.$$



# Differential distributions



- Powerful tool to judge on the production mechanism
- DPS: all kinematic distributions can be calculated from measured inclusive Y and D spectra
  - Make toy-MC:
    - Sample 4-momenta of  $\Upsilon$  and D from the measured published differential cross-sections (+ assume uniform uncorrelated  $\phi$ -distributions)
- SPS: there are no differential predictions
  - But some non-trivial correlations are expected