

# Constraining the CKM angle $\gamma$ from Run 1 data at LHCb

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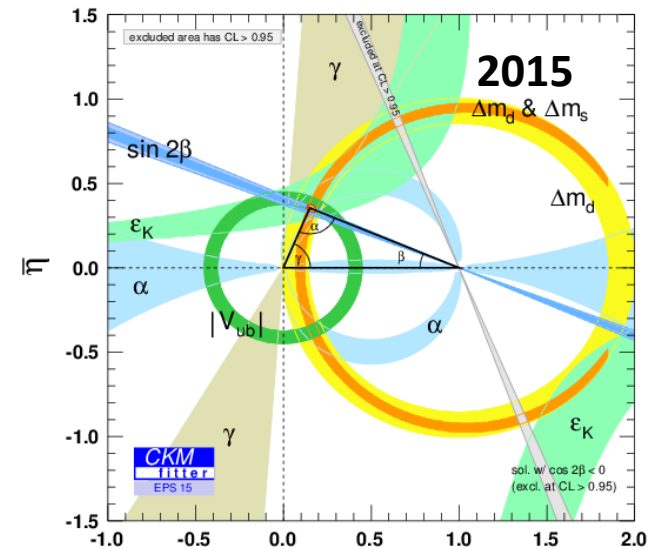
University of Oxford

3<sup>rd</sup> – 10<sup>th</sup> August 2016 – ICHEP, Chicago, USA

On behalf of the LHCb collaboration

# Why a precision measurement of $\gamma$ is important

- Observables related to CPV can provide an insight to NP (there must be other sources of CPV beyond those predicted by the SM)
- Largest uncertainty is on  $\gamma$ , a process accessible at tree level - forms a SM benchmark\*
- Theory uncertainty  $\sim 10^{-7}$  JHEP 01 (2014) 051
- Improvement in direct measurement precision required.



$$\gamma = (66.9^{+0.94}_{-3.44})^\circ$$

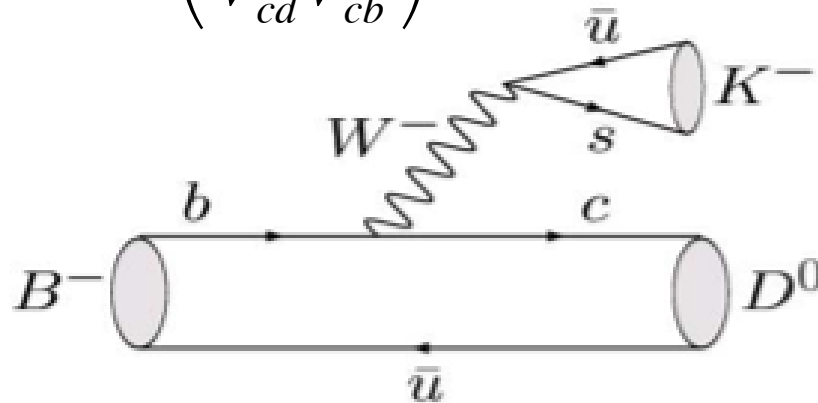
Direct (tree-level) measurements only:

$$\gamma = (73.2^{+6.3}_{-7.0})^\circ$$

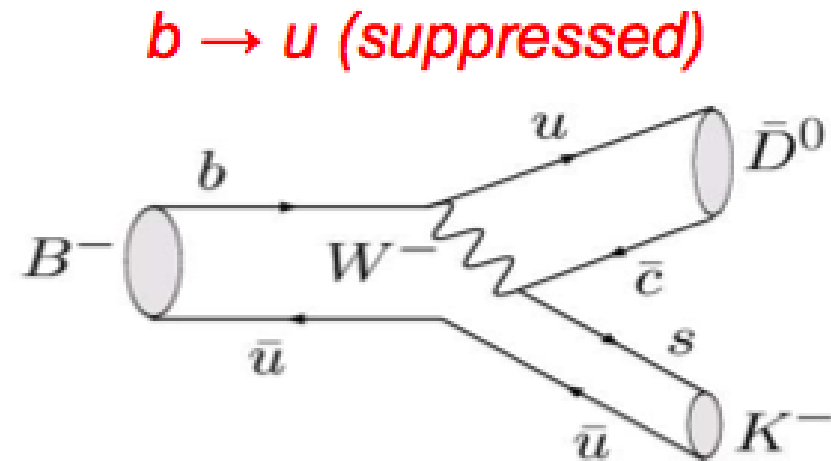
\*assuming no New Physics in tree decays PRD 92(3):033002 (2015)

# B → DK

$$\gamma = -\arg\left(\frac{V_{ud} V_{ub}^*}{V_{cd} V_{cb}^*}\right)$$



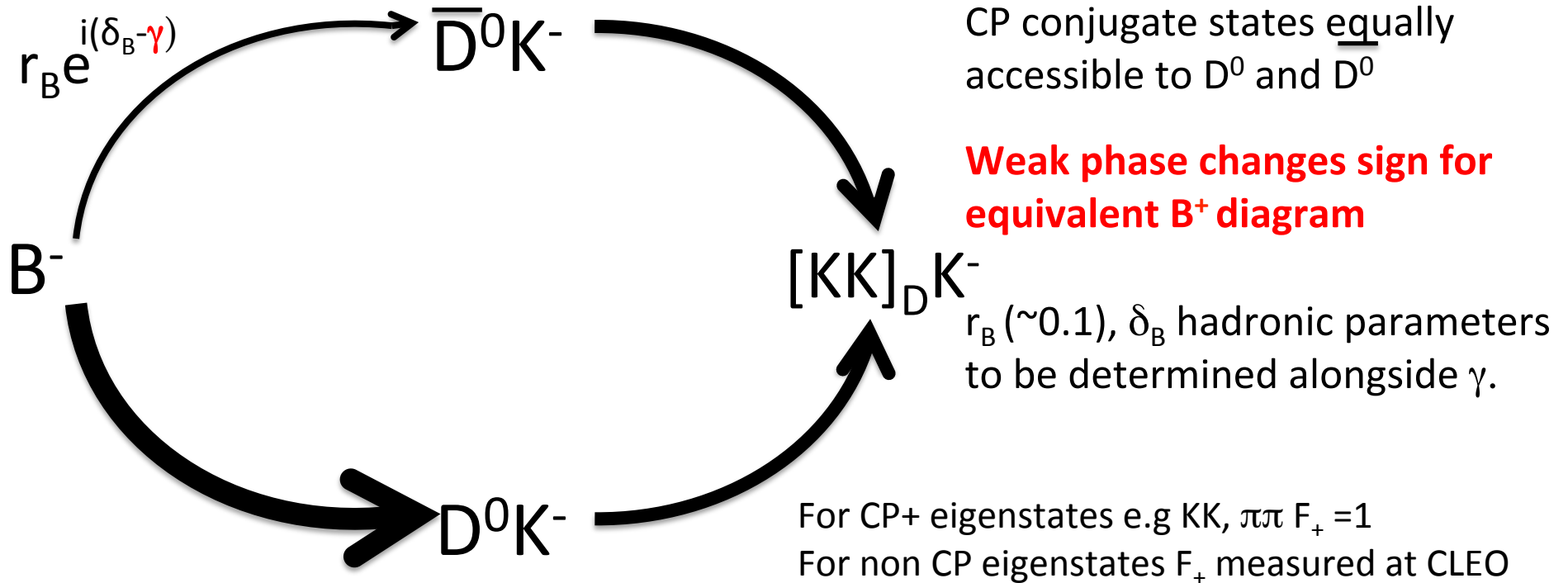
*b → c (favoured)*



*b → u (suppressed)*

- Interference possible if  $D^0$  and  $\overline{D^0}$  decay to same final state
  - Many choices of D final state
- Fully hadronic final state – well suited to LHCb
- Other B modes studied. Today some results from  $B \rightarrow D\pi$  &  $B^0 \rightarrow DK^*$

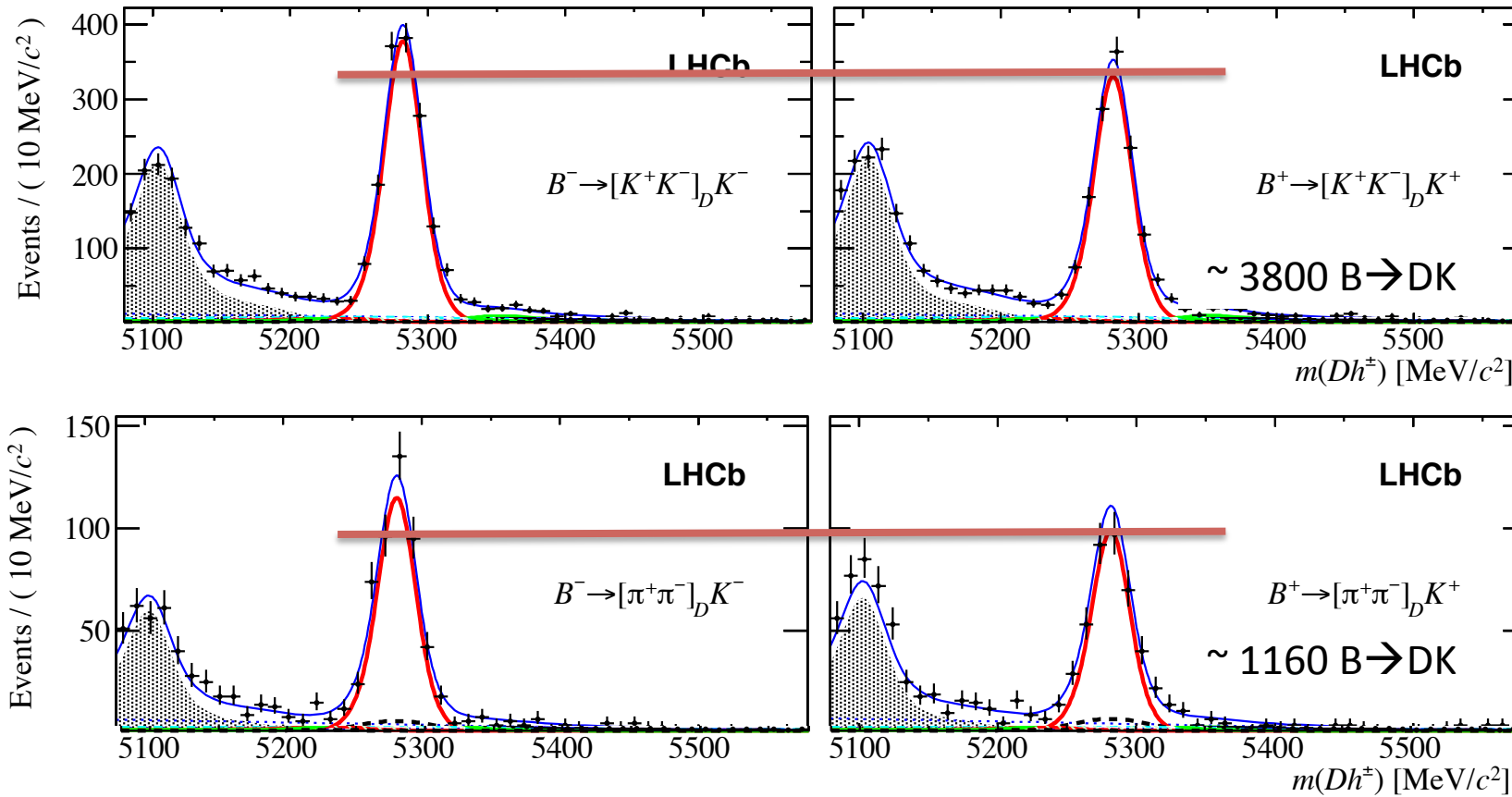
# Interference with self conjugate states “(q)-GLW”



$$\frac{N(B^-) - N(B^+)}{N(B^-) + N(B^+)} = A_{CP^+} = \frac{1}{R_{CP^+}} 2r_B (2F_+ - 1) \sin(\delta_B) \sin(\gamma)$$

$$\frac{N(B \rightarrow [KK]_D K) \times \Gamma(D \rightarrow K\pi)}{N(B \rightarrow [K\pi]_D K) \times \Gamma(D \rightarrow KK)} = R_{CP^+} = 1 + r_B^2 + 2r_B (2F_+ - 1) \cos(\delta_B) \cos(\gamma)$$

# B → D(hh)K



$$A_K^{KK} = 0.087 \pm 0.020 \pm 0.008$$

$$A_K^{\pi\pi} = 0.128 \pm 0.037 \pm 0.012$$

Combined

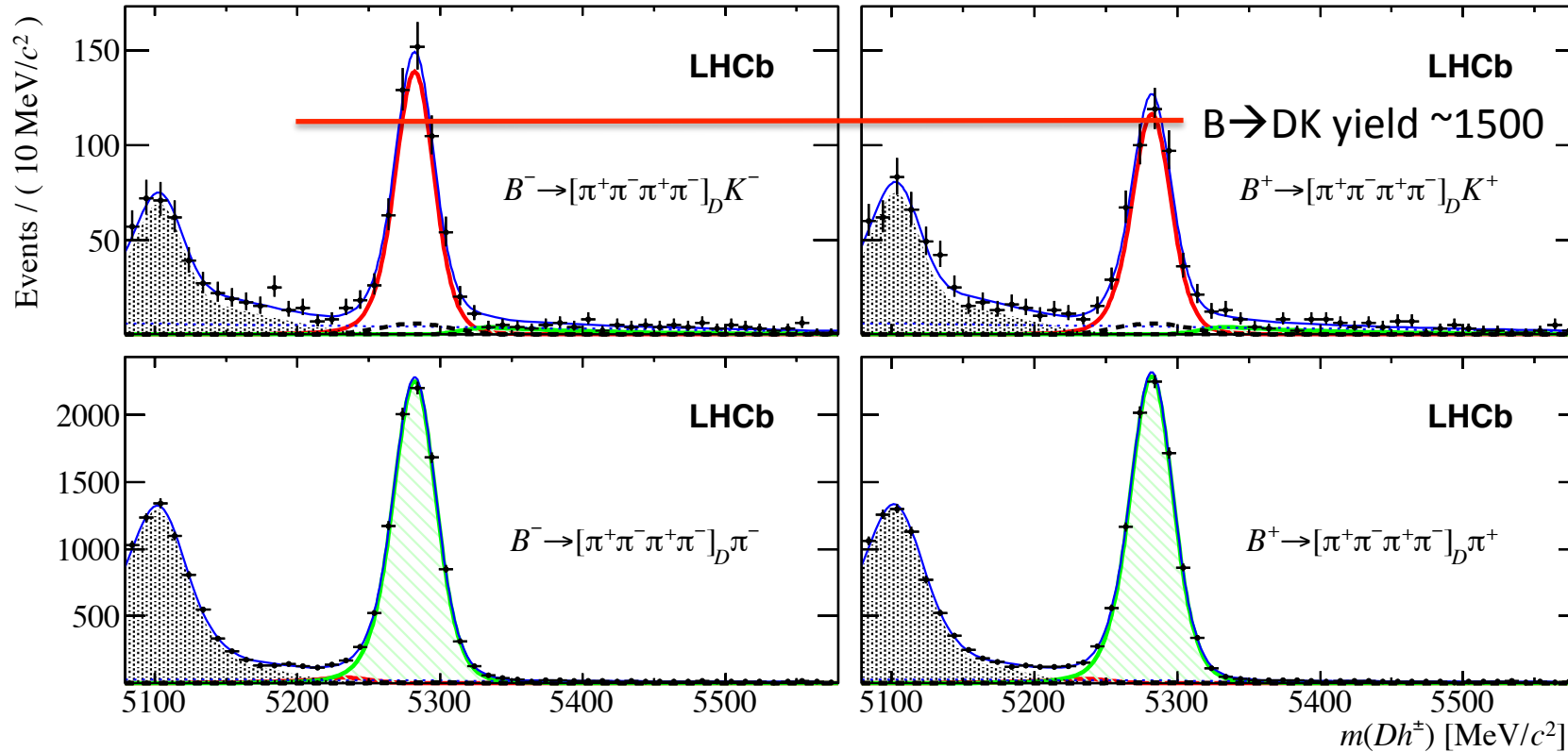


High purity, high yields.

Low crossfeed/other backgrounds

LHCb optimised for this type of physics

# Results $B \rightarrow D(4\pi)h$

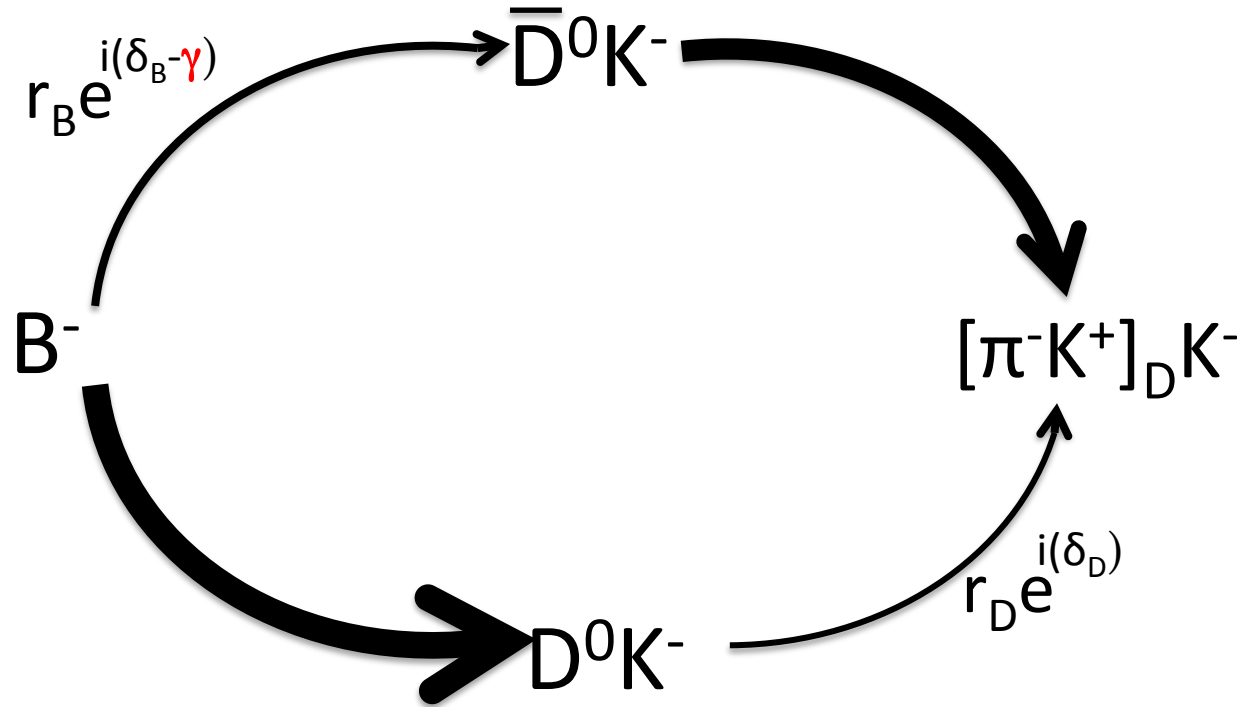


$$A_K^{\pi\pi\pi\pi} = 0.100 \pm 0.034 \pm 0.018$$

First use of this mode - possible due to measurements from CLEO

$$F_+^{4\pi} = 0.737 \pm 0.028 \quad \text{PLB 747 (2015) 9}$$

# Interference with flavour specific “ADS”

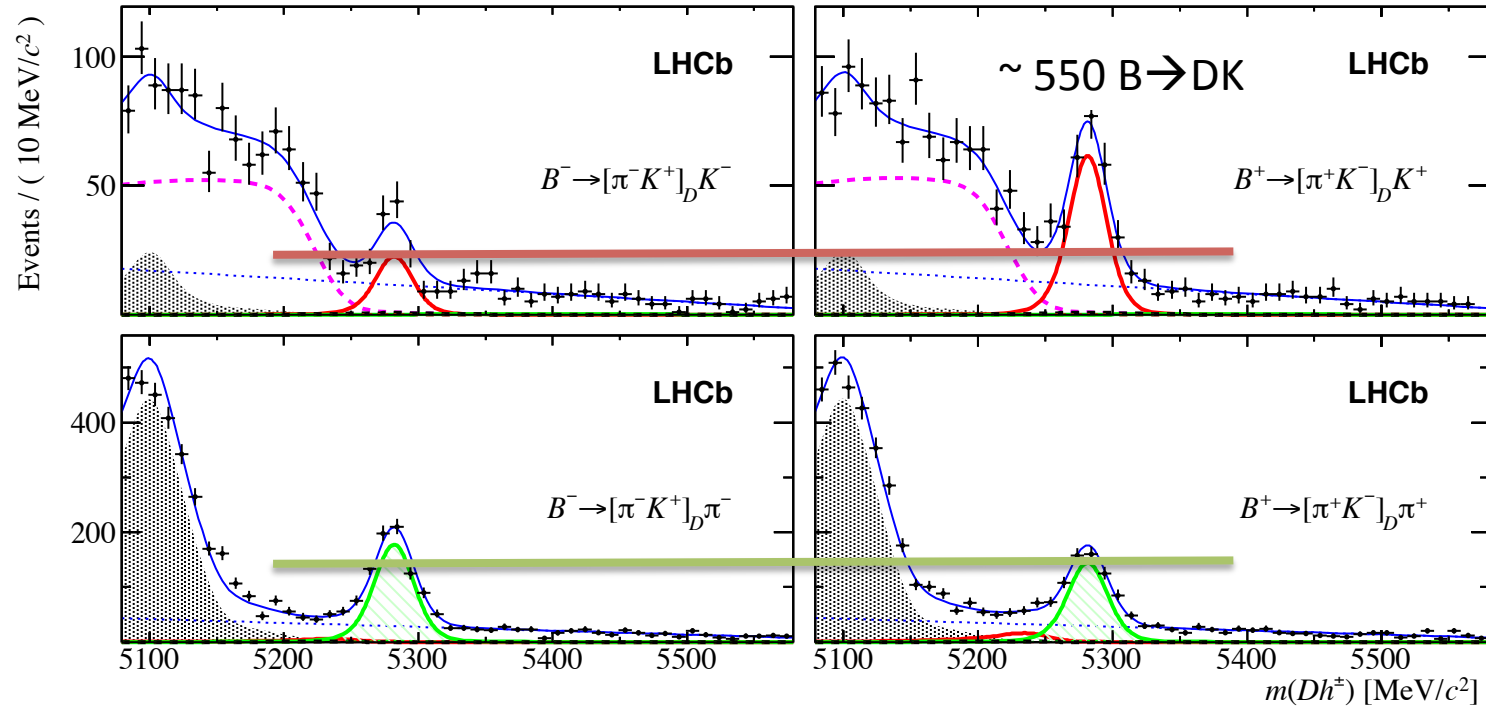


- Larger interference effects as both amplitudes of similar sizes.
- Additional parameters  $r_D, \delta_D$ . External inputs from charm mixing
- Extensions to multibody decays possible

$$\frac{N(B^-) - N(B^+)}{N(B^-) + N(B^+)} = A_{ADS} = \frac{1}{R_{ADS}} 2r_B r_D \sin(\delta_B + \delta_D) \sin(\gamma)$$

$$\frac{N(B^\pm \rightarrow [\pi^\pm K^\mp]_D K^\pm)}{N(B^\pm \rightarrow [K^\pm \pi^\mp]_D K^\pm)} = R_{ADS} = r_B^2 + r_D^2 + 2r_B r_D \cos(\delta_B + \delta_D) \cos(\gamma)$$

# $B \rightarrow D[\pi K]h$



**8 $\sigma$**

Only observed at LHCb, BF  $\sim 10^{-7}$  -- a rare decay

$$A_K^{\pi K} = -0.403 \pm 0.056 \pm 0.011$$

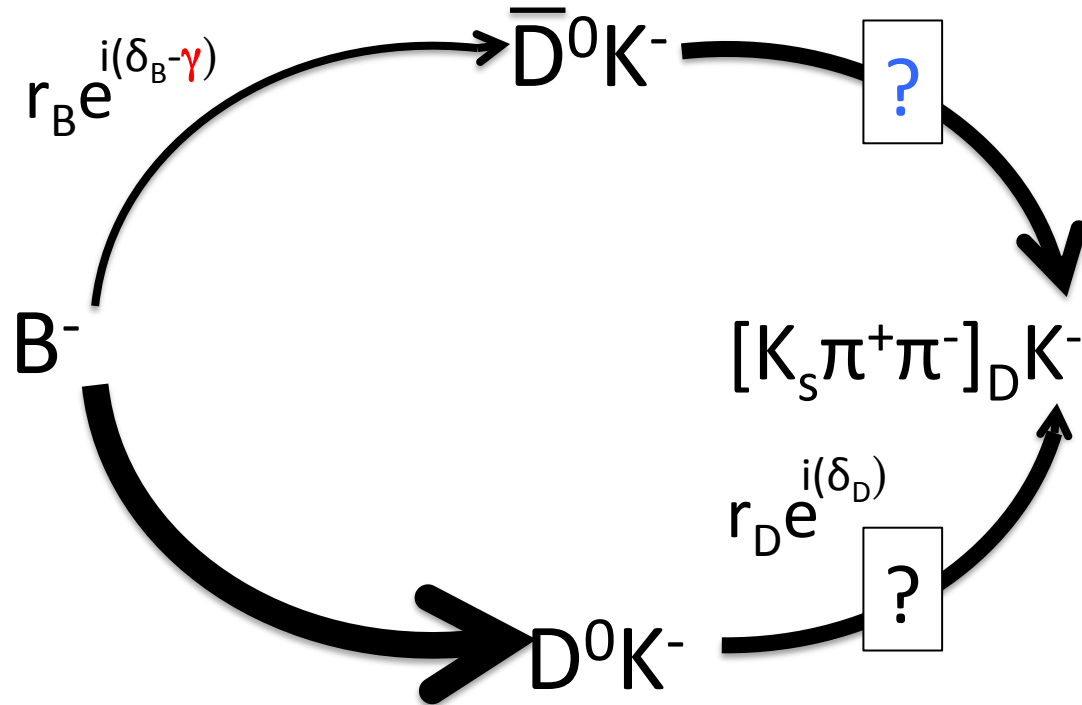
$$A_\pi^{\pi K} = 0.100 \pm 0.031 \pm 0.009$$

CPV starts to become visible in  $B \rightarrow D\pi$  when combining all  $D \rightarrow hh$  and  $D \rightarrow 4h$  modes.

**3.9 $\sigma$**



# Self-conjugate D decays using Dalitz plot “GGSZ”



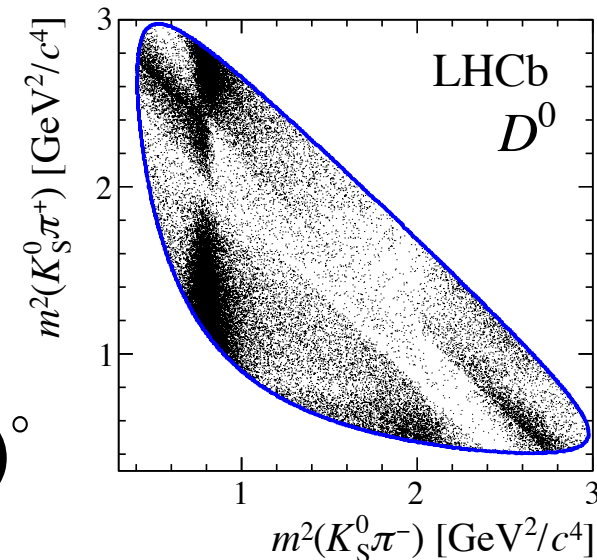
Value of  $F_+$  for certain self conjugate decays would be  $\sim 0.5$

Hence inclusive treatment loses most of the sensitivity to  $\gamma \rightarrow$  Analyse the Dalitz plot

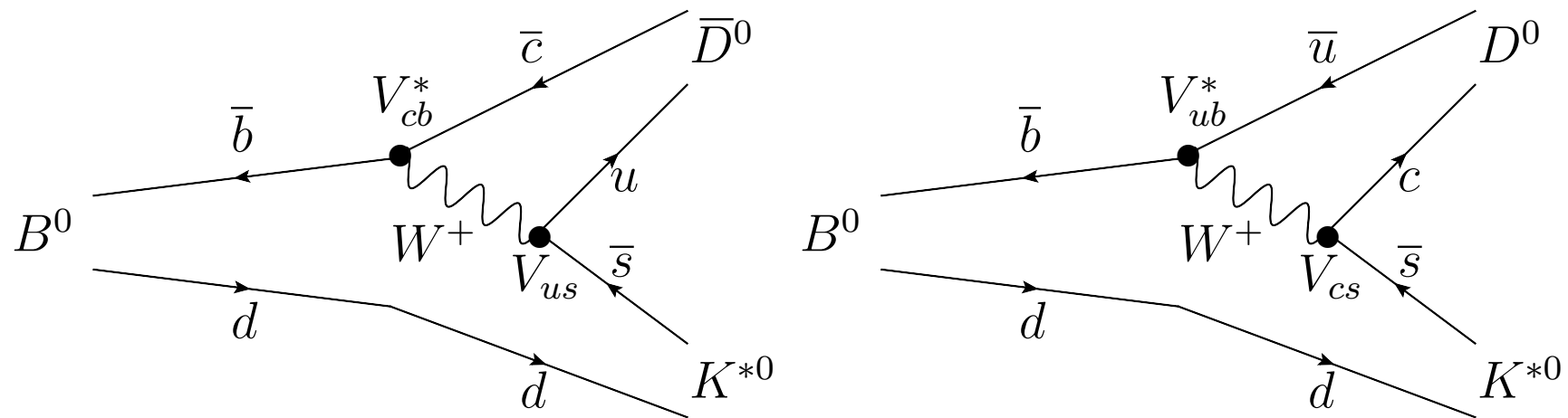
LHCb  $\rightarrow$  DK analysis in this mode : JHEP 10 (2014) 097

Best standalone measurement of  $\gamma = (62_{-14}^{+15})^\circ$

Old result, today show this D decay using another B mode

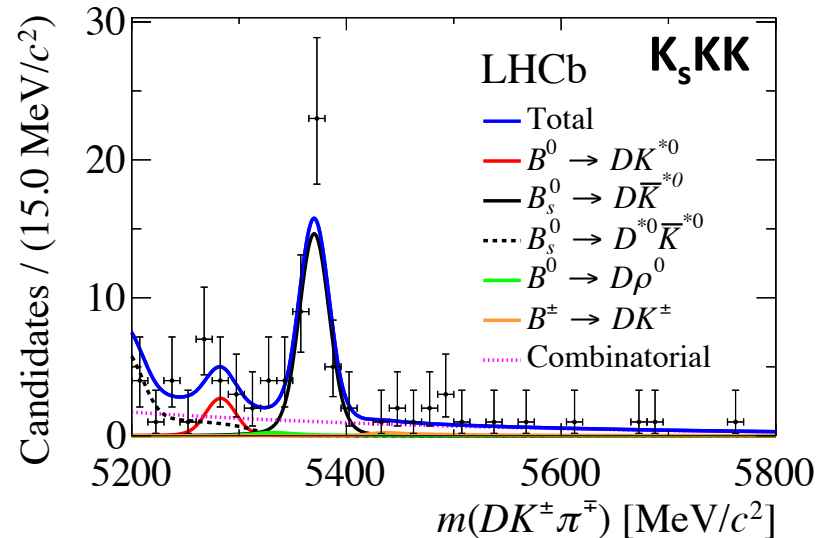
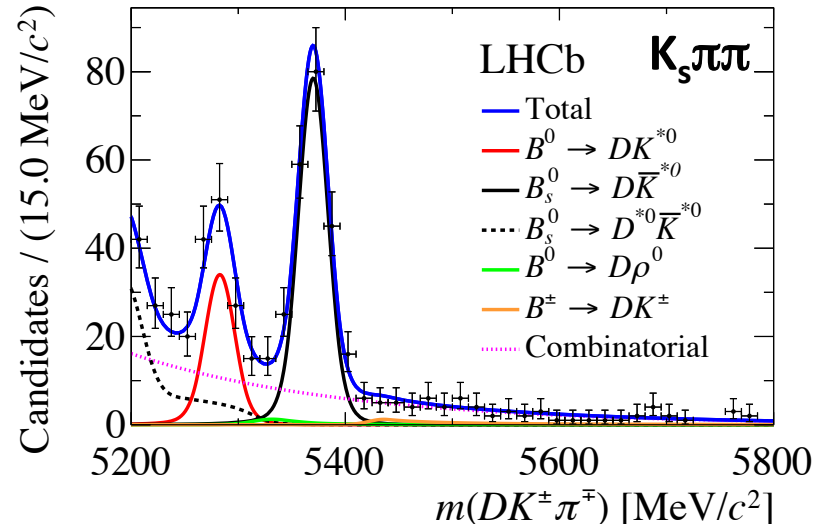


# Other B modes

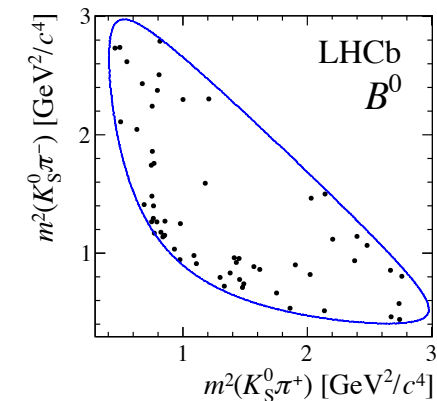
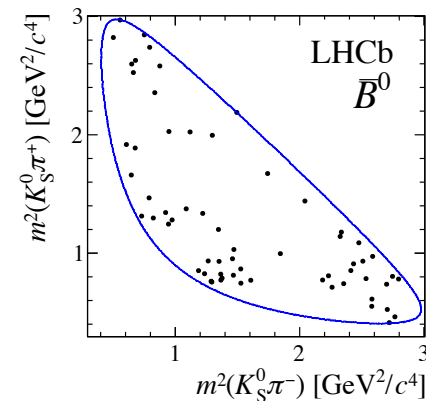


- Favoured and suppressed decay both colour suppressed
- Different  $r_B$  and  $\delta_B$ :  $r_B \sim 0.3 \rightarrow$  Larger interference
- Charge of kaon from  $K^*$  tags tags flavour of B at decay – no need for time dependent analysis
- Yields at LHCb becoming viable for analysis

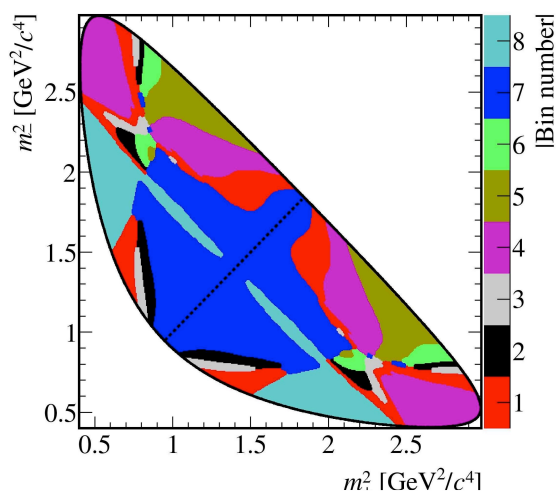
# Selection of $B^0 \rightarrow DK^*$



- Yields  $\sim 90$  in  $K_s\pi\pi$  and 10 in  $\sim K_sKK$ 
  - Twice yield of B factories
- Irreducible  $B_s$  backgrounds
- $\rightarrow$  Look for differences in the D Dalitz Plots distributions



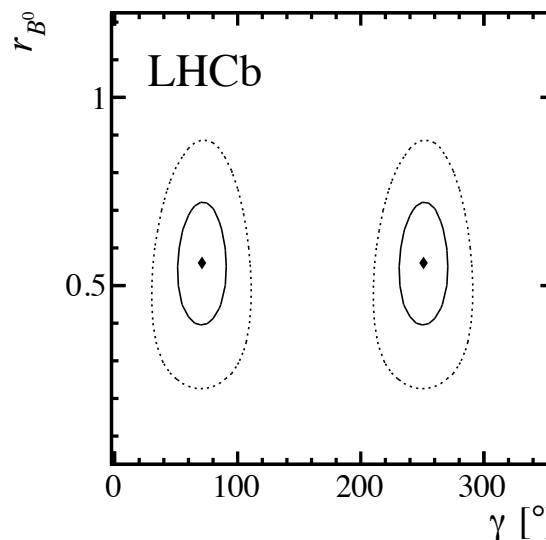
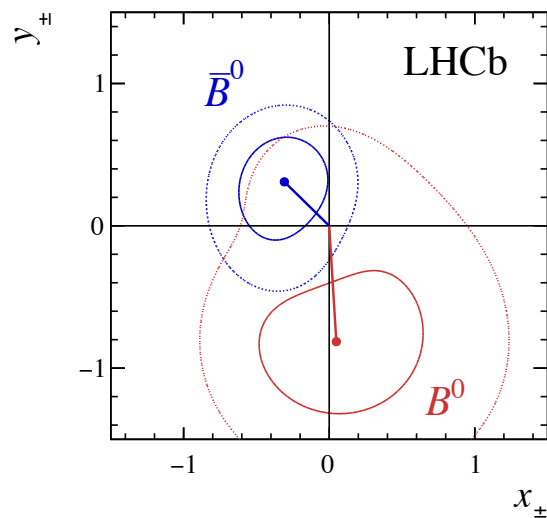
# Model-independent GGSZ analysis



- Divide Dalitz plot into bins and look at asymmetries in yields
- Asymmetries related to  $\gamma$  if input on average strong phases from CLEO is used. PRD 82 (2010) 112006
- Measured parameters are  $x, y$

$$x_{\pm} = r_{B^0} \cos(\delta_{B^0} \pm \gamma)$$

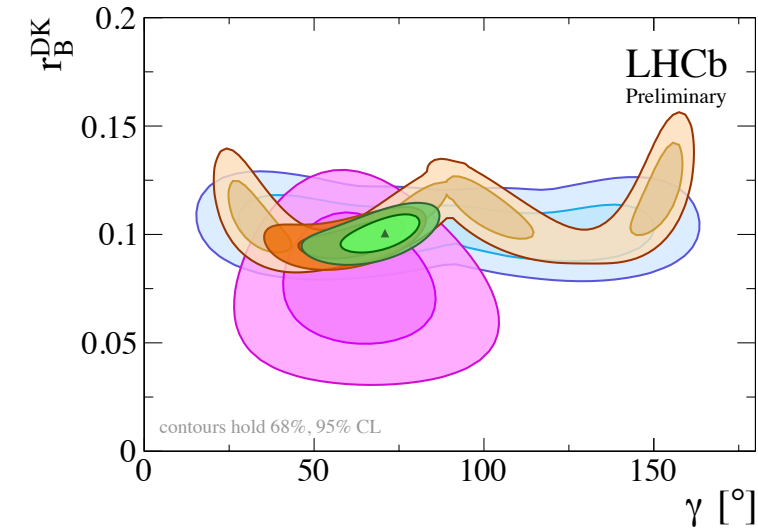
$$y_{\pm} = r_{B^0} \sin(\delta_{B^0} \pm \gamma)$$



- No observation of CPV.
- $\gamma = (71 \pm 20)^\circ$
- $\sigma(\gamma) \sim 1/r_{B^0}$

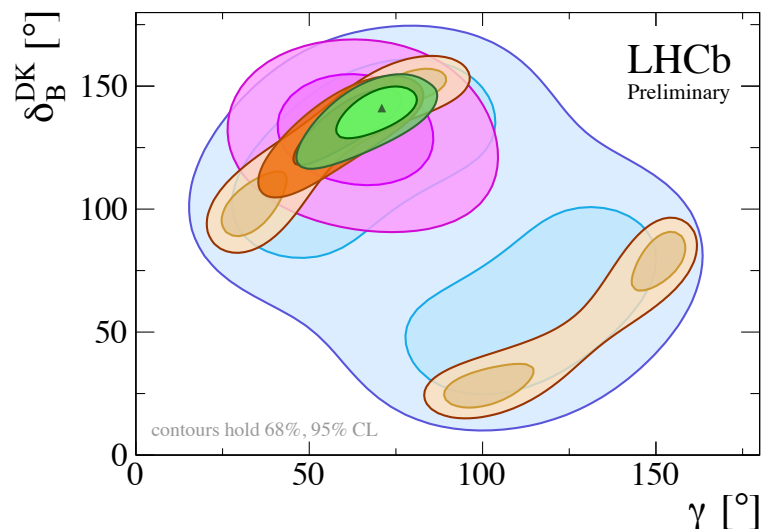
Model-dependent analysis also performed, results compatible. arXiv:1605.01082

# Interplay between different modes: $B^+ \rightarrow DK^+$

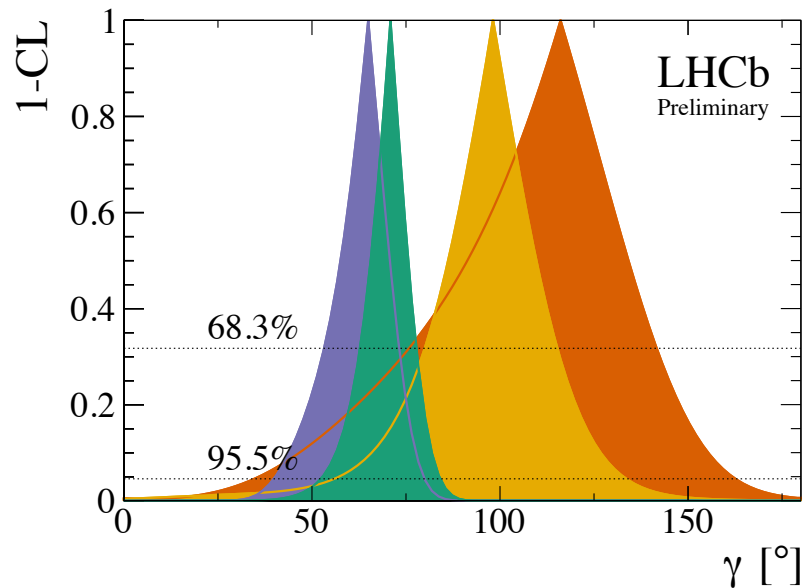


- $B^+ \rightarrow DK^+, D \rightarrow h3\pi/hh'\pi^0$
- $B^+ \rightarrow DK^+, D \rightarrow K_S hh$
- $B^+ \rightarrow DK^+, D \rightarrow KK/K\pi/\pi\pi$
- All  $B^+ \rightarrow DK$  results
- Full “ $B \rightarrow DK$  like” combination

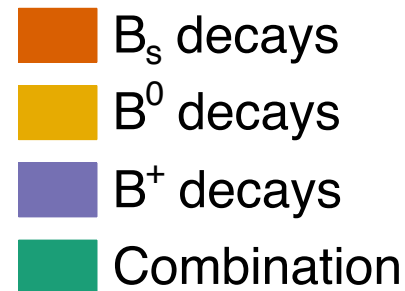
- ADS/GLW/q-GLW observables have non trivial trigonometric relations – leads to 4 solutions
- Single solution selected by GGSZ modes
- Combination can set strong constraints
- Other B modes improve that further
- No single mode dominates  $\rightarrow$  necessary to follow all paths



# Combination results



- Many more modes in total
- 71 observables and 32 parameters.
- Frequentist combination using ‘plugin’ method approximation.
- $B \rightarrow D\pi(\pi\pi)$  results excluded



$$\gamma = (70.9^{+7.1}_{-8.5})^\circ$$

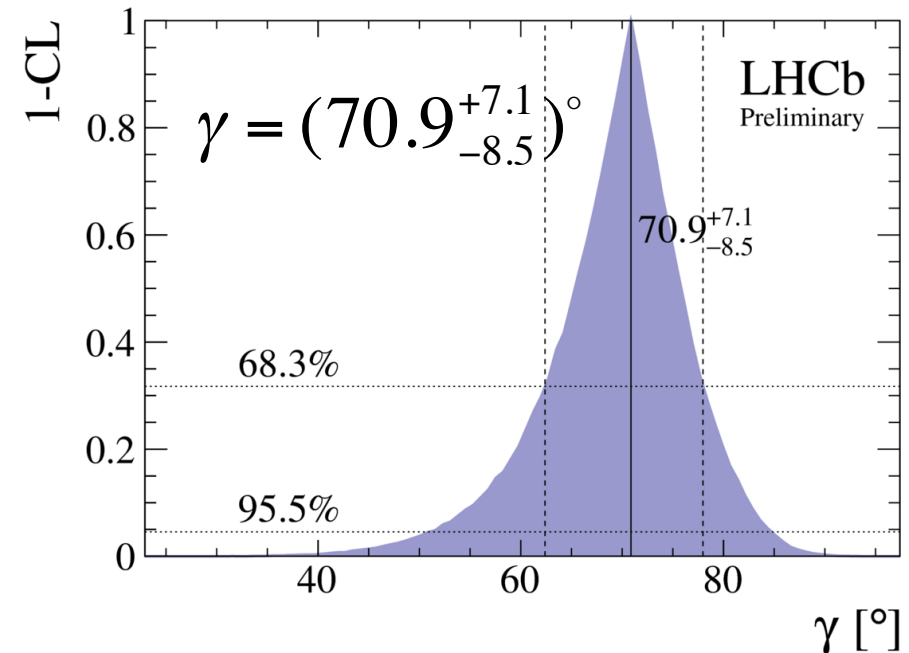
- 2<sup>nd</sup> combination including  $B \rightarrow D\pi$ ,  $B \rightarrow D\pi\pi\pi$  performed.
- Very little real sensitivity in these modes
- Plugin approximation starts to breakdown– no 1D intervals shown.

- Improved precision compared to last combination by  $\sim 20\%$
- Good agreement with B factory results
- Bayesian interpretation is consistent

# Outlook

- Run 1 target of  $8^\circ$  attained
- Nearly all Run 1 analyses complete
- 2015 data + 2016 data being added
- New decay modes being added
- Run 2 target:  $4^\circ$
- **LHCb upgrade projection ( $50 \text{ fb}^{-1}$ ) for  $\gamma$  is  $0.9^\circ$  (~15 yrs from now) -- no showstoppers foreseen**

EPJC (2013) 73:2373



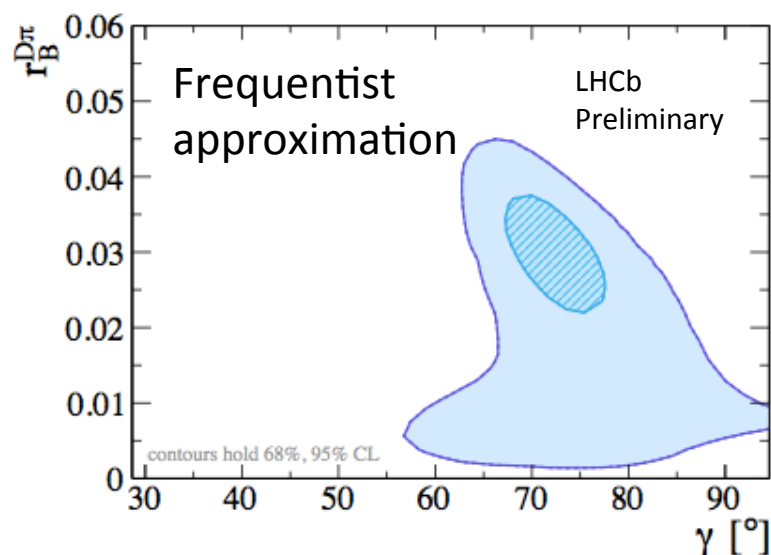
Degree level precision will be required to probe NP

LHCb demonstrates that it remains on target to do so.

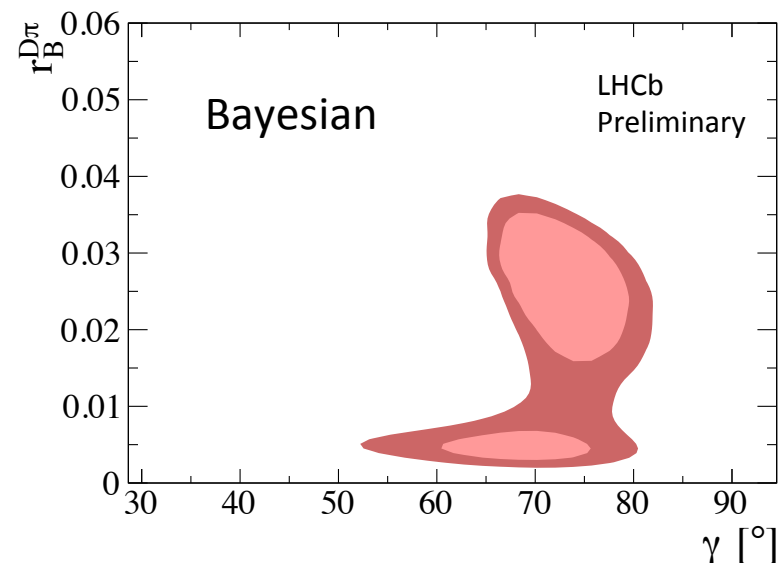
End



# Dh combination



- p-value from 2-D Plugin scan.  $2\sigma$  contour wider for low (expected) values of  $r_B^{D\pi}$ .
- Behaviour not seen in 1-D Plugin scan – result of the approximation that all other nuisance parameters are fixed to best fit values.
- 1-D scan does not lead of accurate description of the Frequentist intervals, hence no result quoted.



Integrating the 2-D posterior PDF leads to non-Gaussian intervals.

Most probable value:  $72.7^\circ$

Credibility intervals:

$\gamma \in [69.0^\circ, 77.6^\circ] @ 68.3\%$

$\gamma \in [57.0^\circ, 83.1^\circ] @ 95.5\%$

$\gamma \in [40.9^\circ, 87.2^\circ] @ 99.7\%$

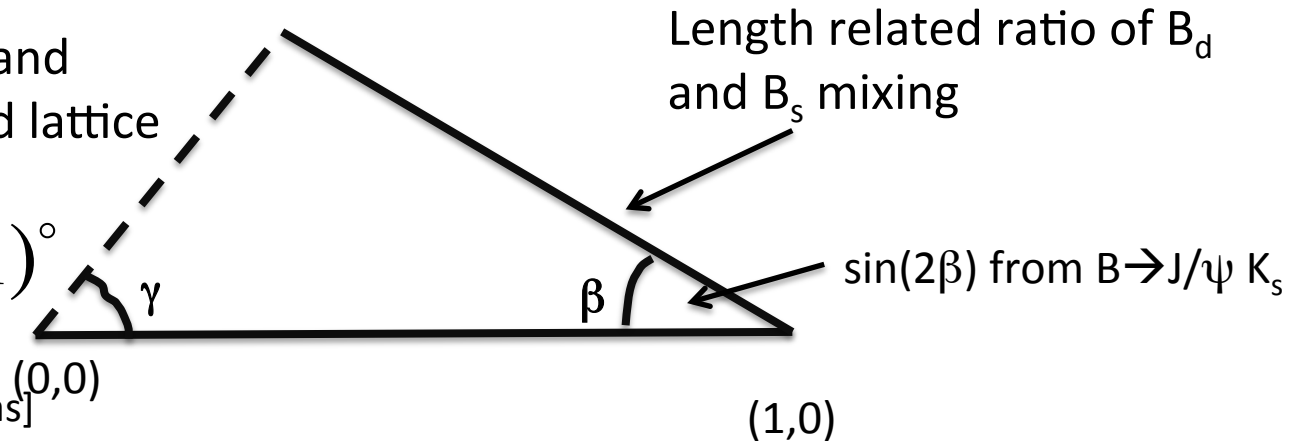
# Combining results -LHCb inputs

LHCb measurement	Type/ Dataset	Reference
$B^+ \rightarrow DK^+ D \rightarrow 2h, 4h$	ADS/(q-)GLW ( $3\text{fb}^{-1}$ )	arXiv:1603.08993
$B^0 \rightarrow DK\pi$	Dalitz ( $3\text{fb}^{-1}$ )	arXiv: 1602.03455
$B^0 \rightarrow DK^* D \rightarrow K_S \pi \pi$	GGSZ MD ( $3\text{fb}^{-1}$ )	arXiv: 1605.01082
$B^+ \rightarrow DK^+ D \rightarrow hh\pi^0$	ADS/q-GLW ( $3\text{fb}^{-1}$ )	PRD 91(2015) 112014
$B^+ \rightarrow DK\pi\pi, D \rightarrow 2h$	ADS/GLW ( $3\text{fb}^{-1}$ )	PRD 92 (2015) 112005
$B^0 \rightarrow DK^* D \rightarrow 2h$	ADS ( $3\text{fb}^{-1}$ )	PRD 90 (2014) 112002
$B^+ \rightarrow DK D \rightarrow K_S hh$	GGSZ MI ( $3\text{fb}^{-1}$ )	JHEP 10 (2014) 097
$B^+ \rightarrow DK, D \rightarrow K_S K\pi$	ADS ( $3\text{fb}^{-1}$ )	PLB 733 (2014) 36
$B_s \rightarrow D_s K, D_s \rightarrow hhh$	Time dep ( $1\text{fb}^{-1}$ )	JHEP 11 (2014) 060

# $\gamma$ from indirect determination

The unitarity triangle is constructed using mixing and  $\sin(2\beta)$  measurements and lattice QCD

$$\gamma = (62.7 \pm 2.1)^\circ$$



EPJC (2016) 76 197 [Blanke, Buras]

Combination of all direct measurements (summer 2015)

$$\gamma = (73.2^{+6.3}_{-7.0})^\circ$$

Alternative approach from CKM fit excluding all direct measurements of  $\gamma$

$$\gamma = (66.9^{+0.94}_{-3.44})^\circ$$

Uncertainties dominated by LQCD, expect to reduce over the next decade

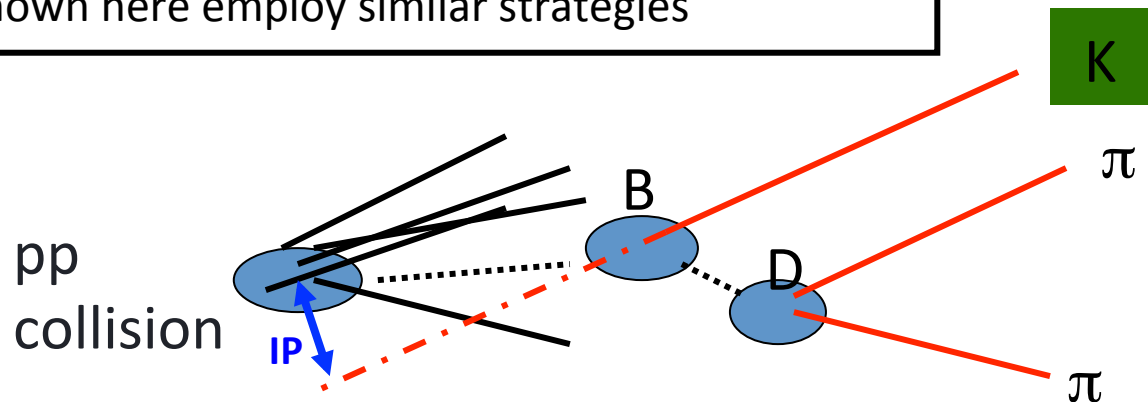
Reaching degree level precision from direct measurements is crucial

# Combing results-other inputs

Parameters	Source	Reference
Charm mixing and CPV in $D \rightarrow hh$	HFAG	<a href="http://www.slac.stanford.edu/xorg/hfag/charm/index.html">www.slac.stanford.edu/xorg/hfag/charm/index.html</a>
$\kappa, \delta_D: D \rightarrow K3\pi, D \rightarrow K\pi\pi^0$	LHCb & CLEO data	PLB 757 (2016) 520
$\kappa, \delta_D: D \rightarrow K_s K\pi$	CLEO data	PRD 85 (2012) 092016
CP fraction $D \rightarrow 4\pi, D \rightarrow hh\pi^0$	CLEO data	PLB 747 (2015) 9
Strong phase information for $D \rightarrow K_s hh$	CLEO data	PRD 82 (2010) 112006
Constraint on $\phi_s$	LHCb data	PRL 114 (2015) 041801

# Selection

All analyses shown here employ similar strategies



Separate the topology of interest from random combinations

Use of multi-variate analysis techniques. Useful variables include:

**Impact parameters**

Flight distances from primary. (B travels a  $\sim$ cm)

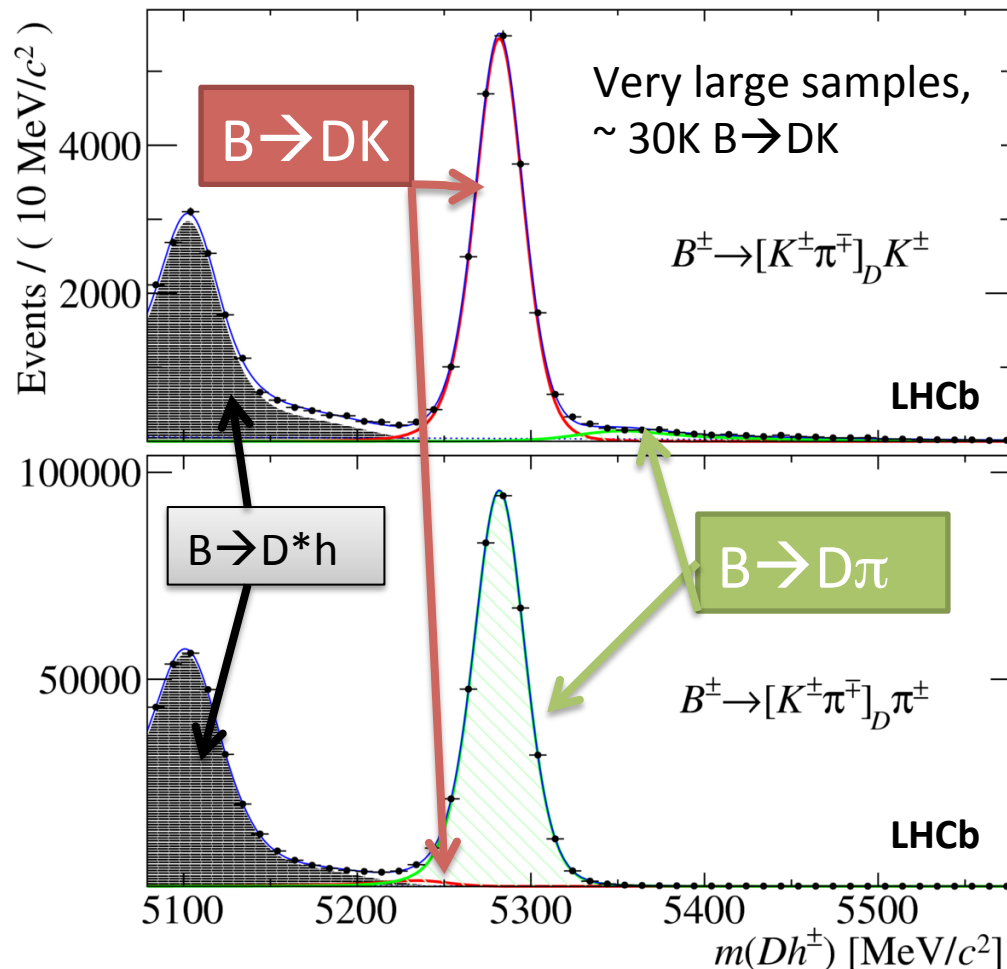
Flight distances from B – removes e.g  $B \rightarrow K\pi\pi$  backgrounds

Vertex quality

**Particle ID**

Specific vetos against particular backgrounds

# $B \rightarrow D[K\pi]h$ – CF control mode



Difference between the two modes only the ID of the bachelor hadron

PID performance  $\rightarrow$  low crossfeed.

$B \rightarrow D^*h$  where a  $\pi^0$  or photon isn't reconstructed sits to the left

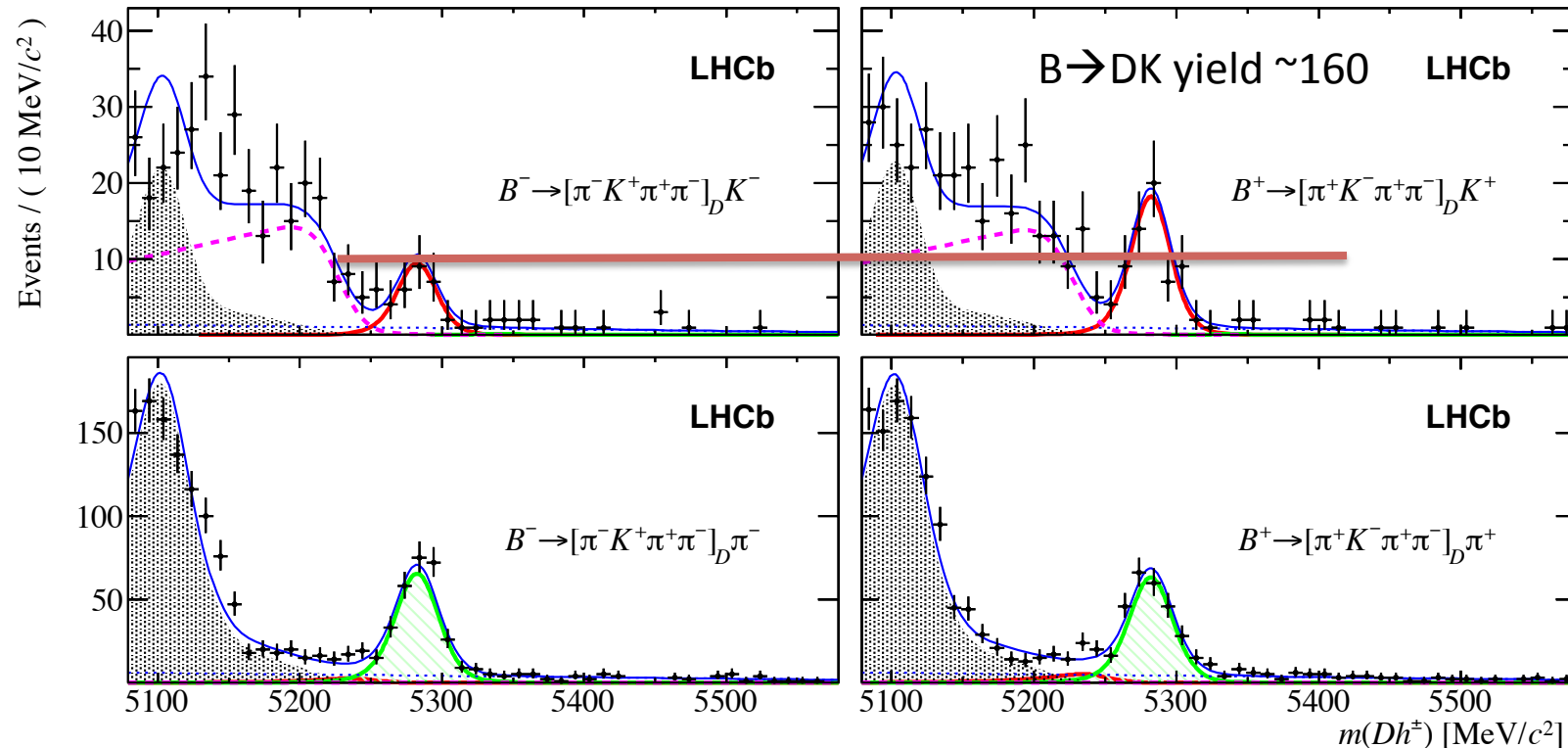
Extremely low level of combinatoric – clean environment

Control mode constrains the shapes of signal and backgrounds

Control mode also used to measure the  $B^\pm$  production asymmetry. Detection asymmetries calibrated from other data.

Results also extracted for  $B \rightarrow D\pi$  mode, interference level expected to be  $\sim$  magnitude smaller

# Results $D \rightarrow K3\pi$



$$A_K^{\pi K \pi \pi} = -0.313 \pm 0.102 \pm 0.038$$

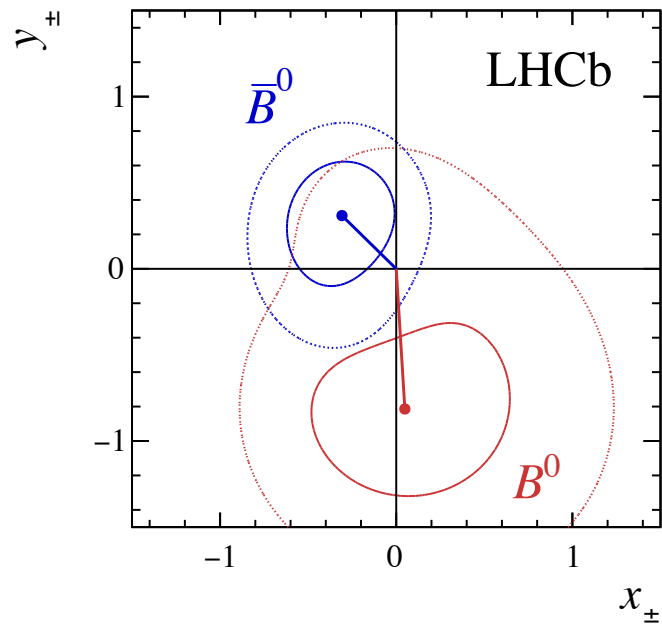
Complementary information to two body modes.

CPV starts to become visible in  $B \rightarrow D\pi$  when combining all  $D \rightarrow hh$  and  $D \rightarrow 4h$  modes.

**3.9 $\sigma$**

# Results

Model - independent



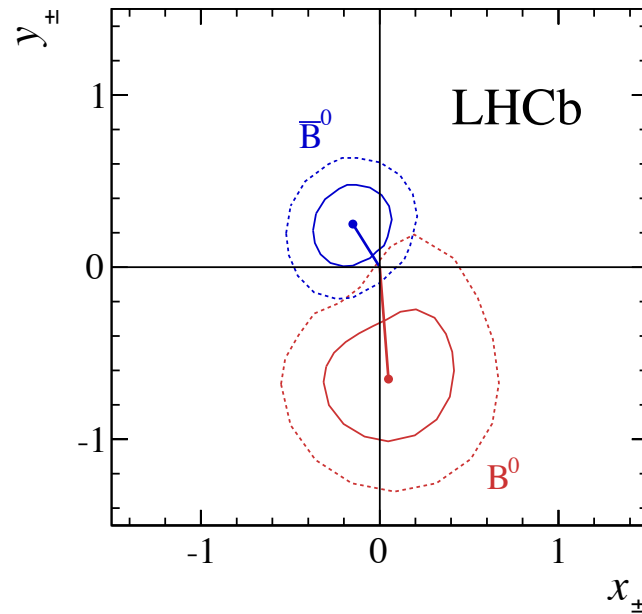
$$x_+ = 0.05 \pm 0.35 \pm 0.02$$

$$y_+ = -0.81 \pm 0.28 \pm 0.06$$

$$x_- = -0.31 \pm 0.20 \pm 0.04$$

$$y_- = 0.31 \pm 0.21 \pm 0.05$$

Model - dependent



$$x_+ = 0.05 \pm 0.24 \pm 0.04 \pm 0.01$$

$$y_+ = -0.65^{+0.24}_{-0.23} \pm 0.08 \pm 0.01$$

$$x_- = -0.15 \pm 0.14 \pm 0.03 \pm 0.01$$

$$y_- = 0.25 \pm 0.15 \pm 0.06 \pm 0.01$$

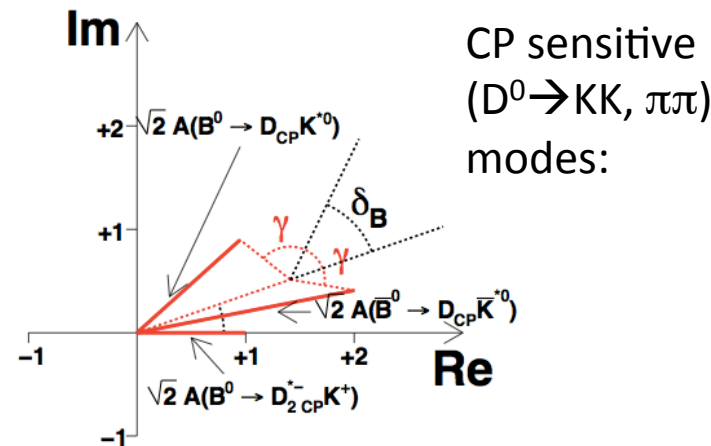
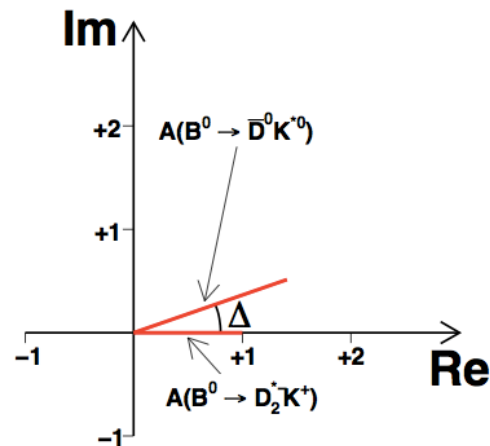
- Good agreement between methods
- Uncertainties from external strong phase information are  $\sim 0.02$  for  $x$  and  $\sim 0.05$  for  $y$ .
- Both methods give  $\sigma(\gamma) = 20^\circ$



# $B^0 \rightarrow DK\pi$ Dalitz plot analysis

- $B^0 \rightarrow DK^*$ ,  $D \rightarrow CP^+$ ,  $K^* \rightarrow K\pi$  restricts the data to the  $K^*$  resonance
- There is sensitivity to  $\gamma$  from the full  $B^0 \rightarrow DK\pi$  decay in any  $K\pi$  resonance
- Amplitude fit of  $B^0 \rightarrow DK\pi$  decay exploits interference between different resonant contributions
- Complex amplitudes of the  $DK^*$  determined relative to flavour-specific  $D_2^* K$
- $\gamma$  measured from amplitudes and not rates  $\rightarrow$  more information than standard GLW analysis
- New method of measuring  $\gamma$

Favoured  
( $D^0 \rightarrow K^+\pi^-$ )  
mode:



CP sensitive  
( $D^0 \rightarrow KK, \pi\pi$ )  
modes:

# $B^0 \rightarrow DK\pi$ Dalitz plot analysis

Favoured ( $D^0 \rightarrow K^+\pi^-$ ) mode:

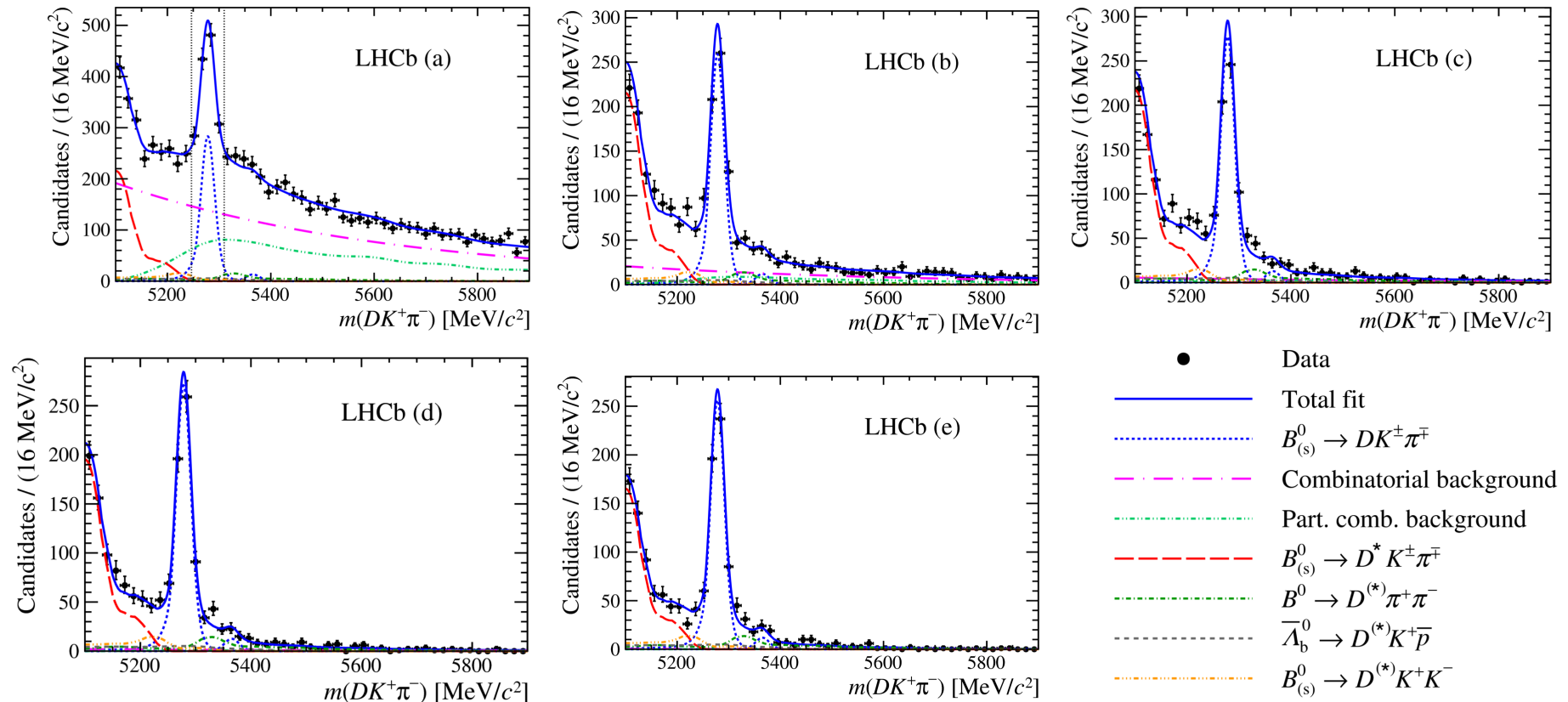
$$A(m^2(D\pi), m^2(K\pi)) = \sum_{j=1}^N c_j F_j(m^2(D\pi), m^2(K\pi))$$

CP sensitive ( $D^0 \rightarrow KK, \pi\pi$ ) modes:

$$c_j \longrightarrow \begin{cases} c_j & \text{for a } D\pi^- \text{ resonance,} \\ c_j [1 + x_{\pm,j} + iy_{\pm,j}] & \text{for a } K^+\pi^- \text{ resonance,} \end{cases}$$

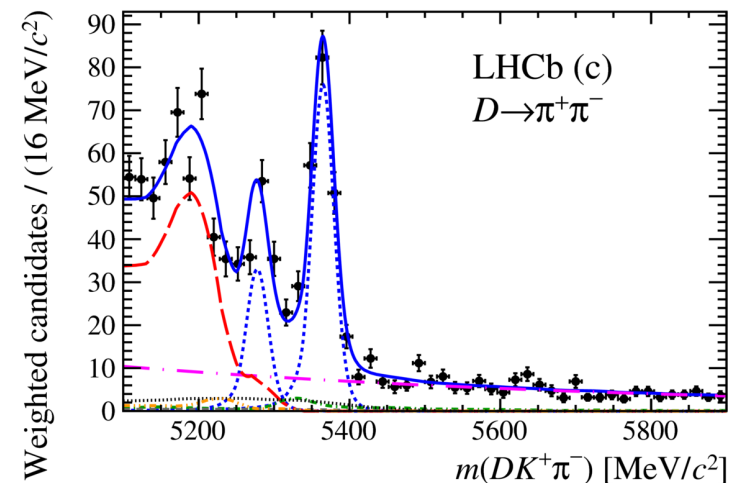
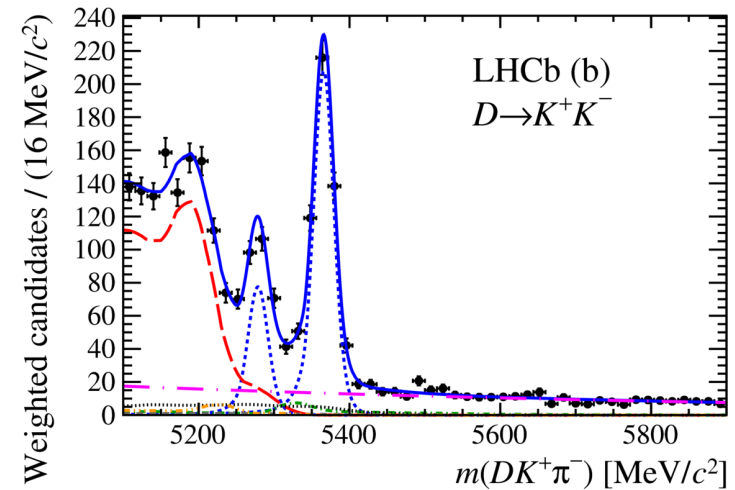
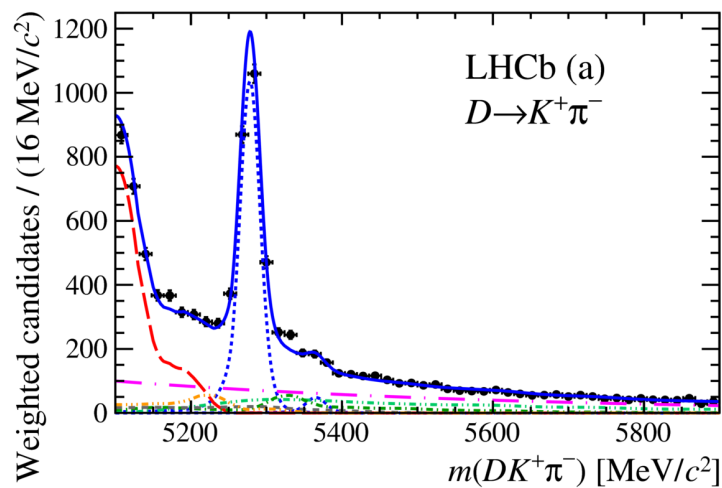
# Larger phasespace $\rightarrow$ higher combinatorics

- Larger phasespace of the  $K\pi$  system leads to high combinatorics and larger amounts of physics bkg.
- To avoid the need to cut hard data is divided into bin of NN output.
- Maximises the statistical sensitivity of the data

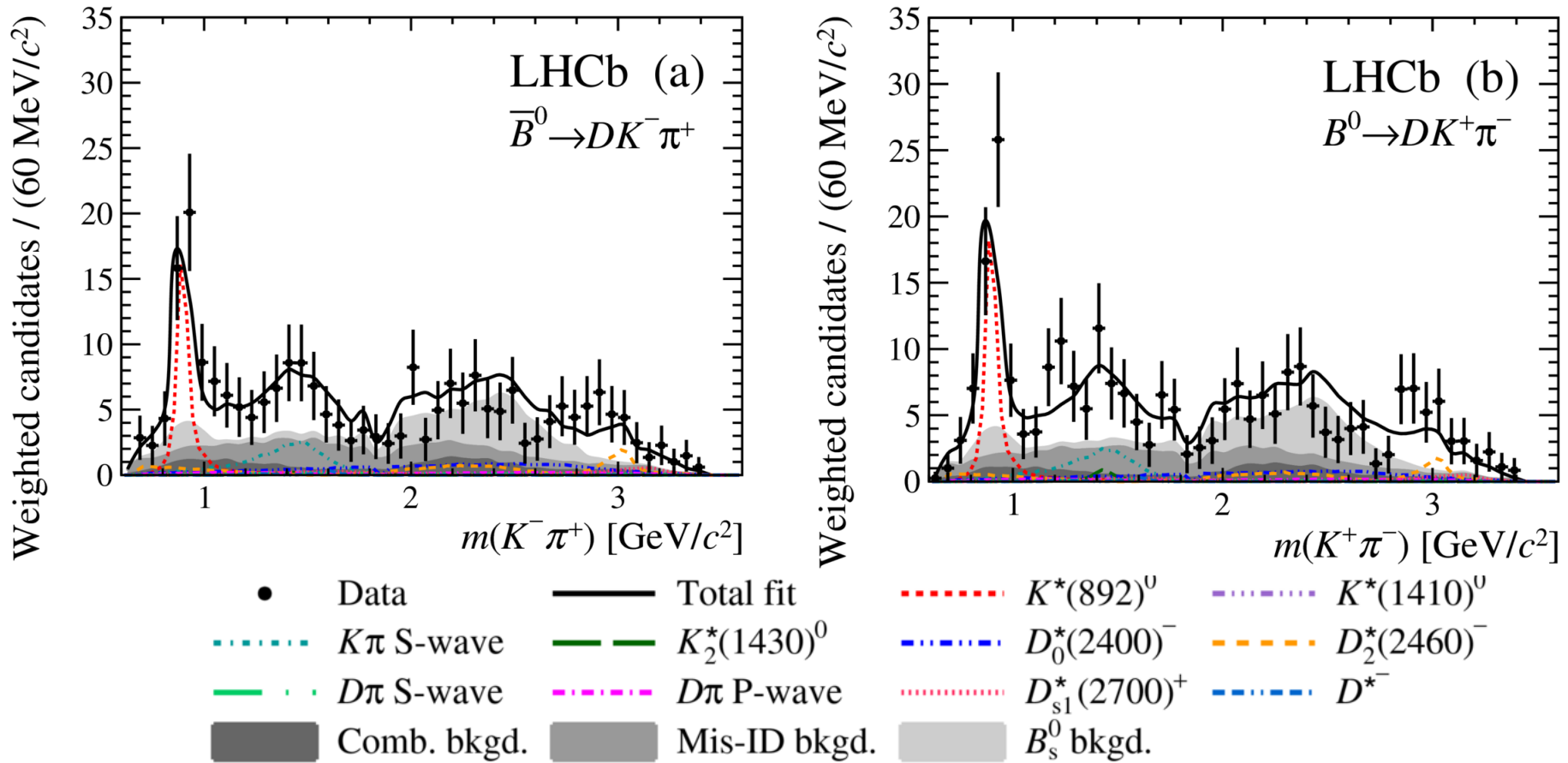


# Signal yields

- To maximise statistical sensitivity data split in bins of MVA output
- Data shown with MVA bins combined weighted according to  $S/(S+B)$
- $339 \pm 22$   $D \rightarrow KK$
- $168 \pm 19$   $D \rightarrow \pi\pi$



# Dalitz Plot fit

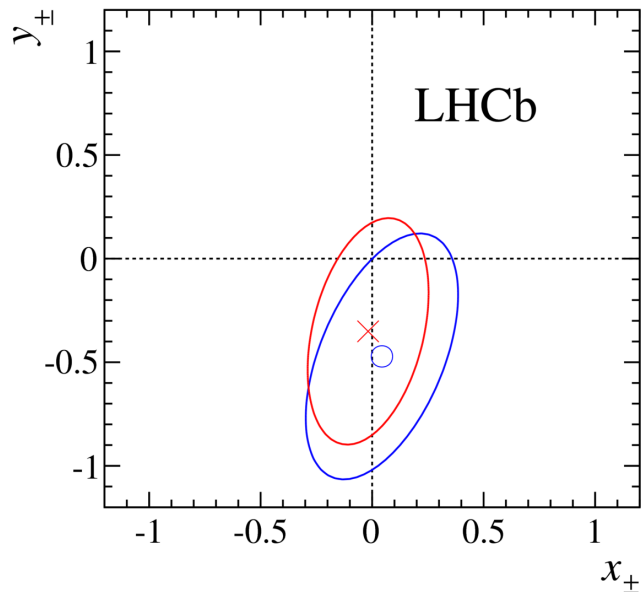


Fit projections of the  $D \rightarrow KK$  and  $D \rightarrow \pi\pi$  samples combined

Only results from  $K^*(892)$  used

Projections look very similar

# Fit Results



$$x_+ = 0.04 \pm 0.16 \pm 0.11$$

$$x_- = -0.02 \pm 0.13 \pm 0.14$$

$$y_+ = -0.47 \pm 0.28 \pm 0.22$$

$$y_- = -0.35 \pm 0.26 \pm 0.41$$

Results for pure  $K^*$

Also determine the coherence factor

$$\kappa = 0.958^{+0.005+0.002}_{-0.010-0.045}$$

