



Scale invariant Volkov–Akulov supergravity



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ABSTRACT

A scale invariant goldstino theory coupled to supergravity is obtained as a standard supergravity dual of a rigidly scale-invariant higher-curvature supergravity with a nilpotent chiral scalar curvature. The bosonic part of this theory describes a massless scalaron and a massive axion in a de Sitter Universe.

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1. Introduction

Motivated by single-field inflationary scenarios [1], several sgoldstinoless [2–5] supergravity extensions of inflationary models were recently considered [6–11] (for a recent review see [12]). Interestingly enough, in [7,11] many of these models were linked to pure higher-derivative supergravity with a nilpotency constraint on the scalar curvature chiral superfield \mathcal{R} . These include the Volkov–Akulov–Starobinsky model [7] and the pure Volkov–Akulov theory coupled to supergravity [7]. Recently, the full component form of the latter theory was presented in [13,14].

Along these lines, various authors considered R^2 theories of gravity [15] and their supergravity embeddings [15,16], which possess a rigid scale invariance and naturally accommodate a de Sitter Universe. It is the aim of this note to give the sgoldstinoless version of these theories, which naturally combines an enhanced rigid scale invariance and a de Sitter geometry. This theory also emerges as a limiting case of the inflationary scenario.

2. Scale-invariant nilpotent supergravity

The superspace action density of the scale-invariant theory that we consider,³

$$\mathcal{A} = \frac{\mathcal{R}\bar{\mathcal{R}}}{g^2} \Big|_D + \sigma \mathcal{R}^2 S_0 + \text{h.c.} \Big|_F, \quad (2.1)$$

where g is a dimensionless parameter, is invariant under the rigid scale transformations

$$\mathcal{R} \rightarrow \mathcal{R}, \quad S_0 \rightarrow e^{-\lambda} S_0, \quad \sigma \rightarrow e^{\lambda} \sigma. \quad (2.2)$$

This theory is equivalent to the theory considered in [16], supplemented with the nilpotency constraint

$$\mathcal{R}^2 = 0, \quad (2.3)$$

which is enforced by the chiral Lagrange multiplier σ present in the second term of eq. (2.1).

Using manipulations similar to those originally introduced in [17], we can now turn this model into a scale-invariant version of the Volkov–Akulov model coupled to standard supergravity. To this end, we first use the superspace identity

$$\sigma \mathcal{R}^2 S_0 + \text{h.c.} \Big|_F = \left(\sigma \frac{\mathcal{R}}{S_0} + \bar{\sigma} \frac{\bar{\mathcal{R}}}{\bar{S}_0} \right) S_0 \bar{S}_0 \Big|_D + \text{tot. deriv.}, \quad (2.4)$$

and then introduce two Lagrange chiral superfield multipliers T and S according to

$$\mathcal{A} = \left(\sigma S + \bar{\sigma} \bar{S} + \frac{S\bar{S}}{g^2} \right) S_0 \bar{S}_0 \Big|_D - T \left(\frac{\mathcal{R}}{S_0} - S \right) S_0^3 + \text{h.c.} \Big|_F. \quad (2.5)$$

The final result is the standard supergravity action density

$$\mathcal{A} = - \left(T + \bar{T} - \sigma S - \bar{\sigma} \bar{S} - \frac{S\bar{S}}{g^2} \right) S_0 \bar{S}_0 \Big|_D + T S S_0^3 + \text{h.c.} \Big|_F + \text{tot. deriv.} \quad (2.6)$$

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³ We use throughout the conventions of [7].

A final shift and a redefinition according to

$$T \rightarrow T + \sigma S, \quad X = \frac{S}{g} \quad (2.7)$$

yield the standard supergravity action density

$$\mathcal{A} = -(T + \bar{T} - X\bar{X})S_0\bar{S}_0 \Big|_D + W(T, X)S_0^3 + \text{h.c.} \Big|_F, \quad (2.8)$$

where

$$W(T, X, \sigma) = gTX + g^2\sigma X^2. \quad (2.9)$$

This is tantamount to the scale-invariant superpotential

$$W(T, X) = gTX, \quad (2.10)$$

where X is subject to the nilpotency constraint

$$X^2 = 0, \quad (2.11)$$

so that X describes the sgoldstinoless Volkov–Akulov multiplet [2–5]. The corresponding bosonic Lagrangian,

$$\mathcal{L} = \frac{R}{2} - \frac{3}{(T + \bar{T})^2} |\partial T|^2 - g^2 \frac{|T|^2}{3(T + \bar{T})^2}, \quad (2.12)$$

is a special case of the result displayed in [7], so that it describes an $SU(1, 1)/U(1)$ Kählerian model of curvature $-2/3$ with a scale-invariant positive potential. As a result, in terms of the canonical variable

$$T = e^{\phi\sqrt{\frac{2}{3}}} + ia\sqrt{\frac{2}{3}}, \quad (2.13)$$

one finds

$$\mathcal{L} = \frac{R}{2} - \frac{1}{2}(\partial\phi)^2 - \frac{1}{2}e^{-2\phi\sqrt{\frac{2}{3}}}(\partial a)^2 - \frac{g^2}{12} - \frac{g^2}{18}e^{-2\phi\sqrt{\frac{2}{3}}}a^2. \quad (2.14)$$

Note that in the Einstein frame the metric is inert under the scale transformation corresponding to eq. (2.2), while

$$\phi \rightarrow \phi + \gamma, \quad a \rightarrow e^{\gamma\sqrt{\frac{2}{3}}}a. \quad (2.15)$$

3. de Sitter vacuum geometry

Since a is stabilized at zero, this model results in a de Sitter vacuum geometry, with a corresponding scale-invariant realization of supersymmetry breaking induced by the non-linear sgoldstinoless multiplet. The supersymmetry breaking scale M_s^2 is

$$M_s^2 = \frac{g}{2\sqrt{3}}M_{\text{Planck}}^2, \quad (3.1)$$

up to a conventional numerical factor. Eq. (2.8) describes the minimal supergravity model that embodies a scale-invariant goldstino interaction and leads unavoidably to a de Sitter geometry. This model involves a single dimensionless parameter g , which determines its *positive* vacuum energy according to

$$V = \frac{g^2}{12}M_{\text{Planck}}^4. \quad (3.2)$$

In contrast, the Volkov–Akulov model coupled to supergravity, depends on the two parameters f and W_0 , and consequently leads to a vacuum energy [18–20,7,13]

$$V = \frac{1}{3}|f|^2 - 3|W_0|^2 \quad (3.3)$$

of arbitrary sign.

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References

- [1] A.A. Starobinsky, A new type of isotropic cosmological models without singularity, *Phys. Lett. B* 91 (1980) 99; D. Kazanas, Dynamics of the Universe and spontaneous symmetry breaking, *Astrophys. J.* 241 (1980) L59; K. Sato, Cosmological baryon number domain structure and the first order phase transition of a vacuum, *Phys. Lett. B* 99 (1981) 66; A.H. Guth, The inflationary Universe: a possible solution to the horizon and flatness problems, *Phys. Rev. D* 23 (1981) 347; V.F. Mukhanov, G.V. Chibisov, Quantum fluctuation and nonsingular Universe, *JETP Lett.* 33 (1981) 532; *Pis'ma Zh. Eksp. Teor. Fiz.* 33 (1981) 549 (in Russian); A.D. Linde, A new inflationary Universe scenario: a possible solution of the horizon, flatness, homogeneity, isotropy and primordial monopole problems, *Phys. Lett. B* 108 (1982) 389; A. Albrecht, P.J. Steinhardt, Cosmology for grand unified theories with radiatively induced symmetry breaking, *Phys. Rev. Lett.* 48 (1982) 1220; A.D. Linde, Chaotic inflation, *Phys. Lett. B* 129 (1983) 177; For recent reviews see: N. Bartolo, E. Komatsu, S. Matarrese, A. Riotto, Non-Gaussianity from inflation: theory and observations, *Phys. Rep.* 402 (2004) 103, arXiv:astro-ph/0406398; V. Mukhanov, *Physical Foundations of Cosmology*, Univ. Press, Cambridge, UK, 2005; S. Weinberg, *Cosmology*, Oxford Univ. Press, Oxford, UK, 2008; D.H. Lyth, A.R. Liddle, *The Primordial Density Perturbation: Cosmology, Inflation and the Origin of Structure*, Cambridge Univ. Press, Cambridge, UK, 2009; D.S. Gorbunov, V.A. Rubakov, *Introduction to the Theory of the Early Universe: Cosmological Perturbations and Inflationary Theory*, World Scientific, Hackensack, USA, 2011, 489 pp; J. Martin, C. Ringeval, V. Vennin, *Encyclopaedia Inflationaris*, arXiv:1303.3787 [astro-ph.CO].
- [2] D.V. Volkov, V.P. Akulov, Is the neutrino a goldstone particle?, *Phys. Lett. B* 46 (1973) 109.
- [3] M. Rocek, Linearizing the Volkov–Akulov model, *Phys. Rev. Lett.* 41 (1978) 451; U. Lindstrom, M. Rocek, Constrained local superfields, *Phys. Rev. D* 19 (1979) 2300.
- [4] R. Casalbuoni, S. De Curtis, D. Dominicis, F. Feruglio, R. Gatto, Nonlinear realization of supersymmetry algebra from supersymmetric constraint, *Phys. Lett. B* 220 (1989) 569.
- [5] Z. Komargodski, N. Seiberg, From linear SUSY to constrained superfields, *J. High Energy Phys.* 0909 (2009) 066, arXiv:0907.2441 [hep-th]; Z. Komargodski, N. Seiberg, Comments on supercurrent multiplets, supersymmetric field theories and supergravity, *J. High Energy Phys.* 1007 (2010) 017, arXiv:1002.2228 [hep-th].
- [6] L. Alvarez-Gaume, C. Gomez, R. Jimenez, Minimal inflation, *Phys. Lett. B* 690 (2010) 68, arXiv:1001.0010 [hep-th]; L. Alvarez-Gaume, C. Gomez, R. Jimenez, A minimal inflation scenario, *J. Cosmol. Astropart. Phys.* 1103 (2011) 027, arXiv:1101.4948 [hep-th].
- [7] I. Antoniadis, E. Dudas, S. Ferrara, A. Sagnotti, The Volkov–Akulov–Starobinsky supergravity, *Phys. Lett. B* 733 (2014) 32, arXiv:1403.3269 [hep-th].
- [8] S. Ferrara, R. Kallosh, A. Linde, Cosmology with nilpotent superfields, *J. High Energy Phys.* 1410 (2014) 143, arXiv:1408.4096 [hep-th].
- [9] R. Kallosh, A. Linde, Inflation and uplifting with nilpotent superfields, *J. Cosmol. Astropart. Phys.* 1501 (2015) 01, arXiv:1408.5950 [hep-th].
- [10] G. Dall'Agata, F. Zwirner, On sgoldstino-less supergravity models of inflation, *J. High Energy Phys.* 1412 (2014) 172, arXiv:1411.2605 [hep-th].
- [11] E. Dudas, S. Ferrara, A. Kehagias, A. Sagnotti, Properties of nilpotent supergravity, arXiv:1507.07842 [hep-th].
- [12] S. Ferrara, A. Sagnotti, Some pathways in non-linear supersymmetry: special geometry Born–Infeld's, cosmology and dualities, arXiv:1506.05730 [hep-th], to appear in a special issue of "p-Adic Numbers, Ultrametric Analysis and Applications".
- [13] E.A. Bergshoeff, D.Z. Freedman, R. Kallosh, A. Van Proeyen, Pure de Sitter supergravity, arXiv:1507.08264 [hep-th].
- [14] F. Hasegawa, Y. Yamada, Component action of nilpotent multiplet coupled to matter in 4 dimensional $\mathcal{N} = 1$ supergravity, arXiv:1507.08619 [hep-th].

- [15] C. Kounnas, D. Lüst, N. Toumbas, R^2 inflation from scale invariant supergravity and anomaly free superstrings with fluxes, *Fortschr. Phys.* 63 (2015) 12, arXiv:1409.7076 [hep-th];
L. Alvarez-Gaume, A. Kehagias, C. Kounnas, D. Lust, A. Riotto, Aspects of quadratic gravity, arXiv:1505.07657 [hep-th].
- [16] S. Ferrara, A. Kehagias, M. Porrati, \mathcal{R}^2 supergravity, *J. High Energy Phys.* 1508 (2015) 001, arXiv:1506.01566 [hep-th].
- [17] S. Cecotti, Higher derivative supergravity is equivalent to standard supergravity coupled to matter. 1, *Phys. Lett. B* 190 (1987) 86.
- [18] D.Z. Freedman, P. van Nieuwenhuizen, S. Ferrara, Progress toward a theory of supergravity, *Phys. Rev. D* 13 (1976) 3214;
S. Deser, B. Zumino, Consistent supergravity, *Phys. Lett. B* 62 (1976) 335;
For a review see: D.Z. Freedman, A. Van Proeyen, *Supergravity*, Cambridge Univ. Press, 2012.
- [19] S. Deser, B. Zumino, Broken supersymmetry and supergravity, *Phys. Rev. Lett.* 38 (1977) 1433.
- [20] E. Cremmer, B. Julia, J. Scherk, P. van Nieuwenhuizen, S. Ferrara, L. Girardello, Super-Higgs effect in supergravity with general scalar interactions, *Phys. Lett. B* 79 (1978) 231;
E. Cremmer, B. Julia, J. Scherk, P. van Nieuwenhuizen, S. Ferrara, L. Girardello, Spontaneous symmetry breaking and Higgs effect in supergravity without cosmological constant, *Nucl. Phys. B* 147 (1979) 105;
E. Cremmer, S. Ferrara, L. Girardello, A. Van Proeyen, Coupling supersymmetric Yang–Mills theories to supergravity, *Phys. Lett. B* 116 (1982) 231;
E. Cremmer, S. Ferrara, L. Girardello, A. Van Proeyen, Yang–Mills theories with local supersymmetry: Lagrangian, transformation laws and superHiggs effect, *Nucl. Phys. B* 212 (1983) 413.