

Naturalness in the dark at the LHC

Nathaniel Craig,^a Andrey Katz,^{b,c,d} Matt Strassler^d and Raman Sundrum^e

^a*Department of Physics, University of California,
Santa Barbara, CA 93106, U.S.A.*

^b*Theory Division, CERN,
CH-1211 Geneva 23, Switzerland*

^c*Department of Theoretical Physics and Center for Astroparticle Physics (CAP),
Université de Genève, 24 quai E. Ansermet, CH-1211 Geneva 4, Switzerland*

^d*Department of Physics, Harvard University,
Cambridge, MA 02138, U.S.A.*

^e*Department of Physics, University of Maryland,
College Park, MD 20742, U.S.A.*

E-mail: ncraig@physics.ucsb.edu, andrey.katz@cern.ch,
strassler@physics.harvard.edu, raman@umd.edu

ABSTRACT: We revisit the Twin Higgs scenario as a “dark” solution to the little hierarchy problem, identify the structure of a minimal model and its viable parameter space, and analyze its collider implications. In this model, dark naturalness generally leads to Hidden Valley phenomenology. The twin particles, including the top partner, are all Standard-Model-neutral, but naturalness favors the existence of twin strong interactions — an asymptotically-free force that confines not far above the Standard Model QCD scale — and a Higgs portal interaction. We show that, taken together, these typically give rise to exotic decays of the Higgs to twin hadrons. Across a substantial portion of the parameter space, certain twin hadrons have visible and often displaced decays, providing a potentially striking LHC signature. We briefly discuss appropriate experimental search strategies.

KEYWORDS: Nonperturbative Effects, Global Symmetries, Effective field theories

ARXIV EPRINT: [1501.05310](https://arxiv.org/abs/1501.05310)

Contents

1	Introduction	1
2	The minimal or “Fraternal” Twin Higgs	5
2.1	The central mechanism	5
2.2	Minimal particle content	7
2.3	Summary of Fraternal Twin Higgs model	9
3	Electroweak breaking and tuning	10
3.1	Effective potential	10
3.2	Matching to SM effective field theory	11
3.3	Estimating electroweak tuning	13
3.4	Twin Higgs effective potential approximation	13
4	Fraternal color	14
4.1	Perturbative considerations	14
4.2	Fraternal confinement	16
5	Twin hadron phenomenology	18
5.1	Kinematic regions	19
5.2	Couplings to the visible sector	20
5.3	Glueball decay	21
5.4	Bottomonium decay	22
5.5	Twin hadron production	24
6	LHC phenomenology	26
6.1	New Higgs decays with displaced vertices	26
6.2	New Higgs decays without displaced vertices	28
6.3	Heavy Higgs decays	28
6.4	Precision Higgs measurements	29
7	Conclusions	31
A	Quarkonium mass spectrum and decays	33
A.1	Spectrum of the quarkonium states	33
A.2	Decays	34
B	Twin hadron production in more detail	35
B.1	Nonperturbative effects in twin gluon production	36
B.2	Nonperturbative effects in twin bottom production	36

C Search strategies	37
C.1 Comments on triggering	37
C.2 Benchmark models	38
C.2.1 Single displaced vertex search	38
C.2.2 Exclusive double displaced vertex search	39
C.2.3 Inclusive double displaced vertex search	39
D Precision electroweak	39
E The effect of twin hypercharge	41

1 Introduction

The principle of Naturalness, the notion that the weak scale should be insensitive to quantum effects from physics at much higher mass scales, necessitates new TeV-scale physics beyond the Standard Model (SM). It has motivated a broad program of searches at the LHC, as well as lower-energy precision/ﬂavor/CP experiments. The absence thus far of any signals in these experiments has disfavored the most popular scenarios, including supersymmetry (SUSY), Composite Higgs and Extra Dimensions, unless their mass scales are raised above natural expectations, leading to sub-percent level electroweak fine-tuning in complete models. The puzzle over why Nature should be tuned at this level has been dubbed the “Little Hierarchy Problem”, and it has led to a major rethinking of naturalness and its implications for experiments.

In a bottom-up approach to this problem, one may take a relatively agnostic view of very high energy physics, and focus instead on naturalness of just the “little hierarchy”, from an experimental cutoff of about 5–10 TeV or so down to the weak scale. Unlike naturalness considerations involving extremely high scales, such as the Planck scale, which are tied to multi-loop virtual effects on the Higgs sector of all SM particles, the bottom-up little hierarchy problem is simpler, relating predominantly to one-loop effects of just the heaviest SM particles, i.e. those coupling most strongly to the Higgs. In Little Higgs, (Natural) SUSY, and extra-dimensional models of gauge-Higgs unification (including warped models that are dual to Higgs Compositeness via the AdS/CFT correspondence), large one-loop radiative corrections to the Higgs from the heaviest SM particles cancel algebraically against those of new symmetry “partners” of these heavy particles, thereby ensuring stability of the little hierarchy.

The most significant of these corrections is associated to the top quark. Naturalness requires that this must be substantially canceled by a corresponding correction from the top’s partner(s), to which it is related by an ordinary global symmetry or supersymmetry. This requirement can only be fulfilled naturally if the associated partner has a mass scale ~ 500 GeV, easily within the kinematic reach of the LHC. Such particles also have significant LHC production cross-sections, since a top partner generally carries the same color charge

as the top quark. Through this logic, the search for top partners in the above incarnations, under a variety of assumptions about possible decay modes, has become a central pursuit of the LHC.

But *must* the top partner be colored? The answer is obviously critical to experimental exploration. Naively the answer is yes, because the algebraic cancellations depend at one-loop on the top Yukawa coupling to the Higgs, and this coupling is itself corrected at one higher loop by QCD. In a rare exception to the “one-loop rule”, such two-loop radiative corrections to the Higgs are still quantitatively important for the little hierarchy problem because of the strength of QCD. It would seem then that the top partner should also be colored so as to parametrically “know” about this QCD effect in symmetry-enforced cancellations.

Yet, remarkably, there do exist solutions to the little hierarchy problem, “Twin Higgs” being the first and prime example, in which the top partners are uncolored [1–3].¹ Here the cancellation among radiative corrections is enforced by a discrete \mathbb{Z}_2 symmetry that exchanges SM particles with new “twin” states. One way to assure naturalness cancellation of QCD two-loop effects is to have the twin symmetry exchange SM color and its gluons with a distinct twin color gauge group and its twin gluons, which couple to and correct the twin top partner just as QCD does the top quark. We will focus on theories of this type, specifically ones in which all twin particles are “dark”, with no SM quantum numbers.

Colorless twin tops are vastly more difficult to produce at the LHC than top partners of more popular theories; indeed this is true for all twin sector particles. Twin particle production can only proceed through a “Higgs portal”, a modest mixing between the SM and twin Higgs sectors that is a necessary consequence of the twin Higgs mechanism for addressing the little hierarchy. Not only is the production rate small, the hidden particles barely interact with ordinary matter, and (at least naively) one would expect they escape the detectors unobserved. The resulting missing energy signature with a very low cross-section would pose great difficulties at the LHC.

How else can the twin sector be detected? Higgs mixing and virtual twin top loops can also subtly affect the SM-like Higgs, making precision tests of its properties extremely important. But with expected LHC precision, the visibility of the twin sector in this manner at the LHC is limited [5]. The Higgs of the twin sector can also potentially be produced, but it may be too wide to observe as a resonance. At best, it is heavy and has a low cross-section, and is far from being excluded or discovered. For these reasons, Twin Higgs remains a viable resolution of the little hierarchy problem, a well-hidden outpost of naturalness.

In this paper, we re-examine the Twin Higgs scenario as an important and distinctive case study in “dark” naturalness, and we identify exciting new experimental opportunities for its discovery. We develop *minimal* Twin Higgs models addressing the little hierarchy problem, roughly paralleling the way in which “Natural SUSY” [6–11] has emerged as a minimal phenomenological approach to the little hierarchy problem in the SUSY

¹Another known solution to the little hierarchy problem which involves uncolored top partners is “Folded Supersymmetry” [4].

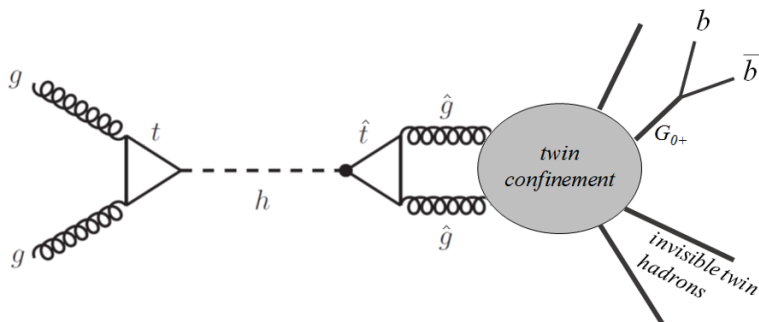


Figure 1. Example of a Twin Higgs collider event. The SM-like Higgs decays through a loop of the twin tops into a pair of twin gluons, which subsequently hadronize to produce various twin glueballs. While some glueballs are stable at the collider scale, G_{0+} decay to Standard Model particles is sufficiently fast to give LHC-observable effects, including possible displaced vertices. The $h\hat{g}\hat{g}$ coupling, indicated by a black dot, is generated by small mixing of the Higgs and the twin Higgs.

paradigm. In both cases, minimalism can be viewed as a tentative organizing principle for doing phenomenology, starting with searches for the minimal natural spectrum and then “radiating outwards” to include searches complicated by non-minimal states. Also in parallel to SUSY, we find that the two-loop relevance of QCD interactions to the little hierarchy problem leads to some of the most promising experimental signals.

In SUSY, the symmetry cancellation at two loops requires the presence of a gluon-partner, the gluino. With large color charge and spin, the gluino is phenomenologically striking over much of motivated parameter space, almost independent of its decay modes [12–14]. In Twin Higgs models, the analogous two-loop role is played by twin gluons, which can again give rise to striking signatures over a large part of parameter space, not because of large cross-sections but because they, along with any light twin matter, are confined into bound states: twin hadrons. Together with the Higgs portal connecting the SM and twin sectors, the presence of metastable hadrons sets up classic “confining Hidden Valley” phenomenology [15–21], now in a plot directly linked to naturalness.

A prototypical new physics event is illustrated in figure 1. The scalar line represents the recently discovered 125 GeV Higgs scalar. This particle is primarily the SM Higgs with a small admixture of twin Higgs; it is readily produced by gluon fusion. But because of its twin Higgs content, it has at least one exotic decay mode into twin gluons, induced by twin top loops, with a branching fraction of order 0.1%. The twin gluons ultimately hadronize into twin glueballs, which have mass in the ~ 1 –100 GeV range within the minimal model. While most twin glueballs have very long lifetimes and escape the detector as missing energy, *the lightest 0^{++} twin glueball has the right quantum numbers to mix with the SM Higgs, allowing it to decay back to the SM on detector timescales.* The first excited 0^{++} state also may have this property. This type of effect was first studied, in the context of a Hidden Valley/quirk model [15, 17, 21, 22] by Juknevič [23].

If the lightest 0^{++} glueball, which we call G_{0+} , has a high mass, then its decay is prompt, and its production rate in Higgs decays may be too rare for it to be observed

at the LHC. However, these non-SM decays of the Higgs would be discoverable at e^+e^- machines, providing strong motivation for ILC, FCC-ee, or CEPC.

For lower mass (typically below ~ 40 GeV in the minimal model we describe) the decay of the G_{0+} may be macroscopically displaced from the interaction point. Such displaced decays are a striking signature, spectacular enough to compensate for the relatively low production rate, and represent an excellent opportunity for the LHC.

Moreover, the signal may be enhanced and/or enriched if there is a sufficiently light twin bottom quark. Depending on this quark's mass, twin bottom production may lead to a larger overall twin hadron production rate; the resulting final states may include twin glueballs, twin bottomonium, or both. In some portions of parameter space, all twin bottomonium states are invisible. In others the lightest 0^{++} state (which we will call $\hat{\chi}$, since it is analogous to the χ_0 states of SM quarkonium) can decay visibly by mixing with the Higgs just like the G_{0+} , though possibly with a small branching fraction. There is also the potential for displaced vertices from this state, though our calculations of lifetimes and branching fractions suffer from large uncertainties.

With a branching fraction of the Higgs to twin hadrons of order 0.1% or greater, our minimal Twin Higgs model should motivate further experimental searches for this signal of hidden naturalness. A branching fraction of 0.1% represents ~ 500 events produced at ATLAS and at CMS during Run I, and we can expect many more at Run II. But triggering inefficiencies threaten this signal. Despite the low backgrounds for highly displaced vertices, triggering on such events can be a significant challenge [16, 24–31]. There is urgency as we approach Run II, since it is not trivial to design triggers that will efficiently capture all variants of the displaced vertex signature arising within the parameter space of the model. In particular, since twin hadron lifetimes are a strong function of their mass, and since displaced decays in different subdetectors require quite different trigger and analysis methods, a considerable variety of approaches will be required for efficient coverage of the parameter space of the model. Further complicating the matter is that precise theoretical predictions of twin glueball and especially twin quarkonium production in Higgs decays is extremely difficult. Hadronization in the twin sector is a complex and poorly understood process, and considerably more investigation will be needed before predictions of glueball and quarkonium multiplicity and kinematic distributions could be possible. Thus this solution to the naturalness problem requires further work on both experimental and theoretical fronts.

We should note that every element that goes into this story has appeared previously in the literature. Hidden glueballs appear in quirk models and other Hidden Valley models [15, 21, 22]; they specifically arise in Folded Supersymmetry [4] and the Quirky Little Higgs [32], which attempt to address the hierarchy problem; the mixing of the G_{0+} with the Higgs to generate a lifetime that is short enough to be observed at the LHC but long enough to often be displaced has appeared in a study [23] of a Hidden Valley model with quirks [21]. However we believe that this is the first time these elements have all been assembled together, giving the striking observable signal of exotic Higgs decays, possibly to long-lived particles, as a sign of hidden naturalness.

Returning from the phenomenology to broader considerations, we note that the Twin Higgs shares with Little Higgs and Composite Higgs models the realization of the Higgs

as a pseudo-Goldstone boson, while representing a significant break with earlier thinking and phenomenology in having a colorless top partner. In the far UV, it is possible that the Twin Higgs structure might match on to more conventional SUSY [33–35] or Composite dynamics [36, 37], or perhaps to something quite novel [38, 39]. We hope that studying the UV matching is facilitated by our bottom-up exploration of minimal Twin Higgs structure and phenomenology. We also hope that this work broadens our perspective on naturalness, motivates more careful investigations of other “darkly” natural mechanisms, such as “Folded Supersymmetry” [4], and perhaps inspires entirely new mechanisms. Ultimately, we hope to broaden the scope of experimental strategies motivated by naturalness, perhaps even leading to a discovery unanticipated by theory.

The paper is organized as follows. Section 2 reviews the basic Twin Higgs structure and develops the minimal model. We show in section 3 that the electroweak tuning in the minimal Twin Higgs model is very mild. Section 4 shows quantitatively that the twin sector likely contains twin QCD in order to maintain naturalness, and its confinement and hadrons are discussed. Section 5 derives some properties of the resulting twin hadrons, and discusses their production and decays. Some subtle points on hadron decays and hadron production are left for appendices A and B. Section 6 synthesizes the earlier considerations and discusses LHC phenomenological implications. Possible experimental strategies for long-lived particle searches are briefly considered in section 6.1 and in more detail in appendix C. Precision Higgs measurements are considered in section 6.4, and precision electroweak constraints are discussed in appendix D. Our conclusions appear in section 7. In appendix E, the phenomenological effect of gauging twin hypercharge, as a non-minimal extension of the model, is considered.

2 The minimal or “Fraternal” Twin Higgs

In this section we construct the *minimal* Twin Higgs model, starting by reviewing the basic symmetries and Higgs structure and then justifying each addition to the twin sector based on the need to maintain naturalness and internal consistency. Because the minimal model does not duplicate *all* SM states in the twin sector (in contrast to the original mirror Twin Higgs model and its descendants [1–3], in which the twin sector and its couplings are an exact copy of the SM), we will refer to this construction as the “Fraternal Twin Higgs”. The model is summarized in subsection 2.3.

2.1 The central mechanism

At its heart, the Twin Higgs mechanism involves realizing the SM-like Higgs as a pseudo-Goldstone boson of an approximate global symmetry, namely SU(4). An SU(4)-fundamental complex scalar \mathcal{H} with potential,

$$V = \lambda(|\mathcal{H}|^2 - f^2/2)^2, \quad (2.1)$$

acquires a vacuum expectation value $\langle \mathcal{H} \rangle = f/\sqrt{2}$, breaking SU(4) \rightarrow SU(3) and giving rise to seven Goldstone bosons, of which one is ultimately identified as the SM-like Higgs scalar. The SU(4) is explicitly broken by the gauge and Yukawa couplings of the Standard Model.

Without additional recourse, this explicit breaking would lead to quadratic sensitivity to higher scales at one loop.

In the context of conventional global symmetry protection, this explicit breaking and UV sensitivity can be ameliorated by extending Standard Model gauge bosons and fermions into representations of the full global symmetry, at the price of introducing additional partner states charged under the SM. In the Twin Higgs, the key insight is that SM states need *not* be extended into full representations of the global symmetry, and instead are merely related to partner states by a \mathbb{Z}_2 exchange symmetry. This \mathbb{Z}_2 is then promoted, at the level of quadratically divergent radiative corrections, to an accidental SU(4) symmetry. The partner particles are no longer related to SM states by a continuous symmetry, and so need not carry SM gauge quantum numbers.

As in any global symmetry mechanism that stabilizes the weak scale, the Twin Higgs does not address the big hierarchy problem all the way to the Planck scale, but merely a little hierarchy up to a cutoff Λ , which is typically $\sim 5\text{--}10$ TeV. This also roughly matches the maximal reach of the LHC. Above Λ we imagine that one of the canonical solutions to the “big” hierarchy problem, such as supersymmetry or compositeness, kicks in to provide protection against yet higher scales.

We can embed the SM Higgs into (2.1) by decomposing $\mathcal{H} = (A, B)$ into two doublets A and B . We identify A with the SM Higgs doublet of gauged electroweak SU(2)_L (and charged under U(1)_Y of course), while B is a doublet of a *different* SU(2) symmetry, which we will call twin SU(2). At this stage, the twin SU(2) group can be either global or gauged. The \mathbb{Z}_2 symmetry acts by exchanging $A \leftrightarrow B$. By far the largest source of explicit breaking from the Standard Model will be the top Yukawa, so to see the magic of the twin mechanism let us also introduce twin top multiplets: three species of the twin fermion \hat{Q}^a transforming as doublets of the twin SU(2) as well as twin right-handed tops \hat{u}^a , where $a = 1 \cdots 3$. The \mathbb{Z}_2 symmetry implies a twin top Yukawa coupling

$$\mathcal{L} \supset \hat{y}_t B \hat{Q}^a \hat{u}^a, \tag{2.2}$$

where we expect $\hat{y}_t \sim y_t$ for the twin mechanism to be effective. Note that the a index implies at least a global SU(3) symmetry acting on fermions \hat{Q} and \hat{u} .

The one-loop radiative potential for the A and B multiplets coming from loops of top and twin top quarks takes the form

$$16\pi^2 V^{(1\text{-loop})} = -6y_t^2 \Lambda^2 |A|^2 - 6\hat{y}_t^2 \Lambda^2 |B|^2 + 3y_t^4 |A|^4 \log(\Lambda^2/y_t^2 |A|^2) + 3\hat{y}_t^4 |B|^4 \log(\Lambda^2/\hat{y}_t^2 |B|^2) \tag{2.3}$$

for a uniform cutoff Λ .² Notice that if $y_t = \hat{y}_t$ then the terms quadratic in the cutoff arrange themselves into an SU(4) invariant $\propto |\mathcal{H}|^2$, while the radiative quartics explicitly break the SU(4) but preserve the \mathbb{Z}_2 . This is the magic of the twin mechanism: if the SM-like Higgs can be identified with a pseudo-Goldstone of the spontaneously broken SU(4), its mass will be insensitive to the SU(4)-symmetric quadratic divergences at one loop (or more) provided the \mathbb{Z}_2 relates y_t and \hat{y}_t .

²One should interpret this cutoff as merely a proxy for physical effects; in a realistic UV completion Λ will be replaced by \mathbb{Z}_2 -symmetric physical thresholds.

A second central issue is vacuum alignment. The vacuum expectation value (vev) of \mathcal{H} , $f/\sqrt{2}$, which breaks the approximate global $SU(4)$ symmetry down to $SU(3)$, can be decomposed,

$$f^2 = v_A^2 + v_B^2. \tag{2.4}$$

In general this vev breaks both $SU(2)_L \times U(1)_Y$ and twin $SU(2)$, such that most components of \mathcal{H} are eaten if twin $SU(2)$ is gauged. The remaining physical scalar states consist of linear combinations of the radial mode and a single uneaten Goldstone boson. We will identify the observed SM-like Higgs with the uneaten Goldstone boson of $SU(4)/SU(3)$. The mass of the radial mode (corresponding to $|\mathcal{H}|^2$ fluctuations) is $\sqrt{2\lambda}f$. (Alternately, we could work purely in terms of the non-linear sigma model of $SU(4)/SU(3)$, in which case there is no perturbative radial mode, and Λ is identified with the cutoff of the non-renormalizable theory. We do not follow this approach here.) To obtain a realistic vacuum, we must break \mathbb{Z}_2 to a small extent. In an exact \mathbb{Z}_2 model the potential favors $v_A = v_B$ and the pseudo-Goldstone Higgs is an equal mixture of A and B , where recall only A carries SM Higgs quantum numbers. Since we have observed a SM-like Higgs experimentally, we will need perturbations stabilizing $v_A^2 \ll v_B^2$, so that the pseudo-Goldstone Higgs is primarily aligned with A .

2.2 Minimal particle content

Thus far we have seen how the essential structure of the twin mechanism operates at the level of the Higgs and the largest source of explicit $SU(4)$ breaking, the top Yukawa coupling, and understood the new twin states thereby required. We continue this process of deducing the minimal ingredients for a realistic and natural Twin Higgs model.

We begin with the top yukawa itself. We have seen schematically that the Higgs is protected against large cutoff sensitivity from top loops provided a twin top with $\hat{y}_t = y_t$. But how much can the top Yukawa \mathbb{Z}_2 be relaxed while preserving the naturalness of the weak scale? When the coupling (2.2) is introduced, by eq. (2.3) the physical mass of the pseudo-Goldstone boson Higgs gets a quadratically divergent radiative correction at the scale Λ ,

$$\delta m_h^2 \approx \frac{3\Lambda^2}{4\pi^2}(y_t^2 - \hat{y}_t^2). \tag{2.5}$$

This precisely cancels out when the \mathbb{Z}_2 symmetry is exact. We can picture this in figure 2, where the pseudo-Goldstone Higgs acquires an effective coupling to the twin top upon integrating out the heavy radial Higgs mode. The cancellation in figure 2 is very similar to that in Little Higgs theories [40–42],³ with the difference that the top partner is uncolored. But without exact \mathbb{Z}_2 symmetry, the naturalness demand that these corrections are not much larger than the observed SM-like Higgs mass-squared of $(125 \text{ GeV})^2$, translates into

$$\left| \frac{\hat{y}_t(\Lambda) - y_t(\Lambda)}{y_t(\Lambda)} \right| \lesssim 0.01, \tag{2.6}$$

for $\Lambda \sim 5 \text{ TeV}$.

³See also [43] for review and references therein.

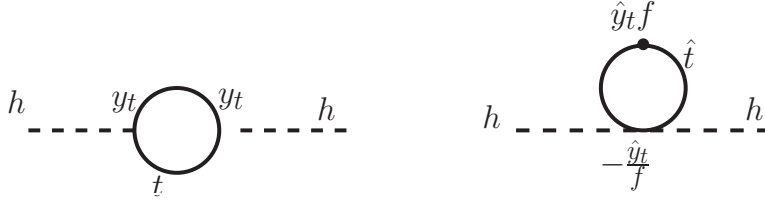


Figure 2. Cancellation of the top divergence in the Twin Higgs model. The effective vertex in the second diagram arises upon integrating out the heavy radial mode.

Ordered by the size of tree-level couplings to the Higgs doublet, the next ingredients to consider are the potential twin sector equivalents of $SU(2)_L \times U(1)_Y$ gauge bosons. The contribution to the Higgs mass-squared from $SU(2)_L$ boson loops in the SM is $\sim (400 \text{ GeV})^2$ for a cutoff $\Lambda \sim 5 \text{ TeV}$ — still a significant source of electroweak destabilization, although subdominant to top loops. This suggests gauging the twin $SU(2)$ global symmetry acting on B and \hat{Q} . Introducing twin weak gauge bosons with coupling \hat{g}_2 translates to the quadratic cutoff sensitivity in the pseudo-Goldstone Higgs,

$$\delta m_h^2 \approx \frac{9\Lambda^2}{32\pi^2} (\hat{g}_2^2(\Lambda) - g_2^2(\Lambda)), \quad (2.7)$$

in analogy with eq. (2.5). Demanding this not significantly exceed the observed Higgs mass-squared implies $|\frac{\hat{g}_2(\Lambda) - g_2(\Lambda)}{g_2(\Lambda)}| \lesssim 0.1$. Note that with this gauging of twin $SU(2)$ all Goldstone bosons of $SU(4)$ breaking, except for the SM-like Higgs itself, are now longitudinal weak bosons of the visible and twin sectors.

In contrast, the contribution to m_h^2 from $U(1)_Y$ loops in the SM is comparable to m_h^2 for a cutoff $\Lambda \sim 5 \text{ TeV}$, and thus already consistent with naturalness. Thus naturalness does not require twin hypercharge, although it was included in the original Twin Higgs [1]. This is analogous to the statement that in natural supersymmetry there is no need for the Bino to be light; its presence in the low-energy spectrum is non-minimal from the bottom-up point of view. Given that our principle in this paper is to seek the most economical version of the twin Higgs that is consistent with the naturalness of the little hierarchy, we do not include twin hypercharge in the minimal twin Higgs model, assuming instead that it was never gauged or that it was broken at or around the scale Λ . However, for the sake of completeness, we will briefly discuss the significant phenomenological consequences of a light twin hypercharge boson in appendix E.

Next we turn to the twin analogue of QCD. Of course the Higgs does not couple to $SU(3)$ at tree level, but rather at one loop via its coupling to the top quark. This nonetheless leads to sizable two-loop corrections to the Higgs mass from physics around the cutoff. As we will discuss in detail in section 4.1, the contribution to the Higgs mass-squared from two-loop $y_t^2 g_3^2$ corrections in the SM is *at least* $\sim (350 \text{ GeV})^2$ for a cutoff $\Lambda \sim 5 \text{ TeV}$, putting QCD on similar footing as the weak gauge group. Gauging the twin $SU(3)$ global symmetry with coupling \hat{g}_3 gives quadratic cutoff sensitivity in the pseudo-Goldstone Higgs

$$\delta m_h^2 \approx \frac{3y_t^2 \Lambda^2}{4\pi^4} (g_3^2 - \hat{g}_3^2). \quad (2.8)$$

This is a key observation that will drive the phenomenology of a viable Twin Higgs model: naturalness and minimality favor a confining gauge symmetry in the hidden sector, “twin glue”. This twin glue has a coupling close to the QCD coupling — we will see how close in section 4.1 — and therefore it confines at a scale $\hat{\Lambda}_3$ which is logarithmically close to the SM QCD confinement scale.

Once the twin SU(2) and SU(3) are gauged, we should include a variety of twin fermions in addition to the twin top quark to cancel anomalies. To render the twin SU(3) anomaly-free we should include a twin RH bottom quark \hat{b} ; symmetries then admit the hidden sector bottom Yukawa coupling

$$\mathcal{L} = \hat{y}_b B \hat{Q} \hat{b}. \tag{2.9}$$

Unlike the case of the top sector, we should not necessarily demand that $\hat{y}_b = y_b$ since the bottom Yukawa has a much weaker effect on the SM Higgs mass at one loop. At this stage it suffices that $\hat{y}_b \ll y_t$ in order to avoid creating a hierarchy problem from the bottom sector.

Similarly, canceling the twin SU(2) anomaly requires an additional doublet neutral under the twin SU(3): \hat{L} , left-handed twin tau. Although not required for anomaly cancellation, introducing a twin right-handed tau $\hat{\tau}_R$ allows the $\hat{\tau}$ to be rendered massive provided a Yukawa coupling

$$\mathcal{L} \supset \hat{y}_\tau B \hat{L} \hat{\tau}_R. \tag{2.10}$$

As in the case of the twin bottom Yukawa, \hat{y}_τ need not respect the \mathbb{Z}_2 as long as $\hat{y}_\tau \ll \hat{y}_t$. The twin neutrino may be rendered massive in the same way as the SM neutrinos; its mass plays no role in naturalness and is essentially a free parameter of the model. Finally, twin light-flavor (first and second generation) fermions are totally unnecessary for naturalness, as their Yukawa couplings too small to meaningfully disturb the Higgs potential, and are therefore absent in our minimal “Fraternal” model.

2.3 Summary of Fraternal Twin Higgs model

Thus we arrive at the ingredients of our minimal Twin Higgs model:

1. An additional twin Higgs doublet and an approximately SU(4)-symmetric potential.
2. Twin tops and a twin top Yukawa that is numerically very close to the SM top Yukawa.
3. Twin weak bosons from the gauged SU(2) with $\hat{g}_2(\Lambda) \approx g_2(\Lambda)$.
4. Twin glue, a gauged SU(3) symmetry with $\hat{g}_3(\Lambda) \approx g_3(\Lambda)$. This gauge group is asymptotically free and it confines, at a scale $\hat{\Lambda}_3$ that we will discuss in section 4.2.
5. Twin bottoms and twin taus, whose masses are essentially free parameters so long as they remain much lighter than the twin top.
6. Twin neutrino from the twin tau doublet, which may have a Majorana mass, again a free parameter as long as it is sufficiently light.

As an aside, we note that in contrast to a model with a perfect twin of the Standard Model, this model is cosmologically safe; with at worst one massless particle (the twin tau neutrino), and fewer degrees of freedom than the visible sector, the effective number of degrees of freedom during nucleosynthesis and recombination is very small.

Not accidentally, the most crucial ingredients for the naturalness of the theory — a twin Higgs, twin tops, and twin glue — strongly resemble the ingredients of natural supersymmetry (Higgsinos, stops, and the gluino). But the key difference here is the likely existence of a new, confining gauge group in the minimal twin sector. Although twin glue does not impact the Higgs directly at one loop, its contributions at two loops make it a key component of a viable twin Higgs model.

3 Electroweak breaking and tuning

In this section, we study the effective potential of the Fraternal Twin Higgs model outlined above. We show how realistic electroweak symmetry breaking can be achieved, accompanied by a 125 GeV Higgs scalar, and estimate the tuning of couplings needed. In subsection 3.1, we write down the effective potential for the full Higgs sector of the model at one-loop order. In subsection 3.2, we integrate out the heavier Higgs to get an effective potential for just the SM-like Higgs. In subsection 3.3, we determine that the degree of fine-tuning needed to have realistic electroweak breaking and SM-like Higgs mass is $\sim 2v^2/f^2$. Finally, in subsection 3.4 we more fully justify the form of our starting effective potential in subsection 3.1, by showing that it is free from other types of fine-tuning.

3.1 Effective potential

The Twin Higgs effective potential is given, to good approximation, by

$$V_{\text{eff}} = \lambda(|A|^2 + |B|^2 - f^2/2)^2 \tag{3.1}$$

$$+ \kappa(|A|^4 + |B|^4) \tag{3.2}$$

$$+ \rho|A|^4 + \sigma f^2|A|^2 \tag{3.3}$$

$$+ \frac{3y_t^4}{16\pi^2} [|A|^4 \ln(\Lambda^2/y_t^2|A|^2) + |B|^4 \ln(\Lambda^2/y_t^2|B|^2)], \tag{3.4}$$

where for concrete estimates we will take the UV cutoff of the Twin Higgs theory to be $\Lambda = 5 \text{ TeV}$. Lines (3.1)–(3.3) represent the most general renormalizable tree-level terms consistent with the SM and twin gauge symmetries. Line (3.1) is just our starting point, eq. (2.1), the subset of terms respecting the global SU(4) symmetry, under which (A, B) transform in the fundamental representation. Line (3.2) consists of the extra terms allowed by breaking SU(4) but preserving the discrete \mathbb{Z}_2 global subgroup, $A \leftrightarrow B$. (The other \mathbb{Z}_2 invariant, $|A|^2|B|^2$, is equivalent to this, modulo SU(4)-invariant terms.) Line (3.3) consists of the remaining extra terms which respect only the gauge symmetries. Line (3.4) is the dominant one-loop radiative correction that cannot be absorbed into a redefinition of the tree potential, due to a (twin) top loop. This is just eq. (2.3), where we have set $\hat{y}_t = y_t$; in section 4, we will justify this as a good approximation because of the gauging of twin

color. While the logarithmic cutoff dependence above can be removed by renormalization of κ , we will keep the above form for later convenience in making estimates.

3.2 Matching to SM effective field theory

Before fully justifying the above approximate structure for the effective potential, we will first work out its consequences, in particular matching it to a SM effective field theory at lower energies. This will allow us to choose the rough sizes of the different couplings needed for realism, and to then self-consistently check our approximation.

Line (3.1) contains the dominant mass scale, set by f . We take the SU(4)-symmetric self-interaction to be modestly weak, $\lambda \lesssim 1$. We seek to stabilize the vacuum such that

$$f = \text{few} \times v_A, \quad v_A = v \equiv 246 \text{ GeV}, \tag{3.5}$$

so that the pseudo-Goldstone Higgs is primarily SM-like. We will also use this small hierarchy to work perturbatively in powers of v/f .

We begin by studying the limit $v/f = 0$. The dominant potential, (3.1), then gives rise to a spontaneous symmetry breaking SU(4) \rightarrow SU(3), where the breaking VEV is in the B direction,

$$\langle B_0 \rangle = f/\sqrt{2}. \tag{3.6}$$

This breaks twin SU(2) gauge symmetry, with three of the seven Nambu-Goldstone bosons being eaten in the process. The remaining four real Nambu-Goldstone bosons form the complex A doublet, namely the SM Higgs doublet of electroweak gauge symmetry. The fourth uneaten B scalar is the radial mode of the potential, a physical heavy exotic Higgs particle with mass,

$$m_{\tilde{h}} = \sqrt{2\lambda}f. \tag{3.7}$$

Later, $\mathcal{O}(v^2/f^2)$ perturbations will mix these boson identifications to a small extent.

The couplings ρ and σ break the discrete \mathbb{Z}_2 symmetry. The only other couplings in the theory that break \mathbb{Z}_2 are the small SM hypercharge coupling and the very small Yukawa couplings to the light fermions (and their twin equivalents in the case of the τ and b , also taken to be $\ll 1$). Therefore it is technically natural to take ρ to be as small as $\sim g_1^4/(16\pi^2)$, where g_1 is the SM hypercharge coupling. This is so small that we neglect it in what follows.⁴ We can however consistently take σf^2 to represent an explicit *soft* breaking of \mathbb{Z}_2 symmetry. Still, we will take $\sigma < \lambda$ so that line (3.1) dominates the mass scales as assumed above.

At energies well below the heavy Higgs mass and heavy twin gauge boson masses, set by f , $|A|^2 + |B|^2$ is rigidly fixed at the bottom of the potential in line (3.1),

$$|B|^2 = \frac{f^2}{2} - |A|^2. \tag{3.8}$$

⁴The possibility of larger ρ offers alternate model building opportunities but we do not pursue them in this paper.

Plugging this into the (A, B) effective potential (and neglecting ρ as discussed above) gives an effective potential for just the lighter A degrees of freedom,

$$\begin{aligned}
 V_{\text{eff}}(A) = & \left[2\sigma - 2\kappa - \frac{3y_t^4}{8\pi^2} \left(\ln(\Lambda^2/m_{\hat{t}}^2) - \frac{1}{2} \right) \right] \frac{m_{\hat{t}}^2}{y_t^2} |A|^2 \\
 & + \left[2\kappa + \frac{3y_t^4}{16\pi^2} \left(\ln(\Lambda^2/y_t^2|A|^2) + \ln(\Lambda^2/m_{\hat{t}}^2) - \frac{3}{2} \right) \right] |A|^4 \\
 & + \mathcal{O}(A^6/f^2),
 \end{aligned} \tag{3.9}$$

where this equation is expressed in terms of the mass of the twin top, or “top partner”,

$$m_{\hat{t}} = y_t \frac{f}{\sqrt{2}}, \tag{3.10}$$

in analogy with the top quark mass.

Eq. (3.9) has the form of a SM effective potential, with the tree-like $|A|^2, |A|^4$ terms, as well as a top-loop induced $|A|^4 \ln(\Lambda^2/y_t^2|A|^2)$ term. Successful electroweak symmetry breaking, $\langle A_0 \rangle = 246 \text{ GeV}/\sqrt{2}$, and a physical Higgs mass of 125 GeV, can therefore be arranged by tuning the $|A|^4$ coefficient using κ , and the $|A|^2$ coefficient using σ . To estimate the tuning involved, we can neglect the modest $\ln|A|$ modulation of $|A|^4$, and just set the logarithm to its expectation value,

$$\begin{aligned}
 V_{\text{eff}} \approx & \left[2\sigma - 2\kappa - \frac{3y_t^4}{4\pi^2} \left(\ln(\Lambda/m_{\hat{t}}) - \frac{1}{4} \right) \right] \frac{m_{\hat{t}}^2}{y_t^2} |A|^2 \\
 & + \left[2\kappa + \frac{3y_t^4}{4\pi^2} \ln(\Lambda/m_{\hat{t}}) + \frac{3y_t^4}{8\pi^2} \left(\ln(m_{\hat{t}}/m_t) - \frac{3}{4} \right) \right] |A|^4 \\
 \equiv & -\lambda_{\text{SM}} v^2 |A|^2 + \lambda_{\text{SM}} |A|^4,
 \end{aligned} \tag{3.11}$$

where $m_t = y_t \langle A_0 \rangle$. For realistic electroweak scale and physical Higgs mass we require $\lambda_{\text{SM}} \approx \frac{1}{8}$, $v = 246 \text{ GeV}$.

Noting that $\ln(m_{\hat{t}}/m_t) - \frac{3}{4} = \ln(\text{few}) - \frac{3}{4} \sim \mathcal{O}(1)$, we will neglect this term relative to the $\ln(\Lambda/m_{\hat{t}})$ -enhanced top-loop contribution to the Higgs quartic, so that

$$\lambda_{\text{SM}} \approx 2\kappa + \frac{3y_t^4}{4\pi^2} \ln(\Lambda/m_{\hat{t}}). \tag{3.12}$$

With $y_t \approx 1$, the top-loop induced quartic coupling is already close to the required value, $\lambda_{\text{SM}} \sim 1/8$. A higher-order and renormalization-group improved analysis, as in studies of analogous corrections in supersymmetry, is expected to reduce this radiative correction, the central feature of which can be captured by using a top-Yukawa coupling renormalized at several TeV, where $y_t^4 \approx 1/2$. In any case, the rough sizes of the radiative corrections in the Twin Higgs theory are comparable to the realistic value of λ_{SM} , and so with a κ of comparable magnitude we are able to successfully and naturally fit the observed physical Higgs mass.

As an aside, it is instructive to compare the form of the logarithmically divergent (twin) top-loop contributions in eq. (3.9) with the analogous contributions from top/stop

loops in weak scale supersymmetry (for large $\tan\beta$ and small stop mixing). As in supersymmetry, the quadratic divergence in the top-loop contribution to the Higgs potential has been canceled by a top partner mechanism. However, there remains a logarithmically divergent contribution to the Higgs mass-squared. This has precisely the same form as in supersymmetry with the replacement, $m_{\text{stop}} \rightarrow m_{\hat{t}}$. We see there are also logarithmically divergent contributions to the Higgs quartic self-coupling from the (twin) top loop. Again, there are analogous contributions in supersymmetry of the same magnitude, but the stop contribution has the opposite sign due to its Bose statistics. Thus in supersymmetry the logarithmic divergence cancels out here, but there is still a finite logarithmic enhancement factor of $\ln(m_{\text{stop}}^2/m_{\hat{t}}^2)$ to the Higgs quartic correction. Unlike the MSSM where the tree-level Higgs quartic is set by electroweak gauge couplings, here we have an unconstrained tree-level quartic contribution, 2κ . (However, κ also appears in the Higgs mass term, so it will affect electroweak tuning, as discussed below.)

3.3 Estimating electroweak tuning

Electroweak tuning involves the quadratic terms of the potential. Fortunately, the same combination of parameters that dominates the quartic self-coupling, in the second line of eq. (3.11), also appears in the quadratic terms of the potential, in the first line of eq. (3.11). We will drop the $1/4$ term relative to the $\ln\Lambda$ -enhanced part of the top radiative correction. Then, matching the quadratic terms to the SM form on the last line, we have

$$\lambda_{\text{SM}}v^2 \approx (\lambda_{\text{SM}} - 2\sigma)\frac{m_{\hat{t}}^2}{y_t^2}. \tag{3.13}$$

The degree of electroweak tuning of σ needed to achieve this is therefore

$$\begin{aligned} \text{Electroweak-tuning} &\sim \frac{\lambda_{\text{SM}}v^2}{\lambda_{\text{SM}}(m_{\hat{t}}^2/y_t^2)} \\ &= \frac{2m_{\hat{t}}^2}{m_t^2} = \frac{2v^2}{f^2}. \end{aligned} \tag{3.14}$$

For example, for $f \sim 3v$ ($m_{\hat{t}} \approx 500\text{--}600$ GeV), this corresponds to a very mild 20 percent electroweak tuning.

3.4 Twin Higgs effective potential approximation

Finally, we justify our starting approximation for the Twin Higgs effective potential upon which our analysis of electroweak breaking and tuning is based. To do this, we examine each term of eqs. (3.1)–(3.4) and ask whether its coefficient is radiatively stable, and also whether this coupling itself significantly radiatively corrects other couplings.

The tuning needed to have f smaller than the cutoff Λ is determined by the leading radiative corrections to the quadratic terms in line (3.1). We have taken the SU(4)-symmetric self-interaction to be weakly coupled enough that the leading quadratic radiative corrections come from the (twin) top loop and the large Yukawa coupling,

$$V^{(1\text{-loop})} \supset \frac{3}{8\pi^2}y_t^2\Lambda^2(|A|^2 + |B|^2). \tag{3.15}$$

The other couplings that can similarly contribute at one loop are the electroweak gauge couplings, as well as κ and ρ . The electroweak couplings are subdominant to the top Yukawa coupling as reviewed earlier. We have estimated that $\kappa \sim \mathcal{O}(\lambda_{\text{SM}})$ (eq. (3.12) and ensuing discussion), and loops using the SM Higgs quartic coupling are also considerably subdominant to top loops. Finally, we have consistently chosen ρ to be very small as explained earlier. Therefore, eq. (3.15) dominates radiative corrections to λf^2 and gives a tuning to keep $f \ll \Lambda$ of

$$f\text{-tuning} \sim \frac{\lambda f^2}{\frac{3}{8\pi^2} y_t^2 \Lambda^2} = \frac{8\pi^2 \lambda f^2}{3 y_t^2 \Lambda^2}. \quad (3.16)$$

If we take for example $f \sim 3v \sim 750 \text{ GeV}$, we see that there is essentially no tuning.

We are taking κ to be comparable to the leading radiative corrections from the top loop (eq. (3.12) and ensuing discussion), so this \mathbb{Z}_2 -preserving but $\text{SU}(4)$ -violating coupling is radiatively stable and natural. As explained earlier, we can naturally take the *hard* breaking of \mathbb{Z}_2 given by ρ to be negligibly small. σf^2 represents a *soft* breaking of \mathbb{Z}_2 , with $\sigma \sim \lambda_{\text{SM}}/2$ (eq. (3.13) and ensuing discussion), and is clearly natural without other sources of soft breaking. To tune to realistic electroweak symmetry breaking we saw that we needed $\sigma \sim \lambda_{\text{SM}}/2 \sim 1/16$, therefore we can easily have $\sigma f^2 \ll \lambda f^2$ to ensure that line (3.1) indeed dominates the mass scales of the Twin Higgs potential as our analysis presumes.

With all couplings in our theory being perturbative, our one-loop analysis suffices for demonstrating the successful matching to a realistic SM effective field theory and for estimating the tuning required.

4 Fraternal color

We now discuss the dynamics of twin color in more detail. We first calculate how close the twin and visible sector color couplings must be to preserve naturalness. Then we estimate the confinement scale of twin color and discuss the associated twin hadrons, including glueballs and quarkonia.

4.1 Perturbative considerations

As we have seen above, the twin Higgs mechanism for naturalness, at one-loop order, requires the top and twin-top Yukawa couplings to be very nearly identical close to the cutoff. Here we show that when QCD effects are taken into account at two-loop order, naturalness favors having a twin QCD, with a gauge coupling similar to that of QCD near the cutoff Λ .

To see this, consider the one-loop RG analysis for the dimensionless Wilsonian running mass-squared parameter of the SM-like Higgs, $x(\mu) \equiv \frac{m_h^2(\mu)}{\mu^2}$:

$$\begin{aligned} \frac{dx}{d \ln \mu} &= -2x + \frac{3(\hat{y}_t^2 - y_t^2)}{2\pi^2}; \\ \frac{dy_t}{d \ln \mu} &= \frac{9y_t^3}{32\pi^2} - \frac{y_t g_3^2}{2\pi^2}; & \frac{d\hat{y}_t}{d \ln \mu} &= \frac{9\hat{y}_t^3}{32\pi^2} - \frac{\hat{y}_t \hat{g}_3^2}{2\pi^2}; \\ \frac{dg_3}{d \ln \mu} &= -\frac{7g_3^3}{16\pi^2}; & \frac{d\hat{g}_3}{d \ln \mu} &= -\frac{29\hat{g}_3^3}{48\pi^2}, \end{aligned} \quad (4.1)$$

where g_3 is the SM QCD coupling and \hat{g}_3 is the twin QCD coupling. Note that g_3 and \hat{g}_3 run differently because the SM has six QCD quark flavors while the minimal model has just two twin QCD flavors. If we neglect the running of $y_t, \hat{y}_t, g_3, \hat{g}_3$, then the solution to the first of these equations is simply given by

$$m_h^2(\mu) = m_h^2(\Lambda) + \frac{3(y_t^2 - \hat{y}_t^2)}{4\pi^2}(\Lambda^2 - \mu^2). \quad (4.2)$$

In running down to the weak scale or physical Higgs mass, $\mu \ll \Lambda$, we see we have merely matched onto the one-loop result of eq. (2.5), which stresses the importance of having y_t and \hat{y}_t be very nearly the same. But taking account of the running of $y_t, \hat{y}_t, g_3, \hat{g}_3$ by solving all of eqs. (4.1) then gives an RG-improved result, which allows us to explore the role of twin color in maintaining $y_t \sim \hat{y}_t$ as the couplings run.

The simplest calculation arises by seeing what happens when we have no twin color, setting $\hat{g}_3 = 0$. The danger to naturalness is then that the SM QCD coupling will give $y_t(\mu)$ a different evolution to $\hat{y}_t(\mu)$ even if they happen to coincide at $\mu = \Lambda$, and that this deviation will feed into m_h^2 . To focus on just this effect we will drop the g_3 -independent terms in the y_t, \hat{y}_t β -functions. since these have identical forms for the twin and SM sectors. (Keeping these effects would be subleading in the running of m_h^2 compared to those of the g_3 -dependent term if we start with $y_t(\Lambda) \approx \hat{y}_t(\Lambda)$.) As a final simplifying approximation we will drop the running of g_3 itself, because its β -function is small near Λ and because we will see that the running in m_h^2 is dominated near Λ . With these approximations, and working to first order in $\hat{y}_t - y_t$, the solution to eqs. (4.1) is given by

$$m_h^2(\mu) \approx m_h^2(\Lambda) + \left[\frac{3y_t^2 g_3^2}{8\pi^4} + \frac{3(y_t^2 - \hat{y}_t^2)}{4\pi^2} \right] (\Lambda^2 - \mu^2) + \frac{3y_t^2 g_3^2}{4\pi^4} \mu^2 \ln(\mu/\Lambda). \quad (4.3)$$

Running down to low scales, $\mu \ll \Lambda$,

$$m_{h,\text{IR}}^2 \approx m_h^2(\Lambda) + \left[\frac{3y_t^2 g_3^2}{8\pi^4} + \frac{3(y_t^2 - \hat{y}_t^2)}{4\pi^2} \right] \Lambda^2. \quad (4.4)$$

In the above equations all the dimensionless couplings are evaluated at Λ .

We see that even if $y_t(\Lambda) = \hat{y}_t(\Lambda)$, just the running from SM QCD has led to a quadratic divergence which would require a fine tuning of the counter-term $m_h^2(\Lambda)$ to get the physical Higgs mass,

$$\text{Two loop fine tuning} \sim \frac{m_{h,\text{physical}}^2}{\frac{3y_t^2(\Lambda)g_3^2(\Lambda)}{8\pi^4}\Lambda^2} \approx 0.25. \quad (4.5)$$

Of course, it is not reasonable for two couplings, y_t, \hat{y}_t , that run differently to be exactly the same at Λ . This would be a fine tuning in itself. A technically natural estimate is that they differ by at least the running of y_t due to QCD over an e-folding of running,

$$|y_t(\Lambda) - \hat{y}_t(\Lambda)| \gtrsim \frac{g_3^2(\Lambda)}{2\pi^2} y_t(\Lambda). \quad (4.6)$$

In other words, we expect a comparable quadratic divergence in $m_{h,\text{IR}}^2$ from the splitting in Yukawa couplings and from the explicit $\mathcal{O}(g_3^2 y_t^2)$ divergence. Thus a better estimate of fine-tuning *in the absence of twin QCD* is $\lesssim 10$ percent.

The tuning due to QCD at two-loop order will clearly become very mild if we do include twin QCD with $\hat{g}_3(\Lambda) \approx g_3(\Lambda)$. The two couplings will run differently in the IR due to the different number of SM and twin generations, but quadratic sensitivity to Λ will be determined by the UV couplings. Roughly, eq. (4.4) is then replaced by

$$m_{h,\text{IR}}^2 \approx m_h^2(\Lambda) + \left[\frac{3y_t^2(\Lambda)(g_3^2(\Lambda) - \hat{g}_3^2(\Lambda))}{8\pi^4} + \frac{3(y_t^2(\Lambda) - \hat{y}_t^2(\Lambda))}{4\pi^2} \right] \Lambda^2. \quad (4.7)$$

Therefore, if $g_3(\Lambda)$ and $\hat{g}_3(\Lambda)$ agree to within even 15%, enforced by an approximate \mathbb{Z}_2 , the tuning in m_h^2 will be a mild $\sim 30\%$, comparable to that in eq. (3.14). This estimate combines the $\mathcal{O}(g_3^2 y_t^2)$ contribution from running and the threshold correction in eq. (4.6) in quadrature to reflect the unknown relative sign of the threshold correction. We will take this to be the case in what follows and study the effects of twin confinement from this twin QCD sector on the twin spectrum and phenomenology.

Finally, of course even g_3 and \hat{g}_3 run differently because the particle content of the *minimal* Twin sector differs from that of the SM, so one may wonder how close they can naturally be at Λ . However, the analogous estimate to eq. (4.6) is

$$\frac{|g_3(\Lambda) - \hat{g}_3(\Lambda)|}{g_3(\Lambda)} \gtrsim \frac{g_3^2(\Lambda)}{6\pi^2}, \quad (4.8)$$

which is easily consistent with the requirement of naturalness discussed above.

4.2 Fraternal confinement

We now determine the confinement scale $\hat{\Lambda}_3$ of the twin SU(3) gauge interaction, as this governs the infrared phenomenology of the twin sector.

If all fermions carrying twin SU(3) quantum numbers are much heavier than the confinement scale, the infrared physics is that of pure SU(3) gauge fields, and the lightest states in the confined twin sector will be glueballs, whose rich spectrum includes states with different angular momentum J , charge conjugation C and parity P . As shown in lattice studies of SU(3) pure glue [44, 45], at least a dozen glueballs are stable against decay to other glueballs, and the lightest, which we will refer to as G_{0+} , has $J^{PC} = 0^{++}$. Lattice data provides the ratios of these glueballs' masses to each other and to the confinement scale. To determine the physics of the twin sector thus only requires us to compute $\hat{\Lambda}_3$.

Once the twin b becomes sufficiently light that twin glueballs and twin bottomonium states (which we will refer to generically as “[$\hat{b}\hat{b}$]”) have comparable masses, the situation becomes more complex. We will not explore this regime carefully in this paper, leaving its details for future study. However, the calculation of $\hat{\Lambda}_3$ and of glueball masses given below still applies approximately.

The twin and SM SU(3) couplings are similar at the cutoff Λ , but the twin sector has fewer quark flavors, faster running (i.e. a more negative beta function), and therefore a modestly higher confinement scale. This is illustrated in figure 3, which shows the strong coupling scale $\hat{\Lambda}_3$ of twin QCD as a function of the variation δg_3 between SM and twin QCD couplings at the cutoff as well as the value of \hat{y}_b relative to y_b . Note that for $g_3 \approx \hat{g}_3$,

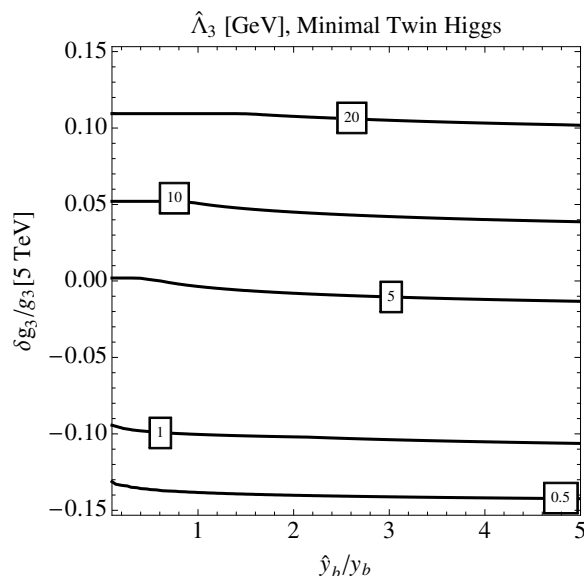


Figure 3. The confinement scale $\hat{\Lambda}_3$ of the twin SU(3) coupling given fractional variations in \hat{g}_3 and \hat{y}_b at the cutoff Λ for the minimal Twin Higgs (dependence on \hat{y}_t is negligible). Here we take $\Lambda = 10\hat{m}_t$ and $f = 3v$. The mild kinks are due to the \hat{b} threshold.

$\hat{\Lambda}_3$ is typically one to two orders of magnitude above that of QCD, with weak dependence on \hat{y}_b through its impact on the twin QCD beta function.⁵

We may now estimate the mass scale of twin glueballs. Using lattice estimates of the glueball mass spectrum in units of the inverse force radius [44, 45] and the zero-flavor SU(3) $\overline{\text{MS}}$ confinement scale in units of the inverse force radius [46], we find the mass m_0 of the G_{0+} glueball to be related to the strong coupling scale via $m_0 = 6.8\hat{\Lambda}_3^{\overline{\text{MS}}}$. The physical scale m_0 determined by running couplings down from the cutoff carries a combined uncertainty of $\mathcal{O}(10\%)$ from the lattice estimates, primarily due to uncertainty in the inverse force radius [46]. Given the mass of the G_{0+} , the masses of higher glueball excitations in terms of m_0 are known to good precision. The next highest states in the glueball spectrum are well separated from the G_{0+} , with the closest states being the G_{2+} , a 2^{++} glueball with $m_{2^{++}} \sim 1.4m_0$, and the G_{0-} , a 0^{-+} state with $m_{0^{-+}} \sim 1.5m_0$ [44, 45]. It appears also that there is a second stable 0^{++} glueball, the G'_{0+} , with $m \sim 1.8m_0$ [47]. The twin glueball spectrum is illustrated on the left-hand side of figure 4.

Meanwhile, the twin bottomonium states form a rich spectrum, whose lowest lying states are narrow if rapid decays via twin glueballs are inaccessible. As is familiar from SM quarkonium data, and as sketched on the right-hand side of figure 4, the spectrum includes towers of 0^{+-} , 1^{--} and j^{++} ($j = 0, 1, 2$) states, which by analogy we call $\hat{\eta}$, \hat{Y} and

⁵At two loops, we define the $\overline{\text{MS}}$ confinement scale $\hat{\Lambda}_3$ via

$$\frac{\hat{\Lambda}_3^{\overline{\text{MS}}}}{\mu} = \exp\left(-\frac{1}{2b_0\hat{g}_3^2(\mu)}\right) (b_0\hat{g}_3^2(\mu))^{-b_1/2b_0^2} \left(1 + \frac{b_1}{b_0}\hat{g}_3^2(\mu)\right)^{b_1/2b_0^2}, \quad (4.9)$$

where b_0, b_1 are the one-loop and two-loop twin QCD beta functions respectively, and $\hat{g}_3(\mu)$ is understood to be the $\overline{\text{MS}}$ coupling.

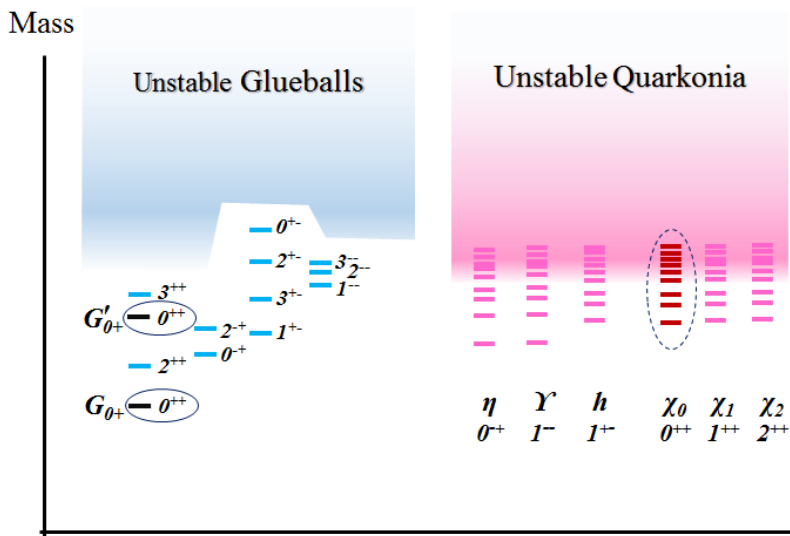


Figure 4. Sketch of the twin hadron spectrum in the regime where $m_0 < 2m_{\hat{b}} < 2m_0$. In addition to the G_{0+} , of mass m_0 , about a dozen other glueballs, with mass splittings of order m_0 , are stable against twin strong decays. Numerous twin bottomonium states, including a tower of 0^{++} states $\hat{\chi}$, are stable against twin strong decays. The circled G_{0+} and G'_{0+} glueballs, and potentially the $\hat{\chi}$ quarkonia, can dominantly decay via annihilation through an s -channel off-shell Higgs to the SM.

$\hat{\chi}_j$. The lowest-lying twin quarkonia states have masses of order $2m_{\hat{b}}$, with mass splittings $\ll 2m_{\hat{b}}$ (as long as $m_{\hat{b}} \gg \hat{\Lambda}_3$). However, since there are no other light twin quarks, there are no “open twin bottom” mesons analogous to the SM’s B_u, B_d mesons. Thus the towers of narrow quarkonium states extend much further up than in the SM, potentially up to a scale of order $2m_0$, as sketched in figure 4, or $m_0 + 2m_{\hat{b}}$.

The reader should note that figure 4 is only illustrative, and must be interpreted with caution. Its details change dramatically as one raises or lowers the quarkonium masses relative to the glueball masses, and it omits the many narrow higher-spin quarkonium states, along with various other phenomenological details.

5 Twin hadron phenomenology

Thus far we have seen that viable Fraternal Twin Higgs models include twin glue, with couplings that favor confinement roughly an order of magnitude or so larger than the SM QCD scale, producing relatively light twin glueballs and/or twin quarkonia. Both twin gluons and twin quarks are connected to the Standard Model via low-dimensional portals, and this can lead to observable and even spectacular twin hadron phenomenology. As in Folded Supersymmetry [4], where twin glueballs also arise, we thus find a connection between dark naturalness and twin hadrons. In our case, this connection manifests itself as new and exciting opportunities for discovery at the LHC.

The model’s phenomenology changes significantly as we move around in the parameter space, and in most regions it is rather complicated. But the most promising and dramatic LHC signals arise even in the conceptually simplest region, namely where $m_{\hat{b}} > \frac{1}{2}m_h$ (i.e.,



Figure 5. The parameter space of the model in terms of the masses of the lightest glueball G_{0+} and the lightest quarkonium $\hat{\eta}$. In region A, only glueballs are produced; in region B, the relevant quarkonia decay to glueballs; in region C, glueballs are either not produced or decay to quarkonia, so only quarkonia appear in the final state; and in region D there are both metastable glueballs and metastable quarkonia, with the potential for mixing. Solid lines indicate kinematic boundaries.

in figure 5, the part of region A above the dashed line). In this case the main phenomenon is that described in figure 1, with twin gluons produced in h decays and hadronizing into twin glueballs, including the G_{0+} . The G_{0+} lifetime is discussed in section 5.3, eqs. (5.4)–(5.6); the (perturbative) production rate for glueballs is discussed in section 5.5, eq. (5.10), with nonperturbative subtleties described in appendix B.1. The reader seeking to avoid becoming lost in details at a first reading may wish to focus merely on this simple scenario, in which case section 5.4, the later portions of section 5.5, and appendices A and B.2 may be omitted.

5.1 Kinematic regions

Before we begin, it is useful to parameterize the theory through m_0 and $m_{\hat{\eta}}$ (as well as f) in place of \hat{g}_3 , \hat{y}_b . Here $\hat{\eta}$ is the lightest $[\hat{b}\hat{b}]$ state, lying slightly below the lightest $\hat{\chi}$ state. We can then divide the parameter space of the model into four qualitatively different kinematic regions, shown in figure 5:

- Region A: $m_h > 2m_0$, $m_h < 2m_{\hat{\eta}}$ and $m_h < m_0 + m_{\hat{\eta}}$, so that h can decay to twin glueballs but not to twin bottomonium.

- Region B: $m_h > m_0 + m_{\hat{\eta}}$ and $m_{\hat{\eta}} > 2m_0$; here h can produce twin bottomonium, but all $\hat{\chi}$ states (and most or all other $[\hat{b}\hat{b}]$ states) decay eventually to twin glueballs.
- Region C: either $m_0 + m_{\hat{\eta}} > m_h > 2m_{\hat{\eta}}$, in which case only twin bottomonium can be produced in h decays, or $m_0 > 2m_{\hat{\eta}}$, so that any produced glueballs decay rapidly to twin bottomonium.⁶ Only bottomonia appear in the final states.
- Region D: $m_h > m_0 + m_{\hat{\eta}}$, $m_{\hat{\eta}} < 2m_0$, $m_0 > 2m_{\hat{\eta}}$; here both the lighter twin bottomonium and glueball states are metastable, and either or both may appear in final states. Mixing between the two classes of states can be important in this region.

As we will see, visible decays are typical, and displaced decays are possible, in regions A, B and D. They may or may not be absent (or very rare) in most or all of region C; this is model-dependent.

5.2 Couplings to the visible sector

In this model, the two portals of greatest importance will involve the dimension-five operator $A^\dagger A \hat{b}\hat{b}$ and the dimension-six operator $A^\dagger A \hat{G}_{\mu\nu} \hat{G}^{\mu\nu}$, where recall A is the SM-like Higgs doublet. After SM electroweak symmetry breaking and twin confinement, the first operator causes mixing between the SM-like Higgs and twin $\hat{\chi}$ quarkonia, while the second operator causes mixing between the SM-like Higgs and twin G_{0+} glueballs. The effective dimension-5 coupling $A^\dagger A \hat{b}\hat{b}$ originates from the twin bottom Yukawa $\hat{y}_b B \hat{Q} \hat{d}$; applying (3.8) gives the leading interaction

$$\mathcal{L}_5 = -\hat{y}_b \frac{A^\dagger A}{\sqrt{2}f} \hat{b}\hat{b}, \tag{5.1}$$

which after electroweak symmetry breaking yields $\mathcal{L} \supset -\frac{\hat{y}_b v}{\sqrt{2}f} h \hat{b}\hat{b}$. This is just the v/f -suppressed coupling of the SM-like Higgs to twin fermions, which gives rise to mixing between h and $\hat{\chi}$ quarkonia.⁷

While the value of the $h - \hat{\chi}$ mixing can vary depending on the (unknown) value of the twin bottom Yukawa, the $h - G_{0+}$ coupling is necessarily generated by the basic ingredients of the minimal Twin Higgs. In a manner entirely analogous to the Standard Model hgg coupling, loops of twin tops generate an effective coupling between the twin Higgs doublet B and twin gluons; after $SU(4)$ breaking and SM electroweak symmetry breaking, this leads to a coupling between twin glue and the SM-like Higgs. The effective coupling between the twin Higgs doublet B and twin glue takes the usual form

$$\mathcal{L}_6 = \frac{\hat{\alpha}_3}{12\pi} \hat{G}_{\mu\nu}^a \hat{G}_a^{\mu\nu} \ln \left(\frac{B^\dagger B}{f^2} \right), \tag{5.2}$$

⁶Not all of region C is physically meaningful. As m_0 rises, so does $\hat{\Lambda}_3$, and $m_{\hat{\eta}}$ always remains heavier than the confinement scale.

⁷No other portals are relevant for h decays. Below the heavy \hat{h} scale, and in the absence of a twin $U(1)$, there are no dimension-4 portals; however we do discuss the effect of these portals in section 6.3 and appendix E. A dimension-5 portal involving SM and twin neutrino mixing is not induced or required in our model and may easily be too small to have any measurable effect.

and applying (3.8) generates the corresponding coupling to $A^\dagger A$, which after electroweak symmetry breaking leads to

$$\mathcal{L} \supset -\frac{\hat{\alpha}_3 v h}{6\pi f} \hat{G}_{\mu\nu}^a \hat{G}_a^{\mu\nu}. \quad (5.3)$$

Here the couplings are largely fixed by naturalness considerations.

5.3 Glueball decay

Once produced, twin glueballs can decay into kinematically available final states. Assuming there are no light quarks in the twin sector, the only potentially available decays are into light Standard Model fermions via the (off-shell) SM-like Higgs h or into the twin lepton sector via the heavier Higgs \hat{h} or twin \hat{Z} . The decay $G_{0+} \rightarrow h^* \rightarrow YY$, where Y are light SM fields, provides a visible signal. This process was studied in [23] in the context of a similar Hidden Valley model [21], with a similar Higgs portal for decays of the glueballs, and with a production portal induced by “quirks” [15, 22]. The width for $G_{0+} \rightarrow YY$ is

$$\Gamma_{G_{0+} \rightarrow YY} = \left(\frac{\hat{\alpha}_3 v f_0}{6\pi f^2 (m_h^2 - m_0^2)} \right)^2 \Gamma_{h \rightarrow YY}^{\text{SM}}(m_0^2). \quad (5.4)$$

Here $\Gamma_{h \rightarrow YY}^{\text{SM}}(m_0^2)$ is the width of a SM-like Higgs of mass $m_h = m_0$ and f_0 is the G_{0+} decay constant; from the lattice we have $4\pi \hat{\alpha}_3 f_0 = 3.06 m_0^3$ [45]. This is the dominant decay mode of twin glueballs in the minimal model; decays into twin sector leptons are subleading, due to suppression factors of $(m_h/m_{\hat{h}})^4 (f/v)^2$ for decays via \hat{h} and by an extra $(v/f)^2$ mixing factor if via h .

Provided that the G_{0+} decays primarily into SM final states, we can determine its lifetime τ_0 in terms of m_0 and f . This exercise is particularly straightforward for glueballs much lighter than the massive Standard Model gauge bosons, for which the factor $\Gamma_{h \rightarrow YY}^{\text{SM}}(m_0^2)$ scales linearly with glueball mass because decays into longitudinally-coupled modes are doubly off-shell. Then in this regime we have simply

$$\Gamma \sim 1.1 \times 10^{-17} \text{ GeV} \times \left(\frac{m_0}{10 \text{ GeV}} \right)^7 \left(\frac{750 \text{ GeV}}{f} \right)^4, \quad (5.5)$$

valid for $2m_\tau \lesssim m_0 \lesssim m_W$. This corresponds to a decay length $c\tau_0$ of approximately

$$c\tau_0 \sim 18 \text{ m} \times \left(\frac{10 \text{ GeV}}{m_0} \right)^7 \left(\frac{f}{750 \text{ GeV}} \right)^4. \quad (5.6)$$

Note $m_0 \sim 10\text{--}50 \text{ GeV}$ is a central range of values for the glueball mass, given (a) the relative factor of ~ 7 relating $\hat{\Lambda}_3$ to m_0 and (b) the higher confinement scale of twin QCD given a reduced number of twin sector fermions, see figure 3. This is a tantalizing result from an experimental perspective; it implies that the twin sector glueballs give rise to displaced decays on the length scale of the LHC detectors. Even for average decay lengths greater than the scale of the detectors, the large number of h bosons produced at the LHC means that an appreciable number of distinctive displaced decays can still occur within the detector. These decays involve a mix of final states with relative rates corresponding to the

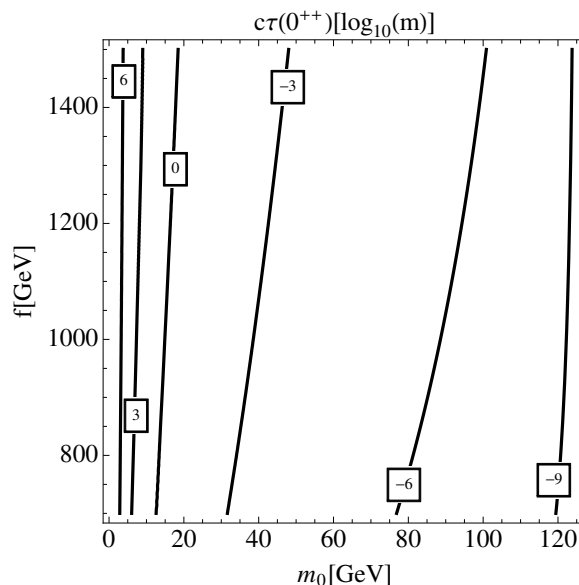


Figure 6. Decay length $c\tau_0$ of the G_{0+} state in \log_{10} (meters) as a function of m_0 and f .

decay of an SM-like Higgs of mass $m_h = m_0$ — primarily bottom quarks, if kinematically accessible, as well as tau pairs and gluons.

We can improve upon the above parametrics by computing the SM Higgs width as a function of mass using `HDECAY` [48]. A precise plot of the decay length $c\tau_0$ as a function of m_0 and f is then shown in figure 6. As we can see, the decay length consistent with naturalness in the minimal model is typically in the range of millimeters to meters, with a jump toward the kilometer scale for $m_0 < 2m_b$.

Note, however, that given the strong dependence of the glueball decay length on the glueball mass, $c\tau_0 \propto m_0^7$, even modest uncertainties in the value of m_0 may substantially influence this estimate. For example, the $\mathcal{O}(10\%)$ uncertainty on the value of $m_{G_{0+}}$ inferred from lattice data translates into a factor of two variation in the value of $c\tau_0$.

The second 0^{++} glueball G'_{0+} decays similarly to the first, with a shorter lifetime, and may have prompt or displaced decays. Others such as the 2^{++} may decay via an off-shell Higgs, e.g. $G_{2+} \rightarrow G_{0+}h^*$. At small masses their lifetimes are very long [23], and they will appear only as missing energy in h decays. At larger m_0 they cannot appear in h decays, though they might possibly appear as displaced vertices in decays of the heavy twin particles \hat{Z} or \hat{h} .

The above calculations apply in regions A and B but are irrelevant in region C, where instead $G_{0+} \rightarrow [\hat{b}\hat{b}][\hat{b}\hat{b}]$. They are only part of the story in region D due to glueball-quarkonium mixing, which we briefly address at the end of section 5.4.

5.4 Bottomonium decay

The twin bottomonium states shown in figure 4 resemble the SM’s towers of charmonium/bottomonium states, yet have unfamiliar decay modes. We relegate most details to appendix A, but summarize key points here. Like the G_{0+} , the $\hat{\chi}$ states can potentially

decay via annihilation to SM states through an s -channel Higgs. However, if twin neutrinos (and/or taus) are light, they can also decay to spin-one \hat{Y} states by twin weak interactions, $\hat{\chi} \rightarrow \hat{Y}\hat{\ell}\hat{\ell}$, where $\ell = \nu, \tau$. If allowed, this decay competes with the decay via the Higgs, and the competition is very sensitive to modeling of the $[\hat{b}\hat{b}]$ states.

We can use non-relativistic quantum mechanics to give a rough leading-order estimate of the width of the $\hat{\chi}$ state to the SM:

$$\Gamma_{\hat{\chi} \rightarrow YY} = \frac{27}{4\pi} |R'(0)|^2 \left(\frac{v}{f}\right)^2 \frac{\hat{y}_b^2}{(m_h^2 - m_{\hat{\chi}}^2)^2} \Gamma_{h \rightarrow YY}^{\text{SM}}(m_{\hat{\chi}}^2), \quad (5.7)$$

where $R(r)$ is the state's radial wave function. Here $R'(0)$ appears because $\hat{\chi}$ is a p-wave state. As justified in appendix A, we take the approximation of a linear confining potential (with slope $\sigma \approx 4\hat{\Lambda}_3^2$, following calculations of [44, 49]) as a starting point, ignoring the Coulomb potential and important relativistic corrections. Our estimate is

$$\Gamma_{\hat{\chi} \rightarrow YY} \sim 2 \times 10^{-3} \left(\frac{v}{f}\right)^4 \frac{m_{\hat{\chi}}^{11/3} m_0^{10/3}}{v^2 m_h (m_h^2 - m_{\hat{\chi}}^2)^2} \Gamma_{h \rightarrow YY}(m_h) \quad (5.8)$$

for the lowest $\hat{\chi}$ state.

Meanwhile the twin weak decay to $\hat{Y}\hat{\ell}\hat{\ell}$ proceeds via an off-shell \hat{Z} , through a dipole transition (analogous to $\chi_b \rightarrow \Upsilon\gamma$ in the SM). Assuming twin neutrinos are massless we roughly estimate

$$\Gamma_{\hat{\chi} \rightarrow \hat{Y}\hat{\nu}\hat{\nu}} \sim \frac{\hat{\alpha}_2^2 (m_{\hat{\chi}} - m_{\hat{Y}})^7}{4\pi (m_{\hat{b}}\beta)^2 m_{\hat{Z}}^4}, \quad (5.9)$$

where β is the typical velocity of the \hat{b} in this state. The extreme dependence of this width on the $\hat{\chi} - \hat{Y}$ mass difference makes any estimate of lifetime and branching fraction highly uncertain.

Using these formulas as a guide, however, we can qualitatively summarize $\hat{\chi}$ phenomenology in regions C and D:

- If twin neutrinos and taus are not light, then one or more low-lying $\hat{\chi}$ states may decay promptly at high mass and displaced at low mass. An approximate formula for the lifetime is given in eq. (A.3).
- If twin neutrinos and/or taus are light, then
 - In region C, twin weak decays dominate, making all $\hat{\chi}$ decays invisible.
 - In region D, the lowest-lying $\hat{\chi}$ state may decay visibly with a substantial branching fraction, especially for $m_{\hat{\chi}} > m_0$.
 - Also in D, the lowest-lying $\hat{\chi}$ decays may be displaced for $m_{\hat{\chi}} > m_0$ and $m_{\hat{\chi}} < 30 \text{ GeV}$ or so.

Recall also that in region D there can be mixing of 0^{++} glueballs and quarkonia. This effect is probably of greatest importance for $m_0 > m_{\hat{\chi}}$, where G_{0+} is nested within the $\hat{\chi}$ tower. For $m_0 \sim m_{\hat{\chi}}$ the quarkonia widths tend to be larger, so the mixed states tend to inherit their properties, with lifetimes somewhat shorter than in figure 6 and the potential for significant invisible decay fractions.

5.5 Twin hadron production

We now discuss twin hadron production via h decays.⁸ Twin hadronization is complicated and quite different from SM QCD, so it is not possible to make reliable estimates as to what fractions of twin glueballs and bottomonia produced are the golden 0^{++} states that we can hope to observe. But the overall rate for $h \rightarrow$ twin hadrons, which occurs through $h \rightarrow \hat{g}\hat{g}$ (if $m_0 < m_h/2$) and through $h \rightarrow \hat{b}\hat{b}$ (if $m_{\hat{b}} \lesssim m_h/2$), can be estimated, at least roughly.

We begin with a perturbative analysis of h decays to the twin sector; non-perturbative effects, which can qualitatively change the story, will be discussed later. We will refer to the $h \rightarrow \hat{g}\hat{g}$ production of glueballs (as shown in section 1, figure 1) as the “irreducible process”, since, proceeding via the interaction (5.3), it is independent of $m_{\hat{b}}$ to a first approximation. It is the only relevant process for $m_{\hat{b}} > m_h/2$, and also dominates for $\hat{y}_b \lesssim 0.13y_b$. The partial width for the irreducible process follows from (5.3),

$$\Gamma(h \rightarrow \hat{g}\hat{g}) \simeq \left(\frac{\hat{\alpha}_3 v^2}{\alpha_3 f^2} \right)^2 \Gamma(h \rightarrow gg), \quad (5.10)$$

leading to a perturbative expectation for the branching ratio of the Higgs to twin glueballs of the order 0.1% for $f = 3v$.

Similarly the decay $h \rightarrow \hat{b}\hat{b}$ can generate $[\hat{b}\hat{b}]$ states in regions B, C and D, and also glueball states which may be produced immediately along with the $[\hat{b}\hat{b}]$ (e.g. $h \rightarrow \hat{\chi}G_{0+}$), or, if kinematically allowed, in radiative decays ($[\hat{b}\hat{b}] \rightarrow [\hat{b}\hat{b}]' + \text{glueball}$) or via $\hat{b}\hat{b}$ annihilation ($[\hat{b}\hat{b}] \rightarrow \text{glueballs}$). In region A, $[\hat{b}\hat{b}]$ states are inaccessible, but still this process can give non-perturbative enhancement to twin glueball production.

At $f \sim 3v$ the perturbative $h \rightarrow \hat{b}\hat{b}$ width equals the irreducible width for $\hat{y}_b \sim 0.13y_b$ and grows as \hat{y}_b^2 , enhancing the irreducible rate by about $\sim 60(\hat{y}_b/y_b)^2$. This branching fraction becomes so large that the perturbative $h \rightarrow \hat{b}\hat{b}$ rate would be inconsistent with current Higgs measurements for $\hat{y}_b \gtrsim 1.25y_b$ (at least for $f \sim 3v$; larger values of \hat{y}_b are allowed as f increases, as we will discuss further in section 6.4) — unless of course $m_{\hat{b}} > m_h/2$, in which case only the irreducible process remains.

In sum, within perturbation theory,

- The high $m_{\hat{b}}$ region — the upper portion of region A, where only glueballs are kinematically allowed — manifests only the irreducible process, with $\text{Br}(h \rightarrow \text{twin glueballs}) \sim 0.1\%$ for $f \sim 3v$, and decreasing like f^{-4} .
- The low $m_{\hat{b}}$ region, including low-mass portions of regions B, C and D, has a substantial $h \rightarrow \hat{b}\hat{b}$ rate, with branching fraction increasing to $\sim 10\%$ near $m_{\hat{b}} \sim 15 \text{ GeV}$ (for $f \sim 3v$).
- Between these two regions the model is ruled out *if we rely on perturbation theory*. However, as we will immediately see, these perturbative considerations are not always applicable.

⁸Twin hadron production via the heavy \hat{h} is discussed in section 6.3.

As in SM QCD, where $e^+e^- \rightarrow$ hadrons is strongly modulated by resonances and other non-perturbative effects below a couple of GeV, non-perturbative effects are potentially substantial in h decays when kinematics restricts the number and types of hadrons that can be produced thereby. We discuss this in some detail in appendix B, but here we just summarize our most important observations.

- At moderate to large m_0 , higher 0^{++} glueball resonances (and gaps between them) can enhance (and suppress) the irreducible rate. A very conservative estimate is that, in the relevant kinematic regime, the suppression can be no worse than 1/10, and is likely less severe. Thus the irreducible rate is at least 10^{-4} , and usually larger, throughout the parameter space.
- At moderate to large $m_{\hat{b}}$, similar enhancement and reduction may occur from excited $\hat{\chi}$ states. If m_h lies between two narrow $\hat{\chi}$ resonances, then there can be substantial reduction relative to the perturbative $h \rightarrow \hat{b}\hat{\bar{b}}$ prediction. As we discuss in a preliminary fashion in appendix B, it appears that wherever we can calculate $\hat{\chi}$ widths and mass-splittings with order-one confidence — relatively large $m_{\hat{b}}$ and relatively small m_0 — the suppression between resonances is always enough to invalidate the perturbative exclusion. At larger m_0 (for fixed $m_{\hat{\chi}}$) the widths tend to be even narrower, the splittings larger, and the suppression somewhat greater, though not calculable with current methods. Due to this non-perturbative suppression, we are confident this model is not universally excluded when $m_{\hat{b}}$ lies near and somewhat below $m_h/2$. In fact we believe, for various reasons, that the model is still allowed in quite far into the lower $m_{\hat{b}}$ portion of region A, and probably also survives in an upper portion (as well as the lower portion) of region D, but much more work is needed to put this suspicion on a solid footing.

In summary, we expect the branching fraction for $h \rightarrow$ twin hadrons to be at least 10^{-4} and, in most of parameter space, much larger. Final states may include various combinations of twin glueballs and bottomonium. Although the rates for production of individual types of hadrons cannot be calculated, we expect a substantial fraction of the twin glueballs (and perhaps bottomonia) to be G_{0+} and $\hat{\chi}$ states that can decay, possibly displaced, by mixing with the Higgs. While $1.25m_b(f/v) \lesssim m_{\hat{b}} < m_h/2$ is excluded *within perturbation theory* by existing measurements of the Higgs, this part of parameter space is likely a patchwork of excluded and allowed regions, whose details we cannot calculate without full non-perturbative information. In the allowed regions, the twin hadron production rate is always substantially enhanced beyond the irreducible rate.

A qualitative summary of the phenomenology in the various regions is given in figure 7. We have conservatively assumed that twin weak decays of bottomonium are kinematically allowed, making decays in region C invisible, and making $\hat{\chi}$ visible only in some limited portion of region D; if instead the twin weak decays are forbidden, $\hat{\chi}$ decays are visible throughout C and D and displaced at low mass (see appendix A). In the next section we explore these and other signals more carefully.

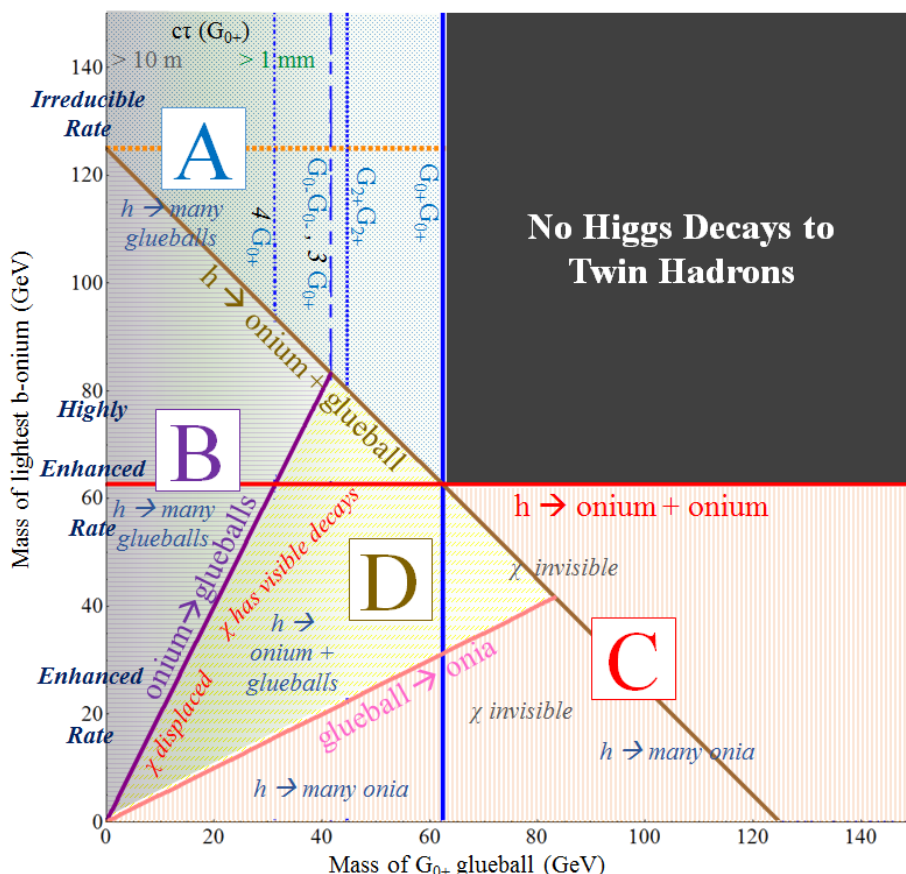


Figure 7. A qualitative overview of the phenomenology, for $f = 3v$, in the various regions of parameter space; see figure 5. Details are explained in subsequent sections. Solid lines indicate kinematic boundaries. Common final states are indicated in italics. At low glueball mass, decays of the G_{0+} are displaced; see figure 6. Here it is assumed that there are light twin leptons, so one $\hat{\chi}$ state is visible, and even displaced, only in small regions; otherwise $\hat{\chi}$ decays visibly throughout regions C and D, and is displaced at low mass.

6 LHC phenomenology

By far the most spectacular signal that can arise from our minimal Twin Higgs model is the displaced decays of twin glueballs and quarkonia. We describe the phenomenology of this signal, as it arises from h decays, in section 6.1; further details on search methods are given in appendix C. If no displaced decays are observable, h decay signals may be challenging for LHC but certainly accessible at a future e^+e^- collider (section 6.2). A brief discussion of how a twin hypercharge U(1) would affect the phenomenology is given in appendix E. Section 6.3 covers signals from a heavier Higgs \hat{h} . Finally, section 6.4, explores the order- $(v/f)^2$ effects on SM Higgs production rates.

6.1 New Higgs decays with displaced vertices

The branching fraction $\text{Br}(h \rightarrow \text{twin hadrons}) > 10^{-4}$ everywhere that it is not kinematically forbidden. Because the number of Higgs bosons produced at LHC in Run II will be

of order 10^7 , and because displaced vertices are spectacular signals when identified, these numbers represent a very promising opportunity. Already hundreds or thousands of events with displaced vertices may have been produced, though in many parts of parameter space they would clearly have evaded existing LHC Run I searches [27–29, 50, 51].

As figure 7 suggests, the model exhibits a great diversity of displaced vertex phenomenology. Rather than address the full story here, we mainly discuss the regions with the simplest phenomenology. These regions, it turns out, produce most of the possible Higgs decay signatures, and are therefore sufficient to motivate the most important searches, which are sensitive to effects in more complicated regions that we will not discuss in detail.

The simplest region is the portion of region A with $m_{\tilde{b}} > m_h/2$, where the irreducible rate applies and only glueballs can be produced. As we move across this region from large to small m_0 , taking $f \sim 3v$, we find the following twin hadron phenomena:

- For $m_0 \gtrsim 40$ GeV, $h \rightarrow G_{0+}G_{0+}$ dominates and G_{0+} decays are prompt.
- For 10 GeV $\lesssim m_0 \lesssim 40$ GeV, the G_{0+} decays are displaced; decays to other glueballs, and to higher multiplicities of glueballs, become more common for smaller m_0 . The decay $h \rightarrow G_{0+}G'_{0+}$ is of particular note, since the G'_{0+} decays visibly.
- Below about 10 GeV the G_{0+} lifetime is so large that decays in the detector are rare. This is partly compensated by higher glueball multiplicity per event.

Consider next small $m_{\tilde{b}} \lesssim 15$ GeV. In region B, where m_0 is small, the irreducible process produces the same phenomena as in region A, but $h \rightarrow \tilde{b}\tilde{b}$ enhances the rate for twin hadron production, leading (via bottomonium decay to glueballs) to ≥ 3 twin glueballs per event. In the low- $m_{\tilde{b}}$ portion of region C, the glueballs instead decay to bottomonium, leading to states that may all be invisible; alternatively (see section 5.4) final states may include prompt or displaced $\hat{\chi}$ decays. In region D, where mixing may be important, and where $\hat{\chi} \rightarrow \text{SM}$ has a larger branching fraction, an even richer set of final states is possible.

With all of these different subregions with different phenomenological details, many of which cannot be calculated, one may rightly worry that experimental coverage of this model, and others like it, will be extremely difficult. However, it is possible to bring the challenges under some control by focusing on simple search strategies that cover multiple regions. For the displaced decays, just a few strategies are potentially sufficient.

1. Search(es) for single vertex production, $h \rightarrow G_{0+} + \dots$, perhaps separated into
 - (a) $h \rightarrow G_{0+} + \cancel{E}_T$ where the \cancel{E}_T is due to twin hadrons that decay invisibly and/or outside the detector.
 - (b) $h \rightarrow G_{0+} + \text{jet}(s)$ where a promptly decaying twin hadron produces the jet(s).

This type of search may only be feasible when requiring the presence of associated objects that may accompany the h , such as a lepton or a pair of vector boson fusion (VBF) jets.

2. Search for exclusive di-vertex production production: as in $h \rightarrow G_{0+}G_{0+}$.

3. Search for inclusive di-vertex production: $h \rightarrow \geq 3$ twin hadrons, of which at least two decay visibly and displaced.

In contrast to exclusive di-vertex production, here the pair of observed twin hadrons generally have invariant mass *below* m_h , and need not be back-to-back in the h rest frame.

To a limited degree, each of the three search strategies has been explored by ATLAS [27, 28, 50, 52–55], CMS [29, 56–58] and/or LHCb [51]. However, due often to trigger limitations or analysis gaps, even the most sensitive of these searches do not yet put significant bounds on this model, and a broader and deeper program of searches is needed in Run II. We will discuss these issues further in appendix C.

We note also that although our minimal model has specific relationships between masses, lifetimes and production mechanisms, these relationships will not necessarily hold in other Twin Higgs and Twin Higgs-like models. It is therefore preferable that the above searches be carried out with the masses and lifetimes of the long-lived particles, and characteristics of the \cancel{E}_T (if any), treated as free parameters. In appendix C we suggest benchmark models for these searches and consider some important triggering and analysis issues.

6.2 New Higgs decays without displaced vertices

When the G_{0+} is heavy, its decays are prompt. Prompt non-SM decays of the Higgs such as $h \rightarrow G_{0+}G_{0+} \rightarrow (b\bar{b})(b\bar{b}), (b\bar{b})(\mu^+\mu^-)$, or $h \rightarrow G_{0+} + \cancel{E}_T \rightarrow (b\bar{b}) + \cancel{E}_T, (\tau^+\tau^-) + \cancel{E}_T, (\mu^+\mu^-) + \cancel{E}_T$, etc., were examined in a recent overview of non-SM Higgs decays [59]. Not all cases have yet been investigated for a 13–14 TeV machine, but it appears that a non-SM branching fraction of order 10^{-3} is far too small for discovery of such modes at LHC, though perhaps an e^+e^- machine producing at least 10^5 Higgs bosons could find it. However, enhancement of the twin hadron branching fraction to $\sim 10\%$, through $h \rightarrow \hat{b}\hat{b}$ or non-perturbative effects, as discussed in section 5.5, could bring these processes within reach of the LHC.

At the other extreme, one can discuss completely invisible decays. These can dominate in region C, and can become important in regions A and B if the G_{0+} has an extremely long lifetime, or in region D if the G_{0+} mixes substantially with invisible $\hat{\chi}$ states. Other twists on the model (such as the presence of a massless twin hypercharge boson with small kinetic mixing, see appendix E) can cause all twin hadrons to decay to invisible hidden particles. Detecting an invisible decay rate much smaller than 10% is very difficult at the LHC, and thus can only be done if there is significant enhancement by the $h \rightarrow \hat{b}\hat{b}$ process. Again, an e^+e^- collider would do much better.

6.3 Heavy Higgs decays

Not only the h but also the heavy twin Higgs \hat{h} may serve as a portal, if the twin SU(2) is linearly realized. The existence of a second perturbative Higgs, while not guaranteed, is favored by precision electroweak data [60]. If present it provides additional opportunities to uncover the twin mechanism. The mass of this second Higgs is $\sim \sqrt{2\lambda}f$, and so typically lies around the TeV scale. It possesses a v/f -suppressed coupling to top quarks and thus

is produced through gluon fusion, albeit with a $(v/f)^2$ -suppressed cross-section compared to an SM Higgs of equivalent mass — falling at $\sqrt{s} = 14$ TeV from 1000 fb at a mass of 300 GeV to 10 fb for a mass of 1 TeV.

On the lower end of this mass range, decays into WW , ZZ , and hh dominate, with branching ratios roughly proportional to $2 : 1 : 1$. Once $\hat{h} \rightarrow \hat{W}\hat{W}, \hat{Z}\hat{Z}$ is kinematically allowed, these processes become at most comparable to WW , ZZ , and hh ; although couplings to the SM bosons are suppressed by v/f due to mixing, the longitudinal coupling scales as m_h^3/v^2 and entirely compensates. This is inevitable, since in the Twin Higgs mechanism the h and longitudinal W , Z , \hat{W} , \hat{Z} are all Goldstone modes under the same symmetry breaking.

The decays $\hat{h} \rightarrow hh, ZZ$ are common in many BSM models, and searches for these promising signals are already underway [61–64]. The \hat{h} will appear as a resonance with width suppressed by $(v/f)^2$ compared to a SM Higgs of the same mass, times $\frac{4}{3} (\frac{7}{3})$ to account for the channel $\hat{h} \rightarrow hh$ (and channels $\hat{h} \rightarrow \hat{W}\hat{W}, \hat{Z}\hat{Z}$, if kinematically allowed). Observation of this resonance at equal rates in $\hat{h} \rightarrow ZZ$ and $\hat{h} \rightarrow hh$, and measurement of its width, could therefore allow for a test of the model. In Run II, CMS expects to exclude $\sigma \times \text{Br}(pp \rightarrow \hat{h} \rightarrow ZZ) \gtrsim 10(4)$ fb for a heavy Higgs of 500 GeV (1 TeV) with 3000 fb^{-1} at $\sqrt{s} = 14$ TeV, or to discover $\sigma \times \text{Br}(pp \rightarrow \hat{h} \rightarrow ZZ) \gtrsim 30(10)$ fb at 5σ [65]. This corresponds to an exclusion reach of 900 GeV or a discovery reach of 750 GeV for a \hat{h} with $f = 3v$.

The \hat{h} may also give rise to twin hadrons, either via $\hat{h} \rightarrow \hat{t}\hat{t}$ (followed by $\hat{t} \rightarrow \hat{b}\tau\nu$) or $\hat{h} \rightarrow \hat{Z}\hat{Z}$ (with $\hat{Z} \rightarrow \hat{b}\hat{b}$). Although the rate is less than the perturbative irreducible rate for $h \rightarrow$ twin hadrons, it can easily happen that the trigger efficiency for h decays is low while that for \hat{h} decays is high, so that \hat{h} decays may provide an easier signal. Moreover the rate to produce twin hadrons via $\hat{Z} \rightarrow \hat{b}\hat{b}$ is larger by a factor of 10 or more than $\hat{h} \rightarrow ZZ \rightarrow \ell^+\ell^-\ell^+\ell^-$ and $\hat{h} \rightarrow hh \rightarrow b\bar{b}\gamma\gamma$, the cleanest $\hat{h} \rightarrow$ SM processes. Decays of \hat{h} may often produce displaced glueballs, including ones too heavy to appear in h decays and decaying via an off-shell h [21, 23]. Even if all twin hadron decays are prompt, the events might be observable at LHC if the rate, multiplicity, and total (or missing) energy are sufficient [20, 66].

On the other hand, if the twin SU(2) is non-linearly realized and the \hat{h} is as indistinct as the σ of QCD, then twin hadrons can be produced, albeit with small LHC rates, through enhancements of $gg \rightarrow \hat{Z}\hat{Z}$ and VBF production of \hat{Z} pairs.

6.4 Precision Higgs measurements

Here we consider the role of the canonical signature of the Twin Higgs [1], namely $\mathcal{O}(v^2/f^2)$ changes in Higgs couplings due to the misalignment between the electroweak vacuum expectation value and the pseudo-Goldstone Higgs. This leads to a suppression of all Higgs couplings by an amount $1 - \frac{v^2}{2f^2}$ relative to Standard Model predictions. There may also be a shift in branching ratios due to the additional partial width of decays into the twin sector, but as we have seen this can be much less than 10%. Assuming that $\text{Br}(h \rightarrow \text{twin sector}) \ll 10\%$, then the sole effect of the twin sector on SM Higgs measurements is a reduction in all production rates, relative to SM predictions, by a factor of

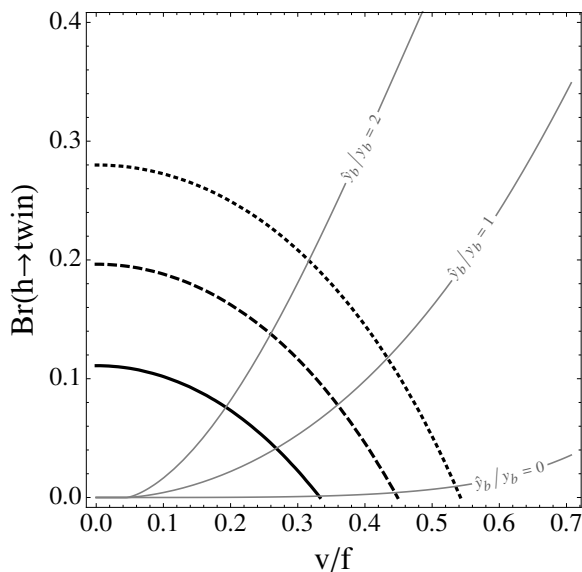


Figure 8. Current bounds on v/f and the Higgs branching ratio into the twin sector from a combined fit to Higgs coupling measurements. Solid, dashed, and dotted black lines denote the 1-, 2-, and 3- σ bounds (defined as $\Delta\chi^2 = 2.30, 6.18, 11.83$) due to ATLAS and CMS Higgs coupling measurements. The grey lines correspond to the perturbative calculation of the Higgs branching ratio into the twin sector as a function of v/f for $\hat{y}_b/y_b = 0, 1, 2$; as discussed in the text, the actual branching ratio may differ significantly from the perturbative result for a given value of \hat{y}_b .

$1 - \frac{v^2}{f^2}$. To evaluate the impact of current Higgs coupling measurements on v/f , we have performed a combined fit of the most recent ATLAS and CMS Higgs measurements [67–75] using the profile likelihood method [76]. The resulting bounds on v/f are shown in figure 8 as a function of v/f and the Higgs branching ratio into the twin sector.⁹ We also show contours corresponding to the perturbative calculation of $\text{Br}(h \rightarrow \text{twin sector})$ as a function of v/f for $\hat{y}_b/y_b = 0, 1, 2$. As discussed in appendix B, the complications of bottomonium production suggest that the actual branching ratio is potentially much smaller than the perturbative value for sufficiently large \hat{y}_b/y_b , while the irreducible rate for glueball production applies for $\hat{y}_b/y_b = 0$. Current measurements of Higgs couplings place a bound on v/f consistent with the benchmark value $f = 3v$ considered here.

For $f \sim 3v$ the shift may be detected definitively before the end of the LHC, but not soon — certainly not within Run II. Future projections are a somewhat delicate matter, as measurements in certain channels will become systematics-limited and naive combinations neglecting correlated systematics are no longer appropriate. However, the collaborations quote appropriate coupling projections taking these effects into account. For example,

⁹This fit does not include implicit precision electroweak bounds from infrared contributions to S and T . However, as we will discuss more in appendix D, in contrast to composite Higgs models where the infrared contribution is cut off by $m_\rho \sim \text{few TeV}$ and provides the strongest constraint on coupling deviations [60], here the infrared contribution is cut off by the mass of the heavy Higgs. For $m_{\hat{h}} \lesssim \text{TeV}$ these corrections to S and T are comfortably compatible with current precision electroweak bounds and do not strongly influence the coupling fit.

ATLAS projects sensitivity to a uniform scaling factor κ of 3.2% (2.5%) assuming current (no) theory systematics with 300 fb^{-1} [77], which corresponds to a 95% CL bound of $v/f \lesssim 0.35$ (0.31) assuming the invisible branching ratio gives a sub-leading correction to the observed Higgs couplings. The remaining high-luminosity run should improve sensitivity to 2.5% (1.6%) assuming current (no) theory systematics with 3000 fb^{-1} [77], leading to bounds of $v/f \lesssim 0.31$ (0.25). It is therefore unlikely that Higgs coupling measurements at the LHC could be used to substantially constrain the parameter space of Twin Higgs models, though if the twin mechanism is operative it may lead to $1-2\sigma$ deviations by the end of the high-luminosity run. (Direct limits on invisible decays are likely to fare even worse, with realistic projections suggesting 95% CL bounds will approach 8% with 3000 fb^{-1} [77], well short of the typical rate for decays into the hidden sector.)

In any case, an overall coupling reduction is purely a sign of mixing and is non-diagnostic; while observation of this reduction would be revolutionary, no unique interpretation could be assigned to it. Only discovery of the twin hadrons and/or discovery and study of the mostly-twin heavy Higgs would allow for a clear interpretation of such a measurement.

7 Conclusions

The “Twin Higgs” mechanism provides an existence proof for the unsettling possibility that the solution to the hierarchy problem involves a sector of particles that carry no Standard Model quantum numbers, and are therefore difficult to produce at the LHC. The existence of dark matter already motivates us to consider hidden sectors, and it is important that the possibility of hidden naturalness be thoroughly considered.

Fortunately, hidden sectors are often not as hidden as they first appear. As we have seen, a Fraternal Twin Higgs model, one whose hidden sector is not a precise twin of the Standard Model, but which contains the minimal ingredients for the theory to address the hierarchy, naturally leads to Hidden Valley phenomenology. Specifically, the Higgs sector requires a twin top, which in turn favors twin color; and the lack of light twin quarks in this minimal model then leads to confinement and twin hadrons that include twin glueballs, the lightest of which necessarily mixes with the Standard Model-like Higgs, and twin quarkonium, whose tower of 0^{++} states has analogous mixing with the Higgs. We have shown that the resulting mixing can often cause these glueballs, and in some cases the lightest quarkonium states, to decay on an observable timescale, leading to a new source of visible non-Standard-Model Higgs decays. The branching fraction for these decays is at worst 10^{-4} , typically at least 10^{-3} , and possibly as large as allowed by Higgs measurements. For heavier twin hadrons with prompt decays, the visible final states — four heavy-flavor fermions, or two heavy-flavor fermions plus missing energy — are among those summarized in a recent overview of non-SM Higgs decays [59]. Searches for these final states and for invisible decays at LHC are possible if the branching fractions approach 10%; if much smaller, a lepton collider may be needed. But for moderately light glueballs (and perhaps quarkonia), these decays can produce a potentially spectacular signal of one or more highly displaced vertices, often accompanied by moderate amounts of missing energy

from other twin hadrons that escape the detector. While several experimental searches for similar vertices have already taken place, a wider array of more powerful search strategies is required if the parameter space for this model is to be fully covered.

The minimal Twin Higgs model we have presented is only mildly tuned, and no more unnatural than bottom-up modeling of Higgs compositeness or (natural) supersymmetry. This model also has no obvious cosmological problems, flavor problems, or other glaring issues. Thus we see no reason from the bottom up, given present knowledge, to treat Twin Higgs as less motivated than, say, composite Higgs models. Meanwhile, in addition to its cousin Folded Supersymmetry, the Twin Higgs model has recently been generalized, by recognizing it as an orbifold model [38, 39]. Variants of these generalized models, by their very construction, share features with our minimal model, though they are different in details. This shows that the model space of sibling Higgses has not yet been fully explored, and should provide additional motivation for considering seriously and more generally the possibility of a hidden-sector solution to naturalness.

On general grounds, we expect anything vaguely resembling a Twin Higgs model with a hidden sector to require, as part of its solution to the naturalness problem, Higgs mixing via a “portal”-type interaction. This feature easily leads to additional Higgs-like resonances, new sources of missing energy, and exotic phenomenology of hidden-valley type, including non-SM Higgs decays to multi-body final states and/or displaced vertices. The challenges are that no individual model is required to produce any or all of these signals, and that production rates for these phenomena are not determined by known interactions (in contrast to gluino or stop production) and can be small. Among the most motivated places to search for new signals are in decays of known particles, whose production rates are known and large. New decays of the Higgs may not even be rare. In non-minimal models there may also be opportunities in rare decays of the Z . Searches for new phenomena generated by rarely produced heavy particles (such as the heavy Higgs in our model) must also be considered.

Our field has tended to assume that the solution to the hierarchy problem lies in particles that resemble the ones that we know. While hidden sectors are often found in string theory vacua and required in models of supersymmetry breaking, their role has been limited to higher energy or purely gravitational interactions, leaving them, as far as the LHC is concerned, out of sight and out of mind. But with the possible scale of supersymmetry receding upwards, and with no sign of Higgs compositeness or of the colored top partners that were widely expected, the possibility of something more radical, such as a hidden sector around the weak scale that communicates with our sector through a portal, cannot be ignored. Our searches must move beyond the easier and more obvious lampposts, for the secrets of nature may lie hidden in the dark.

Acknowledgments

We thank Christopher Brust, Zackaria Chacko, Patrick Draper, Roni Harnik, Simon Knapen, Pietro Longhi, Colin Morningstar, and Agostino Patella for useful conversations. The work of M.J.S. was also supported by NSF grant PHY-1358729 and DOE grant DE-

SC003916. R.S. was supported by NSF grant PHY-1315155 and by the Maryland Center for Fundamental Physics.

A Quarkonium mass spectrum and decays

A.1 Spectrum of the quarkonium states

As explained in section 4.2, the most phenomenologically interesting quarkonium states are the tower of 0^{++} states $\hat{\chi}$, which can mix with the SM-like Higgs h and potentially decay back to the SM. We can make a crude but useful analysis of these states assuming they are governed by non-relativistic quantum mechanics; this approximation holds for low-lying $\hat{\chi}$ states in the regime $m_{\hat{b}} \gg \hat{\Lambda}_3$. The effective quark-antiquark potential can be modeled as a combination of a (logarithmically corrected) Coulomb potential and a long-distance linear potential. However, $\hat{\chi}$ decay to SM particles is only of interest if $\hat{\chi} \rightarrow G_{0+}G_{0+}$ is kinematically forbidden, since otherwise the twin hadronic decay will dominate. This requires $m_{\hat{\chi}} < 2m_0 \approx 13.6\hat{\Lambda}_3$. One may then check that (remembering a p-wave state is larger than an s-wave state) the Coulomb potential would imply an interquark distance of order $\hat{\Lambda}_3^{-1}$ for any relevant portion of the $(m_0, m_{\hat{\chi}})$ plane, showing the Coulomb approximation is very poor. This motivates using a purely linear potential, an approximation which improves for heavier states.

Taking the potential as linear in r with a string tension $\sigma \approx 4\hat{\Lambda}_3^2$, the Schrödinger equation for the p-wave radial function is:

$$\left[\frac{1}{2\mu} \left(-\frac{1}{r^2} \frac{d}{dr} r^2 \frac{d}{dr} + \frac{2}{r^2} \right) + (\sigma r - E_n) \right] R(r) = 0, \quad (\text{A.1})$$

with reduced mass $\mu = \frac{m_{\hat{b}}}{2}$. No exact solutions of this equation are known, but an excellent approximation may be obtained by neglecting the linear potential near $r = 0$ and the p-wave repulsive potential at large r , and then matching the two asymptotic oscillating solutions. Making this approximation we find the energy states

$$E_n \approx 2 \left(\frac{3\pi}{2} \right)^{2/3} \frac{\Lambda^{4/3}}{\mu^{1/3}} \left(n + \frac{1}{4} \right)^{2/3} \quad (\text{A.2})$$

and associated wave functions. This approximate solution is quite close to the exact numerical solution and may be used as a basis for more accurate estimates, though we have not done so here. In any case we believe that this formula correctly captures the parametric behavior of the energy levels and masses.

In the Standard Model, highly excited bottomonium states above 10.56 GeV promptly decay to a pair of B mesons; a similar story applies for charmonium. But in this model there are no light twin quarks, and correspondingly no twin B mesons, so the twin bottomonium states remain narrow until their masses are above $2m_0$ or $2m_{\hat{b}} + m_0$. In most parts of parameter space these are very heavy scales, so that the towers of narrow states extend to much higher n than in the SM.

For the physically interesting values of m_0 and $m_{\hat{b}}$, our approximation does not survive to high n , because relativistic effects become large at rather small n . Still, at small n

our approximation should work for $m_{\hat{b}} \gg \hat{\Lambda}_3$, including region A, most of the region B, and some portion of regions D and C. Full study of the spectrum with Coulombic and relativistic corrections is beyond our scope, but we expect that many of the results that we describe here will be parametrically valid (with order-one corrections) in the relativistic regime as well.

A.2 Decays

Here we explore decays of the light $\hat{\chi}$ states to the SM via mixing with the Higgs, and to a spin-one \hat{Y} state plus twin leptons $\hat{\ell} = \hat{\tau}, \hat{\nu}$ via a radiated off-shell \hat{Z} .

In models where the twin leptons are too heavy to allow $\hat{\chi} \rightarrow \hat{Y}\hat{\ell}\bar{\ell}$, the lowest-lying $\hat{\chi}$ state will dominantly decay to the SM, with a lifetime obtained from eq. (5.8):

$$c\tau \sim 3 \text{ mm} \times \left(\frac{30 \text{ GeV}}{m_{\hat{\chi}}}\right)^7 \left(\frac{m_{\hat{\chi}}}{2m_0}\right)^{10/3} \left(\frac{750 \text{ GeV}}{f}\right)^4 \quad (\text{A.3})$$

for $m_{\hat{\chi}} > 10 \text{ GeV}$. Just as for glueball states (see figure 6), the lifetime jumps upward once $m_{\hat{\chi}}$ falls below the SM $b\bar{b}$ threshold. This formula will also apply for the n^{th} $\hat{\chi}$ state (with an additional $n^{-2/3}$ suppression) if its twin strong and twin weak decays are kinematically forbidden. In this case, all the lowest-lying $\hat{\chi}$ states decay visibly even in region C, and displaced decays occur in low- $m_{\hat{b}}$ portions of both regions C and D.

Now suppose the twin leptons are light enough that $\hat{\chi} \rightarrow \hat{Y}\hat{\ell}\bar{\ell}$ is kinematically allowed. (Note the \hat{Y} states will then always promptly annihilate into twin lepton pairs, which are invisible in this model, via an off-shell \hat{Z} .) We saw in (5.9) that the decay $\hat{\chi} \rightarrow \hat{Y}\hat{\nu}\bar{\nu}$ goes as $(m_{\hat{\chi}} - m_{\hat{\nu}})^7$. While we could attempt to compute this splitting in the non-relativistic approximation, which would not be unreasonable for the higher n states, we know from SM charmonium that this splitting is strongly affected by spin-related effects that push $m_{\hat{\chi}}$ up and $m_{\hat{\nu}}$ down. Calculation of this splitting is therefore beyond the scope of our work.

However, we may use a trick to get a good estimate in a phenomenologically important part of parameter space, namely the part of region D (where both bottomonium and glueballs may be produced, often in the same event) that lies close to region B. This “BD-boundary” lies at $m_{G_{0+}} \approx m_{\hat{b}} \approx \frac{1}{2}m_{\hat{\chi}}$, a mass ratio very similar to the SM charmonium system, for which lattice studies give a SM glueball mass of 1.5–1.7 GeV [45, 78, 79], and a charm quark mass $m_c \approx 1.5 \text{ GeV}$. Therefore we can take results from charmonium data [80],

$$m_{\chi_{c0}} = 3.415 \text{ GeV}, \quad m_{J/\psi} = 3.097 \text{ GeV}, \quad (\text{A.4})$$

and rescale all mass scales by a common factor to obtain a realistic value for $m_{\hat{\chi}} - m_{\hat{\nu}}$ near the BD-boundary.

Using this scaling argument and the formulas of section 5.4, we see from figure 9 that displaced decays are possible for $m_{\hat{\chi}}$ somewhat below 30 GeV, with lifetimes potentially reaching 10 cm; otherwise the decays are prompt. The branching ratio of the lightest $\hat{\chi}$ to SM states is larger than $\sim 10\%$ (larger than $\sim 1\%$) for $2m_{\hat{b}} \sim 25 \text{ GeV}$ (10 GeV). We also remind the reader that in this part of region D one expects the Higgs branching rate to

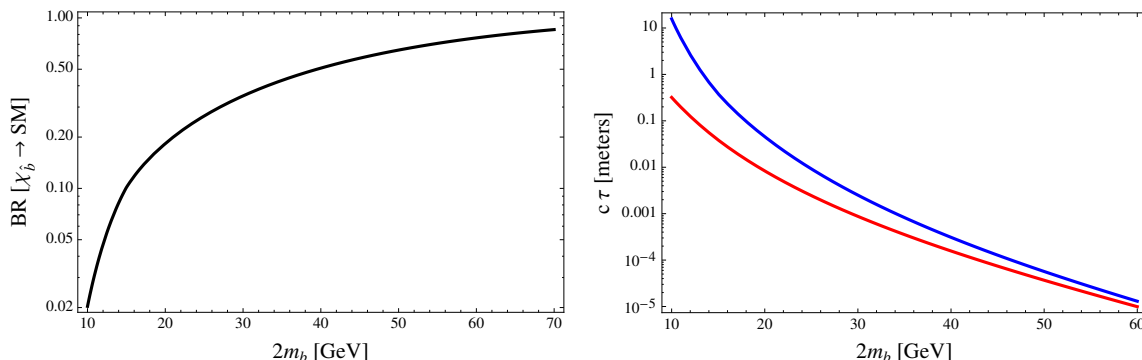


Figure 9. Features of $\hat{\chi}$ decay; we emphasize that these results have very substantial uncertainties due to the limitations of our estimation methods. Left: branching ratios of $\hat{\chi}$ into the SM along the BD-boundary line $m_{G_{0+}} = m_{\hat{b}}$, assuming twin neutrinos are massless. Right: decay length of $\hat{\chi}$ for $m_{G_{0+}} = m_{\hat{b}}$, where the lower red (upper blue) curve refers to massless (heavy) twin neutrinos.

twin bottomonium, from the $h \rightarrow \hat{b}\bar{\hat{b}}$ process, to be well enhanced above the irreducible rate. Consequently even a rather small branching fraction can be interesting.

However, we must emphasize that our estimates are highly uncertain due to our crude methods, which include the fact that we have not computed the numerical coefficient in (5.9). One should therefore only conclude that there is good reason to believe that the lowest $\hat{\chi}$ may be observable near the BD boundary, and possibly displaced, even if twin leptons are light. Excited $\hat{\chi}$ states will decay invisibly.

As we increase m_0 , moving away from the BD-boundary across region D and into C, we cannot reliably compute the $m_0/m_{\hat{b}}$ dependence of the $\hat{\chi} - \hat{Y}$ splitting and corresponding twin weak decay rates. However, both our approximations and reasoning from QCD data suggest the mass splitting rapidly increases with m_0 , at least as fast as $\hat{\Lambda}_3 \propto m_0$ itself. We therefore expect that even the lowest $\hat{\chi}$ state decays invisibly with a branching fraction near unity, across the right side of region D and all of region C.

Finally let us note that we are not aware of any other bottomonium states that have observable decays.

B Twin hadron production in more detail

Twin hadrons are produced when $h \rightarrow \hat{g}\hat{g}$ or $\hat{b}\bar{\hat{b}}$, but twin hadronization is complicated and poorly understood. Despite many years of experimental study of QCD hadron production, theoretical understanding of hadronization is still limited. Moreover a twin sector with no light twin quarks has a very different spectrum and dynamics from SM QCD.

Perturbation theory applies for inclusive calculations, such as $\text{Br}(h \rightarrow \text{twin hadrons})$, when colored particle production occurs at distances short compared to $\hat{\Lambda}_3^{-1}$, so that $\hat{\alpha}_s$ is small. (A similar example is the hadronic branching fraction of the Z .) However, for large m_0 or $m_{\hat{\chi}}$, twin hadron production is analogous to production of QCD hadrons within or just above the QCD resonance region, where non-perturbative effects can be important. Decays of the h can be enhanced relative to perturbative estimates if m_h lies close to a

narrow excited 0^{++} glueball or quarkonium resonance, and suppressed if it lies between two such resonances.

B.1 Nonperturbative effects in twin gluon production

First consider $h \rightarrow \hat{g}\hat{g}$ for $m_{\hat{b}} > m_h/2$. For small m_0 , the glueball resonances near 125 GeV are likely to be both numerous and wide, blending into a continuum. In this case the irreducible rate is given by the perturbative result (5.10) for $h \rightarrow \hat{g}\hat{g}$.

For larger m_0 , resonance effects are potentially important. Based on large- N_c counting and experience from the ρ meson — $\Gamma_\rho \sim m_\rho/5$ is of order $1/N_c = 1/3$ — we expect that excited 0^{++} glueball resonances have $\Gamma/m \sim 1/N_c^2 = 1/9$, perhaps with an additional minor suppression factor. There is also likely a phase-space effect increasing the width for higher excitations, but we ignore this for our conservative estimate. Meanwhile the spacing between 0^{++} glueball resonances is likely to be smaller than m_0 (as is the case for ρ mesons, among others) but it is surely no larger; lattice evidence for the second 0^{++} glueball [47] supports this. The maximum suppression between two resonances of width Γ and spacing Δ , relative to a perturbative calculation, is of order $\Gamma/\Delta \gtrsim (m_0/N_c^2)/m_0 = 1/9$. Thus we expect the worst possible non-perturbative suppression factor is about 0.1, bringing the worst-case rate for glueball production down no further than 10^{-4} .

B.2 Nonperturbative effects in twin bottom production

If the Higgs can decay to \hat{b} quarks and thus to $[\hat{b}\hat{b}]$ states, the rate for twin hadron production is often enhanced. As before, the $[\hat{b}\hat{b}]$ production rate is given by the perturbative rate for $h \rightarrow \hat{b}\hat{b}$ for sufficiently small $m_{\hat{b}}$ and m_0 . As discussed in section 5.5, the perturbative branching fraction for $h \rightarrow [\hat{b}\hat{b}] + X$ grows as \hat{y}_b^2 , contradicting existing Higgs measurements for $\hat{y}_b \gtrsim 1.25y_b$.

But at high \hat{y}_b , the perturbative rate often gives the wrong answer. The widths of the excited $\hat{\chi}$ states with mass $\sim m_h$ may be very small compared to their mass splittings, due to kinematic constraints. For instance, the $\hat{\chi}$ widths are tiny if $m_h < m_{\hat{\eta}} + m_0, 2m_{\hat{\eta}}$, and may be quite narrow until $m_h - m_{\hat{\eta}} \gg m_0$. If m_h lies between two resonances, then there can be a strong non-perturbative suppression compared to the perturbative rate.

We may make an estimate of the maximal suppression factor as we did for glueballs for large $m_{\hat{\chi}}$ and small m_0 . Here the annihilation decay $\hat{\chi} \rightarrow \hat{g}\hat{g}$ is perturbative and depends on $R'(0)$, which we have estimated as described in appendix A; this gives us Γ if radiative decays of the $\hat{\chi}$ are sufficiently suppressed by small twin bottomonium mass splittings. Similarly we may obtain Δ for the higher $\hat{\chi}$ states from (A.2). We find a suppression factor of order

$$\hat{\alpha}_3^2(E_n/m_{\hat{\chi}})^{3/2}, \tag{B.1}$$

where $\hat{\alpha}_3$ arises from the annihilation rate and should be evaluated at the scale $m_{\hat{b}}$, and where E_n is the excitation energy of the relevant $\hat{\chi}$ state. Since the relevant $\hat{\chi}$ state has a mass $\approx m_h$, $E_n \sim m_h - 2m_{\hat{b}}$, as long as n is not too small. This suppression factor can be of order 0.01–0.1. A suppression factor of $(\hat{y}_b/1.25)^2 \approx (2m_{\hat{b}}/30 \text{ GeV})^2$ would be enough to make a perturbatively excluded region allowed, so we conclude that some regions with $m_{\hat{b}}$

somewhat below $m_h/2$, specifically those where m_h lies between two excited bottomonium states, are probably not excluded by data.

For larger m_0 there can be even more suppression because the rate $\hat{\chi} \rightarrow \hat{g}\hat{g}$ can be modulated by excited glueballs for the same reason as $h \rightarrow \hat{g}\hat{g}$ is modulated by excited glueball resonances. We therefore expect that the non-perturbatively allowed portion of region A extends to lower $m_{\hat{b}}$ than that of region B. However, we have no reliable computational methods in this regime.

C Search strategies

Here we briefly discuss some triggering and analysis issues with regard to the search for the displaced decays of long-lived twin hadrons. For brevity, we refer to the visible decay products of a long-lived particle as a “displaced vertex” (DV) even when it occurs in regions where tracks are not actually reconstructed. We also refer collectively to the decay products of a W or Z in Wh and Zh production, and to the vector boson fusion (VBF) jets in VBF Higgs production, as “associated objects” (AO).

C.1 Comments on triggering

Triggering on Higgs decays to long-lived neutral particles requires three classes of trigger strategies, which respectively focus on

- the presence of one or two DVs; this method is largely independent of how h is produced and is sensitive to non-Higgs production of the DVs. Displaced decay objects can include jets with displaced tracks, trackless jets (possibly including a muon), narrow trackless jets with little electromagnetic calorimeter (ECAL) deposition, and unusual clusters of hits or tracks in the muon system.
- the presence of AOs that accompany the Higgs, including VBF jets or daughters of a W or Z (leptons, neutrinos, jets); this method is relatively independent of the details of the h decay and can therefore be used for any exotic h decay mode.
- the presence of both; for instance, in an event with VBF jets along with a trackless jet. Requiring both may be used to lower p_T thresholds on the trigger objects, or to access DVs that would be unusable on their own. However, this powerful method is specifically optimized for Higgs decays to long-lived particles.

Triggers of the first type were used at ATLAS [26–28, 50, 53–55, 81] and CMS [29, 58, 82] in Run I; lepton and \cancel{E}_T triggers are standard, while a VBF trigger was used in 2012 parked data at CMS [83]; and no triggers of the third type were used in Run I, to our knowledge.

Depending on the lifetimes of the long-lived particles and on their masses and other kinematics, any one of the three approaches to triggering can work for any of the three search strategies outlined in section 6.1. We leave the appropriate studies to our experimental colleagues.

C.2 Benchmark models

Next we point out possible benchmarks that may be used as straw-man targets. Although the parameters of the benchmarks are correlated in the Fraternal Twin Higgs — for instance the mass and lifetime of the G_{0+} are highly correlated, eq. (5.5) — it is important to account for the many uncertainties in twin hadronization, and even more important, to retain model-independence. Therefore, notwithstanding the particular features of the Fraternal Twin Higgs, it seems best to ignore these correlations and study the benchmark models across their entire parameter space.

In section 6.1 we suggested three possible search strategies, and we now discuss suitable benchmarks appropriate for each of them. To keep things simple, we discuss them in the context of phenomena that occur in region A. However, with a little thought the reader may verify that the same benchmarks would be useful for these and other processes that occur in other regions of parameter space.

C.2.1 Single displaced vertex search

To look for a single hadronic DV from $h \rightarrow G_{0+} + \dots$ (and similar decays) is challenging, because of large, difficult-to-measure backgrounds. A CMS search [29] that required only one DV was not able to set limits on decays of a 125 GeV particle. Relevant ATLAS searches used single DV events to obtain background estimates on double DV events. However, such a search *is* necessary. When $c\tau_0 \gg 10$ m (as for $m_0 \lesssim 10$ GeV in region A), or if hadronization assures that particles making DVs are rare among twin hadrons, the number of DVs rarely exceeds one per event.

To date no search for a DV has exploited the AOs, the VBF jets and/or lepton(s), that sometimes accompany the Higgs. To obtain background estimates, it may be enough to measure the rates for events with neither an AO nor a DV, and with either an AO *or* a DV; then if the AO and DV are uncorrelated one may predict the rate to have *both* an AO *and* a DV.

Also, searches for a single DV can demand a second object from the twin hadrons that do not produce a DV. This object could be \cancel{E}_T (relevant for very long-lived G_{0+}) or prompt jets, possibly b -tagged (relevant for $h \rightarrow G_{0+}G'_{+0}$, where $G'_{+0} \rightarrow b\bar{b}$ promptly).

In this context we suggest the following benchmark models (in which all X_i of mass m_i decay to SM final states with the same branching fractions as a Higgs of mass m_i , unless otherwise noted). These benchmarks do not cover all the kinematic possibilities but will serve as a useful initial target.

1. $h \rightarrow X_1X_2$, where X_1 has a long lifetime τ_1 , and $X_2 \rightarrow \cancel{E}_T$.
2. $h \rightarrow X_1X_2$, where X_1 has a long lifetime τ_1 and now $X_2 \rightarrow \text{SM}$ with a prompt decay.

It is important to consider a range of masses for m_1 and m_2 . For the first benchmark, $m_1 \neq m_2$ helps account for the possibility of $h \rightarrow$ many glueballs, of which only one gives a DV and the rest are unseen; then X_2 represents a system of ≥ 2 glueballs, with a large invariant mass. The signal of the second benchmark may arise from decays such as $h \rightarrow G_{0+}G'_{0+}$ or $h \rightarrow G_{0+}\hat{\chi}$, which generally have $m_1 \neq m_2$.

C.2.2 Exclusive double displaced vertex search

In the heart of region A ($m_0 \sim 20\text{--}40\text{ GeV}$), $h \rightarrow G_{0+}G_{0+}$ often gives two DV, roughly back-to-back and with invariant mass $\sim m_h$. Several searches for this final state have been undertaken at ATLAS [27, 28, 50] and at LHCb [51]. Also interesting is $h \rightarrow G_{0+}G'_{+0}$; here one has particles of two different lifetimes and masses.

In this context we suggest benchmark models of the form

1. $h \rightarrow XX$, where X has mass m_X and lifetime τ_X .
2. $h \rightarrow X_1X_2$, where now the X_i have different masses $m_1 < m_2$ and lifetimes τ_i .

In our minimal model it is sufficient to consider $m_1 < m_2 < 2m_1$ since otherwise $X_2 \rightarrow X_1X_1$ decays occur. This will not be true in all models however.

C.2.3 Inclusive double displaced vertex search

For $m_0 \sim 10\text{--}25\text{ GeV}$, with lifetimes still within the detector, the probability of producing > 2 glueballs per event is larger, making it more common to have two G_{0+} DVs along with one or more invisible glueballs. One key difference from the exclusive double DV search is that the two DVs may not be well-separated in the lab frame, and may even tend to be found in the same angular region of the detector. Also, the invariant mass of the two (or more) DVs may be well below m_h .

A suitable benchmark highlighting this difference would be

- $h \rightarrow X_1X_1X_2$, where the masses are chosen freely (but typically $m_2 \geq m_1$), X_1 decays as usual with lifetime τ_1 , and $X_2 \rightarrow \cancel{E}_T$. Here the two DVs will have a broad distribution in angular separation and in the momentum that they carry in the h rest frame.

The one serious caveat is the possibility (perhaps remote in the our minimal model, but not necessarily in other models) that the DVs are often clustered [15, 16, 20, 52, 84]. A special benchmark model may be needed if this clustering is sufficiently common that isolation requirements on DV candidates typically fail. We suggest

- $h \rightarrow X_0X_2$, followed promptly by $X_0 \rightarrow X_1X_1$, X_1 decays as usual with lifetime τ_1 , and $X_2 \rightarrow \cancel{E}_T$. By choosing $2m_1 < m_0 < m_2 \ll m_h$, one assures that X_0 is relativistic and the two X_1 decays are correlated in angle.

D Precision electroweak

Here we briefly consider precision electroweak constraints on the Twin Higgs mechanism. In any theory where coupling deviations of the SM-like Higgs are due to mixing with heavier states there are infrared contributions to the S and T parameters whose coefficients depend on the reduced coupling of the SM-like Higgs to electroweak gauge bosons. The logarithmic contributions to S and T scale like $\log(m_h/m_Z) + (1 - a^2) \log(\Lambda/m_h)$, where $a = g_{hVV}/g_{h_{\text{SM}}VV}$ and Λ is the cutoff scale associated with heavy states. In composite

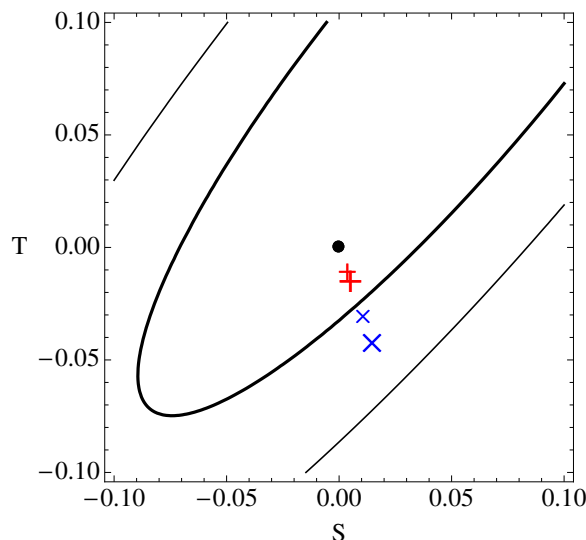


Figure 10. Close-up of the one- and two-sigma S, T ellipses marginalized over U with contributions from both the SM-like Higgs and the heavy twin Higgs \hat{h} . The small (large) blue “ \times ” shows the S, T prediction including a heavy twin Higgs of mass $m_{\hat{h}} = 750$ GeV (1.5 TeV) for $f = 3v$, while the small (large) red “ $+$ ” shows the S, T prediction including a heavy twin Higgs of mass $m_{\hat{h}} = 750$ GeV (1.5 TeV) for $f = 5v$. The black dot denotes the contribution of a purely Standard Model Higgs of mass $m_h = 125$ GeV.

Higgs models the coupling deviations come from mixing with heavy resonances, which must lie in the multi-TeV range due to tree-level contributions to S and T . The cutoff on infrared contributions is then of order $\Lambda = 4\pi v/\sqrt{1-a^2} \sim 4\pi f$, leading to extremely strong constraints on a [60].

In the Twin Higgs mechanism, the $\mathcal{O}(v/f)$ deviations in Higgs couplings come from mixing with the heavy twin Higgs and the cutoff is precisely $\Lambda = m_{\hat{h}}$. If the additional twin Higgs is nonperturbatively heavy (i.e. $m_{\hat{h}} \sim 4\pi f$), the situation is identical to composite Higgs models, but in general the heavy twin Higgs can be much lighter thanks to a custodial symmetry; there are no tree-level contributions to S and T associated with \hat{h} . The complete contributions to S and T from the SM-like Higgs and heavy Higgs take the form

$$\Delta S \approx \frac{1}{6\pi} \left(\frac{v}{f}\right)^2 \ln\left(\frac{m_{\hat{h}}}{m_h}\right) \quad \Delta T \approx -\frac{3}{8\pi c_{\theta_w}^2} \left(\frac{v}{f}\right)^2 \ln\left(\frac{m_{\hat{h}}}{m_h}\right) \quad (\text{D.1})$$

relative to the precision electroweak contributions of a theory with a SM Higgs of mass m_h . The current GFitter bound gives $S = 0.05 \pm 0.11$ and $T = 0.09 \pm 0.13$ for a reference Higgs mass of $m_h = 125$ GeV [85]. We translate this into a fit by marginalizing over U to create the S, T ellipse for free U and plot the spread of IR S, T contributions as a function of $m_{\hat{h}}$ and f in figure 10. Remaining within the 1σ (2σ) error for $f = 3v$ requires $m_{\hat{h}} \lesssim 600$ GeV (5 TeV). In contrast to composite Higgs models, precision electroweak constraints do not substantially constrain Higgs coupling deviations in the Twin Higgs as long as the heavy Higgs is in the TeV range.

E The effect of twin hypercharge

In our minimal model, for reasons described in section 2, we have assumed twin hypercharge is absent. What if it is present? Then the most *natural* values of the mass for the twin photon $\hat{\gamma}$ are (1) $\sim \Lambda$, in which case nothing changes from our present discussion, or (2) zero.

A key issue for twin photons is their kinetic mixing $\frac{\kappa}{2} F_{\mu\nu} \hat{F}^{\mu\nu}$ with the SM photon [86]. In our model the mixing parameter κ is not generated at low-loop order at scales below Λ , so its size is determined by its value at Λ , which is itself determined by physics in the ultraviolet that we do not specify. It is thus a free parameter of the model.

If $m_{\hat{\gamma}} = 0$, we define the twin photon as the massless particle that does not couple to the visible sector, and the $\hat{\tau}$ and \hat{b} acquire electric charges $\varepsilon \equiv \kappa \hat{e}/e$ and $\varepsilon/3$, respectively, in units of e . The twin photon is stable and invisible. All twin hadrons may decay via radiation or annihilation to on-shell or off-shell twin photons — twin bottomonium through tree-level graphs and twin glueballs through a loop of twin bottom quarks. The rates for these decays far exceed rates for decays through the off-shell Higgs, and so most decays to the hidden sector are invisible.

However, any twin photon may be replaced by a SM photon at the cost of $\varepsilon^2 e^2$ in branching fraction. Constraints on ε for a massless (or nearly massless) twin photon arise from e^+e^- production of the fractionally charged twin $\hat{\tau}$ and \hat{b} fermions. Since most twin sector production events are invisible, one can obtain a model-independent limit on ε that depends only on whether twin $\hat{\tau}$ and \hat{b} are kinematically accessible, for instance in Z decays. Such limits are weak, however, of order $\varepsilon \lesssim 10^{-1}$ [87]. But typically the true limits are stronger, because the fraction $\sim \varepsilon^2$ of events that produce a visible signal could have been seen at LEP. The detailed limits are far too complex for us to work out here.

If ε is not small, lying in the $10^{-3} - 10^{-1}$ range, $h \rightarrow \gamma + \cancel{E}_T$ and rare $h \rightarrow \gamma\gamma + \cancel{E}_T$ decays may occur, especially if the twin hadron production rate is large (regions B, C, and D with $m_{\hat{b}}$ not too small). Moreover, annihilation of spin-one states via an off-shell SM photon may produce a visible final state, e.g. $\hat{Y} \rightarrow \gamma^* \rightarrow \ell^+\ell^-$. This prompt resonant decay will be subleading by $\sim \varepsilon^2$ compared to the invisible decay $\hat{Y} \rightarrow \hat{\gamma}^* \rightarrow \hat{\tau}\hat{\tau}$ as long as $m_{\hat{\tau}} < m_{\hat{b}}$; otherwise, it competes favorably with highly-suppressed twin sector decays, and may even dominate. This type of decay is probably common in regions C and D. In region B, where bottomonium decays to glueballs, this decay can perhaps still occur for the 1^{--} glueball, but this glueball is heavy and probably quite rare.

In summary, for $m_{\hat{\gamma}} = 0$ and at small ε , all twin-sector decays are invisible, but partly-visible decays arise at large ε . In region A, where production is small, $\gamma + \cancel{E}_T$ decays may be the best bet but are very rare. In region B, the larger production rate offers the possibility of a large $\gamma + \cancel{E}_T$ rate and a small but important $\gamma\gamma + \cancel{E}_T$ rate. And in regions C and D, the final state $\mu^+\mu^- + \cancel{E}_T$, where the $\mu^+\mu^-$ form the lowest \hat{Y} resonance, may be either rare or common. (Higher \hat{Y} resonances will often decay radiatively.) Thus searches for both invisible and partly visible decays of the Higgs are highly motivated; see section 6.2 above.

Meanwhile, a twin photon with $m_{\hat{\gamma}} \ll \Lambda$ typically introduces a new naturalness problem if Higgsed, since one more Higgs field S is required and its expectation value and mass

must be $\ll \Lambda$. One can get around this if the hypercharge coupling \hat{g}_1 is very small, with $\hat{g}_1\Lambda < m_h/2$. Alternately, the twin photon may be rendered massive by the Stueckelberg mechanism, which is technically natural but entails a parametrically new scale if $m_{\tilde{\gamma}} \ll \Lambda$. In either case, we view this possibility as lying beyond the *minimal* Twin Higgs story.

For $2m_e < m_{\tilde{\gamma}} < m_h$, the twin photon can play a major role in LHC signals. In contrast to the massless case, here we define the massless SM photon as decoupled from twin particles; the twin photon is identified as the mass eigenstate, which couples to SM fields with strength $\sim \varepsilon e$. Assuming the twin photon is light enough that all twin hadrons can decay to it, twin hadron production generically (and not just for 0^{++} hadrons) leads to high multiplicity (≥ 4) twin photon final states. Through kinetic mixing with the SM photon, the twin photons then decay to lepton pairs and jet pairs (or simply hadron pairs, such as K^+K^- and $\pi^+\pi^-$, if $m_{\tilde{\gamma}} \sim \text{few GeV}$ or below). The decays of the twin photon may be prompt or displaced depending on the value of ε , on which there are a number of constraints; for a recent summary, see [88]. If prompt, however, limits on multilepton final states (for $m_{\tilde{\gamma}} \gg 1 \text{ GeV}$) [89–92] and on prompt “lepton-jets” (for $m_{\tilde{\gamma}} \lesssim 1 \text{ GeV}$) [93–98] are strong constraints. Searches for significantly displaced lepton pairs with masses well above 1 GeV [99] and $\lesssim 1 \text{ GeV}$ [52, 54, 55] are sensitive to this signal but have by no means excluded it. Moreover, any such constraints become much weaker once $c\tau_{\tilde{\gamma}} \sim \varepsilon^{-2}m_{\tilde{\gamma}}^{-1} \gg 10 \text{ m}$. Note also that if some twin hadrons are too light to decay to twin photons, a mixture of these signals and those described in the main text is possible.

Open Access. This article is distributed under the terms of the Creative Commons Attribution License ([CC-BY 4.0](https://creativecommons.org/licenses/by/4.0/)), which permits any use, distribution and reproduction in any medium, provided the original author(s) and source are credited.

References

- [1] Z. Chacko, H.-S. Goh and R. Harnik, *The twin Higgs: natural electroweak breaking from mirror symmetry*, *Phys. Rev. Lett.* **96** (2006) 231802 [[hep-ph/0506256](#)] [[INSPIRE](#)].
- [2] R. Barbieri, T. Gregoire and L.J. Hall, *Mirror world at the Large Hadron Collider*, [hep-ph/0509242](#) [[INSPIRE](#)].
- [3] Z. Chacko, Y. Nomura, M. Papucci and G. Perez, *Natural little hierarchy from a partially goldstone twin Higgs*, *JHEP* **01** (2006) 126 [[hep-ph/0510273](#)] [[INSPIRE](#)].
- [4] G. Burdman, Z. Chacko, H.-S. Goh and R. Harnik, *Folded supersymmetry and the LEP paradox*, *JHEP* **02** (2007) 009 [[hep-ph/0609152](#)] [[INSPIRE](#)].
- [5] G. Burdman, Z. Chacko, R. Harnik, L. de Lima and C.B. Verhaaren, *Colorless top partners, a 125 GeV Higgs and the limits on naturalness*, *Phys. Rev. D* **91** (2015) 055007 [[arXiv:1411.3310](#)] [[INSPIRE](#)].
- [6] S. Dimopoulos and G.F. Giudice, *Naturalness constraints in supersymmetric theories with nonuniversal soft terms*, *Phys. Lett. B* **357** (1995) 573 [[hep-ph/9507282](#)] [[INSPIRE](#)].
- [7] A.G. Cohen, D.B. Kaplan and A.E. Nelson, *The more minimal supersymmetric standard model*, *Phys. Lett. B* **388** (1996) 588 [[hep-ph/9607394](#)] [[INSPIRE](#)].

- [8] R. Sundrum, *SUSY splits, but then returns*, *JHEP* **01** (2011) 062 [[arXiv:0909.5430](#)] [[INSPIRE](#)].
- [9] R. Barbieri, E. Bertuzzo, M. Farina, P. Lodone and D. Pappadopulo, *A non standard supersymmetric spectrum*, *JHEP* **08** (2010) 024 [[arXiv:1004.2256](#)] [[INSPIRE](#)].
- [10] M. Papucci, J.T. Ruderman and A. Weiler, *Natural SUSY endures*, *JHEP* **09** (2012) 035 [[arXiv:1110.6926](#)] [[INSPIRE](#)].
- [11] C. Brust, A. Katz, S. Lawrence and R. Sundrum, *SUSY, the third generation and the LHC*, *JHEP* **03** (2012) 103 [[arXiv:1110.6670](#)] [[INSPIRE](#)].
- [12] J.A. Evans, Y. Kats, D. Shih and M.J. Strassler, *Toward full LHC coverage of natural supersymmetry*, *JHEP* **07** (2014) 101 [[arXiv:1310.5758](#)] [[INSPIRE](#)].
- [13] J. Berger, M. Perelstein, M. Saelim and P. Tanedo, *The same-sign dilepton signature of RPV/MFV SUSY*, *JHEP* **04** (2013) 077 [[arXiv:1302.2146](#)] [[INSPIRE](#)].
- [14] Z. Han, A. Katz, M. Son and B. Tweedie, *Boosting searches for natural supersymmetry with R-parity violation via gluino cascades*, *Phys. Rev. D* **87** (2013) 075003 [[arXiv:1211.4025](#)] [[INSPIRE](#)].
- [15] M.J. Strassler and K.M. Zurek, *Echoes of a hidden valley at hadron colliders*, *Phys. Lett. B* **651** (2007) 374 [[hep-ph/0604261](#)] [[INSPIRE](#)].
- [16] M.J. Strassler, *Possible effects of a hidden valley on supersymmetric phenomenology*, [hep-ph/0607160](#) [[INSPIRE](#)].
- [17] M.J. Strassler and K.M. Zurek, *Discovering the Higgs through highly-displaced vertices*, *Phys. Lett. B* **661** (2008) 263 [[hep-ph/0605193](#)] [[INSPIRE](#)].
- [18] T. Han, Z. Si, K.M. Zurek and M.J. Strassler, *Phenomenology of hidden valleys at hadron colliders*, *JHEP* **07** (2008) 008 [[arXiv:0712.2041](#)] [[INSPIRE](#)].
- [19] M.J. Strassler, *Why unparticle models with mass gaps are examples of hidden valleys*, [arXiv:0801.0629](#) [[INSPIRE](#)].
- [20] M.J. Strassler, *On the phenomenology of hidden valleys with heavy flavor*, [arXiv:0806.2385](#) [[INSPIRE](#)].
- [21] J.E. Juknevich, D. Melnikov and M.J. Strassler, *A pure-gluon hidden valley I. States and decays*, *JHEP* **07** (2009) 055 [[arXiv:0903.0883](#)] [[INSPIRE](#)].
- [22] J. Kang and M.A. Luty, *Macroscopic strings and ‘quirks’ at colliders*, *JHEP* **11** (2009) 065 [[arXiv:0805.4642](#)] [[INSPIRE](#)].
- [23] J.E. Juknevich, *Pure-gluon hidden valleys through the Higgs portal*, *JHEP* **08** (2010) 121 [[arXiv:0911.5616](#)] [[INSPIRE](#)].
- [24] L.M. Carpenter, D.E. Kaplan and E.-J. Rhee, *Reduced fine-tuning in supersymmetry with R-parity violation*, *Phys. Rev. Lett.* **99** (2007) 211801 [[hep-ph/0607204](#)] [[INSPIRE](#)].
- [25] ATLAS collaboration, *Triggering on long-lived neutral particles in the ATLAS detector*, [ATL-PHYS-PUB-2009-082](#), [ATL-COM-PHYS-2009-233](#) (2009).
- [26] ATLAS collaboration, *Triggers for displaced decays of long-lived neutral particles in the ATLAS detector*, *2013 JINST* **8** P07015 [[arXiv:1305.2284](#)] [[INSPIRE](#)].
- [27] ATLAS collaboration, *Search for a light Higgs boson decaying to long-lived weakly-interacting particles in proton-proton collisions at $\sqrt{s} = 7$ TeV with the ATLAS detector*, *Phys. Rev. Lett.* **108** (2012) 251801 [[arXiv:1203.1303](#)] [[INSPIRE](#)].

- [28] ATLAS collaboration, *Search for pair produced long-lived neutral particles decaying in the ATLAS hadronic calorimeter in pp collisions at $\sqrt{s} = 8$ TeV*, [ATLAS-CONF-2014-041](#) (2014).
- [29] CMS collaboration, *Search for long-lived neutral particles decaying to quark-antiquark pairs in proton-proton collisions at $\sqrt{s} = 8$ TeV*, *Phys. Rev. D* **91** (2015) 012007 [[arXiv:1411.6530](#)] [[INSPIRE](#)].
- [30] M.R. Buckley, V. Halyo and P. Lujan, *Don't miss the displaced Higgs at the LHC again*, [arXiv:1405.2082](#) [[INSPIRE](#)].
- [31] Y. Cui and B. Shuve, *Probing baryogenesis with displaced vertices at the LHC*, *JHEP* **02** (2015) 049 [[arXiv:1409.6729](#)] [[INSPIRE](#)].
- [32] H. Cai, H.-C. Cheng and J. Terning, *A quirky little Higgs model*, *JHEP* **05** (2009) 045 [[arXiv:0812.0843](#)] [[INSPIRE](#)].
- [33] A. Falkowski, S. Pokorski and M. Schmaltz, *Twin SUSY*, *Phys. Rev. D* **74** (2006) 035003 [[hep-ph/0604066](#)] [[INSPIRE](#)].
- [34] S. Chang, L.J. Hall and N. Weiner, *A supersymmetric twin Higgs*, *Phys. Rev. D* **75** (2007) 035009 [[hep-ph/0604076](#)] [[INSPIRE](#)].
- [35] N. Craig and K. Howe, *Doubling down on naturalness with a supersymmetric twin Higgs*, *JHEP* **03** (2014) 140 [[arXiv:1312.1341](#)] [[INSPIRE](#)].
- [36] P. Batra and Z. Chacko, *A composite twin Higgs model*, *Phys. Rev. D* **79** (2009) 095012 [[arXiv:0811.0394](#)] [[INSPIRE](#)].
- [37] M. Geller and O. Telem, *Holographic twin Higgs model*, *Phys. Rev. Lett.* **114** (2015) 191801 [[arXiv:1411.2974](#)] [[INSPIRE](#)].
- [38] N. Craig, S. Knapen and P. Longhi, *Neutral naturalness from orbifold Higgs models*, *Phys. Rev. Lett.* **114** (2015) 061803 [[arXiv:1410.6808](#)] [[INSPIRE](#)].
- [39] N. Craig, S. Knapen and P. Longhi, *The orbifold Higgs*, *JHEP* **03** (2015) 106 [[arXiv:1411.7393](#)] [[INSPIRE](#)].
- [40] N. Arkani-Hamed, A.G. Cohen and H. Georgi, *Electroweak symmetry breaking from dimensional deconstruction*, *Phys. Lett. B* **513** (2001) 232 [[hep-ph/0105239](#)] [[INSPIRE](#)].
- [41] N. Arkani-Hamed, A.G. Cohen, T. Gregoire and J.G. Wacker, *Phenomenology of electroweak symmetry breaking from theory space*, *JHEP* **08** (2002) 020 [[hep-ph/0202089](#)] [[INSPIRE](#)].
- [42] N. Arkani-Hamed et al., *The minimal moose for a little Higgs*, *JHEP* **08** (2002) 021 [[hep-ph/0206020](#)] [[INSPIRE](#)].
- [43] M. Schmaltz and D. Tucker-Smith, *Little Higgs review*, *Ann. Rev. Nucl. Part. Sci.* **55** (2005) 229 [[hep-ph/0502182](#)] [[INSPIRE](#)].
- [44] C.J. Morningstar and M.J. Peardon, *The glueball spectrum from an anisotropic lattice study*, *Phys. Rev. D* **60** (1999) 034509 [[hep-lat/9901004](#)] [[INSPIRE](#)].
- [45] Y. Chen et al., *Glueball spectrum and matrix elements on anisotropic lattices*, *Phys. Rev. D* **73** (2006) 014516 [[hep-lat/0510074](#)] [[INSPIRE](#)].
- [46] M. Gockeler et al., *A determination of the Lambda parameter from full lattice QCD*, *Phys. Rev. D* **73** (2006) 014513 [[hep-ph/0502212](#)] [[INSPIRE](#)].
- [47] B. Lucini, M. Teper and U. Wenger, *Glueballs and k-strings in SU(N) gauge theories: calculations with improved operators*, *JHEP* **06** (2004) 012 [[hep-lat/0404008](#)] [[INSPIRE](#)].

- [48] A. Djouadi, J. Kalinowski and M. Spira, *HDECAY: a program for Higgs boson decays in the standard model and its supersymmetric extension*, *Comput. Phys. Commun.* **108** (1998) 56 [[hep-ph/9704448](#)] [[INSPIRE](#)].
- [49] K.J. Juge, J. Kuti and C.J. Morningstar, *Bag picture of the excited QCD vacuum with static $Q\bar{Q}$ source*, *Nucl. Phys. Proc. Suppl.* **63** (1998) 543 [[hep-lat/9709132](#)] [[INSPIRE](#)].
- [50] ATLAS collaboration, *Search for displaced vertices arising from decays of new heavy particles in 7 TeV pp collisions at ATLAS*, *Phys. Lett. B* **707** (2012) 478 [[arXiv:1109.2242](#)] [[INSPIRE](#)].
- [51] LHCb collaboration, *Search for Higgs-like bosons decaying into long-lived exotic particles*, [LHCb-CONF-2012-014](#), CERN-LHCb-CONF-2012-014 (2012).
- [52] ATLAS collaboration, *Search for long-lived neutral particles decaying into lepton jets in proton-proton collisions at $\sqrt{s} = 8$ TeV with the ATLAS detector*, *JHEP* **11** (2014) 088 [[arXiv:1409.0746](#)] [[INSPIRE](#)].
- [53] ATLAS collaboration, *Search for long-lived, heavy particles in final states with a muon and multi-track displaced vertex in proton-proton collisions at $\sqrt{s} = 7$ TeV with the ATLAS detector*, *Phys. Lett. B* **719** (2013) 280 [[arXiv:1210.7451](#)] [[INSPIRE](#)].
- [54] ATLAS collaboration, *Search for displaced muonic lepton jets from light Higgs boson decay in proton-proton collisions at $\sqrt{s} = 7$ TeV with the ATLAS detector*, *Phys. Lett. B* **721** (2013) 32 [[arXiv:1210.0435](#)] [[INSPIRE](#)].
- [55] ATLAS collaboration, *Search for displaced muon jets from light Higgs boson decay in proton-proton collisions at $\sqrt{s} = 7$ TeV with the ATLAS detector*, [ATLAS-CONF-2012-089](#), [ATLAS-COM-CONF-2012-112](#) (2012).
- [56] CMS collaboration, *Search for displaced supersymmetry in events with an electron and a muon with large impact parameters*, *Phys. Rev. Lett.* **114** (2015) 061801 [[arXiv:1409.4789](#)] [[INSPIRE](#)].
- [57] CMS collaboration, *Search for long-lived particles decaying to final states that include dileptons*, [CMS-PAS-EXO-12-037](#) (2014).
- [58] CMS collaboration, *Search in leptonic channels for heavy resonances decaying to long-lived neutral particles*, *JHEP* **02** (2013) 085 [[arXiv:1211.2472](#)] [[INSPIRE](#)].
- [59] D. Curtin et al., *Exotic decays of the 125 GeV Higgs boson*, *Phys. Rev. D* **90** (2014) 075004 [[arXiv:1312.4992](#)] [[INSPIRE](#)].
- [60] J.R. Espinosa, C. Grojean, M. Muhlleitner and M. Trott, *First glimpses at Higgs' face*, *JHEP* **12** (2012) 045 [[arXiv:1207.1717](#)] [[INSPIRE](#)].
- [61] CMS collaboration, *Search for the resonant production of two Higgs bosons in the final state with two photons and two bottom quarks*, [CMS-PAS-HIG-13-032](#) (2014).
- [62] ATLAS collaboration, *Search for Higgs boson pair production in the $\gamma\gamma b\bar{b}$ final state using pp collision data at $\sqrt{s} = 8$ TeV from the ATLAS detector*, *Phys. Rev. Lett.* **114** (2015) 081802 [[arXiv:1406.5053](#)] [[INSPIRE](#)].
- [63] CMS collaboration, *Measurement of the properties of a Higgs boson in the four-lepton final state*, *Phys. Rev. D* **89** (2014) 092007 [[arXiv:1312.5353](#)] [[INSPIRE](#)].
- [64] ATLAS collaboration, *Measurements of Higgs boson production and couplings in diboson final states with the ATLAS detector at the LHC*, *Phys. Lett. B* **726** (2013) 88 [[arXiv:1307.1427](#)] [[INSPIRE](#)].

- [65] CMS collaboration, *2HDM neutral Higgs future analysis studies*, [CMS-PAS-FTR-13-024](#) (2013).
- [66] J.A. Evans, *A swarm of Bs*, *JHEP* **08** (2014) 073 [[arXiv:1402.4481](#)] [[INSPIRE](#)].
- [67] ATLAS collaboration, *Search for the $b\bar{b}$ decay of the standard model Higgs boson in associated $(W/Z)H$ production with the ATLAS detector*, *JHEP* **01** (2015) 069 [[arXiv:1409.6212](#)] [[INSPIRE](#)].
- [68] ATLAS collaboration, *Search for the standard model Higgs boson produced in association with top quarks and decaying to $b\bar{b}$ in pp collisions at $\sqrt{s} = 8$ TeV with the ATLAS detector at the LHC*, [ATLAS-CONF-2014-011](#) (2014).
- [69] ATLAS collaboration, *Evidence for Higgs boson Yukawa couplings in the $H \rightarrow \tau\tau$ decay mode with the ATLAS detector*, [ATLAS-CONF-2014-061](#) (2014).
- [70] ATLAS collaboration, *Observation and measurement of Higgs boson decays to WW^* with ATLAS at the LHC*, [ATLAS-CONF-2014-060](#) (2014).
- [71] ATLAS collaboration, *Measurements of Higgs boson production and couplings in the four-lepton channel in pp collisions at center-of-mass energies of 7 and 8 TeV with the ATLAS detector*, *Phys. Rev. D* **91** (2015) 012006 [[arXiv:1408.5191](#)] [[INSPIRE](#)].
- [72] ATLAS collaboration, *Measurement of Higgs boson production in the diphoton decay channel in pp collisions at center-of-mass energies of 7 and 8 TeV with the ATLAS detector*, *Phys. Rev. D* **90** (2014) 112015 [[arXiv:1408.7084](#)] [[INSPIRE](#)].
- [73] CMS collaboration, *Precise determination of the mass of the Higgs boson and studies of the compatibility of its couplings with the standard model*, [CMS-PAS-HIG-14-009](#) (2014).
- [74] CMS collaboration, *Search for $t\bar{t}H$ production using the matrix element method*, [CMS-PAS-HIG-14-010](#) (2014).
- [75] CMS collaboration, *Observation of the diphoton decay of the Higgs boson and measurement of its properties*, *Eur. Phys. J. C* **74** (2014) 3076 [[arXiv:1407.0558](#)] [[INSPIRE](#)].
- [76] G. Cowan, K. Cranmer, E. Gross and O. Vitells, *Asymptotic formulae for likelihood-based tests of new physics*, *Eur. Phys. J. C* **71** (2011) 1554 [[arXiv:1007.1727](#)] [[INSPIRE](#)].
- [77] ATLAS collaboration, *Projections for measurements of Higgs boson cross sections, branching ratios and coupling parameters with the ATLAS detector at a HL-LHC*, [ATL-PHYS-PUB-2013-014](#) (2013).
- [78] UKQCD collaboration, G.S. Bali et al., *A comprehensive lattice study of SU(3) glueballs*, *Phys. Lett. B* **309** (1993) 378 [[hep-lat/9304012](#)] [[INSPIRE](#)].
- [79] W. Ochs, *The status of glueballs*, *J. Phys. G* **40** (2013) 043001 [[arXiv:1301.5183](#)] [[INSPIRE](#)].
- [80] PARTICLE DATA GROUP collaboration, J. Beringer et al., *Review of particle physics*, *Phys. Rev. D* **86** (2012) 010001 [[INSPIRE](#)].
- [81] ATLAS collaboration, *Triggering on long-lived neutral particles in the ATLAS detector*, [ATL-PHYS-PUB-2009-082](#), [ATL-COM-PHYS-2009-233](#) (2009).
- [82] CMS collaboration, *Search for heavy resonances decaying to long-lived neutral particles in the displaced lepton channel*, [CMS-PAS-EXO-11-004](#) (2011).
- [83] CMS collaboration, *Search for invisible decays of Higgs bosons in the vector boson fusion and associated ZH production modes*, *Eur. Phys. J. C* **74** (2014) 2980 [[arXiv:1404.1344](#)] [[INSPIRE](#)].

- [84] N. Arkani-Hamed and N. Weiner, *LHC signals for a superunified theory of dark matter*, *JHEP* **12** (2008) 104 [[arXiv:0810.0714](#)] [[INSPIRE](#)].
- [85] GFITTER GROUP collaboration, M. Baak et al., *The global electroweak fit at NNLO and prospects for the LHC and ILC*, *Eur. Phys. J. C* **74** (2014) 3046 [[arXiv:1407.3792](#)] [[INSPIRE](#)].
- [86] B. Holdom, *Two U(1)'s and ϵ charge shifts*, *Phys. Lett.* **B 166** (1986) 196 [[INSPIRE](#)].
- [87] S. Davidson, S. Hannestad and G. Raffelt, *Updated bounds on millicharged particles*, *JHEP* **05** (2000) 003 [[hep-ph/0001179](#)] [[INSPIRE](#)].
- [88] R. Essig et al., *Dark sectors and new, light, weakly-coupled particles*, [arXiv:1311.0029](#) [[INSPIRE](#)].
- [89] CMS collaboration, *Search for physics beyond the standard model using multilepton signatures in pp collisions at $\sqrt{s} = 7$ TeV*, *Phys. Lett.* **B 704** (2011) 411 [[arXiv:1106.0933](#)] [[INSPIRE](#)].
- [90] CMS collaboration, *Search for electroweak production of charginos and neutralinos using leptonic final states in pp collisions at $\sqrt{s} = 7$ TeV*, *JHEP* **11** (2012) 147 [[arXiv:1209.6620](#)] [[INSPIRE](#)].
- [91] ATLAS collaboration, *Search for new phenomena in events with three charged leptons at $\sqrt{s} = 7$ TeV with the ATLAS detector*, *Phys. Rev.* **D 87** (2013) 052002 [[arXiv:1211.6312](#)] [[INSPIRE](#)].
- [92] ATLAS collaboration, *Search for anomalous production of prompt like-sign lepton pairs at $\sqrt{s} = 7$ TeV with the ATLAS detector*, *JHEP* **12** (2012) 007 [[arXiv:1210.4538](#)] [[INSPIRE](#)].
- [93] D0 collaboration, V.M. Abazov et al., *Search for dark photons from supersymmetric hidden valleys*, *Phys. Rev. Lett.* **103** (2009) 081802 [[arXiv:0905.1478](#)] [[INSPIRE](#)].
- [94] D0 collaboration, V.M. Abazov et al., *Search for events with leptonic jets and missing transverse energy in $p\bar{p}$ collisions at $\sqrt{s} = 1.96$ TeV*, *Phys. Rev. Lett.* **105** (2010) 211802 [[arXiv:1008.3356](#)] [[INSPIRE](#)].
- [95] CMS collaboration, *Search for light resonances decaying into pairs of muons as a signal of new physics*, *JHEP* **07** (2011) 098 [[arXiv:1106.2375](#)] [[INSPIRE](#)].
- [96] CMS collaboration, *Search for a non-standard-model Higgs boson decaying to a pair of new light bosons in four-muon final states*, *Phys. Lett.* **B 726** (2013) 564 [[arXiv:1210.7619](#)] [[INSPIRE](#)].
- [97] ATLAS collaboration, *A search for lepton-jets with muons at ATLAS*, [ATLAS-CONF-2011-076](#) (2011).
- [98] ATLAS collaboration, *A search for prompt lepton-jets in pp collisions at $\sqrt{s} = 7$ TeV with the ATLAS detector*, *Phys. Lett.* **B 719** (2013) 299 [[arXiv:1212.5409](#)] [[INSPIRE](#)].
- [99] CMS collaboration, *Search for long-lived particles that decay into final states containing two electrons or two muons in proton-proton collisions at $\sqrt{s} = 8$ TeV*, *Phys. Rev.* **D 91** (2015) 052012 [[arXiv:1411.6977](#)] [[INSPIRE](#)].