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DYNAMIC APERTURE OF THE PHOTON FACTORY STORAGE RING

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Abstract The dynamic aperture of the Photon Factory storage ring is strongly affected by the octupole magnets. The observations on the beam lifetime and the injection rate are consistent with the calculations on the dynamic aperture.

## INTRODUCTION

The Photon Factory storage ring (PF ring ) is a  $2.5$  GeV electron/positron storage ring dedicated to the synchrotron radiation experiments. In this ring, eleven octupole magnets  $\overline{ }$ OC'T's ) are installed to suppress transverse instabilities • When these OC'T's are excited strongly, the beam lifetime and the injection rate are significantly reduced. In this paper, we present some results of the calculations on the dynamic aperture with the OCT's strongly excited. They are compared with the observations on the beam lifetime and the injection rate.

### OCTUPOLE MAGNETS

In Figure 1, the present optics of the PF ring is shown. The locations of the OCT's are also indicated in the figure. The field strengths of the  $OCT'$ s are shown in Figure 2 as functions of the currents. Three octupole magnets, OCT9, 10, 11, are not used in this work and omitted from this figure.

# DYNAMIC

The OCT's can produce large amplitude-dependent tune shifts and make betatron motions with large amplitudes unstable. We calculated the dynamic apertures for the various currents of the OCT's. For simplicity, the currents of all the OCT's ( $OCT1-8$ ) were set to the same value. We used a lattice, whose betatron tunes were those of the present operation,  $8.41$  ( horizontal ) and 3. 11 ( vertical ), respectively. The sextupole magnets were also included in the calculations. Figure 3 shows the calculated dynamic apertures at the north synmetry point ( see Figure 1 ), where the physical aperture is smallest in the ring ( its half height:  $11 \text{ mm}$  ). As the currents of the OCT's ( I  $I_{\rm oct}$  $\lambda$ 



FIGURE 1 Optics of the PF ring. The locations of the OCT's are indicated by arrows with their names. The north synmetry point is also indicated by "N.S.".







increase, the dynamic aperture shrinks drastically. When the value of  $I_{\text{oct}}$  is negative, the dynamic aperture becomes smaller than the physical aperture.



Dynamic aperture at the north symmetry point for FIGURE 3a the positive values of  $I_{\text{oct}}$ .



FIGURE 3b Dynamic aperture at the north symmetry point for the negative values of  $I_{\text{oct}}$ .

# BEAM LIFETIME

When the OCT's are excited strongly, it is observed that the beam lifetime becomes shorter, as shown in Figure 4 ( in the discussions below, we will use the beam lifetime multiplied by the beam current,  $I \tau [A \cdot hr]$ , as a measure of the beam lifetime ). For the PF ring, I $\tau$  is mainly determined by the gas scattering<sup>"</sup>. We can then calculate I $\tau$  as a function of the smallest aperture as  $\mathrm{follows}^3;$ 

$$
I\tau [A \cdot hr] = (1/I\tau_b + 1/I\tau_c)^{-1} ,
$$
  
\n
$$
I\tau_c[A \cdot hr] = 12 \cdot f_c \cdot (A[mm]/11)^2 \{ (P/I) [nTorr/A]/4.8 \}^{-1} ,
$$
  
\n
$$
I\tau_b[A \cdot hr] = 7.9 \cdot f_b \cdot \{ (P/I) [nTorr/A]/4.8 \}^{-1} ,
$$

where;

$$
I\tau_{b}[A \cdot hr] = 7.9 \cdot f_{b} \cdot \{(P/I) [nTorr/A]/4.8\}^{-1},
$$
  
\n;  
\n
$$
f_{c} = (\Sigma Zi^{2}/100)^{-1} (E[GeV]/2.5)^{2} (\beta_{av}[m]/10)^{-1} (\beta_{u}[m]/13)^{-1},
$$
  
\n
$$
f_{b} = [(4/3 \cdot ln(1/\eta) - 5/6)/5.7]^{-1}
$$
  
\n
$$
\times \{ \Sigma Zi(Zi+1)ln(183Zi^{-1/3})/520\}^{-1}.
$$

i<br>Here, I $\tau$  is the lifetime due to "Bremsstrahlung" and I $\tau$  the lifetime due to "Coulomb scattering". The A is the minimum aperture around the ring, the E the beam energy, the  $\beta$  the



FIGURE 4 Dependency of the beam lifetime on I . White<br>squares are the measured values. The solid line is the calculated value.

averaged value of the betatron function, the  $\beta$  the betatron function at the minimum aperture, the  $\eta$  the RF bucket height. The Zi is the atomic numbers of the residual gas components. We assumed here that the residual gas is only composed of  $\infty$ . The (P/I) is the averaged gas pressure in the ring divided by the beam current. The measured value of (P/l) is 1.2 nTorr/A. The actual vacuum pressure on the beam orbit is considered to be larger than this value, since the pressures are measured at the places near the vacuum pumps. The calculated I $\tau$  is shown in Figure 4 as a function of I, assuming the value of  $(P/I) = 4.8$ nTorr/A, which can give the best fit to the observed data. The calculated I $\tau$  agrees well with the observation. When I <sup>I</sup> I lA, IT is determined by the physical aperture and does oct not depend on  $I \atop \text{oct}$  ets larger than 1 A, the dynamic aperture becomes smaller than the physical aperture and then  $I\tau$ decreases.

## INJECTION RATE

The OCT's also affect the injection rate as shown in Figure 5. When  $|I| \ge 1$ A, the injection rate becomes almost zero. This indicates that the dynamic aperture in the horizontal direction becomes as small as the amplitude of the injected beam, which is



FIGURE 5 Dependency of the injection rate on  $I_{\text{oct}}$ . The measurement was done for the positron injection.

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estimated to be about  $7 \text{ mm}$  at the north symmetry point. Actually, the calculation shows that the dynamic aperture becomes smaller than 10 mm in the horizontal direction when  $|I_{\text{oct}}| \ge 1$ A (see Figure 3 ).

# **SUMMARY**

The excitation of the octupole magnets makes the dynamic aperture seriously small. The calculations show that the dynamic aperture becomes smaller than the physical aperture. The reductions of the beam lifetime and the injection rate can be explained well by this small dynamic aperture.

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