ISR-TH/AH/KH/amb

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CM-P00071503

ISR PERFORMANCE REPORT

# RUN 291, 6th April 1973 R2, 22 GeV/c, 20 bunches

## Study of longitudinal instabilities of bunched beams

#### Summary

Phase oscillations of bunched beams were studied using the "mountain range display". Quadrupole mode oscillations with growth times of  $\tau \sim 0.2$  sec were observed with high rf voltage, and sextupole mode oscillations with  $\tau \sim 0.5$  sec were dominant for a small rf voltage.

#### 1. Rise of the instability

The matched beam is kept bunched on the injection orbit with a constant rf voltage V<sub>i</sub> and  $\Gamma = 0$ . The onset and growth of phase oscillations for bunch 12 and 13 were observed on a "mountain range display". For V<sub>i</sub> = 16 kV - bunch length  $\sim$  16 ns - a quadrupole mode oscillation shows up after  $\sim$  0.35 sec and grows with  $\tau \sim$  0.2 sec, Fig. 1. Later, a dipole mode becomes dominant. For V<sub>i</sub> = 5.8 kV - bunch length  $\sim$  22 ns a sextupole mode oscillation appears after  $\sim$  0.3 sec and grows with  $\tau \sim$  0.5 sec. Later, a dipole mode becomes dominant, and some higher \_modes seem to be present.

#### 2. Phase relation between different bunches

Fig. 3 shows the oscillations of the first 17 bunches 0.5 sec after injection. There is a pattern which repeats itself after  $\sim$  six or seven bunches. This indicates a mode number n = 4 or n = 5.

### 3. Oscillations of the first bunch

Fig. 3 shows that the first bunch oscillates with a smaller amplitude than most of the latter bunches. This indicates that the fields which drive this phase instability, decay to some extent (but not completely) during the "gap" of  $\sim 1 \ \mu$ s.

#### 4. Oscillations during acceleration

Fig. 4 shows the bunches during acceleration with  $V_i = 16 \text{ kV} = \text{const.}$ and  $\Gamma = 0.4$ . The behaviour is very similar to the one with  $\Gamma = 0$ .

#### 5. Conclusions

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For  $V_i = 16 \text{ kV}$  - bunch length  $\sim 16 \text{ ns}$  - mostly m = 2 mode oscillations are excited; for  $V_i = 5.8 \text{ kV}$  - bunch length  $\sim 22 \text{ ns}$  - m = 3 mode oscillations are dominant. Based on Sacherer's <sup>1</sup>) theory one estimates a resonator frequency of  $\sim 75$  MHz to be responsible for the instability (if one deals with only one resonator). Using the mode number n = 4 or 5 (which describes the phase relation between bunches) a set of possible frequencies around 75 MHz could be given. However, because of the large errors this is presently not of much help.

The rate of rise  $\Delta \omega$  of the instability can be obtained approximately by correcting the observed rise with the Landau damping. One gets

> $\Delta \omega_2 \sim 6 \text{ sec}^{-1}$  for V = 16 kV, m = 2  $\Delta \omega_3 \sim 4 \text{ sec}^{-1}$  for V = 5.8 kV, m = 3

Using Sacherer's theory, the shunt impedance of the resonator can now be estimated to be  $Z \sim 5 k\Omega$ ,  $Z/k \sim 23 \Omega$ , (k = resonator frequency/ circumferential frequency).

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1) F. Sacherer; A Longitudinal Stability Criterion for Bunched Beams, CERN/MPS/Int. BR/73-3.









