

# Translating Relevance Scores to Probabilities for Contextual Advertising

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# Contextual Advertising

“Publisher”  
creates page  
content and  
wishes to  
display ads.

“Advertiser”  
supplies ads.

“Ad network”  
decides which  
ads to display.

“User” decides  
whether to  
click on ads.

 Ten Must Read Books about Mathematics  
By Antonio Cangiano. Filed under Essential Math, Suggested reading

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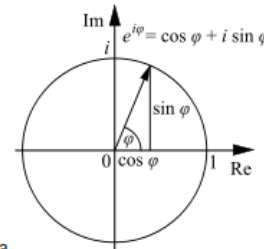
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I love books with the ability to inspire readers. Many non-mathematicians consider mathematics as something abstruse and complicated, suitable only for 'nerds'. Often I highlight the unfounded nature of this prejudice, but nothing is more effective at disproving this stigma than a good book. I was in fact able to quickly change many of my friends' views on the topic, by just giving them a good book which shows the beauty and fascinating nature of mathematics and science in general. The following is a list of great titles, most of which are fairly cheap. Not all of them are suitable for the mathematically illiterate though, and thus cannot simply be



# Click Probabilities are Important

The goal of the ad network is to maximize their revenue:

Expected  
revenue for  
page.

Price advertiser  
pays to have ad in  
position  $i$ .

Probability that ad  
is clicked on, given  
the page content.

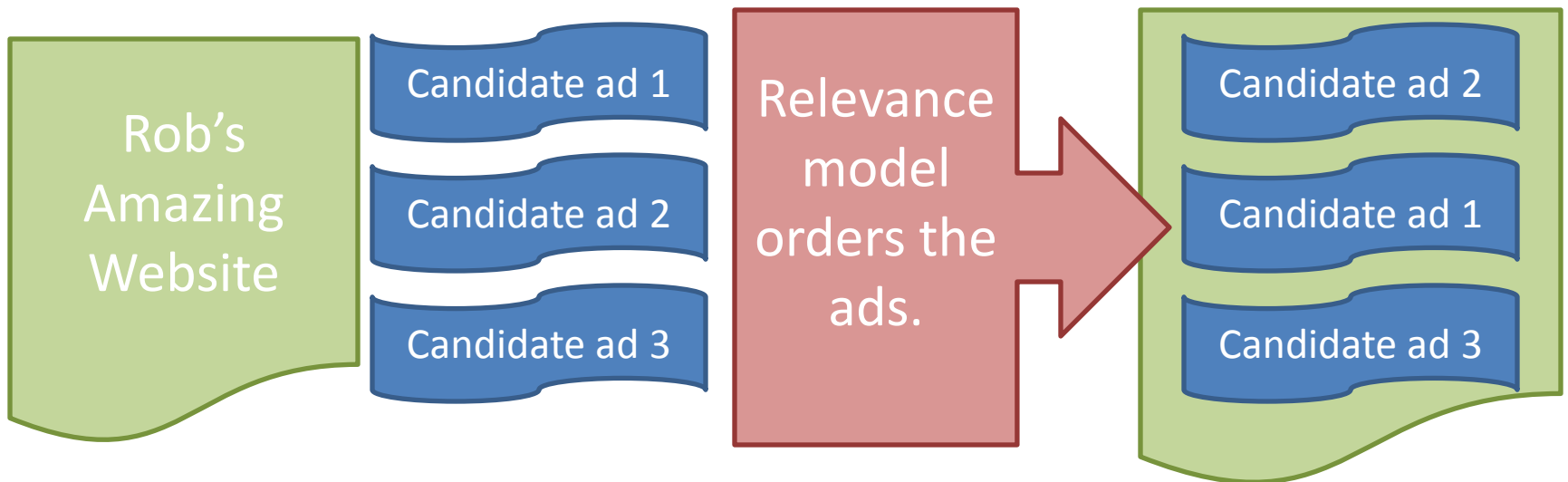
$$ER = \sum_{i=1}^k \text{price}(a_i, i) P(\text{click} | \text{page}, a_i)$$

Ad network  
chooses the ads  
which maximize  
this.

A good model of click  
probability is essential to  
successfully optimize  
revenue .

# Relevance Models of Ads

“Relevance” (e.g., a vector space model) may be used to select ads for display, and to order them:



To maximize revenue we need good absolute scores as well as a good ordering.

# Logistic Regression of Clicks Based on Relevance

$$P(\text{click}|\text{page}, a_i) = p_i$$

$$\text{logit}(p_i) = \phi(\text{page}, a_i)^T \beta + f(r_i)$$

“Features”  
of the page  
and ad.

Model  
parameters

Function of  
the  
relevance

Idea: divide space  
of relevance score  
into bins.

$$f(r) = \sum_{k=1}^M \alpha_k 1(r \in B_k)$$

Model  
parameters

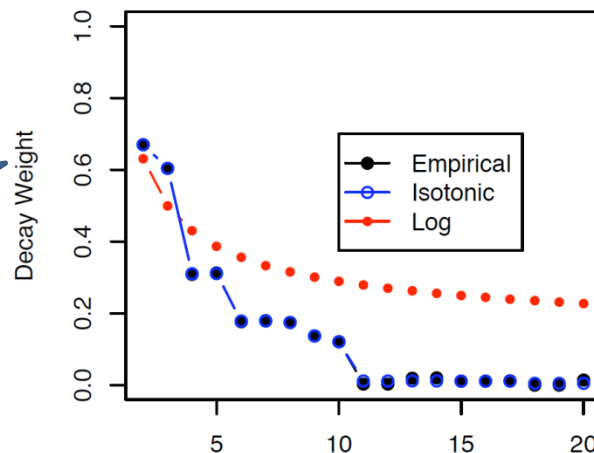
Indicator of  
 $i^{\text{th}}$  bin.

# Page and Ad Features

- **Taxonomy:** Label of page and ad in a large hand-made taxonomy of about 6000 classes.
- **Domain:** Domain on which ads are shown (since pages on the same domain have similar structure and ad visibility).
- **Words in common:** words common to both the ad and the page.
- **Ad Position:** Position in the list of ads (since top ranked ads are more often clicked).

# Experimental Evaluation

- Task is to rank ads.
- Data are 3M slates of ads taken over 22 days.
- 2M used for estimating parameters, 1M for evaluating model performance.
- Metric is Discounted Cumulative Gain (DCG)



Score you  
get if ad  
was clicked.

Position  
you put ad.

# Evaluated Models

- **VSM**: The raw relevance scores.
- **Global**: A single logistic regression fit to all the data.
- **PART**: A logistic regression fit for each of the top 20 publishers (70% of data) and a single logistic regression to the remaining data.
- **EM**: A mixture of logistic regressions to the data.



# Results

- PART is the superior model for two reasonable choices of weights:

Model	VSM	PART	Global	GlobalW	EM	EMW
Log-NDCG	.692	.781	.773	.773	.771	.773
Emp-NDCG	.549	.561	.556	.555	.555	.555

- Improvement over VSM is significant:

